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#### Fondazione Eni Enrico Mattei

## Optimal Privatisation Design and Financial Markets

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## Optimal privatization design and ...nancial markets<sup>\*</sup>

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January 31, 2001

#### **Abstract**

In this paper we consider various privatization mechanisms in a general equilibrium model. We show that privatization has no real exects, if the public sector is excient and lump-sum taxes are implemented. The free distribution of public assets is ...nancially neutral, whereas the sale of public assets is not. If taxes are not available, there is a privatization mix allowing the economy to reach the ...rst best. The maintain of some public property rights is justi...ed, even if the public exciency is removed.

JEL Classi...cation: E44; G1; H4; L33

Keywords: Financial market development; Privatization; Public good

provision; Public sector ine Cciency; Risk diversi...cation

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"Because di¤erent assets have di¤erent distributions of returns, privatization is a way of allocating risks across members of the economy." Maskin [2000]

#### 1 Introduction

Most of theoretical research on privatization analyzes the microeconomic ef...ciency of privatization. However, in a general equilibrium model, massive privatizations, i.e. large property transfers, may have a sensitive macroeconomic impact. This paper suggests a new general equilibrium approach and looks at mass privatization exects. We introduce State-owned property rights and public good production in a simple two-period general equilibrium model inspired by Martin and Rey [2000], without imposing any initial assumption on a lower productivity of the public sector.

In this model, each private agent has a property right over a risky project (more precisely over a second-period stochastic endowment in private good). This risky project provides a return in a speci...c state of nature, and nothing otherwise. Shares of the private property rights can be traded on a ...nancial market.

We assume that the government has a same kind of property right, and that private good can be converted in public good by a speci...c technology if its project is successful. Public good provision is initially not diversi...ed across states of nature. As a consequence, without economic policy such as taxation or privatization, there will be a twofold diversi...cation concern, across states of nature (because of risk aversion) and between goods (because of the strict convexity of preferences). The introduction of lump-sum taxes allows to solve this twofold problem. With an e¢cient tax system, the ...rst-best of this economy is always reachable, and privatization has no real e¤ects, in terms of consumption and/or welfare. However, privatization may have e¤ects on the ...nancial market, depending on the scheme selected (sale of public assets vs voucher distribution). The main interest of lump-sum taxes is therefore the smoothing of public good provision and private good consumption across the di¤erent states of nature.

If such a tax system is not available, privatization has real exects. We show that if the initial weight of the public sector is too high (compared to the weight of the public good in the private agents' preferences), there is always a privatization mix allowing the economy to reach the ...rst best. This optimal privatization mix is composed by:

- <sup>2</sup> some voucher distribution, to reduce the size of the public sector;
- 2 some sale of public assets, whose revenues are invested in a diversi...ed portfolio, in order to smooth public good provision across states of nature.

The simultaneity of voucher distribution and sale of public assets on the ...nancial market is not unrealistic. The stylized facts presented in Verdier and Winograd [1996] among others con...rm that both types of privatization have been implemented at the same time in some countries, for instance in Poland, Hungary, Slovakia and Romania.

The investment of privatization revenues in a diversi...ed portfolio of private assets is also realistic. For instance in France, revenues from the privatization of the saving banks, as well as from the sale of licenses for UMTS mobile phone (interpreted as a waves privatization), are directed to a retirement reserve funds. The debate is still open, but the government recognizes that the need of better returns diverts these funds towards the stock market. Similarly, the United States and Canada are equipped with such a retirement reserve funds, and consider that it should be partly invested on the stock exchange.

Our results can be also discussed in order to take in account a lower (or not) productivity of the public sector as a shareholder<sup>1</sup>. We show that, without e¢cient taxation:

- 2 if the government is an e⊄cient shareholder, there is even so a justi...cation for some privatization;
- <sup>2</sup> if the government is a less eccient shareholder than the private agents, there is even so a justi...cation for the maintain of some public property rights.

Finally, if the government is not an e¢cient shareholder but has at the same time lump-sum taxes at disposal, there is no justi...cation for the maintain of public property rights: the optimal policy is to let the private sector do, and to use the tax system to ensure public good ...nancing.

The rest of the paper is organized as follows. Section 2 presents the model. Section 3 compares the alternative privatization designs. Section 4 investigates the properties of the model with lump-sum taxes. Section 5 treats the case without taxation and provides the optimal privatization mix. Section 6 concludes.

## 2 The general framework

We present in this section a model which is largely inspired by Martin and Rey [2000]. Our main contribution to this model is the introduction of State-owned property rights and of public good production, allowing us to focus on policy guestions such as taxation or privatization.

<sup>&</sup>lt;sup>1</sup>Somehow or other, the usual literature on privatization use assumptions on a lower productivity of the public sector; see for instance, among others, Roland and Verdier [1994], Saint-Paul [1996] and Verdier and Winograd [1996].

We consider a two-period model of a closed economy, populated by n private agents indexed by i 2 f1; :::; ng interacting with a government indexed by g = n + 1. In the second period, there are S exogenously determined and equally likely states of nature indexed by s 2 f1;:::; Sg, revealed at the beginning of the period. There are two types of goods in this economy, produced and consumed in the second period. Let  $c_i$  be the private good consumption of agent i and  $g_i$  his public good consumption. As G is a pure public good, we set  $g_i = G$ ; for every i:

#### 2.1 Endowments and technology

In the ...rst period each private agent has a property right over a second-period stochastic endowment in private good. More precisely the endowment of agent i is equal to:

 $e_i(s) = \begin{cases} 1 & \text{if } s = i \\ 0 & \text{otherwise} \end{cases}$ 

The property right in the ...rst period can be interpreted as a speci...c risky project, which provides a return of 1 in a speci...c state of nature and of 0 otherwise. In this respect there is a complete specialization and no technological diversi...cation at all. This property right can also be interpreted as an Arrow-Debreu security that pays only in one state of nature. The assumption may look quite extreme<sup>2</sup>. However, what is crucial here is not this identity between projects and states of nature, but that the di¤erent projects are imperfectly correlated and there are risk-sharing opportunities for risk-averse agents. We could envisage to replace the relation "one project one state of nature" by n linearly independent payo¤ vectors (one for each agent), each individual project giving di¤erent returns in di¤erent states of nature. This would complicate the analytical solution of the model, without changing the qualitative results.

The government has a same kind of property right at the beginning of the ...rst period, over a second-period stochastic endowment (in private good) equal to:

 $e_g(s) = \begin{cases} 1 & \text{if } s = g = n+1 \\ 0 & \text{otherwise} \end{cases}$ 

With neither taxes nor ...nancial markets, the only resource the government has at disposal is this stochastic endowment. This endowment in private good is used as input and converted in public good by a speci...c technology in the second period. By simplicity we consider an identity production function which transforms one unit of private good in one unit of public good. Initially we assume that the public good provision is initially not diversi...ed across states of nature and arises only in state of nature s = g = n+1. Indeed

<sup>&</sup>lt;sup>2</sup>Acemoglu and Zilibotti [1997] and Martin and Rey [2000] have a similar assumption of contingent projects.

the government has no input to produce the public good in the second period if a "bad" state (s  $\leftarrow$  g) occurs. The traditional literature on privatization usually makes assumptions on the lower productivity of the public sector<sup>3</sup>. We do not impose such an assumption here to justify the privatization. Nevertheless the public sector ine $\leftarrow$ ciency could be modelled by assuming the government has a property right over a second-period stochastic endowment equal to:

 $e_g(s) = \begin{pmatrix} & & & \\ & & \cdot & 1 \text{ if } s = g = n + 1 \\ & & 0 \text{ otherwise} \end{pmatrix}$ 

We simply replace ® by 1 to rule out the ine¢ciency.

The size of the public sector (relative to the whole economy) is given by its weight in the initial property rights, equal to 1=(n + 1).

In n+1 states of nature there will be a strictly positive endowment in the economy (either for a private agent, or for the government). We consider the case where n+1. S: Thereby the markets are possibly incomplete. In this case, there may be no production in some states of nature. With no taxes nor ...nancial markets, agent i's consumption of the two types of good is detailed by the following table.

State of nature	Ci	G
S = I	1	0
s = j 2 f1;:::;ng;j & i	0	0
s = g = n + 1	0	1
s 2 fn + 2; :::; Sg	0	0

Table 1. Autarkic consumption.

#### 2.2 Preferences

The utility of an agent i has the following additively separable form:

$$u(c_i; G) = v(c_i) + w(G)$$

It is a general formulation, which allows us to present most of results. However, for the sake of computation simplicity, we will illustrate some of the properties of our model by a CES speci...cation. The result are general and the main transmission mechanisms are robust. More precisely, we will adopt the following form:

$$u(c_i; G) = (1_i^{-})c_i^{1/2} + {}^{-}G^{1/2}$$
 (1)

where<sup>4</sup> - 2 (0; 1) and ½ 2 (0; 1):

$$\frac{1}{n+1} > -$$

<sup>&</sup>lt;sup>3</sup>See among others Roland and Verdier [1994], Saint-Paul [1996], Verdier and Winograd [1996].

<sup>&</sup>lt;sup>4</sup>The size of the public sector in the economy could be initially greater than the weight of the public good in the preferences. In formula:

#### 2.3 Financial markets

Shares of the private property rights (claims on the stochastic endowments) can be traded on a ...nancial market during the ...rst period by the private agents (this is the only economic activity during this period). Therefore the stochastic revenue of agent i in the second period is given by either the share of his own project in the portfolio or the part of others' project he bought in the ...rst period. Without taxes or subsidies, this revenue will constitute its private good consumption.

Let  $d_{ij}$  denote agent i's demand for the asset sold by agent j, in terms of share of its initial property right. The price of this asset is  $p_j$ . In consequence,  $1_i$   $d_{ii}$  is by de…nition agent i supply in terms of share of its own initial property right, sold at price<sup>5</sup>  $p_i$ : This is a measure of the extent to which he has decided to diversify its own risk. Among many possible de…nitions we will choose this share of private property right exchanged in the market,  $1_i$   $d_{ii}$ ; as a measure of …nancial market development. If  $1_i$   $1_i$   $1_i$   $1_i$  direction is close to one, a large part of property rights is sold on the market. In this respect this variable well captures the …nancial market development. Demirguc-Kunt and Levine [1996] construct a typology of diærent …nancial indicators. According to their typology,  $1_i$   $1_i$  direction is a relevant indicator in terms of market size.

Our initial restriction to the case where n+1. S means now that it will not be possible to eliminate all the risk by holding a portfolio of all traded assets. However, with the described ...nancial market, the need for assurance can be partially achieved through and only through ...nancial choices, as there is a complete specialization and no technological diversi...cation at all. Only ...nancial diversi...cation matters<sup>6</sup>.

Without privatization, the public property right cannot be exchanged on the ...nancial market. The government does not exploit the possibility of ...nancial diversi...cation provided by the market to produce the public good in the second period if a "bad" state (i 2 f1; :::ng) occurs. The government does not enter the market to diversify the risk, does not sell shares of its property right, does not buy shares of assets sold by the private agents.

Let us now compute the equilibrium of this economy without privatization or any government's participation to the ...nancial markets.

This is the relevant case for privatization, as we will see later on.

<sup>&</sup>lt;sup>5</sup>In our world à la Arrow-Debreu, asset markets are assumed to be perfectly competitive. In contrast to Martin and Rey [2000], no assumption of monopoly power is made.

<sup>&</sup>lt;sup>6</sup>For a model stressing the duality between ...nancial and technological diversi...cation, see Saint-Paul [1992].

#### 2.4 Equilibrium without economic policy

Under the above assumptions on the ...nancial market, we write down the ...rst-period budget constraint of a private agent i :

$$\sum_{j=1}^{N} p_j \, d_{ij} \cdot p_i$$

Before introducing taxes and/or privatization, agent i's consumption is given by the following table.

State of nature	Ci	G
s = j 2 f1; :::; ng	d <sub>ij</sub>	0
s = g = n + 1	0	1
s 2 fn + 2; :::; Sg	0	0

Table 2. Consumption with ...nancial market.

For now we compute the decentralized equilibrium without any economic policy such as taxation or privatization. As the expected utility of public good is independent on the consumer's will, the agent i's program is written as follows:

$$\geq \max_{\substack{d_{ij} \\ p}} Ev(c_i) + \overline{Ew}$$

$$\geq s.t. \quad p_j d_{ij} \cdot p_i$$

where, according to the above consumption table, we have:

$$Ev(c_i) = \frac{X^n}{S} \frac{1}{S} v(d_{ij})$$

The ...rst order condition is:

$$\frac{1}{S}v^{0}(d_{ij}) = p_{j}$$

$$j = 1; \dots; n$$

We get that:

$$d_{ij} = v^{\emptyset_i - 1} (S_{\downarrow} p_j)$$
 (2)

The market-clearing condition for the initial property rights of an agent j is:

(2) and (3) lead to:

$$nv^{0_{j}} (S_p_j) = 1; 8i; j$$

This implies that we always have a symmetric equilibrium, such that:

$$p_i = p_j$$
  $p$ 

From the ...rst order condition we get that:

$$\begin{array}{ccc} \frac{v^0(d_{i\,i})}{v^0\,(d_{i\,j}\,)} & = & \frac{p_i}{p_j} \\ j & = & 1; \ldots; n \end{array}$$

In this condition, the left-hand term is the marginal rate of substitution between two assets, and the right-hand term is their relative price. From this condition, together with the budget constraint or the market-clearing condition, at the symmetric equilibrium, demands are as follows:

$$d_{ii}^{x} = d_{ij}^{x} = \frac{1}{n}$$

As seen above, the individual asset supply is a measure of ...nancial market development. Its equilibrium level is:

$$(1_{i} d_{ii})^{x} = 1_{i} \frac{1}{n}$$

Finally, if we choose the price of a particular asset as a numeraire, the equilibrium price  $p^{\pi}$  is equal to one.

It is not surprising to notice that private agents use the ...nancial market to smooth as well as possible their private good consumption across the dixerent states of nature. The equilibrium consumption of the two types of good for the agent i is given by table 3:

State of nature	Ci	G
s = j 2 f1; :::; ng	1=n	0
s = g = n + 1	0	1
s 2 fn + 2; :::; Sg	0	0

Table 3. Decentralized equilibrium consumption.

Why will this equilibrium diæer from the ...rst best? Table 3 shows that there is a twofold diversi...cation concern. First, there is a problem of diversi...cation across states: there is private good consumption only in states  $s = j \ 2 \ f1; :::; ng$ , and no private good consumption in state s = g = n + 1. Similarly, there is public good provision only in one state of nature. That leads to a diversi...cation problem between goods: preferences being convex, private agents wish consume both types of goods. This twofold imperfection is due to the lack of a transfer mechanism between the private agents and the public one: the government is outside the ...nancial market and has not at disposal, for the moment, a taxation system.

#### 2.5 First best

We have explained why, in this economy, the market mechanism does not implement the ...rst best. A central planner would maximize the expected utility of a representative agent under a system of resources constraints:

$$\begin{cases}
8 & \text{max} \\
\text{cs}; G^{s} \\
\text{s.t.} & \text{nc}^{s} + G^{s} \cdot 1; \text{ if s 2 f1}; :::; n + 1g \\
\text{nc}^{s} + G^{s} = 0; \text{ if s 2 fn + 2}; :::; Sg
\end{cases}$$

where  $(c^s; G^s)$  is the allocation of private and public good in the sth state of nature. Clearly if  $s \ 2 \ fn + 2; \ldots; Sg;$  then

$$c^{s} = G^{s} = 0$$

If s 2 f1;:::;n + 1g; the relevant solution is provided by an equivalent sub-program, that can be written:

$$\max_{\substack{c^s;G^s\\s.t.}} u(c^s;G^s)$$
s.t.  $nc^s + G^s \cdot 1$ 

Under our CES functional speci...cation (1) the optimal consumption plan  $(c^s; G^s)^{\pi}$  is given by:

$$(c^{S})^{\pi} = \frac{1}{n + \frac{n^{-}}{1_{i}^{-}}} \frac{1}{\frac{1}{1_{i} \cdot h}}$$

$$(G^{S})^{\pi} = \frac{\frac{n^{-}}{1_{i}^{-}} \frac{1}{1_{i} \cdot h}}{n + \frac{n^{-}}{1_{i}^{-}} \frac{1}{1_{i} \cdot h}}$$

$$s = 1; ...; n + 1$$
(4)

Both types of consumption are perfectly smoothed across the states of nature s = 1; :::; n + 1.

#### 2.6 Optimal taxation design

<sup>&</sup>lt;sup>7</sup>Taxation is said to be ex post because in the second period the following timing is set: (i) the state of nature is revealed, (ii) the private agents and the State receive their endowment in private good, (iii) taxation occurs, (iv) public good is produced and provided, (v) public and private good are consumed.

Taxation will allow the government to diversify the risk, i.e. to produce the public good in the second period even if a bad state (s 2 f1;:::; ng) occurs, and to allow private agents to consume the private good, if the state s = g = n + 1 occurs. The taxation design is announced ex ante. We assume that it does not di¤erentiate taxes in states 1;:::; n:

As the taxation design is announced ex ante, it does not a ect the equilibrium ...nancial choice  $d_{ij}^{\alpha}=d_{ij}^{\alpha}=1$ =n because the agents want to smooth consumption across states of nature. The decentralized consumption of the two types of good for the agent i is given by the table 4:

State of nature	Ci	G
s 2 f1; :::; ng	1=n ¡ ¿ (j )	n¿ (j )
s = g = n + 1	i ¿ (g)	1 + n¿ (g)
s 2 fn + 2; :::; Sg	0	0

Table 4. Decentralized consumption with taxation.

This e¢cient ...scal system permits to reach the ...rst best of the economy (c<sup>s</sup>; G<sup>s</sup>)<sup>\*</sup>. It is easy to check that, under our CES functional speci...cation (1), the optimal ...scal design is the following:

$$\dot{z}^{\pi}(j) = \frac{1}{n} i \frac{n}{n + \frac{n^{-}}{1_{i}^{-}}} \frac{1}{\frac{1}{1_{i} \cdot k}}$$

$$\dot{z}^{\pi}(g) = i \frac{1}{n + \frac{n^{-}}{1_{i}^{-}}} \frac{1}{\frac{1}{1_{i} \cdot k}}$$

$$\dot{z}^{\pi}(s) = 0 \text{ if } s \text{ 2 fn + 2; ...; Sg}$$

## 3 Alternative privatization designs

We envisage two alternative schemes of privatization: (i) free distribution of public assets (voucher distribution) and (ii) sale of assets and holding of a diversi...ed portfolio. In both cases, the government privatizes a share ¼ of its initial property right, for now treated as an exogenous variable: the privatization extent is not decided by the short run policy maker but exogenously ...xed by an independent power such as a parliament, or by a prior electoral program of government's coalition; it belongs to a long-run strategy<sup>8</sup>. By assumption the government is forced to distribute or to sell a given amount ¼.

<sup>&</sup>lt;sup>8</sup>In a di¤erent pattern we will use later, the policy maker decides endogenously the privatization extent.

#### 3.1 A: free distribution of public assets

At the beginning of the ...rst period, the government freely distributes shares of its property right. This distribution occurs ex ante, i.e. before ...nancial markets open. Each one of the n private agents gets 1=n of the issued stocks. In other words, a private agent i has an additional property right over a stochastic second-period endowment (in private good) equal to:

$$4A=n$$
 if  $s=g=n+1$   
0 otherwise

In the ...rst period, private agents can trade shares of this additional property right on a ...nancial market. Let  $d_{ig}$  denote the agent i's demand for these additional property rights sold by other private agents: The price of this asset is  $p_g$ . The ...rst-period budget constraint of a private agent i becomes:

$$\sum_{j=1}^{N} p_j d_{ij} + p_g d_{ig} \cdot p_i + p_g \mathcal{V}_A = n$$

The government has now a property right over a residual second-period endowment, equal to:

$$1_i$$
  $\frac{1}{4}$  if  $s = g = n + 1$  0 otherwise

As the privatization consists in a free-distribution, there is no privatization revenue and in consequence no government's budget constraint.

#### 3.2 B: sale of assets and holding of a diversi...ed portfolio

In the ...rst period the government sells shares of its own property right on a ...nancial market. Let  $d_{ig}$  be agent i's demand for the asset sold by the government, in terms of share of the initial property right. Thereby a private agent i has an additional property right, over a stochastic second-period endowment (in private good), equal to:

$$d_{ig}$$
 if  $s = g = n + 1$   
0 otherwise

The price of the asset sold by the government is  $p_g$ . The ...rst-period budget constraint of a private agent i becomes:

$$p_j d_{ij} \cdot p_i$$

$$j = 1$$

The government has a property right over a residual endowment in private good equal to:

$$1_i$$
  $\frac{1}{4}$ B if  $s = g = n + 1$   
0 otherwise

As the government sells, it gets a revenue from the privatization, equal to  $p_g \%_B$ : We assume that, thanks to this ...rst-period revenue, the government buys a diversi...ed portfolio, which is precisely constituted by the assets sold by the private agents. Let  $d_{gi}$  be the government demand for an asset sold by the agent i; as a share of his initial property right. The government has now a ...rst-period budget constraint, that can be written:

We assume here that the government keeps its diversi...ed portfolio at the end of the ...rst period, and has an additional property right, over a stochastic second-period endowment (in private good, that can be transformed in public good), equal to:

$$d_{gi}$$
 if  $s = i \ 2 \ f1; :::; ng$   
0 otherwise

#### 4 E⊄cient taxation

We assume in this section the government has at disposal an e¢cient ...scal system. The individuals know ex ante the taxation design, but taxes are levied ex post, i.e. after the market closure.

#### 4.1 Public sector e⊄ciency

#### 4.1.1 A neutrality result

Presenting the two alternative privatization schemes, we saw that each one can be viewed as a di¤erent allocation of property rights. The private agents are symmetric: whatever privatization scheme is implemented, there is always a taxation design which changes the consumption plan in the ...rst best.

Even if the agents know the taxes for the dimerent states of nature before choosing, they will reach the general equilibrium allocation which allows the optimal taxation to implement the ...rst best. There are no distortions because the taxes are lump-sum.

That leads to the following proposition.

Proposition 1 With e $\$  cient taxation, privatization does not have any real impact, whatever privatization scheme is implemented. In other words there is always an ex post taxation design allowing to reach the ...rst best consumption plan  $(c^s; G^s)^{\alpha}$  of this economy.

#### 4.1.2 Financial exects

Voucher distribution. First, we can notice the ...nancial neutrality of the free distribution scheme (privatization of type A). The market-clearing condition for the initial property rights of an agent j is:

$$\sum_{i=1}^{N} d_{ij} = 1$$

At the symmetric equilibrium, that can be rewritten

$$nd_{ii} = 1$$

That leads to

$$(1_i d_{ii})^{\pi} = 1_i \frac{1}{n}$$

Financial market development does not depend on the privatization extent, and is equal to ...nancial market development without privatization. Besides, at equilibrium, the additional property rights (uniformly distributed among private agents) are not traded. In consequence, on the ...nancial market, n private agents trade their initial property rights, as if there were no economic policy.

Sale of assets. The ...nancial impact is quite dixerent if the government sells assets and invests in a diversi...ed portfolio (privatization of type B). The government now plays as a (n + 1)th risk-averse agent on the ...nancial market. The market-clearing condition for the property rights of an agent j becomes:

$$^{r}X^{+1}$$
  $d_{ij} = 1$ 

where, at the symmetric equilibrium,  $d_{gi}^{\pi}>0$  is given by the government budget constraint (5). We can then check that:

$$(1_i d_{ii})^{\pi} = 1_i \frac{1}{n} + \frac{d_{gi}^{\pi}}{n} > 1_i \frac{1}{n}$$

where 1  $_{\rm i}$  1=n is the ...nancial market development of the free distribution (privatization of type A). More precisely, in the CES case, for privatization by sale of assets (type B), we can explicitly compute all the asset demands and supplies as functions of the exogenous parameters and of the asset prices. We substitute then these functions into the market-clearing conditions and ...nally we show that, without any ambiguity $^9$ ,

$$\frac{@(1_{i} d_{ii})^{x}}{@N_{B}} > 0$$

That leads to the following proposition.

<sup>&</sup>lt;sup>9</sup>See the appendix A for details.

Proposition 2 From the point of view of the ...nancial market development (de...ned as the share of each private project exchanged on the market), the free distribution of public assets is neutral. Conversely, the sale of public assets leads to a ...nancial market development greater than its initial level. More precisely, with sale of assets, ...nancial market development is a strictly increasing function of privatization extent.

In the CES case with a privatization by sale of assets (type B), we can also plot the function  $(1_i d_{ii})^{\sharp}$  as a function of  ${}^{1}\!\!/_{B}$  for dimerent values of the parameter  ${}^{10}$  n.

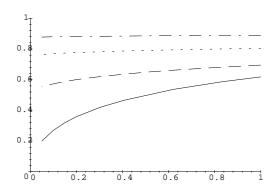


Figure 1 :  $(1_i d_{ii})^{\alpha}$  as a function of  $\mu_B$ 

The …nancial market development is always an increasing and concave function of privatization extent. However, as the initial size of the public sector is less and less important, i.e. as n increases, the privatization impact becomes weaker and weaker, and eventually negligible. In other words, the slope of  $(1_i d_{ii})^{\pi}$  as a function of  $\%_B$  is greater as the initial weight of the public sector is higher  $^{11}$ .

According to a very clear intuition  $^{12}$ , the positive role of privatization on ...nancial market development observed when public assets are sold, might be due to an increase in risk-sharing opportunities. The privatization adds diversi...cation possibilities that encourage listing by private ...rms: the risk-averse agents perceive privatization as a new opportunity to share the risk. However, in our model, this mechanism does not play, and the gains in market development are rather due to a simple demand expect. In our case the demand expressed by the government for a diversi...ed portfolio increases the price of private assets and their equilibrium supply  $(1_i \ d_{ii})^x$ :

 $<sup>^{10}</sup>$ We set ½ = 1=2. Solid line: n = 1; dashed line: n = 2; dotted line: n = 4; dotted and dashed line: n = 8.

<sup>&</sup>lt;sup>11</sup>This is consistent with the intuition of Verdier and Winograd [1996]: only a massive privatization, i.e. large scale property transfers, have a sensitive macroeconomic impact.

<sup>&</sup>lt;sup>12</sup>Suggested among others by Perotti and van Oijen [2001], following the work of Pagano [1993].

## 4.2 Public sector ine⊄ciency: the optimality of total privatization

We saw that we could have modelled a kind of public ine¢ciency, by assuming that the government has a property right over a second-period stochastic endowment equal to:

$$^{\circledR}$$
 < 1 if s = g = n + 1 0 otherwise

With such an imperfection, there is an additional aggregate risk in the economy. Indeed, if s = q = n+1, the total endowment of the economy is equal to ® < 1. A transfer of the public property right to the private sector (assumed here to be a more eccient manager) decreases this additional aggregate risk by decreasing the share of the second-period endowment 1; ¼A axected by the ine $\$ ciency, if s = g = n + 1. The additional aggregate risk is removed if  $4_A$  is equal to one. With a total privatization, the total endowment is always equal to 1; for every s 2 f1; :::; n + 1g. As a consequence, if there is public inecciency, the optimal policy will be a total privatization. The public good provision is ensured by the ...scal system by means of ex post lump-sum taxes. This is a very intuitive result: if the government produces less ecciently than the private sector and if lump-sum taxes are available, the optimal policy is obviously to let the private sector do, and to tax it ex post. In that case where we have simultaneously e⊄cient ex post taxation and public ine⊄ciency, there is no justi...cation for the maintain of public property rights. 13

#### 5 Privatization with no taxation

We assume in this section that the government has not at disposal an e $\$ cient ...scal system, precisely that  $\$ ightharpoonup (s) = 0; for every 14 s:

#### 5.1 Public sector e⊄ciency

#### 5.1.1 Optimal diversi...cation: privatization by sale of assets

The main interest of lump-sum taxes in this model was the smoothing of public good provision and private good consumption across the di¤erent states of nature. If such a ...scal system is not available 15, we can show that, under a very simple condition, a privatization plan can replace it. We are interested here in the only privatization scheme that allows the

<sup>&</sup>lt;sup>13</sup> If the public sector is assumed to be a less e⊄cient manager, whatever kind of assets it holds, the optimal policy will be a total privatization by voucher distribution. Conversely, if the public sector is assumed to be a less e⊄cient manager only concerning its initial property right, the privatization mechanism does not matter.

<sup>&</sup>lt;sup>14</sup>It might be due, for instance, to information problems.

<sup>&</sup>lt;sup>15</sup>We assume here that there is no ...scal system at all.

diversi...cation of public good provision across the di¤erent states of nature, i.e. what we have called privatization by sale of assets followed by the holding of a diversi...ed portfolio (type B): $^{16}$  As we are looking for an optimal policy, we also consider now that the government treats the variable  $^{16}$ B as endogenous. Let us remind that  $^{16}$ B is the government's supply, in terms of share of its initial (public) property rights. We have:

$$M_{B}$$
 1 i  $d_{gg}$ 

where, according to the previous notation,  $d_{gg}$  is the demand of public assets the government directs to itself. We present the results in the CES case<sup>17</sup>. As usual the ...rst step consists in the explicit computation of all asset demands and supplies. We then aggregate them to compute the market-clearing for the both type of assets (the assets sold by private agents and the assets sold by the government). In particular at the symmetric general equilibrium, we get a very simple analytic expression of the optimal level of privatization by sale of assets (type B), which turns out to be strictly positive, and strictly less than 100%:

Proposition 3 Without e $\$ cient taxation, there is justi...cation of some privatization by sale of public assets despite the public sector e $\$ ciency, because of risk-sharing issues. Formally speaking, there is an optimal level of privatization by sale of assets  $\$ B such that:

$$0 < \frac{1}{10} = \frac{n}{n+1} < 1 \tag{6}$$

This privatization level  ${}^{\mu}_{B}$  is the only one that permits to smooth private good consumption and private good provision across the states of nature s 2 f1;:::; n + 1g. If  ${}^{\mu}_{B} > {}^{\mu}_{B}$  and for instance if  ${}^{\mu}_{B} = 1$ ; public good provision is equal to zero in the state of nature s = g = n + 1; entailing a too high marginal utility of public good with respect to marginal utility of private consumption. Conversely, in our setup without taxation, if  ${}^{\mu}_{B} < {}^{\mu}_{B}$ ; for instance if  ${}^{\mu}_{B} = 0$ ; the public good provision will be equal to zero in all the states s  ${}^{\epsilon}$  g.

Besides, at the symmetric general equilibrium, the agent i's consumption plan of the two types of good is the following:

$$c^s = G^s = 1$$
= (n + 1) for every s 2 f1; :::; n + 1g  $c^s = G^s = 0$  for every s 2 fn + 2; :::; Sg

Let us compare this consumption plan with the ...rst best described by (4). That leads to the following proposition:

<sup>&</sup>lt;sup>16</sup>This idea of privatization as a way of allocating risks is suggested in Maskin [2000] among others.

<sup>&</sup>lt;sup>17</sup>See the appendix B for details.

Proposition 4 Without e $\$ cient taxation, the optimal level of privatization by sale of assets  $\$ ^ $\$ B leads to the ...rst best if and only if the size of the public sector is equal to the weight of the public good in the preferences, i.e. if and only if:

$$\frac{1}{n+1} = -$$

If quite by chance the above condition holds, the individuals and the market mechanism give the same importance to the public good, and the economy exactly satis...es the consumers' needs. On the other hand, if the subjective importance — given by consumers to the public good is less than the objective importance recognized by the market, i.e. if

$$\frac{1}{n+1} > - \tag{7}$$

then the economic system decentralizes an excessive provision of public good with respect to the ...rst-best level. Conversely, if (7) holds with a reversed inequality, then the economic system decentralizes a provision of public good under its ...rst-best level, and an excessive private consumption. In our model the possible sub-optimality of decentralized solution arises because private agents maximize the expected sub-utility Ev; while the government maximizes only Ew: This separability of programs breaks the substitution mechanism between the private consumption  $c_i$  and the public good G; and in particular entails that the parameter  $\bar{c}$  does not matter. Therefore the subjective importance the agents give to the public good in terms of utility is not taken in account in the decentralized allocation of resources.

#### 5.1.2 How to alter the size of the public sector?

We just saw that in the case without taxation, i.e. if  $\zeta$  (s) = 0; for every s; the ...rst-best could be reached if and only if the relative size of the public sector (de...ned as the weight of the government in the initial property rights) is equal to the weight of the public good in the preferences. Forget for a short while the diversi...cation issues, to focus on the problem of public sector size. Assume for instance that the size of the public sector is initially too high compared to the weight of the public good in the preferences, as described in (7). A level  $\frac{1}{4}$ A > 0 for a voucher distribution (privatization of type A) reduces the size of the public sector to:

$$\frac{1_i \ \%_A}{n+1}$$

Therefore it is possible to deal with voucher distribution (type A privatization), to alter the size of the public sector.

Remark here that if (7) holds with a reversed inequality, some nationalization ( $\%_A < 0$ ) is needed to bring the size of the public sector up to its desired level.

#### 5.1.3 The optimal privatization mix

Eventually we combine propositions 3, 4 and the intuition of the previous paragraph. The conjecture we want to prove, claims that, if the size of the public sector is initially too high, as described in (7), there exists a privatization mix such that the economy reaches its ...rst best. The optimal privatization mix would be composed by:

- <sup>2</sup> a free distribution of public assets (¼<sub>A</sub>) to reach an optimal size of public sector;
- $^2$  a partial sale of the rest  $\rm ^4_B$  (1  $_{\rm i}$   $\rm ^4_A)$  to decentralize the general equilibrium and optimally smooth both the types of consumption across the dimerent states of nature.

As a consequence, the global privatization extent will be equal to

$$\% = 1_{i} (1_{i} \%_{A}) (1_{i} \%_{B})$$

Broadly speaking the free privatization equalizes the subjective and the objective weight of public good given respectively by the preferences and the initial in‡uence of the State in the market, and it implements the condition the market needs to automatically decentralize the ...rst best.

In order to prove that an optimal privatization cocktail always exists, we rewrite the programs of the private and public agents. At ...rst a share  $\%_A$  of public property right is freely distributed among the n private agents. Afterwards the government enters the market by selling the right part  $\%_B$  of 1  $\%_A$ . We obtain the equilibrium demands and supplies on the asset market as a function of the prices and  $\%_A$ : The reader is referred to the appendix C for details. In particular we get the level of privatization by sale of assets:

$$^{14}_{B}^{x} = \frac{n}{n+1}$$

We notice that it is exactly the same as in the pure privatization by sale of assets. The mix does not matter for this share.

The last step is a backward adjustment of the initial free distribution  $4^n_A > 0$  such that the general equilibrium coincides with the ...rst best consumption plan. It is easy to check that under the condition (7), the ...rst best is reached if and only if

$$\mathcal{V}_{A}^{u} = n \frac{1}{1} \frac{\frac{3}{1} - \frac{1}{1} \frac{1}{1}}{n + \frac{1}{1} - \frac{1}{1} \frac{1}{1} \frac{1}{1}}$$
(8)

(see the appendix C).

We observe that if a reverse inequality holds,  $1=(n+1)<\bar{\phantom{a}}$ ; the size of the public sector is lower than the level the agents wish, and, as  $\frac{\pi}{A}$  becomes negative, a nationalization would be required instead of a privatization.

Proposition 5 Without ecient taxation, if the size of the public sector is initially too high, there exists an optimal privatization mix (free distribution and sale of public assets) such that the economy reaches the ...rst best.

The ...nancial market development is then the following:

$$(1 i d_{ii})^{\alpha} = \frac{n i \mathcal{A}_{A}^{\alpha} = n}{n+1}$$

#### 5.2 Public sector ine¢ciency

Introducing public sector ine¢ciency in the setup without taxation leads to a trade o¤ between two e¤ects. On the one hand, such an ine¢ciency might call for the limitation of State-owned property rights. On the other hand, because of the lack of an e¢cient ...scal system, some maintain of these public property rights is required to ensure consumption smoothing.

We notice ...rst that because of the lack of ...scal system, the ...rst best is not reachable. However, if we take into account the coincidence of productive ( $^{\circ}$  < 1) and ...scal ine $\oplus$ ciencies, there is a taxless optimum. In the CES case, this taxless optimum is characterized by the following consumption levels:

$$C^{S}(\mathbb{B})^{\pi} = \frac{\mathbb{B}}{n^{\mathbb{B}+\frac{1}{1}\frac{\mathbb{B}^{-}}{1_{1}}\frac{\mathbb{C}}{1_{1}}}} \frac{1}{1_{1}^{-\frac{1}{1}}}$$

$$G^{S}(\mathbb{B})^{\pi} = \frac{\frac{1}{1}\frac{\mathbb{B}^{-}}{1_{1}^{-\frac{1}{1}}}\frac{\mathbb{C}^{-}}{1_{1}^{-\frac{1}{1}}}}{n^{\mathbb{B}+\frac{1}{1}\frac{\mathbb{B}^{-}}{1_{1}^{-\frac{1}{1}}}}}$$
(9)

for every s 2 f1;:::; n + 1g: The computations are provided in appendix D.

The consumption smoothing across states is still ensured, as intuition suggests, but without taxation public ine¢ciency leads to consumption levels under the ...rst-best an ex post taxation would implement. We can decentralize this taxless optimum as before by computing a privatization mix. The optimal level of privatization by sale of assets remains unchanged:

$$^{\text{MB}}_{B}(^{\text{@}}) = \frac{n}{n+1}$$

We notice that not only the mix does not matter for  $4^n_B$ ; but moreover this share is invariant with  $^{\circledR}$ :

Besides we get that the taxless optimum is reached by the following level of the initial free distribution:

$$\mathcal{V}_{A}^{\alpha}(^{\otimes}) = n \frac{\frac{3}{8} \frac{1}{1_{i}} \frac{1}{1_{i}} \frac{1}{1_{i}}}{n^{\otimes} + \frac{3}{1_{i}} \frac{1}{1_{i}} \frac{1}{1_{i}}}$$
(10)

In that case ( $^{\otimes}$  < 1) a privatization in terms of a free distribution is needed ( $^{\alpha}_{A}$  ( $^{\otimes}$ ) > 0) if and only if:

$$\frac{1}{1 + {}^{\otimes \frac{1}{N}}n} > \overline{\phantom{a}} \tag{11}$$

The left-hand side is still interpreted as a size of public sector. However it depends now on the preference parameter  $\frac{1}{2}$  because of the public ine $\frac{1}{2}$  ciency  $\frac{1}{2}$ : If there is no ine $\frac{1}{2}$  ciency ( $\frac{1}{2}$ ) (10) and (11) reduce to (8) and (7).

Moreover we notice that always

$$^{1/4}_{A}(^{\circ}) < 0$$

In words the more inectient the public sector is, the larger must be the optimal voucher distribution level (privatization of type A).

The global extent of the optimal mix is given by

$$1_{i} (1_{i} \%_{A}^{x}) (1_{i} \%_{B}^{x})$$

As  $^{\mu}_{B}$  does not depend on  $^{\otimes}$ ; the impact of  $^{\otimes}$  on the optimal extent is negative: the required global degree of privatization is larger under higher public sector ine $\Phi$ ciency.

If condition (11) is veri...ed, the following proposition holds.

Proposition 6 Without ecient taxation and under public ineciency, the total privatization is not optimal. There is a privatization mix (free distribution and sale of public assets) such that the economy reaches the taxless optimum. Furthermore the extent of the optimal mixed privatization increases with the ineciency degree.

The ...nancial market development is now:

$$(1_i d_{ii})^{\alpha} = \frac{n_i \frac{1}{4} \frac{1}{4} (R) = n}{n+1}$$

We notice that

$$\frac{@\left(1_{i} d_{ii}\right)^{x}}{@^{\mathbb{R}}} > 0$$

The more eccient the public sector is, the larger is the equilibrium ...nancial market development.

#### 6 Conclusion

The paper has presented a two-period general equilibrium model of a closed country, inspired by Martin and Rey [2000], in which we have introduced State-owned property rights and public good production, to focus on economic policy questions such as taxation or privatization.

We have shown that if lump-sum taxes are implemented, privatization has no real exects, except under an assumption of public inetciency.

On the other hand, if taxes are not available and there is no public inetciency, there exists a privatization mix (free distribution and sale of public assets) such that the economy reaches its ...rst best. If we introduce

public ine¢ciency, there is even so a justi...cation for the maintain of some public property rights. However the optimal degree of global privatization increases with public sector ine¢ciency.

We also get ...nancial results. The free distribution of public assets is neutral on the ...nancial market development which is here de...ned as the private asset supply at equilibrium. Conversely the sale of public assets is not neutral and increases the ...nancial market because of a demand exect: the government's demand for private assets increases their price and supply. This ...nancial result might give rise to empirical works.

### **Appendix**

## A Financial exects of privatization by sale of assets

Part of Proposition 2. With privatization by sale of assets, ...nancial market development is a strictly increasing function of privatization extent. Proof. With privatization by sale of assets, the consumption of the two types of good is given by the following table:

State s	Ci	G
s = j 2 f1; :::; ng	d <sub>ij</sub>	d <sub>gj</sub>
s = g = n + 1	d <sub>ig</sub>	1; ¼ <sub>B</sub>
s 2 fn + 2; :::; Sg	0	0

Private agents. The program of a private agent i is:

$$8 \geqslant \max_{d_{ij}} Ev(c_i) + \overline{Ew}$$

$$8 \geqslant s.t. \sum_{j=1}^{n p + 1} p_j d_{ij} = p_i$$

With a privatization by sale of assets, the expected utility of the private good is given by:

$$Ev(c_i) = {}^{iX-1} \frac{1}{S} v(d_{ij})$$

Solving this program in the CES case, we get the three di¤erent types of demand for the agent i:

$$\begin{array}{rcl} d_{ij} & = & \frac{(p_i = p_j)^{1 = (1_i \ \frac{1}{2})}}{n!^{\cancel{p}_1}} \\ & & (p_i = p_j)^{\frac{1}{2} = (1_i \ \frac{1}{2})} \\ i & = & 1; \ldots; n \\ j & = & 1; \ldots; n + 1 \end{array}$$

Government. The government maximizes the expected utility of a private agent i under its budget constraint:

Under an exogenous privatization level  ${}^{1}\!\!/_{B}$  the government's asset demand  $d_{gi}$  is the only choice variable that is at the symmetric equilibrium directly ...xed by the budget constraint.

Symmetric equilibrium and price normalization. We normalize  $p_g$   $p_{n+1}$  1. At the symmetric equilibrium we know that we shall have  $p_i = p_j$   $p_i$ , for every i; j: Consequently the demand functions become:

$$d_{ii} = d_{ij} = d_{ji} = \frac{1}{n + p^{1/2} - (1_{i} \frac{1}{2})}$$

$$d_{ig} = \frac{p^{1 - (1_{i} \frac{1}{2})}}{n + p^{1/2} - (1_{i} \frac{1}{2})}$$

$$d_{gi} = d_{gj} = \frac{\frac{1}{1} + \frac{1}{1}}{np}$$
(12)

General equilibrium. The general equilibrium is determined by two market-clearing conditions.

With symmetric agents, these conditions can be rewritten:

$$nd_{ii} + d_{gi} = 1$$
  
 $i = 1; :::; n$   
 $nd_{ia} = \frac{1}{1}$  (13)

One of them is redundant by the Walras' law. After substituting (12) into (13) we obtain:

$$\frac{np^{1=(1_i \ \%)}}{n + p^{\%=(1_i \ \%)}} = \%_B$$

Therefore the general equilibrium price of private assets is always a strictly increasing function of the privatization extent:

$$\frac{@p^{x}}{@\mathcal{H}_{R}} > 0$$

Besides we have:

$$1_{i} d_{ii} = 1_{i} \frac{1}{n + p^{1/2 - (1_{i} 1/2)}}$$
  
 $\frac{@ (1_{i} d_{ii})}{@p} > 0$ 

We then conclude that:

$$\frac{@\left(1_{i} \ d_{ii}\right)^{\pi}}{@\mathcal{V}_{AB}} > 0$$

Financial market development is a strictly increasing function of privatization extent.

## B The optimal level of privatization by sale of assets without taxation

Proposition 3. Without e $\Phi$ cient taxation, there is justi...cation of some privatization despite the public sector e $\Phi$ ciency, because of risk-sharing issues. Formally speaking, there is an optimal level of privatization by sale of assets  $\frac{1}{2}$  such that:

 $0 < \frac{n}{B} = \frac{n}{n+1} < 1$ 

Proof. If we assume that the privatization extent is no longer an exogenous constraint, i.e. that  ${}^{1}_{B}$  becomes endogenous, then the government chooses its asset demands as well as  ${}^{1}_{B}$   ${}^{1}_{B}$  d<sub>gg</sub>; to maximize the expected utility of a representative agent i, under its budget constraint:

$$8 \atop \geqslant \max_{d_{gj}} \overline{Ev} + Ew(G)$$

$$\Rightarrow s.t. \int_{j=1}^{n-1} p_j d_{gj} \cdot p_g$$

According to the consumption table, the expected utility of the public good is given by:

$$Ew(G) = \sum_{j=1}^{rX+1} \frac{1}{S} w(d_{gj})$$

We get that the supply of public project and the demand for private assets are respectively:

$$1_{i} d_{gg} = \frac{\prod_{i=1}^{p} (p_{g} = p_{i})^{\frac{1}{2} = (1_{i} \frac{1}{2})}}{\prod_{i=1}^{p} (p_{g} = p_{i})^{\frac{1}{2} = (1_{i} \frac{1}{2})}}$$

$$(14)$$

$$d_{gi} = \frac{(p_g = p_i)^{1 = (1_i \ \frac{1}{2})}}{\prod_{i=1}^{p-1} (p_g = p_i)^{\frac{1}{2} = (1_i \ \frac{1}{2})}}$$
(15)

At the symmetric equilibrium under a price normalization  $p_g$   $\uparrow$   $p_{n+1}$   $\uparrow$  1; (14) and (15) become:

$$\%_{B} = \frac{n}{n + p^{1/2}(1_{i} \%)}$$

$$d_{gi} = \frac{1}{np + p^{1-(1_{i} \%)}}$$

Demands and supplies expressed by the private agents, as well as the marketclearing conditions, remain unchanged. Then the equilibrium price of private assets is:

$$p^{\pi} = 1$$

That leads to:

$$^{1}_{B}^{x} = \frac{n}{1+n}$$

The optimal level of privatization by sale of assets is strictly positive, strictly less than one.

Proposition 4. Without e $\$ cient taxation, the optimal level of privatization by sale of assets  $\$ ^ $^{\text{m}}_{\text{B}}$  leads to the ...rst best if and only if the size of the public sector is equal to the weight of the public good in the preferences, i.e. if and only if:

$$\frac{1}{n+1} = -$$

Proof. Let us report equilibrium private and public demands and supplies in the consumption table. We get the following consumption plan:

$$c^s = G^s = 1$$
= (n + 1) for every s 2 f1; :::; n + 1g  $c^s = G^s = 0$  for every s 2 fn + 2; :::; Sg

It coincides with the ...rst best if and only if the condition given in proposition 4 holds.

### C The optimal privatization mix without taxation

Proposition 5. Without e $\Phi$ cient taxation, if the size of the public sector is initially too high, there exists an optimal privatization mix (free distribution and sale of public assets) such that the economy reaches the ...rst best. Proof. There is free distribution and sale of public assets. Let  $\%_A$  be the share of the public property rights freely distributed among the n private agents.

Private agent i:  $\frac{1}{4}$ A is taken as given by the private agents. The program of a private agent i is:

$$\geqslant \max \frac{1}{S} \bigvee_{j=1}^{p} v(d_{ij}) + \frac{1}{S}v(d_{ig}) + \overline{Ew}$$

$$\geqslant \text{s.t.} \quad p_j d_{ij} + p_g d_{ig} \cdot p_i + p_g \mathcal{V}_A = n$$

where  $d_{ig}$  is the agent i's demand for public assets. In the CES case, with the price normalization  $p_g$  ´  $p_{n+1}$  ´ 1 we get the following expressions:

$$d_{ig} = \frac{p_i + \frac{1}{4} A = n}{n + \frac{1}{2} p_j^{\frac{1}{1}}}$$

$$i = 1$$
(16)

Government. For now 4/4 is treated as an exogenous variable. The government's program is:

8
$$\geq \max_{\overline{S}} \frac{1}{S} w(d_{gi}) + \frac{1}{S}w(d_{gg}) + \overline{Ev}$$

$$\geq s.t. \quad p_i d_{gi} + p_g(d_{gg}) \cdot p_g(1_i \%_A)$$

In the CES case under the usual price normalization, we get the following expressions:

$$d_{gi} = p_{i}^{\frac{1}{y_{i}-1}} \frac{1_{i} \frac{y_{i}}{y_{i}}}{n^{\frac{y_{i}}{y_{i}-1}}}$$

$$i = 1; \dots; n$$

$$d_{gg} = \frac{1_{i} \frac{y_{i}}{y_{i}}}{n^{\frac{y_{i}}{y_{i}-1}}}$$

$$i = 1 (17)$$

Market symmetry. The private agents have the same fundamentals. Then

$$p_i = p$$

for every i **6** g:

Equilibrium on the public property right market.

$$X^{0}$$

$$d_{ig} + d_{gg} = 1$$

Using (16) and (17) in the previous equation, we obtain the general equilibrium price for private assets:

$$p^{\pi} = 1$$

The equilibrium demands are

$$d_{ig}^{\pi} = d_{ij}^{\pi} = \frac{1 + \frac{1}{4}A = n}{n+1}$$
 (18)

$$d_{gg}^{x} = d_{gi}^{x} = \frac{1 i \frac{1}{A}}{n+1}$$
 (19)

Besides, we know that, by de...nition:

$$d_{qq} = (1_{i} \%_{A})(1_{i} \%_{B}) \tag{20}$$

Therefore from (19) and (20) we get the equilibrium level of privatization by sale of assets:

 $^{1}M_{B}^{x} = \frac{n}{n+1}$ 

What is then the level of voucher distribution (type A privatization)  $\frac{\pi}{A} > 0$  such that the above equilibrium corresponds to the ...rst best consumption plan? We must compare the general equilibrium allocation  $d_{ij}$  in (18) with the ...rst best  $(c^s)^{\pi}$  in (4). Under the initial condition  $1=(n+1) > -\frac{\pi}{2}$ ; the ...rst best is reached for:

$$\mathcal{V}_{A}^{\alpha} = n \frac{1}{n} \frac{\frac{3}{-n}}{\frac{-n}{1_{i}}} \frac{\frac{1}{1_{i} \cdot 1_{i}}}{\frac{1}{1_{i} \cdot 1_{i}}}$$

### D Ine¢ciency without taxation

Proposition 6. Without ectient taxation and under public inectiency, the total privatization is not optimal. There is a privatization mix (free distribution and sale of public assets) such that the economy reaches the taxless optimum. Furthermore the extent of the optimal mixed privatization increases with the inectiency degree.

Proof. First we compute the taxless optimum and the general equilibrium, then we compare them.

Taxless optimum. The public sector is assumed to be a less ectient manager, whatever kind of assets it holds; as a consequence, public good provision is always axected by the productivity parameter ®. The taxless optimum consumption plan (9) results from the following maximization program:

$$\underset{c^{s};G^{s}}{\underset{s=1}{\mathbb{F}}} \frac{1}{s}u(c^{s}; {}^{\otimes}G^{s})$$

$$\underset{s.t.}{\underset{c^{s};G^{s}}{\underset{s=1}{\mathbb{F}}}} \frac{1}{s}u(c^{s}; {}^{\otimes}G^{s})$$

$$\underset{s.t.}{\underset{c^{s};G^{s}}{\underset{s=1}{\overset{s}{\longrightarrow}}}} \frac{1}{s}u(c^{s}; {}^{\otimes}G^{s})$$

$$\underset{s.t.}{\underset{c^{s};G^{s}}{\underset{s=1}{\overset{s}{\longrightarrow}}}} \frac{1}{s}u(c^{s}; {}^{\otimes}G^{s})$$

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Under a CES speci...cation for the utility function, we obtain the consumption of private good:

$$(c^{S})^{\alpha} = \frac{\mathbb{R}}{\mathbb{R}^{n} + \frac{\mathbb{R}^{-n}}{1_{1}^{-n}}} \frac{\mathbb{R}^{-n}}{\mathbb{R}^{n}}$$
 (21)

Privatization mix. The program of the private agents is not a ected by the parameter <sup>®</sup>. The program of the government becomes:

Demands, supplies and thereby market-clearing conditions are not axected by ®: We get as above that:

$$p^{\pi} = 1$$

$$d_{ig}^{\pi} = d_{ij}^{\pi} = \frac{1 + \frac{1}{4}A = n}{n+1}$$

$$d_{gg}^{\pi} = d_{gi}^{\pi} = \frac{1}{n+1} \frac{\frac{1}{4}A}{n+1}$$
(22)

We get in particular that the equilibrium level of privatization by sale of assets remains unchanged:

$$^{14}_{B}^{\alpha}(^{\mathbb{R}}) = \frac{n}{n+1}$$

What is then the level of voucher distribution (type A privatization)  $\mbox{\ensuremath{\mbox{\sc M}}}^{\mbox{\sc a}}_A$  (®) such that the above equilibrium corresponds to the taxless optimum consumption plan? We must compare the general equilibrium allocation  $d_{ij}$  in (22) with (c<sup>S</sup>) in (21). We obtain that:

$$\mathcal{W}_{A}^{n}(\mathbb{B}) = n \frac{\frac{3}{\mathbb{B}^{-n}} \frac{1}{1_{1} \cdot \frac{1}{1_{2}}}}{n^{\mathbb{B}} + \frac{3}{\mathbb{B}^{-n}} \frac{1}{1_{1} \cdot \frac{1}{1_{2}}}}$$

It is then easy to check that:

$$4^{1}_{\Delta}(\mathbb{R}) > 0$$

if and only if

$$\frac{1}{1 + {}^{\text{®}\frac{1}{2}}n} > -$$

and that

$$^{1/4}_{A}(^{\circ}) < 0$$

The global extent of the optimal mix is given by

$$1_{i} (1_{i} \%_{A}^{x}) (1_{i} \%_{B}^{x})$$

As  ${\rm 1}\!\!/{\rm 1}{\rm 8}^{\rm m}$  does not depend on  $^{\rm (B)}$  the impact of  $^{\rm (B)}$  on the optimal extent is negative

28

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