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# Working Paper Short Run Fluctuations in Fertility and Mortality in Preindustrial Sweden

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#### ECONOMIC GROWTH CENTER

#### YALE UNIVERSITY

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#### CENTER DISCUSSION PAPER NO. 410

#### SHORT RUN FLUCTUATIONS IN FERTILITY AND MORTALITY

#### IN PREINDUSTRIAL SWEDEN

Zví Eckstein

T. Paul Schultz

Kenneth I. Wolpin

#### June 1982

Notes: A preliminary draft was presented at a Conference on British Demographic History, Asilomar, California, March 7-9, 1982. We have benefited from comments on the earlier draft from participants at the conference and Jonathan Eaton, Wallace Huffman, Christopher Sims and David Weir. We acknowledge the able research assistance of Thomas Frenkel and Paul McGuire and the financial support of a grant from the Hewlett Foundation to Yale's Economic Demography Program.

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## Short Run Fluctuations in Fertility and Mortality

in Preindustrial Sweden

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Yale University

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#### 1. Introduction

There are basically three phenomena that economic demographers seek to understand. First, what governs the long swings in fertility in industrially advanced countries, such as the United States, after they have completed their demographic transition. Second, what initiates and explains the pace of the demographic transition, during which the level and short-run variability of birth and death rates decreases. Only the third phenomena will be studied in this paper: how have societies before they entered into the demographic transition achieved a balance between resources and population. Malthus most notably addressed this third topic. He characterized the factors underlying the preindustrial economic demographic equilibrium in terms of wages, death rates and birth rates, and the diminishing marginal productivity of labor in traditional agriculture.

One can attempt to translate the insights of Malthus into expectations as to the sign of correlations in coincident series or into a structural equation econometric model and estimate parameters from historical time series (Thomas, 1941 Lee, 1973). The theoretical basis for imposing a particular structure on such data **is**, however, **in our view limited**. Consequently, it would be preferable to summarize historical data and then use this unrestricted summary representation of the data to explore the questions Malthus considered, and even to interpret the data as tentatively testing certain of Malthus' technical and behavioral hypotheses regarding the short run effects of the real wage on birth and death rates.

Vector autoregression is a statistical methodology for summarizing data that has been recently employed to study macroceoonomic time series and to make projections. It has special appeal in those areas in which macroeconomic dynamic theory is unable to identify statistically the

underlying structural system (Sargent, 1979; Sims, 1980). If this statistical methodology is applied to historical aggregate time series on weather, crops, wages, deaths and births, the resulting economicdemographic equation system is in one way more tractable than modern macroeconomic systems. We have strong a priori knowledge that weather is determined outside the system, or isstrictly exogenous, and this information reduces the number of parameters to be estimated. But we also have little theoretical basis for ordering the other variables and treating any one endogenous variable as predetermined with respect to another. Researchers have, nonetheless, regressed one endogenous variable on several others and interpreted the distributed lagged estimates as a technical or behavioral causal relationship (Lee, 1981). These single equation structural formulations implicitly posit many assumptions and restrictions that do not appear justified at this stage in our research. Thus, we have opted for the less restrictive vector autoregression framework, even though it requires the estimation of maly parameters. These more restricted studies are nested within our more general representation.

Sweden is our case study. The annual demographic data for Sweden are good after 1750, and a variety of time series are available to characterize weather conditions, crops, commodity prices and wages.

The paper is ordered as follows. Section 2 discusses the data and Section 3 the statistical model. The empirical results are reported in Section 4 and interpreted in Section 5. A concluding section summarizes our findings. Three appendices provide more detail on data sources, the econometric methodology and the statistical specification

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tests.

#### 2. Data

The registered figures of births and deaths for all of the counties of modern Sweden, as well as the annual number of Swedish inhabitants, are widely regarded as a reliable basis for calculating Swedish birth and death rates after 1749. The historical statistics series (Sweden, 1955, Table B.2) are supplemented by those reported by the United Nations after 1950 (United Nations, 1979). For several reasons we examine here the crude birth rate (CBR), or the number of births occurring in the calendar year per thousand inhabitants at the end of that year. Our measure of fertility is not adjusted for changes in the age composition of the population, since our primary goal is to characterize short run fluctuations in birth rates rather than slow changes in their levels related to the changing age composition. Before Swedish emigration increases in the 1860's, the short run effects of migration on the age composition are also negligible at the national level, even though they may be more important at the level of county or other subnational unit (Thomas, 1941). Changes in fertility are not decomposed into changes in (1) the proportion of women married in the childbearing ages, (2) marital fertility rates, and (3) extra-marital fertility rates. have noted the short run responsiveness of all Thomas and others three components of the Swedish fertility are strongly correlated with each other and with the harvest cycle, particularly in the 18th and early 19th centuries (Thomas, 1941, p. 87 and Table 25). It is not our current objective to consider how fertility changes were accomplished among these three routes.

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Since the level of mortality is substantially higher in the first year of life than in subsequent years, fluctuations in births will tend to affect deaths, in the same direction, in the current and following year. This demographic linkage from births to deaths, by way of the age schedule of mortality, suggests the need to disaggregate deaths of infants from those occurring to persons over the age of one. The causes of mortality among infants and older persons may also be substantially different, since many infants are breastfed and, thereby, derive immunities to certain diseases. Consequently, mortality experienced by infants and older persons may respond differently to conditioning variables. Deaths to members of these two populations may also elicit different patterns of fertility response.

Infant deaths are registered in the year of their occurrence; these infants, under one year of age, may have been born in either the current or previous year. We analyze, therefore, an adjusted infant death rate (IDR) that divides the number of infant deaths in a particular year by a weighted average of the number of births in the current and previous year, where the weights depend simply on the level of the unadjusted infant mortality rate (Shryock, 1971, p. 441).

Other (non-infant) deaths are divided by the current year non-infant population (NIDR). There may still be a slight tendency for the NIDR to increase one to four years after the birth rate increases, since mortality among one to four year olds is greater than at subsequent ages, at least in the early years of our study. But the severity of this problem is discounted by historical demographers (e.g., Lee, 1977), and we do not adjust the series to account for this second-order demographic feedback.

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The general crop index (CROP) reported in the <u>Historical Statistics of</u> <u>Sweden</u> (1959, Table E.12) starts in 1786, but is available from 1748 in Sundbärg's (1907, Table C) original monograph on the Swedish population. The real wage (RWAGE) is the nominal wage in agriculture divided by the price of basic foodgrains or a cost of living index. Crop variation presumably affects real wages, but also influences payments to land and other factors of production in agriculture. Over time, moreover, improvements in the transportation system and storage facilities for grains should have weakened the coincident and lagged relationship between the crop index and the price of foodgrains. Therefore, both the traditional crop index and a new measure of real wages are employed in our exploration of Swedish time series.

Although the composition of basic foodstuffs produced and consumed in Sweden changed in this period, rye was the predominate food grain in Sweden until 1860 (Thomas, 1981). Moreover, the prices of alternative major grains--barley, oats and later wheat--are highly correlated annually at .95 to .99 from 1750 to 1913 (Jörberg,1972). Our measure of the real agricultural wage from 1750 to 1870 is, thus, constructed from Jörberg's (1972) series on the daily male agricultural worker's wage divided by the price of a

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The Sundbärg Index is divided by two to be consistent with the later historical statistics series, in which 3.0 is an average crop year. There does not appear to be a general crop index after 1955, and, therefore, projections are based on an agricultural output index for Sweden from the United Nations Statistical Office.

hectolitre of rye. Since this agricultural wage series is discontinuous after 1913, Jungenfelt's (1966) estimate of annual earnings of workers in agriculture is divided by Phelps-Brown's (1968) cost of living index to define the real agricultural wage (RWAGE) for the entire later period, 1870 to 1955<sup>2</sup>.

Five series are selected to summarize weather. The average annual rainfall is from the average of three Swedish meteorological stations in Lund, Stockholm, and Uppsala (Sweden, 1959, Table C.7).<sup>3</sup> The average annual temperature was also used initially, though it is available only for Stockholm (Sweden, 1959, Table C.2). This is undoubtedly a blunt measure of climate; moderately cold winters were sometimes beneficial for grains, but they increased mortality, while hot summers may have increased mortality, while nonetheless improving the harvest (Le Roy Laduire, 1971). Preliminary exclusion (F) tests led us to replace a single annual or July temperature with the average temperature for each of the four seasons of the year. The winter temperature refers to the average of January, February and March, and so on. The temperature series are published from 1756 and they determine the beginning of our time series analysis.

<sup>2</sup> Where the two real agricultural wage series overlap, 1870-1913, their logarithms are correlated at .94, though the annual earning series is relatively less volatile than the daily wage, i.e., the standard deviation of the logarithms are .18 and .27, respectively.

<sup>3</sup> One annual observation is missing for Lund (1906), 25 are missing from 1761 to 1835 for Uppsala and reports for Stockholm start in 1784. Rather than rely only on Lund or omit the first 29 years of our series, multiple regressions are fit to the existing overlapping data for 1750 to 1955 and used to predict values for the missing observations on rainfall. Using only the Lund series does not change in any noted way the results that are later reported.

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The sources and definitions of all the data series are reported in Appendix A. The final data used in our study are plotted in Figures la through lk and are summarized in Table 1 in absolute form and in natural logarithms in Table 2: they illustrate the transition in Sweden from the preindustrial era of high and unstable death and birth rates to the industrial period of low mortality and low fertility, with the pronounced swing of the postwar baby boom following the depression. The fraction of Sweden's population in urban areas is virtually constant at 10 or 11 percent until 1860, while the fraction of the labor force employed outside of agriculture is roughly twice that amount but growing slowly until the late 19th century (Mosher, 1980). Legislation enacted in the middle of the 18th century sought to modernize Swedish agriculture according to the English example, but the redistribution and consolidation of land holdings associated with the abolition of the common field system and enclosures met with resistance and proceeded slowly. Only by the middle of the 19th century had the process run its course. During this time of increasing rural population density, the proportion of the agricultural labor force without land increased substantially. Migration of workers out of agriculture facilitated after 1850 the expansion of rural industrial centers and urban employment. Later in the 1860s workers leaving agriculture began to leave Sweden, emigrating mostly to North America. These large scale emigrations continued for half a century until internal rural-urban flows of population were more or less again in balance.

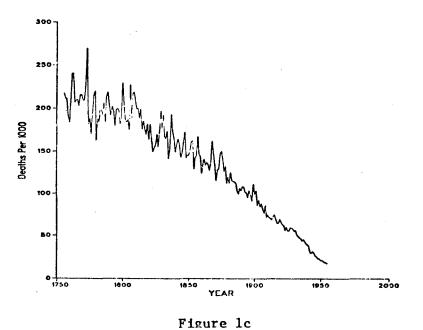
-7-

Figure 1 Basic Data Series

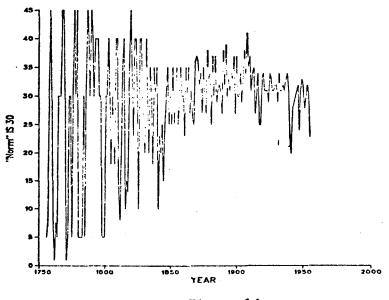
Swedish Non Infant Death Rate...NIDR Swedish Crude Birth Rate...CBR 80 40-45 -35 40 35 30 Deaths Per 1000 Births Por 1000 30-23 20 20 18 -10 \$ 1750 10 1750 1800 1850 1900 1900 1950 2000 1800 1850 YEAR YEAR

Figure la

Swedish Modified Infant Death Rate. IDR



Swedish General Crop Index...





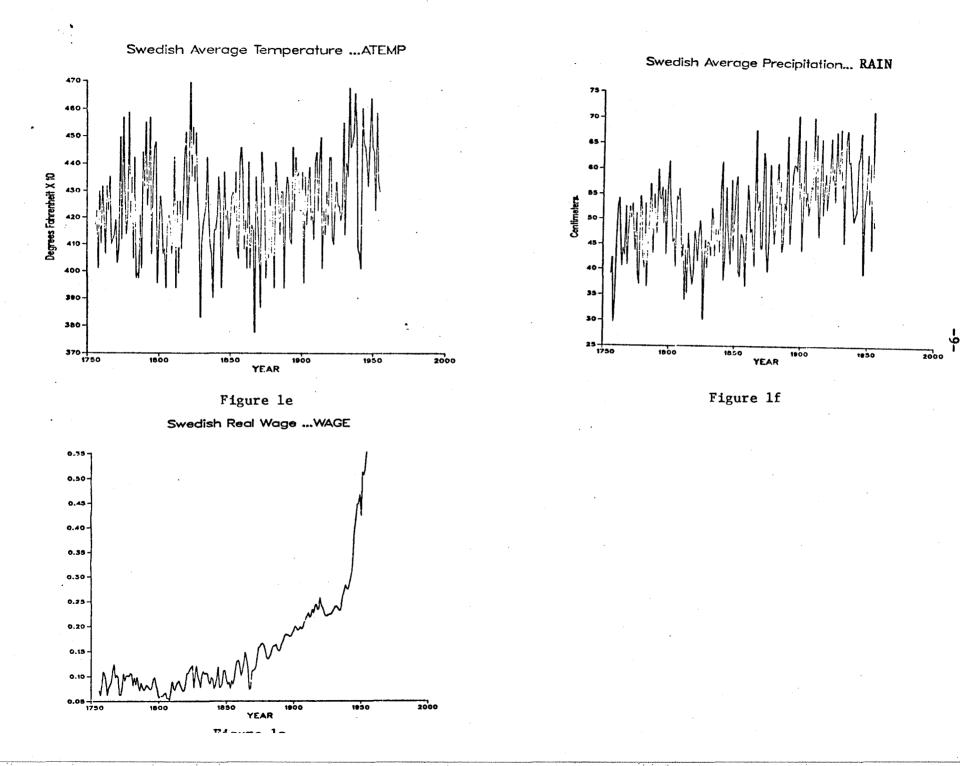
1950 2000





Figure 1 continued

Basic Data Series



#### continued Figure 1 Basic Data Series

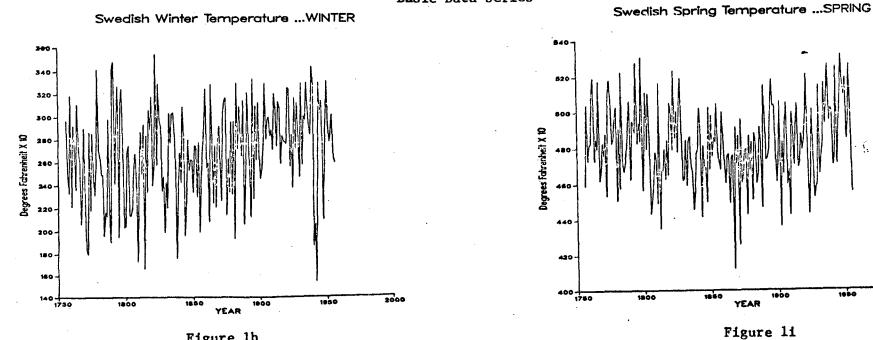
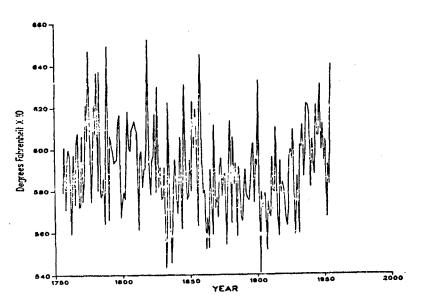


Figure lh

Swedish Summer Temperature ... SUMMER



Swedish Autumn Temperature ...AUTUMN

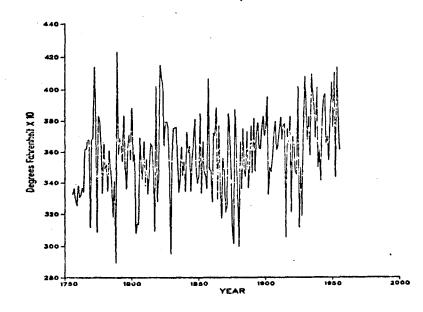


Figure lk

Figure 11

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2000

١.

1980

Simple Correlations among Contemporaneous Variables in Absolute Form and Sample Statistics: 1756-1869 and 1870-1955

|                       |                         | Variable Names          |                          |                                       |                           |                            |                            |                            |  |                   |  |  |  |  |
|-----------------------|-------------------------|-------------------------|--------------------------|---------------------------------------|---------------------------|----------------------------|----------------------------|----------------------------|--|-------------------|--|--|--|--|
| Variable<br>Symbols   | Crude<br>Birth<br>Rate  | Infant<br>Death<br>Rate | Non-In-<br>fant<br>Death | General<br>Crop<br>Index              | Real<br>Agricul-<br>tural | Spring<br>Tempera-<br>ture | Summer<br>Tempera-<br>ture | Autumn<br>Tempera-<br>ture | Winter<br>Tempera <del>-</del><br>ture | Precipi<br>tation |  |  |  |  |
|                       | (1)                     | (2)                     | Rate (3)                 | (4)                                   | Wage<br>(5)               | (6)                        | (7)                        | (8)                        | (9)                                    | (10)              |  |  |  |  |
|                       |                         |                         |                          | · · · · · · · · · · · · · · · · · · · | Period                    | 1: 1756-186                | 9                          |                            |  |                   |  |  |  |  |
| CBR(1)                | -                       | 016                     | 361                      | 037                                   | .359                      | .196                       | .075                       | 075                        | .286                                   | 171               |  |  |  |  |
| IDR(2)                | .909                    | • 🛥                     | •750                     | 180                                   | 536                       | .133                       | .165                       | 004                        | 147                                    | .003              |  |  |  |  |
| NIDR(3)               | ·N .819                 | .908                    | -                        | 093                                   | 415                       | 021                        | .186                       | .108                       | 205                                    | 020               |  |  |  |  |
| CROP(4)               | •819<br>•309            | .312                    | .225                     | -                                     | .363                      | .043                       | 064                        | 045                        | .117                                   | .039              |  |  |  |  |
| RWAGE(5)              | <b>0</b><br><b></b> 693 | 842                     | 781                      | 315                                   | -                         | 025                        | 145                        | .062                       | .223                                   | 088               |  |  |  |  |
| SPTEMP (6)            | <sup>∞</sup> 296        | 345                     | 353                      | .010                                  | •363                      | -                          | .401                       | .112                       | .244                                   | .022              |  |  |  |  |
| SMTEMP(7)             | ~327                    | 331                     | 348                      | 158                                   | .366                      | .413                       | -                          | .142                       | .095                                   | 164               |  |  |  |  |
| AUTEMP (8)            | 350                     | 402                     | 417                      | 120                                   | .330                      | .298                       | .152                       | -                          | .091                                   | .051              |  |  |  |  |
| WNTEMP(9)             | J108                    | 097                     | 138                      | .400                                  | .068                      | .322                       | .156                       | .158                       | -                                      | 087               |  |  |  |  |
| RAIN(1)               | 272                     | 256                     | 285                      | .199                                  | .091                      | 059                        | 159                        | .282                       | .396                                   | -                 |  |  |  |  |
|                       | ·                       |                         |                          |                                       | Period                    | 1: 1756-1                  | 369                        |                            |  |                   |  |  |  |  |
| Mean                  | 32.5                    | 181.0                   | 19.7                     | 26.5                                  | .090                      | 48.1                       | 59.2                       | 35.4                       | 25.9                                   | 472.8             |  |  |  |  |
| Standard<br>Deviation | 2.10                    | 28.8                    | 4.36                     | 12.2                                  | .019                      | 2.12                       | 2.25                       | 2.51                       | 4.18                                   | 70.2              |  |  |  |  |
|                       |                         |                         |                          |                                       | Period                    | 2: 1870-19                 | 55                         |                            |  |                   |  |  |  |  |
| Mean                  | 22.7                    | 75.7                    | 12.5                     | 31.6                                  | .234                      | 48.4                       | 58.7                       | 36.4                       | 28.1                                   | 559.3             |  |  |  |  |
| Standard<br>Deviation | 5.77                    | 35.6                    | 1.89                     | 3.82                                  | •097                      | 2.29                       | 18.5                       | 2.59                       | 3.86                                   | 75.1              |  |  |  |  |

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| Ventable               |                        |                         |                                  |                          | Variable Na                       | mes                        |                            | *                          |                            |                   |
|------------------------|------------------------|-------------------------|----------------------------------|--------------------------|-----------------------------------|----------------------------|----------------------------|----------------------------|----------------------------|-------------------|
| Variable<br>Symbols    | Crude<br>Birth<br>Rate | Infant<br>Death<br>Rate | Non-In-<br>fant<br>Death<br>Rate | General<br>Crop<br>Index | Real<br>Agricul-<br>tural<br>Wage | Spring<br>Tempera-<br>ture | Summer<br>Tempera-<br>ture | Autumn<br>Tempera-<br>ture | Winter<br>Tempera-<br>ture | Precip:<br>tation |
|                        | (1)                    | (2)                     | (3)                              | (4)                      | (5)                               | (6)                        | (7)                        | (8)                        | (9)                        | (10)              |
|                        | <u></u>                |                         |                                  |                          | Period 1:                         | 1756-1869                  | <u> </u>                   |                            |                            |                   |
| CBR(1)                 | -                      | 163                     | 328                              | 077                      | .360                              | .189                       | .066                       | 092                        | .289                       | 176               |
| IDR(2)                 | .832                   | -                       | .788                             | 279                      | 540                               | .134                       | .181                       | 012                        | 158                        | 020               |
| NIDR(3) 6<br>CROP(4) 0 | .812                   | .920                    | -                                | 184                      | 465                               | .015                       | .190                       | .067                       | 243                        | 050               |
| CROP(4)                | .300                   | .333                    | .230                             | -                        | . 384                             | 030                        | 012                        | 030                        | .112                       | .019              |
| RWAGE(5)               | 755                    | 956                     | 850                              | 322                      | -                                 | 092                        | 138                        | .062                       | .231                       | 099               |
| SPTEMP(6)              | 283                    | .362                    | 351                              | .024                     | . 379                             | -                          | .400                       | .112                       | .236                       | 022               |
| SMTEMP(7)              |                        | 385                     | 357                              | 157                      | . 359                             | .420                       | -                          | .135                       | .085                       | 162               |
| AUTEMP(8)              | 337                    | 379                     | 411                              | 105                      | .363                              | .291                       | .141                       | -                          | .084                       | .059              |
| wntemp(9)              | <b>/</b> ]             | 046                     | 100                              | .427                     | .089                              | . 304                      | .140                       | .140                       |                            | 085               |
| RAIN(10)               | 259                    | 173                     | 264                              | . 213                    | .144                              | .048                       | 167                        | .295                       | .379                       | -                 |
|                        |                        |                         |                                  |                          | Period 1:                         | <u>1756–1869</u>           |                            |                            |                            |                   |
| Mean                   | -3.42                  | -1.72                   | -8,56                            | 3.08                     | -2.43                             | 6.18                       | 6.38                       | 5.86                       | 5.55                       | 6.15              |
| Standard<br>Deviation  | .0657                  | .161                    | .188                             | . 776                    | .215                              | .0443                      | .0380                      | .071                       | .166                       | .152              |
|                        |                        |                         |                                  |                          | Period 2:                         | <u> 1870–1955</u>          |                            |                            |                            |                   |
| Mean                   | -3.82                  | -2.72                   | -8.99                            | 3,45                     | -1.52                             | 6.18                       | 6.38                       | 5.90                       | 5.63                       | 6.32              |
| Standard<br>Deviation  | .270                   | .572                    | .153                             | .126                     | . 357                             | .0474                      | .0331                      | .0729                      | .150                       | .138              |

4

# Simple Correlations Among Contemporaneous Variables in Logarithmic Form and Sample Statistics: 1756-1869 and 1980-1955

Non-infant mortality may have been decreasing slowly in the late 18th and early 19th centuries, but the extreme variability in deaths makes it difficult to extract the secular trend with much confidence. Smallpox was brought under control after 1809, and serious outbreaks of dysentary subsided after 1818. Many other epidemic diseases, however, showed no tendency to diminish until well into the 19th century, e.g., measles, whooping cough, typhus and typhoid (Utterström, 1954). After 1880, the only resurgence in the decreasing level of non-infant deaths occurred during the world influenza pandemic of 1918-1920.

Infant mortality rates were decreasing throughout our period, though the rate of decline may have accelerated over time; this pattern in Sweden is similar to that observed in France (Blayo, 1975), but may be contrasted with stability in infant deaths rates in England throughout the 19th century where urbanization proceeded more rapidly than in Sweden (Wrigley and Schofield, 1981). The volatility of the Swedish series is much reduced after 1880, as epidemics receded. While the birth rate and non-infant death rate decreased about 50 percent in our, period of 200 years, the infant death rate decreased 90 percent, from one-in-five to one-in-fifty.

The general crop index shows a tendency to vary less after 1850 than before that date. This may be a result of applying scientific knowledge to agriculture, progress in plant breeding, rotational schemes and increased use of fertilizers, or due to a change in the composition of output that reduced its sensitivity to the weather, or an artifact of how the series was

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constructed, such as shifting from price to quantity series.<sup>4</sup> The real wage in agriculture declined in the last half of the 18th century, particularly after 1775. Deflating the wage by more comprehensive cost of living indexes reduces the deterioration, but does not change the direction of trends or turning points (Jorbärg, 1972, II p. 186). Real agricultural wages increased during and after the Napoleonic wars, 1806 to 1823, regaining their trend upward only after 1854 and continuing until 1913. Overall, the level of real wages in agriculture approximately doubled from 1800 to 1875, and tripled in the next 75 years to 1950.

Rainfall and annual average temperature are highly variable in both subperiods, as is to be expected of the weather. There are, nonetheless, clues of longer run swings. Temperatures tended downward in the 1800s, up in the 1820s, down through the 1860s, and upward thereafter for nearly a century. Rainfall diminished from the 1790s to the 1830s, and increased thereafter to a higher level in the first half of this century.

<sup>&</sup>quot;Official crop yield reports were not available before 1865 (Thomas, 1941), and thus Sundbärg's general crop index must have relied heavily in this earlier period on annual grain price series (Utterstrom, 1954). In this case, it may be particularly interesting in this early period to include the wage series to disentangle changes in the price level of crops from changes in real wages (wage/grain prices). This general crop series has been widely used since Sundbärg (1907) incorporated it into his classic analysis of population developments in Sweden. Utterstrom (1954) doubts whether this series was derived entirely from representative data on harvest yields for he surmises that, at least in the 18th century, only grain price series were available. This he notes may have confounded in the series both variation in real grain prices and also changes in the general price level that had little to do with the abundance of the harvest. If the demand schedule for foodgrains was inelastic with respect to price, reliance on price rather than quantity data might have imparted a bias toward greater variance in the index in earlier years.

#### 3. An Econometric Framework: Vector Autoregression

The methodology we adopt in this paper originated in the work of Sims (1980), and has been applied mainly in the analyses of macroeconomic time series. Sims argued against structural macro-econometric modeling because the identifying restrictions of existing models are "incredible", because the dynamic elements of the models are not well specified, because there is only a weak distinction between endogenous and exogenous variables, and because of the incomplete treatment of expectations. Instead, he proposed estimating unrestricted vector autoregressions (VAR) which can be interpreted as the reduced form relationships that arise from macro-econometric structural models. Sims also developed methods for describing or summarizing the content of the vector autoregression from which hypotheses could be formulated.

Another focus of research on interpreting economic time-series, exemplified in the work of Sargent (1981), argues that in a well formulated equilibrium framework based on optimizing agents who form expectations in a manner consistent with the equilibrium model, restrictions on the parameters across the equations of the VAR will be implied. The underlying structural parameters in this context are those related to preference functions and technological constraints. Structural econometric models are not structural in this sense. Demographic and economic time series should be viewed similarly as having a microeconomic basis. We do not present such a theoretical foundation, although we hope to learn about the important ingredients of such a theory from the descriptive analysis. In this section, we discuss a simplified version of the econometric model actually estimated. The more general and rigorous discussion may be found in Appendix B.

Assume we have time-series observations for a particular country on birth rates, infant mortality rates, and a measure of weather. Further, assume that we can "best" represent the system of these three variables

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(detrended and as deviations from means) in the following manner?

(1) 
$$B_t = \alpha_1 B_{t-1} + \alpha_2 M_{t-1} + \alpha_3 W_t + \alpha_4 W_{t-1} + \varepsilon_{1t}$$

(2)  $M_t = \beta_1 B_{t-1} + \beta_2 M_{t-1} + \beta_3 W_t + \beta_4 W_{t-1} + \epsilon_{2t}$ 

(3) 
$$W_{t} = Y_{1}W_{t-1} + V_{t}$$

where  $B_t$  is the birth rate at time period t,  $M_t$  the death rate at t, and  $W_t$  is weather at t. This system is assumed to arise from a complex structural dynamic model of behavior that is conditioned by biological and technological constraints. In other words, the  $\alpha$ 's and  $\beta$ 's are interpreted as composites of more fundamental biological, technical and behavioral parameters. We will therefore refer to this representation as unrestricted, since the fundamental parameters appearing in the  $\alpha$ 's and  $\beta$ 's are not delineated and the restrictions that could be imposed in the estimation are ignored.

The innovations or random shocks, namely  $\varepsilon_{1t}$ ,  $\varepsilon_{2t}$ , and  $v_t$ , are assumed uncorrelated with the demographic variables or weather. In addition, they are assumed to be serially uncorrelated; all correlations of one error with the lagged values of itself or with the lagged values of the error in other equations ar zero. Neither of the innovations in the demographic variables is permitted to be contemporaneously correlated with the weather shock, although in principle they may be correlated with each other. The force of these

<sup>5</sup>See Appendix B for a more rigorous definition of "best."

assumptions, given that lagged demographic variables do not enter the weather equation, is to ensure that weather is strictly exogenous (see Appendix B). Having estimated this system, we can test statistically for the possible presence of lagged demographic variables in the weather equation. This is a test of causality in the sense of Granger (1969). In addition, we will perform Sims's(1972) exogeneity test which is based on examining future weather effects in the demographic equation; should we find that future weather "affects" current births and deaths, this would imply that the random shocks in the demographic variables are contemporaneously correlated with the random weather shock. Since it seems logical to assume that weather is truly strictly exogenous to the demographic outcomes, if one finds that future weather appears to affect the demographic variables this may be viewed as evidence that explanatory variables are omitted from the system. In other words, exogeneity tests in this context are tests of the completeness of the specification of the model. For example, suppose equations (1)-(3) represent the true model but  $M_{t-1}$  is omitted from equation (1). Then estimating  $B_t = \alpha_1 B_{t-1} + \alpha_3 W_t + \alpha_4 W_{t-1} + \alpha_3 W_t$  $\alpha_5 W_{t+1} + \epsilon_t$  may give rise to a significant estimate of  $\alpha_5 \neq 0$  while exogeneity require that  $\alpha_5 = 0$ . This arises since  $W_{t+1}$  is correlated with  $M_{t+1}(\beta_3)$  and  $M_{t+1}$  with  $M_t(\beta_2)$ 

This system of equations can be efficiently estimated by ordinary least squares (OLS), equation by equation; these OLS estimates are identical with joint conditional maximumlikelihood estimates, even though  $\varepsilon_{1t}$  and  $\varepsilon_{2t}$  may be correlated. The lag length adopted, such as "one" in the example, need not be arbitrary, since statistical tests for alternative lag lengths can be readily performed. However, as the number of parameters expands much more quickly than the number of lags, it is necessary to restrict the lag length.<sup>7</sup>

<sup>6</sup> Conditional maximum likelihood in the sense that it is conditioned on the initial observations, since the system includes lags. <sup>7</sup>There are several tests for the lag length. We used Sims' (1980) "modified" likelihood ratio tests (see Tables C.1 and C.2 in Appendix C).

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A useful way to describe the system, once the parameters have been estimated, is to observe the system's response to random shocks (Sims, 1980). We refer to these as impulse responses. Consider one standard deviation shock in weather  $\sigma_v$ , at time t. In period t, the birth rate will change by  $\alpha_3 \sigma_v$  and the death rate by  $\beta_3 \sigma_v$ . In period t + 1, the birth rate changes , by  $(\alpha_1 \alpha_3 + \alpha_2 \beta_3 + \alpha_3 \gamma_1 + \alpha_4) \sigma_v$  and the death rate by  $(\beta_1 \alpha_3 + \beta_2 \beta_3 + \beta_3 \gamma_1 + \beta_4) \sigma_v$ . In like manner, we can continue to trace out the impact of the t<sup>th</sup> period weather shock on births and deaths at t + 2, t + 3,... If the system is stable, the impulse responses will dampen. Similar responses can be obtained for shocks in the demographic variables.

The interpretation of these impulse responses critically depends upon the extent to which the random shocks that generate the responses are distinct. In the interpretations we choose to give for the impulse responses, we assume the contemporaneous cross equation correlation in shocks to be small as if they are distinct, i.e., we assume the variance-covariance matrix of the residuals to be diagonal. Thus, if the shock to the birth rate ( $\varepsilon_{1t}$ ) is significantly correlated with the shock to the death rate ( $\varepsilon_{2t}$ ), the impulse response to the birth rate shock will ignore the response to the coincident death rate shock.

An alternative approach to the problem of contemporaneous error correlation pursued by Sims (1980) is to apply an orthogonalization transformation of the variance-covariance matrix of the errors so as to make it the identity matrix. One set of possible transformations is to triangularize the variance-covariance matrix, which transforms the unrestricted system to a block-recursive system. For example,  $M_t$  might appear in the  $B_t$  equation but not vice-versa. Since the variance-covariance matrix of the system

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we actually estimate does not appear to be diagonal as we assumed, we report several orthogonalizations to check for robustness in the pattern of impulse response

To illustrate these ideas more concretely, let us suppose that there is a common component to the random elements in the birth and death rates such that

- (4)  $\varepsilon_{1t} = \theta_t + \delta_{1t}$
- (5)  $\varepsilon_{2t} = \beta \theta_t + \delta_{2t}$

where  $\delta_{1t}$  and  $\delta_{2t}$  are independently distributed of each other and of  $\theta_t$ . As an example,  $\theta_t$  might represent an epidemic that reduces conceptions and increases mortality, i.e.  $\beta < 0$ . The existence of this common error causes a contemporaneous correlation between the birth rate and the death rate. If one could distinguish  $\theta_t$  from  $\delta_{1t}$  and  $\delta_{2t}$ , then the impulse responses of interest would be those to innovations in the  $\delta$ 's. An innovation in  $\delta_{1t}$ , for example, would correspond to an unpredicted change in the birth rate alone. However, an innovation in  $\epsilon_{1+}$  comes from two sources and impulse responses based upon the false premise that  $\epsilon_{1t}$  and  $\epsilon_{2t}$  are uncorrelated would neither correctly characterize the response to a shock only in  $\delta_{lt}$  nor to a shock in  $\epsilon_{1t}$ , since  $\epsilon_{2t}$  would also change. However, under the assumptions given above, the no alized variances of the three independent errors and  $\beta$  could be determined from knowledge of the variance-covariance matrix of the  $\varepsilon_{1t}$ ,  $\varepsilon_{2t}$  error vector. Thus, the appropriate one standard deviation shock in  $\delta_{1t}$  and  $\delta_{2t}$  could be ascertained and impulse responses generated. The assumption we maintain, however, is that  $\sigma_{A}^{2} = 0$ , i.e., that the composite shocks in  $\varepsilon_{1t}$  and  $\varepsilon_{2t}$  are independent.

Consider an alternative assumption about the error structure, namely

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where the birth rate shock consists only of a common component, while the mortality rate shock has both a common and specific part.

(6)  $\varepsilon_{1t} = \theta_{t}$ 

(7) 
$$\varepsilon_{2t} = \beta \theta_t + \delta_{2t}$$

It is easy to verify that this error structure is equivalent to a recursive model in the birth rate and the death rate. Ignoring other regressors we may write the corresponding system as

(8) 
$$B_{+} = \theta_{+}$$

(9) 
$$M_t = \beta B_t + \delta_{2t}$$

This recursive system therefore is implied by a particular error structure for the system given by (1) - (3). Normalizing the variance-covariance matrix of the errors in (8) and (9) to be the identity matrix yields one particular orthogonalization that permits contemporaneous correlations between endogenous variables. Clearly, an alternative (more restricted) structure is placed on the errors in a recursive system. A shock in the birth rate must now be interpreted as a shock also in the death rate; it would not be surprising to find that a recursive model yielded quite different impulse responses than would a less structured model, particularly when the contemporaneous correlation is of consequence. To complement the impulse responses, we also calculate the proportion of the forecast error variance in each variable k<sup>th</sup> period in the future that is produced by a particular shock or innovation. For example, an initial shock at time t of one standard deviation in weather, births and deathseach causes the birth rate to deviate from its mean at each future period. The fraction of the total variance in the birth rate caused by this set of standardized innovations k periods ahead, for relatively large k, is called the variance decomposition of the birth rate. The variance decomposition of each dependent variable measures the degree of interaction among the variables in the system. If the variance in a dependent variable created by innovations in all of the variables of the system is explained mostly by its own innovation, it would not appear interdependent with the other system variables. This lack of interdependence Was assumed in the case of weather in the above simplified system.

Since the parameters of the unrestricted system are functions of more fundamental parameters reflecting preferences, biology, and technology, any change in these latter structural parameters will, in general, induce changes in all of the parameters of the unrestricted system. If there is reason to believe that, within the sample period, structural relationships have changed, then it would be important to estimate the system within the appropriate subperiods. Statistical tests for structural change are, therefore, conducted and are described in the next section, although they are not general in the sense of determining what subperiods should be examined for structural change.

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### 4. Estimation and Specification Tests of the Model<sup>8</sup>

The system consists of five endogenous variables: CBR, IDR, NIDR, CROP and RWAGE. The five exogenous variables are the four seasonal temperatures and annual precipitation. All of the variables are expressed in logarithms and we include an annual time trend and its square in each equation of the endogenous variables. Each of the exogenous variables is assumed to be a function of lagged values of itself, that is, they are not detrended. The lag length in the exogenous variable equations is assumed to be the same as the endogenous variable equations.

There are several reasons to think that the parameters of this system of equations may have changed during the period of 1756 to 1955. One noticeable watershed occurred in the late 19th century. First, the secular decline in fertility appeared to start about 1870, although the timing of this development may be affected somewhat by the surge in emigration that begins in the 1860s (Mosher, 1980). Second, not only are the demographic trends more noticeable after 1870, the fluctuations around these trends that we want to account for become smaller, both absolutely and relatively (see Tables 1 and 2). Third, by the last half of the 19th century, Sweden had become closely integrated into world agricultural markets, importing a growing share of its foodgrains and exporting mainly animal products. With improvements in transportation, local crops ceased to determine food prices and to affect as strongly the real wage. Finally, after about 1870 the rate of industrialization increased in Sweden, and the economicdemographic system became more responsive to conditions in the nonagricultural Indeed, the ebb and flow of the business-trade cycle became a economy.

<sup>8</sup>The estimation used the RATS computer package, version 4.01,1980, written by T.A. Doan and R. B. Litterman.

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major short run perturbation to the demographic system in the 20th century, if not earlier (Thomas, 1941; Galbraith and Thomas, 1941). Consequently, we will statistically evaluate the hypothesis that our econometric representation of the economic-demographic system is structurally different for Sweden before and after the onset of the roughly coincident demographic transition and industrialization. We chose 1870 as the year separating these two periods. The null hypothesis in the test is that there is no structural change between these two periods.

Prior to the structural change test it is necessary to establish the approriate lag length for the endogenous and exogenous variables. Appendix Table C.1 reports the (modified) likelihood ratio tests of the number of lags to include in our model.<sup>9</sup> The evidence suggests that the hypothesis of four annual lags over the entire period is supported. The structural change tests are then shown in Table 3, conditional on four lags. The results indicate that the hypothesis of no structural change is distinctly rejected for the entire system as well as for the subset of endogenous variable equations. Tests for structural change of the individual equations indicate that structural changes are most marked in the birth and infant death rate equations. We also tested whether the structurrate al change is due solely to different trends in the two periods by allowing for different trends in the restricted specification (case (b), Table 3). In this manner we test whether the deviations from trend behave differently over the two periods. The results indicate the presence of structural change in the system other than trend. The data, therefore, support the hypothesis that the structure of the economic-demographic system is <sup>9</sup>The modified likelihood ratio test is defined in Table C.2.

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|-------|---|
| Table | 3 |

|   | $\log  V_u $ | $\log  V_{R} $ | x <sup>2</sup> | d.f  | Marginal<br>Significance |
|---|--------------|----------------|----------------|------|--------------------------|
| 4   | (1)          | (2)            | (3)            | (4)  | Level<br>(5)             |
| Entire System <sup>1</sup>                    |              |                |                |      | -                        |
| a)  | -53.02       | -50.70         | 343.0          | 265  | .003x10 <sup>-1</sup>    |
| b)  | -53.02       | -50.99         | 299.6          | 22.4 | $.002 \times 10^{-1}$    |
| Sub <b>syste</b> m of<br>Endogenous Variables |              |                |                |      |                          |
| a)  | -26.70       | -24.61         | 308.7          | 240  | .001                     |
| b)  | -26.70       | -24 • 90       | 265.2          | 225  | .029                     |
| eparate Endogenous<br>Variables               |              |                |                |      |                          |
| CBR a)  | -7.40        | -6.73          | 98.60          | 48   | .002x10 <sup>-2</sup>    |
| b)  | -7.40        | -6.76          | 94.73          | 45   | $.002 \times 10^{-2}$    |
| IDR a)  | -6.00        | -5.41          | 87.18          | 48   | .005x10 <sup>-1</sup>    |
| b)  | -6.00        | -5.56          | 65.41          | 45   | .025                     |
| NIDR a)                                       | -5.18        | -4.81          | 55.31          | 48   | .22                      |
| b)  | -5.18        | -4.85          | 49.38          | 45   | .31                      |
| CROP a)                                       | -2.01        | -1.79          | 32.34          | 48   | .96                      |
| b)  | -2.01        | -1.82          | 28.76          | 45   | .97                      |
| RWAGE a)                                      | -5.25        | -4.84          | 61.88          | 48   | •09                      |
| b)  | -5.25        | -4.92          | 50.17          | 45   | .28                      |

Tests of Structural Change Between the Two Subperiods

<sup>1</sup> Row a)treats the trend and its square exactly as the other variables in the system. Row b)assumes the trend and its square to differ between the two periods as a maintained hypothesis and therefore tests for structural change of the remaining variables only.  $V_u$  and  $V_R$  are explained in Table C.1 and  $\chi^2 = T((2)-(1))$ .

dissimilar in the two periods.

As noted at the outset, the methodology and variables examined here to describe the interplay of economic and demographic processes in a preindustrial and pretransition society are probably less adequate for describing transitional and modern trends for a variety of reasons. In particular, we expect that changes in health technology, the general growth in wealth levels (i.e., human and physical capital), the more rapid growth in women's wages than men's wages, and the incentive effects of the modern tax-transfer system, have all altered the short-run and long-run responses of birth rates and death rates to current economic conditions and fluctuations in weather. Estimates of the model's parameters for the later period, 1870-1955, implied dynamic patterns that are substantially different from those of the early period. Small changes in the model's specifications implied substantial changes in the system outcomes and often unstable processes were estimated for some (or all) variables. Therefore, we restrict our analysis to the first period.

To specify the model for the earlier period, we again perform the test of lag length. Due to the smaller sample size (109 observations), and to the number of parameters, the lag length tests as modified by Sims (1980) cannot reject any lag length less than five (see Appendix Table C.2), supporting the choice of a single year lag.<sup>10</sup> Conversely, if we do not adopt Sims' conservative modification of the conventional  $\chi^2$  statistical significance test, it rejects all lags less than five. Hence, we have adopted the four lag specification accepted above for the entire sample.

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<sup>10</sup> The modified likelihood ratio test (see also Table C.1) reduces the  $\chi^2$  statistic by subtracting the number of coefficients in an unrestricted equation from the number of observations in calculating the likelihood ratio statistic.

Given the lag length, we performed the tests of exogeneity due to Sims as described in the previous section. The test of exogeneity of the weather variables should be viewed as a test for omitted variables. Following Sims (1972), four leading values of the exogenous variables were included in the endogenous variable equations. Table 4 shows that there are no important omitted variables in the demographic and the crop index equations. However, the results for the agricultural real wage equation suggest that there are omitted variables correlated with weather that are also part of the RWAGE process.<sup>11</sup> Nonetheless, a test for the entire system does not reject exogeneity of weather at the conventional 5 percent confidence level.<sup>12</sup>

Table 5 presents the estimated parameters of the endogenous variables while the estimates for the exogenous variables are in Table C.3. Many of the tests for excluding each variable (all lags) from specific equations do not support inclusion of this explanatory variable at usual confidence levels. Overall F statistics are, however, significant for the entire system, and for the NIDR and RWAGE equations separately.

The zero-order contemporaneous correlation between the exogenous and the endogenous variables residuals is due to the inclusion of current exogenous variables in the endogenous variables equations. There is a large positive correlation between the two

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<sup>&</sup>lt;sup>11</sup>For example, if the level of employment should be included in the system as an endogenous variable, weather might appear endogenous as the example in the previous section demonstrated. To repeat that argument, future weather is correlated with future employment, which is correlated with past employment and the current wages.

<sup>12</sup> Table C.5 reports results of exclusion tests (Granger (1969) causality) which indicate a general support for the "no" omitted variables hypothesis except for the results with respect to winter temperature.

| T | al | Ь. | 1 | e | 4 |
|---|----|----|---|---|---|
|   |    |    |   |   |   |

|          | C        | BR                       | I    | DR                       | N        | IDR                      | C        | ROP                      | RWAGE |                         |
|----------|----------|--------------------------|------|--------------------------|----------|--------------------------|----------|--------------------------|-------|-------------------------|
| Leads of | <u>F</u> | Marginal<br>Significance | F    | Marginal<br>Significance | <u>F</u> | Marginal<br>Significance | <u>F</u> | Marginal<br>Significance | F     | Marginal<br>Significanc |
| SPTEMP   | 1.14     | .35                      | .76  | .56                      | .21      | .93                      | 1.26     | .31                      | 2.87  | .03                     |
| SMTEMP   | 2.30     | .07                      | 1.01 | •41                      | •99      | •42                      | •76      | •56 ·                    | .47   | •75                     |
| AUTEMP   | .65      | .63                      | .29  | .88                      | .80      | • 53                     | 2.73     | •04                      | 2.55  | .05                     |
| INTEMP   | •78      | • 54                     | .35  | .84                      | 1.14     | .35                      | .97      | .44                      | 1.90  | .13                     |
| RAIN     | •94      | .45                      | •46  | .77                      | .77      | .55                      | 1.53     | .21                      | 2.99  | •03                     |
| LL       | 1.31     | .22                      | .55  | •92                      | .84      | .64                      | 1.55     | .11                      | 1.75  | .06                     |

 $\chi^2$  test for the entire subsystem:  $\chi^2$  (100) = (110-68)(-24.98-(-27.23)) = 94.5, marginal significance level = .63

#### Table 5

# The Endogenous Variables Equations: 1756-1869

| Regressor  | lag    | CBR                    | IDR                      | NIDR                | CROP                      | RWABE               |
|--|--------|------------------------|--------------------------|---------------------|---------------------------|---------------------|
|  |        |                        |                          |                     |                           |                     |
| Constant   | -      | -5.91 -4               | 8.08                     | 7.23 -2             | -36.06_2                  | 11.90_              |
| Irend,   | -      | $5 \times 10^{-4}_{5}$ | $15 \times 10^{-2}_{-4}$ | $3 \times 10^{-2}$  | $.34 \times 10^{-2}_{-4}$ | 5x104               |
| <b>fre</b> nd <sup>2</sup>   | -      | .3x10 <sup>-5</sup>    | 25x10 <sup>-4</sup>      | 13x10 <sup>-4</sup> | .27x10 <sup>-4</sup>      | .5x10 <sup>-4</sup> |
| CBR  | 1      | .163***                | .040                     | .521                | -3.855                    | -1.373**            |
|  | 2      | 055                    | 281                      | .142                | 4.892                     | 1.248               |
|  | 3      | .188                   | .382                     | .275                | <b>.3</b> 53              | 321                 |
|  | 4      | .156                   | .363                     | .262                | -2.703                    | 036                 |
| IDR  | 1      | .071                   | .078                     | 205                 | 939                       | .359                |
|  | 2      | .084                   | 141                      | 409                 | .637                      | 335                 |
|  | 3      | 083                    | 083                      | .031                | .113                      | .217                |
|  | 4      | .011                   | 172                      | 432                 | -1.31                     | 386                 |
| NIDR   | i      | 019                    | 013                      | .315                | 1.045                     | .040                |
|  | 2      | 022                    | .041                     | .152                | 756                       | .109                |
|  | 3      | .043                   | 003                      | 137                 | .339                      | 789                 |
|  | 4      | .050                   | .141                     | .191                | 1.099                     | •269                |
| CROP   | ī      | • <b>0</b> 05          | 149                      | 048                 | .360*                     | •004                |
| , include the second se | 2      | .013                   | .184                     | .014                | .229                      | .017                |
|  | 3      | 006                    | 0                        | .032                | 136                       | .021                |
|  | 4      | .005                   | .019                     | •009                | 357                       |                     |
| RWAGE  | 1      | .13**                  | 074                      | 137***              | -1.138                    | 051<br>.073*        |
| NWAGE  | 2      | •009                   | 106                      | 304                 | <b>.167</b>               | 016                 |
|  | 3      | 104                    | .155                     | .098                | 977                       | 240                 |
|  | • 4    | 008                    | 166                      |                     | •922                      |                     |
| INTEMP   |        | -•008                  | 072                      | 073                 | •922<br>1•046***          | .230<br>.328***     |
|  | 1      | .017                   |                          | 198***              |                           | -                   |
|  | 2      | •002                   | 123<br>054               | 286                 | 054<br>317                | .065                |
| ·  | 3      | 009                    |                          | 096                 |                           | .064                |
|  | 4      | 011                    | 079                      | 062                 | .550                      | .107                |
| SPTEMP   |        |                        | 006                      | .018                | 1.046                     | .066                |
| SFILMP .   | 0      | • 065**                | 131                      | 362                 | -2.574                    | 470                 |
| <i>i</i> _   |        | .431                   | 215                      | 125                 | 113                       | .723                |
|  | 2<br>3 | .102                   | .032                     | 418                 | 334                       | .051                |
|  |        | .219                   | .081                     | 791                 | 1.531                     | 091                 |
|  | 4      | 013                    | 259                      | 419                 | 1.301                     | .065                |
| SUTEMP   | 0      | .025                   | .089                     | .434                | 2.642                     | .247                |
|  | 1      | 094                    | 235                      | 046                 | 595                       | 333                 |
|  | 2      | .051                   | 280                      | 124                 | -3.175                    | .014                |
|  | 3      | .004                   | .366                     | .557                | 041                       | 185                 |
|  | 4      | .170                   | 217                      | 177                 | 2.177                     | .649                |
| UTEMP  | 0      | 15                     | .058                     | .289                | .280                      | .225***             |
| -  | 1      | 040                    | 144                      | .105                | 1.582                     | .271                |
|  | 2      | .015                   | 013                      | •066                | 2.028                     | .308                |
|  | 3      | .035                   | 032                      | •045                | 1.102                     | .413                |
|  | 4      | 073                    | 158                      | 146                 | 556                       | 226                 |
| RAIN   | 0      | 020                    | 035                      | .001                | .645                      | •008 **             |
|  | 1      | 010                    | .115                     | .021                | <del>-</del> .880         | 360                 |
|  | 2      | 001                    | 018                      | 036                 | 150                       | 056                 |
|  | 3      | 011                    | .031                     | •099                | .235                      | .082                |
|  | 4      | 051                    | .028                     | •007                | .174                      | 016                 |
| 2  |        | . 82                   | 87                       | •74                 | .60                       | .81                 |
|  |        |                        |                          |                     |                           |                     |
| ignificano<br>evel   | e      | .8710                  | .8490                    | •9699               | .7379                     |                     |

\*, \*\*, \*\*\*, indicate that the F-test for excluding this variable (all lags) is rejected at the 1%, 5%, and 10% level respectively.

## TABLE 6

Decomposition of Variance: Percentage of Forecast Error Variance 25 Years Ahead Produced by Each Innovation ( $\rho_{ij}^2$  (25))

|                 | Innovation in: (j) |      |      |      |       |        |        |        |        |      |
|-----------------|--------------------|------|------|------|-------|--------|--------|--------|--------|------|
| esponse in: (i) | CBR                | I DR | NIDF | CROP | RWAGE | WNTEMP | SPTEMP | SUTEMP | AUTEMP | RAIN |
| CBR             | 27                 | 4    | 4    | 3    | 15    | 13     | 15     | 3      | 8      | 6    |
| IDR             | 3                  | 44   | 2    | 4    | 6     | 16     | 3      | 8      | 8      | 5    |
| NIDR            | 4                  | 4    | 34   | 6    | 5     | 23     | 6      | 6      | 5      | 4    |
| CROP            | 6                  | 1    | 2    | 48   | 10    | 8      | 8      | 4      | 8      | 5    |
| RWAGE           | 5                  | 4    | 3    | 3    | 38    | 10     | 3      | 4      | 17     | 13   |

death rates, IDR and NIDR (1.e., .73), the correlation between IDR and CBR is -.31 and the correlation between NIDR and CBR is -.42. Hence, the shocks to the demographic series do not appear to be independent, as we had hoped, in order to confirm the working assumption of our approach. Furthermore, the innovation in RWAGE is positively (.4) correlated with the innovation in the crop index and negatively correlated with the death rates. In interpreting the results we, nevertheless, maintain the assumption of zero contemporaneous correlation among the variables ( $\Sigma_v$  and  $\Sigma_c$  in Appendix B are diagonal), rather than impose a temporal ordering on the endogenous variables. In addition, we have computed the results for various other orthogonalizations (see Appendix B for explanation) and report the results of those that have some plausibility and which are notably different from those implied under the assumption of a diagonal covariance matrix.

Table 6 reports the decomposition of the variance of each variable due to a one standard deviation shock in each variable. Table C.4 reports the estimated variance-covariance matrix of the innovations upon which these shocks are based. The variance decompositions emphasize the magnitude of the importance of each variable in each endogenous variable equation. Each variable accounts for less than 50 percent of its own variance. The winter temperature is especially important in accounting for the variance of the demographic variables. The real wage and spring temperature account for much of the variance in the birth rate. Interactions between the demographic variables are not significant. That does not imply, however, that the impact of a shock in one demographic variable on another is small, in any absolute sense. Alternative decompositions of the covariance matrix of endogenous variables according to alternative triangularizations of the contemporaneous covariance matrix reveal only minor differences. Appendix Table C.6 reports two alternative triangularized decompositions of the variance. The main difference is with respect to the responses of the two death rates, although the sum of the two is not greatly affected. Hence, our interpretation of the covariance between the innovations gives

rise to a decomposition of variance which is almost identical to alternative interpretations of the covariance.

#### 5. Description and Interpretations of Impulse Responses

Impulse responses are presented in figures 2a-g, 3a-c, and 4a-d. The first set shows demographic reactions to shocks in weather and economic variables, the second set shows demographic reactions to demographic shocks, and the third set shows economic reactions to weather shocks. We will discuss each set in turn after first establishing several general features of all of the responses.

The first characteristic to note is the overall stability of the system. Responses to shocks in time period 1 tend to dampen quite rapidly, with convergence to zero (i.e,to mean values) accurring within a 10 to 15 year period. The second notable feature is the relatively short cycle of the responses. There is little evidence of persistence; fluctuations around zero are sharp and frequent.

The reactions of the demographic variables to exogenous and economic (CROP,RV shocks exhibit a consistent pattern. For every individual response depicted in figure 2, the crude birth rate reacts in an opposite fashion as do both of the death rates. Thus, for example, a positive innovation in the general crop index or in the real wage increases fertility for several years and decreases the infant and non-infant death rates over the same period, as hypothesized by Malthus. Also, each seasonal temperature shock that initially reduces the death rates also increases fertility, while an increase in precipitation subsequently increases mortality and reduces fertility. In particular, warm winters have especially beneficial effects on survival. Increases in wealth, broadly defined, tend to increase fertility and reduce both infant and non-infant mortality at

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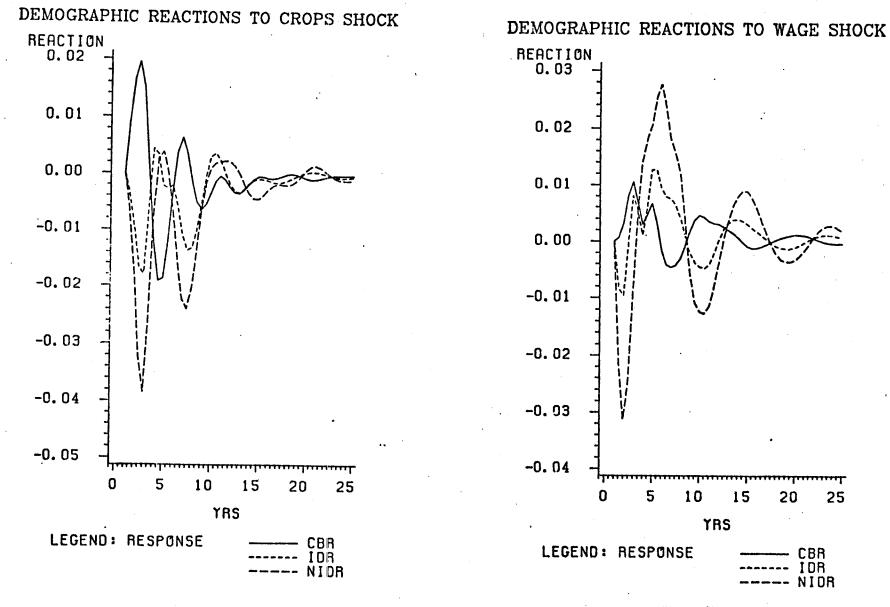
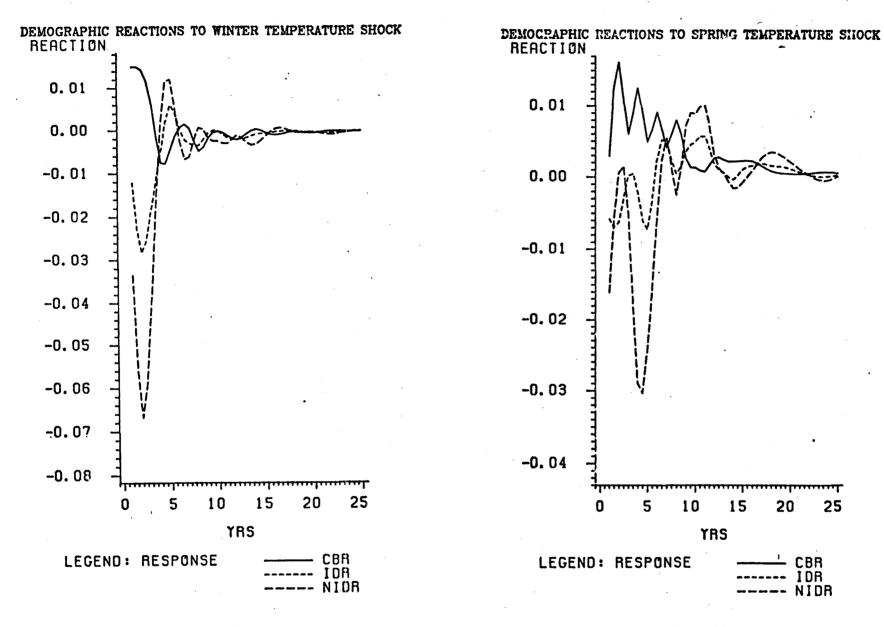




Figure 2b

-33-

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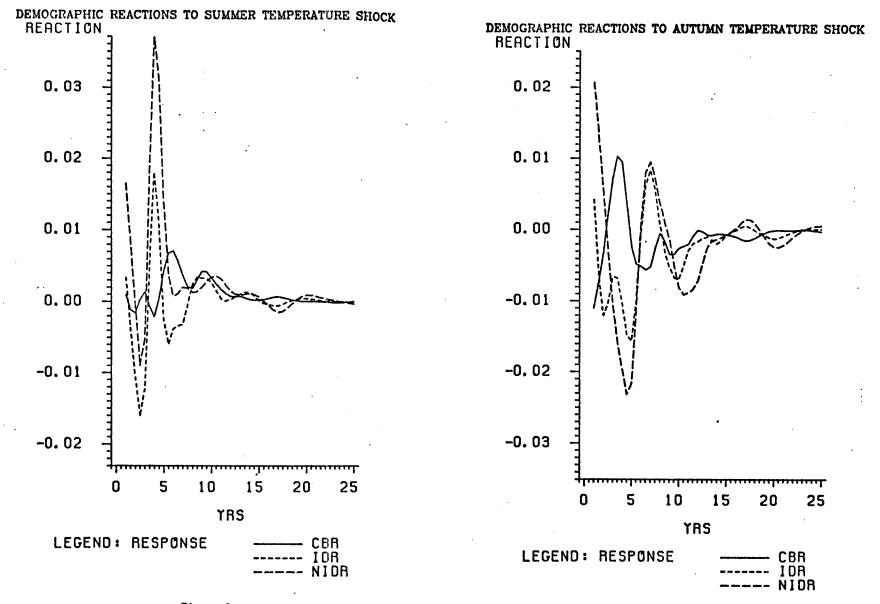




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Figure 2d

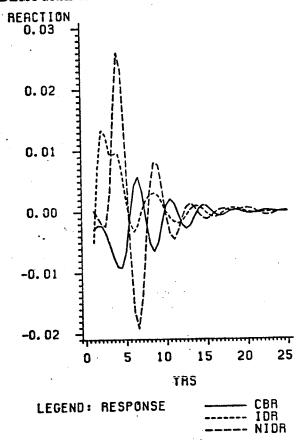
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-35-



# DEMOGRAPHIC REACTIONS TO RAIN SHOCK

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Figure 2g

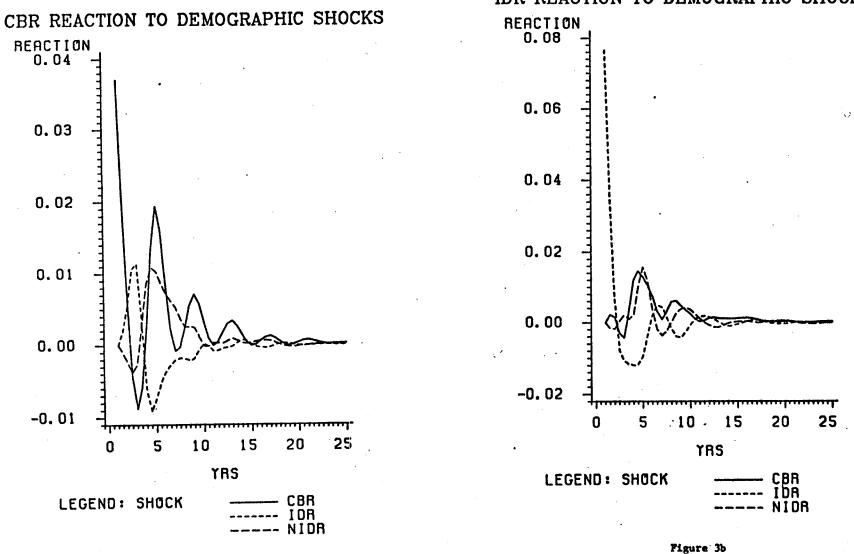
least for several years. In addition, with a few exceptions, the cumulative responses of mortality are in the same direction as the initial response, i.e., the negative response to increased wealth outweighs the positive components of the ensuing cycles. The positive components are explicable as postponement or selection effects, where increased survival of inherently weaker individuals due to, for example, favorable crop outcomes, merely delays some of the deaths that would otherwise have occurred earlier . Note, also, the larger responses in amplitude of the non-infant death rate than of the infant death rate.

The demographic responses to demographic shocks display different patterns of interaction. The birth rate reaction to its own innovation (figure 3a) reveals a three year cycle that seems to be compatible with the biological reproductive cycle, a finding that is also apparent in the previous figures and in the Bengtsson(1981) study of southern Sweden. The birth rate response to mortality rates appears consistent

with a replacement strategy. An increase in the infant death rate is followed by an increase in the birth rate with the peak increase occurring in two years. The cumulative response, however, appears negligible, implying a change in the timing of children rather than in completed fertility. An increase in the non-infant death rate first reduces fertility as would be anticipated if the proportion of child bearing population in marital unions is thereby reduced. But it is then followed by a rise in fertility peaking after approximately five years. This latter response is consistent with the delayed "replacement" that would occur as new households were formed in response to the loss of spouse or parent.

Both the infant and non-infant death rates (figures 3b, 3c) respond

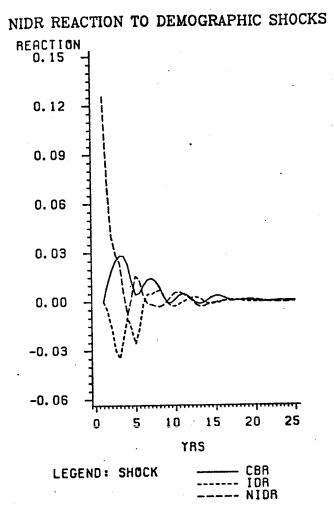
-37-



IDR REACTION TO DEMOGRAPHIC SHOCKS



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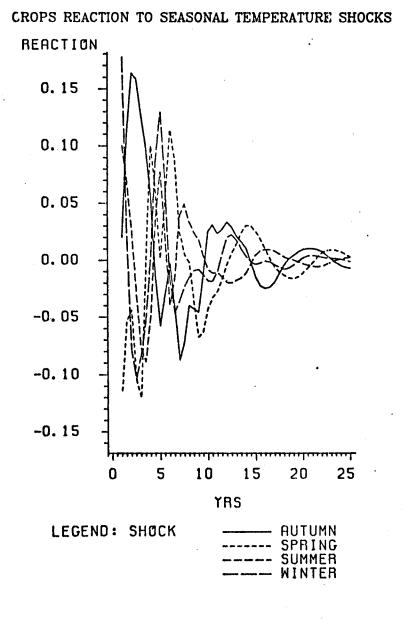


positively to an increase in fertility, although the former response is These may reflect crowding effects delayed for several years. 'as children compete for the limited resources within the family. Interestingly, death rates cycle in opposite fashion when responding to shocks in the death Although we do not completely understand these rate themselves. have plausible interpretations. For example, the interactions, some observed fall in the non-infant death rate due to an increase in the infantdeath rate may represent a selection or "survival of the fittest" process whereby the death of the weakest infants reduces the mortality rate of those that survive. Also, the impacts of the death rate shocks on themselves possibly reveal the short-lived nature of epidemics in this period, with the non-inf death rate responding to its own shock with somewhat more persistance than in the case of the infant death rate.

Figures 4a and 4b illustrate the reaction of crops to the exogenous and economic variables. Except for warm springs, higher temperatures initially increase agricultural output followed by a sharply fluctuating pattern somewhat similar to that obtained from a shock in crops itself (figure 4b). Rainfall also increases crops initially with the same kind of subsequent oscillatory pattern as observed for temperature. An increase in the real wage has a discernible (negative) impact on crops, but only five to seven years later, for reasons that we do not understand.

The real wage responds to seasonal temperatures in a qualitatively similar way as do crops (figures 4c and 4a). The response of wages to rainfall is, however, negligible. The wage response to an increase in crops could not reflect an increase in the marginal product of labor, since the initial response is negative, but would be consistent with an exogenous increase in the supply of agricultural labor.

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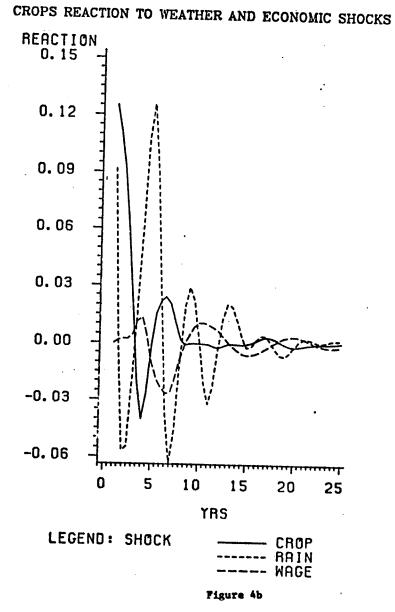
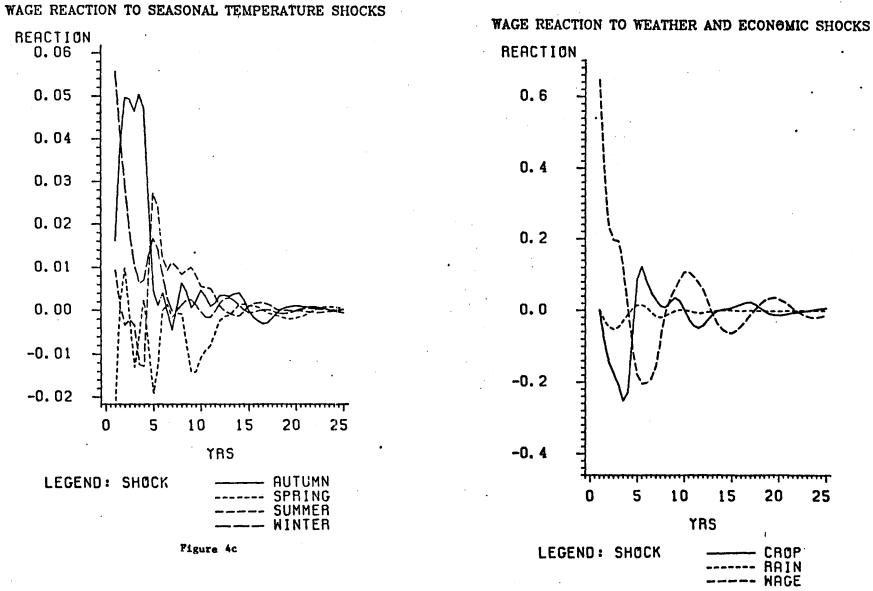


Figure 4a

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We compared the above results to impulse responses where the contemporanous correlations between the errors of the endogenous variables were triangularized as suggested by Sims (1980). We used two alternative orderings of variables which were different only with respect to the order of the pairs NIDR-IDR and RNAGE-CROP. The responses of the demographic variables to weather shocks as well as to shocks in RWAGE and CROPS were basically unchanged. The shape and scale of the responses were insensitive to these different triangularizations of the covariance matrix; the initial sign and cycle of the responses of these variables were particularly robust. However, responses of the demographic variables to shocks in demographic variables showed significant changes with respect to alternative interpretations of the covariance matrix. Specifically, the sign of the initial response, the pattern and the scale were different. Hence, we have less confidence in the robustness of our results with respect to alternative specifications and interpretations of the contemporaneous relationships between the birth rate and the death rates. The example in Section 3 demonstrates a particular rationale for the existence of this type of sensitivity.

The above impulse responses are scaled in logarithmic or proportional changes for each endogenous variable outcome. To compare the magnitudes of these impulse responses and to facilitate their aggregation, responses in the three demographic variables are expressed in common units as they contribute to the natural rate of increase of the population, that is the difference between births and deaths. Table 7 reports the cumulative response from a standard deviation innovation of the residuals contemporaneously, after one year, five

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years and ten years. Since the responses tend to dampen rapidly, the cumulative response after ten years tends to approach an asymptote and thereafter is constant.

Although we previously observed that the response pattern of demographic variables to innovations in real wages and crops were basically similar, their cumulative effects on population growth differ, as seen in Table 7. An unanticipated rise of 12.5 percent in real wages in one year is associated with increase in popul tion growth in the next year by almost one per thousand (.91), and by more than two per thousand (2.24) by the second year. But after the second year the effect of raising birth rates for the first two years is offset by a shortfall in births. The effect of wages reducing deaths, however, continues to accumulate for nearly ten years. Thus, wages affect only the timing of births, whereas the persistent effect of wages on population growth arises from the reduction in mortality, and quantitatively the reduction in noninfant mortality is the bulk of the demographic response (88% of the reduction in deaths after ten years). The importance of the mortality response is consistent with Malthus' supposition and does not accord with Wrigley and Schofield's (1981) conclusion or Lee's (1977) analysis of English data.

On the other hand, with an innovation in the crop index, the response of birth rates cumulates steadily to .44 per thousand in the next year, to .70 after five years, and persists at .77 after ten years. In the case of unanticipated variation in crops, however, infant deaths are little affected, and noninfant mortality falls for only two years, with a more than offsetting reversal in later years, not unlike Lee's (1981) finding for the effect of wheat prices on mortality in England. Thus, abundant

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## Table 7

## Cumulative Impulse Response in Demographic Variables

on Rate of Population Increase Per Thousand Inhabitants Per Year

| Variable Shocked                 |                      | · · · · |      |      |                       | •     |
|----------------------------------|----------------------|---------|------|------|-----------------------|-------|
| by One Standard<br>Deviation     |                      |         |      |      | n Populat<br>Number o |       |
| (Percent of Mean)                |                      | 0       | 1    | 2    | 5                     | 10    |
| Real Wage                        | Crude Birth Rate     | *       | .54  | 1.02 | 07                    | 25    |
| (12.5%)                          | Infant Death Rate    | *       | .05  | .16  | .16                   | .30   |
| See figure 2b                    | NonInfant Death Rate | *       | .33  | 1.06 | 1.25                  | 2.14  |
|                                  | Population Growth    | *       | .91  | 2.24 | 1.34                  | 2.19  |
| Crop Index                       | Crude Birth Rate     | *       | .10  | .44  | .70                   | · .77 |
| (65%)                            | Infant Death Rate    | *       | .06  | .01  | 13                    | 13    |
| See figure 2a                    | NonInfant Death Rate | *       | .60  | .76  | 43                    | 43    |
|                                  | Population Growth    | *       | .76  | 1.21 | .15                   | .21   |
| Infant Death Rate                | Crude Birth Rate     | *       | .18  | .55  | 02                    | 20    |
| (7.65%)<br>See figures 3a and 3b | NonInfant Death Rate | *       | .24  | •96  | 1.65                  | 1.36  |
| NonInfant Death Rate             | Crude Birth Rate     | *       | 08   | 16   | .68                   | 1.03  |
| (12.6%)<br>See figures 3a and 3b | Infant Death Rate    | *       | 01   | .00  | .13                   | .16   |
| Winter Temperature               | Crude Birth Rate     | .49     | .95  | 1.17 | .81                   | .57   |
| (16.9%)                          | Infant Death Rate    | .07     | .24  | .34  | .33                   | .38   |
| See figure 2c                    | NonInfant Death Rate | .64     | 1.91 | 2.63 | 1.95                  | 2.19  |
|                                  | Population Growth    | 1.20    | 3.10 | 4.14 | 3.09                  | 3.14  |

\* Assumed to be zero

harvests in Sweden are associated with only a transitory remission in mortality and the persistent source of population growth linked to good crops accrues through an elevated fertility level.

Among the impulse responses of demographic variables to each other, Table 7 reports the responses to shocks coming from the two death rates. An innovation in infant mortality rate is equal to a 7.7 percent increase, which would itself reduce population growth by .45 per thousand. The increase in the birth rate in the following year adds .18 to the rate of population growth and consequently "replaces" 40% of the additional infant deaths. After two years the cumulative replacement reaches 122 percent, but is completely offset in the next three years by below average fertility, leaving the net effect negative after five or ten years. The replacement of infant deaths is apparently only one of timing, not of raising completed fertility. Noninfant deaths decrease, however, after a rise in infant mortality, perhaps because the more stringent selection of infants who survive improve their health endowments and augment their survival through childhood. This effect cumulates for five years and then tapers off.

As we have noted, shocks in noninfant deaths are associated with a decline in births for two years, followed by a substantial "replacement," cumulating after ten years to one per thousand or 43 percent of the initial number of unanticiapted noninfant deaths. Infant deaths, on the other hand, are not greatly affected by shocks in noninfant deaths.

Finally, the least difficult to interpret relationships are those linking weather innovations to demographic outcomes. The largest effects are associated with Winter mean temperature for which a standard deviation rise involves an increase of 17 percent or 3 degrees Fahrenheit. As shown in Table 7, this shock leads to a rise in birth rates and a decline in

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death rates, with the contemporary rate of population growth increasing 1.5 per thousand, cumulating to an effect of 3.1 by the following year that is more or less persistent. The temperature of the other three seasons have smaller and offsetting effects, suggesting that a general warming of the climate in one year is linked to a substantial increase in population over the following five years, that is not counterbalanced by a later shortfall.

### 6. Conclusions

We have described and interpreted Swedish historical demographic, economic and weather annual data for the entire country using vector autoregression. Our particular emphasis has been on short run interactions in the preindustrial period, as characterized by the impulse responses of the estimated system from 1756 to 1869. We found that unexpected increases in wealth, whether this occurred through changes in real wages, agricultural output, or weather, led to increased fertility and decreased mortality, at least for several years, and thus to an increased rate of population growth cumulatively over a five to ten year period. We observed a short-run replacement phenomenon in that an unanticipated increase in infant deaths increased sharply fertility for one or two years, although only a negligible cumulative effect remained after five or ten years, indicative of a timing response in fertility that did not modify lifetime fertility patterns. An unanticipated increase in non-infant deaths also evoked a fertility response several years later, consistent with a delayed replacement effect, but this response appears to persist for at least a decade.

Although vector autoregression is not designed to account for long term trends and their consequences, our analysis of short term fluctuations suggests the need for further study of how longer trends and swings in weather variables could contribute to persistent changes in population growth, operating principally, perhaps, through variation in mortality rates. Many persons have hypothesized a link from long cycles in weather to swings in mortality; our short run evidence could be seen as consistent with this conjecture.

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The other long term relationship we would like to understand better is that between the wage rate and population growth, but both of these variables are endogenous and detrended in our analysis. In the short to medium term, say less than ten years, real wage innovations contribute to population growth, mainly by reducing death rates. But the response of mortality or fertility to a secular change in real wage may not be as we have discovered here.

These results, like all of the results detailed in the paper, are not interpreted as stemming from a single structural relationship, whether it is a biological or technological constraint, or a function of people's preferences. Our findings are presumed to be derived from a complex behavioral and biological system, and should not be interpreted as distinguishing between particular hypotheses that relate to the existence or importance of particular structural components of the system. Such a task must be left for future work.

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-50-Appendix A

## Table A-1

### Definitions and Sources of Data

### Definition

Symbol

## CBR Crude Birth Rate: The number of births registered per thousand inhabitants during calendar year.

- IDR Infant Death Rate: The number of deaths of children under one year of age per thousand live births during calendar year. See text for minor adjustment of births included in denominator to include some births of previous calendar year.
- NIDR NonInfant Death Rate: The number of deaths of persons one year and older per thousand inhabitants one year and older during calendar year.
- CROPS A general index of Swedish crop yields: The relative abundance of crops in the calendar year season, constructed by G. Sundbarg from Royal Commission estimates and subsequent crop yield information. Not strictly available for last few years, when U.N. index of agricultural output in Sweden was substituted.
- RWAGE The real wage in agriculture: From 1750-1869 series is the daily wage for a male agricultural worker divided by the price of a hectolitre of Rye (representative of foodprices). Alternative cereal prices varies together (r > .98). Beginning in 1870 an overall agricultural annual wage is available (Jungsfeldt), which is deflated by a GNP deflator (Phelps-Brown).
- WNTEMP Mean Winter Temperature: The monthly mean temperatures for January, February and March, averaged for the calendar year in Fahrenheit divided by ten.

Source and Notes

1750-1950, Sweden (1955) Table B.2; 1951-1955 United Nations (1979)

1750-1950, Sweden (1955) Table B.2; 1951-1955, United Nations (1979)

1750-1950, Sweden (1955) Table B.2: 1951-1955, United Nations (1979)

1750-1800, Sundbarg (1907, Table C); 1800-1955,Sweden (1959) Table E12

1750-1869, Joburg (1972); 1870-1955 Jungsfeldt (1966) and Phelps Brown (1968)

1856-1955 Sweden (1959). Table C2

## /----

## Table A-1 continued

- SPTEMP Mean Spring Temperature: The monthly mean as above for WNTEMP temperatures for April, May and June, averaged for the calendar year in Fahrenheit, divided by ten.
- SUTEMP Mean Summer Temperature: The monthly mean tem- as above for WNTEMP perature for July, August and September, averaged for the calendar year in Fahrenheit, divided by ten.
- AUTEMP Mean Autumn Temperature: The monthly mean as above for WNTEMP temperature for October, November and December, averaged for calendar year in Fahrenheit, divided by ten.
- RAIN Precipitation in centimeters during calendar 1750-1955, Sweden year: The average reported at the meteorologi- (1959). Table C7-C8 cal stations at Lund, Stockholm and Uppsala with exceptions noted in text.

### Table A-2

## Basic Data Series in Natural Logarithms

### Table A-2 continued

### Basic Data Series in Natural Logaritime.

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| •        |           |          |          | •       |          |            |          |              | •        |    |
|----------|-----------|----------|----------|---------|----------|------------|----------|--------------|----------|----|
| CALENDAR | CBP       | MIDP     | NIDR     | GINDX   | CALFNDAR |            |          |              |          |    |
| 1756-    | -3.32471  | -1.52649 | -R.49858 | 1.60344 | YEAR     | CBR '      | MIDR     | NIDR         | CINDX    |    |
| 1757-    | -3.42403  | -1.55017 | -8.35791 | 2.01490 | 1810-    | -3.41332   | -1.56939 | -8.25246     | 3.69989  |    |
| 1759-    | -3.39997  | -1.55678 | -R.24454 | 3.40120 | 1811-    | -3. 14693: | -1+61221 | -8.19088     | 2.56495  |    |
| 1759-    | -3.39592  | -1.65838 | -8.49160 | 3.80666 | 1812-    | -3. 19559  | -1.61031 |              | 2.01944  |    |
| 1760-    | -3.33767  | -1.69242 | -8.57031 | 3.40120 | 1813-    | -3.51620   | -1.66648 | ÷ e. 41 738  | 2.99573  |    |
| 1761-    | -3.36209  | -1.57196 | -8.56282 | 2.01490 | 1814-    | -3.47045   | -1.61390 | -8.54043     | 3.55535  |    |
| 1762-    | -3.35181  | -1.42501 | -8.35118 | •0      | 1815-    | -3.36451   | -1.73575 | -8.61052     | 3.68389  |    |
| 1763-    | -3.35383  | -1.42596 | -8.27968 | 2.01490 | 1816-    | -3.34976   | -1.68461 | -8.79001     | 2.30259  |    |
| 1764-    | -3.36452  | -1.57497 | -8.48342 | 1.60944 | 1817-    | -3.40390   | -1.73978 | -8.57794     | 2.70905  |    |
| 1765-    | -3.40153  | -1.56257 | -8.45720 | 3.40120 | 1818-    | -3.39142   | -1.77245 | -0.55713     | 2.56495  |    |
| 1766-    | -3.39136  | -1.55979 | -8.59187 | 3.40120 | 1819-    | -3.41467   | -1.70485 | -8.42276     | 3.55535  |    |
| 1767-    | -3.34662  | -1.59483 | -8.55834 | 3.40120 | 1820-    | -3.41658   | -1.80897 | -e.53605     | 3.20666  |    |
| 1768-    | -3.39576  | -1.53400 | -8.49620 | 3.80666 | 1821-    | -3.34487   | -1.70737 | · -8.51982 . | 3.55535  | •  |
| 1769-    | -3.41203  | -1.53366 | -8.48696 | 3.80666 | 1822-    | -3.33435   | -1.80962 | -8.66400     | 3-13549  |    |
| 1770-    | -3.41471  | -1.56440 | -8.52921 | 3.40120 | 1823-    | -3:30933   | -1.90052 | -8.73743     | 3.69888  |    |
| 1771-    | -3.43645  | -1.56373 | -8.43921 | •0      | 1824-    | -3.37219   | -1.87537 | -8.75129     | 3.68888  |    |
| 1772-    | -3.53983  | -1.47646 | -8.06147 | 1.60944 | 1825-    | -3.31874   | -1.84842 | -8.78137     | 3.40120  |    |
| 1773-    | -3.65440  | -1.31156 | -7.66289 | 3.40120 | 1826-    | -3.36313   | -1.77353 | -8.67256     | 2.30259  |    |
| 1774-    | -3.37388  | -1.70150 | -8.67454 | 3.40120 | 1827-    | -3.46832   | -1.86179 | -8.59356     | 3.68989  |    |
| 1775-    | -3.33959  | -1.67169 | -8.57703 | 1.60944 | 1828-    | -3.39635   | -1.74477 | -8.43707     | 3.65668  |    |
| 1776-    | -3.41860  | -1.77338 | -8.66469 | 3.40120 | 1829-    | -3.35963   | -1.62333 | -8.37966     | 3.40120  |    |
| 1777-    | -3.41409  | -1.62920 | -8.56618 | 3.80666 | 1830-    | -3.41842   | -1.73243 | + E. 58566   | 3.13549  |    |
| 1778-    | -3.36160  | -1.53063 | -8.52207 | 3.40120 | 1831-    | -3.49262   | -1+64665 | -8.49051     | 2.94573  |    |
| 1779-    | -3.30993  | -1.51488 | -8.45317 | 3.80666 | 1832-    | -3.49202   | -1.78578 | -8.59093     | 3.68168  |    |
| 1780-    | -3.33925  | -1.81367 | -8.71845 | 1.60944 | .1833-   | -3.38440   | -1.80157 | -8.69295     | 3.40120  |    |
| 1781-    | -3.40073  | -1.67041 | -8.53204 | 1.60944 | 1834-    | -3.39323   | -1.75201 | -8.49574     | 2.99573  |    |
| 1792-    | -3.44235  | -1.69924 | -8.42634 | 1.60944 | 1835-    | -3.42838   | -1.95551 | -8.85521     | 3+55535  |    |
| 1793-    | -3.49632  | -1.61392 | -8.39313 | 1.40744 | 1836-    | -3.45272   | -1.88451 | -8.77060     | 3.40120  |    |
| 1784-    | -3.45731  | -1.61744 | -8.32043 | 3.40120 | 1837-    | -3.48162   | -1.64479 | -8.55931     | 2.85037  |    |
| 1795-    | -3.46103  | -1.64777 | -8.37999 | 1.60944 | 1838-    | -3.52994   | -1.75535 | -8.54455     | 3.55535  |    |
| 1796-    | -3.41769  | -1.57997 | -8.52262 | 3.40120 | 1839-    | -3.52640   | -1.80377 | -8.55635     | 3.40120  |    |
| 1797-    | -3.44203  | -1.69323 | -8.58998 | 3.80666 | 1840-    | -3.46502   | -1.90357 | -8.72791     | 3.55535  | ι, |
| 1789-    | -3.38459  | -1.54269 | -8.50299 | 3.68988 | 1841-    | -3.50091   | -1.84585 | -8.80757     | 2.30259  | Ň  |
| 1789-    | -3.44087  | -1.52007 | -8.22239 | 3.40120 | 1842-    | -3.45814   | -1.80411 | -8.71753     | 3.13549  | 1  |
| 1790-    | -3.44027  | -1.58752 | -8,30057 | 3.80666 | 1843-    | -3.48561   | -1.84220 | -8.68028     | 2.99573  |    |
| 1791-    | -3.42599  | -1.64728 | -8.51910 | 3.68888 | 1844-    | -3.44308   | -1.94292 | -8.72969     | 3.21888  |    |
| 1792-    | -3.31424  | -1.59835 | -8.65782 | 3.40120 | 1845-    | -3.46556   | -1.90971 | -8.63701     | 2.70805  |    |
| 1793-    | -3.37486  | -1.63064 | -8.67647 | 3.68888 | 1846-    | -3.51241   | -1.82613 | -8.65672     | 3.71868  |    |
| 1794-    | -3.39245  | -1.71470 | -8.62158 | 3.68888 | 1847-    | -3.52339   | -1.75504 | -8.56475     | 3.40120  |    |
| 1795-    | -3.44270  | -1.61645 | -8.41624 | 3.68888 | 1848-    | -3.50068   | -1.94837 | -8.75291     | 3.55535  |    |
| 1796-    | -3.16573  | -1.61102 | -8.59433 | 3.40120 | 1849-    | -3.42239   | -1.92460 | -8.76581     | 3-21088  |    |
| 1797-    | -3.36384  | -1.62598 | -8.64932 | 3.40120 | 1850-    | -3.45142   | -1.92835 | - 2.77010    | 3.40120  |    |
| 1798-    | -3.39543  | -1.70323 | -8.65648 | 1.60944 | 1851-    | -3.45515   | -1.88135 | -8.71989     | 3.21888  |    |
| 1799-    | -3.44401  | -1.67452 | -8.53482 | 1.60944 | 1852-    | -3.48705   | -1.82520 | -8.61116     | 3.55535  |    |
| 1800-    | -3.54008  | -1.47318 | -8.28109 | 1.60944 | 1853-    | -3.46526   | -1.81693 | -8.56058     | 3.21 988 |    |
| 1901-    | -3.50683  | -1.57133 | -8.49102 | 3.40120 | 1854-    | -3.40256   | -2.04559 | -8.74251     | 3.40120  |    |
| 1902-    | -3.45459  | -1.67876 | -8.59820 | 3.40120 | 1855-    | -3.45446   | -1.94616 | - E. 6611 B  | 3.55535  |    |
| 1803-    | -3.46574  | -1.69282 | -8.59491 | 3.68888 | 1856-    | -3.46312   | -1.93273 | -8.63960     | 3.21888  |    |
| 1804-    | -3.44 827 | -1.67575 | -8.54191 | 3.40120 | 1857-    | -3.43068   | -1.78738 | -8.38136     | 3.40120  |    |
| 1805-    | -3.45439  | -1.73954 | -8.59893 | 2.89037 | 1858-    | -3.36518   | -1.92180 | -8.66685     | 3.53535  |    |
| 1806-    | -3.49324  | -1.48256 | -8.46481 | 3.40120 | 1859-    | -3.35972   | -1.93758 | -8.76832     | 3.40120  |    |
| 1807- '  | -3.47094  | -1.66599 | -8.46961 | 3.13549 | 1860-    | -3.36679   | -2.08637 | -8.89619     | 3.40120  |    |
| 1808-    | -3.49109  | -1.52540 | -8.14120 | 2.89037 | 1861-    | +3.43187   | -2.00273 | -8.84825     | 3.17549  |    |
| 1809-    | -3.61720  | -1.51943 | -7.95670 | 3.68888 | 1862-    | -3.40584   | -1.95878 | -8.66691     | 3.55535  |    |
|          |           |          |          |         | 1863-    | -3.39976   | -2.01374 | -8.78625     | 3.40120  |    |
|          |           |          |          |         | 1864-    | -3,39873   | -1.98560 | -8.73405     | 3.55535  |    |
|          |           |          |          |         |          |            |          |              |          |    |

### Table A-2 continued

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#### Banic Data Series in Natural Logarithms

#### Table A-2 continued

Basic Data Series in Natural Logarithms

|    |                  |                      |  |                      |                    |           | Basic Date | A Series in Natural | Logarithms |           |
|----|------------------|----------------------|--|----------------------|--------------------|-----------|------------|---------------------|------------|-----------|
|    | CALENDAR<br>7EAR | CBR                  |  |                      |                    |           |            |                     |            |           |
|    | 1855-            | ~3.42225             | MIDE<br>-2.00615                       | NIUR<br>-8.78202     | CINDX<br>3.29584   |           |            |                     |            |           |
| i. | 1866-            | -3.41353             | -2.05775                               | -8.72642             | 3.43359            |           |            |                     |            |           |
|    | 1867-            | -3.48330             | -1.98588                               | -8.75661             | 3.25810            |           |            |                     |            | •         |
|    | 1968-            | -3.59187             | -1.82086                               | -8.68746             | 3.21888            |           |            |                     |            |           |
|    | 1869-            | -3.56503             | -1.91805                               | -8.58370             |                    | 011 P1010 |            |                     |            |           |
|    | 1870-            | ~3.54918             | -2.01959                               |                      | 3.58352            | CALENDAR  | <b>~~</b>  | Man .               |            | <b>61</b> |
|    | 1871-            | -3.49703             | -2.15956                               | -8.71201             | 3.61092            | YEAR      | CBR        | MIDR                | NIDR       | GINDX     |
|    | 1872-            | -3.51072             | -2.05459                               | -8.96523             | 3.58352            | 1920- 1   | -3.75077   | -2.72556            | -9.02574   | 3.526     |
|    | 1873-            | -3.48580             | -2.03439                               | -8.96851             | 3.46574            | 1921- 1   | -3.94201   | -2.76566            | -9.09546   | 3.433     |
|    | 1974-            | -3.48377             | -1.91546                               | -8.90443             | 3.52636            | 1922- 1   | -3.93572   | -2.79100            | -9.04826   | 3.433     |
|    | 1875-            | -3.47321             |  | -8.72734             | 3.29584            | 1923- 1   | -3.96924   | -2.88455            | -9.15870   | 3.433     |
|    | 1876-            | -3.48424             | -1.89754                               | -8.73695             | 3.55535            | 1924- 1   | -4.01366   | -2.81673            | -9.11152   | 3.367     |
|    | 1877-            |                      | -1.96484                               | -8.76121             | 3.40120            | 1925- 1   | -4.04221   | -2.89355            | -9.12145   | 3.526     |
|    | 1878-            | -3.47769<br>-3.51759 | -2.06714                               | -8.79567             | 3.29584            | 1926- 1   | -4.08679   | -2.89154            | -9.11594   | 3.495     |
|    | 1879-            |                      | -2.01839                               | -8.84485             | 3.63759            | 1927- 1   | -4.12916   | -2.82560            | -9.03523   | 3.433     |
|    | 1980-            | -3.49443<br>-3.52653 | -2.18900                               | -8.88146             | 3.49651            | 1928- 1   | -4.13328   | -2.83381            | -9.09360   | 3.433     |
|    | 1681-            | -3.53989             | -2.12371                               | -8.90363             | 3.52636            | 1929- 1   | -4.18823   | -2.84879            | -9.07363   | 3.465     |
|    | . 1892-          | -3.52919             | -2.18537                               | -8.81642             | 3.21888            | 1930- 1   | -4.17730   | -2.90239            | -9.11345   | 3.465     |
|    | 1883-            | -3.54518             | -2.07990<br>-2.15960                   | -8.96673             | 3.61092            | 1931- 1   | -4.21456   | -2.87791            | -5.04037   | 3.367     |
|    | 1884-            | -3.51079             | -2.16315                               | -8.84978             | 3.40120            | 1932- 1   | -4.23340   | -2.98401            | -9.11805   | 3.526     |
|    | 1985-            | -3.52942             | -2.17143                               | -8.83814             | 3.€1092            | 1933- 1   | -4.29128   | -3.01656            | -9.14508   | 3.433     |
|    | 1886-            | -3.51917             | -2.19181                               | -8.82109             | 3.36730            | 1934- 1   | -4.29389   | -3.05377            | -9.14091   | 3.433     |
|    | 1897-            | -3.51987             | -2.27157                               | -8.89903             | 3.43399            | 1935- 1   | -4.28716   | -3.07967            | -5.09951   | 3.465     |
|    | 1889-            | -3.54957             | -2.30616                               | -8.91432             | 3.46574            | 1936- 1   | -4.25510   | -3.13121            | -9.07153   | 3.473     |
|    | 1897-            | -3.54770             |  | - 8. 91212           | 3.43399            | 1937- 1   | -4.24193   | -3.09418            | -9.06953   | 3.494     |
|    | 1890-            | -3.57841             | -2.24102                               | -8.92162             | 3.29584            | 1938- 1   | -4.20720   | - 3.15079           | -9.11033   | 3.526     |
|    | 1891-            | -3.56785             | -2.26940                               | -8.82980             | 3.63759.           | 1939- 1   | -4.17622   | -3.22477            | -9.10998   | 3.433     |
|    | 1892-            | -3.61193             | -2.22274<br>-2.22600                   | -8.96419             | 3.46574            | 1940- 1   | -4.19755   | -3.24148            | -9.11564   | 3.135     |
|    | 1693-            | -3.60064             |  | -8.78129             | 3.66356            | 1941- 1   | -4.16263   | -3.29021            | -9.13173   | 2.995     |
|    | 1894-            | -3.61319             | -2.28657                               | -8.94386             | 3.40120            | 1942- 1   | -4.03725   | -3.51187            | -9.25942   | 3.332     |
|    | 1995-            | -3.59961             | -2.29395                               | -8.87694             | 3.49651            | 1943- 1   | -3.95162   | -3.52972            | -9.23404   | 3.367     |
|    | 1896-            | -3.00754             | -2.35122<br>-2.27059                   | -8.95731<br>-8.93820 | 3.43399<br>3.52636 | 1944- 1   | -3.88921   | -3.45699            | -9.15810   | 3.401     |
|    | 1897-            | -3.62878             | -2.31950                               |                      |                    | 1945- 1   | -3.89790   | -3.50791            | -9.17336   | 3.413     |
|    | 1899-            | -3.51321             | -2.39297                               | -8.94714<br>-8.95560 | 3.49651            | 1946- 1   | -3.73201   | -3.63313            | -9.19823   | 3.465     |
|    | 1899-            | -3.63953             | -2.19723                               | -8.80117             | 3.61092<br>3.29584 | 1947- 1   | -3.97274   | -3.67836            | -9.16408   | 3-17A     |
|    | 1999-            | -3.51586             | -2.31038                               | -8.83782             | 3.61092            | 1948- 1   | -4.00119   | -3.76712            | -9.25894   | 3.433     |
|    | 1901-            | -3.61451             | -2.27131                               | -8.90379             | 3.40120            | 1949- 1   | -4.05365   | -3.76691            | -9.23893   | 3.496     |
|    | 1902-            | -3.63354             | -2.45294                               | -8.91712             | 3.40120            | 1950- 1   | -4.11110   | -3.87193            | -9.23060   | 3.465     |
|    | 1903-            | -3.66344             | -2.38332                               | -8.94733             | 3.52636            | 1951- 1   | -4.16567   | -3.84286            | -9.24624   | 3.332     |
|    | 1904-            | -3.66312             | -2.47075                               | -8.91648             | 3.36730            | 1952- 1   |            | -3.91056            | -9.27398   | 3.401     |
|    | 1905-            | -3.56620             | -2.42614                               | - 8.89835            | 3.49651            | 1953- 1   | -4.17898   | -3.97716            | -9.25854   | 3.465     |
|    | 1906-            | -3.66523             | -2.51066                               | -8.98275             | 3.63759            | 1954- 1   | -4.23177   | -3.98127            | -9.27153   | 3.401     |
|    | 1907-            | -3.57155             | -2.56602                               | -8.95521             | 3.52636            | 1955- 1   | -4.21860   | -4.04817            | -9.28347   | 3.135     |
|    | 1909-            | -3.66605             | -2.45631                               | -8.94907             | 3.71357            |           |            |                     |            |           |
|    | 1909-            | -3.67011             | -2.62763                               | -9.02141             | 3.55535            |           |            |                     |            |           |
|    | 1910-            | -3.70667             | -2.59542                               | -8.95188             | 3.61092            |           |            |                     |            |           |
|    | 1911-            | -3.73350             | -2.43479                               | -9.00167             | 3.43399            |           |            |                     |            |           |
|    | 1912-            | -3.74191             | -2.64722                               | -8.96644             | 3.52636            |           |            |                     |            |           |
|    | 1913-            | -3.76A32             | -2.66753                               | -J.00488             | 3.55535            |           |            |                     |            |           |
|    | 1914-            | -3.7P128             | -2.62008                               | -8.94444             | 3.29584            |           |            |                     |            |           |
|    | 1915-            | -3.83829             | -2.59294                               | -8.92621             | 3.40120            |           |            |                     |            |           |
|    | 1916-            | -3.95688             | -2.66549                               | -9.00381             | 3.52636            |           | i.         |                     |            |           |
|    | 1917-            | -3.97117             | -2.74221                               | -9.00728             | 3.21888            |           |            |                     |            |           |
|    | 1918-            | -3.89770             | -2.74430                               | -8.67827             | 3.21888            |           |            |                     |            |           |
|    |                  |                      | ~~ · · · · · · · · · · · · · · · · · · |                      |                    |           |            |                     |            |           |
|    | 1919-            | -3.92708             | -2.66933                               | -8.92471             | 3.49651            |           |            |                     |            |           |

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3.52636 3.43399 3.43399 3.43399 3.36730 3.52636 3.49651 3.43349 3.43399 3.46574 3.46574 3.36730 3.52636 3.43399 3.47399 3.46574 3.47399 3.49451 3.52636 3.43399 3.13549 2.99573 3.33220

3.36730 3.40120 3.41399 3.46574 3.17805 3.43399 3.49651 3.46574 3.33220 3.40120 3.46574 3.40120 3.13549

### Basic Data Series in Natural Logarithms

# Table A-3 continued

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## Basic Data Series in Natural Logarithms

| •              |         |          |           | CALENDAR<br>YEAR | RAIN    | RWAGE    | ATEM      |
|----------------|---------|----------|-----------|------------------|---------|----------|-----------|
| CALFNDAR       |         |          |           | 1808-            | 6.33091 | -2.95491 | 6.03357   |
| YEAR           | RAIN    | RWAGE    | ATEMP     | 1809-            | 6.24352 | -2.64636 | 6.00734   |
| 1756-          | 5.97064 | -2.63906 | 6.03357   | 1810-            | 6.04737 | -2.42037 | - 6.02490 |
| 1757-          | 6.04664 | -2.78037 | 6.04643   | 1811-            | 6.10951 | -2.57671 | 6.09221   |
| 1758-<br>1759- | 5.69047 | -2.51231 | 5.57396   | 1812-            | 5.92993 | -2.63223 | 5.97594   |
| -              | 5-93120 | -2.22162 | 6.06332   | 1913-            | 6.08526 | -2.50611 | 6.05491   |
| 1760-          | 6.12898 | -2.26868 | 6.01616   | 1814-            | 5.86930 | -2.44107 | 5.98946   |
| 1761-          | 6.26471 | -2.40695 | 6.06750   | 1815-            | 6.15768 | -2.40057 | 6.05491   |
| 1762-          | 6.29479 | -2.77778 | 6.04216   | 1816-            | 6.06456 | -2.51113 | 6.01176   |
| 1763-          | 6.15436 | -2.56495 | 6.00734   | 1817-            | 5.97720 | -2-59135 | 6.04543   |
| 1764-          | 6.00715 | -2.50041 | 6.06750   | 1818-            | 5.91350 | -2.65854 | 6. CA814  |
| 1765-          | 6.09170 | -2.42591 | 6.04543   | 1819-            | 5.97381 | -2.61675 | 6.11235   |
| 1766-          | 6.06016 | -2.21102 | 6.07581   | 1820-            | 6.16612 | -2.46783 | 6.03797   |
| 1767-          | 6.26370 | -2.09597 | 6.01616   | 1821-            | 6.12395 | -2.24420 | 6.07166   |
| 1768-          | 6.01241 | -2.32728 | 6.02054 * | 1822-            | 6.03229 | -2.23845 | 6.15146   |
| 1769-          | 6.18983 | -2.27727 | 6.02490   | 1823-            | 6.15060 | -2.17891 | 6.07581   |
| 1770-          | 6.26353 | -2.33289 | 6.03787   | 1824-            | 6.20926 | -2.14696 | 6.11633   |
| 1771-          | 6.21794 | -2.76777 | 5.99944   | 1825-            | 6.13988 | -2.11860 | 6.07166   |
| 1772-          | 6.27384 | -2.76777 | 6.01176   | 1826-            | 5.70932 | -2.56953 | 6.11235   |
| 1773-          | 6.17174 | -2.56495 | 6.10836   | 1827-            | 6.02667 | -2.30408 | 6.05912   |
| 1774-          | 6.08016 | -2+25533 | 6.02054   | 1828-            | 6.12687 | -2.12503 | 6.03357   |
| 1775-          | 6.23736 | -2.39790 | 6.12425   | 1829-            | 5.99894 | -2.32440 | 5.94804   |
| 1776-          | 5,96546 | -2.29570 | 6.06332   | 1830-            | 6.11956 | -2.40838 | 6.01616   |
| 1777-          | 5.91449 | -2.28238 | 6.02490   | 1831-            | 6.11325 | -2.56174 | 6.03357   |
| 1778-          | 6.30244 | -2.30992 | 6.04716   | 1832-            | 6.05653 | -2.29976 | 6.04216   |
| 1779-          | 6.25876 | -2.24469 | 6.12818   | 1833-            | 6.25801 | -2.21890 | 6.05068   |
| 1790-          | 6.04658 | -2.25785 | 6.03787 . | 1834-            | 6.21212 | -2.27155 | 6.09221   |
| 1781-          | 5.79499 | -2.51231 | 6.07581   | 1835-            | 6.05492 | -2.24543 | 6.04216   |
| . 1782-        | 6.27683 | -2.23336 | 6.00290   | 1836-            | 6.18902 | -2.25567 | 6.01616   |
| 1783-          | 5.90272 | -2.49010 | 6.09221   | 1837-            | 6.10777 | -2.41169 | 6.00734   |
| 1784-          | 6.09627 | -2.32116 | 5.98494   | 1838-            | 6.18002 | -2.48259 | 5.56666   |
| 1785-          | 6+21749 | -2.53072 | 5.98946   | 1839-            | 6.07458 | -2.33493 | 6.02924   |
| 1786-          | 6.34553 | -2.63706 | 5.98494   | 1840-            | 6.33387 | -2.36627 | 6.02924   |
| 1787-          | 6.25831 | -2.45101 | 6.04216   | 1841-            | 6.41999 | -2.59300 | 6.04216   |
| 1788-          | 6.06940 | -2.56495 | 5.99396   | 1842-            | 5.93754 | -2.49596 | 6.07581   |
| 1789-          | 6.30946 | -2.62949 | 6.09628   | 1843-            | 6.04501 | -2.36211 | 6.05068   |
| 1790-          | 6.21461 | -2.58525 | 6.06750   | 1844-            | 6.33505 | -2.14409 | 5.97594   |
| 1791-          | 6.15486 | -2.49010 | 6.12030   | 1845-            | 6.17725 | -2.56602 | 6.01616   |
| 1792-          | 6.37359 | -2.54207 | 6.05068   | 1846-            | 6.10777 | -2.54662 | 6.07993   |
| 1793-          | 6.29767 | -2.58289 | 6.07166   | 1847-            | 6.01616 | -2.46097 | 6.03787   |
| 1794-          | 6.29095 | -2.61624 | 6.12425   | 1848-            | 6.36015 | -2.20313 | 6.04643   |
| 1795-          | 6.33356 | -2.55334 | 6.00734   | 1849-            | 6.09146 | -2.19722 | 6.02054   |
| 1796-          | 6.19577 | -2.37601 | 6.07166   | 1850-            | 6+22654 | -2.36393 | 6.03357   |
| 1797-          | 6.32496 | -2.32834 | 6.10032   | 1851-            | 6.34095 | -2.48391 | 6.05912   |
| 1799-          | 6.06533 | -2.48491 | 6.10435   | 1852-            | 6.37218 | -2.44055 | 6.06332   |
| 1799-          | 6.13387 | -2.63631 | 5.98040   | 1853-            | 5.97720 | -2.58710 | 6.04216   |
| 1800-          | 6.42162 | -2. 6958 | 6.02054   | 1854-            | 5.95670 | -2.39998 | 6.07993   |
| 1801-          | 6.28164 | -2.00768 | 6.05912   | 1855-            | 6.15415 | -2.48898 | 6.01176   |
| 1802-          | 6.22983 | -2.80896 | 6.04643   | 1956-            | 6.14132 | -2.34260 | 6.00290   |
| 1903-          | 6.11810 | -2.79484 | 6.00734   | 1857-            | 6.09432 | -2.14702 | 6.08814   |
| 1804-          | 6.13556 | -2.73244 | 6.01176   | 1858-            | 5.90536 | -2.04272 | 6.10032   |
| 1805-          | 6.00471 | -2.69607 | 5.97584   | 1859-            | 6.16612 | -2.03175 | 6.07993   |
| 1806-          | 6.30492 | -2.88480 | 6.03787   | 1860-            | 6.34329 | -2.11727 | 6.01176   |
| 1807-          | 6.28972 | -2.87356 | 6.04216   | 1861-            | 6.28351 | -2.29985 | 6.03787   |

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## Table A-3 continued

#### Basic Data Series in Natural Logarithms

CALENDAR

### Table A-3 continued Basic Data Series in Natural Logarithms

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| ON DELEMAN |           |                      |                    |          |         |          |         |
|------------|-----------|----------------------|--------------------|----------|---------|----------|---------|
| YEAR       | RATH      | RWAGE                | ATEMP              |          |         |          |         |
| 1862-      | 6.16171   | -2.20332             | 5.99396            |          |         |          |         |
| 1853-      | 6.17794   | -2.07834             | 6.08814            |          |         |          |         |
| 1964-      | 6.09507   | -1.91249             | 5.99396            | CALENDAR |         |          |         |
| 1865-      | 6.00981   | -2.00585             | 6.03357            | YEAR     | RAIN    | RWACE    | ATEMP   |
| 1866-      | 6.51669   | -2.14908             | 5.02924            | 1915-    | 6.36015 | -1.48955 | 5.99396 |
| 1867-      | 6.29095   | -2.61496             | 5.93384            | 1916-    | 6.49123 | -1.43175 | 6.04643 |
| 1869-      | 6.24933   | -2.57782             | 6.07581            | . 1917-  | 6.23376 | -1.41431 | 6.02490 |
| 1869-      | 6.28724   | -2.21954             | 6.04216            | 1918-    | 6.32675 | -1.45872 | 6.05332 |
| 1870-      | 6.09980   | -2.18811             | 6.01616            | 1919-    | 6.38294 | -1.44621 | 6.03357 |
| 1871-      | 6.09206   | -2.18338             | 5.95739            | 1920-    | 6.25783 | -1.35928 | 6.09221 |
| 1872-      | 6.44889   | -2.13212             | 6.09628            | 1921-    | 6.31897 | -1.42860 | 6.09221 |
| 1873-      | 6.41728   | -1.97966             | 6.07501            | 1922-    | 6.37616 | -1.45006 | 6.02054 |
| 1874-      | 6.08829   | -1.85107             | 6.05912            | 1923-    | 6.49426 | -1.49628 | 6.01616 |
| 1875-      | 5.98141   | -1.84194             | 5.98494            | 1924-    | 6.36245 | -1.51574 | 6.05068 |
| 1876-      | 6.11983   | -1.81080             | 6.01176            | 1925-    | 6.40302 | -1.51264 | 6.07166 |
| 1877-      | 6.41127   | -1.80207             | 6.00290            | 1926-    | 6.28413 | -1.50385 | 6.05058 |
| 1878-      | 6.30992   | -1.82577             | 6.06750            | 1927-    | 6.51175 | -1.49606 | 6.05068 |
| 1879-      | 6.21261   | -1.89706             | 6.00734            | 1928-    | 6.41072 | -1.49857 | 6.03797 |
| 1980-      | 6.11294   | -1.99352             | 6.04643            | 1929-    | 6.38576 | -1.47799 | 6.04543 |
| 1881-      | 6.19780   | -2.01193             | 5.97584            | 1930-    | 6.52062 | -1.45693 | 6.12030 |
| 1882 -     | 6.35495   | -1.97866             | 6.09914            | 1931-    | 6.33742 | -1.43305 | 6.02490 |
| 1883-      | 6.41619   | -1.94298             | 6.06750            | 1932-    | 6.34972 | -1.43078 | 6.08814 |
| 1884-      | 6.27775   | -1.94248             | 6.05491            | 1933-    | 6.11810 | -1.44493 | 6.07581 |
| 1895-      | 6.35611   | -1.93178             |                    | 1934-    | 6.48870 | -1.46453 | 6.14761 |
| 1896-      | 6.07588   | -1.83318             | 6.02490<br>6.06332 | 1935-    | 6.51619 | -1.46279 | 6.10032 |
| 1887-      | 6.11726 * | -1.81435             |                    | 1936-    | 6.41945 | -1.41213 | 6.10435 |
| 1999-      | 6.27915   | -1.87637             | 6.06332            | 1937-    | 6.42325 | -1.34431 | 6.11235 |
| 1889-      | 6.25255   | -1.87961             | 5.97584            | 1938-    | 6.35205 | -1.30583 | 6.14376 |
| 1890-      | 6.49979   |                      | 6.05491            | 1939-    | 6.26593 | -1.26493 | 6.10336 |
| 1891-      | 6.30749   | -1-88009             | 6.07581            | 1940-    | 6.20725 | -1.28950 | 6.01176 |
| 1892-      | 6.11368   | -1.81494<br>-1.78253 | 6.06750            | 1941-    | 6.23048 | -1.29284 | 6.00734 |
| 1893-      | 6.26.276  | -1.72973             | 6.02054            | 1942-    | 6.24869 | -1.25514 | 5.99396 |
| 1894-      | 6.37899   | -1.49555             | 6.01616<br>6.10032 | 1943-    | 6.42325 | -1.21665 | 6.13210 |
| 1895-      | 6.41127   | -1.70168             |                    | 1944-    | 6.44148 | -1.17144 | 6.10435 |
| 1896-      | 6.40908   | -1.70415             | 6.04643            | 1945-    | 6.50976 | -1.04573 | 6.10032 |
| 1897-      | 6.39248   | -1.72018             | €.09221<br>6.07581 | 1946-    | 6.32197 | 935458   | 6.09814 |
| 1898-      | 6.55725   | -1.71950             | 6.07993            | 1947-    | 5.97211 | 884722   | 6.06750 |
| 1879-      | 6.29588   | -1.69472             |                    | 1948-    | 6.28940 | 814397   | 6.10435 |
| 1900-      | 6.35495   | -1.65801             | 6.04643<br>6.04643 | 1949-    | 6.31897 | 809453   | 6.13988 |
| 1901-      | 6.09146   | -1.60999             |                    | 1950-    | 6.44572 | 770854   | 6.10032 |
| 1902-      | 6.27351   |                      | 6.0793             | 1951-    | 6.27727 | 865677   | 6.09628 |
| 1903-      |           | -1.62579             | 5.99040            | 1952-    | 6.42162 | 677762   | 6.04643 |
| 1904-      | 6.48970   | -1.65227             | 6.07581            | 1953-    | 6.08829 | 691493   | 6.12819 |
|            | 6.26973   | -1.64417             | 6.03357            | 1955-    | 6.57042 | 669470   | 6.07166 |
| 1905-      | 6.32197   | -1.61749             | 6.06750            | 1955-    | 6.18552 | 600499   | 6.06332 |
| 1906-      | 6.23245   | -1.63999             | 6.08404            | 1955-    | 0.10372 |          | 0.00332 |
| 1907-      | 6.27915   | -1.62012             | 6.03787            | •        |         |          |         |
| 1908-      | 6.33977   | -1.57328             | 6.04643            |          |         |          |         |
| 1909-      | 6.13150   | -1.54342             | 6.02054            |          |         |          |         |
| 1910-      | 6.55298   | -1.51433             | 5.08814            |          |         |          | • •     |
| 1911-      | 6.29219   | -1.48761             | 6.09628            |          |         |          |         |
| 1912-      | 6.50578   | -1.52725             | 6.04643            |          |         |          |         |
| 1913-      | 6.26593   | -1.51242             | 6.08814            |          |         |          |         |
| 1914-      | 6.14275   | -1.45809             | 6.10836            |          |         |          |         |
|            |           |                      |                    |          |         |          |         |

### Basic Data Series in Natural Logarithms

## Table A-4 continued

#### Basic Data Series in Natural Logarithms

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|   |                  |         |                                |                    |                    | CALENDAR<br>YEAR | WINTER  | SPRING    | SUPPLER  | MUTUA   |       |
|---|------------------|---------|--------------------------------|--------------------|--------------------|------------------|---------|-----------|----------|---------|-------|
|   | CALENDAR<br>YEAR | WINTER  | SPR ING                        | SUMMER             | AUTUMN             | 1807-            | 5.59024 | 6.13210   | 6.41215  | 5.85622 |       |
|   | 1756-            | 5.69238 | 6.12949                        | 6.36165            | 5.80694            | 1808-            | 5.48646 | 6.16919   | 6.41510  | 5.83540 |       |
|   | 1757-            | 5.57022 | 6.22297                        | 6.39826            | 5.81771            | 1809-            | 5.15329 | 6.15910   | 16.41902 | 5.90482 |       |
| • | 1758-            | 5.45104 | 6.15910                        | 6.34704            | 5.79423            | - 18 10-         | 5.54440 | 6.10836   | 6.41313  | 5.92305 |       |
|   | 1759-            | 5.76456 | 6.17670                        | 6.39317            | 5.78506            | 1811-            | 5.65948 | 6.24549   | 6.41017  | 5.97324 |       |
|   | 1760-            | 5.40087 | 6.17919                        | 6.39626            | 5.82305            | 1812-            | 5.52066 | 6.07581   | 6.33008  | 5.80694 |       |
|   | 1761-            | 5.67812 | 6.23245                        | 6.39125            | 5.80151            | 1813-            | 5.68222 | 6.14761   | 6.38823  | 5.85105 |       |
|   | 1762-            | 5.61895 | 6.25229                        | 6.32686            | 5.80513            | 1814-            | 5.11439 | 6.14761   | 6.39526  | 5.90154 |       |
|   | 1763-            | 5.46383 | 6.15910                        | 6.36268            | 5.81949            | 1815-            | 5.64897 | 6 . 17295 | 6.36578  | 5.89495 |       |
|   | 1764-            | 5.74172 | 6.18415                        | 6.39225            | 5.81054            | 1816-            | 5.45618 | 6.13730   | 6.38012  | 5.85105 |       |
|   | 1765-            | 5.61677 | 6.17295                        | 6.35123            | 5.89164            | 1817-            | 5.72620 | 6.18291   | 6.30114  | 5.73399 |       |
|   | 1766-            | 5.56299 | 6.24892                        | 6.40225            | 5.89164            | 1818-            | 5.66781 | 6.14247   | 6.40324  | 5.99695 |       |
|   | 1767-            | 5.33078 | 6.13600                        | 6.40519            | 5.90645            | 1819-            | 5.76268 | 6.22535   | 6.48066  | 5.79240 |       |
|   | 1768-            | 5.46637 | 6.15018                        | 6.34914            | 5.90808            | 1820-            | 5.48147 | 6.21341   | 6.38114  | 5.83890 |       |
|   | 1769-            | 5.66988 | 6.18043                        | 6.35019            | 5.74172            | 1821-            | 5.55606 | 6.17170   | 6.35957  | 6.02780 |       |
|   | 1770-            | 5.41965 | 6.16542                        | 6.40721            | 5.90808            | 1822-            | 5.97155 | 6.26035   | 6.38722  | 6.00881 |       |
|   | 1771-            | 5.21058 | 6.19032                        | 6.35333            | 5.90971            | 1823-            | 5.55373 | 6.18539   | 6.39125  | 5.99993 |       |
|   | 1772-            | 5.19073 | 6.11766                        | 6.37707            | 6.02490            | 1824-            | 5.79788 | 6.21501   | 6.42487  | 5.99660 |       |
|   | 1773-            | 5.65739 | 6.23009                        | 6.43165            | 5.95739            | 1825-            | 5.69642 | 6.16919   | 6.36165  | 5.93859 |       |
|   | 1774-            | 5.38450 | 6.24558                        | 6.40324            | 5.73205            | 1826-            | 5.67607 | 6.22178   | 6.44504  | 5.93359 |       |
|   | 1775-            | 5.65529 | 6.23127                        | 6.47235            | 5.94804            | 1827-            | 5.46129 | 6.25229   | 6.36578  | 5.92746 |       |
|   | 1776-            | 5.52545 | 6.17919                        | 6.41313            | 5.93859            | 1828-            | 5.51343 | 6.18539   | 6.38215  | 5.84932 |       |
|   | 1777-            | 5.44328 | 6.18539                        | 6.35333            | 5.89990            | 1829-            | 5.29531 | 6.13600   | 6.35541  | 5.68630 |       |
|   | 1778-            | 5.54674 | 6.20617                        | 6.38823            | 5.80974            | 1830-            | 5.49388 | 6.13859   | 6.35750  | 5.87930 |       |
|   | 1779-            | 5.93364 | 6:22059                        |                    |                    | 1831-            | 5.39544 | 6.18291   | 6.38215  | 5.92745 |       |
|   | 1780-            | 5.60138 | 6 • 11235                      | 6.43165<br>6.40820 | 5.90318            | 1832-            | 5.71637 | 6.12949   | 6.29748  | 5.92906 |       |
|   | 1781-            | 5.57671 | 0 • 1 1 2 3 7<br>5 • 1 9 5 4 4 | 6.45646            | 5.85450<br>5.86306 | 1833-            | 5.62546 | 6.18167   | 6.33008  | 5.92906 |       |
|   | 1782-            | 5.51826 | 6.12697                        | 6.36268            | 5.81234            | 1834-            | 5.71439 | 6.18662   | 6.43358  | 5.87324 |       |
|   | 1783-            | 5.51526 | 6.25920                        | 6.45740            | 5.88832            | 1835-            | 5.71834 | 6.15273   | 6.35?28  | 5+81054 |       |
|   | 1784-            | 5.28015 | 6.15528                        | 6.35750            | 5.85278            | 1836-            | 5.66157 | 6.14633   | 6.30189  | 5.87540 | ່ ບໍ່ |
|   | 1785-            | 5.39174 | 6.14633                        | 6.35957            | 5.82305            | 1837-            | 5.54440 | 6.10032   | 6.33221  | 5.89495 | ð     |
|   | 1786-            | 5.36223 | 6.15783                        | 6.37298            | 5.16268            | 1838-            | 5.17048 | 6.12162   | 6.36784  | 5.84238 | 1     |
|   | 1787-            | 5.69843 | 6.17420                        | 6.33541            | 5.83188            | 1839-            | 5.46890 | 6.16668   | 6.38823  | 5.86817 |       |
|   | 1788-            | 5.35659 | 6.20132                        | 6.41706            | 5.66781            | 1840-            | 5.59248 | 6.17295   | 6.36061  | 5.81234 |       |
|   | 1789-            | 5.25227 | 6.22772                        | 6.47605            | 6.04784            | 1841-            | 5.49141 | 6.21940   | 6.34389  | 5.92104 |       |
|   | 1790-            | 5.83540 | 6.13730                        | 6.33859            | 5.88165            | 1842-            | 5.73593 | 6.19644   | 6.36990  | 5.88372 |       |
|   | 1791-            | 5.35278 | 6.20496                        | 6.40721            | 5.90971            | 1843-            | 5.64686 | 6.09096   | 6.40622  | 5-84660 |       |
|   | 1792-            | 5.48646 | 6.19889                        | 6.39926            | 5.89660            | 1844-            | 5.28015 | 6.17670   | 6.33115  | 5.81234 |       |
|   | 1793-            | 5.69238 | 6.19154                        | 6.39426            | 5.86817            | 1845-            | 5.42759 | 6.15273   | 6.37911  | 5.87493 |       |
|   | 1794-            | 5.79957 | 6.26834                        | 6.38519            | 5.94804            | 1846-            | 5.63622 | , 6.15146 | 6.44794  | 5.90318 |       |
|   | 1795-            | 5.27402 | 6.17919                        | 6.39722            | 5.85965            | 1847-            | 5.53497 | 6.10969   | 6.38215  | 5.94332 |       |
|   | 1796-            | 5.73786 | 6.20254                        | 6.38923            | 5.81771            | 1848-            | 5.57215 | 6.22059   | 6.35541  | 5.84759 |       |
|   | 1797-            | 5.78321 | 6.18167                        | 6.41804            | 5.88999            | 1849-            | 5.56987 | 6.14890   | 6.35854  | 5.82976 |       |
|   | 1798-            | 5.60138 | 6.27401                        | 6.42390            | 5.91620            | 1850-            | 5.45618 | 6.21100   | 6.38923  | 5.84238 |       |
|   | 1799-            | 5.31616 | 6.12425                        | 6.34071            | 5.87155            | 1851-            | 5.61677 | 6.16416   | 6.36268  | 5.95272 |       |
|   | 1800-            | 5.32203 | 6.17420                        | 6.35333            | 5.96204            | 1852-            | 5.61459 | 6.18539   | 6,43455  | 5.80874 |       |
|   | 1801-            | 5.59249 | 6.23715                        | 6.36165            | 5.96204            | 1853-            | 5.43808 | 6.18043   | 6.39726  | 5.90482 |       |
|   | 1802-            | 5.61677 | 6.17295                        | 6.35541            | 5.69165            | 1854-            | 5.62762 | 6.22416   | 6.42875  | 5.84759 |       |
|   | 1903-            |         | 6.23598                        | 6.38923            | 5.73010            | 1855-            | 5.29531 | 6.16919   | 6.41116  | 5.84238 |       |
|   | 1804-            | 5.36504 |                                | 6.42681            | 5.74939            | 1856-            | 5.51101 | 6.15783   | 6.33328  | 5.01771 |       |
|   | 1805-            | 5.36784 | 6.18043                        | 6.39726            | 5.74748            | 1857-            | 5.61240 | 6.14890   | 6.42390  | 6.00881 |       |
|   |                  | 5.39544 | 6.09492                        |                    | 5.91134            | 1858-            | 5.67607 | 6.21461   | 6.46956  | 5.85450 |       |
|   | 1806-            | 5.54908 | 6.11368                        | 6.39526            | 2441134            | 1859-            | 5.78321 | 6.18291   | 6.38722  | 5.85105 |       |
|   |                  |         |                                |                    |                    |                  |         |           |          | 2007102 |       |

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### Table A-4 continued

#### Banic Data Series in Natural Logarithma

3.4

#### Table A-4 continued Basic Data Series in Natural Logarithms

|               |           |           |         |           | CALENDAR      |           |           |         |          |
|---------------|-----------|-----------|---------|-----------|---------------|-----------|-----------|---------|----------|
| CALENDAR      | WINTER    | SPRING    | SUMMER  | AUTUMN    | YEAR<br>1911- | WINTER    | SPRING    | SUPETER | AUTUREN  |
| 7788<br>1860- | 5.54205   | 6.15273   | 6.36061 | 5.74240   | 1911-         | 5 . 72228 | 6.14522   | 6.39024 | 5.94647  |
| 1961-         | 5.56068   | 6.13210   | 6.36372 | 5.91943   | 1912-         | 5.61459   | 6.15401   | 6.36?64 | 5.9DA09  |
| 1962-         | 5.34733   | 6.16416   | 6.31391 | 5.91458   | 1913-         | 5.74939   | 6.19767   | 6.36165 | 5.93384  |
| 1863-         | 5.75606   | 6.10668   | 6.34071 |           | 1914-         | 5.72010   | 6.22416   | 6.41411 | 5.93542  |
| 1864-         | 5.61459   |           |         | 5.96204   | 1915-         | 5.55837   | 6.15146   | 6.34177 | 5.72228  |
| 1965-         |           | 6.10836   | 6.31500 | 5.79788   | 1916-         | 5.64897   | 6.15783   | 6.32472 | 5.92746  |
|               | 5.41699   | 6.16036   | 6.38012 | 5.93225   | 1917-         | 5.63193   | 6.19032   | 6.38722 | 5.89825  |
| 1866-         | 5.61895   | 6.16542   | 6.35541 | 5.91592   | 1918-         | 5.62978   | 6.17170   | 6.36061 | 5.94504  |
| 1867-         | 5.40087   | 6.02199   | 6.32579 | 5.76079   | 1919-         | 5.62330   | 6.18291   | 6.36590 | 5.77206  |
| 1868-         | 5.62978   | 6.19767   | 6.41508 | 5.87493   | 1920-         | 5.78690   | 6.20738   | 6.36372 | 5.91458  |
| 1869          | 5.67812   | 6.15528   | 6.34909 | 5.84759   | 1921-         | 5.78321   | 6.25575   | 6.34177 | 5.89660  |
| 1870-         | 5.55141   | 6.18785   | 6.35750 | 5.77206   | 1922-         | 5.54708   | 6 . 17295 | 6.33328 | 5.85105  |
| 1971-         | 5.42495   | 6.05491   | 6.34071 | 5 +78506  | 1923-         | 5.65319   | 6.09492   | 6.34493 | 5.84412  |
| 1872-         | 5.72424   | 6.20617   | 6.38114 | 5.95272   | 1924-         | 5.47395   | 6.13730   | 6.39024 | 5.994495 |
| 1873-         | 5.75130   | 6.13210   | 6.38923 | 5.91943   | 1925-         | 5.76079   | 6.21820   | 6.39626 | 5.74172  |
| 1874-         | 5.76079   | 6.14118   | 6.35750 | 5.86136   | 1926-         | 5.60801   | 6.16919   | 6.38923 | 5.85793  |
| 1875-         | 5.36784   | 6.17045   | 6.37502 | 5.73399   | 1927-         | 5.74748   | 6.11501   | 6.41215 | 5.76456  |
| 1876-         | 5.57443   | 6.17295   | 6.37707 | 5.70844   | 1928-         | 5.64474   | 6.12687   | 6.32579 | 5.92265  |
| 1877-         | 5.45618   | 6.09357   | 6.31716 | 5.95894   | 1929-         | 5.51343   | 6.13079   | 6.35019 | 6.01323  |
| 1878- '       | 5.69036   | 6.18785   | 6.35061 | 5.89990   | 1930-         | 5.79970   | 6.24417   | 6.37502 | 5.96666  |
| 1979-         | 5.44946   | 6.14761   | 6.34621 | 5.79970   | 1931-         | 5.55606   | 6.14376   | 6.32686 | 5.90809  |
| 1890-         | 5.59238   | 6.18043   | 6.41902 | 5.70245   | 1932-         | 5.70844   | 6.16163   | 6.40026 | 5.94804  |
| 1891-         | 5.26786   | 6.11235   | 6.33541 | 5.90482   | 1933-         | 5.69642   | 6.18043   | 6.39826 | 5.87997  |
| 1982-         | 5.79970   | 6.19032   | 6.40622 | 5.81771   | 1934-         | 5.30151   | 6.24649   | 6.41508 | 6.01616  |
| 1883-         | 5.60580   | 6.18043   | 6.36784 | 5.92746   | 1935-         | 5.72031   | 6.20132   | 6.37400 | 5.98343  |
| 1994-         | 5.73523   | 6.13210   | 6,38519 | 5.85278 · | 1936-         | 5.67401   | 6.23598   | 6.39626 | 5.96204  |
| 1885-         | 5+65719   | 6.14376   | 6.32472 | 5.84064   | 1937-         | 5.65319   | 6.26606   | 6.43262 | 5.91134  |
| 1886-         | 5.59124   | 6.19767   | 6.38215 | 5.92265   | 1938-         | 5.84238   | 6.20496   | 6.43165 | 5.00544  |
| 1887-         | 5.75321   | 6.17919   | 6.37400 | 5.81949   | 1939-         | 5.79423   | 6.21940   | 6.426P1 |          |
| 1898-         | 5.33078   | 5.10301   | 6.34071 | 5.86647   | 1940-         | 5.23325   | 6.21581   | 6.36578 | 5.88959  |
| 1839-         | 5.51926   | 6.24417   | 6.33753 | 5.93225   | 1941-         | 5.33078   | 6.15401   | 6.40424 | 5.83364  |
| 1090-         | 5.77393   | 6 • 21100 | 6.35957 | 5.84759   | 1942-         | 5.03955   | 6.16289   | 6.38621 | 5.94175  |
| 1991-         | 5.64049   | 6.16036   | 6.38012 | 5.94490   | 1943-         | 5.80151   | 6.26378   | 6.37605 | 5.97889  |
| 1992-         | 5.52545   | 6.16163   | 6.35957 | 5.85105   | 1944-         | 5.71637   | 6.15528   | 6.43165 | 5.98494  |
| 1993-         | 5.35941   | 6.17170   | 6.35541 | 5.91620   | 1945-         |           | 6.20375   | 6.40721 | 5.90154  |
| 1894          | 5.91054   | 6.21581   | 6.35437 | 5.93701   | 1946-         | 5.62546   | 6.22654   | 6.40721 | 5.91458  |
| 1855-         | 5. \$3022 | 6.24978   | 6.36784 | 5.89330   | 1947-         | 5.35091   | 6.27627   | 6.44794 | 5.87155  |
| 1896-         | 5.73786   | 6.22178   | 6.39225 | 5.89164   | 1948-         | 5.66988   | 6.24533   | 6.39626 | 5.94960  |
| 1897-         | 5.56987   | 6.22297   | 6.40125 | 5.92586   | 1949-         | 5.80513   | 6.23363   | 6-41706 | 6.00439  |
| 1998-         | 5.74748   | 6.16668   | 6.35228 | 5.94804   | 1950-         | 5.69441   | 6.25229   | 6.38722 | 5.92906  |
| 1839-         | 5.59248   | 6.13340   | 6.38823 | 5.91458   | 1951-         | 5.67193   | 6.18415   | 6.40424 | 6.01908  |
| 1900-         | 5.50(14   | 6.16416   | 6.39215 | 5.92586   | 1952-         | 5.65739   | 6.20617   | 6.34071 | 5.84064  |
| 1901-         | 5.53769   | 6.22654   | 6.45079 | 5.98040   | 1953-         | 5.71241   | 6.26606   | 6.38418 | 6.02635  |
| 1902-         | 5.41020   | 6.07856   | 6.29305 | 5.80694   | 1954-         | 5.59248   | 6.20738   | 6.36784 | 5.95428  |
| 1903-         | 5.79970   | 6.18043   | 6.36165 | 5.85793   | 1955-         | 5.56299   | 6.12162   | 6.46209 | 5.88999  |
| 1904-         | 5.63835   | 6.14376   | 6.34809 | 5.84932   |               | · .       |           |         |          |
| 1905-         | 5.69642   | 6.20254   | 6.35645 | 5.87324   |               |           |           |         |          |
| 1906-         | 5.70445   | 6.22535   | 6.36061 | 5.91458   | . •           |           |           |         |          |
| 1907-         | 5.64897   | 6.13079   | 6.31282 | 5.94017   |               |           | ,         |         |          |
| 1908-         | 5.56781   | 6.14890   | 6.35333 | 5.88999   |               |           |           |         |          |
| 1909-         | 5.60359   | 6 .09357  | 6.34388 | 5.89660   |               |           |           |         |          |
| 1910-         | 5.77206   | 6.21461   | 6.34071 | 5.92426   |               |           |           |         |          |

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### Appendix B: The Econometric Framework

The econometric model is a system of equations involving a number of endogenous variables (variables determined by the model), exogenous variables (variables that affect the system but are not affected by it) and random shocks (variables that are unobserved and uncorrelated with either the exogenous or the endogenous variables). The idea is to use historical aggregate data to estimate the model. The linear econometric model should be viewed as an unrestricted linear specification of a (or several) structural model(s).

Let  $Y_t$  be an n x l vector of endogenous variables such as the birth rate, the mortality rate etc., and let  $X_t$  be an m x l vector of exogenous variables such as precipitation and temperature. If we subtract from  $Y_t$ and  $X_t$  the deterministic parts, such as the level (constant) and the trend, then we may define the vector  $Z_t = [y_t, x_t]'$ , where  $y_t$  and  $x_t$  are the nondeterministic parts of  $Y_t$  and  $X_t$ , respectively. We can regard the vector of time observations,  $Z_t$ , as a time series stochastic process, that is  $[Z_t]_{t=0}^{\infty}$  is a set of random vectors indexed by time together with a joint distribution functions for the Z's. In particular, past observations may be correlated with current observations of  $Z_t$ .  $Z_t$  is a  $t \ge 1$  (t = n + m) vector. In general, the econometric model can be written as

- (B.1)  $y_t = A_{11}y_{t-1} + A_{12}y_{t-2} + \dots + A_{1g}y_{t-g} + A_{20}x_t + A_{21}x_{t-1} + \dots + A_{2g}x_{t-g} + \epsilon_t$
- (B.2)  $x_t = A_{41}x_{t-1} + A_{42}x_{t-2} + \cdots + A_{4g}x_{t-g} + v_t$

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Here  $\varepsilon_t$  and  $v_t$  are (n x 1) and (m x 1) vectors, respectively, of random disturbances. The matrix  $A_{1j}$  is  $(\ell \times \ell)$ ;  $A_{2j}$  is  $(\ell \times m)$ ;  $A_{4j}$  is (m x m). The disturbance processes of  $\varepsilon_t$  and  $v_t$  are assumed to be serially and contemporaneously uncorrelated with  $E(\varepsilon_t) = E(v_t) = 0$ ,  $E(v_t \varepsilon_t') = E(v_t v') =$  $E(\varepsilon_t \varepsilon_s') = 0$  for all  $t \neq s$ ,  $E(v_t v_t') = \Sigma_v$  and  $E(\varepsilon_t \varepsilon_t') = \Sigma_\varepsilon$ . The definition of the exogenous variables  $x_t$  is that they are uncorrelated with the  $\varepsilon$ 's at all lags, that is  $E(\varepsilon_t x_g') = 0$  for all t and s. The above specification completely describes the first and the second moments of the  $Z_t = [v_t, x_t]'$ process. The equivalence of lags, g, across all variables and equations is assumed for convenience. By the above assumptions  $x_t$  is a strictly exogenous vector of variables.<sup>1</sup>

The model (B.1) and (B.2) can be written as a vector autoregression (VAR) for  $Z_{\perp}$ 

(B.3) 
$$A(L)Z_t = U_t$$
  $U_t = (\varepsilon_{t+1}V_t)'$ 

Where  $A(L) = A \cdot_0 - A \cdot_1 L - A \cdot_2 L^2 - \dots - A \cdot_g L^g$  and  $A \cdot_j$  is an  $(l \times l)$  matrix,  $j=0,\ldots g$ . Given the above assumptions on the error term  $(U_L)$  and the equal lag structure across the model, ordinary least squares (OLS) for each equation turns out to be identical with joint conditional maximum likelihood even for un restricted variance covariance matrices  $\Sigma_u$  and  $\Sigma_c$ .<sup>2</sup> Furthermore, given the strict exogeneity assumption with respect to the x's, we can set the lag structure and estimate (B.1) independently of (B.2). The lag length of the VAR (or B.1)) is initially unspecified, and may be determined using an asymptotic  $\chi^2$  test for alternative lag lengths fitted to the model. An increase of lag increases the number of parameters by  $(n+m)^2$ 

<sup>1</sup>Strict exogeneity is defined in Sims (1972) and implies that the vector of all observations on  $x_t(x_1, x_2, \dots, x_T)$  is orthogonal to the error in the regression equation for  $x_t$ .

<sup>2</sup>This is a special case of Zellner's seemingly unrelated regression method.

(or (n + m)xn). Therefore, we must restrict the number of lags subject to the number of observations and variables, in order to apply statistical tests.

Observe that (B.1) and (B.2) imply that the typical A.  $j_{j-matrix is}$ (B.3) can be written as

(B.4) 
$$A_{j} = \begin{cases} A_{1j} & A_{2j} \\ (n \times n) & (n \times m) \\ A_{3j} & A_{4j} \\ (m \times n) & (m \times m) \end{cases}$$
 for  $j = 0, \dots, g$ 

and we assume that  $A_{2j} = 0$   $V_j \ge 0$ ,  $A_{10} = I_m$  and  $A_{40} = I_n$ . The assumption that  $A_{3j} = 0$  is equivalent to assuming that  $y_t$  does not cause  $x_t$  in the sense define by Granger (1969), which is a necessary condition for  $x_t$  to be exogenous (see Sims, 1972). F-tests of this assumption can be applied to the set of equations (B.2). Given that we assume that  $E(v_t \varepsilon_t^*) = 0$ , it follows from a theorem in Sims (1972) that  $x_t$  is strictly exogenous in (B.1). Sims' exogeneity test can be applied by inserting lead variables of  $x_t$  in (B.1) and statistically evaluating whether the coefficients are zero. The above tests evaluate the specification of the econometric model. The x's in our model are weather variables that are undoubtedly exogenous. Hence, the exogeneity tests should be viewed as indicating omitted variables. If an important omitted variable is correlated both with the x's and the y's, the exogeneity test could fail, because the assumption that  $E(v_t \varepsilon_t^*) = 0$  is violated.

Once the A's in (B.3) are estimated, we can express  $Z_t$  as a linear combination of current and past innovations (U's), in other words, as a distributed lag on  $U_t$ . Then we can write the Wold moving average representation

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(MAR) for Z<sub>t</sub> as

$$(B.5) \qquad \qquad Z_t = \sum_{s=0}^{\infty} B_s U_{t-s}$$

where  $B_s$  is an  $(l \times l)$  matrix of parameters and we use a partition of the B's that is equivalent to that of the A's. Observe that the B's are written as independent of t, which is the result of the A's in (B.3) being independent of t.

A useful way to describe the economic system during the sample period is by looking at the system's response to random shocks.<sup>3</sup> Except for scaling, this is equivalent to tracing out the system's MAR by matrix polynomial long division. In order to see that, we can rewrite the MAR as

$$z_{t} = [A(L)]^{-1}U_{t}$$

Therefore,

$$\sum_{s=0}^{\infty} B_{s}L^{s} = [\Lambda(L)]^{-1}$$

i.e., finding the  $B_{g}$  coefficients is equivalent to inverting the matrix polynomial. Suppose we simulate the VAR of Z by setting for a particular equation j,  $U_{jt} = 1$  and  $U_{it+s} = 0$  for all  $i \neq j$  and s = 0, 1, 2, 3, ...,together with the initial conditions  $Z_{t-r} = 0$  for r = 0, 1, 2, ..., g, . This procedure generates infinite  $Z_{t+s}$  vectors for s = 0, 1, 2, ..., which are equal to the j'th column of the corresponding  $B_{s}$  matrix. <sup>4</sup> Hence, the inversion of the matrix polynomial A(L) is equivalent to the above simulation. <sup>3</sup>This was suggested and implemented by Sims (1980).

For example, take the VAR  $Z_t = aZ_{t-1} + U_t$ , where |a| < 1. Set  $Z_{t-1} = 0$ ,  $U_t = 1$  and  $U_{t+r} = 0$  for all r > 0. Then  $Z_{t+s} = a^s$ , where it is easy to see that

$$z = \sum_{s=0}^{\infty} a^{s} U_{t-s}$$

One can regard the i, j'th component of  $B_s$ ,  $b_{ij}(s)$  as the "average" response, s periods ahead, of the i'th variable, to an initial shock in the j'th variable. However, the components of U may be contemporaneously correlated and the above simulation does not take this possibility into account. In describing and summarizing the data using the above simulation we ignore the effect of a shock in one variable on the current observation of other variables if  $\sum_{V}$  and  $\sum_{E}$  are not diagonal. In what follows we explain one way to take into account the contemporaneous correlation between the U's.

Since it is not possible to partition the variance of Z into pieces accounted for by each innovation, it is appealing to apply an orthogonalization transformation for U, to obtain  $e_t = TU_t$ , where T is a matrix chosen to make the variance-covariance matrix of  $e_t$  the identity matrix. There are many ways one could choose T. Choosing T's of triangular form preserves the connection of the elements of e with the corresponding variables in Z in the sense that, if T is lower triangular,  ${}^5 e_{jt}$  is the normalized error in forecasting  $Z_{i,t}$  for i < j. We can rewrite (B.5) as

$$(B.6) \qquad \qquad Z_t = \sum_{s=0}^{\infty} B_s e_{t-s}$$

A lower triangular matrix has zero elements in the right hand side (above the diagonal elements) of the matrix.

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Now the interpretation above for the components of the MAR can be applied to the components of the matrix function  $B_s T^{-1}$ , since the elements of  $\varepsilon$  are uncorrelated. In particular, the sum of squares from s = 0 to s = k of the i, j'th component of  $B_s T^{-1}$  represents the part of error variance in the k + 1 (step-ahead) forecast of  $Z_i$  which is accounted for by the innovation in  $Z_i$  at s = 0.

Applying this type of orthogonalization is equivalent to restricting the system such that a "shock" in  $Z_1$  has a contemporaneous effect on all n + m - 1 variables,  $Z_2$  on all n + m - 2 variables,..., and  $Z_{n+m}$  only on itself. Hence, each triangularization imposes a particular block recursive system with respect to the contemporaneous relations among the variables. It is important to test this procedure by changing the ordering of the variables, to see whether there are important changes in the results. Note that in our model the following assumption

$$E[U_{t}U_{t}^{\dagger}] = \begin{bmatrix} \Sigma_{v} & 0 \\ 0 & \Sigma_{\varepsilon} \end{bmatrix} = \Sigma$$

has been imposed and all the discussion is with respect to the correlation in  $\Sigma_v$  and  $\Sigma_c$ . We report results that assume that both  $\Sigma_v$  and  $\Sigma_c$  are diagonal. We review the results of other assumptions with respect to orthogonolizations of the covariance matrix. When significant differences are observed, they are noted in the text.

Once the A's in the VAR has been estimated, the matrix  $B_s T^{-1}$  for s = 0, 1, a, ..., k, ... can be computed. Letting the i, j'th component,  $\tilde{b}_{ij}(s)$ , of  $\tilde{B}_s T^{-1}$ , be the response of  $Z_i$  to an innovation or exogenous shock of one standard deviation in  $Z_i$ , then

$$\rho_{ij}^{2}(k) = \frac{\sum_{s=0}^{k} \tilde{b}_{ij}^{2}(s)}{\sum_{s=0}^{m+n} k \tilde{b}_{ij}^{2}(s)}$$

is the proportion of forecast error variance in  $Z_i$ , k periods ahead, produced by an innovation in  $Z_j$ . The vector of  $\rho \cdot {2 \atop j}^2$  (k) for large k is called the variance decomposition of the variable  $Z_i$ . Under the condition that  $\Sigma$  is time invariant, stationarity of the VAR is equivalent to the condition that

$$\lim_{s\to\infty} b_{ij}(s) = 0, \quad \text{for all i and j.}$$

Under that condition,  $\rho_{ij}^2(k) \xrightarrow[k \to \infty]{} \rho_{ij}^2$ , and  $\rho_{ij}^2$  is the overall variance proportion of  $Z_i$  due to a one standard deviation shock in  $Z_i$ .<sup>6</sup>

The main objective of the estimation is to produce values of the A's that seem consistent with a theoretical model. The A's in the VAR are assumed to be related to the objective functions of people as well as to the parameters of given technical relationships and constraints imposed by the exogenous variables. Without an explicit model that gives rise to equations such as are represented in the VAR, we cannot say anything about the underlying economic system by looking merely at the magnitude of the coefficients of the A's.

6

The condition that  $\lim_{s\to\infty} b_{ij}(s) = 0$  for all i, j, is equivalent to the  $\lambda$ 's that solve  $|\Lambda(\lambda)| = 0$  being outside the unit circle. If this condition is violated in the estimated equations the interpretation of the variance decomposition of  $Z_i$  may be misleading. The VAR permits us to test formally the hypothesis of significant change in the parameters of the demographic variables equations during the second half of the last century. We test structural change by splitting the sample period into two parts at the time when the structural change is hypothesized to have occurred. Then we test whether there is a significant difference in parameters between the two parts of the sample. The test statistic is a modified likelihood ratio statistic, and it is distributed asymptotically as  $\chi^2$ . We estimate the deterministic part, constant and trend, of the model jointly with the autoregressive part and test whether the trends (calendar time and its square) in our case are jointly statistically different from zero in each equation.

Using the information gleaned from tests of Granger causality (1969), from the variance decomposition, and from tests of structural change, we construct a VAR with zero restrictions on the A's and Z. These zero restrictions are jointly tested system-wide and equation by equation. The dynamics of the restricted model are summarized by the MAR of the restricted VAR.

## Appendix C

## Table C.1

| Test of<br>lag length | log   V <sub>u</sub>  <br>(1) | 10g V <sub>R</sub>  <br>(2) | $(195-58)[(2)-(1)] = \chi^{2}$<br>(3) | d.f<br>(4) | Marginal<br>Significance<br>Level<br>(5) |
|-----------------------|-------------------------------|-----------------------------|---------------------------------------|------------|--|
| 5 VS-4                | -25.00                        | -24.60                      | 54.8                                  | 50         | .30                                      |
| 5 VB 3                | -25.00                        | -24.08                      | 126                                   | 100        | .01                                      |
| 5 <b>vs</b> 2         | -25.00                        | -23.62                      | 190                                   | 150        | .01                                      |
|                       |                               |                             |                                       |            |  |

Test of Lag Length of the Subsystem of Endogenous Variables<sup>a</sup>

<sup>a</sup>There are 195 observations and 58 variables in each unrestricted equation with 5 lags.  $V_U$  and  $V_R$  correspond to the 5x5 matrices of the estimated variance-co-variance of the innovations of the unrestricted and the restricted systems, respectively.

| •                        | Test of<br>lag length | 10g   V <sub>R</sub> | 1ikelihood<br>X <sup>2</sup><br>X <sup>1</sup> | ratio = $\chi^{2*}$<br>$\chi^2_2$ | d.f.                  |                                  | ificance<br>for x <sup>2</sup> 2 |
|--------------------------|-----------------------|----------------------|--|-----------------------------------|-----------------------|----------------------------------|----------------------------------|
|                          | 5 <b>vs</b> 4         | -25.11               | 57.65  | 123.17                            | 50                    | .21                              | •0                               |
|                          | 5 vs 3                | -24.33               | 97.36  | 207.3                             | 100                   | . 55                             | .0                               |
|                          | 5 vs 2                | -23.60               | 134.67   | 287.8                             | 150                   | .81                              | .0                               |
|                          | 5 vs 1                | -22.95               | 167.84   | 358.7                             | 200                   | .94                              | •0                               |
| Sims (1980)<br>modified: | $x_1^2 = (T - 1)$     |                      |  | where k is th                     | ne number<br>equation | of explanatory<br>of the unrestr |                                  |

| Table C. | .2 |
|----------|----|
|----------|----|

Tests of Lag Length: Period I

Conventional:  $\chi_2^2 = T[\log |V_R| - \log |V_U|]$ 

 $\chi_1^2$  is the modified likelihood ratio test

statistic

 $\log |V_{ij}| = -26.24$ 

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| Tab | le | С | • | 3 |  |
|-----|----|---|---|---|--|
|     |    |   |   |   |  |

| The Exog | enous Var | iables | Equations | : | 1756-1869 |
|----------|-----------|--------|-----------|---|-----------|
|----------|-----------|--------|-----------|---|-----------|

|                |        | Depende      | nt Variabl | .es    |      |
|----------------|--------|--------------|------------|--------|------|
|                | WNTEMP | SPTEMP       | SUTEMP     | AUTEMP | RAIN |
| Constant       | 5.64   | 4.13         | 4.71       | 5.39   | 4.34 |
| Lag 1          | .058   | 008          | .148       | .061   | .219 |
| Lag 2          | 005    | .139         | 046        | .053   | 070  |
| Lag 3          | 010    | .064         | .183       | 096    | .071 |
| Lag 4          | 010    | .137         | 023        | .063   | .076 |
| R <sup>2</sup> | .007   | .049         | .053       | .019   | .062 |
| Significance   |        |              |            |        |      |
| Level          | .617   | <b>.9</b> 60 | .975       | .985   | .935 |

| Table | C.4* |
|-------|------|
|-------|------|

The Variance-Covariance (Correlation) of the Residuals of the Equations

|        | CBR    | IDR     | NIDR                | CROP         | RWAGE      | WNTEMP              | SPTEMP              | SUTEMP              | AUTEMP              | RAIN   |
|--------|--------|---------|---------------------|--------------|------------|---------------------|---------------------|---------------------|---------------------|--------|
| CBR    | .77(1) | 50      | -1.1                | 87           | .18        | 0                   | 0                   | 0                   | 0                   | 0      |
| IDR    | (31)   | •33 (1) | .39                 | .25          | 11         | 0                   | 0                   | 0                   | 0                   | 0      |
| NIDR   | (42)   | (.73)   | • <sup>89</sup> (1) | .25          | 09         | 0                   | 0                   | 0                   | 0                   | 0      |
| CROP   | (65)   | (.09)   | (.05)               | .23          | .01        | 0                   | 0                   | 0                   | 0                   | 0      |
| RHAGE  | (.07)  | (21)    | (10)                | (1)<br>(.39) | •009 (1)   | 0                   | 0                   | n                   | 0                   | 0      |
| WNTEMP | (0)    | (0)     | (0)                 | (0)          | (0)        | • <sup>27</sup> (1) | .15                 | .07                 | .11                 | 13     |
| SPTEMP | (0)    | (0)     | (0)                 | (0)          | <b>(0)</b> | (.21)               | • <sup>19</sup> (1) | .05                 | .03                 | .02    |
| SUTEMP | (0)    | (0)     | (0)                 | (0)          | (0)        | (.11)               | (.35)               | • <sup>13</sup> (1) | •03                 | 10     |
| AUTEMP | (0)    | (0)     | (0)                 | (0)          | (0)        | (.09)               | (.10)               | (.13)               | • <sup>49</sup> (1) | •02    |
| PAIN   | (0)    | (0)     | (0)                 | (0)          | (0)        | (+.06)              | (.04)               | (20)                | (.025)              | .019(1 |

\* The upper triangular component of the matrix shows the residual variance-covariance terms while the lower triangular component shows the residual correlations.

## Table C.5

## F-Test for Exclusion of Weather Variables

|       | ويتباعث والترجيب فيستنب والمترجا |        |        |        | -     |
|-------|----------------------------------|--------|--------|--------|-------|
|       | WNTEMP                           | SPTEMP | SUTEMP | AUTEMP | APREC |
| CBR   | •007                             | .92    | •28    | .10    | .30   |
| IDR   | •008                             | •64    | •65    | .18    | .80   |
| NIDR  | •006                             | .77    | •66    | .20    | .60   |
| CROP  | .61                              | •94    | •80    | •03    | .41   |
| RWAGE | .40                              | • 54   | .10    | •57    | .10   |
|       |                                  |        |        |        |       |

## from Endogenous Variables Equations

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## TABLE C.6

Two Block Recursive Orthogonalizations or Temporal Orderings of Model Decomposition of Variance: Percentage of Forecast Error Variance 25 Years Ahead Produced by Each Innovation

| ponse in    | CBR              | IDR             | NIDR     | CROP        | RWAGE         | WNTEMP       | SPTEMP       | SUTEMP      | AUTEMP | RAI       |
|-------------|------------------|-----------------|----------|-------------|---------------|--------------|--------------|-------------|--------|-----------|
| CBR         | 28               | 1               | 1        | 6           | 13            | 15           | 17           | 3           | 9      | 6         |
| IDR         | 7                | 41              | 1        | 3           | 4             | 17           | 3            | 8           | 9      | 5         |
| NIDR        | 9                | 14              | 16       | 8           | 5             | 25           | 7            | 6           | 6      | 5         |
| CROP        | 7                | 1               | 1        | 46          | 9             | 9            | 9            | 4           | 9      | 5         |
| RWAGE       | 5                | 2               | 2        | 8           | 31            | 11           | 4            | 4           | 18     | 14        |
|             | <br>             |                 |          |             |               | <u></u>      |              |             |        |           |
|             | CBR              | NIDR            | IDR      | RWAGE       | CROP          | WNTEMP       | SPTEMP       | SUTEMP      | AUTEMP | RAII      |
| CBR         | <u>CBR</u><br>27 |                 | IDR<br>1 | RWAGE<br>16 | CROP<br>3     | WNTEMP<br>14 | SPTEMP<br>17 | SUTEMP<br>3 |        | RAII<br>6 |
| CBR<br>NIDR | <br>             | NIDR            |          |             |               | <b>`</b>     |              |             |        |           |
|             | 27               | NIDR<br>2       | 1        | 16          | 3             | 14           | 17           | 3           | 9      | 6         |
| NIDR        | 27<br>9          | NIDR<br>2<br>28 | 1<br>2   | 16<br>7     | <b>3</b><br>6 | 14<br>25     | 17<br>7      | 3<br>6      | 9<br>6 | 6         |

\* The triangularized innovation is according to the order of variables.

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