

Fritsche, Ulrich; Kuzin, Vladimir N.

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Declining Output Volatility in Germany : Impulses, Propagation, and the Role of Monetary Policy

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DIW Berlin

German Institute
for Economic Research

Königin-Luise-Str. 5
14195 Berlin,
Germany

Phone +49-30-897 89-0

Fax +49-30-897 89-200

www.diw.de

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Declining Output Volatility in Germany: Impulses, Propagation, and the Role of Monetary Policy*

Ulrich Fritzsche[†] Vladimir Kuzin[‡]

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Abstract

We analyse the decline in output volatility in Germany. A lower level of variance in an autoregressive model of output growth can be either due to a change in the structure of the economy (a change in the propagation mechanism) or a reduced error term variance (reduced impulses). In Germany the decline output volatility is due to a decline in the persistence of the growth process. This is in contrast to the U.S. results. The structural change is more of a gradual nature than a sudden break. The evolution of Germany's short-term real interest rate volatility coincides with the change of the autoregressive parameter. A change in the conduct of monetary policy (the establishment of another monetary policy regime) could be part of an explanation for the change in propagation. Stochastic simulations with a New Keynesian DSGE model support our hypothesis.

JEL CLASSIFICATION: E32, C22, C51

KEYWORDS: Output, Volatility, Monetary Policy, Markov Switching Model, State Space Model, Spectral Analysis, DSGE model.

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[†]Corresponding author: German Institute of Economic Research (DIW Berlin), Königin-Luise-Str. 5, D-14195 Berlin, phone: +49 30 897 89 315, e-mail: ufritzsche@diw.de.

[‡]Statistics and Econometric Methods, Goethe-University Frankfurt, Gräfr. 78, D-60054 Frankfurt, Germany, Tel: +49 69 798 25 332, Fax: +49 69 798 23 662, e-mail: kuzin@wiwi.uni-frankfurt.de.

1 Outline

Output volatility declined in most industrialized countries over the last decades. This was not unexpected. Arthur Burns (1960) in his Presidential Address to the American Economic Association already noticed and predicted a further decline in U.S. output volatility which he labeled as being of a secular nature. He argued that a trend decline in output volatility is indeed under way due to composition effects, the steady shift to a service economy, improvements in capital markets and a higher ability to 'smooth' consumption during periods of uncertain and variable income.

Recently, several authors investigated the decline in output volatility in the U.S. economy and in other industrialized countries (Blanchard and Simon, 2001, Simon, 2001, Stock and Watson, 2002, 2003a,b, McConnell and Perez-Quiros, 2000, Faust and Doyle, 2003, Barrell and Gottschalk, 2004). Most authors offer explanations for the decline in U.S. output volatility. These explanations include changes in the conduct of monetary policy (Taylor, 1999, Stock and Watson, 2002), a reduction in inflation volatility (Blanchard and Simon, 2001, Barrell and Gottschalk, 2004), an improved inventory management (McConnell and Perez-Quiros, 2000) and several other factors - including 'good luck' or a lower intensity of shocks hitting the economy.

With the notable exception of Buch, Döpke, and Pierdzioch (2002) there is - to our knowledge - little work about this phenomenon in Germany. Our paper differs from the mentioned paper as follows: Buch, Döpke, and Pierdzioch (2002) use SNA 95 data, recalculated for West Germany by the German Statistical Office. These data were seasonally adjusted using Census X11 under standard settings by the authors and an Hodrick-Prescott-Filter was applied to analyse the change in business cycle volatility. We use long time series of seasonally adjusted GDP for West Germany (1970 to 1991) which were made officially available in August 2003 by the German Statistical Office. In contrast to the data set used in Buch, Döpke, and Pierdzioch (2002), our time series were corrected for outliers and calendar effects by the Bundesbank and the German Statistical Office. We did not apply a Hodrick-Prescott-Filter because such a strategy seemed to be too restrictive for us. Furthermore, we used other structural break tests than Buch, Döpke, and Pierdzioch (2002) and a completely different modeling strategy.

In our paper we focus first and foremost on changes in the conduct of monetary policy as the driving force of decreasing output volatility. Our main findings can be summarized as follows: There is a decline in output volatility which is mainly due to a less persistent data generating process. This change is more of a gradual nature than a sudden shift. The boom period associated with the re-unification process disturbs the shift toward a less persistent output growth regime. A decrease of the short-term real interest rate volatility goes hand in hand with the decrease in persistence of output growth. This, and the results of frequency domain analysis, support the hypothesis, that a change in the conduct of monetary policy

is responsible for the reduced volatility. A deeper investigation of this hypothesis calls for a structural model, however.

Our paper is organised as follows: First, we discuss some data properties (Section 2). In Section 3 an autoregressive framework as in Blanchard and Simon (2001) will be used to investigate the sources of Germany's volatility decrease. We use recursive estimates to detect possible changes in the process of output growth. Furthermore, the results of stability and structural break tests are reported and the dates of the breaks are investigated in section 4. In Section 5 and 6 we present the estimation results for a Markov-switching model as well as a state space model. The results support our hypothesis of a gradual shift toward less persistent growth. Section 7 uses spectral analysis to investigate at which frequency the variance diminished mostly. Section 8 establishes a state space model, where the change in the autoregressive parameter is explained by a decrease of the short-term real interest rate volatility.

Since our investigation was done in a reduced form we are interested in changes of the structural equations as well. To that end, in Section 9 we present stochastic simulation results stemming from a model proposed by McCallum (2001) to analyze the changes which might stand behind the volatility change.

A final Section 10 discusses the results and gives some theoretical considerations about the possible sources of the structural change in the output-generating process. Further research should concentrate on the changes in the structure of the propagation mechanism to clarify, if the supply side, the demand side or the change in the conduct of policy is responsible for the changed patterns. This, however, calls for the empirical investigation of structural changes in a fully specified structural model and is beyond the scope of this paper.

2 The Data

The data are quarterly real GDP values, adjusted for outliers and calendar effects and seasonally adjusted using X12-ARIMA. The whole time series is calculated according to the new SNA 95 standard for GDP calculation. From 1970 to 1990 the data are West German data, from 1991 onwards we use the data for Germany until the second quarter 2003. All data are in logs. The time series were chained using the relationship of the 1991 values of German real GDP to West German real GDP as a conversion factor. For a preliminary analysis, we applied a Baxter-King (1995) band pass filter to extract a business cycle component out of the data. First differences and the business cycle component according to the band pass filter are plotted in figure 1.

The visual inspection shows that output volatility seems to be a bit lower in the second half of the sample when measured at the business cycle frequency - especially if we take into

account that the reunification boom was an extraordinary event in German history. To get an impression about the decline in volatility, we divided the sample into two sub-samples of identical length and calculated standard deviations for the first differences as well as the Baxter-King filtered data. The results are shown in table 1 below.

In contrast to the above-cited studies about U.S. growth volatility we found no change in the volatility between the two sub-samples when measured in first differences. However there is a decrease in volatility measured at business cycle frequency.

3 The Basic Model

A decline in growth volatility can be attributed to different factors. To illustrate this argument, assume that output growth follows an autoregressive process given by:

$$\Delta y = g + a(L)\Delta y_{t-1} + \epsilon_t, \quad (1)$$

where y_t denotes the log of GDP in quarter t , Δ is the difference operator and g the underlying growth rate of output. ϵ_t is a white noise process with the standard deviation σ_ϵ , and $a(L)$ a lag polynomial. Assume further, that output growth follows a first order autoregressive process which leads to $a(L) = a$ and $\Delta y = g + a \cdot \Delta y_{t-1} + \epsilon_t$. For output volatility that yields $\sigma_Y = \sigma_\epsilon / \sqrt{1 - a^2}$, so the higher the value of a is, the higher is the standard deviation of output.¹ A change in the output volatility in that model could therefore be attributed either to changes in the intensity of shocks hitting the economy (impulses) or to changes in the autoregressive structure of output growth (propagation).² The autoregressive model can therefore be seen as a simple impulse-propagation framework and serves as a starting point for our investigation.

4 Linear Estimations and Stability Tests

In a related paper, Hess and Iwata (1997) argue, that in general an AR(1) process should be able to capture the dynamics of output growth quite well and can serve as a proxy for our

¹Without loss of generality this holds for high-order autoregressive processes as well, cf. Blanchard and Simon (2001).

²Blanchard and Simon (2001) argue that the decrease in volatility could also be influenced by the underlying growth rate, g , that affects the probability of negative growth occurrences given the other parameters. The authors argue, that the length of expansions is not independent from the underlying growth rates, because the probability of negative growth occurrences (that is, 'recessions' in their definition) increases as the underlying growth rate decreases. Because an economy - once trapped in a recession - shows a different volatility, the overall volatility is at the end not independent from the recession probability. We will focus in the following sections on changes in the autoregressive parameter and in the innovation variance only.

impulse-propagation-framework. At least in history, this process performed not worse than much more complicated non-linear formulations of the output growth process. The appropriate lag length for the German output growth process was investigated using lag selection tests. Specifically, the minima of the Akaike and Schwarz criteria up to a lag order of 24, an Ljung-Box for residual serial correlation, a Langrange multiplier test for residual serial correlation and a general-to-simple reduction test were estimated. The results - shown in table 2 - indicate that an AR(4) seems to be appropriate.

$$\begin{aligned} \Delta y_t = & \underset{(0.001)}{0.004} - \underset{(0.08)}{0.14}\Delta y_{t-1} + \underset{(0.08)}{0.04}\Delta y_{t-2} + \underset{(0.08)}{0.14}\Delta y_{t-3} + \underset{(0.08)}{0.26}\Delta y_{t-4} + \varepsilon_t, \varepsilon_t \sim N(0, \sigma^2) \\ R^2 = & 0.10, \text{ } AR(1-5) = 0.46[0.80], \text{ } ARCH(1-4) = 0.78[0.53], \\ & Normality = 5.76[0.05], \text{ } Hetero = 0.81[0.59], \\ & Hetero - X = 0.69[0.78], \text{ } RESET = 0.55[0.45] \end{aligned} \quad (2)$$

According to the reported criteria the equation is well specified with some signs of non-normality.³ In spite of the fact that some lags are not significant, we decided to use the AR(4) specification in the next sections. The specification should be flexible enough to allow for changes in the dynamics over time which we would like not to restrict prior to the investigation.

In the next stage of our investigation, we tested for structural stability in the impulse-propagation-model. We applied CUSUM and CUSUM square tests. That gave no indication of any instability. More interesting are the results of recursive estimations which are shown in figure 3. The recursive coefficients suggest that there might a 'change' in the propagation structure - the coefficient of the first lag is relatively high in the early seventies but declines steadily over time.

We tested the hypothesis of a change in the propagation structure also within a transformed version of the AR(4) model where the overall persistence is measured in one single parameter. The AR(4) model is given by:

$$\Delta y = g + \rho_1 \Delta y_{t-1} + \rho_2 \Delta y_{t-2} + \rho_3 \Delta y_{t-3} + \rho_4 \Delta y_{t-4} + \epsilon_t \quad (3)$$

The transformed representation is given by:

$$\begin{aligned} \Delta y = & g + (\rho_1 + \rho_2 + \rho_3 + \rho_4) \Delta y_{t-1} - (\rho_2 + \rho_3 + \rho_4) \Delta^2 y_{t-1} \\ & - (\rho_3 + \rho_4) \Delta^2 y_{t-2} - \rho_4 \Delta^2 y_{t-3} + \epsilon_t \end{aligned} \quad (4)$$

³We performed the following tests: serial correlation LM test, ARCH LM test, Jarque-Bera normality test, White heteroscedasticity tests with and without cross terms, RESET test.

$$\Delta y = g + \rho \Delta y_{t-1} + \phi_1 \Delta^2 y_{t-1} + \phi_2 \Delta^2 y_{t-2} + \phi_3 \Delta^2 y_{t-3} + \epsilon_t \quad (5)$$

In this specification Δ^2 stands for the second differences, i.e. $\Delta\Delta$ and ρ for the sum of the AR coefficients. The parameter ρ measures the overall persistence since it covers all AR-parameters.

This equation is of course identical to the AR(4) model. However, the recursively estimated ρ - as can be seen in figure 3 - makes clear that the overall persistence declined over time.

There is a growing literature about the detection and dating of structural breaks - especially if the exact break point is unknown; see Hansen (2001) for an excellent survey. The well-known Chow test is not helpful under such circumstances because the test is appropriate only under the assumption of a known break point. Therefore we applied the Andrews-Quandt- and Andrews-Ploberger-Tests as described in Andrews (1993) and Andrews and Ploberger (1994) to the AR(4) model and the error correction representation of the AR(4) model.

In short, these tests trim the range of the sample by 15 per cent (suggested value in Andrews and Ploberger, 1994) from each side and perform Lagrange multiplier tests for each of the possible break points for the remaining middle range of the sample. The Andrews-Quandt test uses as the test statistic the maximum of the LM statistics, while the Andrew-Ploberger test uses an exponentially weighted average. These both have non-standard distributions. Asymptotic p-values are taken from Hansen (1997).

The results - see tables 3 and 4 - indicate that a structural break can be identified in the autoregressive structure (more precisely: it is found for the AR(1) coefficient) but not in the residuals variance. This is in contrast to the results for the U.S. economy, where a break in the variance of the residuals is found by most methods (McConnell and Perez-Quiros, 2000). The breakpoint for the AR(1) coefficient is dated around 1976. For the period from 1976 onwards no further break was detected. The estimation results of the error correction representation confirm that a break occurred in the AR(1) parameter. However, the recursive coefficients also suggest that there might be a gradual change in persistence over time.

In a further exercise we used the procedure proposed by Bai and Perron (2003) - to check if there are more structural breaks.⁴ The procedure investigates all possible models under the assumption of a given number of breakpoints and a given minimum distance between the break points. Then, the 'optimal' model is chosen according to the (minimum of the) sum of squared residuals and according to information criteria. Therefore, we had to assume the number of breakpoints we would allow to occur in the model at maximum and calculated the optimal break points for each model. We opted for a maximum of four breakpoints with a data range of about thirty years. The minimum distance between two breakpoints was set equal to 6 years - as we assume stability over the cycle. For each model, the Bayesian Information Criteria

⁴We thank Tom Doan of Estima for making the RATS code available to perform the Bai-Perron-Tests.

(BIC) was calculated to check, which of the estimated breakpoint models could be seen as the best one.

The results are presented in table 5. According to the BIC criteria the model with 2 breaks shows the best fit. The breaks occurred in 1977Q2 and 1997Q1. We estimated equation (5) for the sub-samples 1970Q1 to 1977Q2, 1977Q3 to 1997Q1 and 1997Q2 to 2003Q2. The point estimates of the coefficient ρ are .48, .27, and .06 respectively. This supports both of our hypotheses: the hypothesis of a structural break in the mid-seventies as well as the hypothesis of a gradual shift in persistence. To explore this issue further we used a Markov switching and state space (time-varying coefficient) models.

5 A Markov-Switching Model

The results up to here point to the possibility, that there might have been a regime shift in volatility over time. Markov-switching models are appropriate for this kind of problems (McConnell and Perez-Quiros, 2000).⁵ In line with the results of the stability tests mentioned above, the Markov-switching version of equation (5) with a regime-dependent ρ -coefficient was estimated.⁶

$$\begin{aligned}\Delta y &= g + \rho(s_t)\Delta y_{t-1} + \phi_1\Delta^2 y_{t-1} + \phi_2\Delta^2 y_{t-2} + \phi_3\Delta^2 y_{t-3} + u_t, \\ u_t &\sim N(0, e^\gamma), \quad s_t \in \{1, 2\}\end{aligned}\tag{6}$$

where S_t denotes the realizations of the underlying unobservable discrete Markov chain. Two regimes are allowed. The transition probabilities were estimated using a logit transformation: $p_{jj} = \frac{e^{\varphi_j}}{1+e^{\varphi_j}}$. The estimation results and a graph of the corresponding smoothed probabilities can be found in table 6 and figure 4.

The results indicate, that there were two major periods, where the persistence of the data generating process was high: the early 70s and the reunification boom in the early 90s. Also the recession period of the early 80s as well after the millennium sees an increase in persistence which is however much less pronounced than the other two episodes. Output volatility is high either in very pronounced booms or recessions and low in other periods. Since we had only one of this 'extraordinary' episodes in the second half of the sample it is not astonishing that the volatility at the typical business cycle frequency is lower.

⁵A very detailed discussion of Markov-switching models and the corresponding estimation and state extraction procedures is available in Krolzig (1997).

⁶This is an MSA-model. We implicitly assume that only ρ_1 from the specification in equation (4) is changing in dependence from the regime.

6 A State Space Model

Furthermore a state space model (Hamilton ,1994) with a time-varying coefficient was estimated. The system consists of two equations: the space equation, which is the observable part of the model and the state equation, which gives some structure to the unobservable part of the model. The space equation is given by the transformed autoregressive growth model. The coefficient ρ is modeled as a random walk and defined by the state equation. The state space model (state space model I thereafter) is given by the following system:

$$\begin{aligned}\Delta y &= g + \rho_t \Delta y_{t-1} + \phi_1 \Delta^2 y_{t-1} + \phi_2 \Delta^2 y_{t-2} + \phi_3 \Delta^2 y_{t-3} + u_t \\ u_t &\sim N(0, e^\lambda)\end{aligned}\tag{7}$$

$$\rho_t = \rho_{t-1} + v_t, \quad v_t \sim N(0, e^\psi)\tag{8}$$

where the disturbance vectors u_t, v_t are assumed to be serially independent. The variance of the space and the state equation are estimated as exponential functions to restrict the variance to non-negative numbers.

The evolution of the estimated coefficient (Kalman filter result) in model I is plotted in figure 5. The estimation results of state space model I are summarized in Table 8.

As can be seen from the figure there is a decline in persistence over time until the mid-80s. The value of the respective coefficient is about .7 in the early 1970s, it declines in the course of the 80s and is about .25 at the beginning of the 90s. There is an temporary increase of the coefficient during the reunification boom. This is all in line with the results from the recursive estimates and the Markov-switching model.

7 Spectral Analysis

A helpful tool to detect the sources of the change in persistence is furthermore given by spectral analysis (Wolters and König ,1972). Analytically, the correlogram of a stationary time series can be transformed into the frequency domain using Fourier transformation. The spectra functions indicate the contribution of every frequency component to overall variance. By decomposing the overall variance into frequency portions it can be informally checked if long-run movement, business cycle fluctuations or seasonal dynamics are the driving forces of a time series' dynamics. Analysing the spectra functions is therefore a suitable instrument to find out, at which frequency the changes took place. This informal test refers to an idea of Ahmed, Levin and Wilson (2002) who used the spectra functions to investigate if the change

in U.S. growth volatility is due to 'good policy', 'good practices' or 'good luck'. They have the following hypotheses:

Characterizing the post-1984 shift in the spectrum of GDP growth is useful because each explanation can be associated with a specific pattern for the shift: (1) improved monetary policy would be expected to shift the spectrum primarily at business-cycle frequencies; (2) improved inventory management and other relevant changes in business practices would tend to be manifested at relatively high frequencies; and (3) reduced innovation variance would generate a proportional decline in the spectrum at all frequencies. (Ahmed, Levin and Wilson ,2002, p. 1f.)

In figure 6 we plot empirical spectra functions for different periods including some grid lines which define a business cycle frequency from $1 \frac{1}{2}$ to 8 years. According to our test results we splitted the sample in 1976. The empirical spectra functions are given in the first row of the graph. Critics might argue that a sample of 6 years is too short for any reasonable statement about the spectra function. Therefore we splitted the sample in the middle the overall sample and repeated the exercise -see the figures in the second row. The results are fairly robust in that sense that the spectra functions indicate that there must have been a distinctive decline of variance at the business cycle frequency.⁷

8 A State Space Model with Real Interest Rate Volatility

The results from the spectral analysis indicate that there was a decline in the low-frequency contribution to volatility. According to Ahmed, Levin and Wilson (2002) this could be due to a better managed monetary policy. For a deeper investigation of this hypothesis that the 'change in monetary policy' could be responsible for the change in volatility again a state space model was used (state space model II thereafter. In contrast to state space model I here an exogenous variable is allowed to influence the time-varying coefficient ρ_t . Specifically as a proxy of the monetary policy stance we estimated a GARCH(1,1) model for the real short-term interest rate and used the result as a measure for the volatility of monetary policy (X_t for the exogenous variable).⁸ From a preliminary visual inspection it is obvious that the decline in monetary volatility seems to coincide with the decreasing persistence of output growth, measured by the recursively estimated ρ . In figure 7 we jointly present the recursively estimated ρ from the transformed autoregressive growth model (see figure 3) and the GARCH(1,1) results for the short-term real interest rate.

⁷To estimate the spectra functions we used the source SPECTRUM.SRC in RATS 5.04 with standard settings. The window size as well as the smoothing parameters were set automatically according to the number of observations.

⁸The estimation results for the GARCH(1,1) model are available from the authors on request.

We now used these GARCH(1,1) results as an exogenous explanatory variable for the evolution of the persistence parameter ρ_t within a state space model.

The model is therefore specified as follows:

$$\begin{aligned}\Delta y &= g + \rho_t \Delta y_{t-1} + \phi_1 \Delta^2 y_{t-1} + \phi_2 \Delta^2 y_{t-2} + \phi_3 \Delta^2 y_{t-3} + u_t \\ u_t &\sim N(0, e^\lambda)\end{aligned}\tag{9}$$

$$\rho_t = \delta X_t + v_t, \quad v_t \sim N(0, e^\psi)\tag{10}$$

We present the results in figure 8 (Kalman filter results) and table 8. All coefficients are significant and the short-term real interest rate's volatility can explain the evolution of the persistence coefficient quite well. The result points into the direction of the hypothesis of Ahmed, Levin and Wilson (2002), namely that the decline in persistence might be due to a change in the conduct (or the reaction to) monetary policy. This topic will be discussed in the next sections.

9 A Theoretical Model

Up to here the result points to a steady decline of the persistence parameter ρ - which has a strong correlation with measures of monetary policy. The estimations were performed in a reduced form - so nothing can be said about the underlying structural changes. There are two results - the spectral analysis as well as the second state space model including the short-term real interest volatility - which indicate that a change in monetary policy might play a role. There are two ways to investigate that issue further: either to estimate a structural model and test within the structural equations for changes or to calibrate a theoretical model and simulate the consequences of changes in the structural parameters. We opted for the second way. Because of the difficulties involved in that the first option goes beyond the scope of this paper and will be investigated in a separate paper.

There is surely nothing new about the fact that there was a break in the conduct of monetary policy at the beginning of the 1980s. This is at least true for the United States, where Fed chairman Paul Volcker started a radical disinflation in 1979. The fact that there is a break in the conduct of monetary policy in other industrialised countries is, however, also confirmed by studies that estimated Taylor rules for other G7 countries (Clarida, Gali and Gertler, 1998). These studies point out that the monetary policy became more hawkish in that sense that central banks show more aggressive reaction toward fighting against inflation than during the heyday of Keynesian demand policy in the 1960s and the stagflationary 1970s. But how can the reduced volatility and the detected change in propagation be explained by

a change in the conduct of monetary policy? To analyse these aspects, the 'New Keynesian' (NK) model became the new workhorse in the last decade.⁹ The NK model starts from a general equilibrium model with Walrasian equilibrium. The business cycle movement of such a model could be expressed in percentage deviations from the long-run equilibrium values.

The business cycle component of output, y_t , is determined by:

$$y_t = b_0 + b_1 (r_t) + y_{t+1} + v_t \quad (11)$$

where the parameter $b_1 < 0$. Actual output is a (negative) function of the real interest rate r_t . This equation is called the inter-temporal IS equation and can be seen as being at the core of most 'modern' macroeconomic models. Output is furthermore affected by the (expected) future income as consumers intend to 'smooth' consumption over time. The term v_t stands for unforeseeable demand shocks such as unexpected changes in government consumption. In a lot of models the parameter b_1 stands for the elasticity of inter-temporal consumption (Boivin and Giannoni, 2002). As it is usually done in NK models we can assume that the central bank is able to set the real short-term interest rate. Iterating equation the inter-temporal IS equation forward, we obtain:

$$y_t = v_t + b_1 r_t^L \quad (12)$$

where

$$r_t^L = E_t \left[\sum_{j=0}^{\infty} r_{t+j} \right] \quad (13)$$

stands for the long-run real interest rate.¹⁰ The last equation states that it is the long-run interest rate which matters for the IS curve but the short-term real interest rate matters to that extent as it influences the long-run interest rate. For the monetary policy rule let's assume for a moment a simplified version of the Taylor rule which is given by:

$$r_t = \phi y_t + e_t \quad (14)$$

where $\phi > 0$.

Since y_t stands for the 'output gap' this equation simply states that the monetary authority sets the interest rate according to the deviation of the actual output from its long-run path. This does not mean, that inflation does not matter. The gap could be seen as an indicator of the (future) inflationary pressure.¹¹ Combining this yields:

⁹The section draws heavily on Boivin and Giannoni (2002). For this moment we neglect the supply side of the NK model, the 'new' Phillips curve, and focus on the IS curve and the monetary policy rule.

¹⁰Since all values are deviations from long-run equilibrium, the sum should converge.

¹¹This does also not mean that supply shocks do not matter. They are reflected in the potential output because they matter for the long-run (equilibrium) solution in these models.

$$y_t = \frac{v_t + b_1 e_t}{1 - b_1 \phi} \quad (15)$$

Since y_t is the 'gap' (or the business cycle component of output), a reduction in σ , reflecting a change in the elasticity of inter-temporal consumption or an increase in ϕ , reflecting a more aggressive monetary policy, could change the volatility of output around the long-run path. Our analysis so far could be interpreted in the NK framework as probably being associated with a higher ϕ , stemming from a change in the importance of the reaction from potential output of the Bundesbank since the middle/end of the 70s. For the investigation of that topic a fully specified structural model has to be estimated to detect, where the changes in the propagation stem from.

In the following we used a model proposed by McCallum (2001) to analyze the effects of monetary policy on output. Here, we want to explore the effects of changes in 'deep' structural parameters on output volatility. We tried to keep the model as simple as possible. The model is given by the following equations:¹²

$$y_t = b_0 + b_1 (R_t - E_t \Delta P_{t+1}) + E_t y_{t+1} + v_t \quad (16)$$

$$\Delta p_t = \beta E_t \Delta p_{t+1} + \alpha \tilde{y}_t + u_t \quad (17)$$

$$R_t = \mu_0 + (1 - \mu_3) (\mu_1 \Delta p_t + \mu_2 E_{t-1} \tilde{y}_t) + \mu_3 R_{t-1} + e_t \quad (18)$$

Equation (16) states the intertemporal IS curve. Actual output y_t depends positively on future expected income $E_t y_{t+1}$ and negatively on the (short-term) real interest rate $R_t - E_t \Delta P_{t+1}$.¹³ Equation (17) defines a forward-looking Phillips curve with Calvo price setting. Actual inflation depends on expected inflation $E_t \Delta p_{t+1}$ and the output gap $\tilde{y}_t$. Equation (18) gives a standard Taylor rule where the monetary authorities react on inflation and the output gap. Furthermore we assume interest rate smoothing, controlled by μ_3 .

These equations are accompanied by the definition equation of the output gap and some laws of motion for the stochastic terms.

¹²We used the MATLAB files available from Bennett McCallums homepage and some modified versions of these files written by Jan Gottschalk. We are grateful to Jan Gottschalk who kindly offered help to implement the files and handle the output.

¹³It is assumed that the long-term real interest rate depends on the short-term real interest rate.

$$\begin{aligned}
\tilde{y}_t &= y_t - \bar{y}_t \\
v_t &= 0 \cdot v_{t-1} + \nu_t \\
e_t &= 0 \cdot e_{t-1} + \epsilon_t \\
u_t &= 0 \cdot u_{t-1} + \psi_t \\
\bar{y}_t &= .95 \cdot \bar{y}_{t-1} + \eta_t
\end{aligned} \tag{19}$$

The model was solved using the procedure proposed by McCallum (1998) and Klein (2000). First we solved the model under the following standard parameter settings as proposed by McCallum (2001): $b_0 = \mu_0 = 0$, $b_1 = -.4$, $\beta = .99$, $\alpha = .03$, $\mu_1 = \frac{.5}{4}$, $\mu_2 = .5$, $\mu_3 = .8$. The impulse response functions to an IS shock (ν_t), an cost-push shock (ψ_t) as well as a policy rule shock (ϵ_t) are plotted in figures 9 and 10. As can be seen from the IRFs, the model captures a lot of features relevant for macro dynamics. Note that the reaction functions of this model do not create very much persistence. McCallum (2001) used habit formation and a partly backward-looking Phillips curve (so-called Fuhrer-Moore specification), to get more persistence into the model. To keep the factors of influence as limited as we can, we opted for the simplest model we could find.

In the next step, we assumed values for the variances of the different types of shocks. We again opted for the settings as proposed by McCallum (2001). The variances were set as follows: the variance of ν_t was set equal to .03, the variance of ϵ_t was set equal to .002, the variance of ψ_t was set equal to .0017, the variance of η was set equal to .007. We did stochastic simulations with the model (10000 repetitions) and saved the autocorrelation functions. Specifically, we were interested in the change of the autocorrelation function of the variable $\tilde{y}$ - the output gap. We focus on the output gap because empirically we found that changes at the business cycle frequency seem to be the driving force behind the change in persistence.

In the next step, we slightly changed some parameters of the model to see if and how the persistence changes. Specifically, we doubled the value of b_1 to -.8. In two other simulations, we doubled the values of μ_1 and μ_2 to 1. We always changed only one parameter and report the autocorrelation functions together with those from the baseline at different lags. The results are shown in figure 11. As can be seen from that figure, changes in the structural parameters change the implied persistence of the economy. A change in the elasticity of inter-temporal consumption as well as policy reaction parameters can influence the volatility of output growth.

10 Discussion

In our paper we investigated the decline in output volatility in Germany. The results from the structural break tests, the Markov-switching model as well as the state space models show that the decline is more of a gradual nature than a sudden break. Results from spectral analysis estimations as well as a state space model including short-term real interest rate volatility indicate, that monetary policy might have played a role.

However, in contrast to the US results, it is the transmission mechanism of shocks, not the variance of shocks itself which changed. The state space model II indicates that variance of shocks might interplay with the changes in the structure of the economy.

To investigate the possible sources of structural changes which might be responsible for the observed pattern, we used a calibrated DSGE model. We would interpret the results of our stochastic simulations in the following way: changes in policy reaction parameters - as reported for most industrialised countries around the late 70s - should have had an influence on output volatility. Probably these changes also influenced the interest rate sensitivity of the IS curve. This could be a typical case for a Lucas critique phenomenon because it is very plausible that a change toward another policy regime would influence the behavior of households. These changes, however, must be quite pronounced, to generate a significant fall in volatility - at least in our simple model. More complicated models with habit formation and/or more persistence in the Phillips curve could generate different result.

In a further investigation we will focus on the estimation of a fully-fledged structural model based on empirical data and investigate the changes in the propagation within this framework. This research is however beyond the scope of this paper.

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Appendix

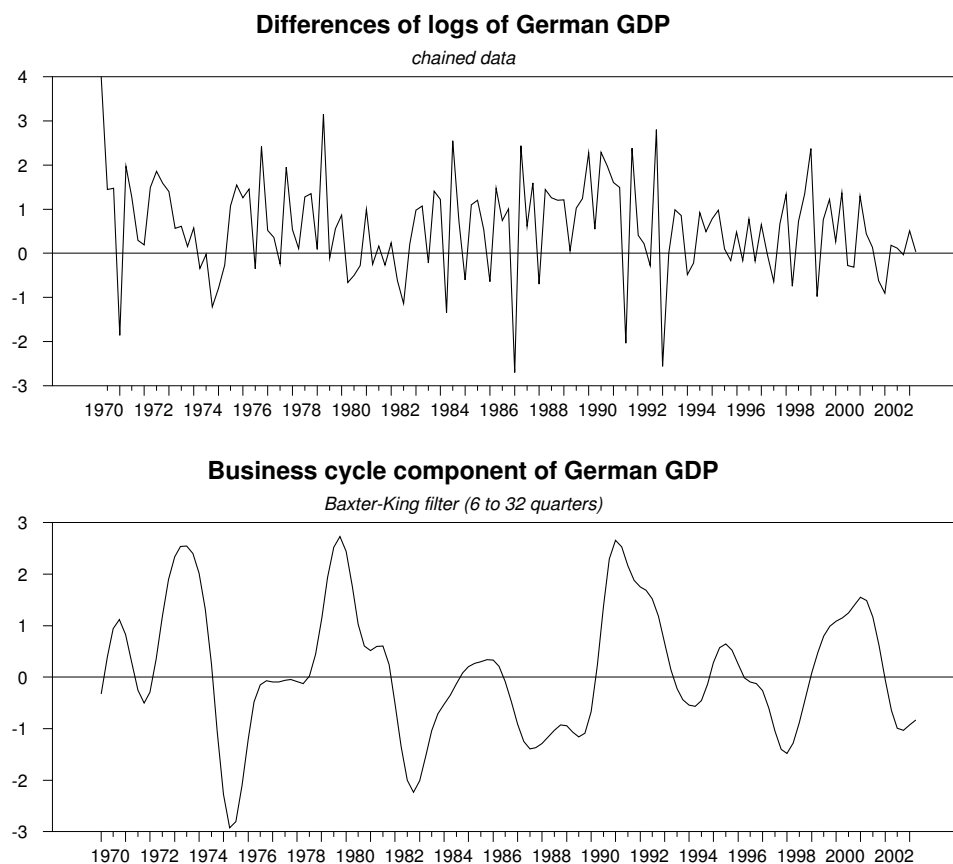


Figure 1: Data graphs

Transformation/sample	S.D.
First differences/ 1970 - 1986	4.29
First differences/ 1987 - 2003	4.38
Baxter-King filtered/ 1970 - 1986	1.32
Baxter-King filtered/ 1987 - 2003	1.13

Table 1: Standard deviations

Criterion	Suggested Lag Length
AIC	4
BIC	0
Ljung-Box-Test	4
LM Test	0
General to Simple	4

Table 2: Results of lag length tests

Variable	Break Date	Andrews-Quandt	p-value	Andrews-Ploberger	p-value
Constant	1991:02	3.26	0.50	0.37	0.55
Δy_{t-1}	1976:02	7.61	0.08	1.29	0.13
Δy_{t-2}	1991:02	3.90	0.39	0.41	0.51
Δy_{t-3}	1991:02	1.40	0.93	0.11	1.00
Δy_{t-4}	1985:02	2.60	0.64	0.41	0.58
All Coeff.	1991:02	10.85	0.44	2.58	0.61
Variance	1993:01	2.01	0.78	0.23	0.73

Table 3: Results of Andrews-Quandt-Ploberger-Test: AR(4) model [equation (3)]

Variable	Break Date	Andrews-Quandt	p-value	Andrews-Ploberger	p-value
Constant	1991:02	3.26	0.50	0.37	0.55
Δy_{t-1}	1976:02	7.61	0.08	1.29	0.13
$\Delta^2 y_{t-1}$	1976:01	3.13	0.52	0.35	0.58
$\Delta^2 y_{t-2}$	1976:04	1.04	0.99	0.16	0.87
$\Delta^2 y_{t-3}$	1985:02	3.98	0.37	0.44	0.49
All Coeff.	1991:02	10.85	0.44	2.58	0.61
Variance	1993:01	2.01	0.78	0.23	0.73

Table 4: Results of Andrews-Quandt-Ploberger-Test: AR(4) model, transformed representation [equation (5)]

Model (breaks)	Model (1)	Model (2)	Model (3)	Model (4)
Sum of Squared Residuals	129.7	100.4	92.1	85.6
BIC	5.04	4.97	5.07	5.18
Breakpoint(s)	1977Q2	1977Q2 1997Q1	1977Q2 1993Q1 1999Q1	1977Q2 1987Q1 1993Q1 1999Q1

Table 5: Results of Bai-Perron-Test: AR(4) model [equation (3)]

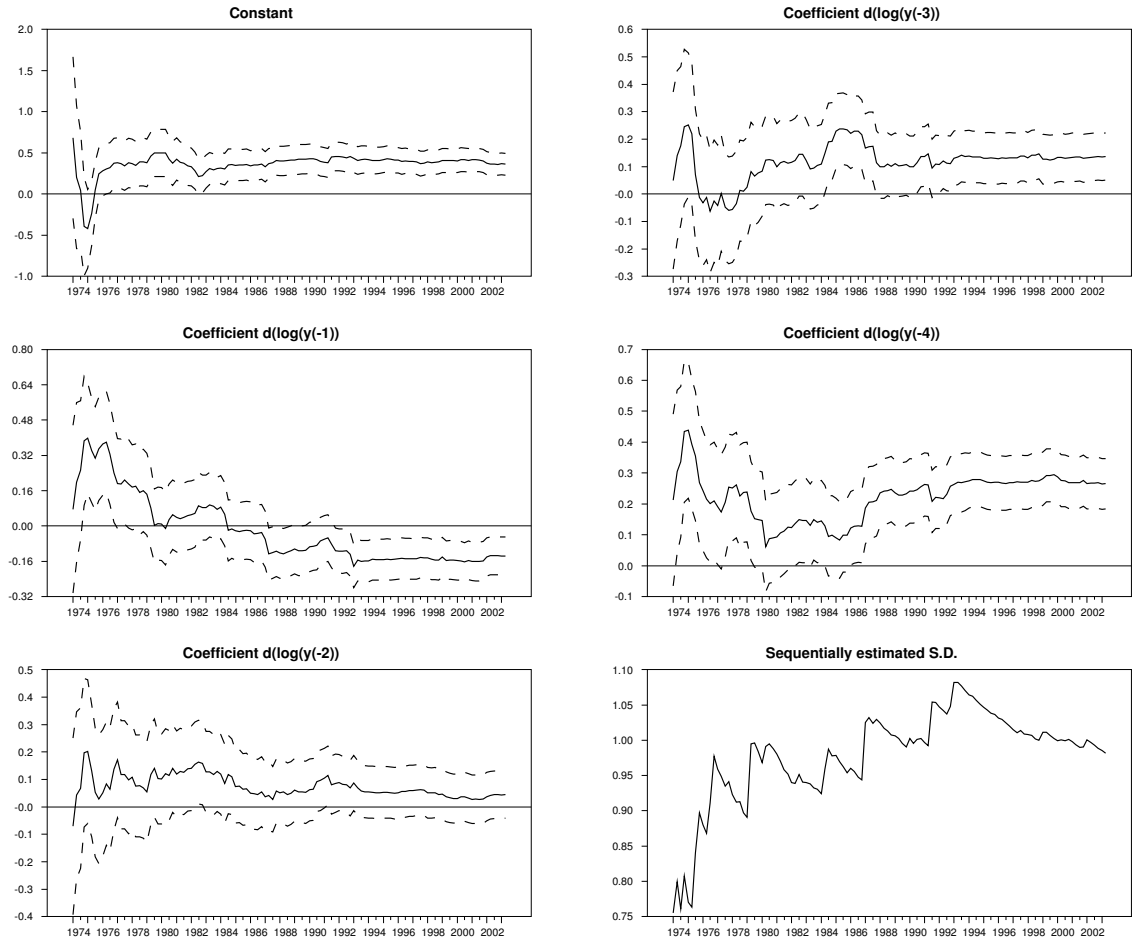


Figure 2: Recursive estimation results: AR(4) model [equation (3)]

Coefficient	Value	Std. Error
g	0.004	0.001
$\rho(s_t = 1)$	0.61	0.21
$\rho(s_t = 2)$	-0.005	0.21
ϕ_1	-0.36	0.16
ϕ_2	-0.39	0.12
ϕ_3	-0.28	0.08
γ	-9.42	0.14
p_{11}	0.89	—
p_{22}	0.94	—
$\log L(\hat{\theta})$	417.16	—
AIC	-6.33	—

Table 6: Estimation results of the Markov switching model [equation (6)]

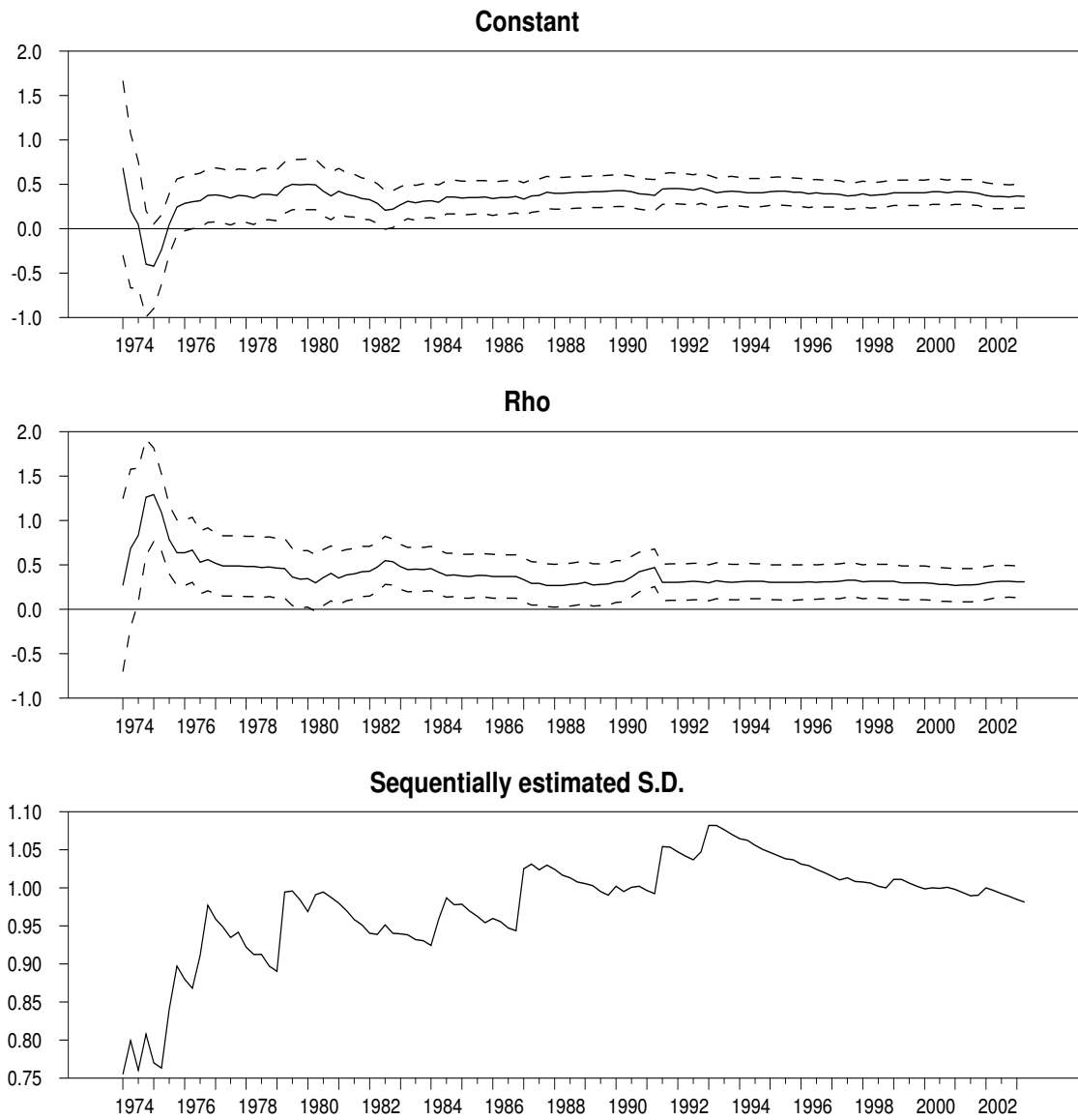


Figure 3: Recursive estimation results: AR(4) model, transformed representation [equation (5)]

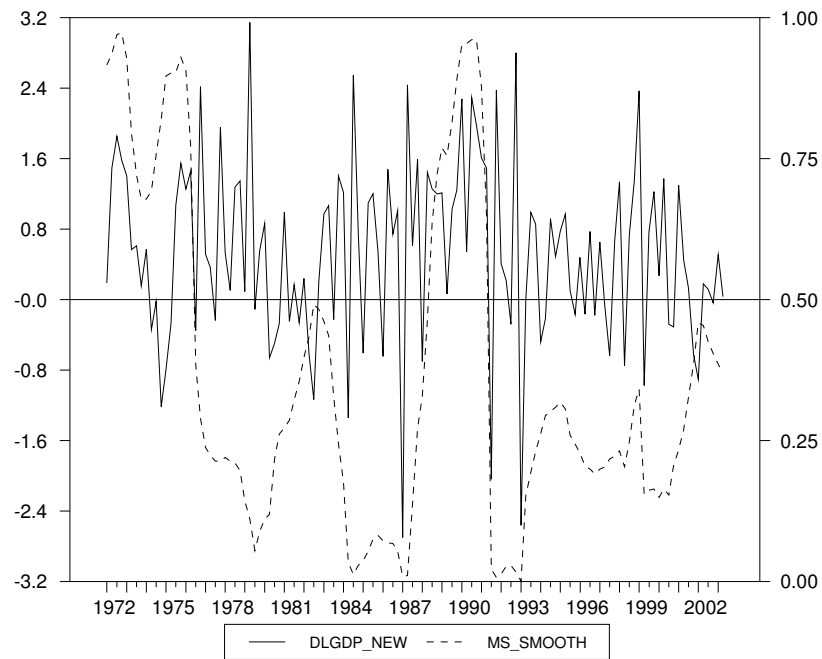


Figure 4: Markov-Switching Results: GDP Growth and High Persistence Regime Probability [equation (6)]



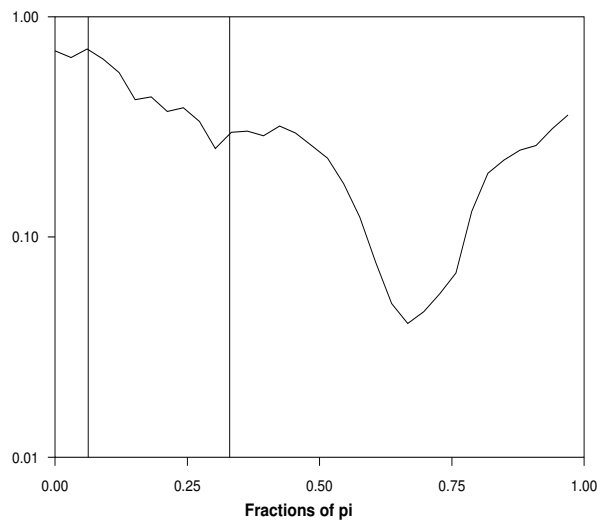
Figure 5: State space model I: filtered estimate [equation (7)]

	Coefficient	Std. Error	z-Statistic	Prob.
g	1.47	0.58	2.52	0.012
ϕ_1	-0.43	0.15	-2.81	0.005
ϕ_2	-0.40	0.13	-3.05	0.002
ϕ_3	-0.27	0.08	-3.22	0.001
λ	2.68	0.11	23.42	0.000
ψ	-7.47	1.99	-3.76	0.000
	Final State	Root MSE	z-Statistic	Prob.
ρ_t	0.25	0.16	1.59	0.112
Log likelihood	-367.60	Akaike info criterion		5.79
Parameters	6	Schwarz criterion		5.93
Diffuse priors	1	Hannan-Quinn criter.		5.85

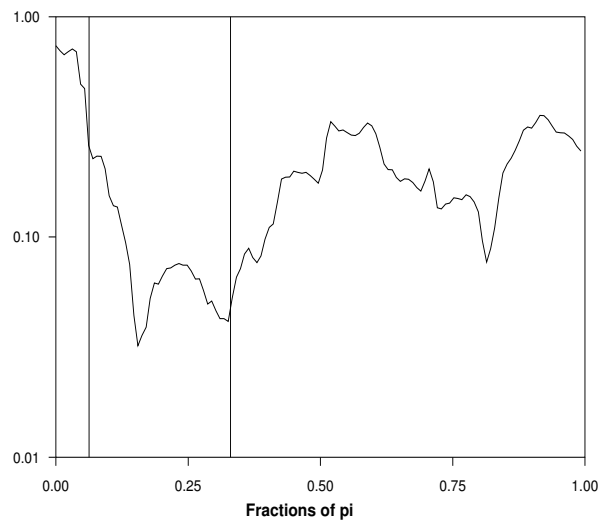
Table 7: Estimation results: state space model I [equation (7)]

	Coefficient	Std. Error	z-Statistic	Prob.
g	1.55	0.43	3.59	0.000
ϕ_1	-0.37	0.10	-3.58	0.000
ϕ_2	-0.36	0.11	-3.27	0.001
ϕ_3	-0.25	0.08	-3.21	0.001
λ	2.57	0.16	16.29	0.000
δ	0.30	0.12	2.62	0.009
ψ	-2.84	1.28	-2.22	0.026
	Final State	Root MSE	z-Statistic	Prob.
ρ_t	0.10	0.24	0.42	0.67
Log likelihood	-357.84	Akaike info criterion		5.75
Parameters	7	Schwarz criterion		5.90
Diffuse priors	1	Hannan-Quinn criter.		5.81

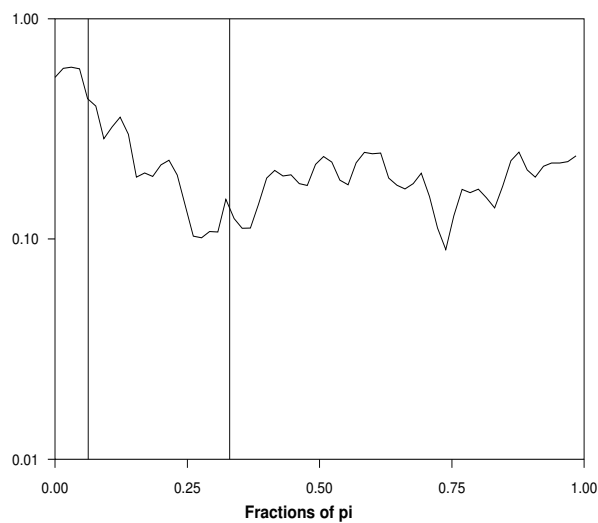
Table 8: Estimation results: state space model II [equation (9)]



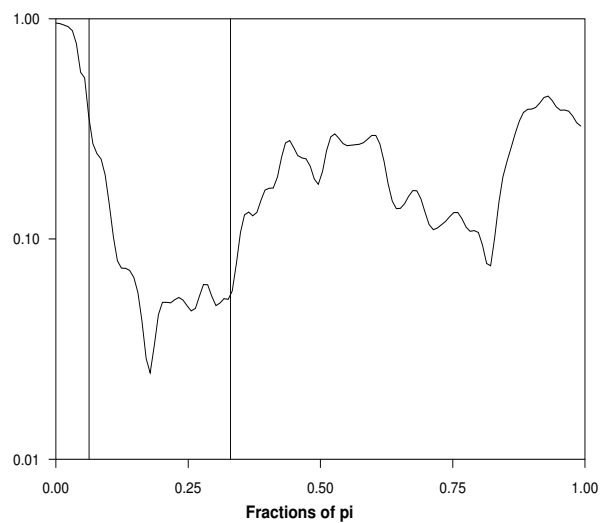
(a) Spectrum: sample 1970 to 1976



(b) Spectrum: sample 1976 to 2003



(c) Spectrum: sample 1970 to 1985



(d) Spectrum: sample 1986 to 2003

Figure 6: Spectral density estimates: different sub-samples

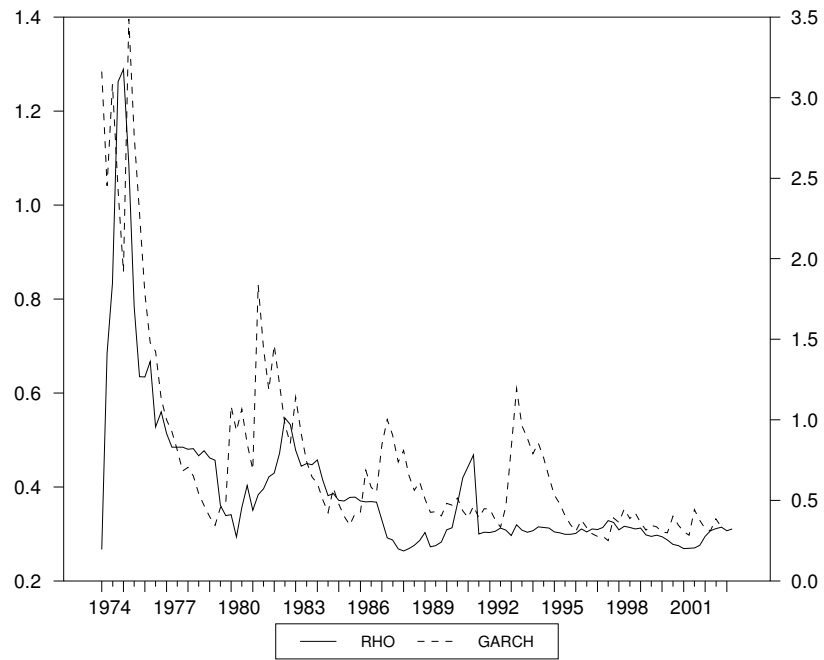


Figure 7: Recursively estimated ρ coefficient [equation (3)] and GARCH(1,1) results

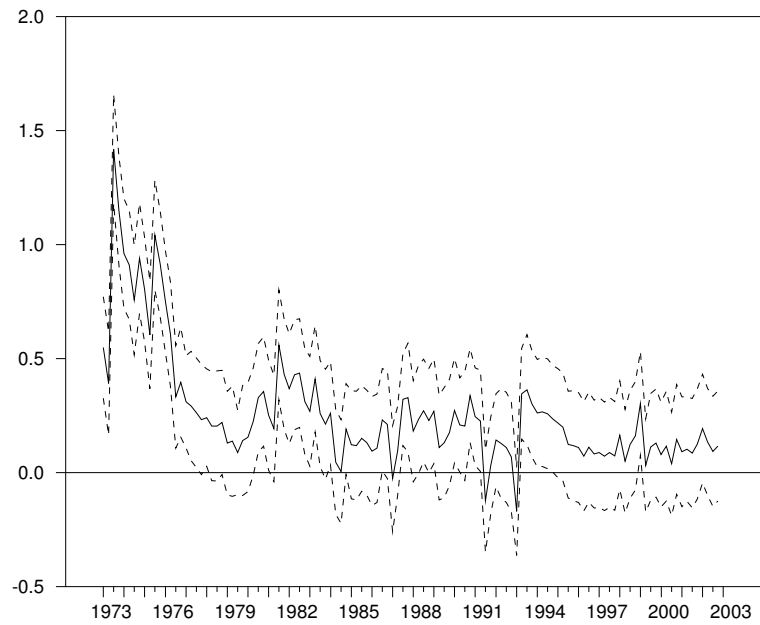
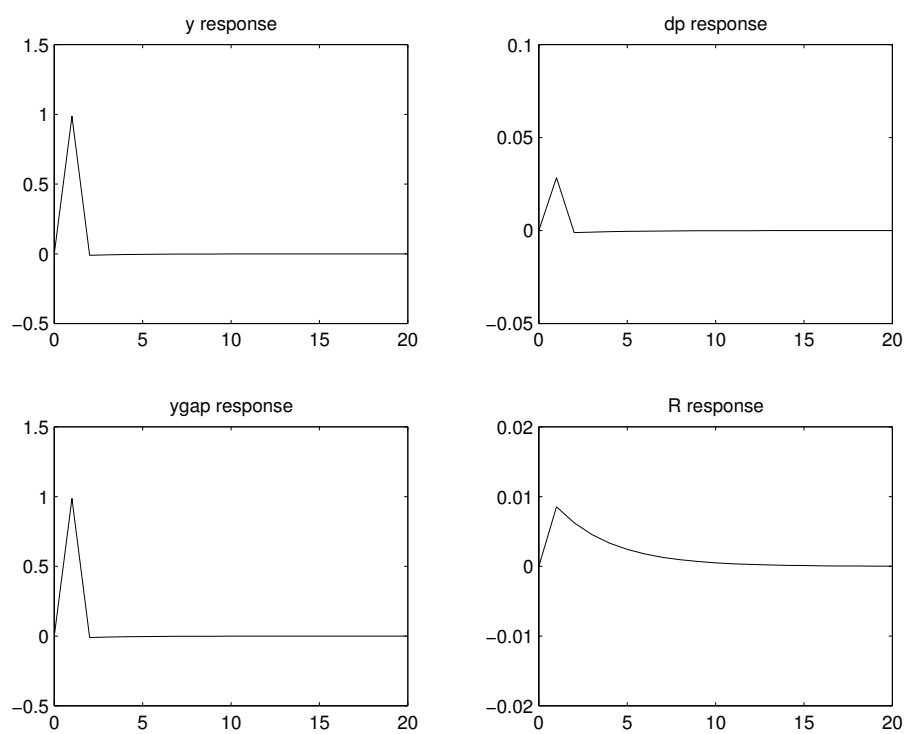
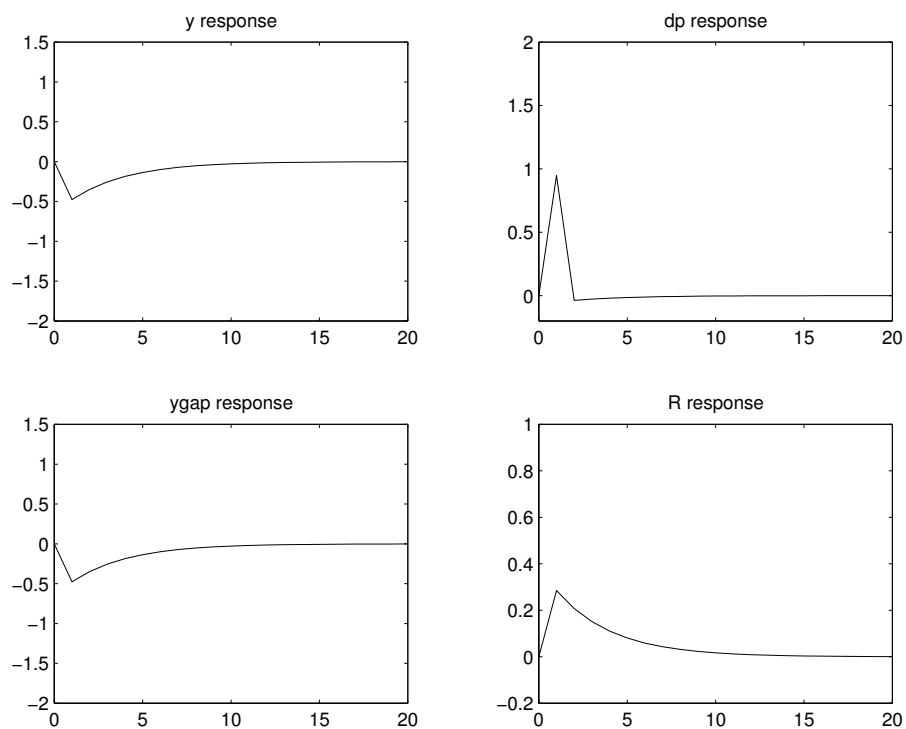


Figure 8: State space model II: filtered estimates [equation (9)]



RESPONSES TO IS SHOCK



RESPONSES TO COST-PUSH SHOCK

Figure 9: Impulse responses: theoretical model

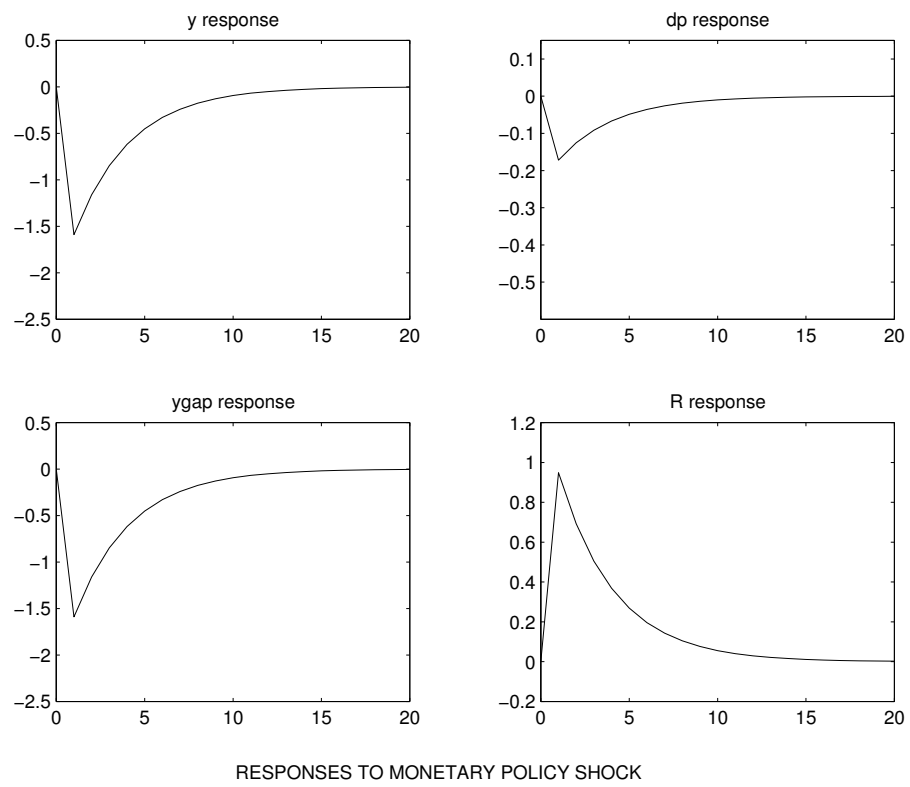


Figure 10: Impulse responses: theoretical model contd.

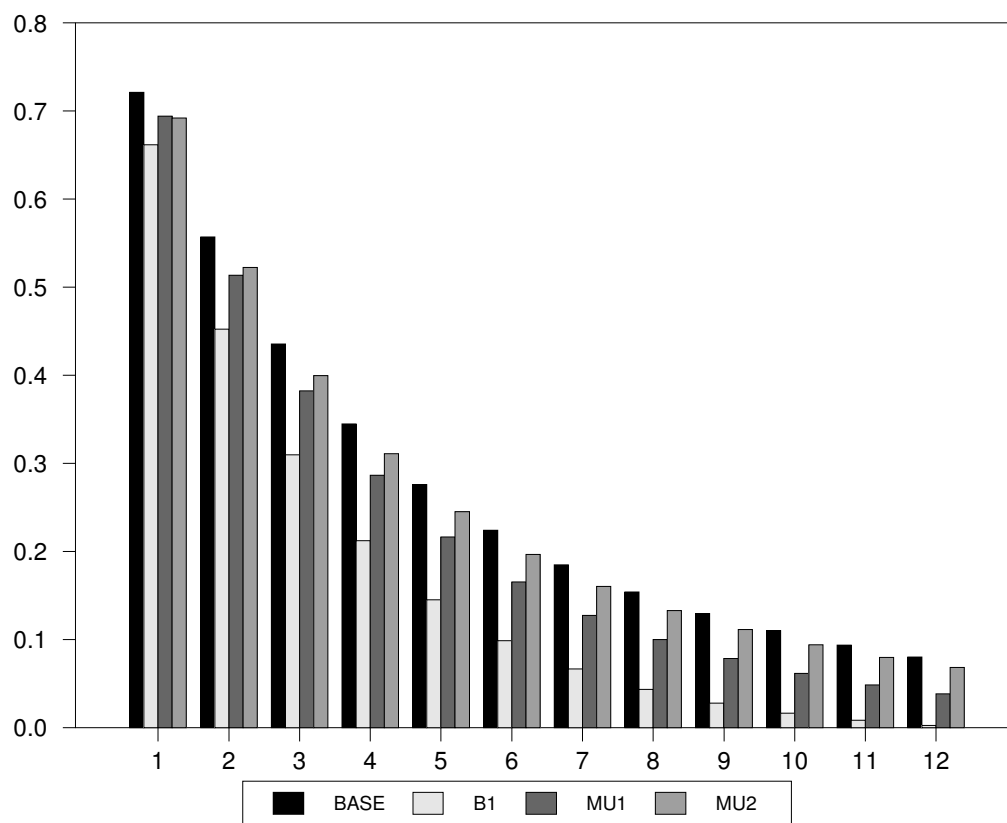


Figure 11: Autocorrelation of output gap under different parameter values at different lags