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# Luxembourg Income Study Working Paper Series

Working Paper No. 101

International Labor Underpayment:  
A Stochastic Frontier Approach

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*(scanned copy)*



INTERNATIONAL LABOR UNDERPAYMENT:  
A STOCHASTIC FRONTIER APPROACH

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## INTRODUCTION

The search theory of unemployment suggests that workers, after expending time and resources in the search process, may accept a position that provides compensation at a level below that which is appropriate to the worker's true capability. In this regard the worker is "underpaid" in the sense that there is unused worker capacity which could be productively employed if there was a perfect match between the worker and the actual job accepted.<sup>2</sup> This underpayment occurs because information about jobs is costly to acquire, because searchers possess positive discount rates, and because searchers have time horizons of finite length. As a result, searchers stop their job hunting before discovering the highest-paying job for which they are qualified.

From an overall United States economic perspective, the degree of underpayment represents lost output (reduced GDP). Since this loss is a result of inefficient matches in the labor market, the issue of federal policies to reduce such inefficiencies and improve national output may be important. Whether this issue is nationally important depends on the answers to two principal questions: (1) Does the amount of underpayment represent a major loss in U.S. GDP? and (2) Does the amount of underpayment in the United States compare favorably or unfavorably with our principal international competitors for the Global Market? If the answer to either of these questions suggests policy action by the U.S. government may be productive, appropriate policy alternatives should be considered. Such alternatives might be a national/regional "Job Bank" of readily available up-to-date

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<sup>2</sup> Mortensen (1970) makes this idea explicit and Ehrenberg and Smith (1988, p. 614) refer to this phenomenon as "underemployment." This type of "underemployment", however, is distinctly different from the more popular usage of the term: workers involuntarily working part-time when they prefer full-time jobs or workers holding jobs well beneath their capabilities. In order to distinguish between the concept to which we refer, i.e., the shortfall of wages below what workers could conceivably earn after a thorough search of the labor market, and the common definition, we shall call the former "underpayment" in this paper.

employment information (to reduce the information collection time) and/or increased unemployment benefits (to reduce the marginal search costs to the worker and make the job seeker more selective in final employment choice).

Hofler and Murphy (1992) [hereafter H&M (1992)] apply the stochastic frontier technique originated by Aigner, Lovell and Schmidt (1977) to the measurement of underpayment in the United States. H&M (1992) use the 1983 Current Population Survey data to address the first of the two questions posed above. Their results suggest the average U.S. worker achieves just over 90% of the potential (highest possible) wage. This equates to approximately 10% underpayment.

The primary purpose of this paper is to extend the research of H&M (1992) to the second question above regarding the comparative performance of the U. S. in the international labor market. A secondary purpose is to compare the performance of the U.S. at different times.

## SEARCH THEORY AND UNDERPAYMENT

### THEORY

We assume that employment seekers use a sequential stopping method in their search process.<sup>3</sup> This approach presumes that each job seeker understands the lower order parameters of the wage distribution but does not possess job-specific information. To obtain the missing information the person searches for a job. Each job offer received during the search process must be accepted or rejected at the time of offer and the decision cannot be deferred or reconsidered at a latter date (the worker cannot "recall" an offer). The worker's problem is to decide when to stop the sampling process by accepting

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<sup>3</sup> This section paraphrases section II. of Hofler and Murphy, 1992.

an offer. The degree to which the wage of the accepted job is different from the wage of the job which perfectly matches the skills of the worker is underpayment. This represents lost economic output to the nation.

McCall (1970), Mortensen (1970) and Lippman and McCall (1976) propose that under these conditions the optimal tactic for the job seeker is to adopt a reservation wage strategy. That is, the job seeker sets a reservation wage  $w(r)$  so that the first offer equal to or greater than  $w(r)$  will be accepted at wage  $w(a)$  and all lower offers will be rejected. The worker determines the reservation wage  $w(r)$  by equating the marginal benefits and the marginal costs of incremental changes in  $w(r)$ .

The wage which an employer will pay is assumed to be a positive function of the required worker skills ( $q$ ) for proper job performance. The higher the required skills, the higher the wage that an employer will pay to a worker with those required skills. Therefore, the potential wage for any worker is based on required skills is  $w(q)$ . Since required job skills will differ by employer the potential wage  $[w(q)]$  offered by employers (and for specific jobs) will also differ.

Each worker possesses a unique set of skills ( $q_0$ ) which represents the worker's accumulated human capital and predetermines the highest possible compensation available, [i.e. the potential wage  $w(q_0)$ ]. Given the worker's human capital ( $q_0$ ) and the availability of appropriate employment paying  $w(q_0)$ , the optimization process for the worker is to match his or her skills with various jobs until the potential wage  $w(q_0)$  is found. In a perfect world with costless information this employment in the worker's most productive use could be found. However, information is not costless. Therefore, the worker will follow the reservation wage strategy until an acceptable position paying  $w(a) \geq w(r)$  is found. Underpayment for the individual worker is represented by the difference between the potential wage and actual wage for the position accepted:

$$\text{Underpayment} = w(q_0) - w(a) \geq 0 \quad (1)$$

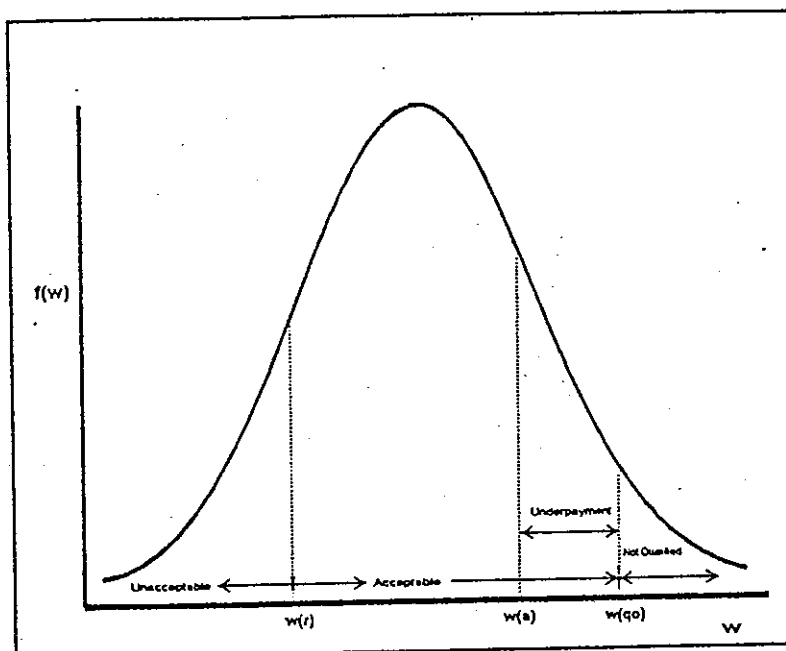


Figure 1  
Theoretical Wage Distribution for Job Seeker

From Figure 1 above, the area under the density function  $f(w)$  between  $w(r)$  and  $w(q_0)$  represents the job seeker's probability of finding acceptable employment. Above  $w(q_0)$  the worker does not possess the job skills required by the employer (i.e. is not qualified for the position) and will theoretically not receive an offer of employment in a competitive market. This probability ( $Pr$ ) of finding an acceptable job ( $J_a$ ) is:

$$Pr_{(J_a)} = \int_{w(r)}^{w(q_0)} f(w) dw \quad (2)$$

and given a reservation wage  $w(r)$ , the conditional expected job seeker's wage will be:

$$E(w | w \geq w(r)) = \frac{\int_{w(r)}^{w(q_0)} w f(w) dw}{\int_{w(r)}^{w(q_0)} f(w) dw} \quad (3)$$

From the above it is clear that, given a distribution of available jobs and wages, the expected wage will be dependent on the costly information obtained by the worker to set the reservation wage  $w(r)$ . This expected wage will fall between  $w(r) \leq E[w|w \geq w(r)] \leq w(q_0)$ . It also follows that a larger reservation wage leads to both a larger expected actual wage and a smaller degree of underpayment. {Appendix A presents the proof of this statement.} Therefore, factors that systematically determine reservation wage rates will, in turn, determine the degree of underpayment.

As noted above, the reservation wage is determined by equating, at the margin, the benefits and costs of a further increment to the reservation wage, as in Figure 2.

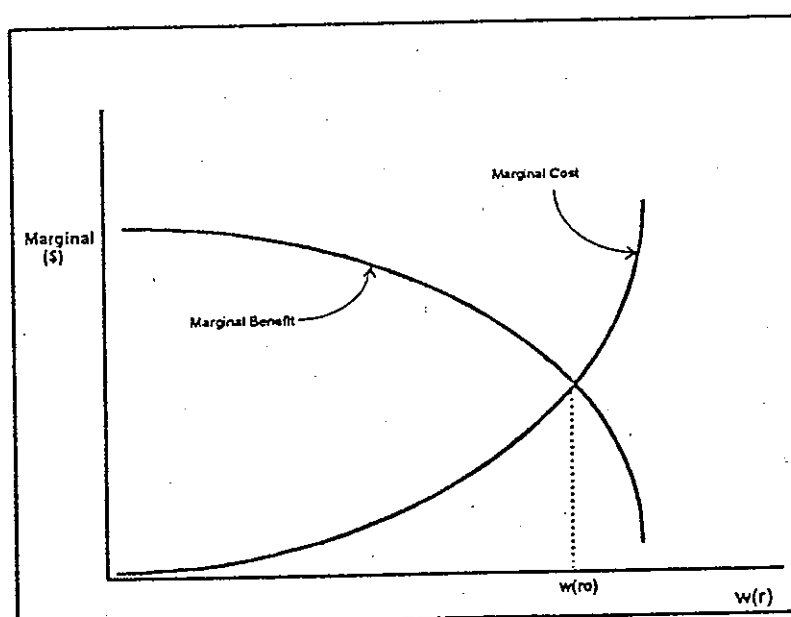


Figure 2  
Reservation Wage Determination for Job Seeker

The benefits of a further increment to the reservation wage are greater lifetime earnings once employment is secured. The height of the marginal benefit curve in the graph depends on the usual factors such as the searcher's discount rate and the amount of time the searcher expects to remain employed.



The cost of a further increment to the reservation wage consists of higher out of pocket costs and additional foregone earnings resulting from a longer duration of unemployment. The height of the marginal cost curve depends on the worker's search efficiency, the worker's skill level (which determines the opportunity cost), the worker's wealth level, and the availability and amount of social welfare payments (such as unemployment benefits) that can be collected during a spell of unemployment.

### HYPOTHESES

Workers differ in terms of the various factors that determine the marginal benefits and marginal costs of increments to the reservation wage. Because of this, the search model discussed earlier implies many testable hypotheses about differences in the degree of underpayment found across workers. In the empirical portion of this paper, we test four hypotheses.<sup>4</sup>

#### Hypothesis 1

**Demographic groups with high rates of time preference will exhibit more underpayment than groups with low rates of time preference.**

This hypothesis intimates that prime-age males will suffer less underpayment than other groups such as females and young workers. Such differences could arise because the former group is less hard pressed to work sooner than later, expects to work longer in the next job, and faces a more extensive geographic labor market.

#### Hypothesis 2

**More-educated workers will exhibit less underpayment.**

This prediction follows for several reasons, two of which follow. First, higher education reveals patience in investing in schooling, which is likely to spill over into

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<sup>4</sup> H&M (1992) test two additional hypotheses. We do not test their Hypotheses 2 and 6 because the required data were not available for this study. See their section II for elaborations on the rationales behind each hypothesis.

patience (and greater selectivity) in seeking employment. Second, direct search costs faced by the more-educated job seekers are likely to be lower than for the less-educated persons for two reasons. They are likely to be more efficient searchers and they are likely to have access to better information networks.

### Hypothesis 3

Workers in urban areas will exhibit less underpayment.

Search costs, and therefore underpayment, are lower in urban locales than in rural area for two reasons. Firms are less dispersed geographically in urban locations and urban transport networks are generally better.

### Hypothesis 4

Workers with greater wealth will exhibit less underpayment.

Wealthier seekers can consume part of their wealth while job hunting and, thus, be more selective.

This study estimates and then uses the underpayment levels for the United States (in 1986) and Canada (in 1987) to empirically test these hypotheses.<sup>5</sup>

## METHODOLOGY

### STOCHASTIC FRONTIER ESTIMATION TECHNIQUE

The stochastic frontier model was originally presented in Aigner, Lovell, and Schmidt (1977). It has been expanded by Jondrow, Lovell, Materov and Schmidt (1982)

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<sup>5</sup> The original intent of this research was to compare underpayment for the G7 nations (US, Canada, Germany, Japan, UK, France and Italy). However, Japan does not contribute to the program which is our data source and three of the countries did not report all of the required data. Germany's residuals were skewed positively, indicating "overpayment" rather than underpayment. In other studies using different data, this kind of strange result has been traced to data measurement errors. Thus, we did not analyze Germany. These factors left us with only two countries to analyze fully.

and many others (see Bauer, 1990 and Battese, 1992) for application to production maximization and cost minimization cases. Further developments of the technique for application with nonproduction and noncost applications have been made by Polachek and Hofler (1985), Hofler and Murphy (1989), and others (again, see Bauer, 1990). This study will estimate a frontier giving a potential (maximum possible) wage,  $w(q_0)$ , for each worker. Based upon this frontier, each individual's unique level of underpayment will be calculated.

Following H&M (1992), the relationship between  $y$  and  $x$  can be expressed as:

$$y_i = \alpha + \beta x_i + \varepsilon_i \quad (4)$$

Where:  $\varepsilon_i$  is  $N(0, \sigma^2)$

The above model assumes that it is the mean of  $y$  that is of interest to the researcher. However, the challenge in some economic research is to identify either the maximum possible value of  $y$  (i.e. production or income) or its minimum possible value (i.e. cost). In measuring underpayment, the goal is to calculate the maximum value that a job seeker's wage could take given that individual's accumulated human capital. We call this wage the "potential wage." The analogue to equation (4) is obtained by specifying an error term with two components: a normal component ( $\gamma_i$ ) and one-sided component constrained to be equal to or less than zero ( $\phi_i \leq 0$ ):

$$y_i = \alpha + \beta x_i + \gamma_i + \phi_i \quad (5)$$

Where:

$$\varepsilon_i = \gamma_i + \phi_i$$

$\gamma_i$  = the two-sided component where  $\gamma_i$  is  $N(0, \sigma^2)$

$\phi_i$  = the one-sided component where  $\phi_i \leq 0$  and  $E\phi_i = \mu < 0$

Equation (5) contains both a "deterministic frontier" and a "stochastic frontier." The deterministic frontier for observation  $i$  is

$$\hat{y}_{i, \text{DET}} = \alpha' + \beta x_i = (\alpha - \mu) + \beta x_i \quad (6)$$

Where:  $E\phi_i = \mu$

This represents the "average maximum"  $y$  for all observations at a specific level of  $x$ , say  $x_i$ .

The frontier in equation (5) is stochastic because, even if two observations have the same level of  $x$ , they likely will differ in the unmeasured factors captured in the two-sided error,  $\gamma$ . In such cases each observation will have its own individual frontier. This stochastic frontier,  $\hat{y}_{i,STO}$ , is the maximum value of  $y$  for one specific observation whose  $x = x_i$ . The stochastic frontier is:

$$\hat{y}_{i,STO} = \alpha' + \beta x_i + \gamma_i \quad (7)$$

Using the stochastic frontier approach permits us to estimate  $\hat{y}_{i,STO}$  for each observation. This, in turn, permits us to estimate each individual's unique level of underpayment,  $\phi_i$ .

Based on the above, a two-step process is necessary to learn the individual levels of underpayment:

- 1) The model's parameters are estimated by maximum likelihood.
- 2) These parameters are used to estimate the individual levels of underpayment from  $\phi_i$ , the one-sided error term.

The software LIMDEP will be used for this purpose.

#### MODEL SPECIFICATION

The proper estimation model must be selected. Murphy and Welch (1990) [hereafter M&W (1990)], expand on the widely accepted Mincer (1974) earnings function to develop a model expressing worker income (defined as the logarithm of wage/period) as a quartic (a quadratic in a quadratic) function of accumulated human capital. The general model developed by M&W (1990) is:

$$y_{lit} = \alpha_{it} + \beta_{1it} z_{lit} + \beta_{2it} z_{lit}^2 \quad (8)$$

Where:

$$z_{lit} = \alpha' + \beta_1' x + \beta_2' x^2 \quad (9)$$

And:

y	=	Income (Ln wage/week)
i	=	Education (Category)
x	=	Years of Experience
t	=	Time (year of observation)

After some manipulation, equation (8) becomes the following model for estimation [see M&W (1990), Equation (18), page 221]:

$$y_{it} = \alpha + \beta_1 x + (\beta_2 + \beta_1 \Gamma) x^2 + 2\Gamma \beta_2 x^3 + \Gamma^2 \beta_2 x^4 \quad (10)$$

Where  $\Gamma = 1/60$  in M&W (1990).

M&W (1990) present empirical evidence on 1964-87 data which suggests that this restricted quartic function would perform better than commonly-used earnings functions. Equation (10) will be the deterministic part of the estimation model. In other words, equation (10) will be the  $\alpha + \beta x$  part of equation (5) for estimating underpayment  $\phi_i$  and for subsequent testing and analysis.

#### ESTIMATION AND TESTING PROCEDURE

As stated above, the model must first be estimated by maximum likelihood. According to Aigner, Lovell and Schmidt, the distribution of  $\varepsilon$  can be parameterized as:

$$f(\varepsilon) = (2/\sigma) f(\varepsilon/\sigma) [1 - F(\varepsilon/\sigma)] \quad (11)$$

Where:

$$\sigma^2 = \sigma_\phi^2 + \sigma_\gamma^2,$$

$$\Gamma = \sigma_\phi / \sigma_\gamma$$

and  $f$  and  $F$  are, respectively, the standard normal density and distribution functions.

The log-likelihood function is

$$\ln L = \text{Constant} + N \ln \sigma^{-1} + \sum_{i=1}^N \ln [1 - F(\varepsilon_i \Gamma \sigma^{-1})] - \left( \frac{1}{2} \right) \sigma^2 \sum_{i=1}^N \varepsilon_i^2 \quad (12)$$

From (12) estimates for all coefficients,  $\Gamma$ , and  $\sigma^2$  are obtainable. The parameters  $\Gamma$  and  $\sigma^2$  can be solved for  $\sigma_\phi^2$  and  $\sigma_\gamma^2$ , which are useful in the next step discussed below.

This study's approach is to estimate the model once for each country and then compute person-specific  $\phi_i$  estimates. The  $\phi_i$  error component plays a crucial role in this analysis.  $\phi_i$  will equal zero and underpayment will be zero, if the worker finds the perfect job-skills match; the actual wage will equal the potential wage for that worker.  $\phi_i$  will be negative and underpayment will exist, if the worker finds an imperfect job-skills match; the actual wage will fall short of the potential wage for that worker. The work of Jondrow, Lovell, Materov and Schmidt (1982) provides a technique for obtaining individual worker estimates of  $\phi_i$ . Equation (13) below presents the conditional estimate of  $\phi_i$  given  $\varepsilon_i$ :

$$E(\phi_i | \varepsilon_i) = \frac{\sigma_\phi \sigma_\gamma}{\sigma} \left[ \frac{f\left(\frac{\varepsilon_i \lambda}{\sigma}\right)}{1 - F\left(\frac{\varepsilon_i \lambda}{\sigma}\right)} - \frac{\varepsilon_i \lambda}{\sigma} \right] \quad (13)$$

Where:

$$\sigma^2 = \sigma_\phi^2 + \sigma_\gamma^2$$

$$\lambda = \frac{\sigma_\phi}{\sigma_\gamma}$$

and  $f$  and  $F$  are, respectively, the standard normal density and distribution functions.

With an estimate of  $\phi_i$  in hand, the estimate for each individual's unique potential wage,  $w(qo)_i$  is simply the individual's actual wage,  $w(a)_i$  plus the individual's underpayment estimate,  $\phi_i$ . From this point, testing various hypotheses for differing worker characteristics becomes straightforward.

Given the above potential wage, the actual wage divided by the potential wage for each individual can be calculated. This variable will be termed **RATIO**. **RATIO** measures each person's success in attaining his or her potential wage. Therefore, it should take

values between 0% - 100%.<sup>6</sup> Mean values of RATIO can be calculated in total and for various subsets of workers so that Hypotheses 1 - 4 may be tested.

Standard pairwise t-tests (when only two subsets of data within a group are compared) and ANOVA F-tests (when more than two subsets of data are compared) will be used to test for significant differences ( $H_0$ : Mean RATIOS are equal) among sample subsets within the countries.<sup>7</sup> When there are more than two subsets of data (categories) within a group (i.e. age and education each have more than two categories) an additional Waller-Duncan K-Ratio t-test for subset pairs and a Tukey Studentized t-test will be performed to identify significant differences between pairs of categories within the group. A level of significance of 5% will be employed in all tests for statistical significance.

## THE DATA

The Luxembourg Income Study (hereafter LIS), originated in 1983 and based in Walferdange, Luxembourg represents the best data found. The LIS is a Division of CEPS/INSTEAD and represents an ongoing, cooperative consortium of researchers in the social sciences from eleven member nations.<sup>8</sup>

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<sup>6</sup> This should be true under normal economic conditions over time in competitive markets; but it may be possible for RATIO to temporarily exceed 100% for a limited period of time in imperfect markets or under severe labor shortages.

<sup>7</sup> Neither the normality nor equal variance assumptions usually made with the use of t-tests hold in cases of one-sided error estimation. The t-test may nevertheless be applied for large samples since such samples allow considering the sampling distribution of the difference of each pair of means to be normal.

<sup>8</sup> The major functions of LIS are to: (1) develop and maintain a database containing data from economic household surveys for the project's member countries, (2) provide remote data access services to the database, and (3) promote research on the economic status of populations in different countries. The member nations in LIS and the most recent reference database years are: Australia - 1986, Norway - 1986, Canada - 1987, Sweden - 1981, Germany - 1984, Switzerland - 1982, Israel - 1987, United Kingdom - 1979, Luxembourg - 1985, United States - 1986, Netherlands - 1987. In addition to the member

The original intent of this research was to apply the stochastic frontier approach and compare underpayment among the G7 nations (US, Canada, Germany, Japan, UK, France and Italy). Japan does not participate in the LIS and not all countries report all the data needed for the analysis. Consequently, survey data for only the U.S., Canada and Germany were collected and analyzed for this study. The residuals from Germany's estimated model were skewed positively, suggesting "overpayment" instead of underpayment. In other studies using different data, this kind of strange result was traced to data measurement errors. Thus, we did not analyze Germany. These factors left us with only two countries to analyze fully.

The specific data variables and definitions requested from LIS are presented in Data Addendum A: Luxembourg Income Study (LIS) Variables. From the LIS data, random samples for the U.S. (sample size = 2000 observations), Canada (sample size = 2000 observations) and Germany (sample size = 1997 observations) were obtained for use in this paper. The total random samples for each nation were further reduced because of missing data.

The above data were converted to a consistent currency (US\$) using the average annual exchange rate from the International Financial Statistics Yearbook published by the International Monetary Fund for the year of the reported data. The data were further adjusted to minimize any inconsistencies among reporting categories (i.e. education, occupations) and new analysis variables were created from the LIS data for use in this research. These new analysis variables are presented and defined in Data Addendum B: Analysis Variables.

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nations above, the LIS database also contains information from the following countries: Italy (1986), Poland (1986), Czechoslovakia (1988), Ireland (1987), and Hungary (1988).



## PRESENTATION OF RESULTS

### OVERALL

The estimated models for both the United States in 1986 and Canada in 1987 are presented in Results Table 1. The overall quality of these models is suggested by two measures: a chi-square statistic and a pseudo- $R^2$ . The chi-square statistic, which tests whether there is an overall relationship between the dependent variable and the set of independent variables, shows that there is such a significant relationship in each model. The pseudo- $R^2$  reveals a value of 0.178381 for the United States model in 1986 and a value of 0.203988 for the Canada model in 1987.

These two estimated models are similar to many earnings functions found in the literature. Like most earnings functions, these models confirm that age, education, and experience influence earnings. We cannot extract the magnitude of those influences because of the "quadratic within a quadratic" nature of these variables. See equations (8)-(10). Some of the earnings adjustment variables play their expected roles. For instance, being female significantly lowers earnings per hour in both countries and earnings differences across occupations do exist in Canada. Greater wealth (as proxied by home ownership: the variable OWN) increases earnings as expected in the United States. The incidental parameter  $\lambda$  is significantly greater than zero in both countries, foreshadowing the underpayment results which are discussed below.

The results for the United States (1986) and Canada (1987) are presented and also are compared to the H&M (1992) results based on 1983 data for the United States. In this discussion, the term underpayment refers to  $(1 - \text{RATIO})$  where RATIO is the actual wage divided by the potential wage. That is, the underpayment results show the percentage shortfall of actual wages below potential wages. Results Tables 2-6 show findings for RATIO only. Underpayment can be calculated as described above.

Table 2A below presents selected information from Results Table 2 in the Summary of Results section. The results from the H&M (1992) paper for the U.S. in 1983 are also presented for comparison.

Table 2A  
National Comparisons  
United States in 1983 & 1986 (US83 & US86) and Canada in 1987 (CN87)

Variable	US86	CN87	US83 (H&M)
RATIO	83.685%	83.143%	90.43%
Underpayment	16.315%	16.857%	9.57%
Wage/hour	\$11.69	US \$10.39	\$9.09
UNDWAGE	\$1.5759	US\$1.6811	\$0.96
Worker Age	40.15	38.78	38.26
Worker Education (years)	13.16	11.04	14.23

The results show very similar labor market characteristics for the United States and Canada, with some changes in the United States from 1983 to 1986. The highest level of underpayment is in Canada - although the U.S. in 1986 is very close. The highest actual wages are in the United States in 1986.

### HYPOTHESIS TESTS

The specific results of the hypotheses' tests are presented in Results Tables 2-6 in the Summary of Results section. In the following sections the results of the significance testing for each hypothesis for both nations and for H&M (1992) for the U.S. in 1983 are summarized.

#### HYPOTHESIS 1:

##### Underpayment Differs by Demographic Category

Gender, marital status, and age are all related to significant differences in underpayment in the United States (1986) and Canada. In both the United States (1986) and Canada lower underpayment was experienced by workers who were males, married,

and in the category prime-age married males. In both the United States (1986) and Canada the lowest underpayment was in the prime-age married males category. These results support the findings of H&M (1992) for the United States in 1983.

The specific results for each nation sampled are:

**United States (1986):**

- 1) Male underpayment (15.08%) is less than female underpayment (21.25%).
- 2) Married workers have less underpayment than single workers: 14.48% vs. 19.24%.
- 3) Underpayment varies across age categories: prime age workers have the lowest underpayment: 14.50%; young workers have the highest underpayment: 24.17%; old workers have underpayment between those others: 18.88%. Middle-aged workers (45-55) have underpayment of 16.01% that is also different from young and old workers but is not different from prime age workers.

Both the Waller-Duncan and Tukey tests reveal that prime-age and middle-age workers differ statistically from both the young and old workers' groups in their underpayment.

- 4) Prime-age married males have less underpayment than young males: 13.15% vs. 22.11%.
- 5) Prime-age married males (13.15%) are less underpaid than females (21.25%).

**Canada (1987):**

- 1) Males (15.94%) are less underpaid than female workers (21.08%).
- 2) Single workers suffer greater underpayment than married workers: 19.75% vs. 15.41%.
- 3) Underpayment differs over age categories. Middle-aged workers have the lowest underpayment: 15.48%; young workers have the highest underpayment: 24.57%; and old (19.52%) and prime age (15.81%) workers have underpayment between those others.

The formal tests show that the strongest differences from other groups occur in the young workers. They are significantly different from all three other groups. Furthermore, the prime-age workers suffer similarly to middle-aged workers.

- 4) Prime-age married males suffer less underpayment than young males: 15.18% vs. 23.33%.
- 5) Females (21.09%) experience greater underpayment than prime-age married males (15.18%).

#### United States (1983):

- 1) Prime age married males (7.93%) endure less underpayment than young workers (12.45%).
- 2) Prime age married males (7.93%) experience less underpayment than female workers (11.08%).

#### **HYPOTHESIS 2:**

##### **Workers With More Education Will Have Less Underpayment**

For the United States (1986) and Canada, educational differences were associated with underpayment differences. This result supports H&M (1992) for the United States in 1983. The results for each country for the sample years are:

#### United States (1986):

- 1) Underpayment decreases progressively with higher education: 0-8 years: 22.24%; 9-11 years: 19.21%; 12 years: 17.25%; 13-15 years: 15.85%; 15+ years: 13.35%.

The Waller-Duncan and Tukey tests reinforce each other in revealing patterns in the levels of underpayment by education. The highest educational level has lower underpayment than any other group. The middle groups (9-11, 12, 13-15) endure similar underpayment.

#### Canada (1987):

- 1) As in the U.S., underpayment, in general, decreases progressively with higher education: 0-8 years: 19.31%; 9-11 years: 17.15%; 12 years: 13.78%; 13-15 years: 16.94%; 15+ years: 12.95%.

The formal tests show that the three middle educational groups suffer roughly equal underpayment. Only the extreme groups (0-8 and 15+) exhibit significantly different levels. The most-educated workers endure the lowest underpayment whereas the least-educated workers suffer the most.

#### United States (1983):

- 1) Workers with college education (9.29%) do better than high school graduates (10.85%).
- 2) High school graduates (10.85%) suffer less than those who never enter high school (12.78%).

#### **HYPOTHESIS 3:**

##### **Workers in Urban Areas Are Less Underpaid**

For the United States (1986) the location (urban vs. rural) of the worker, when measured by population (MSA vs. non-MSA) or land use (farm vs. nonfarm), is not significantly connected to underpayment. For Canada the location of the worker is not significant when based on population but is significant when measured by land use (nonfarm workers have less underpayment). These results are weaker than the findings of H&M (1992) for the United States in 1983. The specific results for each country sampled are:

#### United States (1986):

- 1) Significant differences in underpayment by location are not found. This is true for both population (MSA vs. non-MSA) and land use (farm vs. nonfarm) distinctions.

#### Canada (1987):

- 1) Urban-rural differences in underpayment, when measured by population, are not significant.
- 2) Urban-rural differences in underpayment, when measured by land use, are significant. Non-farm workers experience less underpayment: 15.92% vs. 20.33%.

United States (1983):

- 1) Workers in urban areas (whether measured by population or land use) endure less underpayment than rural workers: population - 9.10% vs. 10.58%; land use - 9.49% vs. 12.84%.

**HYPOTHESIS 4:**

**Workers with Greater Wealth Will Have Less Underpayment**

Wealth is proxied by home ownership under the assumption that homeowners have greater wealth than nonhomeowners. In both countries for the sample periods, home ownership was significantly correlated with lower underpayment. This result supports the findings of H&M (1992). The specific sample results for each nation are:

United States (1986):

- 1) Homeowners have less underpayment than nonhomeowners: 14.67% vs. 19.00%.

Canada (1987):

- 1) Homeowners have less underpayment: 15.62% vs. 19.18%.

United States (1983):

- 1) Homeowners have less underpayment: 9.05% vs. 10.84%.

## CONCLUSIONS

The general conclusion from the data is that the United States and Canada have similar underpayment performance and determinants for the sample years. Furthermore, the findings are consistent and logical and confirm the research performed by Hofler and Murphy (1992) on 1983 data for the United States.

Viewing national underpayment as a measure of a country's lost GDP, the 16.315% underpayment for the United States for 1986 represents a potential gain of \$826.9 Billion,

if effective policies could be carried out to eliminate the underpayment.<sup>9</sup> In Canada, the 16.857% underpayment represents a gross potential gain of \$81.5 Billion.<sup>10</sup>

Comparing the 1986 United States results with the findings of H&M (1992) suggests that between 1983 and 1986 the underpayment performance of the United States worsened from 9.57% to 16.31%.<sup>11</sup> This suggests that efficiency in processing job market information in the United States dropped during this period and resulted in lower GDP growth than might have been achieved. No attempt has been made in this paper to identify the reasons for the estimated decline in United States national performance or to identify policies that might lead to absolute domestic improvement or relative international improvement.

Possibilities for further research are many. First, the reasons for the decline in the underpayment performance of the United States could be investigated. Second, as more recent information becomes available from LIS, other nations could be added and trends in performance among countries could be studied. Finally, the stochastic frontier technique could be used in new domestic and international applications.

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<sup>9</sup> Note that we are not saying that eliminating underpayment completely is possible. We are simply pointing out the extent of the shortfall in each instance and implying where the biggest gains from reducing it might be found.

<sup>10</sup> GDP data was obtained from International Financial Statistics Yearbook published by the International Monetary Fund.

<sup>11</sup> Some of the difference could be due to using different models. However, the robustness of the hypothesis test conclusions about which factors matter, even across different models, is encouraging.

## EXHIBITS

### APPENDIX A

Hofler and Murphy ('91) Proof:  $(E\langle w | w \geq w_{(r)} \rangle > w_{(r)})$

Prove: The higher the individual reservation wage ( $w_{(r)}$ ) selected the higher the conditional expected job seeker's wage ( $E[w | w \geq w_{(r)}]$ ) and the lower the level of underemployment ( $\mu$ ). Since the potential wage ( $w_{(q0)}$ ) is fixed based on the value of the job seekers accumulated human capital, the higher the individual's expected wage, the lower the level of underemployment [ $\mu = w_{(q0)} - w_{(a)}$ ]. The challenge is to prove that:

Prove:

$$E\langle w | w \geq w_{(r)} \rangle > w_{(r)}$$

and

$$\frac{\partial E\langle w | w \geq w_{(r)} \rangle}{\partial w_{(r)}} > 0$$

Given:

$$E\langle w | w \geq w_{(r)} \rangle = \frac{\int_{w_{(r)}}^{w_{(q0)}} w f(w) dw}{\int_{w_{(r)}}^{w_{(q0)}} f(w) dw}$$



Then:

$$\frac{\partial E\langle w | w \geq w_{(r)} \rangle}{\partial w_{(r)}} = \frac{\partial}{\partial w_{(r)}} \left( \frac{\int_{w_{(r)}}^{w_{(qo)}} w f(w) dw}{\int_{w_{(r)}}^{w_{(qo)}} f(w) dw} \right)$$

$$\frac{\partial E\langle w | w \geq w_{(r)} \rangle}{\partial w_{(r)}} = \frac{f(w_{(r)}) \left[ \int_{w_{(r)}}^{w_{(qo)}} w f(w) dw \right] - \left[ w_{(r)} f(w_{(r)}) \right] \left[ \int_{w_{(r)}}^{w_{(qo)}} f(w) dw \right]}{\left[ \int_{w_{(r)}}^{w_{(qo)}} f(w) dw \right]^2} > 0$$

$$\frac{\partial E\langle w | w \geq w_{(r)} \rangle}{\partial w_{(r)}} = \frac{f(w_{(r)}) \left[ \int_{w_{(r)}}^{w_{(qo)}} w f(w) dw - w_{(r)} \int_{w_{(r)}}^{w_{(qo)}} f(w) dw \right]}{\left[ \int_{w_{(r)}}^{w_{(qo)}} f(w) dw \right]^2} > 0$$

Because:

$$E\langle w | w \geq w_{(r)} \rangle = \frac{\int_{w_{(r)}}^{w_{(qo)}} w f(w) dw}{\int_{w_{(r)}}^{w_{(qo)}} f(w) dw}$$

Therefore: {Proof}

$$E\langle w | w \geq w_{(r)} \rangle > w_{(r)}$$

## DATA ADDENDUM

### A. LUXEMBOURG INCOME STUDY (LIS) VARIABLES

Identified and defined below are the variables obtained from the Luxembourg Income Study (LIS) for the United States ('86), Canada ('87) and Germany ('84):

LIS Variable Name	Definition
D1	Age: Head of Family
D3	Sex: Head of Family
D4	Number of Persons in Family
D5	Family Structure (Single/Multiple/Economic/Tax/etc.)
D7	Geographic Location Indicator A (Farm/NonFarm)
D10	Education Level: Head of Family
D12	Occupational Training: Head of Family
D14	Occupational Classification: Head of Family
D16	Industry Classification: Head of Family
D18	Type of Worker Group: Head of Family (Agric/NonAgric/Govt/etc.)
D20	Geographic Location Indicator B (Urban/Rural)
D21	Marital Status: Head of Family
D22	Tenure (Owned or Rented Housing)
D27	Children under age 18
COUNTRY	Country
HWEIGHT	Family Unit Sample Weight
GI	Total Gross Annual Income: Family
SOCI	Social Insurance Income: Family
LFSHD	Labor Force Status: Head of Family
HRSHD	Hours worked per week: Head of Family
SOCRHD	Social Retirement Income: Head of Family
UNEMPHD	Unemployment Income: Head of Family
PRVPENHD	Private Pension Income: Head of Family
PUBPENHD	Public Pension Income: Head of Family
WEEKHDFT	Full-time weeks worked per year: Head of Family
WEEKHDPT	Part-time weeks worked per year: Head of Family
WEEKHDUP	Unemployed weeks per year: Head of Family
V39	Gross Annual Wage/Salary: Head of Family

## B. ANALYSIS VARIABLES

The variables below were created from the LIS data for input and generated as output from the LIMDEP stochastic frontier technique for use in the empirical analysis of international underemployment:

Model Variable	Variable Name	Variable Definition
<b>Input Variables:</b>		
Y	LNWAGEHR	Ln of Wage per hour (Dependent Variable)
X1	AGEQT	Murphy-Welch Age Variable ( $\text{Gamma} = 0.0166667 = 1/60$ )
X2	AGEQTSQ	Murphy-Welch Age Variable Squared
X3	EDQT	Murphy-Welch Education Variable ( $\text{Gamma} = 0.0166667 = 1/60$ )
X4	EDQTSQ	Murphy-Welch Education Variable Squared
X5	EXPQT	Murphy-Welch Experience Variable ( $\text{Gamma} = 0.0166667 = 1/60$ )
X6	EXPQTSQ	Murphy-Welch Experience Variable Squared
X7	NRKIDS	Number of Children under age 18 in Family
X8	FAMINC	Other Family Income (Not Head of Family)
X9	MSA	Dummy Variable (Population > or < 100,000)
X10	LANDUSE	Dummy Variable (Farm/NonFarm)
X11	MARSTAT	Dummy Variable (Married/NonMarried)
X12	SEX	Dummy Variable (Male/Female)
X13	OCCMP	Dummy Variable (Occupation: Mgmt/Professional)
X14	OCCSTCH	Dummy Variable (Occupation: Sales/Tech/Serv/Admin)
X15	OCCCRFT	Dummy Variable (Occupation: Crafts/Skills)
X16	OCCOPER	Dummy Variable (Occupation: Operator/ Assembler/Test)
X17	OCCUNSK	Dummy Variable (Occupation Unskilled)
X18	INDMIN	Dummy Variable (Industry: Mining)
X19	INDCON	Dummy Variable (Industry: Construction)
X20	INDDUR	Dummy Variable (Industry: Durable Goods)
X21	INDNON	Dummy Variable (Industry: NonDurable Goods)
X22	INDTPU	Dummy Variable (Industry: Transport/Comm/Utilities)
X23	INDTRD	Dummy Variable (Industry: Wholesale & Retail Trade)
X24	INDFIRE	Dummy Variable (Industry: Fin/Ins/RE)
X25	INDSERV	Dummy Variable (Industry: Service)
X26	OWN	Dummy Variable (Homeowner)
<b>Output Variables:</b>		
	RATIO	Ratio of Actual Wage to Potential Wage
	WAGEHR	Wage per Hour (Currency)
	UNDWAGE	Measure of Underemployment (Currency)
	UTMNF	Natural Log of Measure of Underemployment

# SUMMARY OF RESULTS

Results Table 1  
Frontier Regression Results: Dependent Variable is Ln Wage/Hr  
United States in 1986 (US86) & Canada in 1987 (CN87)  
(Observations: US86 = 1122; CN87 = 1087)

Variable	US86 Coefficient	t-statistic	CN87 Coefficient	t-statistic
<i>Constant</i>	0.45735	1.123	1.3272	7.856
<i>AGEQT</i>	0.94311E-01	2.703	0.98533E-01	3.345
<i>AGEQTSQ</i>	-0.24446E-03	-3.695	-0.17961E-03	-3.185
<i>EDQT</i>	-0.26150E-01	-0.385	-0.16838	-3.256
<i>EDQTSQ</i>	-0.067790E-02	-0.639	0.28351E-02	3.804
<i>EXPQT</i>	-0.96906E-01	-2.114	-0.11801	-3.120
<i>EXPQTSQ</i>	0.32383E-03	2.285	0.33210E-03	2.790
<i>NRKIDS</i>	-0.11298E01	-0.494	-0.32059E-01	-1.501
<i>FAMINC</i>	0.11540E-05	1.881	-0.22811E-05	-1.394
<i>MSA</i>	0.21375	4.116	-0.18385E-01	-0.400
<i>LANDUSE</i>	-0.20424	-1.163	-0.10751	-2.096
<i>MARSTAT</i>	0.56633E-01	1.008	0.14031	2.080
<i>SEX</i>	-0.18623	-3.140	-0.13723	-2.174
<i>OCCMP</i>	0.22304	1.745	0.88046	9.679
<i>OCCSTCH</i>	-0.11487E-01	-0.091	0.74498	8.780
<i>OCCCRFT</i>	0.79607E-01	0.639	0.71700	7.352
<i>OCCOPER</i>	-0.49412E-01	-0.349	0.77336	8.197
<i>OCCUNSK</i>	-0.93720E-01	-0.698	N/A	N/A
<i>INDMIN</i>	0.38015	1.026	0.31162	3.187
<i>INDCON</i>	0.20195	1.836	0.37173E-05	0.000
<i>INDDUR</i>	0.14466	1.331	0.42743E-01	0.449
<i>INDNON</i>	0.13427	1.137	0.51555E-01	0.490
<i>INDDTPU</i>	0.11073	0.937	0.13972	1.570
<i>INDTRD</i>	-0.23752E-01	-0.229	-0.77021E-01	-1.080
<i>INDFIRE</i>	-0.35816E-01	-0.304	-0.49676E-01	-0.445
<i>INDSERV</i>	-0.18414	-1.898	-0.10803	-1.501
<i>OWN</i>	0.16347	3.232	0.79221E-01	1.584
<i>LAMBDA (<math>\lambda</math>)</i>	1.8334	14.326	2.6491	14.034
<i>SIGMA (<math>\sigma</math>)</i>	0.87193	53.859	0.93278	55.661

RESULTS TABLE 1 (CONTINUED)

Measure	US86	CN87
<i>Log-Likelihood (Unrestricted)</i>	-0.1039649E+04 <sup>a</sup>	-0.9819075E+03 <sup>a</sup>
<i>Log-Likelihood (Restricted)</i>	-0.1265367E+04 <sup>a</sup>	-0.1233533E+04 <sup>a</sup>
<i>Pseudo-R<sup>2</sup></i>	0.178381 <sup>b</sup>	0.203988 <sup>b</sup>
<i>Chi-Square Statistic</i>	451.436 <sup>c</sup>	503.251 <sup>c</sup>
<i>Number of Observations</i>	1122	1087

- a) The Log-Likelihood (unrestricted), denoted by  $\ln L_{UR}$ , is the value of the logarithm of the likelihood function at the optimum (maximum). The Log-Likelihood (restricted), denoted by  $\ln L_R$ , is the value of the logarithm of the likelihood function when all slope coefficients equal zero.
- b) This is calculated as  $1 - (\ln L_{UR} / \ln L_R)$ . It is interpreted roughly the same as the usual coefficient of determination.
- c) This is calculated as  $2(\ln L_{UR} - \ln L_R)$ . It tests the null hypothesis that all slope coefficients equal zero. It also implicitly tests a second null that the Pseudo- $R^2$  equals zero. Both null hypotheses are rejected in both the US86 and CN87 models.

RESULTS TABLE 1A  
UNITED STATES IN 1986

Variable	Mean	Std. Dev.	Min	Max
<i>LOG-LIKELIHOOD</i>	-1039.6490			
<i>RATIO</i>	.83685	.14133	.4145E-03	.9956
<i>WAGEHR</i>	11.687	11.296	.3077E-01	240.4
<i>UNDWAGE</i>	1.5759	2.5821	1.061	74.20
<i>LNWAGEHR</i>	2.2049	.74773	-3.481	5.482
<i>UTMNF</i>	.34793	.29476	.5953E-01	4.307

RESULTS TABLE 1B  
CANADA IN 1987

Variable	Mean	Std. Dev.	Min	Max
<i>LOG-LIKELIHOOD</i>	-981.9075			
<i>RATIO</i>	.83143	.16363	.2142E-03	.9838
<i>WAGEHR</i>	10.386	6.3444	.2357E-01	63.98
<i>UNDWAGE</i>	1.6811	4.0790	1.036	110.0
<i>LNWAGEHR</i>	2.1324	.75301	-3.748	4.159
<i>UTMNF</i>	.32274	.38751	.3525E-01	4.700

Results Table 2:  
Overall

Item	US '86	CANADA '87 (US\$)
Number of Observations	1122	1087
Analysis Variable		
RATIO	83.685%	83.143%
WAGEHR	\$11.687	US\$10.386
UNDWAGE	\$1.5759	US\$1.6811
LNWAGEHR	2.2049	2.1324
UTMNF(ln undwage)	0.34793	0.32274
Indiv. Gross Wage	\$23,419	US\$20,806
Other Family Income	\$11,244	US\$10,535
Total Income	\$34,663	US\$31,341
Exchange Rate		1.326
Age	40.153	38.777
Average Education	13.157	11.044
H.S. (Attended)	11.77%	29.81%
H.S. (Graduate)	36.28%	1.66%
College (Attended)	20.41%	25.58%
College (Graduate)	27.72%	17.39%
Other Educ.	3.83%	25.58%
All Education %	100.00%	100.00%

Results Table 3  
Hypothesis 1: Demographic Group

Country	Variable = RATIO			
	Male	Female	T-Statistic (≠)	Prob> T  (≠)
US86	.8492	.7875	5.5960	.0001
CN87	.8406	.7891	3.5503	.0005

Country	Variable = RATIO			
	Single	Married	T-Statistic (≠)	Prob> T  (≠)
US86	.8076	.8552	-5.4888	.0001
CN87	.8025	.8459	-3.9163	.0001

Country	Variable = RATIO					Prob> F  (≠)
	Age < 25	Age 25-44	Age 45-55	Age > 55	F-Statistic (≠)	
US86	.7583	.8550	.8400	.8112	16.4261	.0001
CN87	.7554	.8424	.8455	.8041	9.46	.0001

Country	Variable = RATIO			
	Prime Age Married Males (Age 25-44)	Young Males (Age < 25)	T-Statistic (≠)	Prob> T  (≠)
US86	.8685	.7789	-5.0232	.0001
CN87	.8482	.7667	-2.8160	.0068

Country	Variable = RATIO			
	Prime Age Married Males (Age 25-44)	Females (All Ages)	T-Statistic (≠)	Prob> T  (≠)
US86	.8685	.7875	-7.0235	.0001
CN87	.8482	.7891	-3.8679	.0001

Results Table 4  
Hypothesis 2: Level of Education

Country	Variable = RATIO					F-Statistic ( $\neq$ )	Prob> F  ( $\neq$ )
	0-8 Years	9-11 Years	12 Years	13-15 Years	15 + Years		
US86	.7747	.8080	.8275	.8415	.8664	7.5462	.0001
CN87	.8069	.8285	.8622	.8307	.8705	4.4988	.0013

Results Table 5  
Hypothesis 3: Urban vs. Rural Location

Country	Variable = RATIO		T-Statistic ( $\neq$ )	Prob> T  ( $\neq$ )
	Non-MSA	MSA		
US86	.8238	.8416	-1.8645	.0628
CN87	.8246	.8407	-1.6457	.1001

Country	Variable = RATIO		T-Statistic ( $\neq$ )	Prob> T  ( $\neq$ )
	Non-Farm	Farm		
US86	.8376	.7806	1.2649	.2249
CN87	.8409	.7967	3.0476	.0025

Results Table 6  
Hypothesis 4: Wealth

Country	Variable = RATIO		T-Statistic ( $\neq$ )	Prob> T  ( $\neq$ )
	Non-Homeowner	Homeowner		
US86	.8100	.8533	-5.1093	.0001
CN87	.8082	.8438	-3.4481	.0006



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## DATA ADDENDUM (SUPPLEMENT)

## A1. REQUIRED VARIABLES (LIS) "NOT REPORTED" BY COUNTRY

Listed below by nation and year of most recent report are the desired LIS variables for the underemployment research using "Stochastic Frontiers." Those desired variables which were not reported are indicated "NR." Note that Japan does not participate in the program.

LIS Variable Name	US('86)	CN('87)	GE('84)	FR('81)	IT('86)	UK('79)
V39				NR	NR	
D1				NR		
D3						
D4						
D5						
D7				NR	NR	NR
D10				NR		NR
D12	NR	NR		NR	NR	NR
D14				NR	NR	
D16				NR		
D18				NR		NR
D20						
D21					NR	
D22						
D27						
COUNTRY						
HWEIGHT						
GI				NR	NR	
SOCI						
LFSHD					NR	
HRSHD						
SOCRHD				NR		NR
UNEMPHD				NR	NR	NR
PRVPENHD				NR	NR	NR
PUBPENHD				NR		NR
WEEKHDFT					NR	NR
WEEKHDPT					NR	NR
WEEKHDUP					NR	NR