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Working Paper

Detrending and financial cycle facts across G7 countries: Mind a spurious medium term!

ECB Working Paper, No. 2138

Provided in Cooperation with:

European Central Bank (ECB)

Suggested Citation: Schüler, Yves S. (2018) : Detrending and financial cycle facts across G7 countries: Mind a spurious medium term!, ECB Working Paper, No. 2138, ISBN 978-92-899-3243-1, European Central Bank (ECB), Frankfurt a. M., <https://doi.org/10.2866/28808>

This Version is available at:

<https://hdl.handle.net/10419/179353>

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EUROPEAN CENTRAL BANK
EUROSYSTEM

Working Paper Series

Yves S. Schöler Detrending and financial cycle facts
across G7 countries:
mind a spurious medium term!

No 2138 / March 2018

Abstract

I show that the detrending of financial variables with the Hodrick and Prescott (1981, 1997) (HP) and band-pass filters leads to spurious cycles. I find that distortions become especially severe when considering medium-term cycles, i.e., cycles that exceed the duration of regular business cycles. In particular, these medium-term filters amplify the variances of cycles of duration around 20 to 30 years up to a factor of 204, completely cancelling out shorter-term fluctuations. This is important because it is common practice, and recommended under Basel III, to extract medium-term cycles using such filters; e.g., the HP filter with a smoothing parameter of 400,000. In addition, I find that financial cycle facts, i.e., differing amplitude, duration, and synchronisation of cycles in financial variables relative to cycles in GDP, are robust. For HP and band-pass filters, differences to GDP become marginal due to spurious cycles.

Keywords: Macroprudential policy · Detrending · Spurious cycles · Financial cycles · Credit-to-GDP gap

JEL-Codes: C10 · E32 · E44 · E58 · G01

NON-TECHNICAL SUMMARY

The recent global financial crisis has led to a broad consensus that microprudential, monetary, fiscal, or other policies may not always assure financial stability, indicating the need to adopt macroprudential policy. Macroprudential policy addresses the time series and cross-sectional dimensions of systemic risk.¹ Within the time series dimension, macroprudential policy aims to limit the build-up and correction phases of ebullient cycles in financial variables, which are often accompanied by financial recessions, i.e., recessions that occur in tandem with banking crises. Thus, the expansionary and contractionary phases, or cycles, of financial variables are at the centre of macroprudential policy-making.

Financial variables, however, are trending; a feature that masks possible cycles. In the business cycle context, the variables of interest are trending as well. Here, it is common practice to decompose the trending variables, such as real output, into a secular (or trend) component and a non-trending, i.e., stationary, component that potentially shows cyclical behaviour. Researchers and practitioners in the financial cycle context have taken a similar approach. However, in contrast to research on business cycles, studies have stressed that financial cycles are of longer duration, i.e. lasting up to 30 years, where eight years is regarded as the usual maximum duration of a business cycle. Further, Basel III regulations advise considering medium-term cycles of the credit-to-GDP ratio to guide the rates of countercyclical capital buffer (CCyB) by mechanically employing a Hodrick and Prescott (1981, 1997) (HP) filter with a smoothing parameter of 400,000. The extraction of such medium-duration cycles, however, is non-standard in the business cycle context and, thus, has not been debated by the previous literature.

The current study fills this gap by providing insights on the effects of different methods of detrending on financial variables, among others, considering the extraction of medium-term cycles. Further, using various methods of detrending, I revisit the question of whether cycles in financial variables are indeed marked by different characteristics than business cycles. Such evidence can serve as an important argument for a complementary role of macroprudential policy to other macroeconomic policies that mainly target the business cycle. Put differently, robust differences would substantiate the argument that, for example, monetary policy may not be able to efficiently stabilise both the business and financial cycle.

Findings suggest that the HP and the Baxter and King (1999) (BK) filters induce artificial boom-bust phases, i.e., spurious cycles, into financial but also business cycle variables. The negative consequences of spurious cycles are particularly stark when extracting medium-term cycles, for example, using the HP filter with a smoothing parameter of 400,000. These results also hold for band-pass filters in general, e.g., the Christiano and Fitzgerald (2003) filter. At a quarterly sampling frequency, extracting medium-term cycles with the HP or with band-pass filters strongly emphasises a small frequency range that

¹Systemic risk can, for example, be defined as “the risk that financial instability becomes so widespread that it impairs the functioning of a financial system to the point where economic growth and welfare suffer materially” (European Central Bank, 2009, p. 134).

cancels out other, possibly relevant, fluctuations. I show that this amplification strongly biases inference, for example, when analysing the synchronisation of cycles across countries. Note that extracting cycles at business cycle frequencies also distorts by amplifying specific frequencies, but to a much lesser extent and, hence, leads to a smaller bias in inference.

In spite of evidence on spurious cycles, financial cycle facts, i.e., differing properties of financial variables relative to GDP, are found to be robust to the method of detrending. Differences only become marginal when considering the HP and BK filters.

Three main policy conclusions may be drawn from this study. First, caution needs to be exercised when analysing extracted medium-term cycles, as for instance suggested in Basel III. The strong amplification of a small range of cycles cancels shorter-term frequencies that could be potentially relevant, say, in signalling the build-up of imbalances prior to systemic banking crises or the abrupt risk materialisation thereafter. Also if the frequency of financial crises increases, build-up phases of imbalances will not be visible when focussing exclusively on a very specific medium-term frequency range. Hence, there is a high risk that the recommended credit-to-GDP gap will misguide the setting of the CCyB rate. Second, assuming the same HP smoothing parameter or BK frequency window across different countries, means that relevant country-specific fluctuations are likely to be missed. While the US Basel credit-to-GDP gap indicates imbalances before the savings and loan crisis and the global financial crisis, the emphasis of such medium-term frequencies does not necessarily imply that Basel credit-to-GDP gaps signal systemic banking crises for other countries as well – rather the opposite: the strong amplification of medium-term cycles is prone to miss fluctuations of relevance for other countries. The same argument also holds for studies researching on business cycles that assume similar detrending specifications across countries; however, the risk of missing relevant fluctuations is greater when considering medium-term cycles. Third, differing empirical properties of financial and business cycle variables make a strong case for macroprudential policy possibly taking a complementary role to other macroeconomic policies that primarily target business cycles.

1 INTRODUCTION

The analysis of the expansionary and contractionary phases, or cycles, in financial variables has become critical to inform about the build-up of imbalances in the financial sector. One example is the Basel III credit-to-GDP gap whose cycles guide the setting of countercyclical capital buffers (CCyBs), as the different phases are claimed to inform about excess aggregate credit growth.² Here, the identification of cycles relies on the detrending of the credit-to-GDP ratio with a Hodrick and Prescott (1981, 1997) filter using a smoothing parameter of 400,000 (HP (400000)), where 1,600 (HP (1600)) is the commonly employed parameter, for instance, when detrending business cycle indicators. The large parameter is motivated by results that fluctuations exceeding the duration of regular business cycles, or medium-term cycles, are important for describing the movements in financial variables; for instance, in signalling financial crises or when compared to business cycle indicators.³ Due to this reason, various detrending approaches have already been considered for identifying the expansionary and contractionary phases in financial variables.

The purpose of this paper is to explore the consequences of these different detrending approaches for the analysis of the expansionary and contractionary phases in financial variables. Such analysis can be motivated by previous studies in the context of business cycles. On the one hand, research has stressed that HP and band-pass filters may generate spurious cycles, in which case, for instance, the duration of expansionary and contractionary phases is strongly determined by a priori chosen parameters (Harvey and Jaeger (1993); King and Rebelo (1993); Cogley and Nason (1995); A'Hearn and Woitek (2001); Pederson (2001); Murray (2003); Hamilton (2017)). On the other hand, studies indicate that different detrending procedures lead to different business cycles facts (Canova (1998a,b); Burnside (1998)). Recent studies suggest that cycles in financial variables relative to cycles in GDP differ in amplitude, duration, and synchronisation (e.g., Claessens, Kose and Terrones (2011, 2012), Aikman et al. (2015), or Schüller et al. (2015, 2017)). The robustness of these financial cycle facts is critical to consistently inform the use of macroprudential policies, as, for instance, the setting of the CCyBs.

My results indicate that the detrending of financial variables across G7 countries with HP and band-pass filters leads to spurious cycles, resulting, for instance, in similar durations of cyclical phases across countries and variables. This calls into question the “one specification of HP or band-pass filters fits all countries” approach, as, for example, recommended in Basel III or when constructing output gaps for several countries. For instance, while the HP (1600) filter may be considered appropriate for the US, as I find that the length of the detrended component roughly coincides with the estimate of the NBER’s business cycle dating committee (i.e., 6.3 versus 5.8 years), 6-year business cycles across all G7 countries seems to be implausible, given different histories, laws, and institutions or as reported by

²See Basel Committee on Banking Supervision (2010). “Guidance for National Authorities Operating the Countercyclical Capital Buffer”, December.

³ See, for example, Borio and Lowe (2002, 2004) or Schularick and Taylor (2012); Drehmann, Borio and Tsatsaronis (2012); Behn, Detken, Peltonen and Schudel (2013); Borio (2014); Hiebert, Klaus, Peltonen, Schüller and Welz (2014); Aikman, Haldane and Nelson (2015); Schüller, Hiebert and Peltonen (2015); Strohsal, Proaño and Wolters (2015a,b); Schüller, Hiebert and Peltonen (2017); Rünstler and Vlekke (2016); Stremmel (2015); Galati, Hindrayanto, Koopman and Vlekke (2016); Verona (2016); Anundson, Gerdrup, Hansen and Kragh-Sørensen (2016).

empirical analyses (e.g., Jordà, Schularick and Taylor (2017)).⁴

Further, I find that the distortions of HP and band-pass filters are much stronger when extracting medium-term cycles instead of business cycle fluctuations. Extracting medium-term cycles amplifies the variance of cycles of duration around 20 to 30 years by a factor of up to 204, completely cancelling out shorter-term fluctuations. Using the common business cycle specification of filters, the amplification of certain cycles is only by a factor of up to 18. This result is important as medium-term filtering is common practice (e.g., Borio and Lowe (2004); Drehmann et al. (2012); Behn et al. (2013); Borio (2014); Meller and Metiu (2015, forthcoming); Stremmel (2015); Anundson et al. (2016); Bauer and Granziera (2016)) and recommended under Basel III. The strong amplification cancels out shorter-term frequencies, which are potentially relevant, say, in signalling the build-up of imbalances prior to systemic banking crises or the abrupt risk materialisation thereafter.⁵ Also, if the frequency of financial crises increases, build-up phases of imbalances will not be visible when focussing exclusively on a very specific medium-term frequency range.

At last, in spite of spurious cycles I observe that financial cycle facts, i.e., the differing properties of financial variables relative to GDP, are broadly robust with respect to several detrending procedures. For HP and band-pass filters, differences to GDP become marginal due to spurious cycles. Robust financial cycle facts substantiate the view of a possibly complementary role of macroprudential policies to other macroeconomic policies that primarily target business cycles. Moreover, robust financial cycle facts should serve to ground the validity of calibrated macro-financial models.

I begin this study by discussing examples that provide intuition on the consequences of spurious medium-term cycles. The intuition is then substantiated by offering insights, first, from a theoretical perspective in the frequency domain, and, second, from an empirical analysis of detrended financial and business cycle variables. As methods of detrending, I use two specifications of difference filters (first and fourth differences), two of the HP filter (smoothing parameter 1,600 and 400,000), and two of the Baxter and King (1999) (BK) filter (frequency window 1.5 to 8 years and 8 to 30 years; denoted by (1.5,8) and (8,30)) that are commonly applied in studies researching on business and financial cycles. In the theoretical exercise, I consider their effects on trend and difference stationary (TS and DS) data generating processes (DGPs) that have been discussed as major candidates for explaining the trends in macroeconomic times series.⁶ In the empirical exercise, I apply these methods of detrending to credit, credit-to-GDP, house prices, equity prices, and bond prices as well as to GDP of G7 countries from 1969Q1 until 2013Q4. After visual inspection of the (log-) levels and the detrended components, I test for unit roots in financial and business cycle variables to provide arguments in favour of TS or DS time series processes. The effects of filters are discussed by considering the amplitude and duration of cycles in the detrended components through standard deviations, first-order autocorrelations, and spectral densities. Further, I compare the synchronisation of the detrended components across countries

⁴5.8 years refers to the NBER estimate of average cycle duration from 1945-2009 considering trough to trough.

⁵Studies on financial crises prediction accommodate the latter point, for instance, by excluding periods during and after financial crises (see Behn et al. (2013); Anundson et al. (2016)).

⁶See Nelson and Plosser (1982); Perron (1989); Zivot and Andrews (1992); Ben-David and Papell (1995); Cheung and Chinn (1997); Diebold and Senhadji (1996); Murray and Nelson (2000); Darne and Dieboldt (2004); Vougas (2007).

on the basis of pairwise correlations and a novel spectral approach that I call dynamic power cohesion (DPCoh). DPCoh complements an analysis of correlations across countries by, on the one hand, uncovering the frequencies that add strongly to overall correlation, and on the other, discriminating between frequencies that contribute positively and negatively to overall correlation.

I base the conclusion that HP and BK filters induce spurious cycles in financial variables (and GDP) on the following: I show that the distortions of HP and BK filters under a DS process – the process, under which it is known that HP and BK filters induce spurious cycles – are the ones found in the empirical exercise. That is, assuming a DS process, theory indicates that a detrended component is characterised by cycles of duration close to 7 years for HP (1600) and BK (1.5,8) filters, around 20 years for the BK (8,30) filter, and close to 30 years for the HP (400000) filter. Further and without assuming any DGP, my empirical exercise reveals that these cycle durations are closely matched by the actual detrended components, irrespective of the country or variable. Clearly, given the different variables (credit, credit-to-GDP, house prices, equity prices, bond prices, and GDP) but also the different histories, laws, and institutions of G7 countries, similar-duration cycles reflect strong evidence of spurious cycles, even if the true underlying DGP is unknown. Still, unit root tests favour a DS process, as the null hypothesis of a unit root cannot be rejected in most variable cases. Next to similar-duration cycles, I also find that the strong amplification of medium-term frequencies of medium-term filters under a DS process is consistent with my empirical results.

The first and fourth difference filters do not suffer from such distortions. Applying these, there is clear evidence of *longer* (or more *persistent*) cycles in credit, credit-to-GDP, house prices, and bond prices than in GDP; e.g., around 15 years for credit versus 6 years for GDP, on average across G7 countries. Equity price cycles have rather similar durations to business cycles. Further, I find different durations of cycles across countries and variables. In the case of HP and BK filters, the durations of cycles are distorted towards the expected lengths given a DS time series. Here, longer financial cycles are still apparent, but differences to GDP become marginal. For instance in case of the HP (1600) filter, my results suggest that on average GDP cycles are 6.2 years while credit cycles 7.4 years. I show that the *synchronisation* of cycles in credit, credit-to-GDP, and house prices is more dispersed across countries and, on average, weaker than that of cycles in GDP, but stronger for cycles in equity and bond prices. Using DPCoh, I find that the weaker synchronisation of cycles in credit and credit-to-GDP across countries relates to medium-term fluctuations. For some country pairs, these cycles are negatively related, cancelling out positively related cycles at other frequencies and consequently inducing weaker overall synchronisation. Finally, higher *amplitude* of financial variables relative to GDP is found for all methods of detrending.

This paper contributes to research on spurious cycles by pointing out the strong amplification of cycles around 20 to 30 years when extracting medium-term frequencies with HP and band-pass filters. Further, I provide first cross-country evidence on spurious cycles using HP and band-pass filters, for a series of variables. Here, the study by A'Hearn and Woitek (2001) is closest. The authors, as well, explore the possibility of spurious cycles in a cross-country setup. However, they do not find any evidence, which is due to their yearly sampling frequency and the consideration of business cycle frequencies that

only lead to small distortions.⁷ This paper also relates to a recent study by Hamilton (2017), in which he argues that one should never use the HP filter, as among others, the typical economic time series is best approximated by a random walk, i.e., a DS time series. My paper extends his findings, first, by providing evidence that band-pass filters are subject to a similar criticism as the HP filter and, second, by providing evidence that also for a broad set of countries his conjecture about the typical economic times series appears to hold.

Additionally, this paper contributes to the emerging strand of literature analysing the properties of financial variables, for instance, relative to the characteristics of business cycle variables, as e.g., Claessens et al. (2011, 2012) or Aikman et al. (2015). First, I show that financial cycle facts, i.e., the characteristics of financial variables to similarly detrended GDP, are broadly robust with respect to several filtering procedures. Second, my results provide evidence that the weak synchronisation of credit and credit-to-GDP cycles (see Schüler et al. (2017)) is partially driven by opposing medium-term developments. This is essential to better understand reciprocities across borders in the short- and long-run and, thus, potential secondary effects of country-specific macroprudential policies. Economically, the existence of such opposing cycles could be related to different degrees of financial market liberalisation across countries, say, in terms of mortgage credit standards (see Favilukis, Kohn, Ludvigson and Van Nieuwerburgh (2013)), which can be ascribed to medium-term developments. Finally, my findings suggest that financial variables, except for bond prices, are rather characterised by stochastic trends. Different natures of trends have direct implications not only for detrending, but also for the modelling of such variables. That is, in the case of TS financial variables, shocks to the latter are small, infrequent, and have only transitory effects. In contrast to this, in the case of DS financial variables, shocks to these indicators are large, frequent, and highly persistent. This has major implications for the conduct and evaluation of macroprudential policies. It is only in the case of a DS process that the modelling and identification of the shocks becomes critical (see Murray and Nelson (2000)).

The structure of the paper is as follows: In Section 2, I briefly exemplify the consequences of spurious cycles for empirical analyses. In Section 3, I introduce the methods of detrending and shed light on their effects on TS and DS time series. Section 4 applies these filters to data of G7 countries, starting with the visual inspection and formal unit root testing of the series, followed by a discussion of amplitude, length, and finally synchronisation both from a time and frequency domain perspective. Section 5 concludes.

2 CONSEQUENCES OF SPURIOUS MEDIUM-TERM CYCLES

To illustrate the consequences of spurious medium-term cycles, I provide two examples in this section. First, I construct gaps using different HP filter specifications on simulated data, and second, I discuss

⁷For instance, researching cycles between 2 years, the minimum frequency available using yearly data, and 15 years, means considering the region π to $\frac{\pi}{7.5}$ for yearly data and $\pi/4$ to $\pi/30$ for quarterly data. The latter region, i.e., using quarterly data, is located closer to the trend (closer to frequency 0) that is more prone to the distortions discussed in the paper. Specifically, as can be seen in the Figure 2 of A'Hearn and Woitek (2001, p. 327), the distortion visible in the power transfer function is much more modest than the ones discussed in this paper, which is related to the sampling frequency. The peak of their power transfer function of the HP (100) filter is around 3.2, while it is around 204 for the HP (400000). For their BK filter ($K = 6$) the peak of the power transfer function is below 1.2, while 120 for the BK (8,30) filter (see Section 3).

the consequences of spurious medium-term cycles for the credit-to-GDP gap in the case of the US and France. In both examples, I discuss the distortions of filters that, on the one hand, are in line with the empirical results of this paper and, on the other hand, can be motivated under a DS DGP.

2.1 Simulated data

The HP-filtered gaps extracted from the simulated data and the true gap itself are shown in Figure 1. The upper panel depicts the true gap, the lower left panel illustrates the HP (1600) gap (together with the true gap), and the lower right panel shows the HP (400000) gap (along with the true and the HP (1600) gap). The data is simulated from an autoregressive model fitted to the changes in the US credit-to-GDP ratio to capture realistic dynamics of financial variables in the true gap. Thus, in this exercise assume that the US credit-to-GDP ratio is a difference stationary process. I simulate 180 observations, which is similar to the sample period available for this paper.⁸

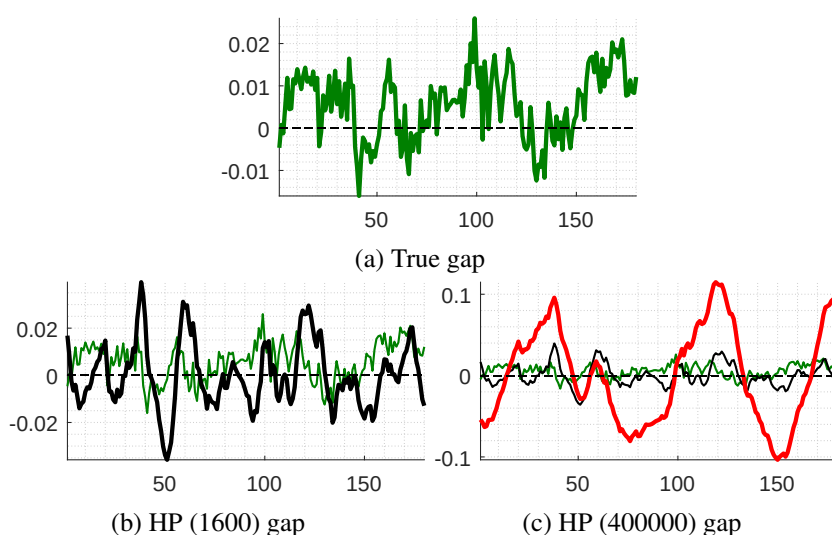


Figure 1: Simulated data

Notes: The HP-filtered gaps are obtained by detrending the level of the simulated data with smoothing parameters 1,600 and 400,000 respectively. I simulate 180 observations; similar to the sample period available for this study. For further details, please see Appendix A.1.

The amplification of specific cycle frequencies (spurious cycles) can be noticed via the relative increase in the variance of the HP filtered gaps, where the HP (400000) gap has the highest variance and the true gap the lowest variance. For instance, the overall variance of the HP (400000) gap is more than 18 times larger than the overall variance of the HP (1600) gap. This is broadly in line with the theory that predicts a maximum factor of amplification of a small frequency range of roughly 13 for the HP (1600) filter and about 204 for the HP (400000) filter. In the first case, cycles of length around 30 observations are most strongly amplified and in the second case frequencies close to 120 observations are most strongly amplified. Note that the longest cycle observed for the HP (400000) gap is actually around 80 observations, indicating that this reflects the longest duration cycle in the simulated data.

As Figure 1 suggests, the amplification implies that shorter frequencies become relatively muted, leading to distortions that are stronger when considering the HP (400000) filter. Or, put differently,

⁸See Appendix A.1 for further details on the simulation procedure.

while shorter-term movements of the true gap are to some degree still observed in the HP (1600) gap, they are almost completely muted in the HP (400000) gap.

The true gap, in this example, is sometimes also referred to as a cycle in growth rates (see Harding and Pagan (2005)). Such a term might suggest that there exists a (possibly not perfect) mapping from the HP-filtered gaps to the true gap via growth rates. That is, a positive (possibly constant) true gap would imply a steady expansion of the HP-filtered gaps. Of course, this is correct, albeit irrelevant if the true DGP is DS. Under a DS DGP, the HP filter amplifies certain frequencies of the true fluctuations that are determined by the selected smoothing parameter. This creates a spurious gap, i.e., artificial expansionary and contractionary periods, from which economists aim to infer, for example, about the build-up of imbalances. The derived gaps, however, are entirely artificial and merely reflect the a priori specification of the filter. As is apparent from this example, the HP (1600) and HP (400000) gaps suggest different periods of positive and negative deviations from trend, leading, in a real world setting, to differing regulatory responses or conclusions, which in both cases would not be in line with the true gap.

2.2 Credit-to-GDP gap: US and France

Next, consider the real-time Basel III credit-to-GDP gaps of the US and France portrayed in Figure 2 along with the starting dates (black vertical lines) of systemic banking crises as defined by Laeven and Valencia (2012). The two examples highlight well the negative consequences of spurious medium-term cycles, as movements in the latter gaps have direct implications for the setting of CCyBs.⁹

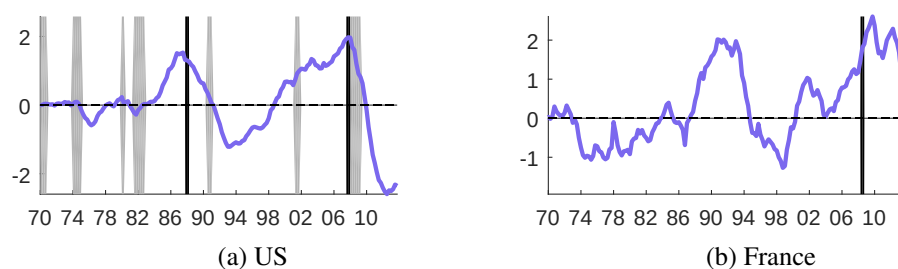


Figure 2: Credit-to-GDP gap

Notes: Credit-to-GDP gaps are constructed using a one-sided HP filter with smoothing parameter 400,000. Series are standardised to unit variance. Grey shaded areas are NBER dates of recession. Black vertical lines indicate the onset of systemic banking crises as defined by Laeven and Valencia (2012).

While both country gaps are positive in the run-up to the GFC, which would support the indicators' use to inform the setting of CCyBs – as the latter should have also been positive to limit the build-up of imbalances through excess aggregate credit growth –, the movements during and after the GFC indicate well the problems related to the amplification of medium-duration cycles. First, the US gap does not indicate the materialisation of systemic risk immediately after the shock hit the economy, but takes until the end of 2009 to close. Second, and even more dramatically, the French gap increases after the shock

⁹Note that, throughout the study, I analyse the effects using a two-sided HP filter, i.e., employing all sample information. The Basel III gaps, however, are constructed exploiting a one-sided, i.e., asymmetric, HP filter. I discuss differences between the two approaches for the simulated data in Appendix A.1 and for the credit-to-GDP gaps of the G-7 countries in Section 4.1.

hit the French economy in 2008, wrongly suggesting that the CCyB should have been raised over that period. However, note the two small downturns visible around 2008 and 2009. It can be argued that these reflect relevant cyclical fluctuations for informing the use of the CCyB, although they are masked by the amplified medium-term cycle.

Thus, while the parameter of 400,000 leads to a gap for the US that peaks before the GFC and also before the saving and loans crisis in 1988, the gap of France does not indicate any strong imbalances prior to the GFC. Hence, due to the strong amplification of medium-term frequencies over shorter-term ones, the extracted gaps are at high risk of not being relevant to the policy task or research question at hand. These observations call into question the common assumption of “one smoothing parameter – or one frequency window in the case of band-pass filters – fits all countries” approach, particularly when considering cycles in the medium-term.¹⁰

3 DETRENDING METHODS AND THEIR EFFECTS ON TREND AND DIFFERENCE STATIONARY TIME SERIES

In the business cycle context it is common practice to decompose real variables, such as output, into a secular (or trend) component and a stationary, possibly cyclical, component. With respect to financial variables, the same approach has been taken. For instance, researchers and policy makers aim at identifying a credit gap measure that should indicate the build-up of excesses or imbalances in order to inform countercyclical macroprudential policies.

In these exercises, a stationary component is identified by deviations from a non-stationary secular component. A non-stationary secular component in credit (possibly over GDP) may arise, for example, from a continued financial deepening or integration that allows an even further expansion of the credit volume, i.e., reflecting developments with permanent effects. The stationary component is regarded as the outcome of transitory, possibly persistent, shocks within an economy, such as phases of high risk aversion triggered by certain financial shocks. It is possible to imagine that shocks to the stationary component may also affect the trend, leading to permanent effects of shocks.

One way to think of this is to decompose (the log of) credit or any other trending series, say y_t , into the sum of such trend and stationary component, for instance, as

$$y_t = \tau_t + \psi_t, \quad (1)$$

where $t = 1, \dots, T$, τ_t reflects a non-stationary trend and ψ_t a stationary, non-deterministic, and possibly cyclical component. In this framework, ψ_t can be referred to as the *gap*, meaning that a permanent component, τ_t , is removed from y_t ; as is the case with the credit-to-GDP or output gap.

To analyse the effects of filters on ψ_t , I consider two data generating processes (DGPs) that have gained prominence in discussions about the trend, i.e., τ_t , in output (see, for instance, Nelson and Plosser (1982)): trend (TS) and difference (DS) stationary DGPs. Both can be nested in Equation (1)

¹⁰Of course, due to country specificities the credit-to-GDP gap could possibly not be the relevant indicator for informing the CCyB for France. However, different transformations of this indicator (see Appendix A.2.1) suggest the existence of relevant movements that signal the downturn during the GFC.

and be formalised as

$$\text{TS: } y_t = \alpha + \beta t + \psi_t \quad (2)$$

$$\text{DS: } y_t = \alpha + y_{t-1} + \psi_t, \quad (3)$$

where α is an intercept (or possibly a drift parameter in Equation (3)), t a deterministic trend and β a slope coefficient of the trend. In the TS case, movements in ψ_t do not affect the trend. In contrast, in the DS case, movements in ψ_t almost completely determine the evolution of the trend.

In the framework proposed by Harding and Pagan (2005), ψ_t in Equation (2), is called a growth cycle and ψ_t in Equation (3) is referred to as a cycle in growth rates. The representation in Equation (1) indicates that such a distinction is not clear-cut, which is acknowledged by Harding and Pagan (2005), who regard Equation (3) as a special case of growth cycles. Clearly, the results of this section are sensitive to the assumptions made on the DGP.¹¹

While both DGPs give rise to the “typical spectral shape” discussed by Granger (1966) when estimating the spectral density of y_t , the effects of filters on ψ_t vary depending on the two DGPs. Depending on the two DGPs, methods may generate spurious cycles in ψ_t by amplifying certain cycle frequencies relative to others, thus biasing the original stationary component.

Below, I first delineate the filters considered and, subsequently, discuss their effects on TS and DS time series. Some final remarks conclude this section.

3.1 Methods of detrending

I consider three different filters and, for each, two different specifications. The first is the difference filter, the second the Hodrick and Prescott (1981, 1997) (HP) filter, and the third the Baxter and King (1999) (BK) filter. The analysis of different specifications is explained by the different detrending approaches adopted by researchers and policy makers when analysing business and financial cycles. Standard filters in the business cycle context (using a quarterly sampling frequency) are the first difference (Δ) filter, the HP filter with a smoothing parameter of 1,600 (HP (1600)), and the BK filter extracting frequencies from 1.5 to 8 years (BK (1.5,8)).¹² The fourth difference (Δ_4) filter, the HP filter with a smoothing parameter of 400,000 (HP (400000)), and the BK filter extracting cycles of duration 8 to 30 years (BK (8,30)) have been recently advocated in the financial cycle context aiming to extract medium-term cycles. For instance, the Δ_4 filter has been employed by Drehmann et al. (2012), Strohsal et al. (2015a), and Verona (2016). The HP (400000) is recommended by the Basel III regulations for constructing the credit-to-GDP gap and is used, for instance, by Anundson et al. (2016). Focussing on cycles between 8 and 30 years by means of a band-pass filter, is suggested by Drehmann et al. (2012) and, for instance, used by Meller and Metiu (2015, forthcoming).

Below, let ξ_t denote the detrended component of y_t , i.e., the estimate of ψ_t .

¹¹For instance, using the classic growth cycle definition, Murray (2003) shows that if y_t is driven by an integrated trend, i.e., $\tau_t = \alpha + \tau_{t-1} + \zeta_t$ with ζ_t stationary and ζ_t uncorrelated with ψ_t , implies that spurious cycles emerge as the first difference of the trend is passed through the filter. Here, the properties of the filtered series are strongly determined by the trend in the unfiltered series. In this framework spurious cycles emerge due to an amplification of specific frequencies in ζ_t and not ψ_t .

¹²The Δ filter has been used by Schularick and Taylor (2012), Aikman et al. (2015), and Schüller et al. (2015, 2017) in the financial cycle context.

Two specifications of the difference filter

I analyse both the first and fourth difference filter. Let $\Delta_i = (1 - L^i)$. The two filters are

$$\xi_t^\Delta = \Delta y_t = (1 - L)y_t = y_t - y_{t-1} \quad \text{and} \quad (4)$$

$$\xi_t^{\Delta_4} = \Delta_4 y_t = (1 - L^4)y_t = y_t - y_{t-4}. \quad (5)$$

Two specifications of the Hodrick and Prescott (1981, 1997) filter

I consider two smoothing parameters: $\lambda = 1,600$ and $\lambda = 400,000$. The smoothing parameter, λ , controls the importance of the penalty term attached to the degree of smoothness of the extracted trend. A parameter of 400,000 leads to a much smoother trend than 1,600.

Most commonly the HP filter is written in the following form:

$$\min_{[\tau_t]_{t=1}^T} \left[\sum_{t=1}^T (y_t - \tau_t)^2 + \lambda \sum_{t=2}^T ((\tau_{t+1} - \tau_t) - (\tau_t - \tau_{t-1}))^2 \right], \quad \lambda > 0. \quad (6)$$

For the analysis of this paper, however, it is convenient to rewrite the latter minimisation problem into a form that directly yields the detrended observations, ξ_t (see, for example, King and Rebelo (1993)):

$$\xi_t^{\text{HP}(\lambda)} = \left[\frac{(1 - L)^2(1 - L^{-1})^2}{(1 - L)^2(1 - L^{-1})^2 + 1/\lambda} \right] y_t. \quad (7)$$

Two specifications of the Baxter and King (1999) filter

I use the BK filter to extract two different frequency bands: first, disentangling fluctuations between 1.5 and eight years and, second, fluctuations between eight and 30 years.

The extracted component is obtained through

$$\xi_t^{\text{BK}(\pi/(2\omega_1), \pi/(2\omega_2))} = a_K(L)y_t, \quad (8)$$

where $(\pi/(2\omega_1), \pi/(2\omega_2))$ denotes the frequency band in years with $\pi/(2\omega_1) < \pi/(2\omega_2)$, $a_K(L) = \sum_{k=-K}^K a_k L^k$ is a symmetric lag polynomial, and $a_k = a_{-k}$ a time-invariant symmetric linear weight. In contrast to the ideal band-pass filter that uses an infinite number of weights, the weights of the BK filter are truncated at lag K . Due to this, Baxter and King (1999) introduce a normalising constant such that $a_K(1) = \sum_{k=-K}^K a_k = 0$, which implies that the filter may neglect long-run trends. More formally,

$$a_k = b_k + \theta, \quad (9)$$

where θ is the normalising constant and b_k the time invariant linear weight of the band-pass filter. θ is defined to be $(-\sum_{k=-K}^K b_k)/(2K + 1)$. Further,

$$b_k = \begin{cases} \frac{\omega_1 - \omega_2}{\sin(\pi k)} & \text{if } k = 0 \\ \frac{\sin(\omega_1 k) - \sin(\omega_2 k)}{\pi k} & \text{if } k \neq 0 \end{cases} \quad (10)$$

For fixed K , the researcher defines the frequency band that she would like to consider by choosing $\omega_1 > \omega_2$. Using a quarterly sampling frequency, filtering frequencies between 1.5 and 8 years implies an

$\omega_1 = \pi/2 \cdot (1.5)^{-1}$ and an $\omega_2 = \pi/2 \cdot (8)^{-1}$; 8 to 30 years an $\omega_1 = \pi/2 \cdot (8)^{-1}$ and an $\omega_2 = \pi/2 \cdot (30)^{-1}$. For the two specifications, I choose $K = 40$ which is larger than the parameter that has been suggested by Baxter and King (1999) for analysing business cycles ($K = 12$), but has been considered by Murray (2003) for the latter purpose. The filter captures medium-term cycles more precisely when using more lags.

3.2 The filters' effects on trend and difference stationary time series

To discuss the effects of the filters on the two data generating processes, I first introduce the concept of power transfer functions (PTFs) which can be used to describe how filtering modifies certain frequencies of a stationary time series and can, thus, indicate induced cycles, i.e., specific frequencies that are amplified relative to others.¹³

3.2.1 The power transfer function and induced cycles

Assume that ψ_t is a stationary stochastic process with an autocovariance generating function defined as $g_\psi(z) \equiv \sum_{t=-\infty}^{\infty} \gamma_t z^t$, where z denotes a complex scalar and γ_t the autocovariances. γ_0 refers to the variance of ψ_t . The spectral density of ψ_t is then defined as

$$S_\psi(\omega) \equiv \frac{1}{2\pi} g_\psi(e^{-i\omega}), \quad (11)$$

where i is the imaginary unit and $\omega \in [-\pi, \pi]$ the cycle frequency in radians. Filtering ψ_t with a time-invariant filter that has absolutely summable weights, say $\xi_t = \sum_{j=-\infty}^{\infty} h_j \psi_{t-j}$, implies that the spectral density is altered via a *transfer function*. This transfer function can be denoted by $h(e^{-i\omega})$ and the exact relation between the spectral density of ψ_t and the spectral density of the filtered series is

$$S_\xi(\omega) = H(\omega) \cdot S_\psi(\omega), \quad (12)$$

where $H(\omega) \equiv |h(e^{-i\omega})|^2$ is referred to as the *power transfer function*. It completely describes the change in the relative importance of the cyclical components in ψ_t .¹⁴ If $H(\omega) > 1$, the amplitude of the cycle component ω of ψ_t is increased. In the case $H(\omega) < 1$, the amplitude of the respective cycle component is dampened. Such amplification or dampening of frequencies in the stationary component ψ_t gives rise to spurious or artificial cycles.

Note that, while ψ_t is stationary, the original time series, y_t , might not be. In this case, i.e., when the filter is applied to a trending variable, the PTF describing the change of cycle frequencies for ψ_t might differ from the PTF of the filter, depending on the source of nonstationarity. This is discussed below.

¹³All frequency domain results are interpreted assuming quarterly sampling frequency, which is the frequency of variables used in this study.

¹⁴The transfer function can be decomposed into gain and phase, where the square of the gain is the power transfer function, i.e., $h(e^{-i\omega}) = |h(e^{-i\omega})|e^{-i\Theta(\omega)}$. $\Theta(\omega)$ refers to the phase. Note that for symmetric linear filters, such as the HP filter the phase is zero. For the first difference filter, it is not. Nonetheless, I refrain from a discussion of phase, as it is not relevant to the analysis of this paper. Changes in the importance of frequencies are fully described by the power transfer function and, for instance, the synchronisation of cycles across countries is analysed using the same filter across countries, in which case the same phase shift applies to all variables.

3.2.2 The filters' effects on trend stationary time series

In the trend stationary case and applying the filters considered in this study on y_t , the linear deterministic trend vanishes from the spectrum of the filtered series, ξ_t , that is

$$S_\xi(\omega) = H(\omega)S_y(\omega) = H(\omega)S_\psi(\omega). \quad (13)$$

This means that in the case of trend stationary data, the PTFs describing the effects of the Δ and the Δ_4 filter on ψ_t are

$$H^\Delta(\omega) = |(1 - e^{-i\omega})|^2 = 2(1 - \cos(\omega)) \quad (14)$$

$$H^{\Delta_4}(\omega) = 2(1 - \cos(4\omega)). \quad (15)$$

The PTFs capturing the effects of the HP filters with $\lambda = 1,600$ and $\lambda = 400,000$ on ψ_t can be derived from

$$H^{\text{HP}(\lambda)}(\omega) = \left[\frac{4(1 - \cos(\omega))^2}{4(1 - \cos(\omega))^2 + 1/\lambda} \right]^2. \quad (16)$$

For the BK filters with frequency windows (1.5,8) and (8,30) respectively, the power transfer function may be obtained from the lag-polynomial and is

$$H^{\text{BK}(\pi/(2\omega_1), \pi/(2\omega_2))}(\omega) = |a_K(e^{-i\omega})|^2. \quad (17)$$

All six power transfer functions are depicted in Figure 3, where the y -axis shows the squared gain induced by each filter across frequencies and the x -axis the cycle length in radians. The conversion to cycle duration in years using quarterly data is $\pi/(2\omega)$, where ω is the value of the x -axis, e.g., $\pi/(2\pi) = 0.5$ years, which is the shortest cycle duration that can be measured using quarterly data. Note that the scale of time is nonlinear, i.e., the closer to 0 radians the larger the increase in cycle length is. To ease the reading of graphs showing the frequency domain, I mark business cycle frequencies (1.5-8 years) in blue and medium-term cycle periods (8-30 years) in purple. The latter area is argued to be important for the financial cycle.

In the case of trend stationary data, $H^\Delta(\omega)$ dampens frequencies of ψ_t which are actually suspected to drive business and financial cycles, as its gain is below one, until a cycle length of 1.5 years. Further, high-frequency components, i.e. cycles of duration less than 1.5 years, are intensified. It cancels cycles of infinite duration, as the squared gain is zero at frequency 0. $H^{\Delta_4}(\omega)$ removes, as well, not only cycles of infinite duration, but also yearly cycles in the case of quarterly data, i.e., at frequency $\pi/2$, and, thus acts as a seasonal filter. Further and in contrast to $H^\Delta(\omega)$, it mutes cycles to a lesser extent in the medium term and business cycle region. Moreover, it amplifies some parts of business cycle frequencies. $H^{\Delta_4}(\omega)$ also amplifies shorter-term cycles, of less than one year's duration, with a peak amplification at $2/3$ years or $3\pi/4$ radians.

In this setting, the HP filter removes low-frequency cycles of the cyclical component, ψ_t , and leaves the others unchanged, meaning it has a PTF of 1. The two HP filters differ in that the filter with a λ of 400,000 leaves longer-term cycles in the cyclical component until a duration of around 30 years. This

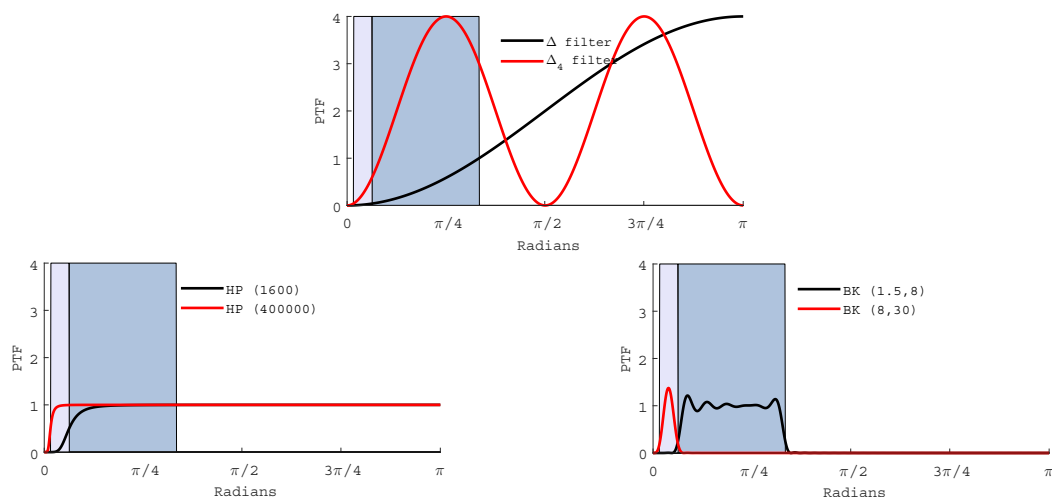


Figure 3: (Trend) stationary time series: power transfer functions, $H(\omega)$

Notes: The blue area marks business cycle frequencies (1.5-8 years) and the purple area medium-term cycles (8-30 years) assuming quarterly data. PTF denotes the power transfer function. Results of the BK filter use $K = 40$.

contrasts with the cyclical component obtained by the HP filter with a λ of 1,600 contains cycles of up to roughly 8 years.

$H^{\text{BK}(\pi/(2\omega_1), \pi/(2\omega_2))}(\omega)$ with $K = 40$ approximates a gain of one for the frequency band specified. In black, I show the specification that leaves frequencies between 1.5 and 8 years in ψ_t and in red the specification that is supposed to leave medium-term cycles in the stationary component. In the case of the latter, there is a marginal amplification of cycles of around 13 years' duration in the region where the PTF peaks at a value greater than one.

In sum, given TS time series, both difference filters induce cycles in ψ_t . The Δ filter amplifies cycles at high frequencies, but not at business and financial cycle frequencies. The Δ_4 filter amplifies cycles at around 2 and 2/3 years, with the former implying induced cycles in the business cycle range. In contrast, the HP and BK filters represent close approximations to the ideal band-pass filters when considering their effects on the stationary component, ψ_t , for which the gain of the PTF is around one. The HP filter with a smoothing parameter of 400,000 implies that longer-term cycles are left in the stationary component. Both specifications of the BK filter emphasise cycles of desired length in ψ_t .

3.2.3 The filters' effects on difference stationary time series

In the difference stationary case, the effects of the filters on ψ_t change. They operate as a two-step linear filter, in which case y_t , in a first step, is differenced to render the series stationary and, in a second step, smoothed with the remainder of the filter. Remainder means that the application of such filters in this setting “uses up” one difference operator (see, for example, Cogley and Nason (1995) and Murray (2003)). Thus, the transfer function of interest, say $J(\omega)$, which describes the effects on the stationary component ψ_t , can be derived by

$$S_\xi(\omega) = H(\omega)S_y(\omega) = J(\omega)S_{\Delta y}(\omega) = J(\omega)S_\psi(\omega), \quad (18)$$

where $J(\omega) = H(\omega)/H^\Delta(\omega)$.

The $J(\omega)$ s for the first and fourth difference filters are

$$J^\Delta(\omega) = H^\Delta(\omega)[H^\Delta(\omega)]^{-1} = 1 \quad \text{and} \quad (19)$$

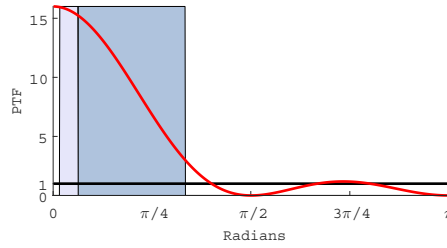
$$J^{\Delta_4}(\omega) = H^{\Delta_4}(\omega)[H^\Delta(\omega)]^{-1} = \frac{1 - \cos(4\omega)}{1 - \cos(\omega)}, \quad (20)$$

for the HP filter

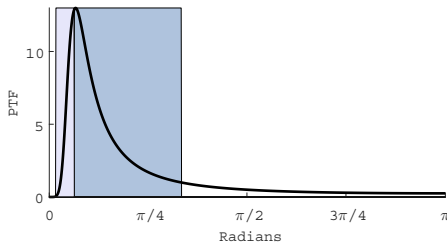
$$J^{\text{HP}(\lambda)}(\omega) = H^{\text{HP}(\lambda)}(\omega)[H^\Delta(\omega)]^{-1} = \frac{8(1 - \cos(\omega))^3}{(1/\lambda + 4(1 - \cos(\omega))^2)^2}, \quad (21)$$

and for the BK filter

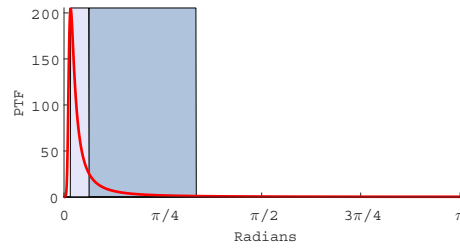
$$J^{\text{BK}(\pi/(2\omega_1), \pi/(2\omega_2))}(\omega) = H^{\text{BK}(\pi/(2\omega_1), \pi/(2\omega_2))}(\omega)[H^\Delta(\omega)]^{-1} = \frac{|a_K(e^{-i\omega})|^2}{1 - \cos(\omega)}. \quad (22)$$



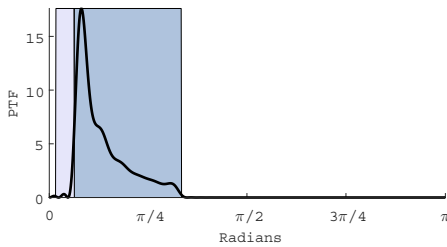
(a) $J(\omega)$ for Δ filter (black) and Δ_4 filter (red)



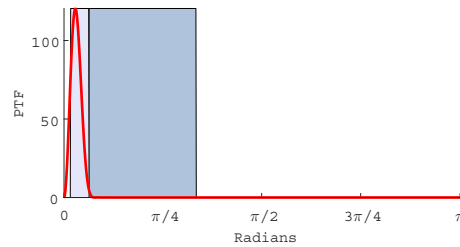
(b) $J(\omega)$ for HP (1600)



(c) $J(\omega)$ for HP (400000)



(d) $J(\omega)$ for BK (1.5,8)



(e) $J(\omega)$ for BK (8,30)

Figure 4: Difference stationary time series: power transfer functions, $J(\omega)$

Notes: The blue area marks business cycle frequencies (1.5-8 years) and the purple area medium-term cycles (8-30 years) assuming quarterly data.

Figure 19 depicts these PTFs. Observe that the scales of the y -axes differ for each of the five figures. $J^{\Delta_4}(\omega)$ amplifies cycles of ψ_t in the business cycle and, more importantly, in the financial cycle region. Thus, after removing the unit root, the Δ_4 filter induces cycles in ψ_t at longer-term frequencies; however, there is no peak in the PTF, which means that the filter emphasises a range of longer-term cycles and not a specific one. Through the emphasis of longer-term cycles, shorter-term frequencies are

almost completely muted. In contrast, the Δ filter does not change the spectrum of the stationary component, ψ_t . The PTF is 1 for all frequencies. Assuming a DS process, the first difference filter thus removes, first, the source of nonstationarity and, then, leaves the stationary component unaltered.¹⁵

In the case of the two $J(\omega)$ s of the HP filter, both PTFs peak and therefore magnify specific frequencies. The higher the smoothing parameter is, the more strongly are cycles in ψ_t magnified – up to around 13 times employing a parameter of 1,600 and up to roughly 204 times using a parameter of 400,000. The HP filter may therefore introduce spurious cycles into the stationary component, i.e., emphasise cycles that are present in the data but may not be important relative to other fluctuations present in the stationary component or not of relevance to the research question at hand. Note that the frequency that is emphasised can be derived from $\omega_{\max} = \arccos(1 - \sqrt{0.75/\lambda})$. Accordingly, in the case of a $\lambda = 1,600$, cycles of lengths around 7.5 years in ψ_t are emphasised, whereas for $\lambda = 400,000$ cycles of lengths around 30 years are emphasised.

Similarly, the two $J(\omega)$ s of the BK filters peak and, thus, emphasise specific cycles in ψ_t . The filter (1.5,8) magnifies durations of around 6.2 years with a factor of around 18 and the (8,30) of around 18 years with a factor of approximately 120. In contrast to the HP filter, the BK filter cancels all shorter-term frequencies that have not been included in the specification, i.e., below 1.5 and below 8 years respectively.

In sum, given a DS process, the HP filter may induce cycles of around 7.5 and 30 years in the stationary component for a smoothing parameter of 1,600 and 400,000 respectively. The BK filters emphasise frequencies of roughly 6.2 and 18 years' duration in the stationary component when filtering (1.5,8) and (8,30) years respectively. The Δ_4 filter amplifies longer-term cycles, whereas the Δ filter does not alter the cyclical component at all. These insights highlight the importance of the a priori choice of the HP smoothing parameter or the BK frequency window for the detrending of DS time series as they lead to a focus on specific fluctuations of the cyclical component.

3.2.4 *Some remarks*

It is worth noting that the effects of filters on DS time series have broad implications, that is, Cogley and Nason (1995) show that the effects of filters on near unit root trend stationary time series are similar to the effects on difference stationary time series.

Further, Pederson (2001) points out that effects of the HP and BK filters on DS time series need to be discriminated from the Slutsky effect. The Slutsky effect is defined as distortions that occur when filtering stationary data. Or, put differently, the PTFs of the filters themselves show peaks and, thus, induce spurious cycles by emphasising specific frequencies relative to others; as is with the difference filters. This is not the case for the HP and BK filters, which both approximate an ideal band-pass filter for the specified frequency range. Even though the distortions of these filters do not coincide with the Slutsky effect, their implications are important, especially when considering medium-term fluctuations.

¹⁵Note, the Δ filter is the non-distorting filter in this application, as I assume a first difference stationary process in this exercise (see Equation (3)). This is in line with Hamilton (2017)'s argument that a typical economic time series is best approximated by a random walk and by the empirical evidence provided in this paper. Clearly, if the true DGP would be a Δ_4 process the fourth difference filter would be best suited.

At last, the exposition in this section emphasises the importance of knowing the true DGP for choosing the “correct” filter, i.e., the one that either minimally distorts the cyclical properties of the underlying series or extracts the fluctuations of interest. However, as the true DGP cannot be known in practice, the following empirical exercise aims to provide evidence on distortions that filters induce in actual economic time series, without the need to assume a specific DGP.

4 FINANCIAL CYCLE FACTS ACROSS G7 COUNTRIES

Having shed light on the theoretical properties of filters, I now turn to discuss the effects of applying them to financial and business cycle variables of G7 countries. To begin with, I introduce the data, depict their (log-)levels and detrended components, and formally test whether there is evidence against the hypothesis of a unit root with possible drift (DS) using the alternative hypothesis of a TS DGP. Subsequently, I examine the amplitude and length of financial cycle variables relative to business cycles. Thereafter, I reflect on the synchronisation of financial cycle variables across countries, also contrasting with the synchronisation of business cycles. In both exercises, I first explore a time and second a frequency domain perspective. I employ both perspectives as each highlights different features of the detrended components.

4.1 *Data and some notes on filtering*

I use the dataset by Schüler et al. (2017) which includes quarterly data on credit, house prices, equity prices, and bond prices, augmented by the credit-to-GDP ratio. This set of variables reflects indicators measuring financial cycles. The representative business cycle variable is GDP. The dataset covers G7 countries and spans the period from 1969Q1 to 2013Q4.

Credit, house prices, and credit-to-GDP reflect time series from the Bank of International Settlements. Credit is total credit, and house prices are measured through residential property prices. For equity prices, the main economic indicators database from the OECD is employed, except for the US, in which case I use the S&P 500 index that is the standard variable in academic studies researching on US equity markets. Corporate bond yields are taken from Global Financial Data and Haver Analytics. GDP is also retrieved from the OECD main economic indicators database.¹⁶ All variables are in real terms, log-transformed (except for credit-to-GDP), and deflated via the CPI index of the OECD main economic indicators database where necessary. Seasonal adjustment is performed using Census X-12.

Note that bond yields are transformed to reflect bond prices as suggested in Schüler et al. (2017), i.e., $p_{b,t} = 1/(1 + y_{b,t})$, where $p_{b,t}$ denotes the price and $y_{b,t}$ is the current yield of the respective bond at time t . Such transformation assures, on the one hand, an interpretation of this variable similar to the other asset price series considered and, on the other, allows for a similar process of deflating, which is important when comparing cyclical structures across indicators.¹⁷

¹⁶For exact details please refer to the Appendix of Schüler et al. (2017)

¹⁷The other option is to construct yearly inflation from the CPI indices and deduct those from the yields. However, as highlighted in the previous section, the year-on-year filter runs the risk of emphasising specific cycles and inducing phase shifts.

Before proceeding with the analysis, it is useful to note that I employ the HP and BK filters using whole sample information.¹⁸ However, the credit-to-GDP gap, as defined in the Basel regulations, is actually constructed via a one-sided HP filter, i.e., an HP filter that is applied to an expanding sample. This implies that only current and past information is employed. Of course, this is due to the restriction that policy makers and regulators need to act in real time. For this study, I assume that all sample information is available. A comparison of both approaches, i.e., constructing the credit-to-GDP gap using a two- versus a one-sided HP filter, is given in Appendix A.2.2. Summarising, the dynamics of the detrended series do not differ strongly. Most remarkable differences occur at the beginning of the sample, when only few observations are available for the one-sided filter. In the case of France or Italy, for instance, this leads to the outcome that the one-sided filtered series seems to be trending, possibly biasing the analysis of the stationary component. Overall, the comparison suggests that the implications derived from the two-sided filter carry over closely to the one-sided filter.

Finally, I compute the detrended component of the BK filter by extending the first and last observations by their respective value for several quarters, such that the sample period common to all filters is longest.

4.1.1 Visual inspection of levels and detrended components

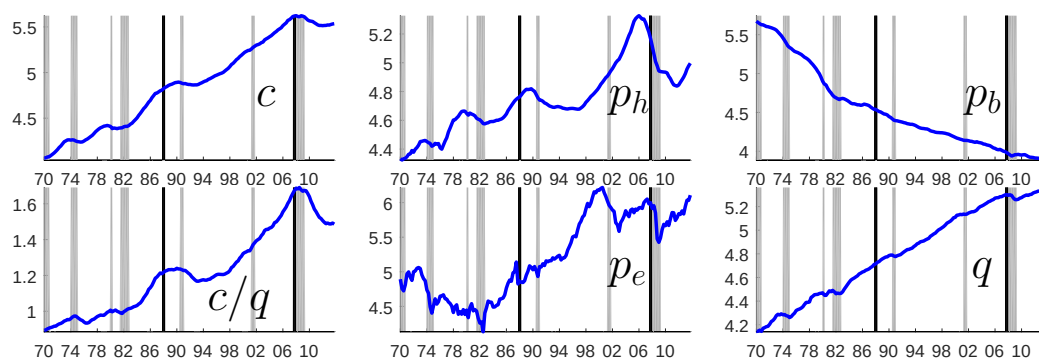


Figure 5: US' financial and business cycle indicators

Notes: Grey area depicts NBER dates of recessions. Black vertical lines indicate the onset of systemic banking crises as defined by Laeven and Valencia (2012). c denotes total credit, c/q credit-to-GDP, p_h house prices, p_e equity prices, p_b bond prices, and q output.

Figure 5 depicts the US data in (log-) levels and Figure 6 shows the detrended components obtained via the three filters as discussed in Section 3. Note that, for ease of exposition, the detrended series are standardised to unit variance. The remaining country charts are placed in Appendix A.2.1.

Considering the time series graphs for the US, several conclusions can be drawn. With respect to the levels, visual inspection suggests that all variables show trending behaviour. For equity prices (p_e) this evidence can be argued to be weakest, reminiscent of a random walk without drift. Further, while the slope of the potential trends or drifts are positive for most series, these would be expected to turn out negative for bond prices (p_b).¹⁹

¹⁸While the HP and BK filters are employed using whole sample information, the difference filters – by construction, asymmetric filters – only use information at time period t together with $t - 1$ or $t - 4$.

¹⁹Clearly, ever declining real bond prices would be a puzzling phenomenon. As this study does not focus on finding

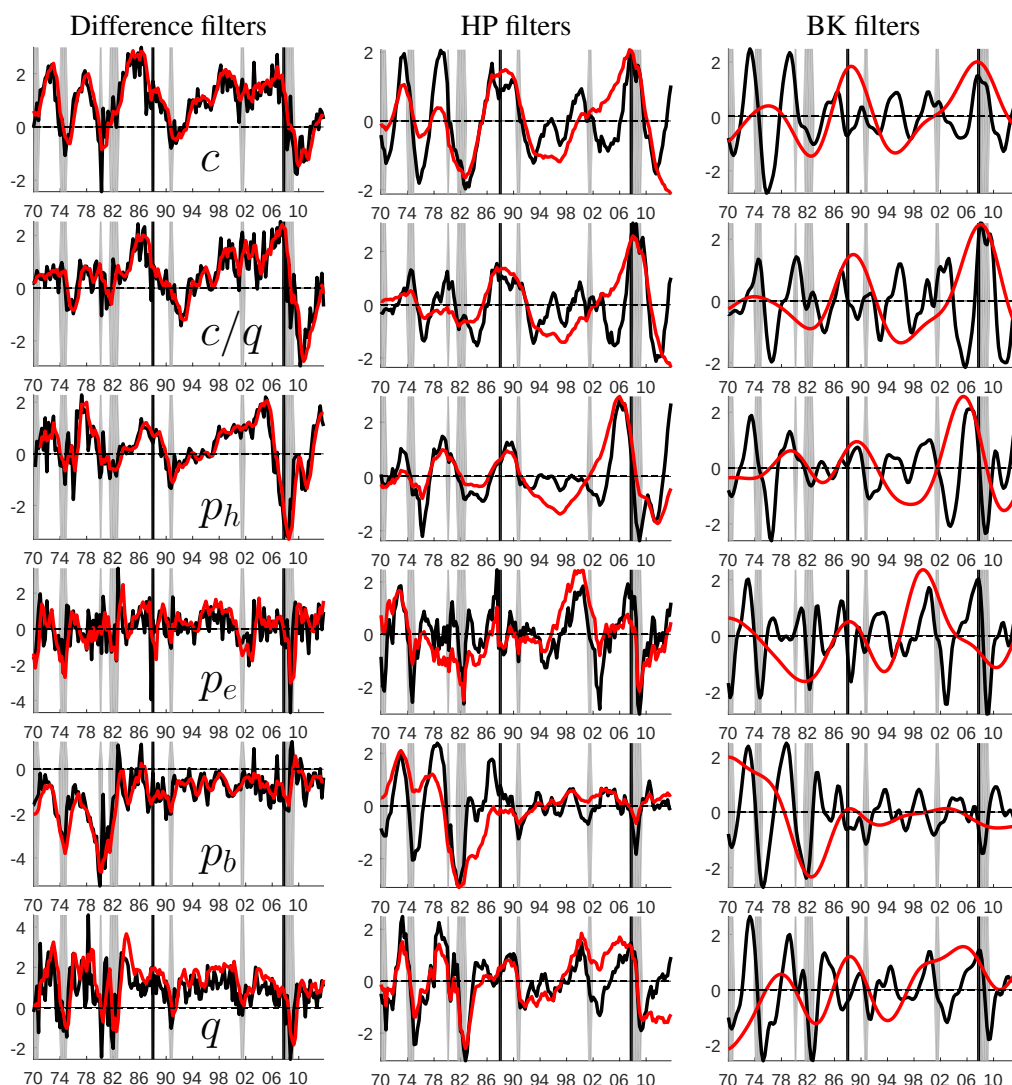


Figure 6: Detrended US' financial and business cycle indicators: Δ , HP (1600), BK (1.5,8) filter in black, Δ_4 , HP (400000), and BK (8,30) filter in red

Notes: Grey area depicts NBER dates of recessions. Black vertical lines indicate the onset of systemic banking crises as defined by Laeven and Valencia (2012). Series are standardised to unit variance for ease of exposition. Each row refers to the variable indicated in the left hand panel. c denotes total credit, c/q credit-to-GDP, p_h house prices, p_e equity prices, p_b bond prices, and q output. The BK filter is specified with $K = 40$ and the cycles are computed by extending the first and last observations by their respective value for several quarters, such that the sample period common to all filters is longest.

Comparing the detrended components obtained with the Δ to those derived with the Δ_4 filter (see Figure 6) leads to the conclusion that, on the one hand, short-term movements are muted using the Δ_4 filter and, on the other, a slight phase shift is induced, i.e., turning points occur later for the Δ_4 treated version of each series. However, the lower frequency movements in both series seem to be similar.

Looking at the HP detrended series suggests that each specification of the filter leads to a different cyclical pattern in each variable case. As expected, the HP filter with a λ of 400,000 captures longer-term cycles than the filter with a λ of 1,600, but also mutes shorter-term fluctuations. Further, both HP-filtered series look different from the fluctuations identified via the difference filters.

arguments for different theoretical mechanisms that generate the trending behaviour, I refrain from a further discussion along these lines.

The two BK-filtered series, similar to the case of the HP filter, show different cyclical patterns. Of course, this can be argued to be an artefact of the specifications, as the filter was required to separate different cycle frequencies.

Interestingly, the BK (1.5,8)-filtered series resemble the HP (1600)-filtered series and the BK (8,30)-filtered series resemble HP (400000) cycles, even though the BK filters completely mute shorter-term fluctuations, for instance, in the case of the BK (8,30) filter, cycles shorter than eight years. Somehow, this is reflected in a number of minor fluctuations in the HP-filtered series. Still, while cycles resemble each other, they are not the same. For instance, credit reaches one of its historic peaks for both HP-filtered series before the post-90 recession. In contrast, the BK (1.5,8)-filtered series only shows a marginal deviation from trend.

Finally, note that the HP (400000) detrended component of equity prices and GDP contain by far more shorter-term frequencies than in any other variable's case.

In sum, all level series can be argued to show a trending behavior. The two difference filters produce rather similar results when focussing on longer-term movements. Shorter-term movements are muted using the Δ_4 filter. Both HP and both BK filter calibrations deliver different cycles for all variables, which are also different from the cycles obtained using the difference filters. Nonetheless, there is some similarity between the HP and BK filter when comparing the cycles for the shorter-term frequencies, on the one hand, and comparing the fluctuations of the longer-term cycles, on the other. These observations are broadly consistent across G7 countries. It is only in the case of Japan that the trends in certain variables are characterised by breaks, e.g., for house prices (p_h), in which case no clear trend behaviour is visible.

4.1.2 Are financial cycle variables trend or difference stationary?

This section explores for each variable whether it is possible to reject the null of unit root with drift against the alternative of trend stationarity, which, as indicated, has important implications for distortions induced by filters. More precisely, I use the following version of the augmented Dickey Fuller test: under the null the series has a unit root with drift, i.e.,

$$y_t = \alpha + y_{t-1} + \sum_{i=1}^p \theta_i \Delta y_{t-i} + \eta_t \quad (23)$$

where the p -lagged differences account for serial correlation and η_t is an iid normal error. Under the alternative, I specify the model as

$$y_t = \alpha + \beta t + \rho y_{t-1} + \sum_{i=1}^p \theta_i \Delta y_{t-i} + \eta_t. \quad (24)$$

Thus, I test the joint restriction that $\beta = 0$ and $\rho = 1$ using an F -test.²⁰ Clearly, such a test cannot completely determine whether a time series follows a stochastic or deterministic trend. First, the test

²⁰Note this test is similar to the test used in Murray and Nelson (2000) who explore whether the trend in US GDP is deterministic or stochastic. The current test, however, differs in that I specify the DGP under the null to be a unit root with linear drift. Murray and Nelson (2000) allow in their specification for a unit root with quadratic drift, which I argue does not reflect the trend observed in the data just discussed.

suffers from low power against local alternatives. Second, breaks in the trend can lead to an under-rejection of the null that could possibly be a factor, for instance, in the case of Japan. Nonetheless, the current formulation of the ADF test gives initial evidence for one of the two data generating processes which is augmented by details on the spectral densities of the detrended components in the following parts.

Table 1: Augmented Dickey Fuller F -test

<i>Variable</i> Country	AR lag	Test statistic	Nominal p -value	<i>Variable</i> Country	AR lag	Test statistic	Nominal p -value
<i>Credit (c)</i>				<i>Equity prices (p_e)</i>			
Canada	2	5.45	0.097	Canada	1	6.29	0.053
Germany	1	13.54	0.001	Germany	1	5.87	0.072
France	1	6.53	0.045	France	1	3.84	0.325
Italy	2	1.88	0.778	Italy	1	4.02	0.285
Japan	2	3.85	0.323	Japan	1	2.40	0.658
UK	3	1.64	0.840	UK	1	3.91	0.310
US	2	5.06	0.128	US	0	3.95	0.300
<i>Credit-to-GDP (c/q)</i>				<i>Bond prices (p_b)</i>			
Canada	1	2.59	0.615	Canada	1	6.32	0.052
Germany	1	2.15	0.716	Germany	1	9.79	0.004
France	1	1.60	0.850	France	1	7.36	0.024
Italy	1	4.26	0.229	Italy	1	7.36	0.024
Japan	2	2.12	0.722	Japan	2	6.84	0.036
UK	3	2.18	0.709	UK	2	7.26	0.026
US	2	3.72	0.354	US	1	5.31	0.108
<i>House prices (p_h)</i>				<i>GDP (q)</i>			
Canada	1	1.79	0.800	Canada	1	5.12	0.123
Germany	1	3.70	0.358	Germany	1	6.63	0.042
France	2	4.51	0.184	France	0	4.93	0.140
Italy	1	7.43	0.023	Italy	4	6.67	0.041
Japan	1	2.22	0.700	Japan	0	18.03	0.001
UK	1	4.64	0.170	UK	0	1.23	0.933
US	2	7.15	0.029	US	1	1.39	0.899

Notes: AR lags are chosen via minimising Schwarz (1978) information criterion over lags 0 to 12. Test statistic refers to an F -test as described in the text. Nominal p -values are obtained by linear interpolation from tables that have been generated for a range of sample sizes and significance levels using Monte Carlo simulations of the null model with Gaussian innovations and five million replications per sample size.

The outcomes of the ADF tests are depicted in Table 1. Note that the AR lags are chosen by minimising the Schwarz (1978) information criterion that has been argued to produce roughly correctly sized ADF tests (Hall (1994)).

Three results stand out: First, tests on credit-to-GDP (c/q) provide the weakest evidence against the null hypothesis of a unit root, as it cannot be rejected for any country case at any given significance level, while for the remaining variables the null hypothesis is at least rejected in two out of the seven country cases using the ten percent significance level. This marks a strong result, as precisely credit-to-GDP is recommended by the Basel regulations to be used with the HP (400000) filter and, thus, a gap measure could be at high risk of representing an artefact of the method of detrending. Second, evidence against a unit root with drift is greatest for GDP (q , rejection in three out of seven country cases) and bond prices (p_b , rejection in six out of seven country cases) considering the five percent significance level. Clearly, the result for bond prices could possibly be driven by the transformation of yields to prices considered in this study. Third, for all other variables, evidence is weak against a unit root with drift. At the five

percent significance level, rejections occur in two country cases for credit (c) and house prices (p_h) and no country case for equity prices (p_e). At the ten percent significance level, the null is rejected in two country cases for equity prices.

In sum, the ADF tests reject the null hypothesis of unit root with drift in only 12 out of 42 cases considering the five percent significance level. I find weakest evidence against a unit root with drift for credit-to-GDP and strongest evidence for bond prices. Thus, tests provide initial evidence that caution should be exercised with regard to spurious cycles when constructing, for instance, a credit-to-GDP gap measure as advised in the Basel regulations.

4.2 Amplitude and duration

To analyse the robustness of higher amplitude and length of financial variables relative to business cycle variables, I first use time domain methods. Second, I consider a frequency domain perspective to evaluate the importance of different contributing cycle frequencies with respect to the overall variance of detrended indicators.

4.2.1 Time domain perspective

I resort to standard deviation to describe amplitude and first-order autocorrelation as a proxy for duration. I summarise these figures using boxplots indicating the spread of the statistics across countries (see Figures 7 and 8).

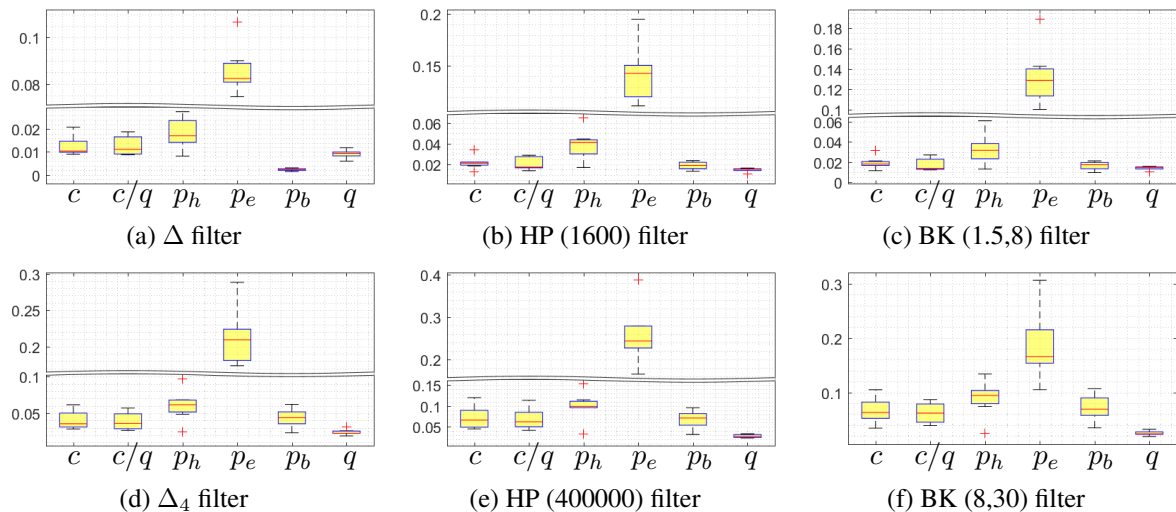


Figure 7: Standard deviation of detrended indicators across G7 countries

Notes: c denotes total credit, c/q credit-to-GDP, p_h house prices, p_e equity prices, p_b bond prices, and q output.

With respect to amplitude, Figure 7 suggests that, independent of the filter, financial variables, except for bond prices, robustly have higher amplitude than GDP. For bond prices, the Δ filter leads to smaller standard deviations across countries when compared to the figures for GDP. For equity prices, I find by far the highest amplitude. This result is least pronounced using the BK (8,30) filter. Second are house prices, although these are very close to the standard deviations of credit, credit-to-GDP, and bond prices.

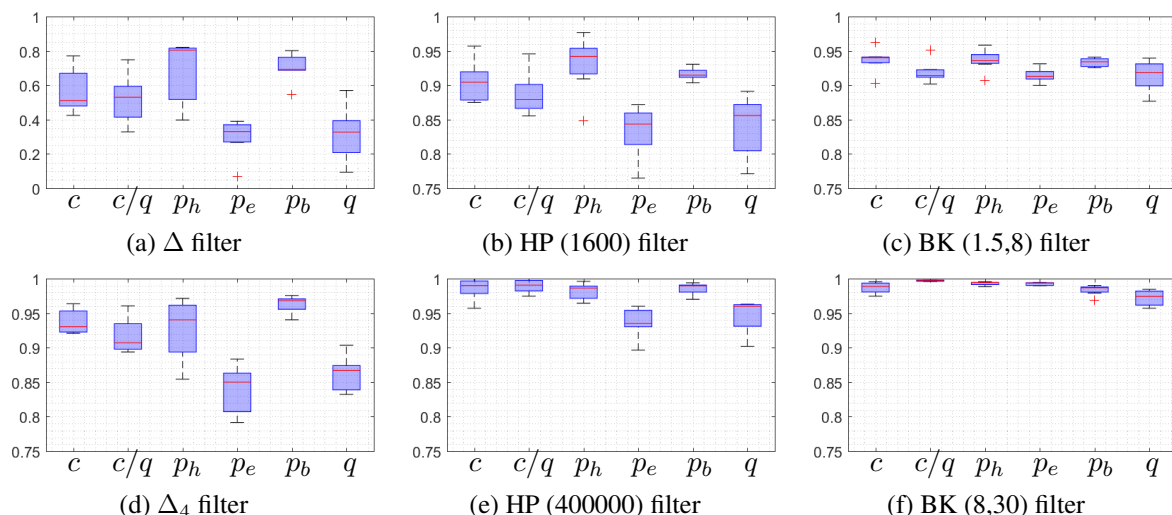


Figure 8: First-order autocorrelation of detrended indicators across G7 countries

Notes: c denotes total credit, c/q credit-to-GDP, p_h house prices, p_e equity prices, p_b bond prices, and q output. Note that scales differ for the Δ filter.

With respect to persistence, Figure 8 indicates that financial indicators, except for equity prices, robustly have higher autocorrelation than GDP. Across detrending methods, it is not clear which variable has the highest persistence. Lowest persistence is found for equity prices across methods of detrending, except for the BK (8,30) filter, in which case output is least persistent.

Across filters and considering both amplitude and persistence, two results are worth noting. First, differences to GDP appear to be rather marginal for HP (400000) and BK (8,30) filters; in the case of persistence, also when considering the BK (1.5,8) filter. Second and in line with the first point, the magnitude and dispersion of statistics vary strongly. Amplitude is highest for the HP (400000) filter, while persistence is strongest for the BK (8,30) filter. These statistics are smallest for the Δ filter. In the case of persistence, for example, the range of the boxplots that describes the effects of the Δ filter stretches from around 0 to 0.9, while, at the other extreme, results of the BK (8,30) filter range from close to 0.95 to around 1.

In sum, higher amplitude and persistence for credit, house prices, and bond prices as well as higher amplitude of equity prices, all relative to GDP, are robust across the different methods of detrending. Nonetheless, differences in the statistics are shown to be only marginally different for the HP (400000) and the BK (8,30) filters – in the case of persistence, also for the BK (1.5,8) filter. In general, the magnitude and dispersion of statistics across countries vary strongly across filters. These findings imply that specific cycle frequencies of the stationary component are altered using the various filters and their specifications.

4.2.2 Frequency domain perspective

Figure 9 shows the estimated smoothed spectral densities for each detrended variable across countries. The solid line reflects the median of all countries at given frequency ω , while the dashed lines denote the 25% and 75% quantiles. For each detrended variable, the estimated spectral density, $\hat{S}_\xi(\omega)$, is obtained

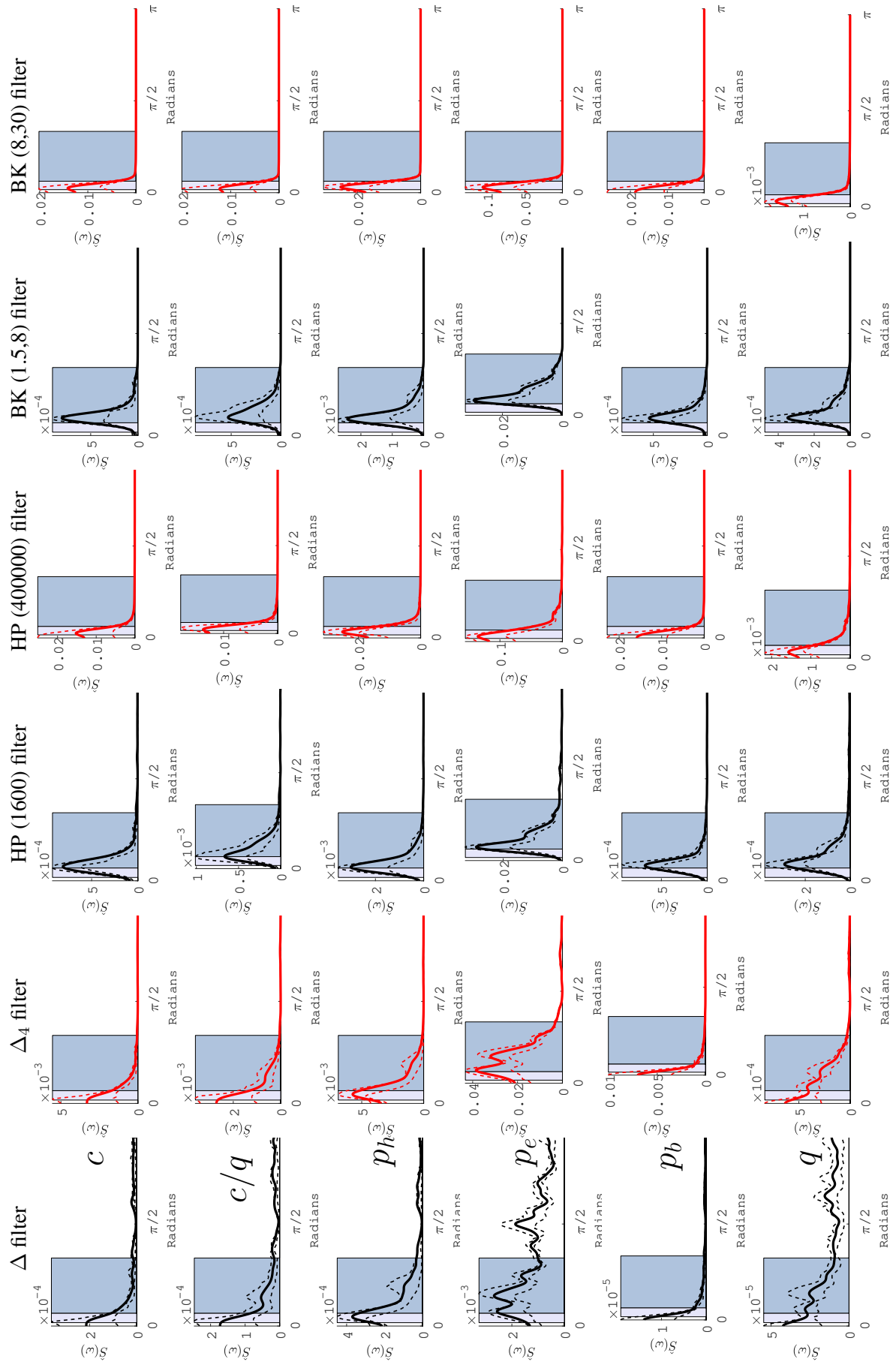


Figure 9: Spectral densities of detrended indicators across G7 countries

Notes: The blue area marks business cycle frequencies (1.5-8 years) and the purple area medium-term cycles (8-30 years). Solid line is median across countries at frequency ω ; dashed lines depict the 25% and 75% quantiles.

using a Parzen window of length $4\sqrt{T}$, where T denotes the sample size.²¹ Again, the blue area marks 1.5 to 8 years and the purple 8 to 30 years. Further, Table 2 reports the most important cycle length as measured by the global maximum of each spectral density, i.e., for all combinations of filters, variables, and countries.

Higher amplitude is supported by the frequency domain perspective (see Figure 9). That is, the magnitude of spectral densities (y -axis) for all detrended financial variables is higher than that of GDP (q), except for bond prices (b_b) in the case of the Δ filter.²²

Visually, longer-duration financial cycles – except for equity prices – are only supported by the difference filters. Here, financial variables are clearly marked by more important, i.e., with respect to overall variance, medium-term cycles than GDP. The exception is the equity price series (p_e) with many important cycle frequencies located in the business cycle range, similar to GDP. Bond prices still seem to be governed by a long-term trend, as most important cycles locate at the zero frequency, except for the HP (1600) and BK (1.5,8) filters. Differences between the durations of financial and business cycles seem to disappear when the HP and BK filters are considered. In that regard, Table 2 offers a more detailed view: while for the difference filters longer-duration cycles in credit, credit-to-GDP, and house prices to cycles in GDP are apparent (for example, looking at the Δ filter and the median values: 12.6/16.0/9.9 versus 5.9 years respectively), they are only marginally longer using the HP and BK filters (e.g., HP (1600) filter and median values: 7.4/8.1/7.8 versus 6.2 years respectively). They are even marginally shorter for house prices in the case of the HP (400000) filter and for credit-to-GDP in the case of the BK (1.5,8) filter.

Looking across filters, there is strong evidence that the data generating process for most of the data is DS, that is, there evidence of filter-induced cycles in the stationary component. First, the detrended components of the HP and BK filters across all countries and variables have durations around frequencies indicated by the PTFs under DS, i.e., close to 7.5/30 and 6.2/18 years (see Table 2). Note that, when interpreting the similarities of durations of the HP (400000) and BK (8,30) filtered series, it is important to keep in mind that the grid of cycle durations above eight years is very small. This becomes clear, for instance, when comparing the size of the large blue shaded area (covering 5.5 years) with the size of the small purple area (covering 22 years; see, for example, Figure 9). That is, even though differences in years may appear large, the outcomes of the latter filters across countries can still be argued to be very similar. Further and in the case of the HP (400000) filter, where deviations from the expected cycle duration under DS are strongest, possibly stationary components do not contain cycles of exactly 30-year duration, thus, revealing other frequencies close to 30 years. These are amplified as well, albeit to a smaller degree than cycles of 30 years. Finally, the Δ_4 -filtered series tend to show the distortions present in case of a difference stationary process as well. For instance, in the case of credit-to-GDP, equity prices, and GDP, the Δ filter suggests the presence of short-term cycles, which are not present using the Δ_4 filter (Figure 9). Moreover, long-term cycles are emphasised more than cycles in the business

²¹Figures actually show pseudo spectra, meaning that the zero frequency is disregarded.

²²Note that to compare overall figures one would have to integrate the spectral densities for each detrended variable and country. Thus, it is not entirely correct to compare the magnitude of important cycles across indicators. The time domain offers an easier to interpret perspective in this case.

Table 2: Cycle duration of detrended indicators

Variable Country	Δ	Δ_4	HP (1600)	HP (4·10 ⁵)	BK (1.5,8)	BK (8,30)	Variable Country	Δ	Δ_4	HP (1600)	HP (4·10 ⁵)	BK (1.5,8)	BK (8,30)
Credit (<i>c</i>)							Equity prices (<i>p_e</i>)						
Canada	12.3	12.3	8.9	14.6	6.5	14.9	Canada	3.5	3.5	6.9	10.2	6.2	13.6
Germany	∞	∞	7.4	50.0	6.9	30.6	Germany	3.3	7.8	7.3	11.7	6.5	13.2
France	11.8	11.9	7.0	13.7	5.9	14.9	France	3.1	7.0	6.8	22.3	6.3	17.8
Italy	17.2	17.4	8.6	17.1	7.0	20.3	Italy	6.4	6.6	6.6	16.8	6.1	16.9
Japan	∞	∞	6.4	∞	5.9	∞	Japan	7.8	7.8	6.8	17.7	5.9	16.8
UK	21.8	20.9	5.8	18.5	5.5	23.3	UK	5.8	6.3	6.3	23.8	5.9	21.8
US	12.6	12.6	7.4	14.2	6.2	17.7	US	3.4	3.5	7.0	∞	6.4	23.5
Average	15.1	15.0	7.4	21.3	6.3	20.3	Average	4.8	6.1	6.8	17.1	6.2	17.7
Median	12.6	12.6	7.4	15.8	6.2	19.0	Median	3.5	6.6	6.8	17.2	6.2	16.9
Credit-to-GDP (<i>c/q</i>)							Bond prices (<i>p_b</i>)						
Canada	11.4	11.4	8.7	14.0	5.4	14.3	Canada	∞	∞	7.1	∞	6.4	∞
Germany	∞	∞	3.8	24.1	4.4	23.0	Germany	∞	∞	8.1	14.1	6.3	16.4
France	17.5	19.1	8.6	16.5	5.3	17.5	France	∞	∞	7.1	∞	6.3	∞
Italy	∞	∞	8.5	19.3	4.0	28.4	Italy	∞	∞	6.8	∞	6.2	∞
Japan	∞	∞	6.0	∞	5.7	∞	Japan	∞	∞	6.5	36.6	5.5	23.5
UK	18.0	17.1	8.1	16.8	5.6	24.1	UK	∞	∞	6.0	∞	5.4	75.9
US	14.4	14.3	7.6	15.4	6.4	20.9	US	∞	∞	6.5	81.9	5.7	∞
Average	15.3	15.5	7.3	17.7	5.3	21.4	Average	n.a.	n.a.	6.9	44.2	6.0	38.6
Median	16.0	15.7	8.1	16.7	5.4	22.0	Median	n.a.	n.a.	6.8	36.6	6.2	23.5
House prices (<i>p_h</i>)							GDP (<i>q</i>)						
Canada	12.6	12.6	7.0	15.1	6.5	15.6	Canada	13.9	14.0	6.2	16.1	5.8	15.3
Germany	8.4	8.3	7.8	13.2	6.9	13.6	Germany	∞	∞	6.6	14.1	5.8	14.6
France	15.2	15.2	9.5	16.3	5.7	16.8	France	0.9	5.7	5.9	15.6	5.7	15.1
Italy	9.9	10.0	7.7	12.3	6.4	14.0	Italy	∞	∞	5.6	14.8	5.4	19.1
Japan	9.2	8.9	7.8	∞	6.0	40.2	Japan	∞	∞	6.8	∞	6.0	21.6
UK	9.4	10.1	6.7	14.8	5.9	16.7	UK	5.8	5.9	5.9	14.4	5.6	17.1
US	11.4	11.6	8.0	14.9	6.2	15.1	US	6.0	6.2	6.3	15.2	6.0	∞
Average	10.8	11.0	7.8	14.4	6.2	18.8	Average	6.7	7.9	6.2	15.1	5.8	17.1
Median	9.9	10.1	7.8	14.9	6.2	15.6	Median	5.9	6.0	6.2	15.0	5.8	16.2
Duration of maximum amplified cycle under DS time series process													
	-	-	7.5	30.0	6.2	18.0		-	-	7.5	30.0	6.2	18.0

Notes: Numbers indicate cycle length in years referring to global maximum of spectral density from 0 to π of the detrended component obtained by the indicated filter. ∞ denotes that maximum cycle duration is global maximum of spectral density. Average and median are derived neglecting countries with cycle duration of ∞ .

cycle region. For instance, the three peaks in the financial and business cycle range of equity prices are biased as though the underlying data was DS, i.e., amplifying the longer-duration cycles and relatively dampening shorter-term ones. The same holds true for GDP and credit-to-GDP.

Second, the differences in variances of the detrended components (*y*-axis) across filters are broadly in line with the distortions present with difference stationary data, implying that strongest biases of the stationary component occur when extracting medium-term cycles (see Figure 9). Magnitudes are by far the strongest for the HP (400000)- and BK (8,30)-filtered series, in which case the filters have an amplification of cycles in the stationary component of a factor of around 204 for cycles close to 30 years and 120 for cycles close to 18 years. For instance, the detrended credit-to-GDP ratio has a peak above 0.01 for both filters and the peak of the HP (400000)-detrended component is above the peak of the BK (8,30)-filtered component. Second are the magnitudes of the Δ_4 filtered series in which case the filter has an amplification of cycles of a maximum factor of around 16 for longer-term cycles (peak of credit-to-GDP above 0.002). The HP (1600) filter leads to values only slightly smaller than the Δ_4 filter (peak of credit-to-GDP above 0.0005), relating to the PTF in the DS case that shows a magnification

of cycles of around 7.5 years by a factor of up to roughly 13. Interestingly, the BK (1.5,8) filter shows magnitudes similar to the HP (1600) filter (peak of credit-to-GDP close to 0.0005), even though its PTF in the DS case shows a magnification of up to 18 times, which is a stronger amplification than in the case of the Δ_4 filter. This can be reconciled by the fact that the Δ_4 filter magnifies a greater range of frequencies and does not sharply peak at a specific cycle duration. The smoothing of the spectral densities in the estimation process can be argued to lead to such differences. The mentioned differences in magnitudes across filters also hold true for bond prices, in which case, however, the ADF tests reject the null hypothesis of unit root with drift in most cases. Bond prices, however, seem to be a special case, as even after filtering they are governed by a long-term trend (except for the HP (1600) filter), thus possibly neither being trend nor difference stationary.

In sum, the frequency domain perspective suggests two things: It supports higher amplitude and longer-duration of financial cycles relative to business cycles for all methods of detrending and variables, except for equity prices in the case of the difference filters. However, most important cycles of financial variables reported using the HP and BK filters are, in nearly all cases, only marginally longer than cycles in GDP. Second, there is strong evidence of spurious cycles for all HP- and BK-detrended series, since each specification and filter leads to a similar-duration cycle that is line with the predicted duration of the maximum amplified cycle under DS. Similar lengths of most important cycles across countries marks a very strong result as different country histories, laws, and institutions should lead to different country cycles, which are apparent using the difference filters. Note that, even though cycles of HP (1600)- and BK (1.5,8)-detrended series have each similar durations, the potential bias for inference is still less strong than considering HP (400000)- and BK (8,30)-detrended series, that is, while the former filters still include fluctuations of other frequencies besides the maximum amplified frequency, the latter filters – in relative terms – do not. Finally, the fourth difference filter eliminates all short run frequencies and emphasises longer-term frequencies, which specifically matters for credit-to-GDP, equity prices, and GDP.

4.3 Synchronisation of financial cycle variables across countries

Below I shed light on the synchronisation of financial cycle variables across G7 countries. First, I consider a time domain perspective using average contemporaneous correlations for each detrended series across countries and, second, I depict results from a frequency domain perspective. The frequency domain analysis starts by introducing a measure I call dynamic power cohesion. This represents the equivalent to the average contemporaneous correlation employed in the time domain, additionally allowing to differentiate between the importance of common cycles, considering their relation to overall variance of indicators and whether these common cycles contribute positively or negatively to the overall correlation.

4.3.1 Time domain perspective

For the analysis of synchronisation of variables across countries, I employ, as indicated, the standard correlation measure between country pairs. These statistics are depicted in the boxplots of Figure 10,

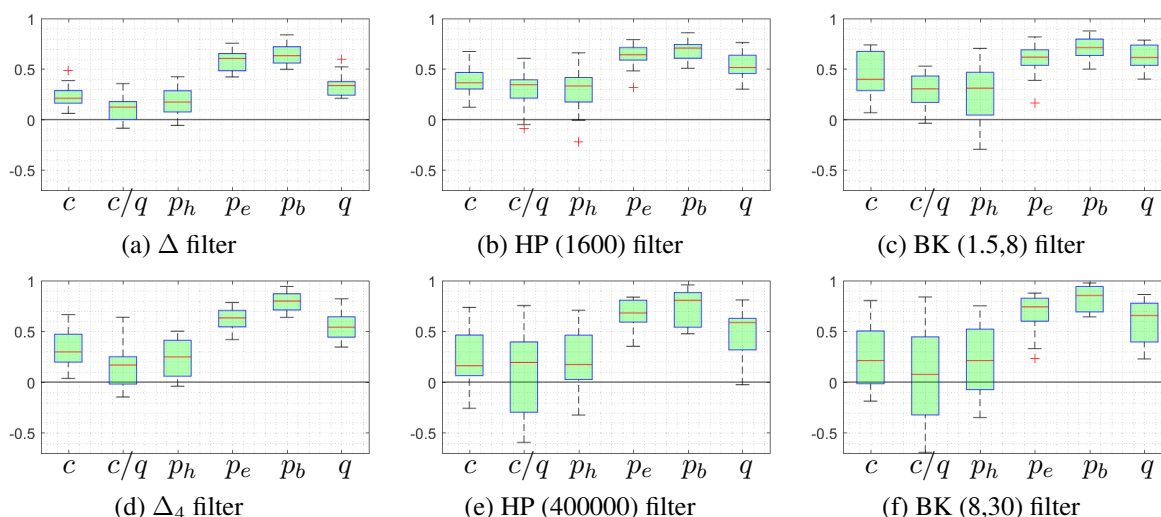


Figure 10: Correlation of detrended indicators across G7 countries

Notes: c denotes total credit, c/q credit-to-GDP, p_h house prices, p_e equity prices, p_b bond prices, and q output. BK filter uses $K = 40$.

showing their dispersion across countries. Each panel contains a comparison of correlations across variables for one of the filters. The y -axis has been restricted for all panels and ranges from one to the minimum value over all boxplots.

Equity and bond prices always belong to the variables that are most strongly synchronised across countries. However, a clear difference to the synchronisation of GDP only exists when employing the Δ filter – for bond prices also using the Δ_4 filter. For the remaining filters and specifications, the differences become more marginal or disappear. Differences are least marked when considering the BK (1.5,8) filter. In this case, equity prices and GDP show a similar degree of synchronisation across countries, caused by a strong increase in the synchronisation of GDP at these frequencies. Differences to GDP are rather similar when considering the HP (1600) and the Δ_4 filter. The HP (400000)- and the BK (8,30)-filtered series show a strong increase in dispersion of country correlation, leading to a vanishing of marked differences.

For credit, house prices, and credit-to-GDP results suggest a weaker (for example, looking at the median) synchronisation than GDP across methods of detrending. However, the dispersion of statistics is stronger than for GDP, thus leading to country cases that show a similar synchronisation to cycles in GDP. While these results broadly hold for the difference filters and the HP (1600) and BK (1.5,8) filters, they are distorted when considering the HP (400000) and BK (8,30) filters. Here, similar to the case of equity and bond prices, the dispersion of statistics particularly increases, such that differences become less clear. More severely, the filtered series show a strong negative correlation for some of the country cycles, being strongest for credit-to-GDP, which, to this degree, is not apparent from any of the other detrending procedures.

In sum, equity and bond prices belong to the variables that are most strongly synchronised, and credit, credit-to-GDP, and house prices among the variables that are most weakly synchronised across methods of detrending, in most cases being different from the synchronisation of GDP. Differences to

the synchronisation of GDP turn marginal or disappear, e.g., for equity prices and bond prices when using the BK (1.5,8) filter or for credit, credit-to-GDP, and house prices when considering medium-term frequencies. The dispersion of synchronisation of cycles in credit, credit-to-GDP, and house prices is largest, such that some country pairs are more strongly and some more weakly related. In that regard, the application of the HP (400000) and BK (8,30) filters induces the greatest dispersion, resulting in a strong negative correlation of cycles which, to this degree, is not apparent using any of the other methods of detrending.

4.3.2 Frequency domain perspective

First, I introduce the methodology of dynamic power cohesion, subsequently, the method is used to shed light on the synchronisation of financial cycle variables across G7 countries.

Methodology: Dynamic power cohesion – Are important common cycles positively or negatively related?

The methodology developed in this section is based on work by Croux, Forni and Reichlin (2001) and Schüler et al. (2015, 2017). Specifically, I combine, on the one hand, the idea of dynamic correlation that indicates contemporaneous correlation over the frequency band and, on the other hand, power cohesion that provides information about the common cycle frequencies that matter most with respect to the overall variance of a set of indicators. Dynamic power cohesion can be argued to be the direct correspondence of the previous exercise, just in the frequency domain. It allows to point out cycles that account for the overall contemporaneous correlation measured in the last section. This highlights whether the synchronisation of common cycles occurs at different frequencies using different filters, also indicating whether cycles contribute positively or negatively to overall correlation.

As indicated, I call the proposed method dynamic power cohesion (DPCoh) and define it as

$$\text{DPCoh}_{\Xi}(\omega) = \frac{1}{(M-1)M} \sum_{i \neq j} \frac{\mathfrak{c}_{\xi_i \xi_j}(\omega)}{\sigma_{\xi_i} \sigma_{\xi_j}}, \quad (25)$$

where $1 \leq i \leq M, 1 \leq j \leq M, \Xi = (\Xi'_1, \dots, \Xi'_T)'$ is a $T \times M$ matrix and $\Xi_t = (\xi_{1,t}, \dots, \xi_{M,t})$ ($1 \times M$). Further, $t = 1, \dots, T$ and $M \geq 2$ reflect the time dimension and number of variables respectively, and $\omega \in [-\pi, \pi]$ denotes the cycle frequency.²³ Ξ is assumed to contain stationary stochastic processes with well-defined normalised cross-spectral densities, where σ_{ξ_i} and σ_{ξ_j} are the standard deviations and $\mathfrak{c}_{\xi_i \xi_j}(\omega)$ is the co-spectrum of the detrended components $\xi_{i,t}$ and $\xi_{j,t}$. The co-spectrum is defined as the real part of the cross-spectrum, $s_{\xi_i \xi_j}(\omega)$, which can be decomposed into the co-spectrum and the quadrature-spectrum, $\mathfrak{q}_{\xi_i \xi_j}(\omega)$, as

$$s_{\xi_i \xi_j}(\omega) = \mathfrak{c}_{\xi_i \xi_j}(\omega) + i\mathfrak{q}_{\xi_i \xi_j}(\omega). \quad (26)$$

The co-spectrum measures the covariance in phase and the quadrature-spectrum out of phase.

²³ Actually, considering the frequencies from 0 to π suffices to provide all information on cycles in phase, as only the real part of the cross-spectral density is considered.

To give some intuition on the proposed measure, note that integrating from $-\pi$ to π yields the correlations analysed in the previous section, i.e.,

$$\frac{\int_{-\pi}^{\pi} \mathfrak{C}_{\xi_i \xi_j}(\omega) d\omega}{\sigma_{\xi_i} \sigma_{\xi_j}} = \frac{\text{Cov}[\xi_{it}, \xi_{jt}]}{\sigma_{\xi_i} \sigma_{\xi_j}} = \rho_{\xi_i \xi_j} \quad (27)$$

The above identity has two implications: first, the co-spectrum may take positive as well as negative values and, second, a positive co-spectrum at some frequency and negative at some other can potentially cancel each other out when integrating to the overall covariance. For instance, Croux et al. (2001) show that while a white noise process and its one-period lagged value have zero correlation, the co-spectrum indicates perfect positive correlation in the long run (at frequency 0) and perfect negative in the short run (at frequency π), overall, however, integrating to zero. Thus, dynamic correlation makes it possible to gain more insights on the linear relation of two stationary processes than the standard correlation measure.

Finally, note that dynamic power cohesion differs from cohesion based on dynamic correlation (see Croux et al. (2001)) by relating the co-spectrum to the overall standard deviations and not the respective auto-spectra at frequency ω . Thus, while dynamic correlation cohesion – as proposed by Croux et al. (2001) – can be used to study linear similarities of two processes at each frequency ω , the suggested measure provides information on the relative importance of frequencies with respect to the indicators' overall fluctuations. For a further discussion – including a comparison to squared coherency – please refer to Schüler et al. (2015, 2017).

Results

Dynamic power cohesion is depicted for all detrended series in Figure 11.²⁴ The solid line reflects the mean across countries at frequency ω , whereas the dashed lines represent the 25% and 75% quantiles. The blue area marks the business cycle region, which is 1.5 to 8 years, and the purple marks the medium-term cycle region of 8 to 30 years. The x -axis is restricted and shows the spectra from close to 0 to $\pi/2$, i.e., one year is the shortest cycle length depicted. Note that, due to the normalisation of cross-spectral densities (see Equation (25)), a comparison of the strength of synchronisation among indicators without integrating over ω is difficult. Nonetheless, graphs serve to highlight differences in important cycle frequencies that explain the synchronisation of detrended indicators across countries.

The correlation of indicators occurs at cycle frequencies that contribute strongly to the overall variance of the single detrended indicators (see Section 4.2.2). Thus, DPCoh suggests that synchronisation of detrended series is based on filter-induced cycles in the case of the HP and BK filter, calling for caution when analysing cross-country correlation. Emphasised cycles do not necessarily represent important fluctuations of the stationary component, i.e., with respect to its overall variance. Again, special caution needs to be taken when extracting medium-term frequencies, as other cyclical components are relatively more strongly muted than when considering the HP (1600) or BK (1.5,8) filters. For instance, the HP (1600) and BK (1.5,8) detrended house prices still contain fluctuations in the business cycle

²⁴The cross-spectral densities used in the derivation of DPCoh are similarly obtained as the spectral densities, i.e., using a Parzen window with length $4\sqrt{T}$. Again, I show pseudo spectra, i.e., for which I exclude the zero frequency.

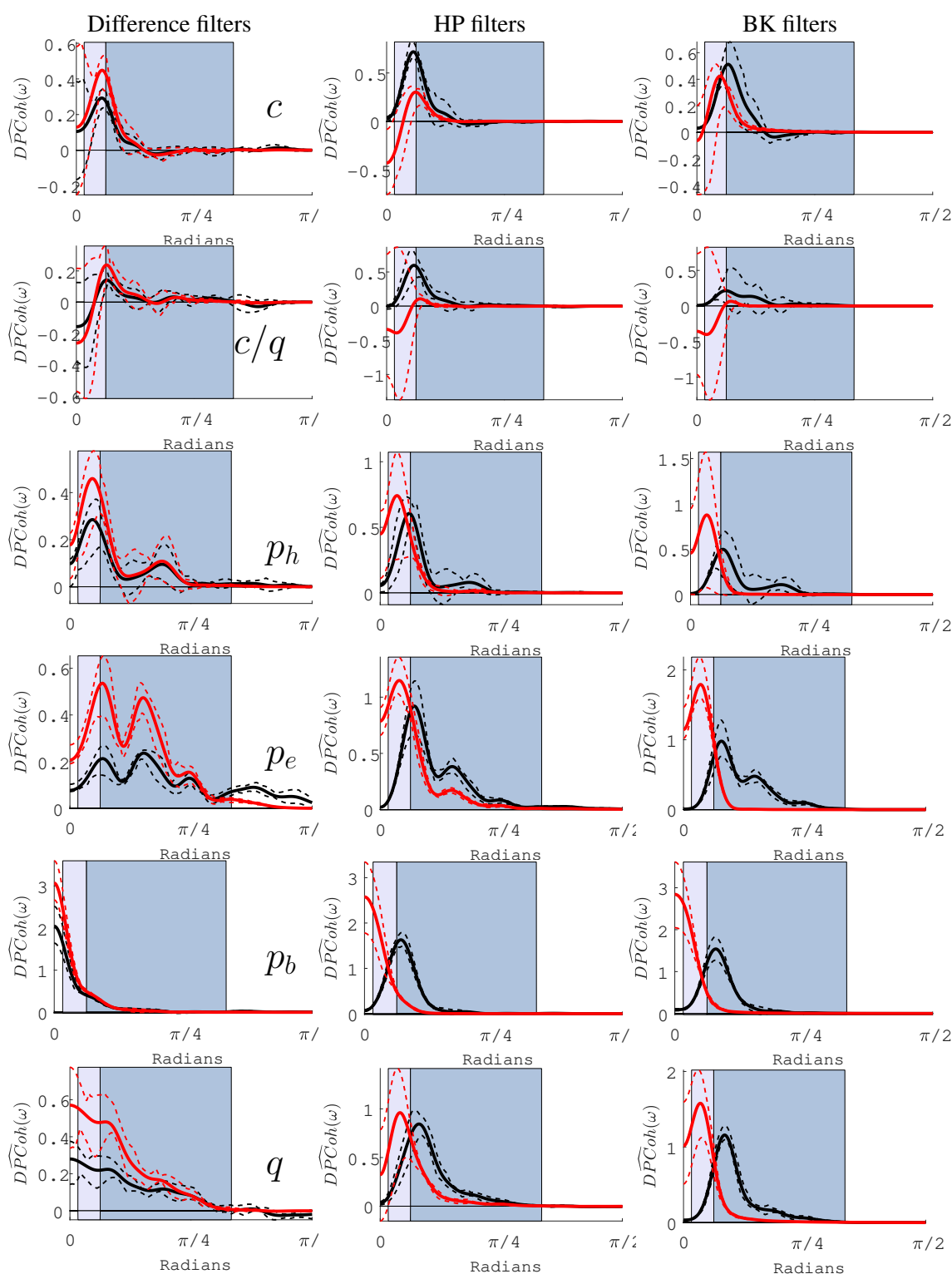


Figure 11: Dynamic power cohesion of detrended indicators across G7 countries: Δ , HP (1600), BK (1.5,8) filter in black, Δ_4 , HP (400000), and BK (8,30) filter in red

Notes: The blue area marks business cycle frequencies (1.5-8 years) and the purple area medium-term cycles (8-30 years). Solid line is mean across countries at frequency ω ; dashed lines depict the 25% and 75% quantiles. c denotes total credit, c/q credit-to-GDP, p_h house prices, p_e equity prices, p_b bond prices, and q output.

range, which are relatively muted considering the HP (400000) filter. Clearly, the BK (8,30) was specified to exclude frequencies below eight years, nonetheless, due to the amplification of medium-term cycles, the HP (400000) detrended series contains similarly few important cycles in the business cycle range.

Further, DPCoh suggests that the lower overall synchronisation of detrended credit and credit-to-GDP is due to opposing medium-term cycles for certain country pairs, that is, the negative co-movement at medium-term frequencies cancels out positive co-movement at shorter frequencies, such that overall correlation is found to be lower than for GDP, e.g., for the Δ filter. In general, for all filters, except the HP (1600) filter, the range between the 75% and 25% quantile also reaches into the negative support of the y -axis for medium-term cycles. In the case of the HP (1600) filter, these opposing medium-term cycles are disregarded. In this light, previous results of strong negative correlation of HP (400000)- and BK (8,30)-detrended series, e.g., of credit-to-GDP, can be explained by the amplification of medium-term cycles that are negatively related for some country pairs and the relative dampening of shorter-term fluctuations that are positively related.

Summarising, there is strong evidence that the synchronisation of HP- and BK-detrended series occurs mostly at cycles induced by the filters, calling for caution in drawing inference from the latter. Special attention needs to be taken when considering the medium term, as the amplification of such cycles - in relative terms - strongly mutes shorter-term cycles, for instance, leading to strong negative correlation of the HP (400000)- and BK (8,30)- detrended credit-to-GDP ratio. Finally, weaker overall synchronisation of credit and credit-to-GDP is found to be due to opposing medium-term cycles.

5 CONCLUSIONS

Beyond enhancing financial system resilience, one of the key objectives of macroprudential policy is to attenuate financial cycles. Clearly, central to this objective are the properties of financial variables. These are of vital importance not only in terms of consistently informing policy makers and regulators, but also in influencing the design of theoretical models. While I find that financial cycle properties differ markedly across methods of detrending, their differences from similarly detrended GDP are qualitatively akin.

Nonetheless, caution needs to be exercised regarding the method of detrending, since I find significant evidence of spurious cycles that bias inference, for instance, regarding the synchronisation of detrended variables across countries. Specifically, a frequency domain perspective suggests that the Hodrick and Prescott (1981, 1997) (HP) and Baxter and King (1999) (BK) filters, and, in general, any band-pass filter amplify certain frequencies that lead to a relative dampening of other cycles, which could be relevant for the research question or the specific policy task (see Section 2 for examples). The negative consequences of spurious cycles increase for the HP filter in the magnitude of the smoothing parameter and for the BK filter in the filtering of longer-term cycles, raising concerns about a HP smoothing parameter of 400,000, as recommended in the Basel regulations or the smoothing window 8 to 30 years suggested by Drehmann et al. (2012).

Further, I find evidence that the weak synchronisation of credit and credit-to-GDP across countries (see Schüller et al. (2017)) is partially due to opposing medium-term cycles, which could potentially relate to differing degrees of financial market liberalisation (see Favilukis et al. (2013)).

Three main policy conclusions may be drawn from this study. First, caution needs to be exercised when analysing extracted medium-term cycles, as for instance suggested in Basel III. The strong amplification of a small range of cycles cancels shorter-term frequencies that could be potentially relevant, say, in signalling the build-up of imbalances prior to systemic banking crises or the abrupt risk materialisation thereafter. Also, if the frequency of financial crises increases, build-up phases of imbalances will not be visible when focussing exclusively on a very specific medium-term frequency range. Hence, there is a high risk that the recommended credit-to-GDP gap will misguide the setting of the CCyB rate. Second, assuming the same HP smoothing parameter or BK frequency window across different countries, means that relevant country-specific fluctuations are likely to be missed. While the US Basel credit-to-GDP gap indicates imbalances before the savings and loan crisis and the global financial crisis, the emphasis of such medium-term frequencies does not necessarily imply that Basel credit-to-GDP gaps signal systemic banking crises for other countries as well – rather the opposite: the strong amplification of medium-term cycles is prone to miss fluctuations of relevance for other countries. The same argument also holds for studies researching on business cycles that assume similar detrending specifications across countries; however, the risk of missing relevant fluctuations is greater when considering medium-term cycles. Third, differing empirical properties of financial and business cycle variables make a strong case for macroprudential policy possibly taking a complementary role to other macroeconomic policies that primarily target business cycles.

Two avenues for addressing the risks of spurious cycles seem reasonable: First, one could completely avoid the application of HP and BK filters on trending levels by considering their growth rates. Of course, stationary growth rates could still be filtered to focus on specific frequencies. In this regard, Schüller et al. (2015, 2017) suggest forming cross-sectional averages (with time-varying weights) of standardised growth rates of credit and asset prices which allow to focus on expansions and contractions common to this set of variables, thus dampening idiosyncratic movements. Such measure already provides a relatively smooth estimate of cyclical fluctuations without the need to rely on further filtering techniques. The authors show in a real-time early warning exercise that a filtered composite financial cycle – by far – outperforms the credit-to-GDP gap for G7 countries, possibly reflecting the fact that the large HP smoothing parameter emphasises frequencies that are not relevant in some country cases. Second, one could still rely on HP and BK filters for detrending, albeit using country-specific HP smoothing parameters or frequency windows (possibly changing over time) that amplify frequencies relevant for the specific task. In this context, Schüller et al. (2015, 2017) propose a methodology for forming country-specific cycle frequencies that are based on the cohesion, i.e., correlation, between the growth rates of financial cycle indicators in the frequency domain. Alternatively, one could use unobserved components models that lead to country-specific cycles (see, for example, Rünstler and Vlekke (2016); Galati et al. (2016)). However, for this class of models, too, studies find evidence of spurious cycles if the true DGP is DS (Nelson (1988)).

There are ample paths for future research. Studies could highlight the potential distortions to financial cycle variables implied by other methods of detrending, such as different setups of unobserved components models. Further, one could shed light on the implications of different trends for the classical turning points approach that has also been considered to characterise financial variables. Also, given the long debate on the nature of the trend in GDP, there is a clear need for further – not only empirical – research on the nature of trends present in financial variables. Further, Hamilton (2017) recently suggests an alternative to HP filters based on simple regression techniques. It would be of great interest to understand how such a method could be used in the context of medium-term filtering. Finally and with respect to the synchronisation of credit and credit-to-GDP cycles, more research is needed to shed light on the potential driving factors behind the opposing medium-term cycles.

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A APPENDIX

A.1 Simulated data

In order to illustrate the negative consequences of spurious medium-term cycles, I simulate data from a difference stationary time series process. To recover realistic dynamics, I fit an autoregressive (AR) model to changes in the US credit-to-GDP ratio. The lag structure of the AR model is determined to be five by considering the Schwarz (1978) information criterion and residual autocorrelation. Specifically, I generate data for $t = 1, \dots, 180$, which is similar to the number of observations available for the financial indicators used in this study. The AR model with five lags is

$$\psi_t = 4.48 \cdot 10^{-4} + 0.56\psi_{t-1} + 0.20\psi_{t-2} + 0.21\psi_{t-3} - 0.32\psi_{t-4} + 0.21\psi_{t-5} + \nu_t,$$

where $\nu_t \sim N(0, 2.89 \cdot 10^{-5})$. I derive the level, y_t , by cumulatively summing up the simulated time series. y_t as well as the one- and two-sided HP (400000) filtered gaps are shown in Figure 12.

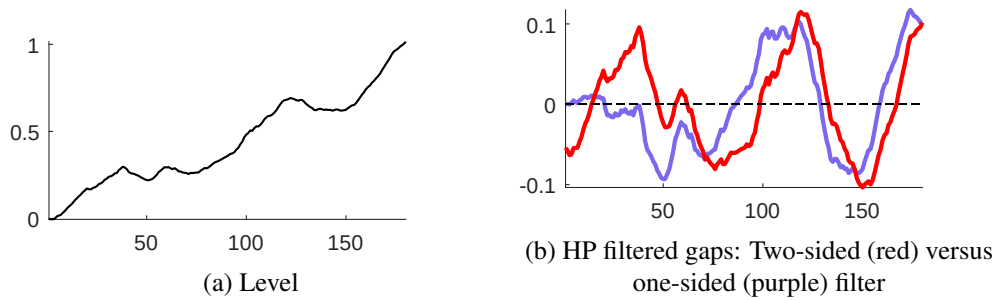


Figure 12: Simulated data

Notes: The HP-filtered gaps are obtained by detrending the level of the simulated data with a smoothing parameter 400,000.

A.2 Data

A.2.1 Indicators and detrended levels

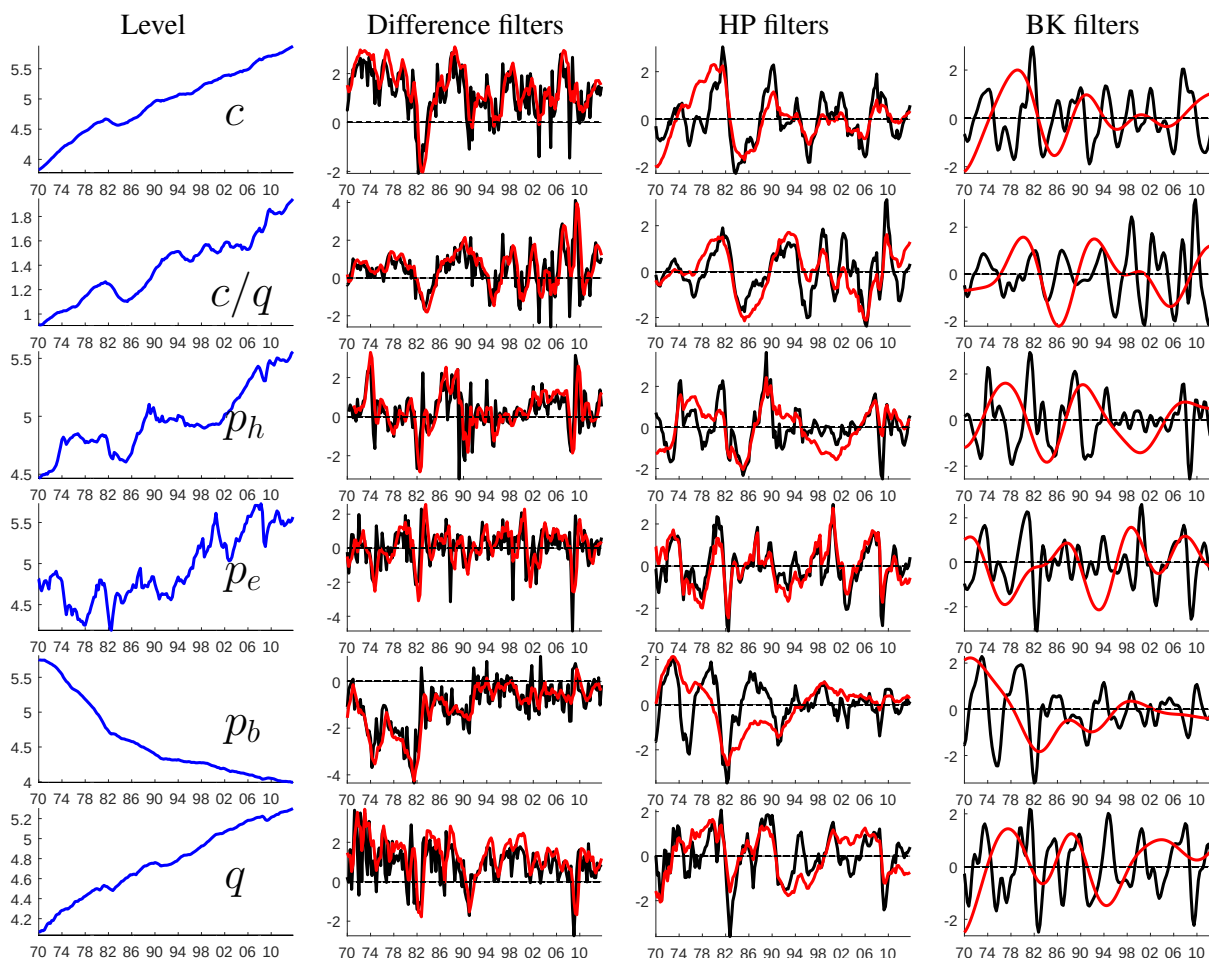


Figure 13: Canada's financial and business cycle indicators and their detrended components: Δ , HP (1600), and BK (1.5,8) filter in black; Δ_4 , HP (400000), and BK (8,30) filter in red

Notes: All series, except the level, are standardised to unit variance for ease of exposition. Each row refers to the variable indicated in the left hand panel. c denotes total credit, c/q credit-to-GDP, p_h house prices, p_e equity prices, p_b bond prices, and q output.

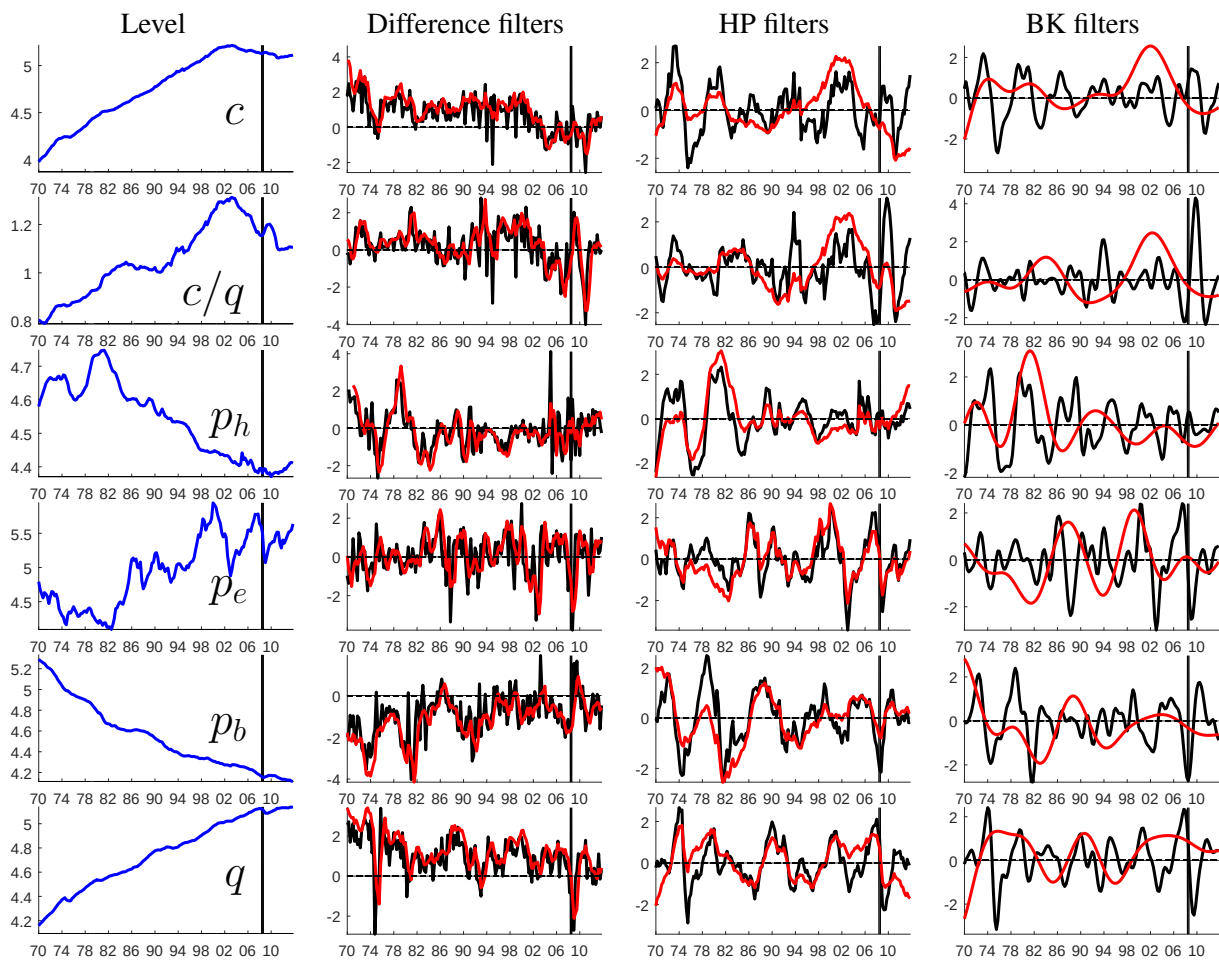


Figure 14: Germany's financial and business cycle indicators and their detrended components: Δ , HP (1600), and BK (1.5,8) filter in black; Δ_4 , HP (400000), and BK (8,30) filter in red

Notes: All series, except the level, are standardised to unit variance for ease of exposition. Each row refers to the variable indicated in the left-hand panel. Black vertical lines indicate the onset of systemic banking crises as defined by Laeven and Valencia (2012). c denotes total credit, c/q credit-to-GDP, p_h house prices, p_e equity prices, p_b bond prices, and q output.

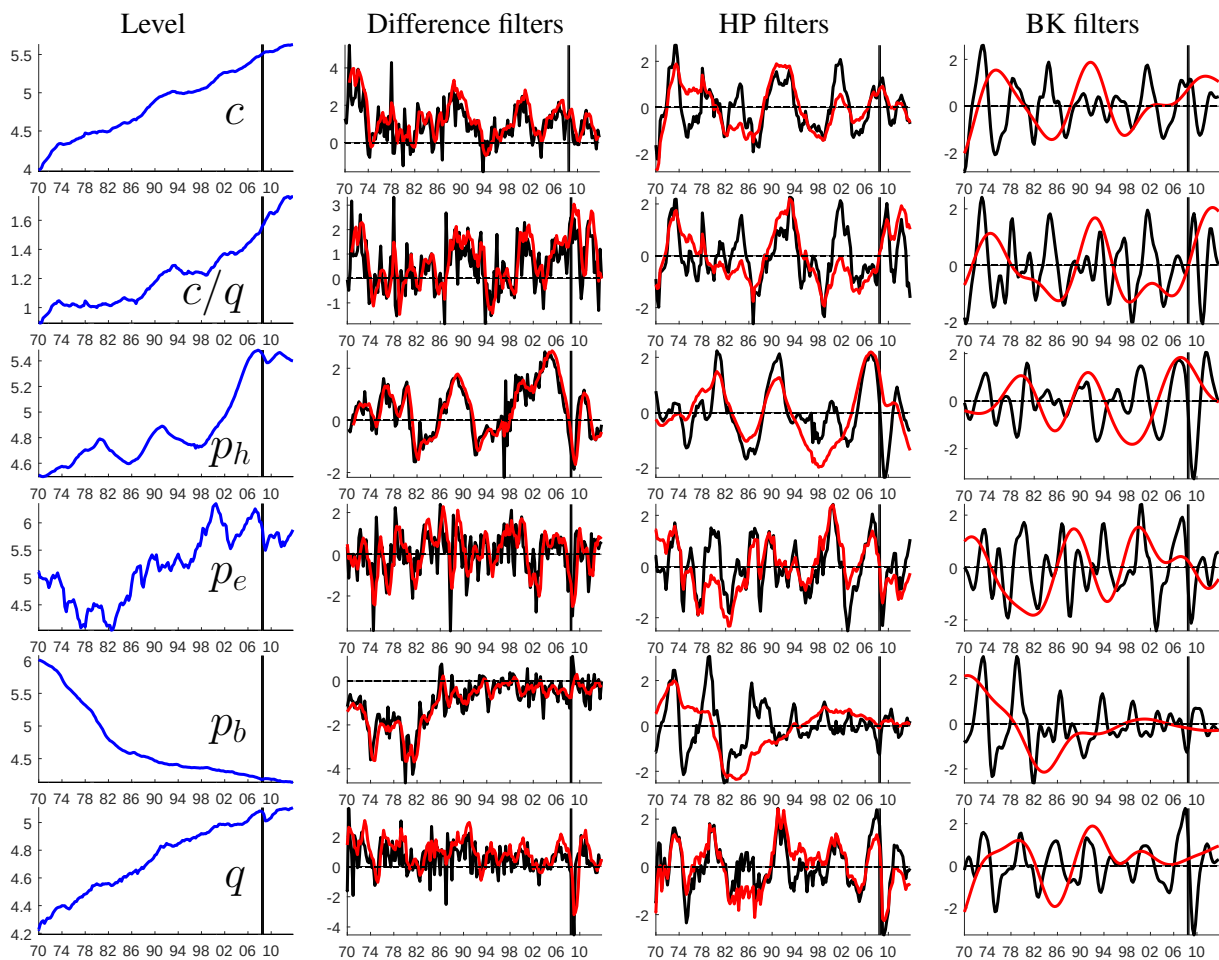


Figure 15: France's financial and business cycle indicators and their detrended components: Δ , HP (1600), and BK (1.5,8) filter in black; Δ_4 , HP (400000), and BK (8,30) filter in red

Notes: All series, except the level, are standardised to unit variance for ease of exposition. Each row refers to the variable indicated in the left-hand panel. Black vertical lines indicate the onset of systemic banking crises as defined by Laeven and Valencia (2012). c denotes total credit, c/q credit-to-GDP, p_h house prices, p_e equity prices, p_b bond prices, and q output.

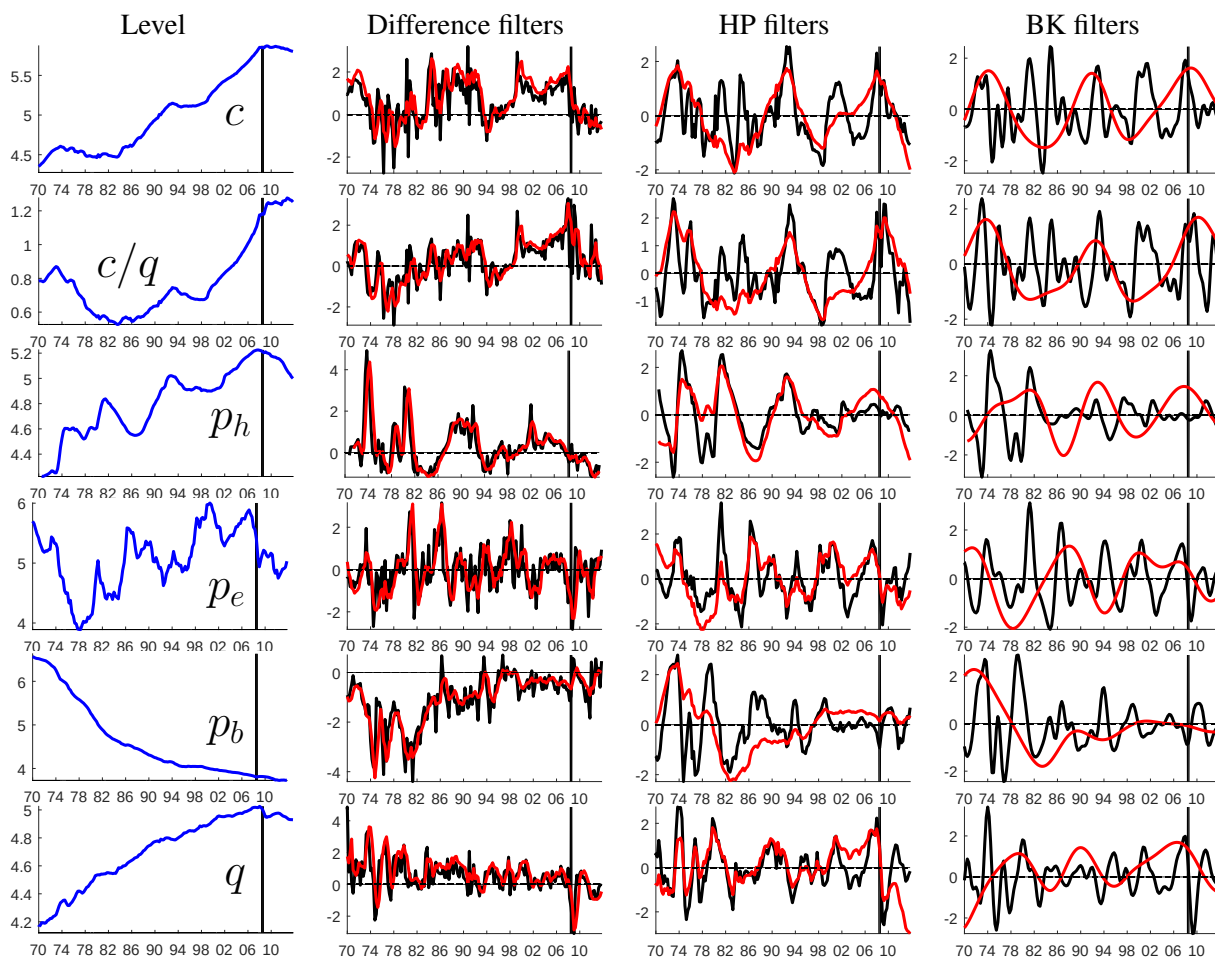


Figure 16: Italy's financial and business cycle indicators and their detrended components: Δ , HP (1600), and BK (1.5,8) filter in black; Δ_4 , HP (400000), and BK (8,30) filter in red

Notes: All series, except the level, are standardised to unit variance for ease of exposition. Each row refers to the variable indicated in the left hand panel. Black vertical lines indicate the onset of systemic banking crises as defined by Laeven and Valencia (2012). c denotes total credit, c/q credit-to-GDP, p_h house prices, p_e equity prices, p_b bond prices, and q output.

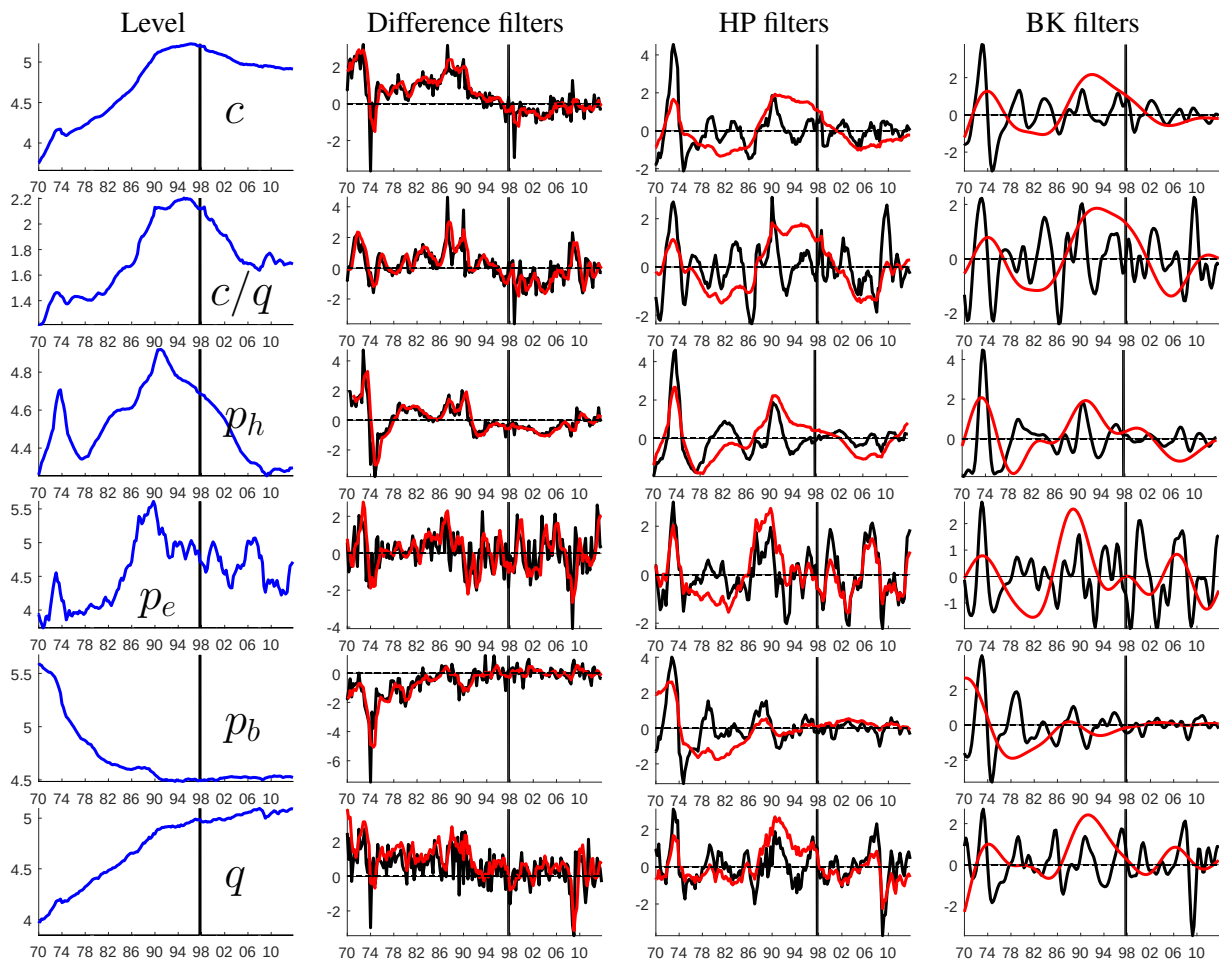


Figure 17: Japan's financial and business cycle indicators and their detrended components: Δ , HP (1600), and BK (1.5,8) filter in black; Δ_4 , HP (400000), and BK (8,30) filter in red

Notes: All series, except the level, are standardised to unit variance for ease of exposition. Each row refers to the variable indicated in the left-hand panel. Black vertical lines indicate the onset of systemic banking crises as defined by Laeven and Valencia (2012). c denotes total credit, c/q credit-to-GDP, p_h house prices, p_e equity prices, p_b bond prices, and q output.

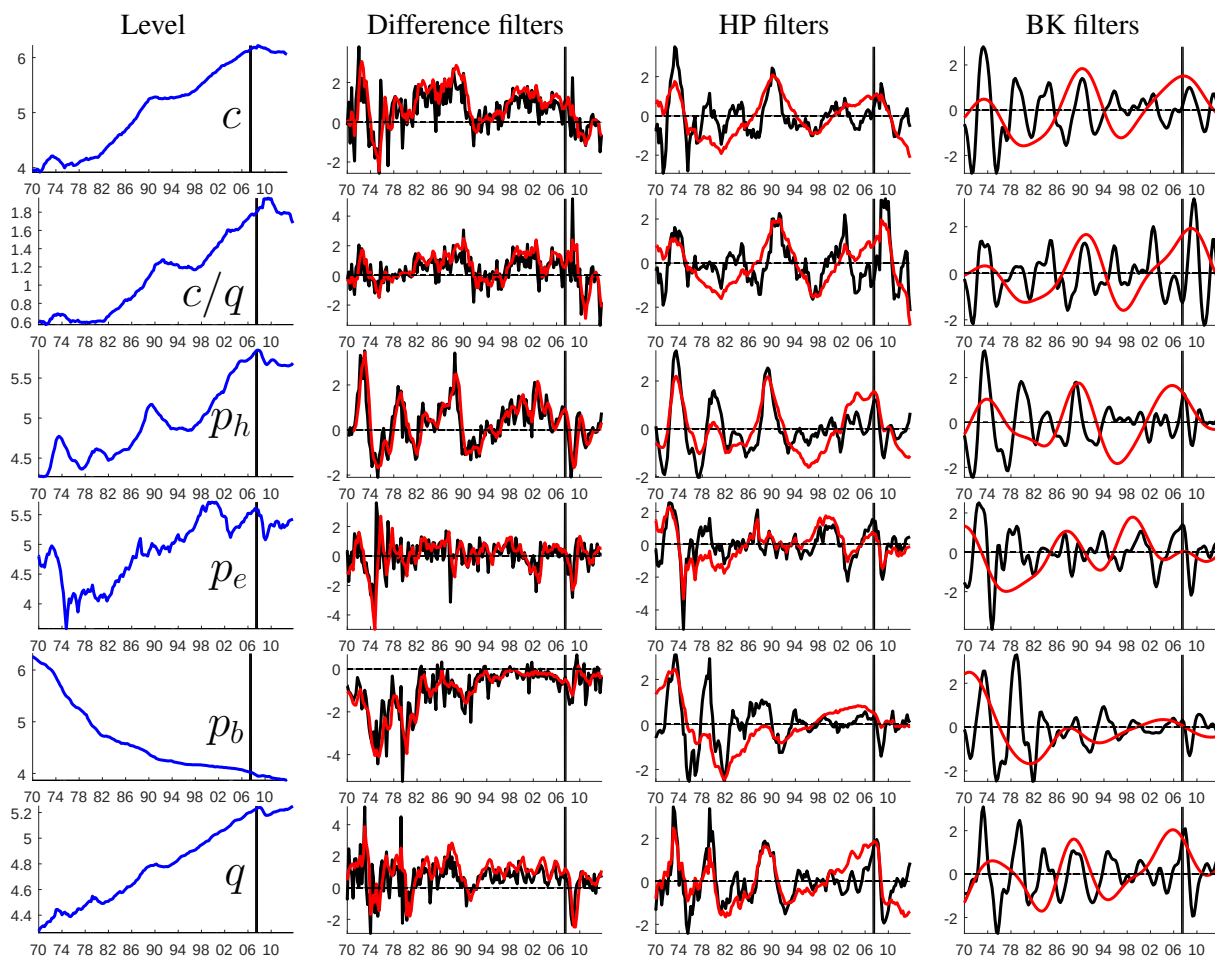


Figure 18: UK's financial and business cycle indicators and their detrended components: Δ , HP (1600), and BK (1.5,8) filter in black; Δ_4 , HP (400000), and BK (8,30) filter in red

Notes: All series, except the level, are standardised to unit variance for ease of exposition. Each row refers to the variable indicated in the left-hand panel. Black vertical lines indicate the onset of systemic banking crises as defined by Laeven and Valencia (2012). c denotes total credit, c/q credit-to-GDP, p_h house prices, p_e equity prices, p_b bond prices, and q output.

A.2.2 Credit-to-GDP gap: Two-sided versus one-sided HP filter

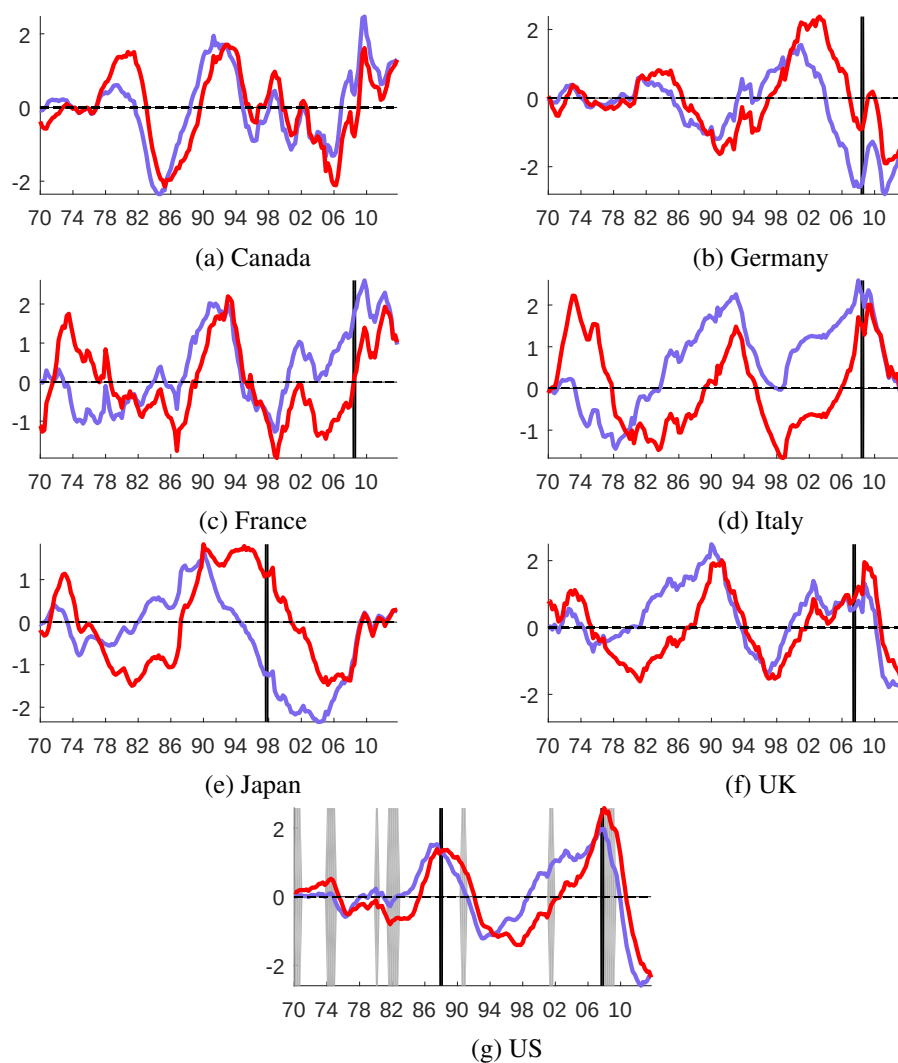


Figure 19: Credit-to-GDP gap: Two-sided (red) versus one-sided (purple) HP filter

Notes: Black vertical lines indicate the onset of systemic banking crises as defined by Laeven and Valencia (2012). All series are standardised to unit variance for ease of exposition.

Acknowledgements

I would like to thank Klaus Adam, Geert Bekaert, Claudia Foroni, James Hamilton, Lutz Kilian, Fabian Krüger, Petros M. Migiakis, Emanuel Mönch, Gerhard Rünstler, Bernd Schwaab, Lars Svensson, Jesus Fernandez-Villaverde, Mark Watson, and Kenneth West for helpful discussions. Further, I would like to thank the audience at the CFE 2016, 1st Annual Workshop of the ESCB Research Cluster 3, and the Bundesbank Research Seminar, as well as an anonymous referee for their valuable comments and suggestions. Annika Bacher provided outstanding research assistance. The views expressed in this paper are those of the author and do not necessarily coincide with the views of the Deutsche Bundesbank, the European Central Bank, or the Eurosystem. Any errors are the responsibility of the author.

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ISSN	1725-2806 (pdf)	DOI	10.2866/28808 (pdf)
ISBN	978-92-899-3243-1 (pdf)	EU catalogue No	QB-AR-18-018-EN-N (pdf)