

Aguiar, Angel et al.

Working Paper

The WTO Global Trade Model: Technical documentation

WTO Staff Working Paper, No. ERSD-2019-10

Provided in Cooperation with:

World Trade Organization (WTO), Economic Research and Statistics Division, Geneva

Suggested Citation: Aguiar, Angel et al. (2019) : The WTO Global Trade Model: Technical documentation, WTO Staff Working Paper, No. ERSD-2019-10, World Trade Organization (WTO), Geneva,
<https://doi.org/10.30875/337f4736-en>

This Version is available at:

<https://hdl.handle.net/10419/207086>

Standard-Nutzungsbedingungen:

Die Dokumente auf EconStor dürfen zu eigenen wissenschaftlichen Zwecken und zum Privatgebrauch gespeichert und kopiert werden.

Sie dürfen die Dokumente nicht für öffentliche oder kommerzielle Zwecke vervielfältigen, öffentlich ausstellen, öffentlich zugänglich machen, vertreiben oder anderweitig nutzen.

Sofern die Verfasser die Dokumente unter Open-Content-Lizenzen (insbesondere CC-Lizenzen) zur Verfügung gestellt haben sollten, gelten abweichend von diesen Nutzungsbedingungen die in der dort genannten Lizenz gewährten Nutzungsrechte.

Terms of use:

Documents in EconStor may be saved and copied for your personal and scholarly purposes.

You are not to copy documents for public or commercial purposes, to exhibit the documents publicly, to make them publicly available on the internet, or to distribute or otherwise use the documents in public.

If the documents have been made available under an Open Content Licence (especially Creative Commons Licences), you may exercise further usage rights as specified in the indicated licence.

World Trade Organization

Economic Research and Statistics Division

The WTO Global Trade Model:

Technical documentation

Angel Aguiar
Erwin Corong
Dominique van der Mensbrugge
Center for Global Trade Analysis (GTAP), Purdue University

Eddy Bekkers
Robert Koopman
Robert Teh
World Trade Organization (WTO)

Manuscript date: 6 November 2019

Disclaimer: This is a working paper, and hence it represents research in progress. This paper represents the opinions of individual staff members or visiting scholars and is the product of professional research. It is not meant to represent the position or opinions of the WTO or its Members, nor the official position of any staff members. Any errors are the fault of the author.

The WTO Global Trade Model: Technical documentation

by

Angel Aguiar, Erwin Corong, Dominique van der Mensbrugge,
Eddy Bekkers, Robert Koopman and Robert Teh

6 November 2019

Abstract

This document provides a technical description of the WTO Global Trade Model developed by the Center for Global Trade Analysis (GTAP) and the World Trade Organization (WTO). The model can be used to generate global trade projections and to assess the medium and long run effects of a wide range of global and national trade policies. The WTO Global Trade Model is a recursive dynamic extension of the static GTAP model (Corong et al., 2017), and implements a parsimonious approach to incorporate monopolistic competition—i.e., Eithier-Krugman or Melitz-type firm heterogeneity— in the standard GTAP model following Bekkers and Francois (2018).

Keywords: Computable general equilibrium; recursive dynamics; baseline projections; international trade

JEL-codes: C68, F12, F17

The WTO Global Trade Model: Technical documentation

Angel Aguiar

Erwin Corong

Dominique van der Mensbrugghe

Center for Global Trade Analysis (GTAP), Purdue University

Eddy Bekkers

Robert Koopman

Robert Teh

World Trade Organization (WTO)

November 6, 2019

Abstract

This document provides a technical description of the WTO Global Trade Model developed by the Center for Global Trade Analysis (GTAP) and the World Trade Organization (WTO). The model can be used to generate global trade projections and to assess the medium and long run effects of a wide range of global and national trade policies. The WTO Global Trade Model is a recursive dynamic extension of the static GTAP model ([Corong et al., 2017](#)), and implements a parsimonious approach to incorporate monopolistic competition—i.e., Eithier-Krugman or Melitz-type firm heterogeneity—in the standard GTAP model following [Bekkers and Francois \(2018\)](#).

Contents

1	Introduction and overview	1
2	Core model	3
2.1	Overview	3
2.2	Demand	4
2.3	Production	5
2.4	Factor supply	6
2.5	Trade	7
2.6	Savings and investment	9
2.6.1	Investment preliminaries	9
2.6.2	Rate-of-return sensitive investment allocation	9
2.6.3	Investment allocation based on initial capital shares	10
2.6.4	Fixed real foreign savings	10
2.6.5	Fixed relative foreign savings	11
2.6.6	Summary of investment allocation rules	11
2.7	Income and equilibrium	12
2.8	Numéraire and closure	13
2.8.1	A note on price indices	13
2.8.2	Factor price index	15
2.8.3	Price of regional Absorption and MUV price index	15
2.8.4	Definition of GDP	16
3	Model dynamics	19
3.1	Introduction	19
3.2	Endowments	19
3.2.1	Population and labor force	19
3.2.2	Capital	20
3.2.3	Land and natural resources	21
3.3	Technology	21
3.3.1	Multi-sector models	23
3.4	Preferences	24
3.5	Policies	27
3.6	Data sources for exogenous baseline assumptions	27
4	Conclusions and future directions	28
A	Mathematical appendix	31
A.1	Sets and subsets	31

List of Tables

A.1 Basic sets in the model	31
A.2 Commodity subsets	32
A.3 Endowment subsets	32

List of Figures

2.1	Circular flows in a regional economy	4
2.2	Production structure	6
2.3	Price linkages in the model	8

Chapter 1

Introduction and overview

This document provides a technical description of the WTO Global Trade model which is built upon the latest version of the standard GTAP model (Corong et al., 2017). First developed in 1992, the GTAP model has become the *de facto* standard and starting point for nearly all economy-wide analyses of global trade issues. As a recursive dynamic extension of the static GTAP model (Corong et al., 2017), the WTO Global Trade Model can be used to generate global trade projections and to assess the medium- and long run effects of a wide range of global and national trade policies. The model also includes a number of dynamic features and incorporates the so-called new quantitative trade theory. It is well-suited for studying a wide variety of issues, not only those involving changes in trade policy, but also other topics of fundamental importance to WTO members, such as the long-term impact of technological, demographic and environmental changes.

The WTO Global Trade Model also extends the core GTAP model structure Corong et al. (2017) by introducing:

1. additional closures to model global savings;
2. upward sloping factor supply curves;
3. Fisher "ideal" price and quantity indices;
4. a flexible structure combining perfect competition with Armington preferences and monopolistic competition—either homogeneous (Ethier-Krugman) or with heterogeneous firms (Melitz)—based on Bekkers and Francois (2018).

The model's dynamic module allows for changes in endowments, technology and preferences over time. In terms of endowments, the size of the labor force is imposed exogenously using external projections while supplies of land and natural resources are modeled via an upward-sloping supply curve. Capital stock changes are modeled using the standard capital motion equation (discussed below) wherein capital stock at the beginning of period t is equal to beginning of period capital stock at $t-1$ plus net investment (i.e., gross investment less depreciation) at $t-1$. In addition, technological changes are used, for example in the baseline scenario, to target externally imposed GDP per capita growth rates or to model differences in productivity growth between sectors. The model also allows for preference changes (e.g., domestic versus imported goods in Armington demand or labor versus capital use in total value added mix) in a cost-neutral way by employing the so-called *twist* approach developed by Dixon and Rimmer (2002). Under this approach, for example, spending shares between domestic and imported goods can be changed exogenously while holding the aggregate cost of domestic and imported bundle constant.

This manual is organized as follows. The next section provides an overview of the extensions introduced to the core static GTAP model (Corong et al., 2017), while Section 3 provides a detailed description of the model's dynamic features. Both Sections 2 and 3 include easy-to-read algebraic equations and associated TABLO codes of the model, as implemented in GEMPACK Harrison and Pearson (1996). Section 4 concludes and identifies future research directions needed to improve the construction of dynamic baselines for the global economy and which will be the subject of a future paper.

Chapter 2

Core model

This section provides an overview of the core structure of the WTO Global Trade Model which is based on the standard GTAP model, version 7 (Corong et al., 2017). We also pay attention to the core GTAP model extensions introduced in the WTO Global Trade Model:

1. additional closures to model global savings
2. upward sloping factor supply curves
3. Fisher "ideal" price and quantity indices
4. a flexible structure combining perfect competition with Armington preferences and monopolistic competition—either homogeneous (Ethier-Krugman) or with heterogeneous firms (Melitz)—based on Bekkers and Francois (2018).

These extensions are described in detail in this section, as do the necessary GTAP model code changes. To avoid repetition, we do not reproduce the core GTAP model description found in Corong et al. (2017) and the monopolistic competition implementation by Bekkers and Francois (2018).

2.1 Overview

The WTO Global Trade Model distinguishes multiple sectors and regions. Figure 2.1.¹ shows the model's structure based on a circular flow logic of an economy (formally a circular flow diagram). In each region, a so-called *regional household* collects all income and then spends on three final goods: government, private, and savings. Savings are used to finance investment goods via a so-called *global bank* which collects each region's savings into a global pool for eventual investment allocation across regions depending on the chosen closure rule.

On the production side, producers employ factors of production (capital, labor, natural resources and land) and demand goods from other firms, reflecting intermediate linkages. Commodities are either sourced locally or from abroad, with the latter reflecting international trade. Regional income consists of the sum of factor income and tax revenues. We now discuss the different components of the model, namely: demand, production, factor supply, trade, savings-investment, income and equilibrium, and numeraire and closure.

¹The figure is an adaptation from Brockmeier (2001).

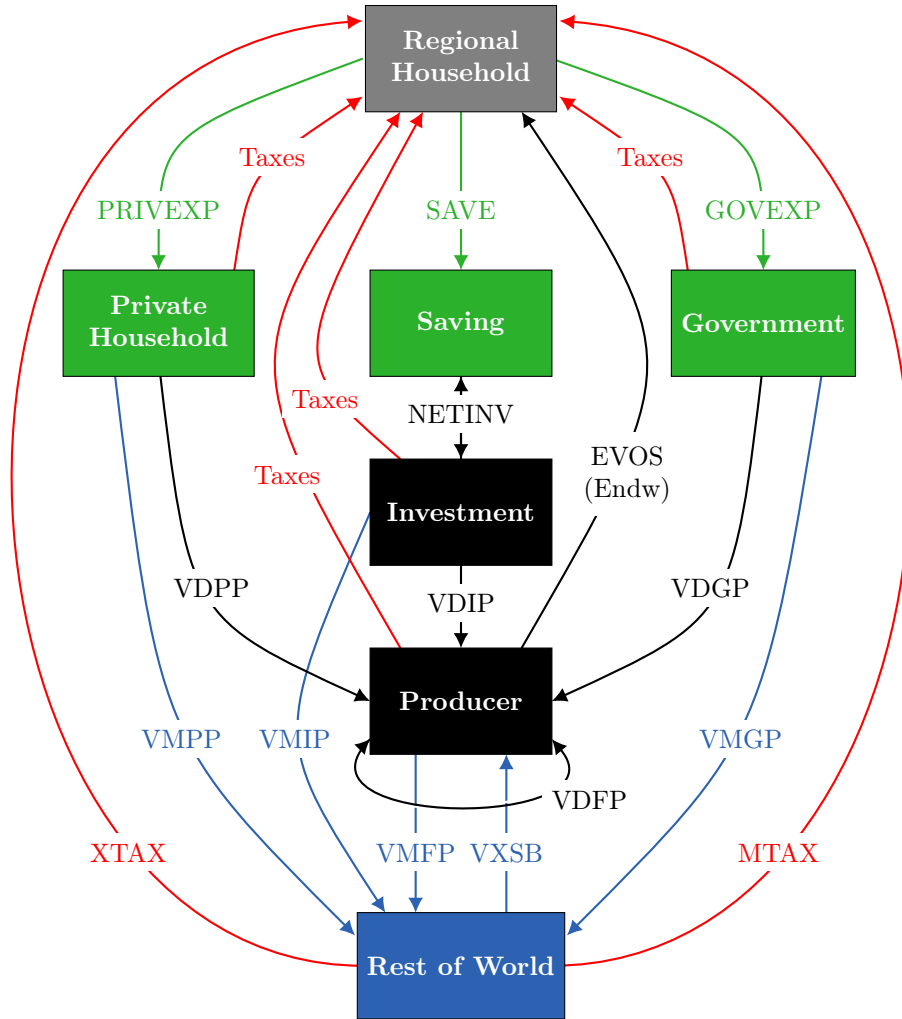


Figure 2.1: Circular flows in a regional economy

2.2 Demand

For each region, a regional household allocates its income on three sources of final demand (i.e., private, government and savings) according to a Cobb-Douglas utility function.

Expenditures on private goods are allocated across different commodities according to a non-homothetic utility, constant difference elasticity (CDE) utility function. Under non-homothetic preferences spending shares vary with income: the share of income on food tends to fall as income rises, whereas the share of income spent on most service commodities tends to rise as income increases. With a CDE utility function, income changes generate shifting average and marginal budget shares. The number of parameters required by the CDE function is limited and is thus a compromise between the linear expenditure system and for example, AIDADS. The former utility function is more restrictive than the CDE, as income elasticities converge quickly to one for all sectors, whereas the latter requires many parameters to calibrate and is not easy to reconcile correctly with the (upper-nest) choice among government, private household and savings expenditures.

Non-homothetic preferences for private goods imply that the shares spent on the three types

of goods (government goods, private household goods, and savings) change with income, despite the fact that these shares are determined by a Cobb-Douglas utility function. The share spent on private goods is determined by the marginal utility of private expenditures, which changes with income. Hence, in dynamic simulations growing income will lead to changing spending shares on private household goods.²

Government expenditures are allocated across different commodities according to a Cobb-Douglas utility function, implying fixed commodity spending shares. Expenditures on savings are channeled to investment goods as discussed below. By including savings in the static utility function we prevent that a shift towards (current) consumption and away from savings (and thus implicitly from future consumption) generates strong welfare effects. With savings in the static utility function we can account for the intertemporal nature of savings-investment decisions in a static setting.³

2.3 Production

The model includes a so-called ‘make’ matrix enabling us to model either activities producing multiple commodities (such as ethanol) and/or commodities produced by more than one activity (such as electricity). On the supply side, multi-product activities produce multiple outputs according to a constant elasticity of transformation (CET) function. On the demand side, commodities produced by various activities are combined using a CES function. The absence of multi-production implies a diagonal make matrix—i.e., each activity produces just one commodity.

Perfectly competitive firms produce homogeneous commodities by combining value added (labor, capital, natural resources, and land) and intermediate inputs. The model’s nested production structure 2.2 assumes weak separability between value added and intermediate commodities. This implies that for each activity, the price of intermediates are invariant to factor mix. The default allocation between intermediate and value added bundle is Leontief—hence, there is no scope for substitution.⁴ The optimal factor mix is determined via a CES function with degree of substitutability governed by sector- and region-specific substitution elasticities (*ESUBVA*).

Production factors can be of three types: perfectly mobile, sluggish, or sector-specific. In the standard closure, capital and labor are perfectly mobile, land is typically sluggish while natural resources is sector-specific. A sluggish factor is partially mobile across sectors and is modeled according to a CET function with degree of mobility governed by elasticity of transformation *ETRAE*. Factor returns also vary by endowment types. Perfectly mobile factors receive uniform returns across activities (i.e., an economy-wide price) while returns to sector-specific factors vary by activity. Returns to sluggish factors depend on their mobility (i.e., sector-specific returns if immobile or an economy-wide return if perfectly mobile).

²See McDougall (2003) for further discussion.

³Hanoch (1975) shows formally that a static utility maximization problem with savings in the utility function is implied by an inter-temporal consumption decision problem.

⁴The Leontief specification can be relaxed by modifying the elasticity parameter *ESUBT* in the model.

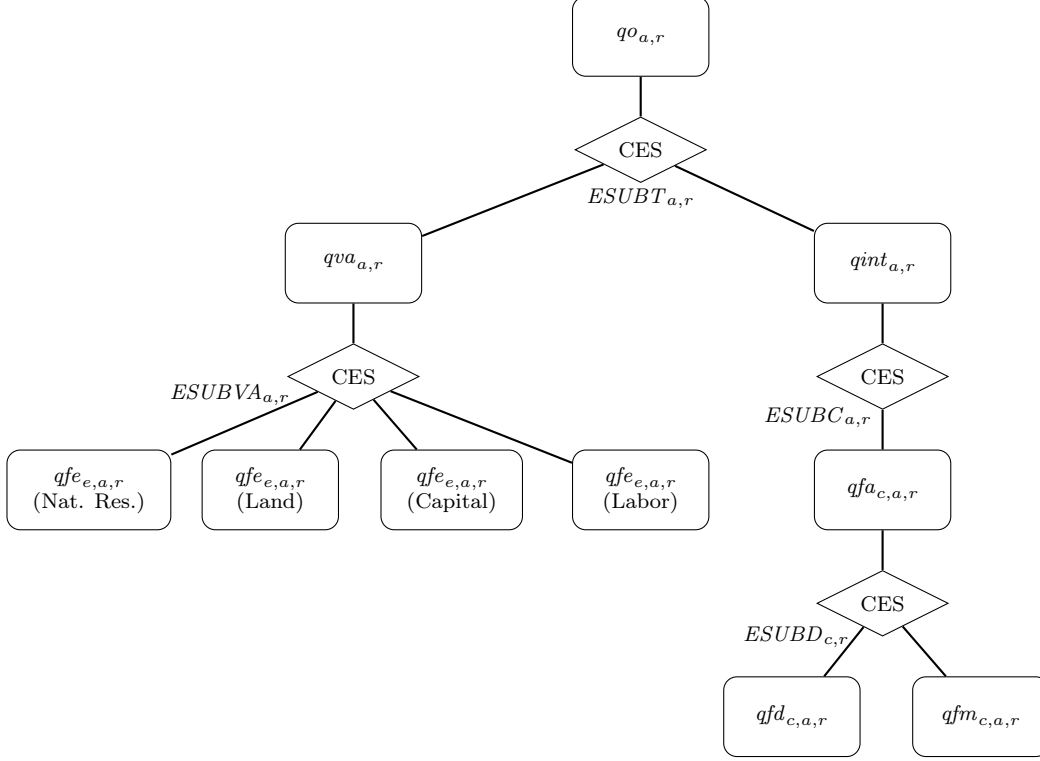


Figure 2.2: **Production structure**

2.4 Factor supply

The model allows for upward sloping supply specification for the non-capital endowments (land, labor and natural resources). Since upward sloping supply functions for endowments are new in the WTO Global Trade Model, they will be discussed into detail here. A description of the sets definitions employed in the exposition is in Appendix A.

Equation (2.1), which is conditioned on the set $ENDWMSXC^5$, specifies an upward sloping supply curve for aggregate land and labor endowments as a function of the endowment- and region-specific supply elasticity, $ESUPMS_{e,r}$, and the endowment's real return. The latter is derived as a ratio of an endowment's aggregate return, $pe_{e,r}$, to the private consumption price index, $ppriv_r$.

Similarly, Equation (2.2) implements upward sloping supply for the sector-specific endowment as a function of its supply elasticity $ESUPF_{e,a,r}$ and real return (i.e., sector-specific return, $pes_{e,a,r}$, relative to the private consumption price index, $ppriv_r$).

$$qe_{e,r} = ESUPMS_{e,r}[pe_{e,r} - ppriv_r] \quad \text{for } e \in \{ENDWMSXC\} \quad (2.1)$$

$$qes_{e,a,r} = ESUPF_{e,a,r}[pes_{e,a,r} - ppriv_r] \quad \text{for } e \in \{ENDWF\} \quad (2.2)$$

This unit determines $QE_{e,r}$ for land and labor endowments, and $QES_{e,a,r}$ for the sector-specific endowment when the upward sloping supply specification for these factors are active. In the model

⁵MSXC is a shorthand for Mobile and Sluggish endowments eXcept Capital. In the model code, $ENDWMSXC$ is derived as the complement of mobile/sluggish ($ENDWMS$) and capital ($ENDWC$) sets.

code, equation `E_qelsupply` implements equation (2.1), while `E_qesfsupply` implements equation (2.2).⁶

The TABLO codes in Listing 2.1 include two shift variables that facilitate upward sloping supply specification. To specify upward sloping supply for land and/or labor, the shift variable $qelsupply_{e,r}$ must be swapped with $qe_{e,r}$ in the closure file.⁷ Similarly, swapping the shift variable $qesfsupply_{e,a,r}$ with $qesf_{e,a,r}$ in the closure file activates the upward sloping supply specification for the sector-specific factor.

Listing 2.1: GEMPACK equations for upward sloping supply

```

1 Equation E_qelsupply
2 # upward sloping aggregate supply specification for land (sluggish) and labor #
3 (all,e,ENDWMSXC) (all,r,REG)
4 qe(e,r) = ESUPMS(e,r) * [pe(e,r) - ppriv(r)] + qelsupply(e,r);

6 Equation E_qesfsupply
7 # upward sloping supply specification for sector-specific (natures) factor #
8 (all,e,ENDWF) (all,a,ACTS) (all,r,REG)
9 qes(e,a,r) = ESUPF(e,a,r) * [pes(e,a,r) - ppriv(r)] + qesfsupply(e,a,r);

```

Capital supply will be discussed in Section (3).

2.5 Trade

Private, government and investment expenditures, as well as purchases of intermediate goods comprise both domestic and imported purchases, thereby generating both domestic and export sales by firms.

Each commodity is an aggregate of domestic and imported goods according to an Armington CES specification—the so-called top-level Armington demand. The sourcing of imports by region of origin—i.e., the second-level Armington—is done at the regional level in the destination country. This implies that goods from different regions of origins are distinct in the eyes of their buyers or destination regions. Goods from a particular source are homogeneous: French cars are different from German cars, but there is only type of French car. Because of love of variety between goods from different countries, the Armington structure allows for the possibility that each country imports goods from each and every trading partner.

Figure 2.3 displays the price linkages in international trade. Starting from the top the figure shows activities are converted into commodities with a CET and CES. Then the figure shows the different margins in international trade, in turn the export taxes, the transport margins, user-generic import tariffs and finally user-specific import tariffs.

The international transport margin, the difference between FOB-values and CIF-values, is paid for by using so-called margin (or transport) services supplied by the international transport sector. The quantity of transport services needed is proportional to the quantity of goods shipped. This corresponds with a Leontief specification: the CIF-quantity is a Leontief aggregate of the FOB-quantity and transport services. The international transport sector in turn buys transport services from the so-called margin sectors in all countries. The three margin sectors in each exporting country (air transport, water transport, and other transport) sell services to the domestic market, to the exporting market and to the international transport sector

⁶Equations `E_qelsupply` and `E_qesfsupply` simplify to $qe_{e,r} = qelsupply_{e,r}$ and $qes_{e,a,r} = qesfsupply_{e,a,r}$ when their associated supply elasticities are zero.

⁷The user could selectively implement this specification by conditioning the swap statements with the relevant factor sets—e.g., `ENDWS` if limited to the sluggish land factor, `ENDWL` if limited to labor, or `ENDWMXSC` for both land and labor.

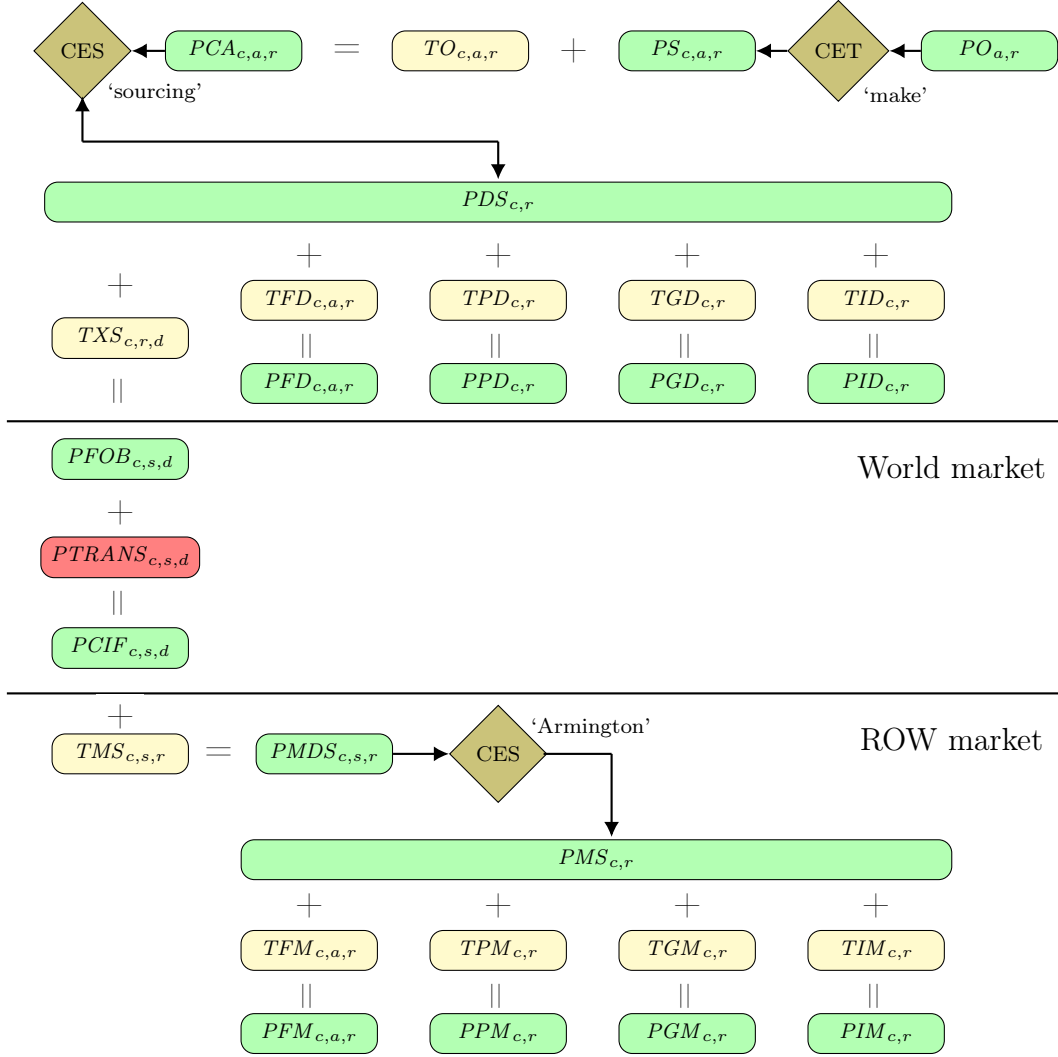


Figure 2.3: Price linkages in the model

The WTO Global Trade Model is flexible in its trade structure, allowing to switch from the default perfect competition Armington specification to monopolistic competition Ethier-Krugman or Melitz specification with respectively homogeneous or heterogeneous firms. The model follows the setup in Bekkers and Francois (2018) making it possible to switch easily (through changes in the parameter file) between the different trade structures. The monopolistic competition model combines product differentiation at the firm level (instead of the country level) with increasing returns to scale in production: each firm (and not each country) makes a unique variety by paying fixed costs: French cars produced by different firms are perceived as separate varieties by consumers. This setup leads to so-called variety scaling of consumed goods (by private agents or firms): more resources in a supplying country enable the country to produce more varieties and with consumers displaying love of variety, this leads to higher welfare and lower (welfare-adjusted) prices. Adding firm heterogeneity to the model allows us to account for the reallocation effect of trade: more international trade leads to a reallocation of market shares from less productive to more productive firms (See Bekkers and Francois (2018) for details on modeling setup and parameterization).

2.6 Savings and investment

Savings in each country are collected by a global bank. The global bank spends the total amount of savings on aggregate investment goods in different countries. The aggregate investment good in each country is a composite of investment goods.

Global savings can be allocated to investment in the different regions according to four different foreign investment *closure* rules. First, global savings can be allocated to investments in different regions such that (percentage) changes in the expected rate of return on capital are equalized across regions. In the second rule, investment in each country moves such that the regional composition of capital stocks does not change. A third rule fixes net foreign capital flows in real terms. Given the simplified version of the balance of payments, this in essence fixes the net trade balance. An *ex ante* change to the trade balance, for example a tariff reduction, typically requires a change to the real exchange rate. In this third closure option, the global bank ignores changes in the relative rates of return, as in the case of a fixed investment allocation, and it is the net saving flow that is fixed, not the regional investment shares. A fourth mechanism fixes net capital flows relative to regional income. Both the third and fourth mechanisms can only be implemented for $n - 1$ regions and thus there is a residual region that becomes the lender/borrower of last resort.

2.6.1 Investment preliminaries

Before describing the four ways to allocate global savings across investment in different regions, we define the nominal (after-tax) rate of return on capital and the net current rate of return on capital.

The nominal rate of return on capital, $RENTAL_r$, is defined in equation (2.3) as the product of the after tax return to capital in sector a , $PES_{endwc,a,r}$, and the quantity of capital endowments, $QES_{endwc,a,r}$, divided by the beginning-of-period capital stock, KB_r :

$$RENTAL_r = \sum_a PES_{endwc,a,r} QES_{endwc,a,r} / KB_r \quad (2.3)$$

The net current rate of return on capital is equal to the nominal rate of return on capital divided by the replacement cost of capital, $PINV_r$, minus the depreciation rate, δ_r .

$$RORC_r = \frac{RENTAL_r}{PINV_r} - \delta_r \quad (2.4)$$

If a trade policy change would for example affect the price of investment goods or replacement cost of capital, then it would also affect the current rate of return on capital.

Finally, the end of period capital stock, KE_r , is equal to the beginning of period capital stock net of depreciation, $(1 - \delta_r) KB_r$, plus new investment, $QINV_r$:

$$KE_r = (1 - \delta_r) KB_r + QINV_r \quad (2.5)$$

2.6.2 Rate-of-return sensitive investment allocation

Under the first foreign investment rule the global bank responds to changes in relative rates of return. According to equation (2.6) the expected rate of return, $RORE_r$ is determined by the net rate of return, $RORC_r$, and an additional term depending on the change in the capital stock. The expected rate of return tends to fall with a larger increase in the capital stock with elasticity $RORFLEX_r$.

$$RORE_r = RORC_r \left(\frac{KE_r}{KB_r} \right)^{-RORFLEX_r} \quad (2.6)$$

Equation (2.6) determines the allocation of global investment funds as follows. A shock raising the demand for capital would increase the nominal rental rate. This in turn would lead to an increase in the rate of return on capital, $RORC_r$. By equation (2.6) this would raise the end-of-period capital stock, KE_r , relative to beginning-of-period capital stock, KB_r . The rise in KE_r in turn would generate an increase in investment flows to country r . The degree to which an increasing rate of return on capital, $RORC_r$, leads to additional investment (and thus capital inflows into a country) is determined by $RORFLEX_r$. A small value of $RORFLEX_r$ would generate a larger response in KE_r and thus a larger investment response.

Under the rate-of-return sensitive investment allocation, the percentage change in the expected rate of return in each region, $RORE_r$, is equal to the percentage change in the global rate of return, $RORG$, such that the percentage change in the expected rate of return equalizes across regions.

$$RORE_r = RORG \quad (2.7)$$

2.6.3 Investment allocation based on initial capital shares

Under the second foreign investment rule the regional composition of capital stocks is invariant to variations in changes in the expected relative rates of return. In Equation (2.8) global net investment is defined consisting of the sum of net investment in all regions.

$$GLOBALCGDS = \sum_r (QINV_r - \delta_r KB_r) \quad (2.8)$$

Under this rule regional investment is a constant share of global investment, with the share determined by base investment shares, equation (2.9).

$$QINV_r - \delta_r KB_r = \chi_r^I GLOBALCGDS \quad (2.9)$$

This equation is only defined for $(R - 1)$ regions, because the equality of global savings and global investment determines regional investment in the last region. Under this foreign investment closure the aggregate rate of return, $RORG$, is still defined, being equal to the weighted sum of the regional expected rate of return variable with the weights determined by the regional share in global net investment.

$$RORG = \sum_r \varphi_r RORE_r \quad \text{where } \varphi_r = \frac{PINV_r (QINV_r - \delta_r KB_r)}{\sum_s PINV_s (QINV_s - \delta_s KB_s)} \quad (2.10)$$

2.6.4 Fixed real foreign savings

We start by defining foreign savings as the difference between domestic investment and domestic savings.

$$PINV_r QINV_r = SAVE_r + FSAVE_r + \delta_r PINV_r KB_r \quad (2.11)$$

where $FSAVE_r$ is the region's net nominal foreign capital flow.

The third specification fixes net real foreign savings—typically to base year levels, but not required, i.e. one can shock net foreign savings. Foreign savings are fixed for $n - 1$ regions and are

given by the exogenous parameter $FSAVEX$, equation (2.12). These are multiplied by a global price, in this case, $PGLOBALCGDS$, which is the average price of investment defined in equation (2.13). Equation (2.14) is implemented to ensure that global net foreign savings sum to zero, in essence evaluating foreign savings for the residual region.

$$FSAVE_r = PGLOBALCGDS \times FSAVEX_r \quad (2.12)$$

$$PGLOBALCGDS = \sum_r PINV_r (QINV_r - \delta_r KB_r) \quad (2.13)$$

$$\sum_r FSAVE_r \equiv 0 \quad (2.14)$$

2.6.5 Fixed relative foreign savings

The fourth specification fixes net foreign savings relative to regional income. Relative foreign savings are fixed for $n - 1$ regions and are set equal to the exogenous parameter χ^f , equation (2.15). The parameter is calibrated to the base year ratio of foreign savings to income, but can be changed in a simulation shock. Equation (2.14) determines net foreign savings for the residual region, i.e. the borrower/lender of last resort.

$$FSAVE_r = \chi_r^f Y_r \quad (2.15)$$

In summary we have four foreign savings closure. Common to all closures are the following equations: equation (2.5), equation (2.3), equation (2.4), equation (2.6), equation (2.8), equation (2.13), (2.11) and (2.14). Common to the last three closures, i.e. all except the rate-of-return sensitive closure is also equation (2.10).

2.6.6 Summary of investment allocation rules

The four cases involve specifying the following to essentially determine $FSAVE$:

- *Rate of return sensitive investment* Equation (2.7)
- *Investment based on initial capital shares* Equation (2.9)
- *Fixed real foreign savings* Equation (2.12)
- *Fixed relative foreign savings* Equation (2.15)

This unit determines $GLOBALCGDS$, KE_r , $RENTAL_r$, $RORC_r$, $RORE_r$, $QINV_r$ and $RORG$ using equations `E_ke`, `E_rental`, `E_rorc`, `E_rore`, `E_qinv` that implements equations (2.4) and (2.9), `E_globalcgds` that implements equations (2.8) and (2.10), `E_del_rfsave` that implements $FSAVEX$ in equation (2.12) and `E_del_fsavery` that implements equation (2.15).⁸

⁸The parameter $RORDELTA$ determines global investment closure. A value of 1 uses the rate-of-return sensitive closure. A value of 0 uses the fixed investment allocation closure. A value of 1 coupled with the appropriate swap statement facilitate either fixed real or fixed relative foreign savings closure. For fixed real foreign savings closure, the appropriate swap statement is: `Swap cgdslack(REGN-1) = del_rfsave(REGN-1)`, while the appropriate swap statement for fixed relative foreign savings closure is: `Swap cgdslack(REGN-1) = del_fsavery(REGN-1)`. In both cases, `REGN-1` is the set of all regions except a residual region.

Listing 2.2: GEMPACK equations for investment allocation

```

1 Equation E_ke
2 # ending capital stock equals beginning stock plus net investment. #
3 (all,r,REG)
4 ke(r) = INVKERATIO(r) * qinv(r) + [1.0 - INVKERATIO(r)] * kb(r);

6 Equation E_rental
7 # defines a variable for capital rental rate #
8 (all,r,REG)
9 rental(r) = sum{e,ENDWC, [VES(e,r) / GROSSCAP(r)] * pe(e,r)};

11 Equation E_rorc
12 # current rate of return on capital in region r #
13 (all,r,REG)
14 rorc(r) = GRNETRATIO(r) * [rental(r) - pinv(r)];

16 Equation E_rore
17 # expected rate of return depends on the current return and investment #
18 (all,r,REG)
19 rore(r) = rorc(r) - RORFLEX(r) * [ke(r) - kb(r)];

21 Equation E_qinv
22 # either gross investment or expected rate of return in region r #
23 (all,r,REG)
24 RORDELTA * rore(r)
25 + [1 - RORDELTA]
26 * [[REGINV(r) / NETINV(r)] * qinv(r) - [VDEP(r) / NETINV(r)] * kb(r)]
27 = RORDELTA * rorg + [1 - RORDELTA] * globalcgds + cgdslack(r);

29 Equation E_globalcgds
30 # either expected global rate of return or global net investment #
31 RORDELTA * globalcgds + [1 - RORDELTA] * rorg
32 = RORDELTA
33 * sum{r,REG,
34 [REGINV(r) / GLOBINV] * qinv(r) - [VDEP(r) / GLOBINV] * kb(r)}
35 + [1 - RORDELTA] * sum{r,REG, [NETINV(r) / GLOBINV] * rore(r)};

37 Equation E_del_rfsave
38 # computes ordinary change in real foreign saving by region, $US million #
39 (all,r,REG)
40 del_rfsave(r) = 0.01 * [NETINV(r) * qnetinv(r) - SAVE(r) * qsave(r)];

42 Equation E_del_fsavery
43 # computes change in foreign saving as a percentage of regional income #
44 (all,r,REG)
45 INCOME(r) * 100 * del_fsavery(r)
46 = NETINV(r) * vnetinv(r) - SAVE(r) * vsave(r) - FSAVE(r) * y(r);

```

2.7 Income and equilibrium

The representative agent allocates income on three types of final expenditures: private, government and savings. Income is the sum of gross factor income and income from indirect taxes. Gross factor income is equal to gross payments to factors of production minus depreciation. There are two types of indirect taxes in international transactions: Bilateral import tariffs and bilateral export taxes. Furthermore, there are four types of domestic taxes: sector-specific endowment taxes (firms' use of labor in the paddy rice sector); direct income tax on factor remuneration; production tax (e.g., production of steel); and source-specific sales taxes for private, government, investment and intermediate purchases (e.g., tax on sales of domestic or imported raw milk to private consumers).

In equilibrium all markets clear. In particular, we impose goods market equilibrium, factor market equilibrium, transport services equilibrium, and global savings equilibrium. First, the quantity

produced/supplied in each country and for each commodity is equal to the domestic and exported quantity, including margin commodities sold to the global transport sector. Second, total factor supply equals factor demand. Third, the supply of transport services by the different margin sectors is equal to the demand for transport services from all the bilateral trade relations. Fourth, global supply of savings is equal to global demand for investment. This last equation is not imposed in the model: by Walras law one equation in the model is redundant and the difference between global savings and global investment (walraslack) is calculated residually to check the consistency of model.

2.8 Numéraire and closure

The default numéraire in the model is *PFACTWLD*, which is a weighted average of the factor prices in all regions. Before introducing this numéraire, we first turn to a discussion of the definition or price indices.

2.8.1 A note on price indices

The model uses Fisher price indices for both factor price and GDP indices. The Fisher price index, sometimes also referred to as the ‘ideal’ price index (see for example Eurostat (2008)), is the geometric mean of the Laspeyres and Paasches indices.

We outline the specification for a generic formulation before depicting the specific formulations used in the GTAP model. For a price index over set i , the Fisher *price* index is equal to the following:⁹

$$F^p = \sqrt{\frac{\sum_i P_{i,t} Q_{i,t-1}}{\sum_i P_{i,t-1} Q_{i,t-1}} \cdot \frac{\sum_i P_{i,t} Q_{i,t}}{\sum_i P_{i,t-1} Q_{i,t}}} = \sqrt{L^p \cdot P^p}$$

The Fisher price index represents the geometric mean of the Laspeyres (L^p) and Paasche price indices (P^p), with the former using lagged volume weights and the latter using current volume weights.

$$L^p = \frac{\sum_i P_{i,t} Q_{i,t-1}}{\sum_i P_{i,t-1} Q_{i,t-1}} \quad P^p = \frac{\sum_i P_{i,t} Q_{i,t}}{\sum_i P_{i,t-1} Q_{i,t}}$$

These indices represent percent change relative to the previous period and thus the price indices are chain weighted. The price index itself is thus defined as:

$$PI_t = PI_{t-1} F_t^p$$

where typically the price index will be set to 1 or 100 in some base period.

The Fisher *volume* index has a similar definition using different price weights:

$$F^q = \sqrt{\frac{\sum_i P_{i,t-1} Q_{i,t}}{\sum_i P_{i,t-1} Q_{i,t-1}} \cdot \frac{\sum_i P_{i,t} Q_{i,t}}{\sum_i P_{i,t} Q_{i,t-1}}} = \sqrt{L^q \cdot P^q}$$

The Fisher volume index represents the geometric mean of the Laspeyres (L^q) and Paasche volume indices (P^q), with the former using lagged price weights and the latter using current price weights.

⁹It is natural to think of the index ‘t’ as time. However, in a comparative static framework it represents the pre- and post-shock values.

$$L^q = \frac{\sum_i P_{i,t-1} Q_{i,t}}{\sum_i P_{i,t-1} Q_{i,t-1}} \quad P^q = \frac{\sum_i P_{i,t} Q_{i,t}}{\sum_i P_{i,t} Q_{i,t-1}}$$

It is easy to show that the aggregate nominal value is equal to the product of the price and volume indices:

$$P_t \cdot Q_t = \sum_i P_{i,t} \cdot Q_{i,t} = F_t^p \cdot F_t^q \cdot P_{t-1} \cdot Q_{t-1}$$

These formulas can be log-differentiated for use in GEMPACK. We start with the following expressions:

$$L_t^p = \frac{\sum_i Q_{i,t-1} P_{i,t}}{\sum_i Q_{i,t-1} P_{i,t-1}} = \frac{LQ1P_t}{LQ1P1_t} \quad P_t^p = \frac{\sum_i Q_{i,t} P_{i,t}}{\sum_i Q_{i,t} P_{i,t-1}} = \frac{LQP_t}{LQP1_t}$$

Since $LQ1P1_t$ only has lags, it is a constant and does not require differentiation. The other three formulas in log-differentiated form are:

$$\begin{aligned} lq1p_t &= \sum_i \varphi_{i,t}^p p_{i,t} & \text{where } \varphi_{i,t}^p &= \frac{Q_{i,t-1} P_{i,t}}{\sum_i Q_{i,t-1} P_{i,t}} \\ lqp_t &= \sum_i \varphi_{i,t}^v (q_{i,t} + p_{i,t}) & \text{where } \varphi_{i,t}^v &= \frac{Q_{i,t} P_{i,t}}{\sum_i Q_{i,t} P_{i,t}} \\ lqp1_t &= \sum_i \varphi_{i,t}^q q_{i,t} & \text{where } \varphi_{i,t}^q &= \frac{Q_{i,t} P_{i,t-1}}{\sum_i Q_{i,t} P_{i,t-1}} \end{aligned}$$

We can insert these in the expression for L^p and P^p :

$$l_t^p = lq1p_t \quad p_t^p = lqp_t - lqp1_t$$

The final step is to insert these expressions into the price index:

$$p_t = 0.5[l_t^p + p_t^p]$$

Thus we can proceed in four steps:

1. Calculate the share vectors, of which there are three: φ^p , φ^v and φ^q
2. Calculate the percentage change in the numerators and denominators of the Laspeyres and Paasche indices—using the weights
3. Calculate the percentage change in the Laspeyres and Paasche indices
4. Calculate the percentage change in the Fisher price index

2.8.2 Factor price index

We defined two indices for factor prices—a regional and global factor price index. Equation (2.16) defines the regional factor price index, $PFACTOR_r$, using the Fisher price index expression. The relevant factor prices are represented by the variable PEB , i.e. the market price, or basic price, of factors.

Any single price, or price index, could be chosen as the model numéraire, or price anchor. The default numéraire is the global price index of factor remuneration using the Fisher price index expression, $PFACTWLD$, which is aggregated over all endowments, activities and regions, i.e., it represents the average global return to endowments, equation (2.17). The left-out equation, or Walras' Law was described in the investment section and represents the global saving=global investment identity.¹⁰

$$PFACTOR_r = PFACTOR_{r,-1} \times \sqrt{\frac{\sum_e \sum_a PEB_{e,a,r} QFE_{e,a,r,-1}}{\sum_e \sum_a PEB_{e,a,r,-1} QFE_{e,a,r,-1}} \cdot \frac{\sum_e \sum_a PEB_{e,a,r} QFE_{e,a,r}}{\sum_e \sum_a PEB_{e,a,r,-1} QFE_{e,a,r}}} \quad (2.16)$$

$$PFACTWLD = PFACTWLD_{-1} \times \sqrt{\frac{\sum_r \sum_e \sum_a PEB_{e,a,r} QFE_{e,a,r,-1}}{\sum_r \sum_e \sum_a PEB_{e,a,r,-1} QFE_{e,a,r,-1}} \cdot \frac{\sum_r \sum_e \sum_a PEB_{e,a,r} QFE_{e,a,r}}{\sum_r \sum_e \sum_a PEB_{e,a,r,-1} QFE_{e,a,r}}} \quad (2.17)$$

This unit determines the regional and global factor price indices in the model. Equation E_pfactor implements equation (2.16) while E_pfactwld implements equation (2.17).

Listing 2.3: GEMPACK equations for numéraire definition and Walras' Law

```

1 Equation E_pfactor
2 # computes % change in factor (Fisher) price index, by region #
3 (all,r,REG)
4 pfactor(r) = 0.5 * [pfacLaspeyres(r) + pfacPaasche(r)];

6 Equation E_rorg
7 # computes % change in world factor (Fisher) price index #
8 pfactwld = 0.5 * [pfacwLaspeyres + pfacwPaasche];

10 Equation E_walras_sup
11 # extra equation: computes change in supply in the omitted market #
12 walras_sup = pcgdsfld + globalcgsd;

14 Equation E_walras_dem
15 # extra equation: computes change in demand in the omitted market #
16 GLOBINV * walras_dem = sum{r,REG, SAVE(r) * [psave(r) + qsave(r)]};

18 Equation E_walraslack
19 # Check Walras' Law. Value of "walraslack" should be zero #
20 walras_sup = walras_dem + walraslack;
```

2.8.3 Price of regional Absorption and MUV price index

The model also includes two additional price indices—a regional absorption price index and a global index of so-called manufactured exports from high-income countries¹¹

¹⁰The equation in the TABLO code is labeled E_rorg. This is because $PFACTWLD$ is exogenous as the model's price anchor and thus this equation 'explains' $RORG$ which has no separate equation.

¹¹Intended to be closely related to the World Bank's Manufactured Unit Value (MUV) index.

Equation (2.18) defines the absorption price index for each region as a weighted average price index of the final demand subset $DOMABS$ which includes private, public and investment demand. Equation (2.19) then defines the regional absorption price using the Fisher index.

Equation (2.20), defines a weighted average of FOB export prices for a subset of commodities and regions. The commodity index covers manufactured commodities defined in the subset $CMUV$. The first regional sum covers all regions defined in the subset $RMUV$, which consists of high-income countries. The second regional sum is over all regions. Equation (2.21) defines the associated MUV Fisher price index.

This unit describes the variables $PABS_r$, $PABSFISHER_r$, $PMUV$ and $PMUVFISHER$ using equations E_pabs, E_pabsFisher, E_pmuV and E_pmuVfisher.

$$PABS_r = \sum_{d \in DOMABS} \varphi_{r,d} PGDPEXP_{r,d} \quad (2.18)$$

$$PABSFISHER_r = \frac{PABSFISHER_{r,-1}}{\sqrt{\frac{PABS_r QABS_{r,-1}}{PABS_{r,-1} QABS_{r,-1}} \cdot \frac{PABS_r QABS_r}{PABS_{r,-1} QABS_r}}} \quad (2.19)$$

$$PMUV = \sum_{c \in CMUV} \sum_{s \in RMUV} \sum_d \alpha_{c,s,d} PFOB_{c,s,d} \quad (2.20)$$

$$PMUVFISHER = \frac{PMUVFISHER_{-1}}{\sqrt{\frac{\sum_c \sum_s \sum_d PFOB_{c,s,d} QXS_{c,s,d,-1}}{\sum_c \sum_s \sum_d PFOB_{c,s,d,-1} QXS_{c,s,d,-1}} \cdot \frac{\sum_c \sum_s \sum_d PFOB_{c,s,d} QXS_{c,s,d}}{\sum_c \sum_s \sum_d PFOB_{c,s,d,-1} QXS_{c,s,d}}}} \quad (2.21)$$

Listing 2.4: GEMPACK equations for regional absorption and MUV price indices

```

1 Equation E_pabs
2 # computes % change in the price of aggregate domestic absorption in region r #
3 (all,r,REG)
4 pabs(r) = sum{d,DOMABS, ABSSHR(d,r) * pgdpexp(r,d)};

6 Equation E_pabsFisher
7 # computes % change in in aggreg. absorption: Fisher price index in r #
8 (all,r,REG)
9 pabsFisher(r) = 0.5 * [pabsLaspeyres(r) + pabsPaasche(r)];

11 Equation E_pmuV
12 # computes % change in manufactures unit value (MUV) price index #
13 pmuV = sum{c,CMUV, sum{s,RMUV, sum{d,REG, MUVSHR(c,s,d) * pfob(c,s,d)}}};

15 Equation E_pmuVfisher
16 # computes % change in MUV Fisher price index #
17 pmuVfisher = 0.5 * [pmuVLaspeyres + pmuVPaasche];

```

2.8.4 Definition of GDP

Equation (2.22) defines nominal GDP at market prices (in levels). It is the sum of the value of private, public and investment expenditures, exports of international trade and transport services, and net trade at world prices. Equation (2.23) defines the Fisher *volume* index for real GDP, where the formula for $VGDP$ follows. The expression for $VGDP$ evaluates the generic GDP expression at

prices tp and volumes tq .¹² Equation (2.24) rather trivially determines the GDP at market price deflator.¹³

$$\begin{aligned}
GDP_r &= \sum_c [PPA_{c,r} QPA_{c,r} + PGA_{c,r} QGA_{c,r} + PIA_{c,r} QIA_{c,r}] \\
&+ \sum_m^c PDS_{m,r} QST_{m,r} \\
&+ \sum_c \left[\sum_d PFOB_{c,r,d} QXS_{c,r,d} - \sum_s PCIF_{c,s,r} QXS_{c,s,r} \right]
\end{aligned} \tag{2.22}$$

$$\begin{aligned}
QGDP_{r,t} &= QGDP_{r,t-1} \sqrt{\frac{VGDP_{r,t-1,t}}{VGDP_{r,t-1,t-1}} \cdot \frac{VGDP_{r,t,t}}{VGDP_{r,t,t-1}}} \\
&= QGDP_{r,t-1} \sqrt{\frac{GDP_{r,t}}{GDP_{r,t-1}} \cdot \frac{VGDP_{r,t-1,t}}{VGDP_{r,t,t-1}}}
\end{aligned} \tag{2.23}$$

$$\begin{aligned}
VGDP_{r,tp,tq} &= \sum_c [PPA_{c,r,tp} QPA_{c,r,tq} + PGA_{c,r,tp} QGA_{c,r,tq} + PIA_{c,r,tp} QIA_{c,r,tq}] \\
&+ \sum_m^c PDS_{m,r,tp} QST_{m,r,tq} \\
&+ \sum_c \left[\sum_d PFOB_{c,r,d,tp} QXS_{c,r,d,tq} - \sum_s PCIF_{c,s,r,tp} QXS_{c,s,r,tq} \right]
\end{aligned}$$

$$PGDP_r = GDP_r / QGDP_r \tag{2.24}$$

This unit describes the variables GDP_r , $QGDP_r$, $VGDP_{r,tp,tq}$ and $PGDP_r$ using equations E_vgdp, E_qgdpFisher, E_vgdpFisher and E_pgdpFisher.

Listing 2.5: GEMPACK equations for nominal GDP

```

1 Equation E_vgdp
2 # change in value of GDP #
3 (all,r,REG)
4 GDP(r) * vgdpr(r)
5 = sum{c,COMM, VGP(c,r) * [qga(c,r) + pga(c,r)]}
6 + sum{c,COMM, VPP(c,r) * [qpa(c,r) + ppa(c,r)]}
7 + sum{c,COMM, VIP(c,r) * [qinv(r) + pinv(r)]}
8 + sum{c,COMM, sum{d,REG, VFOB(c,r,d) * [qxs(c,r,d) + pfob(c,r,d)]}}
9 + sum{m,MARG, VST(m,r) * [qst(m,r) + pds(m,r)]}
10 - sum{c,COMM, sum{s,REG, VCIF(c,s,r) * [qxs(c,s,r) + pcif(c,s,r)]}};

12 pgdpexp(r,g) # GDP-expenditure component price indices #;
13 Equation E_pgdpexp
14 # GDP-expenditure component price indices #
15 (all,r,REG) (all,g,GDPEX)
16 pgdpexp(r,g) = IF[g="household", ppriv(r)] + IF[g="Investment", pinv(r)]
17 + IF[g="Government", pgov(r)] + IF[g="Exports", pfobxw(r)]
18 + IF[g="IntlMargins", pstxw(r)] + IF[g="Imports", pmwreg(r)];

20 Equation E_qgdpexp
21 # GDP-expenditure side quantity indices #
22 (all,r,REG) (all,g,GDPEX)
23 qgdpexp(r,g) = IF[g="household", qp(r)] + IF[g="Investment", qinv(r)]

```

¹²In a dynamic context these will represent t and $t-1$. For comparative static simulations, they represent pre- and post-shock values.

¹³N.B. $GDP_t = VGDP_{r,t,t}$.

```

24 + IF[g="Government", qg(r)] + IF[g="Exports", qfobxw(r)]
25 + IF[g="IntlMargins", qstxw(r)] + IF[g="Imports", qmwreg(r)];

27 Equation E_vgdpxp
28 # value index for each GDP-expenditure component #
29 (all,r,REG) (all,g,GDPEX)
30 vgdpxp(r,g) = pgdpxp(r,g) + qgdpxp(r,g);

32 Equation E_pgdpLaspeyres
33 # computes % change in GDP Laspeyres price index in r #
34 (all,r,REG)
35 0 = sum(g, GDPEX, GDPEX_FPIQ(r,g) * [pgdpxp(r,g) - pgdpLaspeyres(r)]);

37 Equation E_qgdpLaspeyres
38 # computes % change in GDP Laspeyres quantity index in r #
39 (all,r,REG)
40 0 = sum(g, GDPEX, GDPEX_IPFQ(r,g) * [qgdpxp(r,g) - qgdpLaspeyres(r)]);

42 Equation E_pgdpPaasche
43 # computes % change in GDP Paasche price index in r #
44 (all,r,REG)
45 pgdpPaasche(r) = vgdpxp(r) - qgdpLaspeyres(r);

47 Equation E_qgdpPaasche
48 # computes % change in GDP Paasche quantity index in r #
49 (all,r,REG)
50 qgdpPaasche(r) = vgdpxp(r) - pgdpLaspeyres(r);

52 Equation E_pgdpFisher
53 # computes % change in GDP Fisher price index in r #
54 (all,r,REG)
55 pgdpFisher(r) = 0.5 * [pgdpLaspeyres(r) + pgdpPaasche(r)];

57 Equation E_qgdpFisher
58 # computes % change in GDP Fisher quantity index in r #
59 (all,r,REG)
60 qgdpFisher(r) = 0.5 * [qgdpLaspeyres(r) + qgdpPaasche(r)];

62 Equation E_vgdpxpFisher
63 # computes % change in GDP Fisher value in r #
64 (all,r,REG)
65 vgdpxpFisher(r) = pgdpFisher(r) + qgdpFisher(r);

```

Chapter 3

Model dynamics

3.1 Introduction

From a specification point of view, dynamics broadly involves four areas:

1. Update of exogenous endowments;
2. Changes to technologies;
3. Changes to preferences; and
4. Changes to policies.

In all other ways, the dynamic model is solved as a sequence of comparative static equilibria with updates in the aforementioned four areas occurring between periods. A dynamic solution can be found in the absence of any external information with informed guesses about the evolution of endowments, technology and preferences. However, a dynamic baseline is typically coupled to external information about certain future trends, such as population growth, labor force growth, and per capita income growth. The baseline scenario is then used to calibrate key parameters to target values based on the external information. As mentioned in the introduction, this document contains a technical description of the tools to construct a dynamic baseline of the global economy but does not describe the construction of the baseline itself.

3.2 Endowments

3.2.1 Population and labor force

In most baselines, population and labor force growth are taken from external demographic projections, for example the United Nation’s Population Division typically biennial projections (<http://www.un.org/en/development/desa/population/>).¹⁴ Data sources for baselines are discussed further below.

Demographic projections typically include various demographic slices—for example by age group (0-4, 5-9, ..., 95-99, 100+ or some aggregation thereof), by gender, by country-origin and/or by education level. The standard GTAP-based baseline mostly uses total population as well as some indicator for the labor force. The simplest for the latter is to equate labor force growth to the

¹⁴Their latest projection, entitled *2017 Revision of World Population Prospects* was issued in June, 2017.

growth of the so-called ‘working age’ population—often defined as the 15-64 age group. A somewhat more sophisticated version could use age- and gender-specific labor force participation rates and create an aggregate labor force growth rate combining the labor force participation rates with the demographic projections. Assuming the demographic projections and the assumptions on labor force participation are exogenous, these calculations can be done separately and the inputs to the baseline are simply the growth of total population and the labor force. Due to the lack of additional information, we assume no differentiation in the growth of labor endowments across skill types. We could use the education information included with the International Institute for Applied Systems Analysis (IIASA) projections to guide the relative growth of skilled versus unskilled workers, further discussed below.

3.2.2 Capital

The model uses the standard capital accumulation expression to drive the growth in the capital stock:¹⁵

$$K_t = (1 - \delta)K_{t-1} + I_{t-1} \quad (3.1)$$

Note that in this case the capital stock is no longer pre-determined but depends on the endogenous level of investment in the current period. Capital growth will be determined by savings behavior (possibly adjusted by public and foreign savings) and the rate of depreciation. It is often the case that adjustments will be required for both the rate of saving and depreciation to develop a baseline with long-run steady state properties, which could be defined for example, by a (near) constant rate of return. In this case, we may have an exogenous target for the investment to GDP ratio in which case we would override the savings level determined via the top level regional household utility function.

Listing 3.1 implements the year-on-year link between investment and capital growth in the model’s TABLO code. In dynamic simulations, this link is activated in equation `E_capadd` by swapping the variable `capaddr` with `qecapitalr` in the closure file¹⁶ and by shocking the homotopy variable, `del_uni`, with a value of 1. With `capaddr` exogenous, equation `E_capadd` then associates net investment changes to aggregate capital growth in each region, `qecapr`, based on changes in the ratio of two coefficients—i.e., the value of investment generated in the previous year adjusted for depreciation (`VKADDr`) relative to the initial value of beginning period capital stock (`VKBINIr`). In the code `VKADDr` is a parameter equal to the initial value of net investment—i.e. gross investment minus depreciation.

The next equation, `E_qecap`, is simply a bridging equation that relates aggregate capital growth, `qecapr`, to aggregate capital endowment, `qee,r`.¹⁷ Equation `E_kb`—which is already included in the

¹⁵Note that if we move to multi-year steps, the capital accumulation equation needs to include investment for the skipped years. If we assume that investment growth is constant in the inter-period step, the capital accumulation formula is:

$$K_t = (1 - \delta)^n K_{t-n} + \frac{(1 + g)^n - (1 - \delta)^n}{g + \delta} I_{t-n}$$

where g is the inter-period growth rate of investment:

$$g = \left(\frac{I_t}{I_{t-n}} \right)^{1/n} - 1$$

¹⁶This swap exogenizes `capaddr` and endogenizes `qecapital,r`. The appropriate statement in the closure file is: `Swap qe("capital",REG) = capadd(REG)`

¹⁷Equation `E_qecap` simplifies to `qecap(r) = qe("capital",r)` since the capital endowment set, `ENDWC`, contains just one element named capital. This equation along with the variable `qecapr` can be deleted from the model

standard model—equalizes changes in the aggregate capital endowment, $qe_{e,r}$, with the beginning-of-period capital stock, kb_r .

Listing 3.1: **GEMPACK equations for year-on-year capital accumulation function**

```

1 Equation E_capadd
2 # associates net investment changes to aggregate capital endowment in r #
3 (all,r,REG)
4 VKADD(r) * del_unity + capadd(r) = 0.01 * VKBINI(r) * qecap(r);
5 Coefficient (parameter) (all,r,REG)
6   VKADD(r) # addition to capital stock from previous period's investment #;
7 Formula (initial) (all,r,REG)
8   VKADD(r) = REGINV(r) - [VKB(r) * DEPR(r)];
9 Equation E_qecap
10 # computes % change in aggregate capital endowment in region r #
11 (all,r,REG)
12 qecap(r) = sum{e,ENDWC, [VES(e,r) / GROSSCAP(r)] * qe(e,r)};
13 Equation E_kb
14 # associates change in cap. services w/ change in cap. stock #
15 (all,r,REG)
16 kb(r) = sum{e,ENDWC, [VES(e,r) / GROSSCAP(r)] * qe(e,r)};

```

3.2.3 Land and natural resources

Aggregate land supply is determined by an iso-elastic supply curve. This is a sound specification for relatively short-term horizons, as it is possible to set land supply elasticity relatively low for land-scarce regions. The basic land supply function could be extended to one with lower and upper limits such as a logistic function, which would imply movements up and down the supply curve. One could also adjust the shift parameters in the land supply curve to handle possible events such as sea-level rise.

Sector-specific natural resources—such as fossil fuel reserves—should also have their own sector-specific supply functions. In the current model we work with iso-elastic supply functions. This specification allows us to target projected changes in the price of natural resources such as oil and gas from external sources. As possible extension to this specification, we could include kinks in the supply elasticities. The kinks allow for differential response based on market conditions as it is typically easier to contract supply than to expand it. More sophisticated models tend to have resource depletion modules for natural resources that puts an overall cap on supply—this is typically the case for energy-based models.

3.3 Technology

The baseline normally involves calibrating one economy-wide variable to hit a given target for GDP (per capita) growth. A simplified model can be specified as:

$$Y = A \cdot F(\lambda^l L, \lambda^k K)$$

where Y is output that is a function of labor and capital in efficiency units. The variables λ^l and λ^k represent the growth of labor and capital in efficiency units, normally set to 1 in the base year. The variable A is a total factor productivity (TFP) shifter, whereas the other two variables induce biased technical change. The discussion above described the dynamics of labor and capital. If the growth of output, Y , is given, then we have three parameters that enable the model to target output

code. However, we retain them for flexibility and to avoid hard-coding $qe_{capital,r}$ in place of $qecap_r$ in equation E_capadd.

growth—TFP or one of the two biased technical change parameters, or some combination of the three. In principle the choice should be based on historical observations and linked to other variables such as the evolution of factor prices. History provides only partial guidance—particularly at the global level. The most frequent assumption used in dynamic baselines, particularly those associated with integrated assessment, is to assume that residual growth is embedded in labor-biased technical change. Hence given the output equation above, F is inverted to evaluate the value of λ^l given L , K and Y .¹⁸ One alternative, used in the GREEN model (van der Mensbrugghe, 1994), is to implement so-called balanced growth. The interpretation is that the long-term capital/labor ratio, expressed in efficiency units is constant:

$$\frac{\lambda^k K}{\lambda^l L} = \chi$$

where χ could be set to the base year capital to labor ratio, or some anticipated long-term trend. With Y and χ given, we have two equations and two unknowns and thus we can calibrate λ^l and λ^k simultaneously. A third strategy, pioneered by Dixon and Rimmer (2002) is to use the historical evolution of the capital/labor ratio, subject to a cost-neutral constraint on the cost function, (to be described below) and TFP to target Y , i.e. calibrate A to the growth target. This is the so-called ‘twist’ strategy.

In its simplest form, the ‘twist’ strategy is applied to a CES bundle. The idea is to move the capital/labor ratio from some initial value, to some terminal value:

$$\frac{K}{L} = (1 + tw) \frac{K_0}{L_0}$$

where tw represents the percent change in the ratio. The ‘twist’ is done in such a way maintain the same cost level (with unchanged factor prices). In the case of the CES function, this implies:

$$P = \left[\alpha^l \left(\frac{W}{\lambda^l} \right)^{1-\sigma} + \alpha^k \left(\frac{R}{\lambda^k} \right)^{1-\sigma} \right]^{1/(1-\sigma)} = P_0 = \left[\alpha^l W^{1-\sigma} + \alpha^k R^{1-\sigma} \right]^{1/(1-\sigma)}$$

We now have a system of three equations—the output equation, the twist equation and the constant cost equation—and these can be solved simultaneously to determine A , λ^l and λ^k . With a little bit of algebra it is possible to provide expressions for λ^l and λ^k with respect to the desired twist, tw , and the value shares:

$$\lambda^l = \left[1 + tw \cdot s^k \right]^{1/(1-\sigma)}$$

$$\lambda^k = \left[\frac{1 + tw \cdot s^k}{1 + tw} \right]^{1/(1-\sigma)}$$

where tw represents the percent change in the capital to labor ratio and s^k is the base year value share of capital.

This unit implements baseline calibration of alternative economy-wide factor productivity variables to hit a given target for GDP. As shown in Listing 3.2, Equation E_afe allows 3 possible alternatives:

- Hicks-neutral TFP shifter (*afereg_r*)
- Labor-biased technology shifter (*afelabreg_r*)

¹⁸Note that exogenous changes to A and λ^k are also possible.

- Non-capital-biased technology shifter ($afendwxcreg_r$)

This unit also implements labor-capital twist mechanisms by modifying equation E_qfe . In the revised code shown in Listing 3.2, equation E_qfe has been partitioned into two parts, i.e., the labor and capital endowment set, $ENDWLC$, and non labor-capital endowments set, $ENDWXC$. The former implements labor-capital twists via the variable $afetwist_{e,a,r}$. The next equation, $E_afetwistave$, imposes a cost-neutral constraint on the labor-capital bundle while the last equation, $E_afetwist$, provides user flexibility with the inclusion of various labor-capital twist shifters—e.g., activity-specific and all region twist shifter ($afetwistact_{a,r}$), all activity and region-specific shifter ($afetwistreg_{e,r}$), and activity- and region-specific shifter ($afetwistall_{e,a,r}$).

Listing 3.2: GEMPACK equations for factor demands with labor-capital ‘twist’

```

1 Equation E_afe
2 # sector/region specific average rate of prim. factor e augmenting tech change #
3 (all,e,ENDW) (all,a,ACTS) (all,r,REG)
4 afe(e,a,r)
5 = afecom(e) + afesec(a) + afereg(r) + afeall(e,a,r) + afecomreg(e,r)
6 !< endowment-biased technical change and shifters >!
7 + IF[e in ENDWL, afelabreg(r) + afelabact(a,r) + afelab(e,a,r)]
8 + IF[e in ENDWXC, afendwxcreg(r) + afendwxact(a,r) + afendwxc(e,a,r)];

10 Equation E_qfe
11 # demands for endowment commodities #
12 (all,e,ENDW) (all,a,ACTS) (all,r,REG)
13 qfe(e,a,r)
14 = IF[e in ENDWLC,
15     - afe(e,a,r) + [afetwist(e,a,r) - afetwistave(a,r)] + qva(a,r)
16     - ESUBVA(a,r) * [pfe(e,a,r) - afe(e,a,r) - pva(a,r)]]
17 + IF[e in ENDWXC,
18     - afe(e,a,r) + qva(a,r)
19     - ESUBVA(a,r) * [pfe(e,a,r) - afe(e,a,r) - pva(a,r)]];

21 Equation E_afetwistave
22 # average endowment twist shifter in activity a in reg r #
23 (all,a,ACTS) (all,r,REG)
24 0 = sum{e,ENDWLC, VFP(e,a,r) * [afetwist(e,a,r) - afetwistave(a,r)]};

26 Equation E_afetwist
27 # sector and region specific twist towards use of endowment e #
28 (all,e,ENDWLC) (all,a,ACTS) (all,r,REG)
29 afetwist(e,a,r) = afetwistact(e,a) + afetwistreg(e,r) + afetwistall(e,a,r);

```

3.3.1 Multi-sector models

The description above is straight-forward in the case of a single sector macro model, but multi-sector models need additional assumptions. In the case of labor-biased technical change, there are as many potential labor productivity factors as there are activities and labor types. The simplest assumption imposes uniformity across activities and skill types. Somewhat more generically, we can assume that labor productivity takes the following form:

$$\pi_{l,a}^l = \alpha_{l,a}^l + \beta^{l,a} \gamma^l$$

where γ^l is an economy-wide parameter that can be calibrated to target GDP. Uniformity implies α^l is zero and β^l is one for all skill types and activities (See equation listing below for corresponding TABLO implementation). While the econometric evidence is relatively scant, it nonetheless suggests that there are differences across activities (see Jorgenson et al. (2013) and Roson and van der Mensbrugge (2017)) that can be exploited. Our standard starting point is to assume that α^l is

between 1 and 2 percent in agriculture and 2 percent in manufacturing¹⁹. This implies that the calibrated γ^l represents labor productivity in services and that there is a constant (positive) wedge in agriculture and manufacturing. These assumptions obviously have structural assumptions beyond those generated by shifting patterns of demand.

If we use the [Dixon and Rimmer \(2002\)](#) approach, one would have assumptions about the ‘twist’ between capital and labor, i.e. some assumptions regarding the capital/labor ratio, at the activity level. [Dixon and Rimmer \(2002\)](#) are able to use the richness of historical data for Australia and the United States ([Dixon and Rimmer, 2005](#)) to measure historical ‘twists’ that can then inform the projected ‘twist’. The approach above, for labor-biased technical change can then be used to determine TFP with a calibrated economy-wide productivity measure and linear transformations to allocate the economy-wide measure across activities.

In the balanced growth scenarios, there has been no explicit assumption about productivity across activities/labor types. Instead the following expression is assumed to hold, which is a generalization of the balanced growth equation above:

$$\frac{\sum_a \lambda_a^k K_a}{\sum_a \sum_l \lambda_{l,a}^l L_{l,a}} = \chi$$

Typical baselines may also include other exogenous assumptions on technological progress such as yield changes in crops, energy efficiency improvement (identified by end-user, energy carrier, etc.) and autonomous improvements in trade and transport margins. The use of expert models could be used to drive some of these assumptions such as crop and energy models.

This unit implements labor-biased technical change, with many potential labor productivity factors as there are activities and labor types, using Equation `E_afelab`. The variables `afelabregr` and `afelabadde,a,r` correspond to γ^l and α^l respectively, while the coefficient (`LABMULTe,a,r`) corresponds to the β^l parameter.

Listing 3.3: GEMPACK equations for labor productivity changes

```

1 Equation E_afelab
2 # labor productivity shifters #
3 (all,e,ENDWL) (all,a,ACTS) (all,r,REG)
4 afelab(e,a,r) = afelabadd(e,a,r) + LABMULT(e,a,r) * afelabreg(r);

```

3.4 Preferences

Trade preferences are governed by a two-level nested CES (Armington) structure. Similar to [Dixon and Rimmer \(2002\)](#), we have introduced a twist specification in the top-level Armington nest that allows for shifts in preferences for domestic vs. imported commodities for all agents—i.e., firms, private households, investment and government. We have also introduced a twist specification in the second-level nest that allows for shifts in import preferences across trading partners.

This unit implements the two-level nested CES (Armington) structure with twist preferences by modifying equations `E_qfd`, `E_qfm`, `E_qpd`, `E_qpm`, `E_qid`, `E_qim`, `E_qgd`, `E_qgm` and `E_qxs`. The agent-specific domestic and imported twist variables —`afdc,a,r`, `apdc,r`, `aidc,r`, `agdc,r`, `afmc,a,r`, `apmc,r`, `aimc,r` and `agmc,r`—facilitate cost-neutral preference shifts towards domestic and imported commodities in each agent’s top level Armington demand. The second level Armington twist variable, `amdstwistc,s,d`, in equation `E_qxs` facilitates preference shifts towards a specific trading partner

¹⁹With β^l set to 1.

or a group of trading partners. The last equation, E_amdstwistave, imposes a cost-neutral constraint on the second level import cost function.

Listing 3.4: GEMPACK equations for Armington demands with ‘twist’ specification

```

1  Equation E_qfd
2  # act. a demands for domestic good c #
3  (all,c,COMM) (all,a,ACTS) (all,r,REG)
4  qfd(c,a,r) = qfa(c,a,r) - ESUBD(c,r) * [pfd(c,a,r) - pfa(c,a,r)]
5  + afd(c,a,r);

7  Equation E_qfm
8  # act. a demands for composite import c #
9  (all,c,COMM) (all,a,ACTS) (all,r,REG)
10 qfm(c,a,r) = qfa(c,a,r) - ESUBD(c,r) * [pfm(c,a,r) - pfa(c,a,r)]
11 + afm(c,a,r);

13 Coefficient (all,c,COMM) (all,a,ACTS) (all,r,REG)
14 FMSHR(c,a,r) # share of firms' imports in dom. composite, purch. prices #;
15 Zerodivide default 0.5;
16 Formula (all,c,COMM) (all,a,ACTS) (all,r,REG)
17 FMSHR(c,a,r) = VMFP(c,a,r) / VFP(c,a,r);
18 Zerodivide off;

20 Equation E_afd
21 # equation to facilitate shift towards domestic input c in act.a in region r #
22 (all,c,COMM) (all,a,ACTS) (all,r,REG)
23 afd(c,a,r) = FMSHR(c,a,r) * afdmtwist(c,a,r);

25 Equation E_afm
26 # equation to facilitate shift towards imported input c in act. a in region r #
27 (all,c,COMM) (all,a,ACTS) (all,r,REG)
28 afm(c,a,r) = [FMSHR(c,a,r) - 1] * afdmtwist(c,a,r);

30 Equation E_qpd
31 # private consumption demand for domestic goods #
32 (all,c,COMM) (all,r,REG)
33 qpd(c,r) = qpa(c,r) - ESUBD(c,r) * [ppd(c,r) - ppa(c,r)] + apd(c,r);

35 Equation E_qpm
36 # private consumption demand for aggregate imports #
37 (all,c,COMM) (all,r,REG)
38 qpm(c,r) = qpa(c,r) - ESUBD(c,r) * [ppm(c,r) - ppa(c,r)] + apm(c,r);

40 !< Composite Tradeables >!
41 Coefficient (all,c,COMM) (all,r,REG)
42 PMSHR(c,r) # share of imports in private hhld cons. at producer prices #;
43 Formula (all,c,COMM) (all,r,REG)
44 PMSHR(c,r) = VMPP(c,r) / VPP(c,r);

46 Equation E_apd
47 # equation to facilitate shift towards cons of dom. c by priv hhld in region r #
48 (all,c,COMM) (all,r,REG)
49 apd(c,r) = PMSHR(c,r) * apdmtwist(c,r);

51 Equation E_apm
52 # equation to facilitate shift towards cons of imp. c by priv hhld in region r #
53 (all,c,COMM) (all,r,REG)
54 apm(c,r) = [PMSHR(c,r) - 1] * apdmtwist(c,r);

56 Equation E_qid
57 # demand for domestic investment commodity c #
58 (all,c,COMM) (all,r,REG)
59 qid(c,r) = qia(c,r) - ESUBD(c,r) * [pid(c,r) - pia(c,r)] + aid(c,r);

61 Equation E_qim
62 # demand for imported investment commodity c #
63 (all,c,COMM) (all,r,REG)

```

```

64 qim(c,r) = qia(c,r) - ESUBD(c,r) * [pim(c,r) - pia(c,r)] + aim(c,r);

66 !< Composite tradeables >!
67 Coefficient (all,c,COMM) (all,r,REG)
68 IMSHR(c,r) # share of imports for investment at producer prices #;
69 Formula (all,c,COMM) (all,r,REG)
70 IMSHR(c,r) = VMIP(c,r) / VIP(c,r);

72 Equation E_aid
73 # equation to facilitate shift towards use of dom. investment commodity c in r #
74 (all,c,COMM) (all,r,REG)
75 aid(c,r) = IMSHR(c,r) * aidmtwist(c,r);

77 Equation E_aim
78 # equation to facilitate shift towards use of imp. investment commodity c in r #
79 (all,c,COMM) (all,r,REG)
80 aim(c,r) = [IMSHR(c,r) - 1] * aidmtwist(c,r);

82 Equation E_qgd
83 # government consumption demand for domestic goods #
84 (all,c,COMM) (all,r,REG)
85 qgd(c,r) = qga(c,r) - ESUBD(c,r) * [pgd(c,r) - pga(c,r)] + agd(c,r);

87 Equation E_qgm
88 # government consumption demand for aggregate imports #
89 (all,c,COMM) (all,r,REG)
90 qgm(c,r) = qga(c,r) - ESUBD(c,r) * [pgm(c,r) - pga(c,r)] + agm(c,r);

92 !< Composite tradeables >!
93 Coefficient (all,c,COMM) (all,r,REG)
94 GMSHR(c,r) # share of imports for gov't hhd at producer prices #;
95 Formula (all,c,COMM) (all,r,REG)
96 GMSHR(c,r) = VMGP(c,r) / VGP(c,r);

98 Equation E_agd
99 # equation to facilitate shift towards cons. of domestic c by gov in region r #
100 (all,c,COMM) (all,r,REG)
101 agd(c,r) = GMSHR(c,r) * agdmtwist(c,r);

103 Equation E_agm
104 # equation to facilitate shift towards cons. of imported c by gov in region r #
105 (all,c,COMM) (all,r,REG)
106 agm(c,r) = [GMSHR(c,r) - 1] * agdmtwist(c,r);

108 Equation E_qxs
109 # regional demand for disaggregated imported commodities by source #
110 (all,c,COMM) (all,s,REG) (all,d,REG)
111 qxs(c,s,d)
112 = -ams(c,s,d) + [amdstwist(c,s,d) - amdstwistave(c,d)]
113 + qms(c,d) - ESUBM(c,d) * [pmds(c,s,d) - ams(c,s,d) - pms(c,d)];

115 Equation E_amstwistave
116 # average top-level import twist shifter for com c by importing reg d #
117 (all,c,COMM) (all,d,REG)
118 0 = sum{s,REG, VMSB(c,s,d) * [amdstwist(c,s,d) - amdstwistave(c,d)]};

120 Equation E_amstwist
121 # commodity and region specific twist towards imports of com c from source s #
122 (all,c,COMM) (all,s,REG) (all,d,REG)
123 amdstwist(c,s,d) = amdstwistall(c,s,d) + amdstwistsrc(c,s) + amdstwistreg(s,d);

```

3.5 Policies

A dynamic baseline starts in a given year—for example 2014—and with policies calibrated to the base year. A number of policy changes may already be in the process of being implemented—for example the commitments made under the 2015 Paris Agreement, or bilateral or regional trade agreements, or may already have been negotiated with a future phase-in period, such as the Comprehensive and Progressive Agreement for Trans-Pacific Partnership. The baseline scenario should include these policy changes, to the extent possible. In some cases, the changes are relatively straightforward, such as a percentage cut in a tariff rate. In other cases it may require interpretation. For example, is a commitment to an x-percent improvement in energy efficiency a binding commitment, or one that might have been anticipated in a baseline.

3.6 Data sources for exogenous baseline assumptions

GDP or per capita GDP projections are typically sourced from international agencies such as the International Monetary Fund (IMF), the Organisation for Economic Cooperation and Development (OECD) and the World Bank—though often these are short- and medium-term projections. Global population and labor force growth are available from demographic projections by the United Nations Population Division²⁰ or IIASA²¹.

An alternative source of exogenous baseline assumptions is IIASA’s Shared Socioeconomic Pathways (SSPs) dataset, which allows users to choose among five potential socioeconomic development pathways.²² The SSPs include projections on GDP, population and educational attainment—the latter could be used to differentiate the relative growth of skilled versus unskilled workers. Three economic modeling teams developed an independent set of projections for the five SSPs—the OECD, IIASA and the Potsdam Institute for Climate Impact Research (PIK). All are harmonized to the same set of demographic projections for the 5 SSPs undertaken by the demographers at IIASA. The GDP projections of the OECD and IIASA are based on country-level assumptions (some 150+ countries covering most of world GDP and population). The PIK GDP projections are available for a fixed set of 32 aggregate regions—some of which are individual countries. GTAP Center’s staff has prepared a GTAP-friendly version of the SSPs (including the UN’s population projections). It has extended the SSP dataset: 1) gap filled all of the missing countries to match the UN’s population dimensionality; and 2) annualized the projections that were initially available in 5-year time steps.

²⁰ <http://www.un.org/en/development/desa/population/>

²¹ <http://www.iiasa.ac.at/web/home/research/researchPrograms/WorldPopulation/Introduction.html>

²² For further information on SSPs, see <https://tntcat.iiasa.ac.at/SspDb> or the special issue of the Journal of Global Environmental Change devoted to SSP <http://www.iiasa.ac.at/web/home/research/researchPrograms/Energy/news/161005-SSP.html>

Chapter 4

Conclusions and future directions

Since the development of the standard GTAP model in the late 1990s, the comparative static trade model has served as the workhorse of much of trade policy analysis. There have been many applications of the standard GTAP model as well as many modifications and extensions. Over time however, many academics, think-tanks and international organization interested in the analysis of trade have been turning to dynamic computable general equilibrium models. One reason is that dynamic models are better suited to deal with examining the consequences of important long-term processes posed by demographic, technological and climatic changes. And even for "traditional" questions like the impact of regional and multilateral trade liberalization, dynamic models can give additional insights not available to comparative static models because, among other advantages, dynamic models are able to incorporate the interaction between trade and investment flows.

It is in this spirit - strengthening the technical basis of long-term trade analysis - that the Global Trade Model has been developed by the Center for Global Trade Analysis and the WTO. There is broad consensus on the way international trade is to be modeled in the dynamic CGE literature. We have followed this consensus in the development of the Global Trade Model. The model has already been used to study the economic effects of digital innovation (WTO, 2018), the future of trade in agriculture (Bekkers and Jackson, 2018) and trade in services (WTO, 2019), China's future development (Bekkers et al., 2019) and the evolution of global trade policy (Bekkers, 2019).

But this consensus notwithstanding, there is a need for further research and work to improve dynamic CGE models and the construction of baselines, specially along the following lines. First, better coverage is needed of the different components of the balance of payments such as remittances (in relation to migration) and capital income (related to net debt and asset positions and intertemporal budget constraints). Second, the discrepancy between real trade growth generated by business-as-usual dynamic CGE models and historical trade growth deserves further attention. Third, new modeling tools (e.g. including monopolistic competition in the model) have to be developed and additional data, not currently part of the GTAP database, have to be collected to explore international trade questions related to the rapidly growing digital economy. The WTO hopes to contribute to this future research agenda and a future paper will describe progress that has been made in this regard using the Global Trade Model.

Bibliography

- Bekkers, E. 2019. “Challenges to the Trade System: The Potential Impact of Changes in Future Trade Policy.” *Journal of Policy Modeling*, 41(3): 489–506. doi:10.1016/j.jpolmod.2019.03.016. <https://www.sciencedirect.com/science/article/pii/S0161893819300420>.
- Bekkers, E., and J. Francois. 2018. “A Parsimonious Approach to Incorporate Firm Heterogeneity in CGE-Models.” *Journal of Global Economic Analysis*, 3(2): 1–68. doi:10.21642/JGEA.030201AF. <https://jgea.org/resources/jgea/ojs/index.php/jgea/article/view/69>.
- Bekkers, E., and L.A. Jackson. 2018. “Challenges to the Trade System: The Potential Impact of Changes in Future Trade Policy.” *Economic Review*, Special Issue, pp. 5–26. <https://www.kansascityfed.org/~media/files/publicat/econrev/econrevarchive/2018/si18bekkersjackson.pdf>.
- Bekkers, E., R. Koopman, and C.L. Rego. 2019. “Structural change in the Chinese economy and changing trade relations with the world.” CEPR, London: CEPR, Report. <https://ideas.repec.org/p/cpr/ceprdp/13721.html>.
- Brockmeier, M. 2001. “A Graphical Exposition of the GTAP Model, 2001 Revision.” Global Trade Analysis Project (GTAP), Purdue University, West Lafayette, IN, GTAP Technical Paper No. 8. <https://www.gtap.agecon.purdue.edu/resources/download/181.pdf>.
- Corong, E., T. Hertel, R. McDougall, M. Tsigas, and D. van der Mensbrugghe. 2017. “The Standard GTAP Model, Version 7.” *Journal of Global Economic Analysis*, 2(1): 1–119. doi:10.21642/JGEA.020101AF.
- Dixon, P.B., and M.T. Rimmer. 2002. *Dynamic general equilibrium modelling for forecasting and policy: a practical guide and documentation of MONASH*, 1st ed., vol. 256. Amsterdam: Elsevier.
- Dixon, P.B., and M.T. Rimmer. 2005. “Mini-Usage: reducing barriers to entry in dynamic CGE Modeling.” Report. <https://www.gtap.agecon.purdue.edu/resources/download/2251.pdf>.
- Eurostat. 2008. “European Price Statistics: An Overview.” European Commission, Report. <http://ec.europa.eu/eurostat/documents/3217494/5700847/KS-70-07-038-EN.PDF/6b78bcc3-b219-4038-80d2-4180a9410678?version=1.0>.
- Harrison, W., and K.R. Pearson. 1996. “Computing Solutions for Large General Equilibrium Models Using GEMPACK.” *Computational Economics*, 9(2): 83–127. doi:10.1007/BF00123638.
- Jorgenson, D.W., H. Jin, D.T. Slesnick, and P.J. Wilcoxon. 2013. “Chapter 17 - An Econometric Approach to General Equilibrium Modeling.” In *Handbook of Computable General Equilibrium Modeling SET, Vols. 1A and 1B*, edited by P. B. Dixon and D. W. Jorgenson. Elsevier, vol. 1 of *Handbook of Computable General Equilibrium Modeling*, pp. 1133–1212. doi:10.1016/B978-0-444-59568-3.00017-1.
- McDougall, R. 2003. “A New Regional Household Demand System for GTAP (Revision 1).” Global Trade Analysis Project (GTAP), Purdue University, West Lafayette, IN, GTAP Technical Paper No. 20. <https://www.gtap.agecon.purdue.edu/resources/download/1593.pdf>.
- Roson, R., and D. van der Mensbrugghe. 2017. “Assessing Long Run Structural Change in Multi-Sector General Equilibrium Models.” Global Trade Analysis Project (GTAP), Department of Agricultural Economics, Purdue University, West Lafayette, IN, Presented at the 20th Annual

- Conference on Global Economic Analysis, West Lafayette, Indiana, United States. https://www.gtap.agecon.purdue.edu/resources/res_display.asp?RecordID=5221.
- van der Mensbrugge, D. 1994. "GREEN: The Reference Manual." OECD, OECD Economics Department Working Papers No. 143, January. doi:10.1787/054442860076.
- WTO. 2018. "World Trade Report 2018: The Future of World Trade. How Digital Technologies are Transforming Global Commerce." World Trade Organization (WTO), Geneva: Switzerland, Report. https://www.wto.org/english/res_e/publications_e/wtr18_e.htm.
- WTO. 2019. "World Trade Report 2019: The Future of Services Trade." World Trade Organization (WTO), Geneva: Switzerland, Report. https://www.wto.org/english/res_e/publications_e/wtr19_e.htm.

Appendix A

Mathematical appendix

A.1 Sets and subsets

The GTAP model’s ‘geometry’ relies on a number of sets that are defined at model implementation. In other words, the model description is based on a generic definition of sets and its implementation will be based on a specific definition of the sets as defined by the user. Table A.1 describes the most basic sets used in the GTAP model. For the regional indices, the model description will at times use s and d instead of r , particularly for bilateral trade variables. Their use is to clearly distinguish between source (s) and destination (d) regions. All bilateral variables assume that the source index appears before the destination index, i.e. exports are read along the row of the bilateral trade matrix and imports are read down a column.

The current version of the full GTAP database assumes a diagonal ‘make’ matrix, i.e. there is a one-to-one correspondence between an activity and a commodity. The aggregation facility allows for separate aggregation of activities and commodities and hence the model does not assume the one-to-one correspondence.²³

Table A.1: **Basic sets in the model**

<i>Name</i>	<i>Description</i>
$REG(r, s, d)$	Regions (s for source, d for destination)
$ACTS(a)$	(Production) Activities
$COMM(c)$	Commodities
$ENDW(e)$	Endowments

Table A.2 describes the only subsets for the commodity set. It represents a partition of the commodity space into margin and non-margin commodities. The former are specific to the international trade and transport module of the model.

Table A.3 describes the subsets used for endowments. There is an initial partition of endowments between sector-specific factors and economy-wide factors. The former are specific to a single activity. These are typically the natural resource base of the activity such as oil reserves in the case of oil extraction.²⁴ The economy-wide endowments are partitioned into two separate sets. The

²³Future releases of the GTAP database may depart from diagonality, for example a new version of the GTAP-Power database.

²⁴In GTAP classic, these factors were part of the sluggish endowments, however with a very small transformation elasticity.

Table A.2: **Commodity subsets**

Commodities: $COMM(c)$	
$MARG(m)$	$NMARG(n)$
Margin commodities	Non-margin commodities

first reflects the degree of mobility of the endowment—perfect mobility and partial (or sluggish) mobility. The user can decide the degree of mobility by defining the subsets $ENDWM$ and $ENDWS$, and in the case of sluggish factors, by also setting the transformation elasticity ($ETRAE$).²⁵ In a standard configuration, labor and capital endowments are mobile and land is sluggish. However, a simulation’s time framework may warrant departures from the standard configuration. For example, a short-term time horizon may be more compatible with moving capital to the sluggish subset.

Table A.3: **Endowment subsets**

Endowments: $ENDW(e)$		
$ENDWF(e)$	$ENDWMS(e)$	
Sector-specific factors	Economy-wide factors	
	Mobility	
	$ENDWM(e)$	$ENDWS(e)$
	Mobile factors	Sluggish factors
	Supply assumption	
	$ENDWC(e)$	$ENDWMSXC(e)$
	Capital	Other non-capital

The second partition of the economy-wide endowments partitions these into the capital endowment and the non-capital endowments (most often labor and land). [NEW] This version of the model introduces upward sloping supply curves for the non-capital economy-wide endowments (the elasticity of which could be zero). The capital stock is typically fixed in both comparative static and recursive dynamics. In the case of the latter, the capital stock evolves according to the standard capital accumulation equation.²⁶

²⁵Transformation elasticities are entered as negative values for the GTAP model.

²⁶ $K_{t+1} = (1 - \delta)K_t + I_t$