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Article

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Journal of Industrial Engineering and Management (JIEM)

Provided in Cooperation with:

The School of Industrial, Aerospace and Audiovisual Engineering of Terrassa (ESEIAAT), Universitat Politècnica de Catalunya (UPC)

Suggested Citation: Mishra, Vinod Kumar (2013): An inventory model of instantaneous deteriorating items with controllable deterioration rate for time dependent demand and holding cost, Journal of Industrial Engineering and Management (JIEM), ISSN 2013-0953, OmniaScience, Barcelona, Vol. 6, Iss. 2, pp. 496-506,

https://doi.org/10.3926/jiem.530

This Version is available at: https://hdl.handle.net/10419/188541

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JIEM, 2013 - 6(2): 495-506 - Online ISSN: 2013-0953 - Print ISSN: 2013-8423

http://dx.doi.org/10.3926/jiem.530

An inventory model of instantaneous deteriorating items

with controllable deterioration rate for time dependent demand

and holding cost

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Received: August 2012 Accepted: March 2013

A bstract:

Purpose The purpose of this paper to develop an inventory model for instantaneous

deteriorating items with the consideration of the facts that the deterioration rate can be

controlled by using the preservation technology (PT) and the holding cost & demand rate both

are linear function of time which was treated as constant in most of the deteriorating inventory

model.

Design/methodology/approadr Developed the mathematical equation of deterministic deteriorating

inventory model in which demand rate and holding cost both is linear function of time,

deterioration rate is constant, backlogging rate is variable and depend on the length of the next

replenishment, shortages are allowed and partially backlogged and obtain an analytical solution

which optimizes the total cost of the proposed inventory model.

Findings: The model can be applied for optimizing the total inventory cost of deteriorating items

inventory for such business enterprises where they use the preservation technology to control

the deterioration rate under other assumptions of the model.

Originality/value: The inventory system for deteriorating items has been an object of study for a

long time, but little is known about the effect of investing in reducing the rate of product

deterioration and their significant impact in the business. The proposed model is effective as

-495-

well as efficient for the business organization that uses the preservation technology to reduce the deterioration rate of the instantaneous deteriorating items of the inventory.

Keywords inventory, deteriorating items, shortages, controllable deterioration rate, partial backlogging, preservation technology, time dependent holding cost

1. Introduction

Inventory System is one of the main stream of the Operations Research which is essential in business enterprises and Industries. Interest in the subject is constantly increasing, and its development in recent years closely parallels the development of operations research in general. Some authors even claim that "More operations research has been directed towards inventory control than toward any other problem area in business and industry" and among these the deteriorating items inventory have gain large emphasis in last decade. The inventory system for deteriorating items has been an object of study for a long time, but little is known about the effect of investing in reducing the rate of product deterioration. So in this paper, an inventory model is developed to consider the fact that the uses of preservation technology reduce the deterioration rate by which the retailer can reduce the economic losses, improve the customer service level and increase business competitiveness.

Inventory of deteriorating items first studied by Within (1957), he considered the deterioration of fashion goods at the end of prescribed storage period. Ghare and Schrader (1963) extended the classical EOQ formula with exponential decay of inventory due to deterioration and gave a mathematical model of inventory of deteriorating items. Dave and Patel (1981) developed the first deteriorating inventory model with linear trend in demand. He considered demand as a linear function of time. Goyal and Giri (2001) gave recent trends of modeling in deteriorating items inventory. They classified inventory models on the basis of demand variations and various other conditions or constraints. Ouyang, Wu and Cheng (2005) developed an inventory model for deteriorating items with exponential declining demand and partial backlogging. Alamri and Balkhi (2007) studied the effects of learning and forgetting on the optimal production lot size for deteriorating items with time varying demand and deterioration rates. Dye and Ouyang (2007) found an optimal selling price and lot size with a varying rate of deterioration and exponential partial backlogging. They assume that a fraction of customers who backlog their orders increases exponentially as the waiting time for the next replenishment decreases.

In (2008) Roy Ajanta developed a deterministic inventory model when the deterioration rate is time proportional, demand rate is function of selling price and holding cost is time dependent. Skouri, Konstantaras, Papachristos and Ganas (2009) developed an Inventory

models with ramp type demand rate, partial backlogging and Weibell's deterioration rate. Hsu, Wee and Teng (2010) develop a deteriorating inventory policy when the retailer invests on the preservation technology to reduce the rate of product deterioration. Mishra and Singh (2010) developed a deteriorating inventory model with partial backlogging when demand and deterioration rate is constant. They made Abad (1996, 2001) more realistic and applicable in practice. He, Wang and Lai (2010) gave an optimal production inventory model for deteriorating item with multiple market demand. Mandal (2010) gave an EOQ inventory model for Weibull distributed deteriorating items under ramp type demand and shortages. Chang, Teng and Goyal (2010) gave optimal replenishment policy for non instantaneous deteriorating items with stock dependent demand. Dye and Ouyang (2011) Studied a deteriorating inventory system with fluctuating demand and trade credit financing and establish a deterministic economic order quantity model for a retailer to determine its optimal selling price, replenishment number and replenishment schedule with fluctuating demand under two levels of trade credit policy. Hung (2011) gave an inventory model with generalized type demand, deterioration and backorder rates. Mishra and Singh (2011) developed deteriorating inventory model for time dependent demand and holding cost with partial backlogging. Leea and Dye (2012) formulate a deteriorating inventory model with stock-dependent demand by allowing preservation technology cost as a decision variable in conjunction with replacement policy. Maihami and Kamalabadi (2012) developed a joint pricing and inventory control system for non-instantaneous deteriorating items and adopt a price and time dependent demand function.

The deterioration rate of items in the above mentioned papers is viewed as an exogenous variable, which is not subject to control. In practice, the deterioration rate of products can be controlled and reduced through various efforts such as procedural changes and specialized equipment acquisition. The consideration of PT is important due to rapid social changes and the fact that PT can reduce the deterioration rate significantly. By the efforts of investing in preservation technology we can reduce the deterioration rate. So in this paper, we made the model of Mishra and Singh (2011) more realistic by considering the fact that the use preservation technology can reduce the deterioration rate significantly which help the retailers to reduce their economic losses.

The assumptions and notations of the model are introduced in the next section. The mathematical model and solution procedure is derived in section 3 and numerical and graphical analysis is presented in section 4. The article ends with some concluding remarks and scope of future research.

2. Assumption and Notations

The mathematical model is based on the following notations and assumptions.

2.1. Notations

- A the ordering cost per order.
- C the purchase cost per unit.
- h(t) the inventory holding cost per unit per time unit.
- π_b the backordered cost per unit short per time unit.
- π_1 the cost of lost sales per unit.
- ξ preservation technology (PT) cost for reducing deterioration rate in order to preserve the product, $\xi > 0$.
- θ the deterioration rate.
- $m(\xi)$ reduced deterioration rate due to use of preservation technology.
- τ_p resultant deterioration rate, $\tau_p = (\theta m(\xi))$.
- t_1 the time at which the inventory level reaches zero, $t_1 \ge 0$.
- t_2 the length of period during which shortages are allowed, $t_2 \ge 0$.
- T $(= t_1 + t_2)$ the length of cycle time.
- IM the maximum inventory level during [0, T].
- IB the maximum inventory level during shortage period.
- Q (= IM + IB) the order quantity during a cycle of length T.
- $I_1(t)$ the level of positive inventory at time t, $0 \le t \le t_1$.
- $I_2(t)$ the level of negative inventory at time t, $t_1 \le t \le t_1 + t_2$.
- TC (t₁,t₂ξ) the total cost per time unit.

2.2. Assumptions

- The demand rate is time dependent that is if 'a' is fix fraction of demand and 'b' is that fraction of demand which is vary with time then demand function is f(t) = a + bt, where a>0, b>0.
- Preservation technology is used for controlling the deterioration rate.
- Holding cost is linear function of time $h(t) = \alpha + \beta t$, $\alpha \ge 0, \beta \ge 0$.
- Shortages are allowed and partially backlogged.

- The lead time is zero.
- The replenishment rate is infinite.
- · The planning horizon is finite.
- · The deterioration rate is constant.
- During stock out period, the backlogging rate is variable and is dependent on the length
 of the waiting time for next replenishment. So that the backlogging rate for negative

inventory is, B (t) = $\frac{1}{1 + \delta(T - t)}$ δ is backlogging parameter and (T-t) is waiting time $(t_1 \le t \le T)$.

3. Mathematical Model

The rate of change of inventory, during positive stock period $[0,t_1]$ occur due to demand & resultant deterioration rate (τ_p) , and in shortage period $[t_1,T]$ occur due to demand & a fraction of demand is backlogged & backlogging rate is B(t). Hence, the inventory level at any time during $[0,t_1]$ and during $[t_1,T]$ is governed by the differential equations

$$\frac{d I_{\perp}(t)}{d t} + \tau_{p} I_{\perp}(t) = -(a + b t); 0 \leq t \leq t_{1}$$

$$\tag{1}$$

$$\frac{dI_{1}(t)}{dt} = \frac{-(a+bt)}{1+\delta(T-t)} ; t_{1} \leq t \leq T$$
 (2)

With boundary condition

$$I_1(t) = I_2(t) = 0$$
 at $t=t_1$ and $I_1(t) = IM$ at $t=0$

Inventory Level (Q(t))

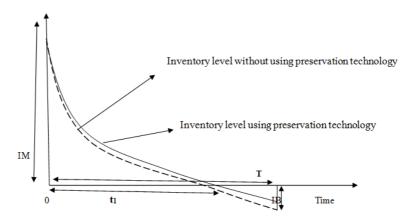


Figure 1. Graphical Representation of Inventory System

4. Analytical Solution

Case I: Inventory level without shortage

During the period $[0, t_1]$, the inventory depletes due to the deterioration and demand. Hence, the inventory level at any time during $[0, t_1]$ is described by differential equation

$$\frac{d I_1(t)}{d t} + \theta I_1(t) = -(a + b t) ; 0 \le t \le t_1$$
(3)

With the boundary condition $I_1(t_1) = 0$ at $t=t_1$

The solution of equation (3) is

$$I_{1}(t) = \begin{bmatrix} -\frac{a}{\theta - m(\xi)} - \frac{b}{\theta - m(\xi)}(t - \frac{1}{\theta - m(\xi)}) + \\ e(\theta - m(\xi))(t_{1} - t) \left[\frac{a}{\theta - m(\xi)} + \frac{b}{\theta - m(\xi)}(t_{1} - \frac{1}{\theta - m(\xi)}) \right] \end{cases}; 0 \le t \le t_{1}$$
(4)

Case II: Inventory level with shortage

During the interval $[t_1,T]$ the inventory level depends on demand and a fraction of demand is backlogged. The state of inventory during $[t_1,T]$ can be represented by the differential equation

$$\frac{d I_1(t)}{d t} = \frac{-(a + b t)}{1 + \delta(t_1 + t_2 - t)}; t_1 \le t \le t_1 + t_2$$
 (5)

With the boundary condition $I_2(t_1) = 0$ at $t=t_1$

The Solution of equation (5) is

$$I_{2}(t) = \begin{bmatrix} \frac{a}{\delta} \log \frac{1 + \delta(t_{1} + t_{2} - t)}{1 + \delta t_{2}} + \frac{b[1 + \delta(t_{1} + t_{2})]}{\delta^{2}} \log \frac{[1 + \delta(t_{1} + t_{2} - t)]}{1 + \delta t_{2}} \\ - \frac{b(t_{1} - t)}{\delta} \end{bmatrix}$$
(6)

Therefore the total cost per replenishment cycle consists of the following components:

1) Inventory holding cost per cycle;

$$IH C = \int_{0}^{t_{1}} h(t) I_{1}(t) dt$$

$$= \int_{0}^{t_{1}} (\alpha + \beta t) I_{1}(t) dt$$

$$= \int_{0}^{t_{1}} (\alpha + \beta t) I_{1}(t) dt$$

$$= \int_{0}^{t_{1}} (\theta - m(\xi))^{4} (-6 e^{(\theta - m(\xi))t_{1}} b t_{1} \alpha (\theta - m(\xi))^{2} - 6 a \beta (\theta - m(\xi)) e^{(\theta - m(\xi)t_{1})}$$

$$+ 6 a \alpha (\theta - m(\xi))^{3} t_{1} + 3 a \beta (\theta - m(\xi))^{3} t_{1}^{2} + 3 b (\theta - m(\xi))^{3} \alpha t_{1}^{2} + 2 b \beta (\theta - m(\xi))^{3} t_{1}^{3}$$

$$+ 3 b \beta (\theta - m(\xi))^{2} t_{1}^{2} + 6 b \beta e^{(\theta - m(\xi))t_{1}} - 6 a \alpha (\theta - m(\xi))^{2} e^{(\theta - m(\xi))t_{1}}$$

$$+ 6 b \alpha (\theta - m(\xi)) e^{(\theta - m(\xi))t_{1}} - 6 b \beta t_{1} (\theta - m(\xi)) e^{t_{1}(\theta - m(\xi))} + 6 a (\theta - m(\xi))^{2} \alpha$$

$$+ 6 \beta a \theta + 6 a \beta t_{1} (\theta - m(\xi))^{2} - 6 (\theta - m(\xi)) b \alpha - 6 \beta b$$

2) Backordered cost per cycle;

$$BC = \pi_{b} \left(\int_{t_{1}}^{t_{1} + t_{2}} -I_{2}(t) dt \right)$$

$$BC = \pi_{b} \left(\frac{1}{2 \delta^{3}} (2 a t_{2} \delta^{2} + b t_{2}^{2} \delta^{2} + 2 b t_{1} t_{2} \delta^{2} + 2 b \delta t_{2} + 2 b t_{2} \delta \log \left(\frac{1}{1 + \delta t_{2}} \right) \right)$$

$$+ 2 b \log \left(\frac{1}{1 + \delta t_{2}} \right) + 2 a \delta \log \left(\frac{1}{1 + \delta t_{2}} \right) + 2 b t_{1} \delta \log \left(\frac{1}{1 + \delta t_{2}} \right) \right)$$
(8)

3) Lost sales cost per cycle;

$$LS = \pi_{1} \begin{pmatrix} t_{1} + t_{2} \\ \int_{t_{1}}^{t_{1}} \left((1 - \frac{1}{1 + \delta(t_{1} + t_{2} - t)}) (a + b t) \right) dt \end{pmatrix}$$

$$LS = \pi_{1} \begin{bmatrix} (\frac{1}{2 \delta^{2}} (2 a t_{2} \delta^{2} + 2 b t_{1} t_{2} \delta^{2} + b t_{2}^{2} \delta^{2} - 2 a \delta \log(1 + \delta t_{2}) \\ -2 b \log(1 + \delta t_{2}) - 2 b \delta t_{1} \log(1 + \delta t_{2}) - 2 b \delta t_{2} \log(1 + \delta t_{2}) + 2 b \delta t_{2})) \end{bmatrix}$$
(9)

4) Purchase cost per cycle = (purchase cost per unit) * (Order quantity in one cycle)

$$PC = C*Q$$

When t=0 the level of inventory is maximum and it is denoted by IM (= $I_1(0)$) then from the equation (4)

$$IM = \left[-\frac{a}{(\theta - m(\xi))} + \frac{b}{(\theta - m(\xi))^2} + e^{(\theta - m(\xi))t_1} \left[\frac{a}{(\theta - m(\xi))} - \frac{b}{(\theta - m(\xi))} (t_1 - \frac{1}{(\theta - m(\xi))}) \right] \right]$$
 (10)

The maximum backordered inventory is obtained at $t = t_1 + t_2$ then from the equation (6)

$$IB = -I_2 (t_1 + t_2)$$
 (11)

$$IB = -\left[\frac{a}{\delta} \log \frac{1}{1 + \delta t_2} + \frac{b[1 + \delta (t_1 + t_2)]}{\delta^2} \log \frac{1}{1 + \delta t_2} + \frac{b t_2}{\delta}\right]$$

Thus the order size during total time interval [0,T]

$$Q = IM + IB$$

Now from equations (10) and (11)

$$Q = \begin{bmatrix} -\frac{a}{(\theta - m(\xi))} + \frac{b}{(\theta - m(\xi))^{2}} + e^{(\theta - m(\xi))t_{1}} \begin{bmatrix} \frac{a}{(\theta - m(\xi))} - \frac{b}{(\theta - m(\xi))} \\ \frac{b}{(\theta - m(\xi))} (t_{1} - \frac{1}{(\theta - m(\xi))}) \end{bmatrix} \\ -\frac{a}{\delta} \log \frac{1}{1 + \delta t_{2}} - \frac{b[1 + \delta(t_{1} + t_{2})]}{\delta^{2}} \log(1 + \delta t_{2}) - \frac{bt_{2}}{\delta} \end{bmatrix}$$
(12)

Thus

$$PC = C*O$$

$$= C \left[-\frac{a}{(\theta - m(\xi))} + \frac{b}{(\theta - m(\xi))^{2}} + e^{(\theta - m(\xi))t_{1}} \left[\frac{a}{(\theta - m(\xi))} - \frac{b}{(\theta - m(\xi))} (t_{1} - \frac{1}{(\theta - m(\xi))}) \right] - \frac{a}{\delta} \log \frac{1}{1 + \delta t_{2}} - \frac{b[1 + \delta(t_{1} + t_{2})]}{\delta^{2}} \log(1 + \delta t_{2}) - \frac{bt_{2}}{\delta} \right]$$

$$(13)$$

5) Ordering Cost

$$OC = A \tag{14}$$

Therefore the total cost per time unit is given by,

=
$$\frac{1}{\left(t_{\perp} + t_{2}\right)}$$
 [Ordering cost + carrying cost + backordering cost + lost sale cost + purchase Cost]

$$TC(t_1, t_2, \xi) = \frac{1}{(t_1 + t_2)} [OC+ IHC + BC + LS + PC]$$

Putting the values of OC, IHC, BC, LS and PC then,

$$TC(t_1,t)=$$

$$\left\{ A - \frac{1}{6\theta^4} \left(-6e^{(\theta - m(\xi))t_1} b \, t_1 \alpha \, (\theta - m(\xi))^2 - 6 \, (\theta - m(\xi)) \, a \, \beta \, e^{(\theta - m(\xi))t_1} \right. \\ + 6 \, a \, \alpha \, t_1 \, (\theta - m(\xi))^3 + 3 \, a \, \beta \, (\theta - m(\xi))^3 \, t_1^2 + 3 \, b \, (\theta - m(\xi))^3 \, \alpha \, t_1^2 + 2 \, b \, \beta \, (\theta - m(\xi))^3 \, t_1^3 \right. \\ + 3 \, b \, \beta \, (\theta - m(\xi))^2 \, t_1^2 + 6 \, b \, \beta \, e^{(\theta - m(\xi))t_1} - 6 \, e^{(\theta - m(\xi))t_1} \, a \, \alpha \, (\theta - m(\xi))^2 \\ + 6 \, e^{(\theta - m(\xi))t_1} \, b \, \alpha \, (\theta - m(\xi)) - 6 \, e^{(\theta - m(\xi))t_1} \, b \, \beta \, t_1 \, (\theta - m(\xi)) + 6 \, a \, (\theta - m(\xi))^2 \, \alpha \right. \\ + 6 \, \beta \, a \, (\theta - m(\xi)) + 6 \, a \, \beta \, t_1 \, (\theta - m(\xi))^2 - 6 \, (\theta - m(\xi)) \, b \, \alpha - 6 \, \beta \, b \, b \right) \\ + \frac{1}{2\delta^2} \left(\pi_1 \left(2 \, a \, t_1 \delta^2 + 2 \, b \, t_1 t_2 \delta^2 + b \, t_2 \delta^2 - 2 \, a \, \delta \, \log \, (1 + \delta \, t_1) - 2 \, b \, \log \, (1 + \delta \, t_1) \right. \\ - 2 \, b \, t_1 \delta \, \log \, (1 + \delta \, t_1) - 2 \, b \, t_2 \delta \, \log \, (1 + \delta \, t_2) + 2 \, b \, \delta \, t_2 \right. \\ + 2 \, b \, t_1 \delta \, \log \, \left(1 + \delta \, t_1 \right) - 2 \, b \, t_2 \delta \, \log \, \left(1 + \delta \, t_1 \right) + 2 \, a \, \log \, \left(\frac{1}{1 + \delta \, t_2} \right) \delta + 2 \, b \, \log \, \left(\frac{1}{1 + \delta \, t_2} \right) \delta \right. \\ + 2 \, b \, t_2 \, \log \, \left(\frac{1}{1 + \delta \, t_2} \right) \delta + 2 \, b \, \log \, \left(\frac{1}{1 + \delta \, t_2} \right) + 2 \, a \, \log \, \left(\frac{1}{1 + \delta \, t_2} \right) \delta + 2 \, b \, \log \, \left(\frac{1}{1 + \delta \, t_2} \right) \delta \right. \\ + c \left. \left. \left(\frac{a}{\theta - m(\xi)} \right) + \frac{b}{(\theta - m(\xi))} + \frac{b}{(\theta - m(\xi))^2} + e^{\theta \, t_1} \left[\frac{a}{(\theta - m(\xi))} - \frac{b}{(\theta - m(\xi))} \left(t_1 - \frac{1}{(\theta - m(\xi))} \right) \right] \right] \right] \right) \right. \\ + c \left. \left. \left(\frac{a}{\theta - m(\xi)} \right) + \frac{b}{(\theta - m(\xi))} + \frac{b}{(\theta - m(\xi))^2} + e^{\theta \, t_1} \left[\frac{a}{(\theta - m(\xi))} - \frac{b}{(\theta - m(\xi))} \left(t_1 - \frac{1}{(\theta - m(\xi))} \right) \right] \right] \right) \right. \right.$$

Differentiates the equations (15) with respect to t_1 , t_2 and ξ then we get

$$\frac{\partial TC}{\partial t_1}$$
, $\frac{\partial TC}{\partial t_2}$ and $\frac{\partial TC}{\partial \xi}$

To minimize the total cost TC (t_1 , t_2 , ξ) per unit time the optimal value of t_1 , t_2 and ξ can be obtained by solving the following equations

$$\frac{\partial TC}{\partial t_1} = \emptyset, \frac{\partial TC}{\partial t_2} = \emptyset \quad \text{and} \quad \frac{\partial TC}{\partial \xi} = 0$$
 (16)

Provided the determinant of principal minor of hessian matrix (H-matrix) o TC (t_1 , t_2 , ξ)f is positive definite. i.e. $det(H_1)>0$, $det(H_2)>0$, $det(H_3)>0$ where H_1 , H_2 , H_3 is the principal minor of the H-matrix.

The H-matrix of function TC (t_1, t_2, ξ) is defined as

$$H = \begin{bmatrix} \frac{\partial^2 TC}{\partial t_1^2} & \frac{\partial^2 TC}{\partial t_1 \partial t_2} & \frac{\partial^2 TC}{\partial t_1 \partial \xi} \\ \frac{\partial^2 TC}{\partial t_2 \partial t_1} & \frac{\partial^2 TC}{\partial t_2^2} & \frac{\partial^2 TC}{\partial t_2 \partial \xi} \\ \frac{\partial^2 TC}{\partial \xi \partial t_1} & \frac{\partial^2 TC}{\partial \xi \partial t_2} & \frac{\partial^2 TC}{\partial \xi^2} \end{bmatrix}$$

5. Numerical Illustration

For numerical illustration we consider an inventory system with the following parameter in proper unit A=250, α =0.5, β =0.01, C=40, π_b =10, π_i =8, δ =8, a=10, b=2, θ =0.002 and m (ξ)= θ (1-e^{-2k}). The computer output of the program by using maple mathematical software is t_1 =0.09, t_2 =1.323 and ξ =9.84. i.e. the value of t1 at which the inventory level become zero is 0.09 unit time, shortage period is 1.323 unit time and the optimal value of preservation technology cost is 9.84 per unit.

6. Conclusion

The purpose of this study is to present an inventory model involving controllable deterioration rate to extend the traditional EOQ model. The products with high deterioration rate are always crucible to the retailer's business. In real markets, the retailer can reduce the deterioration rate of product by making effective capital investment in storehouse equipment.. In this study to reduce the deterioration rate retailer invested in the PT cost and a solution procedure has presented to determine an optimal replenishment cycle, shortage period, order quantity and preservation technology cost such that the total inventory cost per unit time has minimized. A numerical example has presented to illustrate the model. The model is very practical for the retailers who use the preservation technology in their warehouses to control the deterioration rate under other assumptions of this model. This model can further be extended by taking more realistic assumptions such as finite replenishment rate, Probabilistic demand rate etc.

Acknowledgement

The author would like to thank the editor and anonymous reviewers for their valuable and constructive comments, which have led to a significant improvement in the revised version of the paper.

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Journal of Industrial Engineering and Management, 2013 (www.jiem.org)



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