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Estimating nonlinear intergenerational income mobility with correlation curves

William Nilsson

Abstract

A correlation curve is introduced as a tool to study the degree of intergenerational income mobility, i.e. how income status is related between parents and adult child. The method overcomes the shortcomings of the elasticity of children's income with respect to parents' income (i.e. its sensitiveness to different dispersion among the generations) and the correlation coefficient (i.e. its inability to capture nonlinearities). The method is particularly suitable for comparative studies and in this study labour earnings are compared to disposable income. The correlation between the parental income and the child's adult disposable income becomes stronger for higher percentiles in the income distribution of the parents. Above the median the correlation is found to be stronger than for labour earnings. Interestingly, the elasticity is higher for labour earnings for most parts of the distribution and complementing the elasticity with correlation curves provides a much more complete picture of the intergenerational income mobility.

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Keywords Intergenerational mobility; nonlinear; nonparametric; correlation curve

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1. Introduction

The empirical literature on intergenerational income mobility has, during the last 20–25 years, been highly focused on estimating the correlation between a father's income and a child's income in adulthood. Often the estimate of interest has been the elasticity obtained from a regression of the father's log income on the child's adult log income. Compared to the earlier literature, Zimmerman (1992) and Solon (1992) provide important contributions by underlining the importance of not using homogenous samples as well as avoiding the use of short-run measures of income, which otherwise would result in downward-biased estimates. Other important methodological concerns when it comes to estimating the intergenerational income elasticity are life cycle bias (Jenkins, 1987; Haider and Solon, 2006; and Grawe, 2006) and the possibility of a nonlinear relation (Corak and Heisz, 1999; Österbacka, 2001; Björklund and Chadwick, 2003; Fertig, 2003; Grawe, 2004; and Bratsberg et al. 2007). Couch and Lillard (1998) highlight the sensitivity of the elasticity due to different sample selection rules.

Estimating intergenerational income elasticity has become the main way to study intergenerational income mobility, but in some occasions it is complemented with alternative methods. Dearden et al. (1997), Fertig (2003) and Bratberg, Nilsen and Vaage (2005) complement their analyses with transition matrices. Eide and Showalter (1999) use quantile regression to estimate different elasticities for different quantiles of the son's earnings distribution. Österberg (2000), Fertig (2003) and Jäntti et al. (2006) estimate the probability that the child will end up at a particular decile (or quintile) given the decile (or quintile) of the parent. Many recent studies complement the elasticity with Spearman rank correlation. See, for example, Chetty et al. (2014), Corak et al. (2014), Chen et al. (2017), Gregg et al. (2017), Heidrich (2017) and Bratberg et al. (2017). Nybom & Stuhler (2016) show that rank correlation is particularly robust to the problems of measurement that are mentioned above, i.e. life cycle bias and few years of observed income.

Data on parents' and children's adult income are usually measured at different times. Even if the aim is to collect data for the two generations at more or less the same stage of the life cycle, the distributions of parents' and children's incomes are likely to differ. Different generations grow up in quite different societies and it is not necessary that the distributions are approximately the same. Solon (1992) discusses the assumption that the variance in income for the two generations is the same. If it is not, the elasticity cannot be used as a measure of the degree of association. This important observation has in many cases been left aside, and only the elasticity has been reported in many empirical studies (Blanden, 2011). A difference in dispersion would, *ceteris paribus*, affect the intergenerational income elasticity, while the correlation coefficient would not be affected (Jäntti et al., 2006). The difference between these two measures of mobility is also discussed by Fertig (2003) and Aaronson and Mazumder (2008), where trends in inequality are also related to trends in intergenerational elasticity. In Blanden et al. (2007) the elasticities are scaled, i.e. multiplied by the ratio of standard deviations of the parent's income to the standard deviation of the income of the adult children (σ_x / σ_y), to obtain partial correlation coefficients. The reason is precisely to cope with different dispersion for the different generations. Recent research on intergenerational income mobility has focused on comparing different measures of economic situation (for example father's or parents' incomes or earnings) or different subgroups (for

example intact families or divorced families and trends over time). See for example Nordli Hansen (2010), Lucas and Kerr (2013), Bratberg et al. (2014) and Lefranc et al. (2014). The ratio of σ_x / σ_y can be very different for different subgroups or depending on which measure is used and it is important to complement the elasticity with the coefficient of correlation.

Björklund et al. (2012) found an intergenerational elasticity of 0.260 for earnings and 0.168 for income for Swedish data. The difference between the measures was found to be much smaller when the elasticities were standardized to obtain correlation coefficients (0.23 respective 0.19). The difference between an intergenerational *transmission*, i.e. an elasticity, and a *degree of association* measured with a correlation coefficient can be crucial for comparisons. In the same study, using a linear spline regression across fathers' fractiles, elasticities of 0.896 for incomes and 0.447 for earnings, for the top 0.1% of the income distribution of the fathers were found. Comparing the descriptive statistics for the log earnings of the fathers and the sons reveal a much higher dispersion, at the top tail of the distribution, for the sons. This is in particular the case when income is analysed. Hence, it is expected that the elasticity will be higher at this position of the income distribution. While the intergenerational income transmission is found to be very strong, the measures cannot provide a conclusion about the *degree* of intergenerational income or earnings association.

The purpose in this study is to introduce a local measure of the degree of association of incomes of two generations. Using a *correlation curve* follows the recommendation in Blanden (2011) to complement the elasticity with a correlation coefficient, and, in addition, the measure is local, which allows a varying degree of association as recommended in Bratsberg et al. (2007). The approach avoids the sensitivity to differences in dispersion in the two generations that is accompanied by the (nonlinear) elasticity. The correlation curve was in fact mentioned by Björklund and Jäntti (2000) as "an obvious direction in which to move" in a survey of the literature on intergenerational mobility of socio-economic status.

Bjerve and Doksum (1993) and Doksum et al. (1994) introduced correlation curves, $\rho(x)$, to measure the strength of a relation locally at different values of a covariate X . Their correlation curve is a universal scale-free measure which shares many properties with the correlation coefficient, but it is, in addition, suitable for nonlinear models. In the same way as the correlation coefficient is a standardized version of the regression slope, the correlation curve is a standardized local regression slope. The correlation curve is invariant to changes in the origin and scale and is $-1 \leq \rho(x) \leq 1$ for all x . Accordingly, the measure is easy to interpret and fairly easy to implement once a nonparametric estimation technique for the local regression slope is specified. Point wise confidence intervals can be included with a bootstrap technique (Nilsson and del Barrio Castro, 2012). The concept of a local correlation is a natural extension of the correlation coefficient to nonlinear models and can be applied to any area in social science. Despite that, very few applications can be found and it appears that the method is not very well known. The concept of a local correlation has probably gained most interest in financial economics, but even there only a few articles have used the method (see, for example, Inci et al. (2011) and Støve et al. (2014)).

An advantage of using this method is that intergenerational mobility is measured at each position in the income distribution of the parents, which allows a varying strength

of the relation as suggested in previously mentioned literature. In addition, the method is particularly suitable for comparing different populations, for example different countries, or comparisons over time. It is important to clarify that the correlation curve is proposed as a complement, and not as an alternative to the nonlinear intergenerational income elasticity.

In this study the method is applied to Swedish data and nonparametric estimates of the elasticity are also included. The purpose is to compare two different aspects of intergenerational income mobility. First, mobility is measured for individual labour earnings; i.e., interest is in equality of opportunity in providing a salary for the household. Labour earnings are measured before paying taxes and receiving benefits and without taking into account the size of the household. The second aspect studies income mobility in terms of equality of opportunity to enjoy a certain standard of living. In this case, disposable income is used and income is measured after paying taxes and receiving benefits. This measure also contains income acquired by other household members, and disposable income is weighted for the composition of the household.¹ Both parents' income is used, instead of only the father's income, to better capture the standard of living.

The results indicate important nonlinearities, both for labour earnings and disposable income, in intergenerational income correlation. Using the correlation coefficient does not give an accurate summary of the degree of association. The correlation for both measures of the son's income and parental income is higher for higher deciles of the income distributions of the parents. For higher deciles the correlation is stronger for disposable income than for labour earnings. At the same time, the nonparametric elasticity is clearly higher for most parts of the distribution when labour earnings are analysed compared to disposable income. The explanation for these seemingly contradictory results is the sensitivity of the elasticity to differences in the dispersion of the children's and parents' incomes. Using the correlation curve for comparisons is clearly justified.

The method is described in section 2. The data are explained in section 3 and the results are presented in section 4. Concluding remarks are offered in section 5.

2 Method

The literature review of intergenerational income mobility is very brief as important surveys are available (see, for example, Solon (1999) and Blanden (2011)). The focus in this section is on the introduction of an alternative method to study intergenerational income mobility. The method is based on nonparametric techniques to estimate correlation curves. Bootstrap is used to obtain point wise confidence intervals.

2.1 Intergenerational income correlation and intergenerational income elasticity

Consider a data set of individuals with income measured at a point several years into

¹ The consumption weights are based on norms defined by the National Board of Health and Welfare in Sweden. A family of one adult implies a weight of 1.16. For two or more adults, each adult is weighted 0.96. Children 0-3, 4-7 and 11-17 years old add, respectively, 0.56, 0.66 and 0.76.

adulthood. Several years of data on parental income are available. The incomes for the individual and the parents could be measured at the same years, but then the incomes would be measured at very different times in the life cycle for the two generations. Another possibility is data where the incomes for parents are measured sometime during the childhood or youth of the individuals. In either case it is possible that the distribution of incomes will be different for the two generations. Being in different positions in the life cycle is likely to provide different distributions. The income dispersion could also have increased or decreased over time. Differences in standard deviation of the income distributions affect the intergenerational income elasticity, while the correlation coefficient is unaffected. As a consequence, using the correlation coefficient makes the comparison of intergenerational income mobility much more transparent. The degree of relation is not mixed up with differences in the standard deviation for the incomes in the two generations.

2.2 Intergenerational correlation curves and nonparametric elasticities

The intergenerational income elasticity can easily be allowed to vary over the income distribution of the fathers/parents by estimating the regression function with nonparametric techniques, $m(x) = E(Y|X = x)$, where X in this case is the logarithm of income of the fathers/parents and Y is the logarithm of income of the children at adult age. The slope of the regression function, $m'(x)$, corresponds to a local measure of the intergenerational income elasticity. An advantage of a nonparametric estimation technique is, of course, that we do not impose restrictions on the functional form. A disadvantage, at least when the interest is in comparing the results, is, however, that the elasticity is still affected by the distributional differences of the two generations. The local *degree* of association can be estimated using a correlation curve,

$$\rho(x) = \frac{\sigma_x m'(x)}{[\{\sigma_x m'(x)\}^2 + \sigma^2(x)]^{1/2}} \quad (1)$$

where $\sigma^2(x) = \text{var}(Y|x)$ is the residual variance. σ_x is the standard deviation of X . The correlation curve is easily calculated once a nonparametric technique is used to estimate the derivative of the regression function and the residual variance.

Bjerve and Doksum (1993) discuss in detail the properties of the correlation curve. A few of the properties that are relevant for this application are mentioned below. First, the correlation curve is invariant to changes in the origin and scale. The correlation curve is standardized to be $-1 \leq \rho(x) \leq 1$ for all x , and the strength of the association is interpreted in the same way as the correlation coefficient: $\rho(x) = 0$ for all x when X and Y are independent, and $\rho(x) = \pm 1$ for all x when X is a function of Y . For linear models the correlation curve reduces to the correlation coefficient. An important difference compared to the correlation coefficient is that, in general, $\rho_{XY}(\cdot) \neq \rho_{YX}(\cdot)$. In this particular application the main interest is on $\rho_{XY}(x)$, which can be compared to $m'(x)$. $\rho_{XY}(x)$ is clearly affected by $m'(x)$, but also detects a possible heteroscedastic pattern where the association could be locally weaker or stronger.

To implement the correlation curve it is appropriate to use a flexible technique to obtain a local measure of the regression slope and a local measure of the residual variance. In this case, the nonparametric method is local polynomial regression, due to its advantageous properties (Fan, 1992, 1993). The data-driven procedure suggested by Fan and Gijbels (1995a) to find the optimal bandwidth for the first derivative is used. Confidence intervals for the correlation curve is added using wild bootstrapping. The method was introduced for the correlation curve in Nilsson and del Barrio Castro (2012) and the coverage rates are found to be satisfactory.

3 Data

The empirical analysis in this study is based on Swedish register data administered by Statistics Sweden. The sample consists of 10% random sample of individuals born between 1949 and 1958. The sample is divided into male and female samples that are analyzed separately. The years of outcome are 1994 to 1999. The income is, accordingly, measured over six years between the ages of 36 and 50. The Population and Housing Census is used to identify parents. It is not necessary for the parents to be biological parents, although this is the most common scenario. Parents identified in the Population and Housing Census in 1965 are identified. By using the censuses in 1960 and 1970, the final sample is restricted to individuals where both the father and the mother are identified twice within a five-year difference. For example, for individuals born in 1949 the censuses in 1960 and 1965 are used and the parents are identified at age 11 and 16. The reason for restricting the samples to cases where the parents were actually present is to capture both biological and social reasons for an intergenerational income correlation.

The incomes of the parents are available for the years 1971, 1974 and 1977 and come from the Income and Wealth Register. Parents were required to be alive until at least the year 1978 to be included.

The longitudinal database LOUISE is used for the income of the individuals, which is measured for the years 1994 to 1999. Labour earnings and disposable income are used in the analysis. Note that an exact counterpart to the measure of parents' income is not available in the registers. Fathers' and mothers' income is aggregated net labour and capital income. The income is averaged over time for both generations. Individuals who died, or were living outside Sweden for at least one period, have been dropped from the sample. All income variables are measured in Swedish Crowns (krona) deflated to the price level of 2001. Summary statistics are included in Table 1.

The natural logarithm is used for all income measures. The samples are restricted to adult child and parents with positive average income/earnings. This restriction decreases the male sample size by about 6% when labour earnings are used. The sample size is reduced by about 5% when the female sample is used. The restriction to exclude an average income that is zero hardly affects the sample sizes at all when disposable income is the variable measuring adult income.

The standard deviation of labour earnings is substantially higher than the standard deviation for the income of the parents. The larger dispersion for the adult children is also evident when incomes in different percentiles are compared. Note, however, that parents' average income is based on incomes over several nonconsecutive years and also that the measures of income actually are different. It is also possible that a general

tendency for increased inequality in society, as well as life cycle differences, could explain the differences in dispersion.

Table 1: Summary statistics

	Years	Mean age	P10	P30	P50	P70	P90	Mean	Std. dev.	n
Labour income										
Sons	1994-1999	42.9	10.96	12.12	12.33	12.51	12.86	12.04	1.21	34539
Parents	1971, 74, 77.	Father: 52.3 Mother: 49.0	11.94	12.32	12.55	12.74	13.06	12.52	0.48	
Disposable income										
Sons	1994-1999	42.9	11.12	11.37	11.54	11.75	12.07	11.57	0.42	36886
Parents	1971, 74, 77.	Father: 52.4 Mother: 49.0	11.92	12.31	12.54	12.74	13.05	12.47	0.48	
Labour income										
Daughters	1994-1999	42.9	10.82	11.74	12.00	12.18	12.42	11.73	1.03	33797
Parents	1971, 74, 77.	Father: 52.3 Mother: 49.0	11.95	12.33	12.55	12.74	13.06	12.52	0.48	
Disposable income										
Daughters	1994-1999	42.9	11.14	11.36	11.52	11.69	11.95	11.53	0.38	35404
Parents	1971, 74, 77.	Father: 52.3 Mother: 49.0	11.94	12.33	12.55	12.74	13.06	12.52	0.48	

Notes: All income variables are expressed after taking the logarithm. When individual income is disposable income it is based on the disposable family income, where an equivalence scale has been used to individualize the income. 'Parents' income' refers to the sum of the aggregate net labour and capital income for both parents. Note that parents' incomes are after deducting possible deficit in income sources. The incomes are measured in Swedish Crowns (krona) deflated to the price level of 2001. Mean age refers to the age when income is measured.

It is also important to remember that the parents were selected based on being present in the household. Individuals spending shorter periods in the household, for example due to divorce, or individuals never in a partnership are accordingly not included in the income distribution. If individuals in a stable partnership tend to have a more stable position in the labour market it is possible that the distribution is more compressed. This selection is, of course, not applied for the adult sons.

Disposable income has a smaller standard deviation for the adult children, and this is in fact quite similar to the standard deviation for the combined income of the parents.

4 Results

The main measure for intergenerational income mobility in this study is the correlation curve. As a departure for the analysis, correlation coefficients and linear elasticities are estimated. These results can be found in Table 2. The correlation coefficient of Pearson is higher when disposable income is used compared to when labour earnings are used, while the opposite is the case for the elasticity. Comparing the results for the different measures it is clear that the intergenerational elasticity only captures intergenerational income transmission, and not the degree of association. Without knowing the standard deviations of the samples, the intergenerational income elasticity would have led us to believe the intergenerational mobility to be higher for disposable income than for labour earnings. It is, however, clear that such a conclusion is only correct if we are willing to include distributional differences, hence different

dispersion, as an important part of the ‘intergenerational mobility’ concept. The correlation coefficient of Pearson indicates that society is more rigid when it comes to disposable income compared to labour earnings. In this case, the results are not affected by a different standard deviation between the income of the individuals and that of the parents. Rank correlation is found to be fairly similar for the two measures. It is even slightly higher for labour earnings compared to disposable income.

Table 2: Elasticities and correlation coefficients

	Elasticity	Std. error	Pearson correlation	Rank correlation
Sons				
Labour income	0.3488***	0.0134	0.1382***	0.2171***
Disposable income	0.1665***	0.0045	0.1904***	0.1865***
Daughters				
Labour income	0.1810***	0.0178	0.0834***	0.1479***
Disposable income	0.1121***	0.0041	0.1421***	0.1323***

Notes: *** $p < 0.01$.

The estimated values for the correlation coefficients and the elasticity can be found in Table 2. We should, however, be careful when interpreting the magnitude of these summary measures as the pattern could be different over the parents’ income distribution.

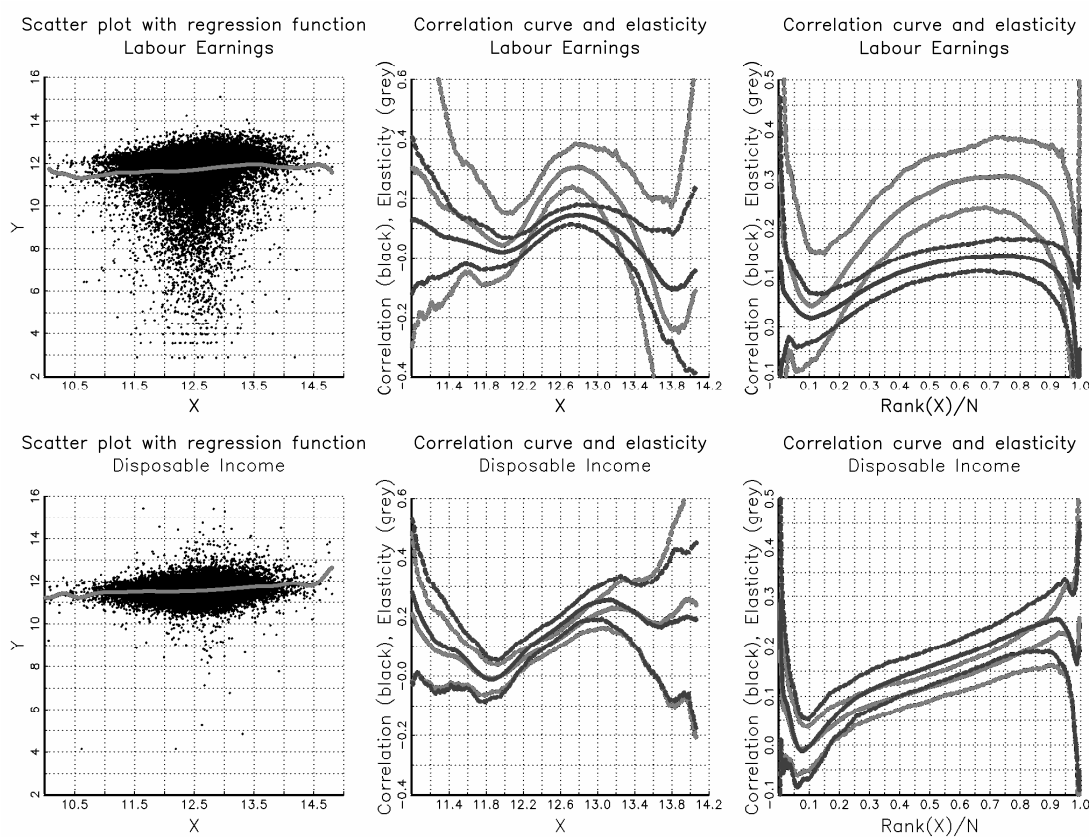


Fig. 1. Scatter plot and correlation curves (and elasticity) for sons.

Figure 1 includes scatter plots, nonparametric elasticities and the correlation curves using labour earnings respectively disposable income for the male sample. 95% confidence intervals are also included. The nonlinear elasticity is found to be well above the correlation curve.

When analysing the second figure for both labour earnings and disposable income it is important to remember that 80% of the sample is found between log income of 11.94 (first decile) and 12.86 (the 9th decile) and the measures are relevant for fewer individuals in the tails of the distribution. The correlation gradually increases until between the 8th and 9th decile, where it starts to decrease.

The second figure for disposable income shows the elasticity and correlation curve. The elasticity and the correlation curve are in this case found to be fairly similar. The general pattern is that the correlation (and the elasticity) is higher for higher parental income.

To simplify the comparison the figure in the third column in figure 1 includes the elasticity and correlation curves expressed for different percentiles of the parents' income distributions. The elasticity is found to be substantially higher for labour earnings compared to disposable income for most parts of the distribution. From percentile 35 the elasticity is above 0.4 and from decile 7th to almost 9th decile the elasticity is even above 0.45 for labour earnings.

When disposable income is analysed, the elasticity is below 0.15 at percentile 35 and reaches its highest value, i.e. about 0.28, at about the 9th decile. The intergenerational income *transmission* is stronger for labour earnings compared to disposable income.

For lower deciles, i.e. from the first to the fifth decile, the correlations are fairly similar for labour earnings and disposable income. The correlation is found to be slightly above 0.15 at percentile 35 for labour earnings, but even at the highest position, the curve is only about 0.2. This happens approximately at percentile 85. For disposable income the highest correlation is about 0.3 for the same percentile. At the eighth decile the correlation is found to be statistically significantly higher for disposable income compared to labour earnings.² The *degree of association* is, accordingly, quite similar below the median parents' income distribution, but for higher deciles, the degree of association is much higher for disposable income. The correlation is particularly low for the first deciles.

An elasticity of about 0.45 that is found for labour earnings at the 7th decile (to almost 9th decile) of the parents' income distribution, implies that an increase of 1% of the parents' income would, on average, mean a 0.45% increase in labour earnings for the son. It is important to remember that it is not possible to make a causal interpretation of the elasticity. An elasticity of 0.45 is comparatively large, in particular, for the Swedish case, but complementing the elasticity with a measure of local correlation of about 0.2 provides an important perspective. If the local correlation is squared, we obtain a local coefficient of determination of about 0.04, and the average transmission that is given by the elasticity is clearly uncertain. Despite an elasticity of 0.45, the child's labour earnings are fairly weakly related to the income of the parents.

² Note that the figures show 95% pointwise confidence intervals, and the correlation curve for the population is below the lower confidence interval with a probability of approximately 0.025. The same probability is applied for above the upper confidence interval for the other population. Hence, only using the figure to tell whether the two populations have statistically significant different correlations at some point implies a very restrictive significance level, i.e. less than 0.1%.

Inequality of opportunity to acquire labour earnings does not seem to be too severe, as long as parents' income is used as the only relevant circumstance. Factors unrelated to parents' income, could, however, still be important to create inequalities of opportunity to acquire labour earnings.

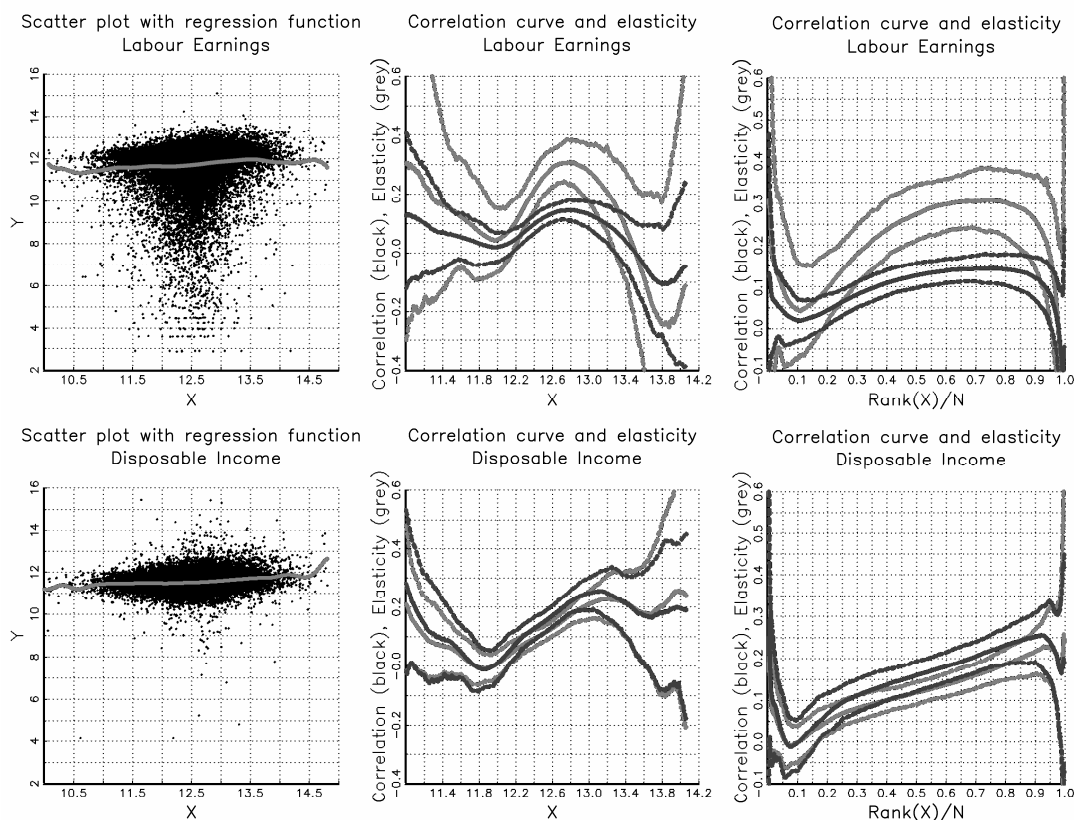


Fig. 2. Scatter plot and correlation curves (and elasticity) for daughters.

The pattern is fairly similar for the female sample. The difference is relatively large between the correlation curve and the elasticity when labour earnings are analyzed. The elasticity does, however, not reach as high values as for the male sample. For example, at percentile 35 the elasticity is below 0.2 and between decile 6 and 8 the point estimate is slightly above 0.3. For disposable income the elasticity is below 0.1 at percentile 35 and rises as the parents' income increases. At decile 9 the elasticity is above 0.2. The correlation curve, when labour earnings are analyzed, is much below the curve for the elasticity. At its highest position, i.e. about decile 7 and 8, the correlation is still below 0.15. For disposable income the correlation increases as the parents' income increases and the curve reaches its highest value, i.e. slightly above 0.25, at about decile 9. The shapes of both the correlation curves as well as the elasticity are similar to the male sample, but the magnitude is lower.

Using the elasticity to evaluate the *intergenerational income transmission*, and the correlation curve to study the *degree of intergenerational income association*, provides different conclusions concerning if the income mobility is higher or lower for labour earnings or disposable income. The results underline the main argument of the paper, i.e. the intergenerational income transmission should be accompanied with an analysis

on the degree of intergenerational income association, and the method should be able to capture nonlinearities.

5 Concluding remarks

The literature on intergenerational income mobility has been dominated by summary measures such as the correlation and elasticity of adult child income with respect to father's income. An advantage with the correlation coefficient is that the dispersion has been standardized. An increased income inequality would (if it increases the standard deviation), for example, result in a higher elasticity, while the correlation would not be affected. An important problem with the correlation coefficient is, however, that it does not capture different degrees of association over the distribution. In this study, correlation curves are introduced to measure intergenerational income mobility. The results indicate that irrespective of what income measure that is used, the correlation is found to be nonlinear. Using the correlation coefficient is not enough to give a representative measure for the correlation at different parts of the distribution. For example, using the correlation coefficient underestimates the correlation at the eighth decile by about 50% when disposable income is analysed. For lower deciles the correlation is overestimated.

The results indicate fairly high intergenerational income mobility at the lower part of the distribution. This result is similar to what Bratsberg et al. (2007) found for Denmark, Finland and Norway. It is possible that the Nordic welfare state, with its highly redistributive educational policies, could have an important role to play in explaining the pattern.

Particularly for higher deciles of the parents' income distribution the results show that the degree of intergenerational income correlation is higher for disposable income than for labour earnings. If nonlinear intergenerational income elasticity were to be used to measure the intergenerational income mobility the opposite conclusion would be reached. The reason is that the dispersion of labour earnings is substantially higher than the dispersion of disposable income and this inflates its elasticity. Comparing elasticities from nonparametric models can be informative regarding the pattern over the distribution, but the magnitude of different samples is sensitive to differences in the dispersion of the distributions. For example, the elasticity is about 0.45 at the eighth decile when labour earnings are analysed for a male sample. The corresponding elasticity, at the same decile, but when disposable income is analysed, is less than 0.3. Despite this, the correlation is stronger in the latter case, with a correlation of 0.3 compared to a correlation of only 0.2 when labour earnings are studied. Therefore, the elasticity suggests that the labour earnings are transmitted with much higher persistence among generations than disposable income. The correlation curve effectively clarifies that this result is due to the different dispersion that inflates the elasticity when labour earnings are used. The *degree* of relation is, in fact, stronger at higher deciles for disposable income than for labour earnings. It is important to remember that the elasticity does not measure the *degree* of a relation, and a comparative study would benefit from using the correlation curve to measure intergenerational income mobility. The results are otherwise sensitive to differences in income dispersion of the two generations, which could be due to life cycle difference, changes in society over time, or simply different definitions of the income variables in the two generations.

The data used in this study covers six years of income for the adult child, measured around age 43, and three years of *both* father's and mother's income, measured in 1971, 1974 and 1977. Despite that it is fairly good situation to avoid large life cycle bias and measurement error due to transitory variation it cannot be ruled out that these concerns are present. In particular it would be interesting to evaluate how the correlation curve would perform in different parts of the distribution going from using a complete working life history to a less favorable situation. It is also important to remember that father's income is not really a proxy for parents' combined income. Father's income is an underreported amount of parents' income which in some cases can be an important share, but yet in other cases, can be far from the actual combined income of the parents. This difference of father's income and parents' income can be particularly important when local measures are used to measure intergenerational income mobility.

The key argument in this paper is that the correlation curve provides an important complement to nonlinear elasticities. The correlation curve is not proposed as a substitute to the traditional elasticity, but it is important to be clear what conclusion is warranted from an analysis of the elasticity.

Applying the correlation curve to studying intergenerational income mobility is particularly useful for making cross-country comparisons. Firstly, the correlation curve captures different mobility in different parts of the distribution. Different countries could have different patterns of the intergenerational income mobility over the income distribution of the parents. Secondly, the correlation curve is not, in contrast to the elasticity from a nonparametric regression, sensitive to different dispersion in the two generations. In addition, if mobility matrices or other rank-based measures of mobility are used, a country with high income dispersion would have a greater (monetary) difference from one income category to the next, for example from the second decile to the third decile. Therefore, the income could be fairly different without resulting in a changed category, and, accordingly, a higher inequality would automatically imply lower mobility. This problem is avoided with the correlation curve, and international comparisons can be made more easily. Note that the correlation curve can be implemented using a linear regression, adding higher-order polynomial terms of the parents' income, instead of working with a nonparametric regression that requires large data sets (Blyth, 1994). A disadvantage is of course that this imposes a restriction of the functional form that could be fulfilled to different degrees for different samples. The correlation curve is easy to interpret, and since it is a scale-free measure it is, in fact, a highly useful tool for making comparisons, not only for measuring intergenerational income mobility, but for a wide range of empirical topics.

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Appendix

Nonparametric technique

The nonparametric method used in this study is local polynomial regression. For x in a neighbourhood of x_0 , $m(x)$ is approximated locally by a polynomial of order p :

$$m(x) \approx m(x_0) + m'(x_0)(x - x_0) + \dots + m^{(p)}(x_0)(x - x_0)^{(p)} / p! \quad (A1)$$

The bandwidth, h , controls the size of the local neighbourhood and $K(x)$ is a kernel function that weights the data points closer to x_0 more heavily. The solution to the weighted polynomial regression is: $\hat{\beta} = (X^T W X)^{-1} X^T W y$. $\beta = (\beta_0, \dots, \beta_p)^T$ is the nonparametric estimate of the regression function and its derivatives, $v! \hat{\beta}_v = m^{(v)}(x_0)$, $v = 0, \dots, p$. W is a diagonal matrix with $W_i = K((x_i - x_0)/h)$. X is a design matrix with (l, j) -th element as $(x_i - x_0)^{j-1}$ and $y = (y_1, \dots, y_n)^T$. The standardized residual variance is:

$$\hat{\sigma}^2(x_0) = \frac{1}{\text{tr}\{W - (X^T W X)^{-1} X^T W^2 X\}} \sum_{i=1}^n (y_i - \hat{y}_i)^2 K\left(\frac{x_i - x_0}{h}\right) \quad (A2)$$

where $\hat{y} = (\hat{y}_1, \dots, \hat{y}_n)^T = X \hat{\beta}$. To estimate the model it is necessary to choose which kind of kernel to use, what order of polynomial to use and the size of the bandwidth. Regarding the choice of kernel, there is a wide variety of different kernels to use: Gaussian, Uniform, Epanechnikov, Biweight and Triweight, to mention but a few. The choice of kernel has received less attention in the literature than the choice of bandwidth. An important branch of the literature has, however, focused on the importance of the order of the kernel. In particular, it has been shown that the bias can be reduced by choosing a kernel of sufficient high order compared to the order of the function that is estimated (see Newey, Hsieh and Robins, 2004 and McMurry and Politis, 2004).

A higher order of polynomial has a few important implications for the estimator. A higher-order polynomial reduces the bias, but this comes at the cost of increased variability. Note that the variability increases when going from an odd-order to an even-order polynomial, while the asymptotic variance is kept constant when going from an even-order polynomial to the consecutive odd-order polynomial. For this reason Fan and Gijbels (1995b) recommend using an odd-order polynomial to estimate the regression function. Ruppert and Wand (1994) show that $p - v$ should be odd, and as a consequence a second-order polynomial ($p = 2$) can be used if the purpose is to estimate the first derivative ($v = 1$) of the regression function. A disadvantage of using a higher-order polynomial is that problems of singularity could occur due to the sparseness of the data points in combination with a too-small bandwidth.

The size of the bandwidth has a similar trade-off between bias reduction and variability. A large bandwidth reduces the variance, but it comes at the cost of increased bias. A small bandwidth reduces the bias while increasing the variance. Several data-driven procedures are available for finding an optimal bandwidth. Fan and Gijbels (1995a) and Ruppert (1997) are two important references. The main idea is to choose a bandwidth that minimizes an estimated mean-squared error (MSE) function. The estimate of the variance is the same, but the estimate of the bias differs for each method. Both these methods can be used to find an optimal bandwidth to estimate the regression function as well as its derivatives. These methods can be used as a guidance to choose the bandwidth when the main objective is the *correlation curve*, but it is no guarantee that the optimal choice has been made. Nilsson and del Barrio Castro (2012) show in a simulation study that using a bandwidth optimal for the first derivative and using the median among bootstrap replications as a point estimate works well for regression functions without abrupt changes in the curves.

Selection of bandwidth

The data-driven procedure suggested by Fan and Gijbels (1995a) to find the optimal bandwidth for the second derivative is used. Before starting the procedure a short algorithm was used to avoid sparse data automatically forcing too large a bandwidth. In the C-code available at Professor J. Fan's Web page, <http://orfe.princeton.edu/~jqfan/fan/publications.html>, Fan and Gijbels (1995a) include a restriction that counts the number of effective data points. The number of effective data points has to be at least equal to the order of the polynomial used. Therefore, $|x_0 - x| < h$, at least for 'order' observations. When the procedure aims to find the optimal bandwidth for a second-order polynomial regression, the 'order' is actually 4, since it is necessary to estimate a higher-order polynomial to evaluate the bias in the estimate of the MSE. If the effective data points are too few, the loop automatically chooses a larger bandwidth until the restriction is fulfilled for the complete sample. This means that a few sparse observations could force the optimal bandwidth to be the first bandwidth that becomes possible to estimate; hence it could be too large. This is inconvenient, as the bandwidth would be influenced by a few extreme outliers. To avoid this, the same restriction as suggested in the computer code was used before initiating the procedure to find the optimal bandwidth. 'h' was set to 0.1 and observations x_0 that did not fulfil the restrictions were dropped from the sample, and the same restriction was tested again. This sequence was used until the entire sample fulfilled the restriction. Between 9 and 38 observations were dropped before initiating the program. These observations are concentrated at the bottom and top tails of the distributions, and since the method estimates a local measure it is plausible to assume that dropping the observations is harmless.

The C-code suggested the starting bandwidth to be $h_{min} = (x_{max} - x_{min}) * (order + 2.0) / n$, where x_{max} and x_{min} are the maximum and minimum values of fathers'/parents' income in the sample. With almost 40,000 observations this would be a very small value, and it would require a lot of time to reach the optimal bandwidth. The starting bandwidth for the procedure was, for this reason, set to 0.04, which, in the case of a second-order polynomial, in practice means an initial bandwidth of 0.08.

Point wise confidence intervals for the correlation curve

The correlation curve can easily be estimated with the nonparametric method described in the Appendix. It is necessary to complement this method with confidence intervals to be able to make statistical inferences based on the correlation curve. This is particularly the case if it is of interest to compare correlation curves for different populations. Nilsson and del Barrio Castro (2012) suggest bootstrapping to estimate confidence intervals and the coverage rates are found to be satisfactory. They use a wild bootstrap technique that maintains a possible heteroscedastic pattern in the data. Härdle and Mammen (1993) introduced wild bootstrapping to obtain confidence intervals for nonparametric regressions.

To obtain a bootstrap point wise confidence interval the following steps are used:

1. Estimate $\hat{m}_h(x)$ using equation (A1) with an optimal bandwidth, h , to calculate the residuals: $\hat{\varepsilon}_i = y_i - \hat{m}_h(x_i)$. A local quadratic regression ($p = 2$) is used for estimating the regression function to reduce the bias.

2. Define a new random variable ε_i^* , which is $\varepsilon_i^* = \gamma \hat{\varepsilon}_i (1 - \sqrt{5})/2 + (1 - \gamma) \hat{\varepsilon}_i (1 + \sqrt{5})/2$, where $\gamma = 1$ with probability $p = (5 + \sqrt{5})/10$ and $\gamma = 0$ with probability $1 - p$. This assures that $E\varepsilon^* = 0$ and $E\varepsilon^{*2} = \hat{\varepsilon}_i^2$.

3. Add the resampled residuals to $\hat{m}_g(x)$, where g indicates a larger bandwidth compared to h , i.e. $y_i^* = \hat{m}_g(x_i) + \varepsilon_i^*$, to obtain new observations for the dependent variable. Galindo et al. (2001) suggest the bandwidth $g = h^{(2p+5)/(2p+7)}$ when p is even.

4. Estimate $m'(x)$ and $\hat{\sigma}^2(x_0)$ using equations (A1) and (A2) for the new sample using $(x_1, y_1^*), \dots, (x_n, y_n^*)$. The results are combined as indicated in equation (1) to obtain the correlation curve. A local quadratic polynomial, ($p = 2$), is used with a bandwidth, h , optimal for estimating the first derivative.

5. Steps 2–4 are repeated R times to obtain a pointwise confidence interval based on R bootstrap replications. The percentile method is then used to find a $(1 - \alpha)$ -point wise confidence interval, where α is the chosen level of significance. Therefore, the graphs show percentile $100 \times (\alpha/2)$ and $100 \times (1 - \alpha/2)$ of all estimated correlation curves at each x_i .

Kernel

For the nonparametric estimations, a Gaussian kernel was used:

$$K(x) = X \left(\frac{x_i - x}{h} \right) = \frac{1}{\sqrt{2\pi}} \exp \left\{ -\frac{1}{2} \left(\frac{x_i - x}{h} \right)^2 \right\}$$

Figures

All figures exclude 100 observations in each tail of the income distribution of the fathers/parents. The reason for this is that the derivative can be taken to very extreme values in the extremes of the distributions.

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