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An experimental analysis and optimization of machining rate and surface characteristics in WEDM of Monel-400 using RSM and desirability approach

Vinod Kumar · Vikas Kumar · Kamal Kumar Jangra

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Abstract In the present work, an experimental investigation on wire electrical discharge machining (WEDM) of Monel-400 has been presented. Monel-400 is a nickel-copper-based alloy, mostly employed in ships and corrosion-resisting applications. Four input WEDM parameters namely discharge current (I_p), pulse-on time (T_{on}), pulse-off time (T_{off}) and servo voltage (SV) have been investigated and modeled for two performance characteristics namely machining rate (MR) and surface roughness (SR). Effect of WEDM parameters has been discussed using response surface graphs. Using analysis of variance, quadratic model is found significant for MR while two factors interaction (2FI) model has been suggested for SR. To optimize multi-performance characteristics, desirability function has been employed. Corresponding to highest desirability, the optimal combination of discharge parameters is I_p : 103 A; T_{on} : 113 μ s; T_{off} : 37 μ s and SV: 50 V. The effect of discharge energy on surface morphology has also been examined. High discharge energy increases the extent of surface damage and results in large size and overlapped craters on machined surface. Low discharge energy and high value of T_{off} result in minimum defects on machined surface. Trim cutting operations were

performed at low discharge energy using different wire offset values. Result shows that surface finish can be improved significantly after a single trim cut irrespective of high discharge energy in rough cut.

Keywords Wire electrical discharge machining (WEDM) · Monel-400 · Response surface methodology (RSM) · Machining rate · Surface characteristics · Process optimization · Trim cutting operation

Introduction

Monel-400 is a solid solution of nickel and copper, having high strength and toughness over a wide temperature range. Because of its high resistance to corrosive and most acidic environment, Monel has been widely used in chemical industries, food processing industry, heat exchanger tubing, nuclear reactors, sub-marine and ship propellers, etc. (Shoemaker and Smith 2006).

Surface integrity of a machined component significantly affects its performance such as fatigue life, creep and corrosion. Surface integrity of a machined component may include residual stresses, recast layer, heat-affected zone and microcracks (Klink et al. 2011). In past, several investigations have been carried out for machining performance of nickel-based alloys except Monel, with conventional and non-conventional machining processes. Due to high heat-resisting capacity, nickel-based alloys are very difficult to machine with conventional machining processes such as milling, turning and drilling (Wei 2002; Sharman et al. 2006; Krain et al. 2007; Soo et al. 2011; Hood et al. 2011; Antar et al. 2011). Machining of nickel alloys using conventional cutting tools results in the formation of built-up edge on tool face and high tendency of

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welding to the tool, resulting in large crater wear and poor surface integrity involving several surface defects such as surface drag, material pull-out/cracking and tearing surface. (Ulutan and Ozel 2011; Kortabarria et al. 2011; Herbert et al. 2012).

Wire electrical discharge machining (WEDM) can be proved more economic and efficient for machining complex and intricate profiles in high strength and high heat-resisting materials. In WEDM, material is removed by melting and vaporization through high localized heat generation by repetitive sparks occurring between conductive work material and wire electrode separated by dielectric fluid which carries away the eroded particles. In past, some investigations have been carried out on machining of nickel alloys with EDM or WEDM. But most of earlier investigations evaluated the machining of Inconel grade of nickel alloys (In-718, In-601 etc.). Kang and Kim (2003) investigated the EDM characteristics of nickel-based heat resistance alloy Hastelloy-X. Pulse-on time was the main factor that affect the surface integrity of the work material. Hewidy et al. (2005) correlated the various WEDM parameters such as peak current, duty factor, wire tension, and water pressure with the performance outputs namely metal removal rate (MRR), wear ratio and surface roughness in WEDM of Inconel 601. Liu et al. (2005) investigated the significant machine parameters which are affecting the characteristics of microholes in nickel alloy in terms of microhole expansion, electrode depletion and material removal rate. A proper discharge current is very important to achieve optimum results. Aspinwall et al. (2008) presented roughing and finishing strategies for machining of Ti-6Al-4 V and Inconel 718 on WEDM. The average recast layer thickness less than 11 μm was found in rough cut and after trim passes apparently no recast layer was obtained.

Previous investigations show that the discharge current and pulse-on time are the most important parameters in WEDM that significantly affect the material removal rate and surface characteristics of the machined component (Shivade and Shinde 2014). To obtain high material removal rate, high discharge energy is required which results in high heat generation across the work material and wire electrode. But high heat generation results in poorer surface integrity including large recast layer, heat-affected zone and several microcracks (Klink et al. 2011; Rebelo et al. 1998). The main cause of poor surface integrity is due to either re-solidification of melted materials on the machined surface or generation of high-pressure energy in plasma channel across the electrodes (Li et al. 2013). Using trim cuts, damaged surface layer can be removed and surface integrity can be improved significantly (Jangra 2012, 2014; Sakar et al. 2008; Sanchez et al. 2007).

In the present work, machining performance of Monel-400 has been evaluated on WEDM. Four important parameters have been investigated and modeled for machining rate (MR) and surface roughness (SR) using response surface methodology (RSM). RSM is the most used statistical technique for determining the relationship between various input parameters and output responses (Hewidy et al. 2005; Myers and Montgomery 1995; Jangra and Grover 2012). Using face-centered central composite design, experimental data were obtained to develop mathematical models for input variables and output machining characteristics. Influence of discharge energy on surface morphology has been compared using micrograph of machined surface and microhardness profiles. After modeling the machining characteristics in rough cutting operation, trim cutting operations have been performed at low discharge energy and different wire offset values to examine the effect of trim cut on final surface finish of the work material.

Experimentation

In the present work, experiments were performed on 5-axis sprint cut (ELPULSE-40) wire EDM manufactured by Electronica M/C Tool LTD India. Monel-400, a nickel-based alloy containing 63 % Ni, 33 % Cu, 2.13 % Fe, and 1 % Mn, hot forged in rectangular sheet of 12.5 mm thickness, has been selected as workpiece material. Using WEDM, work material was machined and samples were obtained in the form of rectangular punch of dimension 5 mm \times 6 mm \times 12.5 mm.

In rough cutting operation, only discharge parameters namely discharge current (I_p), pulse-on time (T_{on}), pulse-off time (T_{off}) and servo voltage (SV) have been selected as variable parameters while parameters under the category of wire electrode and dielectric conditions have been assigned a constant value. Zinc-coated brass wire having a fixed diameter of 0.25 mm has been selected as wire electrode. In WEDM, wire feed rate should be kept at low value to minimize the machining cost. Therefore, a constant value of 5 m/min has been assigned to wire feed rate with adequate value of 10 N of wire tension. Experiments for rough cutting operation were conducted at zero wire offset value. Distilled water having conductivity 20 mho has been utilized in the present study. High flow rate of dielectric results in complete and quick flushing of the melted debris out of the spark gap which results in high machining rate and good surface finish. Therefore, dielectric flow rate was kept at high value of 12 liters per minute (LM^{-1}). Range and levels of four variable parameters have been listed in Table 1.



Table 1 Variable parameters and their levels

Symbol	Parameter	Units	Levels		
			Low (−1)	Middle (0)	High (+1)
A	Discharge current (Ip)	A	90	120	150
B	Pulse-on time (Ton)	μs	106	112	118
C	Pulse-off time (Toff)	μs	35	40	45
D	Servo voltage (SV)	V	30	40	50

MR was measured in mm/min which was observed directly from machine tool monitor screen. SR value (in μm) was measured in terms of mean absolute deviation (Ra) using the digital surface tester Mitutoyo 201P. SEM images were obtained through SEM equipment (JSM-6610 LV) manufactured by JEOL USA Inc, USA.

Results and discussions

Response surface methodology (RSM) is a collection of mathematical and experimental techniques that requires sufficient number of experimental data to analyze the problem and to develop mathematical models for several input variables and output performance characteristics (Myers and Montgomery 1995; Kansal et al. 2005). Using the design of experiments and applying regression analysis, the modeling of the desired response (Y) to several independent input variables (x_i) can be gained. In RSM, the quantitative form of relationship between desired response and independent input variables could be represented as:

$$Y = \Phi(x_1, x_2, \dots, x_k) \pm e_r \quad (1)$$

The function Φ is called response surface or response function. The residual e_r measures the experimental errors (Cochran and Cox 1962).

By applying the RSM, the dependent variable is viewed as a surface to which a mathematical model is fitted. For the development of regression equations related to various performance characteristics of WEDM process, the second-order response surface has been assumed as:

$$Y = b_0 + \sum_{i=1}^k b_i X_i + \sum_{i=1}^k b_{ii} X_i^2 + \sum_{i < j=2}^2 b_{ij} X_i X_j \pm e_r \quad (2)$$

This assumed surface Y contains linear, squared and cross-product terms of variables X_i 's. The model parameters can be estimated most effectively if proper experimental designs are used to collect the data.

In the present study, four numerical variables are set at three levels. Therefore, a standard second-order experimental design called face-centered central composite design (CCD) has been adopted for analyzing and

modeling the WEDM parameters for MR and SR. This design consists of full factorial having 30 runs including 6 central points. The center points, as implied by the name, all levels set to the midpoint of each parameter range. Based on the experimental layout shown in Table 2, the experiments were performed and two machining characteristics were measured.

The regression equation for output machining characteristics (MR and SR) and input parameters can be obtained using generalized Eq. (2) and experimental data in Table 2. But in the present case, design expert (DX-7), a statistical tool is used to generate the regression equation for MR in coded and actual terms as given in Eqs. 3 and 4. Analysis of variance (ANOVA) has been performed on the experimental data to test the goodness of fit of the model. This includes the test for significance of the regression model, test for significance on model coefficients and test for lack-of-fit model adequacy.

Analysis of machining rate (MR)

Fit summary for MR, after backward elimination process, has been listed in Table 3. Using backward elimination process, insignificant terms (p value > 0.05) have been eliminated from the reduced quadratic model. Table 3 shows that p value for quadratic model is significant which shows that the terms in the model have significant effect on output response. In the present case, the value of R^2 and R^2 (adj.), called coefficient of determination, is over 99 %. When R^2 approaches unity, the better the response model fits the actual data. Also, test of 'lack of fit' shows insignificant effect, which is desirable for selecting the models (Kansal et al. 2005). Figure 1 shows that the residuals are normally distributed about a straight line which means that the errors are normally distributed. The final response equation for MR is given as follows:

In coded terms:

$$\begin{aligned} \text{MR} = & 2.50 + 0.11A + 0.72B - 0.19C - 0.16D \\ & - 0.12(A)^2 - 0.36(B)^2 - 0.078(C)^2 + 0.057(D)^2 \\ & + 0.031A \times B + 0.046B \times C. \end{aligned} \quad (3)$$



Table 2 Test conditions in face-centered central composite design for four parameters

Trial no.	Ip (A)	Coded value	Ton (μs)	Coded value	Toff (μs)	Coded value	SV (V)	Coded value	MR (mm/min)	SR (μm)
1	90	−1	106	−1	35	−1	30	−1	1.60	1.33
2	150	1	106	−1	35	−1	30	−1	1.78	1.69
3	90	−1	118	1	35	−1	30	−1	2.86	2.21
4	150	1	118	1	35	−1	30	−1	3.16	2.60
5	90	−1	106	−1	45	1	30	−1	1.12	1.11
6	150	1	106	−1	45	1	30	−1	1.30	1.20
7	90	−1	118	1	45	1	30	−1	2.60	1.98
8	150	1	118	1	45	1	30	−1	2.89	2.20
9	90	−1	106	−1	35	−1	50	1	1.28	1.12
10	150	1	106	−1	35	−1	50	1	1.39	1.33
11	90	−1	118	1	35	−1	50	1	2.57	1.78
12	150	1	118	1	35	−1	50	1	2.88	2.16
13	90	−1	106	−1	45	1	50	1	0.79	0.98
14	150	1	106	−1	45	1	50	1	0.97	1.14
15	90	−1	118	1	45	1	50	1	2.30	1.68
16	150	1	118	1	45	1	50	1	2.54	1.93
17	90	−1	112	0	40	0	40	0	2.29	1.54
18	150	1	112	0	40	0	40	0	2.46	1.81
19	120	0	106	−1	40	0	40	0	1.40	1.20
20	120	0	118	1	40	0	40	0	2.86	2.11
21	120	0	112	0	35	−1	40	0	2.64	1.79
22	120	0	112	0	45	1	40	0	2.19	1.55
23	120	0	112	0	40	0	30	−1	2.73	1.83
24	120	0	112	0	40	0	50	1	2.37	1.52
25	120	0	112	0	40	0	40	0	2.50	1.64
26	120	0	112	0	40	0	40	0	2.51	1.68
27	120	0	112	0	40	0	40	0	2.50	1.69
28	120	0	112	0	40	0	40	0	2.53	1.67
29	120	0	112	0	40	0	40	0	2.54	1.68
30	120	0	112	0	40	0	40	0	2.51	1.69

In actual terms:

$$\begin{aligned}
 \text{MR} = & -132.79107 + 0.016153 \text{ Ip} + 2.30068 \text{ Ton} \\
 & - 0.042170 \text{ Toff} - 0.061652 \text{ SV} - 1.31579\text{E} \\
 & - 004 (\text{Ip})^2 - 0.010095(\text{Ton})^2 - 3.13684\text{E} \\
 & - 003\text{Toff}^2 + 5.65789\text{E} - 004\text{SV}^2 + 1.70139\text{E} \\
 & - 004 \text{ Ip} \times \text{Ton} + 1.52083\text{E} - 003\text{Ton} \times \text{Toff}.
 \end{aligned}
 \quad (4)$$

Effect of WEDM parameters on MR

To analyze the effect of WEDM parameters on MR, response surface graphs have been plotted as shown in Fig. 2a–c. Response surface graph shows that the machining rate increases with increasing value of Ton and Ip. Effect

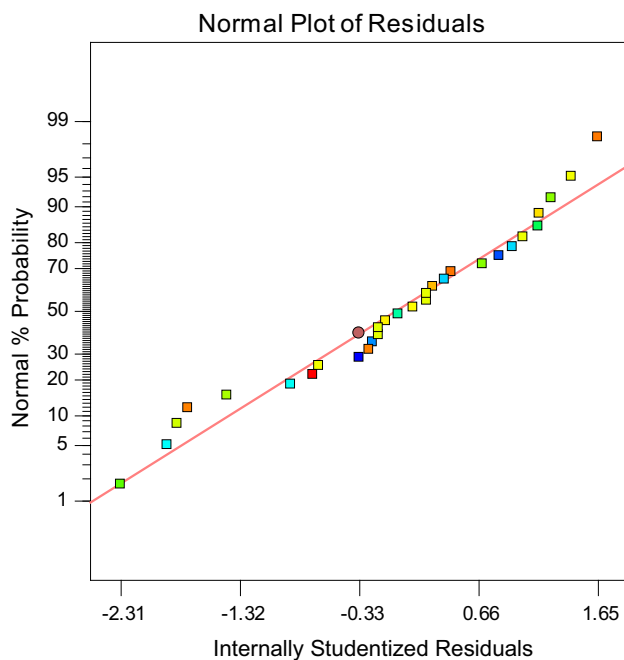
of pulse-on time is highly significant as compared to discharge current. Increasing Ip and Ton increases the discharge energy across the electrode and hence results in high melting and evaporation of material. High melting and evaporation combined with high dielectric supply result in high machining rate (Jangra and Grover 2012). Machining rate decreases with increase in value of Toff from 35 to 45 μs as shown in Fig. 2b, c. Increasing pulse-off time decreases the effective discharge frequency and hence decreases the discharge energy across the electrodes resulting in low machining rate.

Servo voltage (SV) controls the discharge gap across the wire electrode and work surface. Decreasing servo voltage results in narrow spark gap which results in large ionization of spark gap and hence more melting of work material, as a result machining rate increases as shown in Fig. 2c. Highest machining rate is obtained corresponding to Ton: 118 μs; Ip:



Table 3 ANOVA table for fitted model for MR

Source	Sum of squares	Degree of freedom	Mean square	<i>F</i> value	<i>p</i> value	
Model	12.47	10	1.25	1797.41	<0.0001	Significant
A	0.21	1	0.21	307.56	<0.0001	
B	9.43	1	9.43	13592.64	<0.0001	
C	0.67	1	0.67	958.44	<0.0001	
D	0.48	1	0.48	696.72	<0.0001	
A ²	0.036	1	0.036	52.36	<0.0001	
B ²	0.34	1	0.34	493.13	<0.0001	
C ²	0.016	1	0.016	22.96	<0.0001	
D ²	8.29E–003	1	8.294E–003	11.95	0.0026	
AB	0.015	1	0.015	21.63	0.0002	
BC	0.033	1	0.033	48.00	<0.0001	
Residual	0.013	19	6.939E–004			
Lack of fit	0.012	14	8.453E–004	3.13	0.1069	Not significant
Pure error	1.350E–003	5	2.700E–004			
Cor total	12.49	29				
Standard deviation = 0.026		$R^2 = 0.9989$	R^2 (Adj.) = 0.9984			

**Fig. 1** Residuals plot for MR

150 A; Toff: 35 μ s; SV: 30 V. Increasing the value of Ton, Ip and decreasing Toff and SV beyond these limits, discharge energy increases enough to cause wire breakage.

Analysis of surface roughness (SR)

Fit summary for surface roughness is listed in Table 4. Two factors interaction (2FI) model has been suggested for SR. In case of SR, value of R^2 and R^2 (adj.) is greater than 99 % which shows that regression model provides an

excellent explanation of the relationship between input variables and the response. The *p* value for model is less than 0.05, indicating that the model is statistically significant. The lack of fit is also non-significant. The input parameters A, B, C, D and interaction terms AB, AC, BD and CD have significant influences on surface roughness as indicated by the associated *p* value (less than 0.05). Figure 3 shows the normal probability plot of residuals for SR. Residuals are falling on a straight line which means that the errors are normally distributed. After eliminating the non-significant terms, the final response equation for SR is given as follows:

In coded terms

$$\begin{aligned} \text{SR} = & 1.66 + 0.13 A + 0.42 B - 0.12 C - 0.14 D \\ & + 0.026 A \times B - 0.039 A \times C \\ & - 0.042 B \times D + 0.043 C \times D. \end{aligned} \quad (5)$$

In actual parameters

$$\begin{aligned} \text{SR} = & -6.22607 - 1.68519\text{E} - 003 \text{ Ip} + 0.080741 \\ & \times \text{Ton} - 0.027889 \text{ Toff} + 0.31389 \text{ SV} \\ & + 1.45833\text{E} - 004 \text{ Ip} \times \text{Ton} - 2.5833\text{E} - 004 \text{ Ip} \\ & \times \text{Toff} - 7.08333\text{E} - 004 \text{ Ton} \times \text{SV} \\ & + 8.5000\text{E} - 004 \text{ Toff} \times \text{SV}. \end{aligned} \quad (6)$$

Figure 4a–c shows the combined effect of input parameters on surface roughness. Increasing the value of Ip and Ton increases the value of surface roughness. High discharge energy due to high value of Ton and Ip results in melting and evaporation of work material that causes formation of gas bubbles that explode when the discharge ceases. Explosion of gas bubbles causes generation of



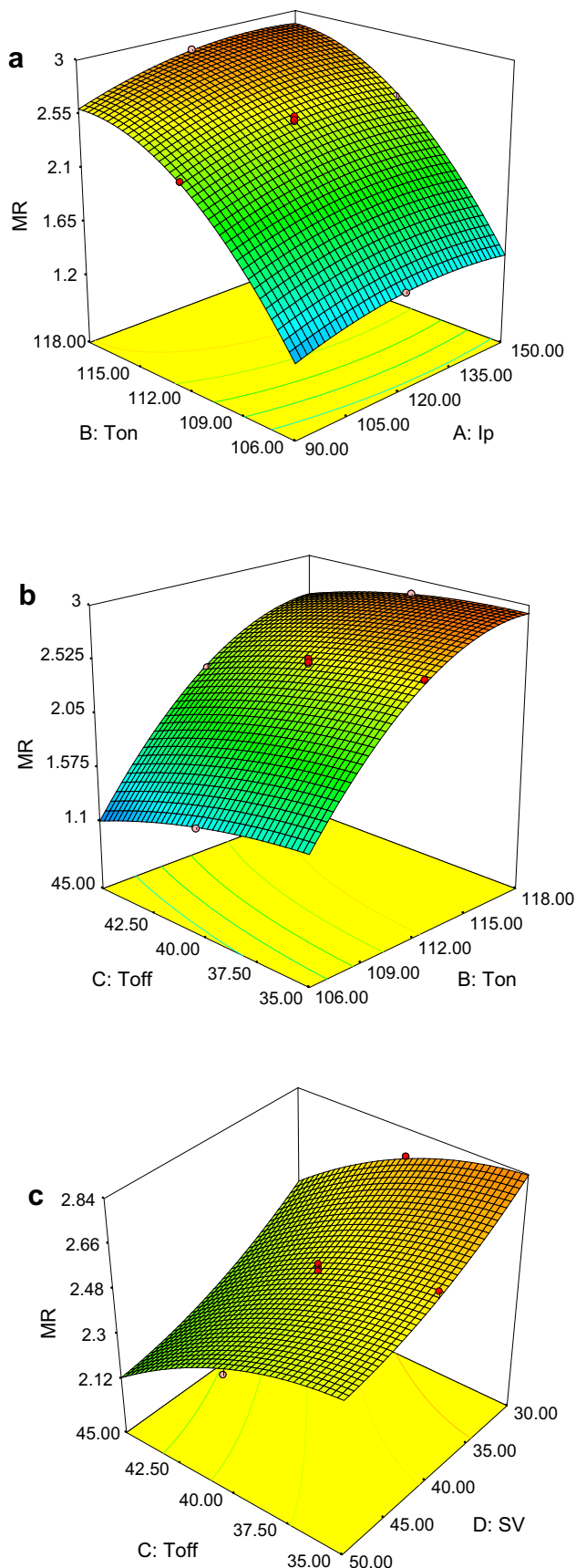


Fig. 2 a Effect of I_p and T_{on} on MR at T_{off} : 40 μ s; SV: 40 V, b effect of T_{on} and T_{off} on MR at I_p : 120 A; SV: 40 V, c effect of T_{off} and SV on MR at I_p : 120 A; T_{on} : 120 μ s

high-pressure energy that creates large-size craters on work surface. The diameter and depth of crater increases with increasing discharge current and pulse-on time and hence increases the surface roughness (Hewidy et al. 2005). High discharge energy (I_p : 150 A; T_{on} : 118 μ s; T_{off} : 35 μ s; SV: 30 V) results in the formation of overlapped and deep craters with large-size diameters as shown in Fig. 5a. High density of melted globules gets accumulated at the machined surface resulting in poorer surface finish.

Increase in the value of T_{off} decreases the spark frequency and hence reduces the discharge energy, as a result smooth surface with small crater size is generated as shown in Fig. 5b. Increasing the T_{off} results in quick and easy flushing of melted debris that results in minimum accumulation of melted globules and hence decreases SR as shown in Fig. 4b. Surface roughness decreases with increasing the value of servo voltage as shown in Fig. 4c. Increasing SV increases the gap between work material and wire electrode that results in low ionization of dielectric medium and hence low discharge energy get generated. Minimum surface roughness is obtained corresponding to low discharge energy, i.e., I_p : 90 A; T_{on} : 106 μ s; SV: 50 V and high value of T_{off} 45 μ s.

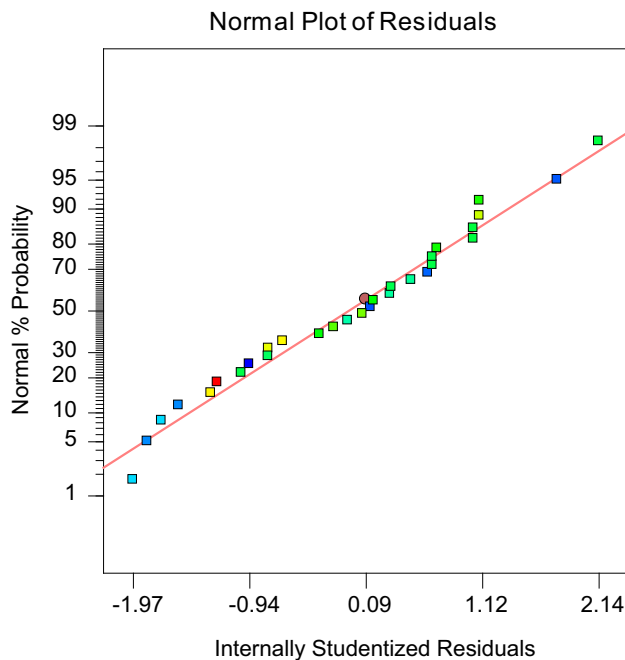
In WEDM, the extent of surface damage depends on the discharge energy across the work surface. Figure 6 shows the microhardness profile underneath the machined surface corresponding to high and low discharge energy. It is clear from Fig. 6a that the microhardness reduces at the top layers of machined surface as compared to bulk material. This reduction is mainly due to the thermal energy across the work surface which increases with increasing discharge energy (Li et al. 2013). Copper is a main constituent in Monel-400 which results in good thermal conductivity of Monel-400. As a result, fraction of heat transferred toward the bulk material is more as compared to other ceramics and carbide materials (Garcia Navas et al. 2008) and hence the heat-affected zone increases that lower the microhardness underneath the machined surface as compared to bulk material.

Multi-performance optimization through desirability function approach

Increasing the value of I_p and T_{on} and decreasing the value of T_{off} and SV, increases the discharge energy and vice versa. The generation of high discharge energy causes high machining rate but result in poor surface finish. Therefore,

Table 4 ANOVA table for SR (after backward elimination)

Source	Sum of squares	Degree of freedom	Mean square	F value	p value	
Model	4.19	8	0.52	665.61	<0.0001	Significant
A	0.30	1	0.30	383.29	<0.0001	
B	3.17	1	3.17	4024.52	<0.0001	
C	0.28	1	0.28	354.25	<0.0001	
D	0.35	1	0.35	444.80	<0.0001	
AB	0.011	1	0.011	14.01	0.0012	
AC	0.024	1	0.024	30.53	<0.0001	
BD	0.029	1	0.029	36.73	<0.0001	
CD	0.029	1	0.029	36.73	<0.0001	
Residual	0.017	21	7.869E-004			
Lack of fit	0.015	16	9.234E-004	2.64	0.1442	Not significant
Pure error	1.750E-003	5	3.500E-004			
Cor total	4.21	29				
Standard deviation = 0.028		$R^2 = 0.9961$	R^2 (Adj.) = 0.9946			

**Fig. 3** Residuals plot for SR

an optimal parameters setting is needed for simultaneously obtaining higher machining rate as well as minimum surface roughness. Using desirability function, the optimal WEDM parameters setting for MR and SR has been obtained.

Derringer and Suich (1980) proposed a multiple response optimization technique approach called desirability function. The general approach is to first convert each response $y_i(x)$ into an individual desirability function (d_i) and vary over the range $0 \leq d_i \leq 1$. The simultaneous objective function is a geometric mean of all converted responses. In the present study, design expert 7 has been used to optimize the response variables.

Derringer and Suich defined the three types of desirability function depending on the type of response characteristics as:

1. For the “larger-the-better” type:

$$d_i = \begin{cases} 0, & y_i \leq y_i^* \\ \left[\frac{y_i - y_i^*}{y_i' - y_i^*} \right]^t, & y_i^* < y_i < y_i' \\ 1, & y_i \geq y_i' \end{cases} \quad (7)$$

where y_i^* is the minimum acceptable value of y_i , y_i' is the highest value of y_i and t is the shape function for desirability.

2. For the smaller-the-better type:

$$d_i = \begin{cases} 1, & y_i \leq y_i'' \\ \left[\frac{y_i'' - y_i}{y_i'' - y_i^*} \right]^r, & y_i'' < y_i < y_i^* \\ 0, & y_i \geq y_i^* \end{cases} \quad (8)$$

where y_i'' is the lowest value of y_i , y_i^* is the maximum acceptable value of y_i and r is the shape function for desirability.

3. For the nominal-the-best type:

$$d_i = \begin{cases} \left[\frac{y_i - y_i^*}{C_i - y_i^*} \right]^s, & y_i^* < y_i < C_i \\ \left[\frac{y_i - y_i^*}{C_i - y_i^*} \right]^t, & C_i < y_i < y_i^* \\ 0, & y_i > y_i^* \text{ or } y_i^* > y_i \end{cases} \quad (9)$$

where C_i is the most acceptable or target value and s and t are the exponential parameters that determine the shape of desirability function.

Overall desirability function of the multi-response system can be measured by combining the individual desirability



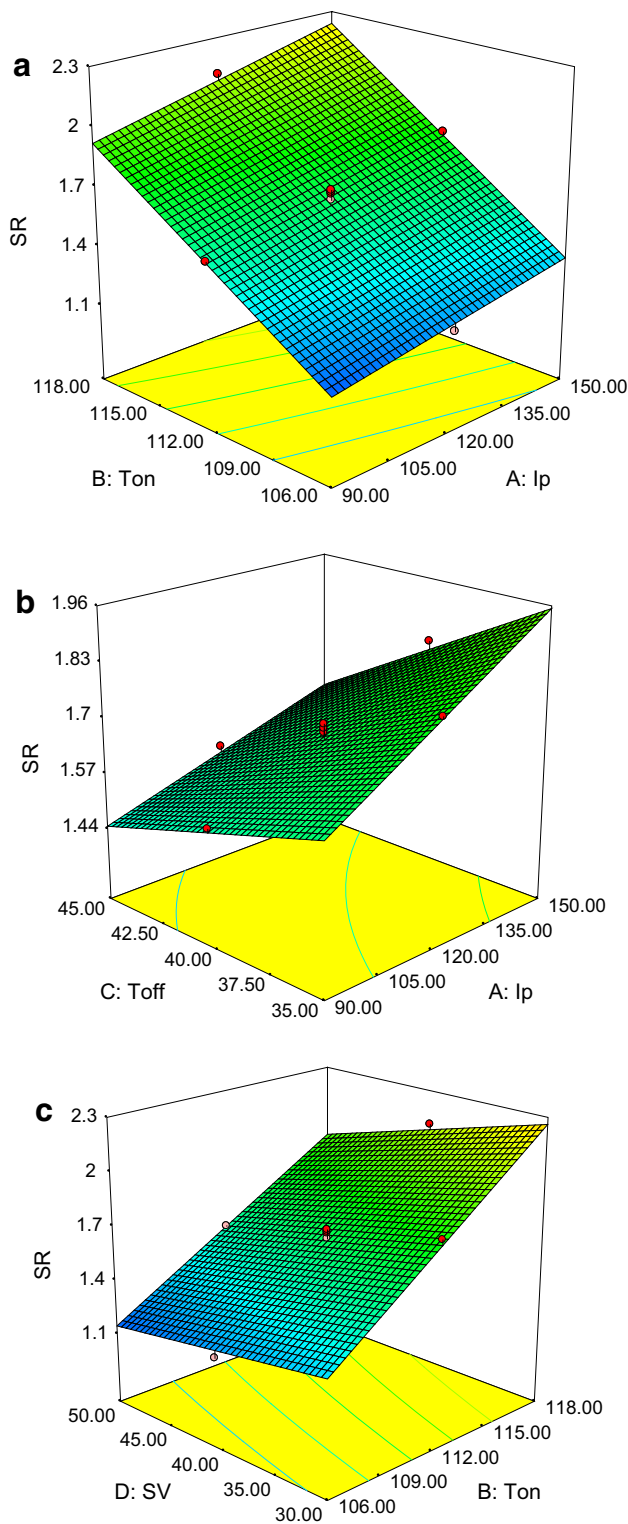


Fig. 4 **a** Effect of Ip and Ton on SR at Toff: 40 μ s; SV: 40 V, **b** effect of Toff and Ip on SR at Ton: 112 μ s; SV: 40 V, **c** effect of Ton and SV on SR at Ip: 120 A; Toff: 40 μ s

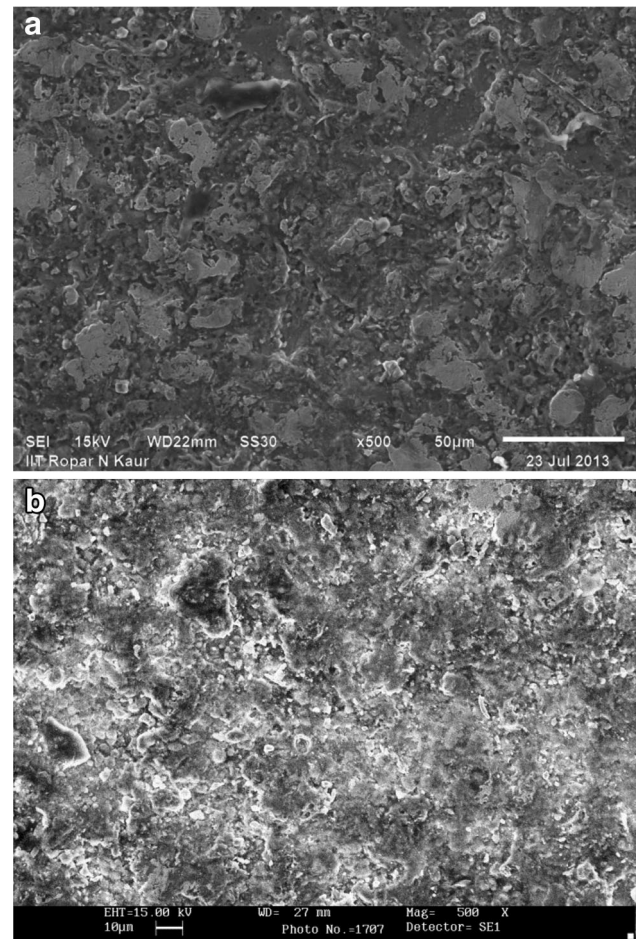


Fig. 5 **a** WEDM machined surface at Ip: 150 A; Ton: 118 μ s; Toff: 35 μ s; SV: 30 V, **b** WEDM machined surface at Ip: 90 A; Ton: 106 μ s; Toff: 50 μ s; SV: 50 V

functions. It can be represented as $D = (d_1^{w_1} \cdot d_2^{w_2} \cdot \dots \cdot d_n^{w_n})$, where w_j ($0 < w_j < 1$) is the weight value given for the importance of j th response variable and $\sum_{j=1}^n w_j = 1$. The parameter settings with maximum overall desirability value are considered to be the optimal parameter combination.

In the present study, the goal is to find optimal parameter settings that maximize the overall desirability function for higher machining rate and minimum surface roughness value. The ranges and targets of input parameters namely Ip, Ton, Toff and SV and the response characteristics machining rate and surface roughness are given in Table 5.

Table 6 shows the possible combination of WEDM process parameters that gives the high value of desirability. Contour plots offering overall desirability for multi-performance characteristic are drawn as shown in Fig. 7. The



Fig. 6 **a** Microhardness profile underneath the machined surface, **b** microindents on transverse section

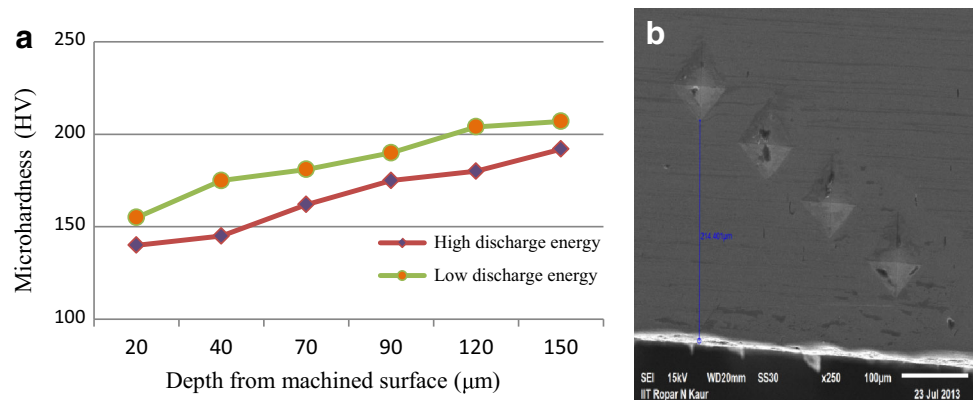


Table 5 Range of input parameters; MR and SR for desirability

Constraint	Goal	Lower limit	Upper limit	Important
Discharge current (I_p)	In range	90	150	3
Pulse-on Time (T_{on})	In range	106	118	3
Pulse-off time (T_{off})	In range	35	45	3
Servo voltage (SV)	In range	30	50	3
MR (mm/min)	Maximize	0.79	3.16	3
SR (μm)	Minimize	0.98	2.60	3

Table 6 Process parameters combination for high value of desirability

Number	Process parameters				Predicted response		Desirability
	I_p	T_{on}	T_{off}	SV	MR	SR	
1	103.20	112.88	37.14	50.00	2.48	1.54	0.68304
2	102.73	112.93	37.17	50.00	2.48	1.54	0.68303
3	102.80	112.84	37.17	50.00	2.47	1.53	0.68303
4	103.27	112.90	37.35	50.00	2.47	1.54	0.68301
5	102.47	112.78	37.13	50.00	2.46	1.53	0.68298
6	101.55	112.94	37.15	50.00	2.47	1.53	0.68296
7	102.34	113.00	37.35	50.00	2.48	1.54	0.68296
8	102.02	112.97	36.77	50.00	2.48	1.54	0.68293

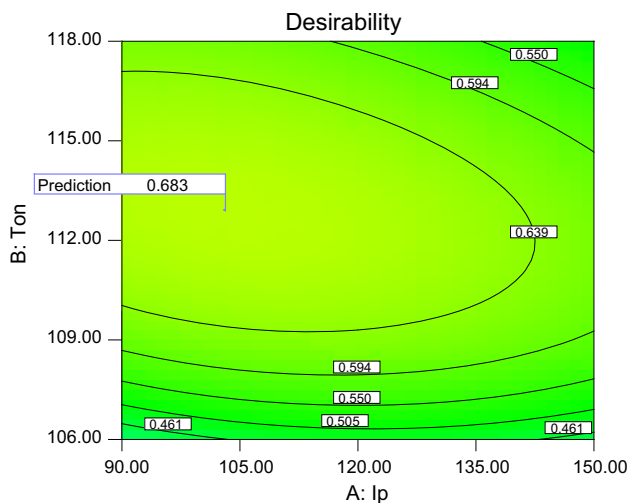


Fig. 7 Contour plot for overall desirability (T_{off} : 37 μs; SV: 50 V)

optimal region has been located near to left-hand side which has a desirability value of 0.683 that gradually reduced as we moved right and downwards. Corresponding to highest desirability, optimal combination of WEDM parameters for multi-performance characteristics is I_p : 103 A, T_{on} : 113 μs; T_{off} : 37 μs; SV: 50 V. Experimental values obtained corresponding to optimal setting for MR and SR were 2.65 mm/min and 1.7 μm that are closer to the predicted values in Table 6.

Trim cutting operation in WEDM

In WEDM, trim cutting operation is used to reduce surface damage such as thickness of recast layer, micro cracks and job inaccuracies developed in rough cutting operation. Damaged surface layer can be removed using single- or



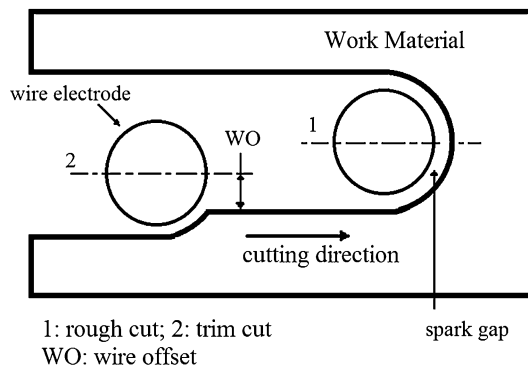


Fig. 8 Terminology used in trim cutting operation

multi-trim cuts. In trim cutting operation, wire electrode traces back the rough cut path but with some offset (Jangra 2014) as shown in Fig. 8. In the present study, trim cutting operations have been performed with two different wire offsets 105 and 85 μm at constant discharge energy. In the present work, wire offset (WO) is taken as distance between center of electrode and work surface before trim cut as shown in Fig. 8.

Trim cutting operations conducted after a rough cutting operation that was performed at high level of discharge energy (HDE) correspond to the parameters shown in Table 7. In contrast to rough cutting operation, low discharge energy is required in trim cutting operation, to obtain fine surface finish. Because of low discharge energy, a laminar dielectric flow is required in trim cutting operation for effective spark generation which otherwise is not possible at high or turbulent dielectric supply as in case of rough cutting operation. Therefore, a low dielectric supply is allowed through upper nozzle while bottom nozzle is closed. Figure 9 shows the comparative influence of trim cutting operation on surface roughness. It is clear from the Fig. 9 that surface roughness has been improved in trim cutting operation after a rough cut at high discharge energy. But the effect of multi trim cuts is negligible on surface roughness. It implies that using single trim cut with appropriate wire offset value and discharge parameters, surface integrity can be improved significantly irrespective of the rough cutting parameters.

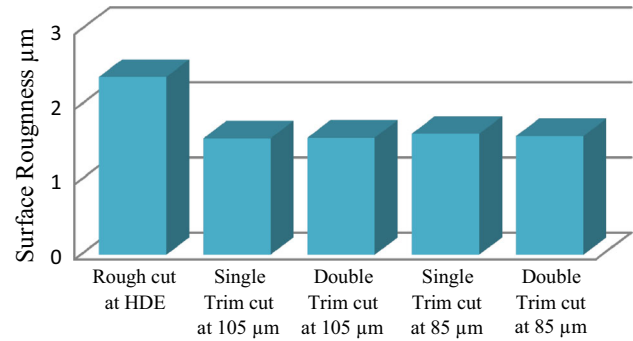


Fig. 9 Effect of trim cutting operation on surface roughness

Conclusions

This work presents the experimental study on wire electrical discharge machining of Monel-400, a nickel–copper-based alloy. Using response surface methodology and face-centered central composite design, experiments for rough cutting operation were performed to investigate and model the four WEDM parameters namely I_p , T_{on} , T_{off} and SV for two performance characteristics namely machining rate (MR) and surface roughness (SR).

Using analysis of variance (ANOVA), quadratic model is found significant for MR while two factors interaction (2FI) model has been suggested for SR. Increasing I_p and T_{on} increases the discharge energy that results in high value of MR but it adversely affects the SR. Increasing T_{off} decreases the MR but improves the surface finish by flushing out melted debris completely. Increase in SV decreases the MR and improves the SR. Microhardness profile underneath the machined surface describes the extent of thermal damage due to the discharge energy across the work surface.

Using desirability function, a scale-free quantity called desirability has been obtained for two performance characteristics to optimize multi-performance characteristics, i.e., MR and SR. Corresponding to highest desirability, the optimal combination of discharge parameters was I_p : 103 A; T_{on} : 113 μs ; T_{off} : 37 μs and SV : 50 V. Trim cutting operations at low discharge energy (T_{on} : 105 μs ; T_{off} : 35 μs ; I_p : 90 A; SV : 30 V) and different wire offset

Table 7 Parameter setting in trim cutting operation

WEDM operation	Discharge parameters	Wire offset value (WO)	Other parameters
Rough cut	T_{on} 118 μs , T_{off} 35 μs , I_p 160 A, SV : 30 V	0	Wire diameter (WD): 250 μm ; wire tension (WT): 10 N; wire feed rate (WF): 5 m/min Dielectric flow rate (DFR) 12 LM^{-1} ; servo feed (SF): 2080
Trim cut	T_{on} 105 μs , T_{off} 35 μs , I_p 90 A, SV 30 V	105 μm 85 μm	Wire tension 8 N; WF 2 m/min; DFR: 3 LM^{-1} (upper nozzle); bottom nozzle: closed



values (105 and 85 μm) were performed after a single rough cut at high discharge energy. Results showed that using single trim cut at low discharge energy and appropriate wire offset value, surface integrity of work material can be improved successfully.

Authors' contribution All the three authors have equally contributed to this work. Dr. Kamal Kumar Jangra and Dr. Vikas Kumar are the research supervisors of Vinod Kumar. They contributed in conducting the experiments, writing and correction of this research article.

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