Toulemonde, Eric

Working Paper

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IZA Discussion Papers, No. 939

Provided in Cooperation with:
IZA – Institute of Labor Economics

Suggested Citation: Toulemonde, Eric (2003) : Acquisition of skills, education subsidies, and agglomeration of firms, IZA Discussion Papers, No. 939, Institute for the Study of Labor (IZA), Bonn

This Version is available at:
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Eric Toulemonde

November 2003
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Eric Toulemonde
University of Lausanne
and IZA Bonn

Discussion Paper No. 939
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IZA
P.O. Box 7240
D-53072 Bonn
Germany
Tel.: +49-228-3894-0
Fax: +49-228-3894-210
Email: iza@iza.org

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ABSTRACT

Acquisition of Skills, Education Subsidies, and Agglomeration of Firms

An analytically solvable model of new economic geography is developed. Acquisition of skills is costly for workers but it allows them to earn wages that are larger than those of the unskilled. Moreover, skills acquisition can be subsidized by a regional government. For large transport costs, firms spread more or less evenly between regions, their precise location being determined by the level of education subsidies. For low transport costs, firms agglomerate in one region. We also identify equilibria with partial agglomeration of firms. Finally, we show that the incentives to subsidy education largely depend on the level of transport costs.

JEL Classification: F12, F15, J51, R12

Keywords: economic geography, education, subsidies

Eric Toulemonde
DEEP, HEC
University of Lausanne
BFSH 1
1015 Lausanne
Switzerland
Email: eric.toulemonde@hec.unil.ch
1 Introduction

Economic geography models predict that mobile activities are agglomerated (resp. dispersed) when transport costs are sufficiently low (resp. high) (Krugman, 1991; Fujita, Krugman and Venables, 1999; Neary, 2001; Ottaviano and Thisse, 2003). On the one hand, to save on costs involved in selling at a distance, manufacturing firms are willing to locate their production in regions where the demand for their product is large. Since the size of the demand in a region depends on the numbers of workers residing in that region, firms locate at proximity of workers. On the other hand, workers prefer to live in regions that have good access to the products that they consume. They want to reside at the proximity of manufacturing firms. As a result, manufacturing firms and workers may have an incentive to agglomerate in a single region (the core). The other region (the periphery) hosts firms and workers from the traditional sector.

Krugman and Venables (1995), Venables (1996) make the same point using an alternative framework in which workers do not migrate. Instead, an input-output structure explains agglomeration of manufacturing firms. Upstream firms prefer to locate their production at the proximity of their customers (the downstream firms) whereas downstream firms are attracted towards regions where they have a good access to their inputs. Again, a core-periphery structure may emerge: downstream and upstream firms agglomerate in the core region.\footnote{The same type of results is also emphasized in Puga (1999).}

More recently, these models have been adapted to study policy implications (see Baldwin et al., 2003 for a review). Issues on taxation (Ludema and Wooton, 2000; Kind, Midelfart Knarvik and Schjelderup, 2000), on public goods (Andersson and Forslid, 2003; Trionfetti, 2001), on trade agreements (Baldwin and Robert-Nicoud, 2000) are now under study. Questions such as how do these policies affect firms’ location and how does firms’ location affect these policies are analyzed. In this paper, we address the issue of educational policies. Is it fruitful for a local government to subsidize higher education in order to increase the supply of skilled labor and attract new
firms? To what extent is there a “subsidy competition” between regional
governments to raise the number of skilled workers and attract new firms?
Do transport costs matter for these policies? These are the questions that
are treated in this paper.

As Baldwin et al. (2003) explain, early models of economic geography
are useful to illustrate the emergence of a core-periphery structure but are
tedious to work with, forcing numerical simulations for most results, which
makes them not suitable for the analysis of policy making. Therefore, Bald-
win et al. (2003) develop alternative models that present most character-
istics of the core-periphery model but are also analytically tractable2. Of
these models the footloose capital model (initially developed by Martin and
Rogers, 1995) displays agglomeration forces and is easy to handle. How-
ever it does not display the circular causality that is at the center of the
core-periphery models.

To study the issue of education we build a model that is inspired by
the footloose capital model in which circular causality is re-introduced. The
main difference with existing models is that agents have the choice of acquir-
ing skills and working in a modern industry where goods are differentiated,
or remaining unskilled and working in a constant returns to scale sector.
Acquisition of skills is costly but can be subsidized by a regional govern-
ment; moreover it allows individuals to earn wages that are larger than in
the constant returns to scale sector. As in Venables (1996), we ignore the
issue of migration between regions, which might be justified on the ground
that migrations between European countries are fairly low (see Decressin
and Fatás, 1995; Bentolila 1997 and Faini, Galli, Gennari and Rossi, 1997).

As usual in economic geographic models, firms from the modern industry
are willing to locate their production in regions where the demand for their
product is large in order to save on transport costs. The size of the demand in
a region depends on the numbers of workers who have invested in education
and earn large wages relative to the number of workers who remain unskilled

2See also Fujita and Thisse (2002) and Ottaviano, Tabuchi and Thisse (2002) for linear
models that are analytically tractable.
and earn low wages. Hence firms from the modern sector want to settle at the proximity of high-wage skilled workers. In addition, more workers decide to invest in education when more firms ask for skilled workers in their own region. The proportion of skilled workers increases with the number of firms in a region. As a result, if firms move towards a region, more workers from that region are induced to become skilled. In turn, this raises the demand in that region and reinforce the movement of firms to that region. The circular causality that was lost in the basic footloose capital model is now re-introduced through the modelling of skill acquisition. Despite this slight modification, the model remains analytically tractable and allows to get a closed-form solution for the location of firms. This model could therefore prove useful to analyze other policy implications.

We show that if subsidies are equal in both regions, firms spread evenly across regions for large transport costs whereas they agglomerate in a core region for low transport costs. When subsidies differ across regions, firms partially agglomerate in the low subsidy region for large transport costs, they partially agglomerate in the high subsidy region for intermediate transport costs and they fully agglomerate for low transport costs. In that case, the core produces the whole of the differentiated products and export these goods to the periphery whereas the periphery exports the good produced under constant returns to scale. In contrast with existing literature, agglomeration is explained by differences between wages of skilled and unskilled workers. Moreover, the model exhibits equilibria with partial agglomeration of firms for which we derive an explicit closed-form solution.

We also explore to what extend a change in the subsidy in one region affects welfare. We show that for low transport costs, a change in the subsidy has a minor impact on firms’ location. The incentive to compete on educational subsidies is low. In contrast, for larger transport costs, a change in the subsidy strongly affects firms’ location. In that case, local governments have a strong incentive to compete on educational subsidies: the government that affords the largest subsidy is in good position to attract firms and, through this way, improve welfare.
The paper is organized as follows. Section 2 presents the basic core-periphery model. Section 3 analyzes firms’ location. In that section, we start with a simple case in which both local governments set identical subsidies. Then we examine firms’ location when subsidies are differentiated. Finally we explore the issue of the optimal subsidy set by a local government. This is followed by the conclusions.

2 The Model

2.1 Consumption

The model builds on Dixit-Stiglitz (1977). Preferences are represented by a Cobb-Douglas function with a share $\mu \in (0, 1)$ of income spent on modern goods (the manufactured goods) and a share $1 - \mu$ spent on a traditional good that is produced under constant returns to scale (the agricultural good). The modern good is a composite made of a continuum of differentiated varieties $i \in [0, N]$. Preferences for these varieties are represented by a CES function with an elasticity of substitution equal to $\sigma > 1$. Accordingly, the demand for variety $i$ by households located in region $r$ is as follows:

$$C_r(i) = \frac{\mu Y_r}{P_r} \left[ \frac{\varsigma_r(i)}{P_r} \right]^{-\sigma} \quad i \in [0, N]$$

where

$$P_r \equiv \left[ \int_0^N \varsigma_r(i)^{-\sigma-1} di \right]^{-1/(\sigma-1)}$$

is the price index of the varieties sold in region $r$, $\varsigma_r(i)$ the price paid by a household living in region $r$ for one unit of variety $i$, and $Y_r$ the income available in region $r$.

The traditional good is traded at no cost, whereas the proportion $0 < \phi < 1$ of a single unit of each variety of the modern goods shipped from one region arrives in the other region (iceberg transport cost). Therefore, households residing in region $r$ buys the variety $i$ that is produced in their own region at the price $\varsigma_r(i)$, which is equal to the mill price $p_r(i)$. If variety $i$ is produced in the other region $s$, then the price paid by households equals the delivered price, which exceeds the mill price; $\varsigma_r(i) = p_s(i)/\phi > p_s(i)$.  

5
For notational convenience we define $\Phi \equiv \phi^{\sigma-1}$ which is an indicator of trade openness.

Accordingly, the price level of modern goods in region $r$ is

$$P_r = \left\{ \int_{0}^{n_r} p_r(i)^{-\sigma-1} \, di + \Phi \int_{n_r}^{N} p_s(i)^{-\sigma-1} \, di \right\}^{-1/(\sigma-1)}$$

where $n_r$ denotes the number of varieties produced in region $r$ (with $n_r + n_s = N$). Given (1), the demand for output of a firm $i$ that is established in region $r$ is

$$q_r(i) = \psi_r \left[ \frac{p_r(i)}{P_r} \right]^{-\sigma}$$

where

$$\psi_r \equiv \mu \left[ \frac{Y_r}{P_r} + \Phi \left( \frac{P_s}{P_r} \right)^{\sigma} \frac{Y_s}{P_s} \right]$$

is the total real income adjusted for transport costs.

### 2.2 Firms

The model is a variant of the footloose capital model developed by Martin and Rogers (1995). Each firm requires one unit of capital. There exists $N$ units of capital available worldwide. Accordingly, $N$ firms are active in the economy. Capital is mobile but their owners are immobile: they repatriate the revenues to the region where they live. In order to avoid initial conditions that favours one region, it is assumed that fifty percent of capital owners live in each region.

Each variety is produced by a single firm and the production of one unit of variety $i$ requires $\beta$ skilled workers; without loss of generality, we normalize $\beta = 1$ so that the number of units produced by a firm is equal to the number of workers it employs. Because firms from the modern industry have market power, they may earn profits. However they compete for the available units of capital so that all profits are distributed to capital owners.

Suppose that firm $i$ is located in region $r$. Its profits (gross of capital costs) are defined as follows

$$\pi_r(i) = [p_r(i) - w_r]q_r(i)$$
where $w_r$ is the wage prevailing in region $r$ whereas the demand $q_r(i)$ is given by (2). Since there is a continuum of firms in the modern industry, each of them is negligible and accurately considers the price index $P_r$ as given. The firm producing variety $i$ chooses its mill price to maximize its profits $\pi_r(i)$. As a result, all firms settled in region $r$ set the same equilibrium price given by:

$$p_r \equiv p_r(i) = \frac{\sigma}{\sigma - 1} w_r. \tag{4}$$

A firm $i$ producing in region $r$ has the following demand for labor:

$$l_r(i) = q_r(i) \equiv q_r = \psi_r \left[ \frac{\sigma}{\sigma - 1} \frac{w_r}{P_r} \right]^{-\sigma}. \tag{5}$$

Using (2), it is easy to show that the gross profits made by a firm located in region $r$ are such as

$$\pi_r = \frac{1}{\sigma} \left( \frac{\sigma}{\sigma - 1} \frac{w_r}{P_r} \right)^{1-\sigma} P_r \psi_r. \tag{6}$$

### 2.3 Labor

It is a stylized fact of European labor markets that workers are rather immobile between European countries and within each country (see e.g. Decressin and Fatás, 1995; Bentolila, 1997; Faini, Galli, Gennai and Rossi, 1997). To fit this European fact, we assume that workers cannot move across regions. This contrasts with Krugman (1991) who mainly focuses on the long-run behavior of workers in the United States.

Each region is populated by the same number of individuals, $\bar{L}$, who can work either in the traditional or in the modern sector. We assume that individuals are able to work in both sectors. However, to work in the modern sector, an individual has to invest in education, which reduces his/her leisure time. If $L_r$ persons have invested in education, the remaining $\bar{L} - L_r$ workers must be employed in the traditional sector. The traditional good is produced under constant returns to scale. One unit of the traditional good requires one unit of labor. Since the traditional good is the numeraire, wages are equal to one in this sector.

All individuals are a priori alike. The utility derived from leisure and consumption is supposed to be Cobb-Douglas: $(\text{Leisure})^\gamma * (\text{sub-utility from consumption})^{1-\gamma}$. 


By suitable transformations, this utility is equivalent to \((\text{Leisure})^{\gamma/(1-\gamma)}\) (sub-utility from consumption). Finally, set \((\text{Leisure})^{\gamma/(1-\gamma)} = 1\) for unskilled workers and \((\text{Leisure})^{\gamma/(1-\gamma)} = 1/(1+d)\) for skilled workers where \(d\) is some given positive constant. Given the preferences for the traditional good and the differentiated varieties, the utility derived from consumption is the real wage, that is, either \(1/P_r^G\) for unskilled workers living in region \(r\) or \(w_r/P_r^G\) for the skilled workers. The variable \(P_r^G\) denotes the general price index of both traditional and modern goods consumed in region \(r\).

For some individuals to work in the modern sector and others in the traditional sector, wages in the modern sector must compensate for the loss of utility:

\[
\frac{w_r}{1+d} = \frac{1}{P_r^G} \iff w_r = 1 + d
\]

Wages of skilled workers must be larger than wages of unskilled workers. By construction, the wage differential is constant.

In each region, a local government can help workers to become skilled by granting them a subsidy \(s_r\) aimed at reducing the costs of education. Thus, the revenue from being skilled is now \(w_r + s_r\) rather than \(w_r\). As a consequence, wages in region \(r\) are now

\[w_r = 1 + d - s_r\]

The net revenue of workers in the modern sector is therefore equal to \(w_r + s_r = 1 + d\). The subsidy granted to skilled workers is equivalent to a direct subsidy to firms per employee they hire. This is a consequence of the assumption that all individuals are alike. To avoid situations in which all workers in one region acquire skills, we assume that \(d - s_r \geq 0\).

In each region, the total earnings are \(Y_r = (\bar{L} - L_r) + L_r (1 + d) + \Pi/2 - T_r\), that is, they are respectively made of revenues of individuals working in the traditional sector, workers from the modern sector, half the total gross profits of both regions \(\Pi\), minus the taxes paid to finance the government, \(T_r\). Under balanced budget, \(T_r = s_r L_r\) and

\[Y_r = \bar{L} + L_r (d - s_r) + \frac{\Pi}{2}\]
3 Location Equilibrium

We assume that firms are myopic, that is, the driving force in firms’ location is firms’ current profit differential between \( r \) and \( s \), \( \Delta \pi(n_r) = \pi_r(i) - \pi_s(i) \):

\[
\frac{dn_r}{dt} = \begin{cases} 
\Delta \pi(n_r) & \text{if } 0 < n_r < 1 \\
\min \{0, \Delta \pi(n_r)\} & \text{if } n_r = N \\
\max \{0, \Delta \pi(n_r)\} & \text{if } n_r = 0
\end{cases}
\]

where \( t \) is time. This assumption is standard in the literature (see e.g. Fujita, Krugman and Venables, 1999; Ottaviano, Tabuchi and Thisse, 2002). A location equilibrium is interior \( (n_r^* \in (0, N)) \) if \( \Delta \pi(n_r^*) = 0 \); it is the corner \( n_r^* = 0 \) if \( \Delta \pi(0) \leq 0 \) and it is the corner \( n_r^* = N \) if \( \Delta \pi(N) \geq 0 \). A spatial location equilibrium is \textit{stable} if, for any marginal deviation from the equilibrium, the equation of motion brings the distribution of firms back to the original one. As a result, any interior location equilibrium is stable if and only if \( \Delta \pi \) is a decreasing function around \( n_r^* \). Any corner location is stable when it is an equilibrium.

In order to evaluate \( \Delta \pi(n_r) = (p_r - w_r) q_r - (p_s - w_s) q_s \), we need to compute prices and output. Since wages are constant, the mill prices (4) are equal to \( (1 + d - s_r) \sigma / (\sigma - 1) \). Hence, the profit differential between regions \( r \) and \( s \) becomes

\[
\pi_r - \pi_s = \frac{1 + d - s_r}{\sigma - 1} \left( q_r - \frac{1}{D} q_s \right) \quad \text{where} \quad D = \frac{1 + d - s_r}{1 + d - s_s} = \frac{w_r}{w_s}
\]

The determination of \( q_r \) is more complex. To find it, we need to compute the values of \( P_r \) and \( \psi_r \). In region \( r \), the consumption of one unit of good produced in that region costs \( (1 + d - s_r) \sigma / (\sigma - 1) \) whereas the consumption of one unit of good produced in the other region costs \( (1 + d - s_s) \sigma / \phi (\sigma - 1) \). Therefore, the regional price indices of goods in the modern sector can be written as

\[
P_r = \frac{\sigma}{\sigma - 1} (1 + d - s_r) (n_r + n_s \Phi D^{\sigma - 1}) \pi_r^{\frac{\sigma - 1}{\sigma}} \tag{7}
\]

Using (7), the expression of \( \psi_r \) can be simplified to

\[
\psi_r = \frac{\mu}{P_r} \left[ Y_r + \frac{n_r + n_s \Phi D^{\sigma - 1}}{n_s + n_r \Phi D^{1-\sigma}} \Phi D^{1-\sigma} Y_s \right] \tag{8}
\]
In the appendix we use (5), (7) and (8) to find expressions for \( Y_r, Y_s, q_r \) and \( q_s \).

We first develop a simple case where both regions are identical: \( s_r = s_s \). Then we examine two regions that set different subsidies. Finally we give some indications on the way the government of one region can improve the welfare in its own region by modifying the subsidy.

### 3.1 Identical regions

Under identical regions, \( s_s = s_r \), and \( D = 1 \). Using the values of \( q_r \) and \( q_s \) derived in the Appendix, it is readily checked that the profit differential becomes

\[
\pi_r - \pi_s = (N - 2n_r) K_2 \left( \Phi - \bar{\Phi} \right)
\]

where

\[
\bar{\Phi} \equiv \frac{\sigma (1 + d - s_r) - \mu (\sigma - 1) (d - s_r)}{\sigma (1 + d - s_r) + \mu (\sigma - 1) (d - s_r)}
\]

\[
K_2 \equiv -\mu K_A (1 - \Phi) \frac{\sigma (1 + d - s_r) + \mu (\sigma - 1) (d - s_r)}{1 + d - s_r} < 0
\]

and \( K_A \) is positive and defined in the Appendix. As the following proposition and Figure 1 indicate, the sole interior equilibrium is the symmetric equilibrium where \( n_r = N/2 \), and it is stable if and only if \( \Phi < \bar{\Phi} \).

---

![Graph](image)

**Figure 1:** Share of firms in region \( r \). Stable equilibria in plain and unstable in dash. \( \sigma = 5, \mu = .7, s_r = s_s = .01, d = .1 \), which gives \( \bar{\Phi} = 0.90 \).
Proposition 1 Symmetric location \((n_r = N/2)\) is the unique stable equilibrium if \(\Phi < \hat{\Phi}\). Agglomeration in one region is a stable equilibrium if \(\Phi > \hat{\Phi}\).

Proof. Stable equilibria are given by the behavior of \(\pi_r - \pi_s\). The equilibrium \(n_r = N/2\) is stable when \(\pi_r - \pi_s\) decreases with \(n_r\). Because \(K_2 < 0\), the equilibrium is stable if and only if \(\Phi < \hat{\Phi}\). There exist corner equilibria when the profit differential is positive at \(n_r = N\), and negative at \(n_r = 0\), that is, when \(\Phi > \hat{\Phi}\). ■

The location pattern results from the trade-off between two forces: product market competition and home market effect. To avoid tough competition, firms locate away from competitors. However, to benefit from the home market effect, they settle at the proximity of high-wage skilled workers, i.e., at the proximity of the other firms.

For large transport costs (low \(\Phi\)), the effect of product market competition dominates. Exports are negligible and firms produce for their domestic market. If domestic markets have equal sizes, firms locate where competition is the lowest, that is, in the region with the smallest number of firms. Hence, the location equilibrium is symmetric.

However, when the transport cost drops, firms can serve both markets and they suffer from competitors settled in both regions. Since it becomes more difficult to avoid competition, the main force driving firms’ location is the home market effect. The relocation of firms to a region induces more workers to become skilled in that region and fewer workers to become skilled in the other region. As a consequence, the number of high-wage skilled workers, the earnings and the product demand rise in the first region whereas they decrease in the other. Since firms are attracted towards the region with the larger demand, they tend to cluster in a single region. When the home market effect is larger than the competition effect (\(\Phi > \hat{\Phi}\)), agglomeration is the location equilibrium. Since globalization is characterized by decreasing transport costs, it leads to increased agglomeration.

Any factor that strengthens the home market effect fosters agglomeration of firms in a single region. A larger share of the modern goods in the
individual’s spending (larger $\mu$) increases the effect of the home market. Therefore, the set of economic parameters supporting symmetric location equilibria is smaller (the transport cost threshold $\hat{\Phi}$ decreases in $\mu$). In the same spirit, larger wages (via a larger cost of education $d$ or a lower subsidy $s_\tau$) increases the revenues of skilled workers in the modern industry and therefore strengthens the home market effect. Hence the value of $\hat{\Phi}$ is reduced. In contrast, when it is not costly to become skilled ($d - s_\tau = 0$), wages are equal for both types of workers and there is no interest to locate at the proximity of skilled workers anymore. The home market effect vanishes and the only equilibrium is the symmetric location of firms ($\hat{\Phi} = 1$).

Finally, and more surprisingly, a more elastic product demand ($\sigma$) promotes agglomeration. In Krugman, a more elastic product demand fosters symmetry. This result may seem intuitive: a more elastic demand means more competition between firms and a stronger incentive to avoid competition. Hence firms from the core prefer to settle away from competitors, which fosters a symmetric location of firms. As intuitive this explanation may seem, it is not satisfactory. Indeed, a rise in $\sigma$ increases competition in the core but also in the periphery where firms suffer from stronger competitions from firms established in the core. Hence it is not clear that firms effectively manage to avoid competition by settling in the periphery. The result of this section suggests that the impact of the demand elasticity on firms’ location is not straightforward.\footnote{The result also contrats with Picard and Toulemonde (2002) despite the closeness of the two models. The main difference lies in the wage determination. In Picard and Toulemonde (2002), wages decrease when goods become closer substitute because the rent that is shared between firms and unions is smaller. The decrease in wages reduces the agglomeration force and induces firms to locate more symmetrically; this force does not exist in the present model where wages are independent of $\sigma$.}

Note that the threshold $\hat{\Phi}$ does not depend on fixed costs, $f$. Hence, increasing returns to scale are not a necessary condition for agglomeration when the number of varieties is fixed. See Picard, Thisse and Toulemonde (2002) for a detailed analysis of the role of increasing returns to scale and profit distribution in economic geography models.
3.2 Different regions

Let us now examine the case in which both regions set different subsidies. Without loss of generality, we assume that \( s_s > s_r \), which implies that wages are larger in region \( r \) and \( D > 1 \). As shown in the appendix, the profit differential can be written as

\[
\pi_r - \pi_s = \mu K_A D^r \left( -\text{Den} \ast n_r + \text{Num} \right)
\]

where

\[
\text{Den} = \left\{ 2\sigma + \mu Z_r [D (d - s_s) + (d - s_r)] \right\} \Phi^2 - 2\sigma D^{1-r} \left[ 1 + D^{2(1-r)} \right] \Phi + 2\sigma - \mu Z_r [D (d - s_s) + (d - s_r)]
\]

\[
\text{Num} = N \left\{ [\sigma + \mu Z_r D (d - s_s)] \Phi^2 - 2\sigma D^{1-r} \Phi + \sigma - \mu Z_r D (d - s_s) \right\}
\]

For an interior equilibrium, \( \pi_r - \pi_s = 0 \), which requires \( n^*_r = \text{Num}/\text{Den} \). We analyze this expression in the appendix where we first prove that the numerator only has one root in \( \Phi \) on the relevant domain \( \Phi \in [0,1] \). We then prove the same result for the denominator. Numerical simulations indicate that the root of the numerator is always smaller than the root of the denominator. Moreover, at \( \Phi = 0 \), \( n^*_r > N/2 \).

As illustrated in Figure 2, the function \( n^*_r \) starts above \( N/2 \) (slightly above \( N/2 \) for the parameters chosen to draw the figure), it decreases to zero (the root of the numerator) and then has a vertical asymptote at the root of the denominator (the asymptote is not drawn in the figure). After the asymptote, \( n^*_r \) tends to the infinity and decreases; depending on parameters, it may fall below \( N \) (the dash curve in panel b of the figure) or not (panel a of the figure). However it always stays larger than 0.

The interior equilibrium is stable if and only if the derivative of \( \pi_r - \pi_s \) with respect to \( n_r \) is negative at the equilibrium, i.e., if and only if Den is positive. Den is positive at the left of the vertical asymptote and negative at the right. Hence, if it exists, the interior equilibrium is stable at the left of the asymptote and unstable at the right of it. Depending on the agglomeration force, an unstable interior equilibrium may exist: in the left panel, it does not exist for \( \sigma = 5 \), \( \mu = 0.7 \), \( s_r = 0 \), \( s_s = .01 \) and \( d = 0.1 \) whereas it exists for the same values of parameters and \( d = 1 \).
Figure 2 a: Share of firms in region r. Stable equilibria in plain and unstable in dash. \( \sigma = 5, \mu = .7, s_s = .01, s_r = 0, d = .1 \).

Figure 2 b: Share of firms in region r. Stable equilibria in plain and unstable in dash. \( \sigma = 5, \mu = .7, s_s = .01, s_r = 0, d = 1 \).

By continuity of the profit differential function, agglomeration cannot be stable when the (sole) interior equilibrium is stable. Indeed, the function decreases when it is equal to zero and must therefore be negative in case of agglomeration in region \( r \) and positive in case of agglomeration in the other region. By the same argument, agglomeration in either region \( r \) or region \( s \)
is stable if there exists an unstable interior equilibrium. Finally, when there exists no stable interior equilibrium (that is, when \( n_r^* > N \) or \( n_r^* < 0 \), the profit differential is negative and the only equilibrium is agglomeration in region \( s \). Stable location equilibria are depicted by the bold curves in the figure; unstable are depicted by the dash curves.

The location pattern results from the trade-off between three forces: product market competition, wage differential effect and home market effect. Product market competition induces firms to settle away from each other, that is, to spread evenly across regions. To reduce their costs, firms prefer the region with the lowest wages; this is the wage differential effect. However, they also prefer the region where the demand is the highest. Since the demand is positively related to wages, they are attracted to the region where wages are higher. They are also attracted towards the region where most firms are located. This is the home market effect.

To illustrate the interaction of these three forces, assume that the subsidy in region \( r \) is set to 0 and is positive in region \( s \). At prohibitive transport costs (\( \Phi = 0 \)), it is not possible to export the production. Therefore, by spreading across regions, firms effectively manage to avoid competition from firms established in the other region. Product market competition is the leading force. Costs are lower in region \( s \) because education is subsidized there. However the home market effect also plays a role. Suppose that there is the same number of skilled workers (\( \hat{L} \)) in both regions. In region \( r \), earnings are \( \hat{L} + \hat{L}d + \Pi/2 \) whereas they are \( \hat{L} + \hat{L}d - \hat{L}s + \Pi/2 \). That is, earnings are lower in region \( s \) because of the taxes paid to finance education. Since transport costs are prohibitive, it is not possible for a firm to settle in the low cost region and export to the high demand region. To match the large demand, more than 50 percent of firms settle in region \( r \), which is the high wage region (\( n_r^* > N/2 \)). In the simulations, we set \( \sigma = 5 \) and \( \mu = 0.7 \) and we fix low values for the cost of education (\( d = 0.1 \)) and for the subsidy in region \( s \) (\( s = 0.01 \)). We use low values for \( d \) and \( s \) in order to depart as little as possible from a more standard model with no subsidy and in which it is not costly to become skilled. Under these values at most 50.3% of firms
settle in the high wage region (when $s_r = 0$). Once we increase the cost of education ($d = 1$) and the subsidy set in region $s$ ($s_s = 1$, which reduces wages in region $s$), up to 91% of firms may settle in the high wage region $r$. More generally, the larger is the difference between subsidies in the two regions ($s_s - s_r$) and the more costly it is to become skilled, the larger is the wage differential and the home market effect: more firms settle in the high wage region.

When the foreign region becomes accessible (through a reduction in transport costs), product market competition becomes less influential because it is more difficult to avoid competition by changing location. In contrast, it becomes possible to benefit from low wages in region $s$ and at the same time to serve the large market $r$. It is therefore less attractive to settle in region $r$: partial agglomeration in that region is reduced and even vanishes at some threshold value of the transport costs: the benefit from low costs outweighs the advantage of settling in the large wage region; partial agglomeration now occurs in region $s$.

Globalization weakens the relative influence of product market competition and exacerbates the effect of costs differences on firms location: as $\Phi$ is increased, partial agglomeration is fostered in the region with the lowest wages. As region $s$ hosts more firms, it also increases its wage bill, which fosters the demand coming from that region. The home market effect now favors the high subsidy region because the number of high wage skilled workers is larger there. This contributes to accelerate agglomeration in the low wage region until complete agglomeration in that region.

For low transport costs, the market competition force becomes so weak that it is dominated by the two other forces. If the home market effect is weak (low value of the cost of education $d$), the wage differential remains the leading force and agglomeration in the low wage region is the only stable equilibrium. In contrast, if the home market effect is stronger (large $d$), agglomeration in the high wage region becomes feasible: if all firms are located there, the demand becomes so high that firms do not want to settle in the low wage region. This situation is similar to the context of tax competition.
analyzed by Ludema and Wooton (2000) and by Kind, Midelfart Knarvik and Schjelderup (2000): they show that there may be agglomeration in a region with higher taxes because firms earn higher profits when they are located near a large agglomeration of firms. Since their only alternative is to settle in a region without a concentration of firms, the core region may extract some of the agglomeration rent through higher taxes without losing firms (see also Baldwin et al., 2003). In our context, taxes are replaced with subsidies to education. If there is agglomeration of firms in the core, the core region can extract some of the agglomeration rent through higher wages (via lower subsidies). However when the transport cost vanishes (Φ close to 1), the home market effect also disappears because it is possible for all firms to serve both markets at no extra cost. Therefore, firms agglomerate in the low wage (high subsidy) region.

In line with the literature, these results confirm that globalization induces more agglomeration; as a complement to the literature, agglomeration increases smoothly in our setting, which is more realistic than the sudden jumps emphasized in most existing models. In contrast to the literature, for a given set of parameters, we do not have interior equilibria coexisting with complete agglomeration.

3.3 Optimal subsidies

In this section we examine the incentives of a regional government to use education subsidies in order to increase regional welfare. Unfortunately there does not exist a simple measure of welfare with the CES utility function when agents receive different earnings. In particular, the utilitarian approach is difficult to justify because skilled workers, unskilled workers and capital owners have different incomes, hence a different marginal utility for the numeraire (see Ottaviano, Tabuchi and Thisse, 2002, and Charlot et al., 2003). Therefore we limit the analysis to the identification of several incentives to use subsidies.

We do not examine here the case in which full agglomeration emerges as
an equilibrium\textsuperscript{4}; we rather restrict ourselves to partially asymmetric equilibria\textsuperscript{5}. Doing so, we are able to examine the impact of subsidies when changes of firms’ location is not catastrophic.

A change in the subsidy set by region $r$ has three effects. A direct impact on nominal earnings, another on the price level, and an indirect impact on these two variables through variations in the firms’ location. The direct effect of subsidies on the price level is straightforward: they reduce the costs, and by this way the price set by each firm and the general price level. Hence, through this effect, subsidies increase welfare. Simulations suggest that is effect is limited. By contrast, the direct effect through earnings is stronger. An increase in subsidies in region $r$ has three effects on earnings. First, it reduces wages in that region but leaves net revenues of skilled workers unchanged ($w_r + s_r = 1 + d$). Second, it raises the taxes necessary to finance subsidies, which reduces nominal earnings. Third, it decreases the costs, which increases profits and thus earnings. Simulations show that the net effect of an increase in subsidies is to decrease nominal earnings, which worsens welfare.

The two preceding direct effects are standard to any model using a CES utility. The novelty in this paper is the analysis of firms’ location in such a model. How does the partition of firms between both regions affect welfare? Everything else equal, an increase in the number of firms in region $r$ raises the earnings and reduces the price level in that region: more high wage skilled workers are employed in that region and more goods are produced locally and do not have to be imported from the other region. An increase in $n_r$ is therefore good for welfare.

Let us now examine to what extent an increase in the subsidy in region $r$ affects firms’ location, $n_r$. An increase in the subsidy in region $r$ reduces wages in that region. We have seen that for prohibitive transport costs, firms are attracted towards the region with larger wages (larger demand). Hence, regional government should decrease subsidies when transport costs

\textsuperscript{4}See Ludema and Wooton (2000) for this kind of analysis in a tax competition framework.

\textsuperscript{5}Thus, $\Phi$ must be small enough to prevent full agglomeration.
are prohibitive. However simulations suggest that this effect is weak and limited to a small domain of $\Phi$. This is represented by the dot-dot-dash curve in Figure 3.

![Figure 3: share of firms in region $r$ as a function of $s_r$, when $\Phi = 0$ (dash), $\Phi = 0.3$ (dot-dash), $\Phi = 0.5$ (plain) and $\Phi = 0.6$ (dash). Parameters are $\sigma = 5$, $\mu = .7$, $d = .1$, $s_s = .01$.

This figure is drawn for a subsidy in region $s$ set to .01 and under the assumption that the regional government in $r$ sets a lower subsidy. It is clear from the figure that firms’ location does not strongly respond to subsidies in that case. For larger transport costs, firms are attracted towards the region where wages are the lowest. There is thus an incentive to use subsidies to reduce wages. This is represented by the other curves in the figure: an increase in the subsidy in region $r$ raises the share of firms in that region, until both subsidies are equalized and both regions host fifty percent of firms (when $s_r = s_s = .01$). If one only takes this effect into account, one can conclude that there is a risk of a “subsidy competition”: both regions raise subsidies to attract the firms that are located in the other region. The incentive to use subsidies raises with globalization: the figure shows that the smaller are transport costs, the stronger is the re-allocation of firms following a change in subsidies. Therefore, we can expect that globalization (a reduction in the transport cost) exacerbates the incentive to use subsidies
to attract firms and increase the local welfare. The room for a “subsidy competition” is stronger when transport costs are lower. This effect was observed for all of the numerous simulations we made.

4 Conclusions

This paper develops an analytically solvable model of the new economic geography that exhibits a core-periphery structure. Workers who invest in education earn larger wages than workers who remain unskilled. Firms want to locate their production in regions where the demand for their product is large in order to save on transport costs. The size of the demand in a region depends on the numbers of workers who have invested in education and earn large wages relative to the number of workers who remain unskilled and earn low wages. Hence firms want to settle at the proximity of high-wage skilled workers. In addition, workers are eager to invest in education when more firms ask for skilled workers in their own region. Therefore, if firms relocate in a region, more workers from that region are induced to become skilled. In turn, this raises the demand in that region and reinforce the movement of firms to that region. This circular causality implies that for low transport costs, firms agglomerate in a core region. In contrast they partially agglomerate in one region for intermediate and high transport costs. The region that benefits from this partial agglomeration is the low subsidy region when transport costs are prohibitive, whereas it is the high subsidy region when transport costs are intermediate.

The incentive to use education subsidies to attract firms in a region therefore highly depends on the level of transport costs. Globalization, measured as a reduction in transport costs, increases this incentive and may well create a “subsidy competition” in which local governments compete to promote skill acquisition in their own region.

Interestingly, the model allows to derive an explicit closed-form solution, even when agglomeration is partial. This analytical tractability could therefore prove useful to analyze other policy implications of a economic geography models.
5 References


6 Appendix

**Determination of** $Y_r$, $Y_s$, $q_r$ and $q_s$. In each region total profits are equal to the value of production minus labor and fixed costs, $n_r\pi_r = n_r(p_r - w_r)q_r - n_rf$. Hence,

$$\begin{align*}
Y_r &= \bar{L} + L_r(d - s_r) + \frac{\Pi}{2} = \bar{L} - \frac{Nf}{2} + (d - s_r)n_rq_r + \frac{1 + d - s_r}{\sigma - 1} n_rq_r + n_sq_sD^{-1}
\end{align*}$$

$$\begin{align*}
Y_s &= \bar{L} + L_s(d - s_s) + \frac{\Pi}{2} = \bar{L} - \frac{Nf}{2} + (d - s_s)n_sq_s + \frac{1 + d - s_r}{\sigma - 1} n_rq_r + n_sq_sD^{-1}
\end{align*}$$

Earnings ($Y_r$ and $Y_s$) are function of output ($q_r$ and $q_s$). Using (5), (7) and (8), we find other relations between output and earnings:

$$\begin{align*}
q_r &= \frac{\mu}{1 + d - s_r} \frac{\sigma - 1}{\sigma} \left( \frac{Y_r}{n_r + n_s \Phi D^{\sigma - 1}} + \frac{Y_s}{n_s + n_r \Phi D^{\sigma - 1}} \Phi D^{1 - \sigma} \right)
\end{align*}$$

$$\begin{align*}
q_s &= \frac{\mu}{1 + d - s_s} \frac{\sigma - 1}{\sigma} \left( \frac{Y_s}{n_s + n_r \Phi D^{\sigma - 1}} + \frac{Y_r}{n_r + n_s \Phi D^{\sigma - 1}} \Phi D^{1 - \sigma} \right)
\end{align*}$$

Solving the four expressions with four unknowns allows to get $q_r$, $q_s$, $Y_r$ and $Y_s$:

$$\begin{align*}
q_r &= \mu Z_r K_A \left[ \sigma D^\sigma \left( \Phi D^{1 - \sigma} A_r + A_s \right) - \mu Z_r D^{\sigma + 1} n_s (d - s_s) (1 - \Phi^2) \right]
\end{align*}$$

$$\begin{align*}
q_s &= \mu Z_r K_A \left[ \sigma D^{\sigma + 1} \left( \Phi D^{\sigma - 1} A_r + A_s \right) - \mu Z_r D^{\sigma + 1} n_r (d - s_r) (1 - \Phi^2) \right]
\end{align*}$$

$$\begin{align*}
Y_r &= \sigma A_r K_A \left\{ \mu Z_r \left[ \Phi D n_r (d - s_r) - D^{\sigma + 1} n_s (d - s_s) \right] + \sigma A_s D^{\sigma} \right\}
\end{align*}$$

$$\begin{align*}
Y_s &= \sigma A_s K_A \left\{ \mu Z_r \left[ \Phi D^{\sigma + 1} n_s (d - s_s) - D^{\sigma} n_r (d - s_r) \right] + \sigma A_r D^{\sigma} \right\}
\end{align*}$$

where

$$Z_r \equiv \frac{\sigma - 1}{1 + d - s_r}, \quad A_r \equiv n_r + n_s \Phi D^{\sigma - 1}, \quad A_s \equiv n_s + n_r \Phi D^{1 - \sigma}$$

and

$$K_A \equiv \frac{D^{-\sigma} (2L - Nf)}{2\sigma(\sigma - \mu) A_r A_s - 2\sigma^2 Z_r [(d - s_r)n_r A_s + (d - s_s) D n_r A_r] + \mu^2 Z_s n_s n_r (1 - \Phi^2) [2D Z_r (d - s_s) + D (d - s_s) + (d - s_r)]}$$

It can be shown that $K_A$ is positive. The proof is tedious and available from the author.
**Different regions**  Without loss of generality, we assume that $s_s > s_r$, which implies that wages are larger in region $r$ and $D > 1$. Using the values of $q_r$ and $q_s$ from the preceding appendix, we can write the profit as

$$\pi_r - \pi_s = \mu K A D^r \ast \left\{ \sigma \left[ A_s (1 - D^{r-1} \Phi) - (1 - D^{1-s} \Phi) A_r \right] - \mu Z_r (1 - \Phi^2) \left[ Dn_r (d - s_s) - n_r (d - s_r) \right] \right\}$$

Using the definitions of $A_r$, $A_s$ and $n_s = N - n_r$, we have

$$\pi_r - \pi_s = \mu K A D^r (\text{Den} \ast n_r + \text{Num})$$

where

$$\text{Den} = \{2\sigma + \mu Z_r [D (d - s_s) + (d - s_r)]\} \Phi^2$$

$$-2\sigma D^{r-1} \left[1 + D^{2(1-\sigma)}\right] \Phi + 2\sigma - \mu Z_r [D (d - s_s) + (d - s_r)]$$

$$\text{Num} = N \{[\sigma + \mu Z_r D (d - s_s)] \Phi^2 - 2\sigma D^{r-1} \Phi + \sigma - \mu Z_r D (d - s_s)\}$$

For an interior equilibrium, $\pi_r - \pi_s = 0$, which requires $n_r^* = \text{Num}/\text{Den}$. We first prove that the numerator only has one and only one root in $\Phi$ on the relevant domain $\Phi \in [0, 1]$. We then prove the same result for the denominator and we combine both results to analyze the fraction $n_r^*$.

**The numerator**

- The numerator is a square expression of $\Phi$; it has two roots in $\Phi$:

  $$\Phi = \frac{D^{\sigma-1} \sigma \pm \sqrt{\sigma^2 \left[D^{2(\sigma-1)} - 1\right] + \mu^2 Z_r^2 D^2 (d - s_s)^2}}{\sigma + \mu Z_r D (d - s_s)}$$

- The largest root is larger than 1 because the first term in the numerator is larger than the first term in the denominator ($D^{\sigma-1} \sigma > \sigma$) and the second term in the numerator is larger than the second term in the denominator ($\sqrt{\sigma^2 \left[D^{2(\sigma-1)} - 1\right] + \mu^2 Z_r^2 D^2 (d - s_s)^2} > \mu Z_r D (d - s_s)$).

  The largest root is therefore outside the domain of $\Phi$.

- The smallest root is positive because the square of the first term in the numerator minus the expression under the square root is positive.
Indeed, using the definitions of $Z_r$ and $D$, we get

$$D^{2(\sigma-1)} \sigma^2 - \sigma^2 \left[D^{2(\sigma-1)} - 1\right] - \mu^2 \left(\frac{\sigma - 1}{1 + d - s_s}\right)^2 (d - s_s)^2$$

$$= \sigma^2 - \mu^2 (\sigma - 1)^2 \left(\frac{d - s_s}{1 + d - s_s}\right)^2 > 0$$

- The smallest root is also smaller than 1. Indeed, rearranging, it is readily checked that this root is smaller than 1 if and only if

$$\sigma \left(D^\sigma - 1\right) - \mu Z_r D (d - s_s) < \sqrt{\sigma^2 \left(D^{2(\sigma-1)} - 1\right) + \mu^2 Z_r^2 D^2 (d - s_s)^2},$$

$$\Leftrightarrow -2\sigma \left(D^\sigma - 1\right) \left(\sigma + \mu Z_r D (d - s_s)\right) < 0$$

which holds because $D \geq 1$.

Therefore, the numerator changes its sign at most once on the relevant values of $\Phi$. At $\Phi = 1$, it is equal to $-2\sigma N \left(D^\sigma - 1\right) < 0$. So the numerator is negative for large $\Phi$ and positive for low $\Phi$.

**The denominator**

- The denominator is a square expression of $\Phi$; it has two roots in $\Phi$:

$$D^{\sigma-1} \sigma \left[D^{2(1-\sigma)} - 1 + D^{2(1-\sigma)} \right] \pm \sqrt{D^{\sigma-1} \sigma^2 \left[1 + D^{2(1-\sigma)}\right]^4 - 4\sigma^2 + \mu^2 Z_r^2 [D(d-s_s) + (d-s_r)]^2}$$

$$2\sigma + \mu Z_r [D(d-s_s) + (d-s_r)]$$

- The largest root is larger than one. To see this, note that the expression under the square root can be written as

$$\sigma^2 \left(D^{2(\sigma-1)} \left[1 + D^{2(1-\sigma)}\right]^2 - 4\right) + \mu^2 Z_r^2 [D(d-s_s) + (d-s_r)]^2$$

First note that under $D \geq 1$, the first brackets is positive. Indeed, it is positive if and only if $D^{\sigma-1} \left[1 + D^{2(1-\sigma)}\right] - 2 > 0$, which always holds under $D \geq 1$. Hence, the expression under the square root of $\Phi$ is at least equal to $\mu^2 Z_r^2 [D(d-s_s) + (d-s_r)]^2$. Assume that it is equal to that value. Then, the largest root of $\Phi$ becomes

$$\Phi = \frac{D^{\sigma-1} \sigma \left[1 + D^{2(1-\sigma)}\right] + \mu Z_r [D(d-s_s) + (d-s_r)]}{2\sigma + \mu Z_r [D(d-s_s) + (d-s_r)]}$$

25
Since the first term in the numerator is larger than the first term in the denominator (we have just checked above that \( D^{\sigma - 1} \left( 1 + D^{2(1-\sigma)} \right) - 2 > 0 \)) and the second term in the numerator is equal to that in the denominator, this root is larger than 1.

- The smallest root takes its largest value for \( \mu = 0 \), which gives
  \[
  \Phi = \frac{D^{\sigma - 1} \left[ 1 + D^{2(1-\sigma)} \right] - \sqrt{D^{2(\sigma - 1)} \left[ 1 + D^{2(1-\sigma)} \right]^2 - 4}}{2}.
  \]

It is readily checked that this expression is smaller than one if and only if \( D^{\sigma - 1} \left[ 1 + D^{2(1-\sigma)} \right] - 2 > 0 \), which always holds under \( D \geq 1 \) (see above). Hence, the smallest root is always smaller than 1.

- Now we prove that the smallest root is always positive. To do that, it suffices to prove that the last two terms under the square root are negative (the first term under the square root is the square of the term outside the square root). These two terms are negative if and only if
  \[-2\sigma + \mu Z_r \left[ D (d - s_s) + (d - s_r) \right] < 0.\]
  Using the definitions of \( Z_r \) and \( D \), this amounts to
  \[
  (\sigma - 1) \mu \left( \frac{d - s_s}{1 + d - s_s} + \frac{d - s_r}{1 + d - s_r} \right) - 2\sigma < 0 \quad (9)
  \]
  Since \( (d - s_r) / (1 + d - s_s) < 1 \) and \( (d - s_s) / (1 + d - s_s) < 1 \), this expression is at most equal to \( 2 (\sigma - 1) \mu - 2\sigma \) which is always negative.

Therefore, the denominator changes its sign once on the relevant values of \( \Phi \). At \( \Phi = 1 \), it is equal to \( 2\sigma \left\{ 2 - D^{\sigma - 1} \left[ 1 + D^{2(1-\sigma)} \right] \right\} < 0 \). So the denominator is negative for large \( \Phi \) and positive for low \( \Phi \).

**The fraction** \( n_r^* \)  It was not possible to prove analytically that the root of the denominator is always larger than the root of the numerator. However, all of the numerous numerical simulations that were done show that this property holds.

At \( \Phi = 0 \), \( n_r^* \) is positive and larger than \( N/2 \)

**Proof.** At \( \Phi = 0 \),
\[
 n_r^* = \frac{N}{2} \frac{2\sigma - 2\mu Z_r D (d - s_s)}{2\sigma - \mu Z_r \left[ D (d - s_s) + (d - s_r) \right]}
\]
The numerator is larger than the denominator because $2\mu Z_r D (d - s_s) < \mu Z_r [D (d - s_s) + (d - s_r)]$ if and only if $D (d - s_s) < (d - s_r)$ which always holds under $s_r < s_s$. For $n_r$ to be positive, it is necessary that the denominator be positive. Using the definitions of $Z_r$ and $D$, it is readily checked that the denominator is positive if and only if (9) holds, which is always correct. ■
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<th>No.</th>
<th>Author(s)</th>
<th>Title</th>
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<tr>
<td>925</td>
<td>A. P. Damm</td>
<td>Employment Effects of Dispersal Policies on Refugee Immigrants, Part II: Empirical Evidence</td>
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<td>11/03</td>
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<td>926</td>
<td>S. E. Black</td>
<td>Why the Apple Doesn’t Fall Far: Understanding Intergenerational Transmission of Human Capital</td>
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<td>L. Goette</td>
<td>Loss Aversion and Labor Supply</td>
<td>5</td>
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<td>928</td>
<td>H. Selod</td>
<td>Does City Structure Affect the Labor-Market Outcomes of Black Workers?</td>
<td>3</td>
<td>11/03</td>
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<td>Y. Zenou</td>
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<tr>
<td>929</td>
<td>Z. Eckstein</td>
<td>Empirical Labor Search: A Survey</td>
<td>1</td>
<td>11/03</td>
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<tr>
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<td>M. Lindeboom</td>
<td>Individual Mortality and Macro Economic Conditions from Birth to Death</td>
<td>3</td>
<td>11/03</td>
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<td>931</td>
<td>P. Kooreman</td>
<td>Time, Money, Peers, and Parents: Some Data and Theories on Teenage Behavior</td>
<td>5</td>
<td>11/03</td>
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<td>932</td>
<td>H. N. Mocan</td>
<td>Guns, Drugs and Juvenile Crime: Evidence from a Panel of Siblings and Twins</td>
<td>3</td>
<td>11/03</td>
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<td>W. Arulampalam</td>
<td>Training in Europe</td>
<td>5</td>
<td>11/03</td>
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<td>934</td>
<td>M. Piva</td>
<td>The Skill Bias Effect of Technological and Organisational Change: Evidence and Policy Implications</td>
<td>5</td>
<td>11/03</td>
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<td>935</td>
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