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Investment Reluctance in Supply Chains: An Agent-Based Real Options Approach

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ABSTRACT

This paper shows how agent-based stochastic approaches can provide a complementary and more flexible approach to study investment incentives and price dynamics in a real options framework. We particularly study the case of two-stage production chains in which one sector produces an intermediate product and the other the final product, and the intermediate product is traded on the spot market. An agent-based competitive model using a genetic algorithm allows us to explicitly model the behaviors and interactions of the firms competing in each subsector and trading the intermediate product with each other on a spot market, and optimal investment strategies can be identified.

Keywords: Real Options; Supply Chain; Agent-Based Models; Genetic Algorithms

1. Introduction

According to the real options approach, irreversible investment decisions under uncertainty should consider the opportunity costs of deferring the investment decision in order to obtain improved information on the involved risks ([1,2]). Particularly [3,4] illustrate how option values as well as optimal investment triggers can be determined. Numerous empirical applications apply the developed concepts and show that price uncertainty creates investment reluctance beyond risk aversion. The very most of these studies ignore strategic aspects and presume the uncertainty to be exogenous. This simplification can be justified by [5] who showed that under perfect competition the endogenous price response to demand shocks leads to price dynamics with identical investment triggers, i.e. a myopic investor can ignore competition. Comparatively little research has been undertaken to study the more complex strategic interactions. Nevertheless, there are a number of analyses which identify equilibrium conditions for game theoretic settings, including [6-8]. A particular strength of these studies is that the equilibrium conditions are based on closed-form analytical solutions. While this allows the derivation of quite general results, also limitations exist such as restrictive assumptions regarding e.g. the assumed stochastic process and homogeneity.

Because of the limitations of the analytical approaches, the objective of this paper is to illustrate that agent-based stochastic approaches may provide a complementary approach to study more flexible settings. Therefore, we show how agent-based models can be applied to a real options framework and what additional insights into the resulting market dynamics they can provide. Starting point is a simple two-stage value chain in which one sector produces an intermediate product while the second sector produces the final product. An empirical application of such a situation is provided by [9] who study the pork chain in Finland using a real options approach. The pork chain also provides a good example for our setting as we can presume a polypolistic market structure, a one to one relation between the two sectors as well as a non-storable intermediate product. This results in a high volatility of the intermediate product’s price. To compare the alternative production chains, we apply an agent-based framework. As an example of a perfectly integrated system, every firm can invest in an integrated system in which the intermediate product and the final product are produced in equal amounts. In the alternative production system, one group of firms can invest in the intermediate product, while a second group of firms can invest in the final product. The intermediate product is assumed to be...
traded on a spot market. As source of uncertainty, it is assumed that an iso-elastic demand curve for the final product follows a random walk.

Within this setting, the subsectors and the spot market interaction are explicitly modeled. Instead of looking at the market at an aggregate level, we develop an agent-based model which follows a bottom-up approach by explicitly modeling the firms and their behavior, as well as their interaction. In this discrete-time model, a number of agents represent identical firms which compete within their subsector and trade with another subsector. The firms identify optimal investment strategies for Monte Carlo simulations of demand shocks for the final product and can invest irreversibly into production assets without knowing how the market environment will evolve in the future. Producers of the intermediate product and producers of the final product are assumed to be aware of the investment strategies and the production capacities of other producers, i.e. we presume a rational expectation hypothesis. Moreover, the producers of the intermediate product are assumed to know the actually existing production capacity of the producers of the final product, but not the actual (dis-)investments. Every firm invests according to its individual investment trigger which is derived by linking Monte Carlo simulations of the agent-based model with a genetic algorithm (cf. [10,11]). The combination with genetic algorithms allows identifying dynamic investment equilibria for polypolistic as well as for oligopolistic settings by either using a social or an individual learning approach ([12]). As we address a polypolistic market structure, we apply a social learning approach.

The model is adapted to parameters and cost structures reflecting pork production in the EU and thus considers, as in [9], piglets as the intermediate product and finished hogs as the final product. Our analysis shows that the closed system and spot market solutions both lead to very similar production dynamics. Differences in investment behavior are only marginal, even in the case of inelastic demand respectively high price flexibility for the intermediate product. This contradicts what [9] found for pork production chains in Finland but the differences can be attributed to the different methodological approaches applied; e.g. we here model firms’ behaviors explicitly assuming rational expectations instead of looking at the market at an aggregate level.

The outline of this paper is the following. First, the model and the application of the genetic algorithm are described, followed by a description of the parameters reflecting the pork supply chain which are used in the simulations. The model is thereafter validated and the simulation results presented. Summary and conclusions end the paper.

2. Model and Scenarios

2.1. An Agent-Based Investment Model of a Two Stage-Value Chain

In order to model the interactions between firms within a two-stage value chain in which one sector produces an intermediate product and the other sector produces the final product, an agent based approach is used. This allows for explicitly modeling the behaviors and interactions of the firms competing in each subsector and trading the intermediate product with each other on a spot market. The two-stage scenario is compared with a scenario of one sector producing the final product in a one-stage production system, i.e. a vertically integrated (or closed) production system. We begin the model description by presenting the investment problem in the latter case, which is similar to [11,13]. Thereafter we extend the model to the case of a two-stage system in which the intermediate and final products are produced by the separate sectors and traded on a spot market.

In a time-discrete setting it is assumed that $N$ firms repeatedly have the opportunity to invest in identical assets or a fraction thereof, and that no firm has initially invested. The asset stock of firm $n$ has a maximum size of 1 and can be used by the firm to produce up to $x_n\leq 1$ units of output per period. Size, investment outlay and production are assumed to be proportional, i.e. there are no economies of scale. If a firm invests for the first time, its maximum initial investment outlay $M_{\text{max}}$ is 1. The investment outcome $M_{i,n}$ is assumed to be totally sunk after the investment is carried out. In every future period, a geometrical decay of the asset with a depreciation rate $\lambda$ is assumed. However, in every period, the firms can invest or reinvest in order to increase production or to regain a production capacity of up to one unit of output. The total asset of firm $n$ in period $t + \Delta t$ can thus be written as:

$$x_{i,n,t+\Delta t} = (1-\lambda)^{\Delta t} \cdot x_{i,n,t} + \frac{M_{i,n}}{I}$$

such that $x_{i,n,t+\Delta t}^{\max} = 1$ and where $M_{i,n}/I$ is the additional available asset in $t + \Delta t$ due to investment decision in $t$.

Each firm’s investment decisions aim to maximize the expected net present value of future cash flows by choosing an optimal investment trigger, $P^*$. The objective function of firm $n$ is thus represented by:

$$\max_{P^*} \{ \hat{\Pi}_n(P^*) \}$$

where $\hat{\Pi}_n(P^*) = E \left[ \sum_{t=0}^{\infty} \left( x_{t,n} \cdot (P_t - c) - M_{t,n} \left( x_{t,n}, P^*_n \right) \right) \cdot (1+r)^{-t} \right]^{-1}$

and where $P_t$ is the output price in period $t$, $c$ is the variable production costs per unit of output and period, and $r$
is the risk-free interest rate. To capture competition, the firms and their interaction are represented in an agent-based setting in which the firms are represented as agents that perceive their environment and respond to it individually and autonomously ([14]).

The environment of a firm \( n \) consists of two parts: the behavior of other firms and the demand for outputs. Total supply in period \( t \) is

\[
X_i^S = \sum_{n=1}^{N} X_{i,n}^S
\]

and demand is

\[
X_i^D = \frac{\alpha_i}{(P_i)^{\eta}}
\]

where \( \eta \) is the elasticity of demand. For the identity of demand and supply, (6) must hold:

\[
P_i = \left( \frac{\alpha_i}{X_i^D} \right)^{\frac{1}{\eta}} = \left( \frac{\alpha_i}{X_i^S} \right)^{\frac{1}{\eta}}
\]

The demand parameter \( \alpha_i \) is assumed to follow a geometric Brownian motion. Assuming discrete time, this can be modeled as

\[
\alpha_i = \alpha_{i-\Delta t} \cdot \exp \left[ \left( \mu - \frac{\sigma^2}{2} \right) \cdot \Delta t + \sigma \cdot \epsilon_i \cdot \sqrt{\Delta t} \right]
\]

with a volatility \( \sigma \), a drift rate \( \mu \), and where \( \epsilon_i \) is a normally distributed random number and \( \Delta t \) is the time step length.

Firm \( n \) invests in period \( t \) if the expected price \( \hat{P}_{t+\Delta t} \) is larger than or equal to the trigger price \( P^\prime_n \). For the expected price \( \hat{P}_{t+\Delta t} \), the following holds:

\[
\hat{P}_{t+\Delta t} = \left( \frac{\hat{\alpha}_{t+\Delta t}}{X_{t+\Delta t}} \right)^{\frac{1}{\eta}} \quad \text{with} \quad \hat{\alpha}_{t+\Delta t} = \alpha_{t+\Delta t} \cdot \exp \left[ \left( \mu - \frac{\sigma^2}{2} \right) \cdot \Delta t + \sigma \cdot \epsilon_i \cdot \sqrt{\Delta t} \right]
\]

\[
\hat{X}_{t+\Delta t} = \sum_{n=1}^{N} X_{t+\Delta t,n} \quad \text{and} \quad \hat{X}_{t+\Delta t,n} = \begin{cases} 1, & \text{if } n \text{ invests } M_{t+\Delta t,n} = M_{t+\Delta t,n}^\text{max} \\ (1-\lambda)^{\hat{X}_{t+\Delta t,n}} \cdot X_{t+\Delta t,n} + \frac{M_{t+\Delta t,n}}{I}, & \text{if } n \text{ invests } 0 < M_{t+\Delta t,n} < M_{t+\Delta t,n}^\text{max} \\ (1-\lambda)^{\hat{X}_{t+\Delta t,n}} \cdot X_{t+\Delta t,n}, & \text{if } n \text{ invests } M_{t+\Delta t,n} = 0 \end{cases}
\]

The questions now are: Which firms invest and how much do they invest? It is assumed that firms with lower trigger prices \( P^\prime_n \) have a stronger tendency to invest. Consequently, all firms can be sorted according to their trigger prices, starting with the lowest investment trigger, \( i.e., P^\prime_n \leq P^\prime_{n+1} \). It is considered that: 1) If firm \( n \) does not invest in \( t \), firm \( n+1 \) will also not invest in \( t \), \( i.e., M_{t,n} = 0 \Rightarrow M_{t+1,n+1} = 0 \), 2) If firm \( n \) does invest in \( t \), then firm \( n-1 \) will invest \( M_{t,n-1}^\text{max} \) in \( t \), \( i.e., M_{t,n-1} > 0 \Rightarrow M_{t+1,n-1} = M_{t+1,n-1}^\text{max} \Rightarrow x_{t+1,n-1} = 1 \).

In every period \( t \), a marginal (or last) firm \( n^\prime \) exists which invests \( M_{t,n} \) such that the expected price for the next period is equal to the investment trigger of firm \( n^\prime \), \( i.e., P^\prime_n = \hat{P}_{t+\Delta t} \) with \( 0 < M_{t,n} \leq M_{t,n}^\text{max} \) and \( 0 \leq n^\prime \leq N \).

The investment of firm \( n^\prime \) can be computed according to

\[
P^\prime_n = \hat{P}_{t+\Delta t} = \left( \frac{\alpha_{t+\Delta t}}{\hat{X}_{t+\Delta t}} \right)^{\frac{1}{\eta}}
\]

\[
x_{t+\Delta t,n^\prime} = \left( \frac{\hat{\alpha}_{t+\Delta t}}{P^\prime_n} \right)^{\frac{1}{\eta}} - \left( (n^\prime - 1) + (1-\lambda)^{\Delta t} \sum_{n=n^\prime+1}^{N} x_{t,n} \right)
\]

\[
M_{t,n}^\text{max} = \frac{\hat{\alpha}_{t+\Delta t}}{I} \left( n^\prime - 1 \right) - (1-\lambda)^{\Delta t} \sum_{n=n^\prime+1}^{N} x_{t,n}
\]

\( n^\prime \) can now be identified by iteratively testing all firms for \( P^\prime_n < \hat{P}_{t+\Delta t} \). The last firm with a positive investment is \( n^\prime \).

Equation (11) is an equilibrium condition: All firms which fully invest and hence produce at maximum capacity have trigger prices which are less than or equal to the trigger price of firm \( n^\prime+1 \) which is also equal to the expected price for \( t+\Delta t \). All firms which do not invest have trigger prices which are higher than or equal to the expected price for \( t+\Delta t \).

For a given set of trigger prices, \( P^\prime_n \), and arbitrary initializations of \( \alpha_0 \), the expected profitability of each strategy

\[
\hat{\Omega}_n \left( P^\prime_n \right) = \mathbb{E} \left[ \sum_{t=0}^{\infty} \left( P_{t+\Delta t,n} - c - M_{t+\Delta t,n} \left( x_{t+\Delta t,n} \cdot P_{t+\Delta t,n} - \hat{P}_{t+\Delta t} \right) \right) \cdot (1+r)^{-\Delta t} \right]
\]

can be simultaneously determined by a sufficiently high number of repeated stochastic simulations of the market. Due to the competitive environment and identical production technologies, the expected profitability of a rational strategy will fulfill the zero-profit condition given all other strategies are also rational.

Until now, the model reflects a firm’s investment problem for a closed production system in which the intermediate product and the final product are produced in appropriate amounts within a production unit. The investment cost \( I \) is then assumed to cover the costs for both production assets, \( i.e., I = \alpha I + \beta I \), where the italic

Note that \( n^\prime \) is zero if there is no investor in period \( t \).
superscripts on the left side denote intermediate and the final product respectively.

The question is now what the consequences of a spot market relationship between the producers of the intermediate and final product for their investment triggers are. In such a system, the production capacity of the producer of the final product can be interpreted as a demand parameter of the producers of the intermediate product, i.e.

$$\beta X = \ln \alpha$$  \hspace{1cm} (13)

Regarding the price formation for the intermediate product, a logistic relationship is considered. This allows for a maximum price of $$\ln P_{i}^{\text{max}}$$ to avoid that the expected gross margin of the final product is negative as well as to ensure that there is a minimum price for the intermediate product $$\ln P_{i}^{\text{min}}$$ assuring non-negativity of gross margins for the intermediate product. Considering iso-elastic demand for the intermediate product, the market equilibrium for the first-stage producers fulfills

$$\ln P_{i} = \frac{\ln P_{i}^{\text{max}}}{1 + e^{\ln \alpha_{i} \ln P_{i}^{\text{max}} - \ln P_{i}^{\text{min}}}} \text{ with } R_{i} = \left(\frac{\beta X_{i}}{\ln X_{i}}\right)^{-\eta} \text{ and (14)}$$

a normalization parameter

$$Q_{i} = -\ln \left(\frac{\ln P_{i}^{\text{max}}}{\ln P_{i}^{\text{max}} - 1}\right) \cdot \left(\ln P_{i}^{\text{max}} - 1\right)^{-1}.$$  \hspace{1cm} (15)

The normalization parameter $$Q_{i}$$ ensures that in case of identity of production capacities of the two producers, the price of the intermediate product is proportional to the relation of the price triggers of the final and intermediate products. $$R_{i}$$ is to be interpreted as a price response coefficient considering the relation of supply and demand for the intermediate product where $$\ln \eta$$ represents a kind of “demand elasticity” for the intermediate product.

The intermediate producer $$n$$ invests in the marginal investor in the period $$t + \Delta t$$ is

$$\ln P_{i, t + \Delta t} \text{ is larger than or equal to her trigger price } \ln P_{i}^{*}.$$  \hspace{1cm} (16)

Total production of the intermediate product in the period $$t + \Delta t$$

$$\ln x_{i, t + \Delta t} = \frac{\ln x_{i, t} \alpha_{i} P_{i}^{*}}{\ln P_{i}^{*}} - \sum_{n=1}^{\ln x_{i, t}} \alpha_{n} x_{i, t}^{\text{max}} - \alpha \lambda \sum_{n=1}^{\ln x_{i, t}} \ln x_{n, t}^{\text{max}} - \ln X_{i, t}$$  \hspace{1cm} (17)

where $$\hat{P}_{i} = \left(\hat{P}_{i + \Delta t}\right)^{0.8} (\ln P)^{0.2}$$, i.e. an adaptive price expectation is used as a proxy. Note that in contrast to the one-stage case, the net return for the producers of the final products $$\beta G$$ must be adjusted by the price of the intermediate product and other variable costs in the second stage, $$\beta c$$. Additionally, since the second stage producers would not spend more money on the intermediate product and other variable costs than the expected return for the final product, the expected minimum net return is zero which is formalized in Equation (16):

$$\beta G = \begin{cases} 0, & \text{if } \ln P_{i}^{*} + \beta c \geq \hat{P}_{i}^{*} \\ \left(\frac{\beta \alpha_{i}}{\ln \eta}\right) - \ln P_{i}^{*} - \beta c, & \text{otherwise} \end{cases}$$  \hspace{1cm} (16)

The following is assumed to hold for the second stage producers:

$$\beta X = \ln P_{i}^{*} \left(\ln \alpha_{i} \right)^{-\eta}$$  \hspace{1cm} (17)

As for the closed system, the optimal trigger prices, $$\ln P_{i}^{*}$$ and $$\ln P_{i}^{*}$$, are determined by combining the multi-firm market models with a genetic algorithm (GA), which is described in the following section.

### 2.2. The Genetic Algorithm and Its Implementation

Even though many variations of GA exist, some common elements can be recognized (cf. [15-18]). The first task of a GA application is to specify a way of representing each possible solution or strategy as a string of genes located on one or more chromosomes. Since our problem is relatively simple, i.e. we are searching for a single value (every strategy consists just of a certain trigger price) and we can assume a convex search space, we take the investment trigger as a real value and apply the GA operators to the nominal value of trigger price. The second task is to define a population of genomes to which the genetic operators, i.e. selection, crossover and mutation, can be applied. The population size is set equal to $$N$$, the number of firms. This allows the direct mapping of the set of genomes to the various firms’ strategies, i.e., every firm’s trigger price in our model is represented by one genome from the genome population.

After random initialization, the genome population passes, in every generation, through the steps of fitness evaluation, selection, recombination (crossover) and mutation. These operators are in our model implemented in the following way:

**Fitness evaluation:** The fitness value is directly derived from the strategy’s average profitability for 1000 to 5000 repeated stochastic simulations of the market model.

**Selection:** The selection procedure replaces the least profitable strategies with the most profitable ones. The higher the relative profitability, the higher is the prob-
ability for replication.

Recombination: For recombination or crossover, the geometric average of two parent genomes is calculated resulting in one offspring which replaces one parent.

Mutation: Mutation is implemented here by multiplying every solution by chance (with a small likelihood) with a random number within a closed range (e.g., [0.95, 1.05]. The mutation likelihood, as well as the range of the random number, may be chosen according to experience or according to the already obtained results.

These steps are repeated until the model converges (i.e. the strategies are similar from one generation to the other). A flow diagram of this procedure can be found in Figure A1 in the appendix. In one particular point, our GA application deviates from the conventional use of GA for optimization problems. Here, the GA is not just used to solve a complex optimization problem in which the goodness of the solution respectively the problem at hand are directly related. In our case, the goodness of a solution rather depends on the alternative solutions generated by the GA, i.e., the genomes compete directly. Thus, we are applying the GA to a market and we are searching not just for an optimal solution, but for an equilibrium solution (i.e., the Nash-equilibrium strategy). A number of publications during the past 15 years show that agent-based GA approaches function quite well for analyzing such strategic interactions. Examples and discussions are given, for instance in [10,19-22]. However, as [12] shows, one has to differentiate whether one aims to identify an equilibrium investment rate of 5% (in the base scenario), and a time step length of 0.25. This implies that an investment cost of 5% 10% or 15%. The total time span is determined as 100 years. For later periods, the expected returns are set equal to the returns in year 100. The possible error can be assumed to be negligible since later returns are discounted by more than 99.7%.

Regarding production costs, it is assumed that the total production cost per piglet is 2.5 (which, multiplied by 20, corresponds to 50 € per piglet), of which 1.0 (20 €) is fixed costs (related to the annual irreversible investment cost) and 1.5 (30 €) is variable costs. The production costs for pork (per hog) are 3.5 (which multiplied by 20, corresponds to 70 € per hog), of which 1.0 (20 €) is fixed costs (related to the annual irreversible investment cost) and 2.5 (50 €) is variable costs, plus the cost of the piglet. These production costs correspond approximately to the cost structure of pig production within the EU.

3. Validation and Results

3.1. Validation of the Model

In order to validate the agent-based model of multiple competing farms, it can be shown that the agent-based approach leads for the standard case of a one-stage production system to the same dynamics as a direct simulation of the price dynamics.

Consider the existence of an equilibrium investment trigger $P^*$ at which all firms invest and assume that in period $t - \Delta t$ firms have invested according to $P_{t-\Delta t} = P^*$. From Equations (6) and (7) we know that after the investment decisions are made, $P_t$ purely depends on the relation of $\alpha_i$ and $a_{i,t}$. Hence, the price in $t$ will be

$$P_t = P^* \cdot \exp \left[ \left( \frac{\mu - \sigma^2}{2} \right) \cdot \Delta t + \sigma \cdot \epsilon \cdot \sqrt{\Delta t} \right]. \quad (18)$$

Consider now that the actual price in period $t$ is $P_t \geq P^*$. Then the firms will respond and invest such that $P_{t+\Delta t} = P^*$. For $P_t \leq P^*$, two cases have to be differentiated. If $P^* \geq P_t > (1 - \lambda)^{\Delta t} \cdot P^*$ then some firms will reinvest, such that $P_{t+\Delta t} = P^*$. Otherwise, if $P_t \leq (1 - \lambda)^{\Delta t} \cdot P^*$ no firm will reinvest and $P_{t+\Delta t} = P_t (1 - \lambda)^{\Delta t}$. With this knowledge and in accordance with Equations (1) to (12) the price dynamics can be described as:

$$P_t = P^* \cdot \exp \left[ \eta \cdot \left( \frac{\sigma^2}{2} \cdot \Delta t + \sigma \cdot \epsilon_i \cdot \sqrt{\Delta t} \right) \right],$$

If $P_{t+\Delta t} \geq \exp \left[ -\eta \cdot (\mu - \ln (1 - \lambda) \cdot \Delta t) \right] \cdot P^*$

$$P_{t+\Delta t} = P_{t+\Delta t}, \quad (19)$$

otherwise.

The figures are within the same range as those reported by [23,24].
Equation (19) represents the discrete time version of a so-called regulated Brownian motion, which permits the simulation of price dynamics directly, i.e., without the explicit representation of firms ([5,25]). Moreover, (19) can be used to determine the equilibrium investment trigger $P^*$. Repeated stochastic simulations of Equation (19) for various values of $P^*$ should reveal that the zero-profit condition will only be fulfilled if $P^*$ is equal to the equilibrium investment trigger. If $P^*$ is higher, the dynamics should allow for profits. If $P^*$ is smaller, this should imply losses. Accordingly, the equilibrium trigger price $P^*$ can be determined by minimizing the square of the expected profits, i.e.

$$
\min_{P^*} \left\{ E^2 \left[ \left( P^* \right) \right] \right\} =
$$

$$
E^2 \left[ \sum_{t=0}^{\infty} \mathbb{I}_{k,t,r} \left( P_{t-M} - c \right) - M_{t-M,r} \left( x_{t-M,r}, P^* \right) \left( 1 + r \right)^{-t-M} \right] \right\}
$$

with $P_0 = P^*$ and $P_t$ follows Equation (19).

Figure 1 shows that for identical trigger prices, $P^*$, and identical $\alpha$, the agent-based model and the direct price simulation lead to an identical price path. Moreover, the direct price simulations lead to identical trigger prices. Hence, the direct price simulation validates the results of the agent-based approach.

### 3.2. Results

Our results suggest that vertical integration does not strongly influence production volume and welfare. This is shown by Figure 2. For given dynamics of demand for pork, the scenarios lead to very similar price paths. The fluctuations in piglet prices in the simulated data arise because we assume there is not an exact adjustment of piglet production to the hog finishing capacities (this is implied by Equation (14)).

Table 1 presents the trigger prices for investments under alternative assumptions concerning the parameter values for demand elasticities and volatility. For a given demand elasticity, the trigger prices for pork in the closed systems do not differ substantially from the trigger prices of the spot market solution. In general, the difference is below 0.1% of the trigger price respectively 0.5% of the difference between the trigger price and the total production cost. Thus, our results suggest that from a pure real options perspective, a stronger vertical integration does not significantly increase investments. This result contradicts the empirically-based results of, e.g., [9]. This may be explained by our implicit assumption of rational expectations regarding the behavior of competitors as well as the information about the current production capacities on the other production stage. This, however, is not unrealistic considering that public statistics usually provides information about production capacities of piglet and pork producers. Moreover, capacity differences are usually reflected in market prices, which give signals to invest or disinvest in reasonable time. In the following analysis, the assumptions of $\sigma = 10\%$ and $\lambda = \lambda = 0.05$, $\eta = \eta = 0.5$ will be used (estimated demand elasticities for pork that can be found in the literature are often around $-0.5$).

In order to analyze the impact of the price flexibility on the spot market for piglets, demand elasticities for piglets have been varied. In Table 2, it is illustrated that the trigger prices are not affected substantially when varying the demand elasticity for piglets. Accordingly, the above presented findings can be considered as robust against assumptions regarding the definition of the piglet prices.

A variation of the useful lifetime of the breeding barns (represented by the depreciation rate) changes the price dynamics for piglets. This is illustrated in Table 3. However, variations of the depreciation rate of breeding barns do not affect the trigger price for finishing barns strongly. Higher depreciation rates for piglet breeding barns lower their trigger price as a consequence of the higher flexibility of piglet production. Vice versa, lower depreciation

---

1If we would consider that piglet and pork producers would be perfectly aware of the investment behaviour of each side, identical trigger prices for closed systems and market interaction would be achieved.

2E.g., [26] obtained an elasticity of demand for pork of $-0.47$. 

---
Table 1. Trigger prices in closed systems and spot market solutions for different demand elasticities \( (\eta \lambda = \eta = 0.05) \).

<table>
<thead>
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<th>( \eta )</th>
<th>( \pi^\ast )</th>
<th>( \pi = \pi )</th>
<th>( \pi^\ast \pi )</th>
<th>( \pi^\ast \pi^C )</th>
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<tr>
<td>( \sigma = 10% )</td>
<td>-1/2</td>
<td>6.677</td>
<td>-1/2</td>
<td>2.783</td>
<td>6.687</td>
</tr>
<tr>
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<td>-1/3</td>
<td>2.891</td>
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<td>1.157</td>
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<tr>
<td>-s1/6</td>
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<td>-1/6</td>
<td>3.037</td>
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<td>6.829</td>
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<td>( \sigma = 15% )</td>
<td>-1/2</td>
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<td>-1/2</td>
<td>3.082</td>
<td>7.470</td>
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<td>7.882</td>
<td>-1/3</td>
<td>3.220</td>
<td>7.910</td>
<td>1.318</td>
</tr>
<tr>
<td>-s1/6</td>
<td>8.297</td>
<td>-1/6</td>
<td>3.237</td>
<td>8.349</td>
<td>1.392</td>
</tr>
</tbody>
</table>

Table 2. Trigger prices in closed systems and spot market solutions for different demand elasticities for piglets \( (\kappa \eta = -1/2, \eta \lambda = \eta = -1/2, \sigma = 10\% ) \).

<table>
<thead>
<tr>
<th>( \pi^\ast )</th>
<th>( \kappa \eta )</th>
<th>( \pi^\ast \pi )</th>
<th>( \kappa \pi^\ast \pi )</th>
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<tbody>
<tr>
<td>6.677</td>
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<td>6.687</td>
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<tr>
<td></td>
<td>-1</td>
<td>2.778</td>
<td>6.687</td>
</tr>
<tr>
<td>5%</td>
<td>-1/2</td>
<td>2.783</td>
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<tr>
<td></td>
<td>-1/3</td>
<td>2.806</td>
<td>6.688</td>
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<td></td>
<td>-1/6</td>
<td>2.871</td>
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</table>

Table 3. Trigger prices depending on depreciation rates \( (\kappa \eta = \kappa \eta = -1/2, \sigma = 10\% ) \).

<table>
<thead>
<tr>
<th>( \lambda ) (in %)</th>
<th>( \pi^\ast )</th>
<th>( \kappa \lambda ) (in %)</th>
<th>( \kappa \lambda ) (in %)</th>
<th>( \kappa \pi^\ast )</th>
<th>( \kappa \pi^\ast \pi )</th>
</tr>
</thead>
<tbody>
<tr>
<td>5%</td>
<td>6.677</td>
<td>5%</td>
<td>10%</td>
<td>5%</td>
<td>2.783</td>
</tr>
<tr>
<td>10%</td>
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<td>10%</td>
<td>10%</td>
<td>2.696</td>
<td>6.672</td>
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<tr>
<td>20%</td>
<td>6.036</td>
<td>10%</td>
<td>20%</td>
<td>2.585</td>
<td>6.045</td>
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<tr>
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<td>20%</td>
<td>20%</td>
<td>2.506</td>
<td>6.044</td>
<td></td>
</tr>
</tbody>
</table>
rates for piglet breeding barns lead to a higher volatility of the piglet prices and therefore to higher trigger prices.

Figures 3 and 4 illustrate the dynamics of prices for hogs and piglets for different depreciation rates for breeding barns ($\mu_\lambda = 20\%$ and $\mu_\lambda = 5\%$ for $ho_\lambda = 10\%$). Note that if the depreciation rates for piglet and hog producers are equal, higher depreciation rates lead to lower trigger prices and vice versa. Higher depreciation is equivalent to higher flexibility of adjustment. That is to say, investments with high depreciation rates can be considered as less irreversible and thus also investment reluctance is lower. On the aggregate level, this means that production can relatively quickly respond to negative demand shocks. In [25] it is shown that the depreciation rate corresponds to a positive drift rate for prices. In the case that depreciation rates differ within a supply chain, this allows in certain situations the sector with the higher depreciations rate to exploit the upstream (downstream) sector.

Although the experiments show that certain assumptions regarding elasticities and depreciation rates have an impact on investment triggers of the different production steps, our general result is that from a pure real options perspective, closed systems are hardly superior to market solutions.

4. Summary and Conclusions

Participants along a production chain which exchange intermediate products on spot markets face price risks such as a certain transmission of price fluctuations of the final product. In a real options environment this uncertainty may cause investment reluctance on the different steps of the production chain. This paper analyses whether stronger vertical integration along the production chain reduces investment reluctance. For this purpose an agent-based competitive model of production chains was developed in which firms use optimal investment strategies identified by genetic algorithms. Two production systems were compared: As an example of a perfectly integrated system, it was considered that every firm can invest in closed systems in which the intermediate product is produced in equal amounts. In an alternative production system, firms can either invest in the intermediate product or the final product. The intermediate product is traded on a spot market.

Our simulations showed that the spot market solution and the closed system lead to practically the same production dynamics. The only precondition is that for the spot market system, producers of the intermediate product and producers of the final product have a good guess of the investment strategies and production capacities of other producers. This general finding is independent of different depreciation rates of the production steps, though the price dynamics for the intermediate product is strongly affected by the relation of depreciation rates on the different levels of the chain.

At first glance, our results may be intuitively surprising, but this is in accordance with several other surprising insights provided by the real options theory, for example, that myopic investors who ignore the impacts of competition behave efficiently ([5]) or that real options theory does not justify price stabilization policies ([27]).

5. Acknowledgements

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REFERENCES

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Appendix

Figure A1. Flow diagram of the agent-based simulation approach.

- $N$ = number of genomes
- $n = 1, \ldots, N$
- $G$ = number of generations
- $g = 1, \ldots, G$
- $S$ = number of stochastic simulations
- $s = 1, \ldots, S$
- $T$ = investment period
- $t = 0, \ldots, T$
- $r$ = interest rate
- $P$ = price