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# Endogeneous Allocation of the Exit Option between Workers and Shareholders<sup>x</sup>

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#### **Abstract**

We deal with e¢cient allocation of the shut-down decision of a ...rm in which there is pro...t sharing. The paper can be considered as a complement to the literature on the endogenous ownership structure of the ...rm. We examine a variety of cases according to both di¤erent schemes of layo¤ compensation and various degrees of speci...city of human and physical capital. It appears that there are circumstances in which granting workers the decision to close can maximize the total payo¤ accruing to both contenders, with respect to the usual practice of shareholders decision making. Traditional conduct reveals an ine¢ency that may add to the well known principal-agent concern. Leaving the decision to close to shareholders gives rise to a deadweight loss, since a failure arises in the internal market for highly speci...c factors. Loss of control over the decision to exit is costly for shareholders. Proper compensation schemes can be devised for e¢-cient transfer and/or sharing of the closing decision.

JEL Classi...cation L20, D92

<sup>&</sup>lt;sup>\*</sup>An early version of the paper has bene...ted from presentations at the Universities

## 1 Introduction

Labor participation in ...rms' decisions takes di¤erent forms. It may be con...ned to pro...t-sharing or extended to key decision variables such as investment (Aoki, 1984), entry-exit and layo¤s (Lazear and Freeman, 1996).

Recent literature (Barrett and Pattanaik, 1989; Moretto and Rossini, 1995, 1997) has shown that the shape and extent of pro...t-sharing schemes are in‡uenced by the degree of ‡exibility of both factors of production and by institutional factors. By and large the responsibility and the ...nancial burden of the closure is mostly born by the shareholders. In these cases, the opportunity to shut-down, when pro...tability goes below a predetermined threshold level, acts as a credible threat and a¤ects distribution of organizational rent among workers and shareholders.<sup>1</sup>

Casual observation suggests that it may be quite a narrow perspective to assume that the allocation of the decision to close a ...rm is exogenously given and controlled only by the shareholders. As a matter of fact, there are other agents, either external or internal to the ...rm, who have some in uence on it. This is the case of local authorities, trade unions, joint boards consisting of workers and ...rm representatives. Even though all this is, by and large, more common for medium-large enterprises, in small size ...rms it can often be observed that the executive board does not completely share the views of shareholders because workers may have a voice in it because of closeness between employees and owners. Something similar happens in all cases of codetermination, in some ESOP (Employee Stock Ownership Plan) cases in the United States and in most Japanese-like ...rms where managers are mostly insiders who have gone up the whole career ladder within the same ...rm and are therefore nearer to workers' views (Drucker, 1976; Aoki, 1984). In Germany codetermination dramatically axects the behavior of many large ...rms as far as hiring and ...ring workers is concerned (Freeman and Lazear, 1994).

In all these cases workers are no longer passive vis à vis most of the

the two polar cases represented respectively by the traditional one where shareholders alone decide on closure and the extreme opposite where workers take the decision and /or have a veto power, there may exist a whole range of allocations of the shut down decision. Then, theoretically, the problem may be seen as one of optimal allocation of the shut down decision.

Traditionally, when shareholders carry out their closure threat they intict a loss to the workers who are laid o¤. E¢ciency requires that the loss that workers (in game-theoretic terms we name them the victims) su¤er be slightly smaller than the bene…t (future expected losses) shareholders (the threateners) get from the closure. If the loss is strictly higher, ine¢ciency, measured by a deadweight loss, arises. If that is the case we face a new form of ine¢ciency in the theory of …rm organization, which may be added to other cases such as those related to the principal-agent relationship.

In which circumstances does this happen? And, if so, is there any escape from it? We shall try to answer these questions, which are at the core of the paper, considering as a status quo the case where shareholders have the possibility of carrying out their closure threat at their earliest convenience.

By and large shutting down implies a private and a social cost and the coincidence of the two costs is ensured only in particular circumstances. The contender who is exogenously supposed to be the decision maker has an advantage since he can axect distribution of pro...ts. The victim may be willing to pay an amount slightly lower than the loss he suxers in order to condition or "buy" the right to decide. This appears quite consistent with Lazear and Freeman (1996) who maintain that "worker ownership can increase worker support for ecient ...rm policies, even on such a potentially divisive topic as layoxs". Our concern is somewhat similar. If workers are allowed to decide when the ...rm should stop, are there circumstances in which they may do so eciently? Or, are there cases in which the ...rm's policy can be agreed upon by workers as well? In this sense the paper may be considered a complement to the literature on the ...rm's endogenous ownership structure (Hart and Moore, 1990; Dow, 1988, 1993) since we examine the opportunity

by varying the institutional setting and the degree of speci...city of human and physical capital. The context is one of timing decisions of an irreversible investment with stochastic payo¤s. Much of the vast recent research that has considered this issue was recently surveyed by Pindyck (1991), Dixit (1992) and Dixit and Pindyck (1994). We associate it with pro...t sharing during activity and compensation schemes for laid-o¤ workers.

So far, the traditional practice of letting the owners have the right to decide has never been evaluated in terms of maximization of the total payo¤ accruing to both contenders. Nor has been considered the closure threat as a shut down option.

In the ...rst section we present the general model and we distinguish the case in which shareholders decide exit from the one in which workers take the hold. In section 3 we design a gain function for each contender. By comparing the two functions we get a net gain function. In section 4 we evaluate the net gain function in di¤erent scenarios and, accordingly, we trace the lines for a compensation scheme that may lead to e¢ciency, i.e. to maximization of total payo¤ for the two contenders (the Appendix proposes a continuous time repeated game representation of one of the many possible compensation schemes). We provide some conclusions in section 5. In

## 2 The basic model

In this section we lay out the general formulation of the model and analyse the contenders' objective functions. For simplicity we consider an incumbent ...rm which exhibits a constant-returns-to-scale technology and is endowed with a capital stock of in...nite life. Each period the ...rm produces one unit of output. Cost c; inclusive of labor payment, is known and constant. The labor force is, for the sake of simplicity, normalized to one.

Workers get a share of the pro...t or "organizational rent". The extent of pro...t-sharing may be considered either as the outcome of bargaining between workers and shareholders as envisaged by Aoki (1980, 1984), or more generations.

as renegotiation processes are highly costly, ...rms and workers cannot change the sharing rule continuously. Moreover, in the interest of both workers and shareholders, national legislation tends to limit the frequency in changes of sharing criteria (OECD, 1995).<sup>3</sup>

Revenue, coinciding with the market price, is uncertain and driven by a geometric Brownian motion:

$$dp_t = {}^{\mathbb{R}}p_t dt + {}^{1}\!\!\!/ p_t dz_t \quad \text{with } p_{t_0} = p_0 \text{ and } {}^{\mathbb{R}}; {}^{1}\!\!\!/ > 0;$$
 (1)

where  $dz_t$  is the standard increment of a Wiener process (or Brownian motion), uncorrelated over time and satisfying the conditions that  $E(dz_t) = 0$  and  $E(dz_t^2) = dt$ :

The operating pro...t (loss), as residual over the unit cost c, at time t is termed organizational rent and is a function of the market price:

$$\%(p_t) = p_t i c \tag{2}$$

In keeping with the above arguments, this residual is distributed between shareholders and workers according to a constant (over time) sharing rule. De…ning with  $0 < \mu < 1$  the distributive parameter of pro…ts going to shareholders, the premium earning per employee is simply:

$$\mathbb{C} w(p_t; \mu) = (1; \mu) \%(p_t) \ \ (1; \mu)(p_t; c) \tag{3}$$

As the market price may go below c equation (3) becomes negative, and workers and shareholders partake both pro...ts and losses in a symmetric way.<sup>4</sup>

tional legislation. Pro...t-sharing is compulsory in Mexico and partially also in France. In Canada it is linked to accumulation of retirement funds (OECD, 1995, Vaughan-Whitehead, 1995, Biagioli, 1995).

<sup>&</sup>lt;sup>3</sup>Moretto and Rossini (1997) analyse the case of a policy maker who uses pro...t distribution as a way of regulating the ...rm, calls the workers and the shareholders to renegotiate their distributive share through new bargaining if pro...ts reach a predetermined level.

<sup>&</sup>lt;sup>4</sup>A recent study undertaken by the OECD in major industrialized countries has shown that, among the ...rm characteristics relevant to the choice of a pro...t sharing scheme, a

When the ...rm shuts down, shareholders bear a lump-sum cost  $K_s = K_k + K_w$ : The capital loss su¤ered by shareholders due to abandonment of the economic activity for which the ...rm has idiosyncratic know-how is  $K_k$ . This amount is net of scrapping value, and/or shareholders' discounted value of future pro...ts associated with alternative asset investment from exit onwards. The legally required termination allowance the ...rm has to pay to laid o¤ workers is represented by  $K_w$ . These two capital losses constitute the cost of closure born by shareholders. Also the workers face an exit cost  $K_{11}$  which represents the loss due to their speci...c skill acquired in the ...rm. This is the loss of speci...c human capital that cannot be used elsewhere without su¤ering an adjustment cost lower than  $K_{11}$ . Also  $K_{11}$  may be considered net of the workers' discounted value of future earnings associated with an alternative job. Exit costs on both parts imply the existence of rents while the ...rm is in operation. We may therefore equally think in terms of rent-sharing as well as pro...t-sharing.

As for both actors there is an opportunity cost of abandoning now rather than waiting for new information about market demand conditions, the ...rm would rather decide to exit when these conditions become su¢ciently adverse, i.e. only if the price falls below a trigger value b < c which has to be endogenously determined. To this purpose we have to consider future opportunities vis à vis the exit cost. The trigger price is going to change according to who holds the decision to close and may be strongly in‡uenced by possible asymmetry between shareholders and employees as to the exit costs  $K_w + K_k$  and  $K_w$  i  $K_{II}$ . This asymmetry is the major source of con‡icting interests as to the timing of closing and, as a consequence, as to who should hold the option to close. The way sunk costs are allocated is crucial as to both the threatening power of the closing decision and the private and social cost of ending the activity.

As long as shareholders are homogenous in all respects and the relative share  $\mu$  remains constant over time, the shareholders' expected sum of discounted pro...ts up to the shut down is simply given by:

where 1/2 (> ®) is the cost of capital. On the other hand, incumbent employees are interested in the lifetime amount of earnings they can get by taking part in the ...rm's production. Under the simplifying assumptions: (a) that workers are risk neutral, (b) that the market wage w is constant over time and (c) that workers are ...red only when the ...rm closes, the level of lifetime income per worker can be represented as:<sup>6</sup>

$$L(p; \mu) = E_0 \sum_{0}^{\infty} [w + (1_i \mu)(p_{t_i} c)]e^{i t_i t_i} dt \ j \ p_0 = p + (5)$$

$$+ E_0 (K_{w_i} K_{II})e^{i t_i t_i} \ j \ p_0 = p$$

Finally, in both equations  $T(b) = \inf(t \cdot 0 \mid p_t \cdot b)$  indicates the (stochastic) stopping time at which the ...rm exits.

Some remarks on outside opportunities simplify matters. Since the workers' wage from alternative jobs can be expressed by  $\frac{w}{k}$ ; and we can set  $K_{II} = K_{II} \frac{w}{k} e^{i \frac{kT}{k}}$ ; the level of lifetime well-being of a worker may be ordered according to the expected discounted sum of the premium earnings up to the shut down. That is:

$$W(p; \mu) = E_{0} \int_{0}^{\pi} (1_{i} \mu)(p_{t} i c)e^{i\frac{1}{2}t} dt j p_{0} = p + (6)$$

$$+ E_{0} [(K_{w} i K_{I})e^{i\frac{1}{2}t} j p_{0} = p$$

where W (p;  $\mu$ )  $\int L(p; \mu)_i \frac{w}{b} > 0$ ; appears as a participation constraint.

## 2.1 Exit in the shareholders' hands

Let us consider ...rst the traditional case when the shut down option is owned by shareholders whose objective is maximization of the market value of the ...rm represented by (4). The stopping time can be speci...ed as  $T(b_s) = \inf(t \circ 0 \mid p_t \cdot b_s)$  where  $b_s$  stands for the shareholders' trigger exit price.

As the opportunity to keep the ...rm in operation can be considered an asset that is held by shareholders for a series of small intervals of time dt, for a given value of  $\mu$ ; the value  $S(p;\mu)$  must satisfy a non-arbitrage condition which requires that the sum of the returns on the investment, given by the dividend  $\pm ow \ \mu \%(p)$ dt plus the capital gain  $E(dS(p;\mu))$ ; equals the market return on capital investment  $\% S(p;\mu)$ dt: Since  $p_t$  is driven by (1), applying Ito's Lemma to dS the asset equilibrium condition yields the following di¤erential equation (Dixit and Pindyck, 1994, pag. 147-152):

$$\frac{1}{2} \frac{1}{4} p^2 S^{00} + {}^{\circ}pS^{0}_{i} / {}^{\circ}S = {}^{\circ}\mu(p_{i} c) \quad \text{for } p \ 2 \ [b_{s}; 1); \tag{7}$$

with boundary conditions:

$$\lim_{p! \to 1} [S(p; \mu)_{i} \mu^{\frac{p}{N_{i}}} \frac{c}{s}_{i} \frac{q}{N_{i}}] = 0$$
 (8)

$$S(b_s; \mu) = i K_s i (K_k + K_w)$$
(9)

$$S^{0}(b_{s}; \mu) = 0 \tag{10}$$

As usual, equation (8) states that, when the market price goes to in...nity the value of the ...rm must be bounded. The second term in (8) represents the discounted present value of shareholders' pro...t  $\ddagger$ ows over an in...nite horizon starting from price level p (Harrison, 1985, p.44). Boundary conditions (9) and (10) stem from consideration of optimal operation. The ...rst one, i.e. (9), says that when the price reaches the trigger level, at which it becomes convenient for the shareholders to exit ( $b_s$ ), the value of the ...rm must be equal to its liabilities (matching value condition). The second condition, i.e. (10), rules out arbitrary or suboptimal exercise of the option to exit at a di¤erent point (smooth pasting condition).

Since, from (8), the term  $A_1p^{-2}$  indicates the option value to abandon production, the constant  $A_1$  must be positive. Yet, the constant  $A_1$  as well as the trigger value  $b_s$  are determined by using the boundary conditions (9) and (10):

$$A_1(b_s) \wedge \mu A(b_s) = \mu \frac{1}{2} \frac{1}{\frac{1}{2} \ln b_s^{1_i - 2}} > 0;$$
 (12)

and

$$b_{s} = \frac{-\frac{1}{2} \frac{1}{\mu} \frac{1}{\mu} (c_{i} \frac{1}{\mu} K_{s})}{\frac{1}{\mu} (c_{i} \frac{1}{\mu} K_{s})}$$
(13)

To make the option to shut down viable for shareholders we add an assumption that guarantees that the exit price  $b_s$   $_{\mbox{\tiny s}}$  0:

Assumption 1.  $c\mu_i \ \%K_s \ c\mu_i \ \%(K_w + K_k) \ 0$ :

Trivial comparative statics follow.

Proposition 1 : 
$$\frac{db_s}{dK_s} < 0$$
; hence  $\frac{dA_1}{dK_s} < 0$ :

These results derive directly from (12) and (13) by inspection.  $K_s$  is the whole sunk cost born by shareholders; as it gets larger the ...rm stays longer in the market and the value of the option to exit decreases. Finally, substituting (12) and (13) into (11), we can write:

$$S(p; \mu) = \mu V_s(p; \mu) = \mu Ap^{-2} + (\frac{p}{\frac{V_s}{i} \otimes i} \frac{c}{\frac{V_s}{i}})^{-1}$$
: (14)

where  $V_s$  stands for the ...rm's market value before distribution when the exit policy is in the hands of shareholders.

Let us now consider workers, who do not have any intuence on the shut down option. We indicate the discounted sum of the premium earnings (6) with  $\hat{W}(p;\mu)$  to mark with the **b** that workers do not participate in the choice of the exit policy. The paper arbitrage condition pow requires that the

Since the exit policy is controlled by shareholders, boundary conditions reduce to (i.e. no smooth pasting condition holds):

$$\lim_{p! \to 1} [\hat{W}(p; \mu)_{i} (1_{i} \mu) \frac{\mu}{\frac{p}{k_{i} \otimes i} \frac{c}{k}}] = 0$$
 (16)

$$\hat{W}(b_s; \mu) = K_w i K_1 \tag{17}$$

By symmetry with (11), the solution has the form:

$$\hat{W}(p; \mu) = \hat{B}_1 p^{-2} + (1_i \mu) (\frac{p}{\chi_i \otimes i} \frac{c}{\chi}) \quad \text{for p 2 [b_s; 1]}$$
 (18)

The part of the workers' well-being attributable to the exit decision (possessed by shareholders),  $\hat{B}_1p^{-2}$ ; depends now on the size and magnitude of the net bonus  $K_{w\ i}$   $K_1$ : In fact, applying the value matching condition (17), we get:

$$\hat{B}_{1}(b_{s}) = i \left(1_{i} \mu\right) \left(\frac{1}{2} \frac{1}{\frac{1}{2} \frac{1}{\frac{1}{2} \frac{1}{1} e^{b_{s}^{1}}}{1}} b_{s}^{1_{i}^{-2}}\right) \left(\frac{c\mu_{i}^{-2} \frac{1}{2} \frac{1}{\frac{1}{2} \frac{1}{1} e^{b_{s}^{-2}}}{1}}{c\mu_{i}^{-2} \frac{1}{\frac{1}{2} e^{b_{s}^{-2}}} + (K_{w_{i}^{-1}} K_{l})b_{s}^{i}^{-2}} \right)$$
(19)

Considering now the ...rm's market value before distribution  $V_s$  and taking account of (11), (17), (18) and (19), we compute:

$$\hat{W}(p; \mu) = (1; \mu)V_s(p; \mu) + D_1(p) + D_2(p)$$
 (20)

where:

$$D_1(p) = \frac{1}{\mu} (K_k + K_w) (\frac{p}{b_s})^{-2} > 0; \quad D_2(p) = \frac{1}{i} (K_k + K_l) (\frac{p}{b_s})^{-2} < 0$$

Although  $D_1 + D_2 > 0$  is always positive whenever  $K_{w i} K_l > 0$ ; negative exects cannot be a priori excluded.: Therefore,  $D_1 + D_2$  provides, in equation (20), a measure of workers' well-being induced by the asymmetry between the exit costs born respectively by shareholders and employees, i.e.  $K_w + K_k$ 

## 2.2 Exit in workers' hands

Let us now consider the case where the shut down option is owned by workers, whose objective is maximization of their lifetime well-being (6). The exit time becomes now  $T(b_w) = \inf(t \ 0 \ j \ p_t \cdot b_w)$ ; where  $b_w$  is the workers' exit price. By using a procedure similar to the one adopted above, the lifetime well-being W is the solution of the following dixerential equation:

$$\frac{1}{2} \frac{3}{4} p^{2} W^{00} + {}^{\textcircled{m}} p W^{0}_{i} \text{ } \frac{1}{2} W = i (1_{i} \mu)(p_{i} c) \text{ for } p 2 [b_{w}; 1);$$
 (21)

with limit conditions:

$$\lim_{p! \to 1} [W(p; \mu)_{i} (1_{i} \mu)^{\mu} \frac{p}{\frac{p}{k_{i} \otimes i} \frac{c}{k}}] = 0$$
 (22)

$$W(b_w; \mu) = K_w i K_1$$
 (23)

$$W^{0}(b_{w}; \mu) = 0 \tag{24}$$

Letting  $B_1$  be a constant to be determined and  $\bar{a}_2$  the negative root of the characteristic equation  $\bar{a}_2$ ; the solution of (21) is given by:

$$W(p; \mu) = B_1 p^{-2} + (1_i \mu) (\frac{p}{\sqrt[M]{i} \otimes i} \frac{c}{\sqrt[M]{2}}) \quad \text{with p 2 [b_w; 1)}$$
 (25)

Applying the value matching condition (23) and the smooth pasting condition (24), we obtain:

$$B_{1}(b_{w}) \wedge (1_{i} \mu)B(b_{w}) = i (1_{i} \mu)\frac{1}{2}\frac{1}{\frac{1}{2}}\frac{1}{\frac{1}{2}}b_{w}^{1_{i}}^{1_{i}} > 0$$
 (26)

and

$$b_{w} = \frac{1}{2} \frac{\frac{1}{2} i^{*}}{2} (c + \frac{\frac{1}{2}}{2} (K_{w} i K_{1}))$$
 (27)

Proposition 2 If  $K_{w \ i} \ K_{I} > 0$ ; then  $\frac{db_{w}}{d(K_{w \ i} \ K_{I})} > 0$  and hence  $\frac{dB_{1}}{d(K_{w \ i} \ K_{I})} > 0$ :

If the (positive) net bonus increases, workers would like to exit earlier. The increase in the net transfer boosts the value of the exit option to workers. The opposite happens if  $K_{w\ i}\ K_{l}<0$ : Substituting (26) and (27) into (25), we write:

$$W(p; \mu) = (1_{i} \mu)V_{w}(p; \mu) = (1_{i} \mu)^{2} Bp^{-2} + (\frac{p}{\chi_{i}^{8}} \frac{c}{\chi})^{3}; \qquad (28)$$

where  $V_{\rm w}$  indicates the ...rm's market value before pro...t distribution and exit policy owned by workers.

Let us now turn back to shareholders. Referring to (4) which we indicate with  $\hat{S}(p; \mu)$  since shareholders do not decide the exit policy, the non arbitrage condition leads to:

$$\frac{1}{2} \frac{3}{4} p^2 \hat{S}^{00} + {}^{\circ}p \hat{S}^{0}_{i} / {}^{\circ}\hat{S}^{0} = {}_{i} \mu(p_{i} c) \quad \text{for p 2 [b_{w}; 1);}$$
 (29)

Shareholders' optimization problem is similar to the one seen in the previous section. The boundaries are

$$\lim_{p! \to 1} [\hat{S}(p; \mu)_{i} \mu^{\mu} \frac{p}{\chi_{i}^{0}}_{i} \frac{c}{\chi}^{\eta}] = 0;$$
 (30)

$$\hat{S}(b_w; \mu) = i K_s i (K_k + K_w):$$
 (31)

The solution is:

$$\hat{S}(p; \mu) = \hat{A}_1 p^{-2} + \mu (\frac{p}{\sqrt{h_i} |_{B}} i \frac{c}{h}) \quad \text{for p 2 [b_w; 1)};$$
 (32)

while applying the value matching condition (31) we get:

where:

$$D_{3}(p) = i \frac{\mu}{1 i \mu} (K_{w i} K_{l}) (\frac{p}{b_{w}})^{-2}?; D_{4}(p) = i (K_{k} + K_{w}) (\frac{p}{b_{w}})^{-2} < 0$$

Again, although the asymmetry due to the respective exit costs and a reversed allocation of the shut down option, may induce a reduction in the ‡ow of pro…ts accruing to shareholders, i.e.  $K_{w\,i}$   $K_{l} > 0$  assures that  $D_{3} + D_{4}$  is always negative, positive exects cannot be a priori excluded. Then we may indicate  $D_{3} + D_{4}$  as the shareholders' loss (gain) induced by the exit cost asymmetry.

From (14), (20), (28) and (34), it is apparent that the threatening power has a distributive exect. Carrying out the threat (i.e. closing) by one of the contenders is privately optimal, but we do not know whether and in which circumstances the individually optimal program leads to maximization of the two contenders aggregate payox. The next section will be devoted to analysis of the eciency of workers' and shareholders' choices by using a gain function.

# 3 The (net) gain function

Whenever we attribute the decision to close to one contender we actually give him the power to carry out a threat (Moretto and Rossini, 1995). Carrying out the threat is privately optimal. For instance, shareholders receive a net bene...t with respect to the alternative case in which workers decide to close. Workers lose when shareholders decide. They are laid ox without having the possibility to halt the shareholders's decision. As Klein and O'Flaherty (1993) and Shavell and Spier (1996) have pointed out, this situation may give rise to inecciency if the bene...t shareholders get when they exercise their threat (close) is strictly smaller, in absolute value, than the loss workers bear. Then, it is in the interest of both contenders to ".....negotiate around the inectioners and avoid the dead weight loss associated with carrying out

conditions will allow us to ...gure out some institutional scenarios providing suggestions to solve real questions of the ...rm's internal organization. For this purpose we resort to individual gain functions and then to a net (aggregate) gain function. The individual gain function indicates how much a contender holding (not holding) the decision to close bene...ts (losses) with respect to the case in which he does not (he does) control the decision. The net gain function aggregates algebraically the two individual gain functions, providing information as to the desirability of attributing the decision to one of the two contenders. If the bene...t from closing is smaller than the loss in‡icted to the victim we face a deadweight loss and total payo¤ is not maximized.

Taking for granted that the decision to close should be attributed to the shareholders (our benchmark position) is equivalent to assuming that this deadweight loss never shows up. In this section we shall see that this is not always the case and that, because of the nonlinerarity of the abandonment option coupled with the asymmetry of the exit costs, the usual conduct rule of a ...rm owned and directed by shareholders may lead to ine¢ciency.

Let us ...rst consider the gain function of shareholders de...ned as the difference  $S_i$   $\hat{S}$ : Substituting (11) and (32) we obtain:

$$S(p; \mu)_{i} \hat{S}(p; \mu) = (A_{1i} \hat{A}_{1})p^{-2} > 0;$$
 (35)

By the same arguments, de...ning the gain function of workers as W  $_{i}$   $\hat{W}$ ; substituting (18) and (25) we get:

$$W(p; \mu)_{i} \hat{W}(p; \mu) = (B_{1}_{i} \hat{B}_{1})p^{-2} > 0$$
 (36)

As long as the discounted value of expected pro...t, when the ...rm is active forever, is independent of who has the right to decide the exit the dixerence concerns only the part of the value of the ...rm coming from the shut down option, that is:  $A_1$  i  $\hat{A}_1$  and  $B_1$  i  $\hat{B}_1$ : Moreover, as the optimal policy is to exit at  $b_s$  for shareholders and at  $b_w$  for workers, by Bellman's principle we realize that  $A_1$  i  $\hat{A}_1 > 0$  and  $B_1$  i  $\hat{B}_1 > 0$ : Therefore, for any given price

exit. Traditional organization is e $\$ cient and no deadweight arises. If G < 0 the reverse applies and the workers' loss is larger in absolute terms than the shareholders' gain. Maximization of the total payo $\$ mipplies attributing the closing decision to workers, for instance, by giving them veto power. Otherwise the deadweight loss appears equal to G: If G = 0 it is irrelevant who decides to exit. Contenders agree on the exit decision.

Recalling from (12) and (33) (or equivalently (14) and (34)) that constants  $A_1$  and  $\hat{A}_1$  are functions of the trigger prices  $b_s$  and  $b_w$ , their dimerence can be simplimed as:

$$A_{1 i} \hat{A}_{1} = A_{1}(b_{s})_{i} A_{1}(b_{w}) + \frac{\mu}{1_{i} \mu}(K_{w i} K_{l}) + (K_{k} + K_{w})^{3} b_{w}^{i-2}$$
 (38)

The gain from holding the exit option for the shareholders can be split into two parts. The ...rst captures the dixerence (positive or negative) in the value of the shareholders' shut down option evaluated at two distinct trigger prices, one chosen optimally by shareholders and the other chosen by workers  $A_1(b_s)_i$   $A_1(b_w)$ : The second part gives the gain or loss accruing to shareholders due to the asymmetry in sunk exit costs.

Symmetrically, for the workers from (19) and (26) (or equivalently (20) and (28)) we can write:

$$B_{1 j} \hat{B}_{1} = B_{1}(b_{w})_{j} B_{1}(b_{s}) + \frac{1}{i} \frac{1_{j} \mu}{\mu} (K_{k} + K_{w})_{j} (K_{w j} K_{l})^{3} b_{s}^{j-2}$$
(39)

 $B_1(b_w)_i$   $B_1(b_s)$  is the gain or loss in exit option evaluated in correspondence of the two trigger prices when the decision to exit is granted to workers. The second part accounts for the exit costs asymmetry between the two contenders

Since 
$$A_1(b_s) + B_1(b_s) = i^{\frac{1}{2} \frac{1}{b_i} \frac{1}{8}} b_s^{1i^{-2}} \land A(b_s)$$
 and  $A_1(b_w) + B_1(b_w) =$ 

## 4 Optimal allocation of the exit decision

We now see how the net gain function (40) varies as we change both the institutional setting and the degree of factor speci...city, captured respectively by the parameter  $\mu$  and the exit costs  $K_w$ ,  $K_k$  and  $K_l$ : The question we face may be considered a complement to the literature on the ...rm's optimal ownership structure (Hart and Moore, 1990; Dow, 1986, 1993) in environments with diæerent degrees of factor speci...city and diæerent compensation schemes for layoæs.

To reduce the complexity of the net gain function (40) we consider 3 "main" cases which may be taken as representative of the totality of factor speci...city within the ...rm. In the ...rst capital and labor have the same degree of speci...city. In the second capital is speci...c while labor can be deployed elsewhere without costs. The third is the opposite of the second. Numerical simulations have been undertaken in these cases.

## 4.1 Equal speci...city between capital and labor

Capital and labor can be deployed elsewhere by bearing a sunk cost equal for both of them. Laid-ox labor receives a positive compensation. That is:

Assumption 3. 
$$K_k = K_1 > 0$$
 and  $K_w > 0$ :

Before analyzing the net gain function G, we show that under assumptions 1, 2 and 3 the feasible set where the exit option is viable for both actors can be split into two subsets according to whether the shareholders' trigger value is higher or lower than the workers' trigger value. Considering the ratio of the two trigger prices, from (13) and (27) we get:

$$\frac{b_{w}}{b_{s}} = \frac{c + \frac{1}{1_{i} \mu} (K_{w i} K_{l})}{c_{i} \frac{1}{\mu} (K_{w} + K_{k})}.$$
(41)

If  $K_w > K_1$  workers receive a positive net exit bonus and wish to exit

#### FIGURE 1 ABOUT HERE

Parallelogram ABCE indicates the area where  $b_w > b_s$ ; triangle CDE where  $b_w < b_s$ , while along the line CE we have  $b_s = b_w$ .

The net gain function (40), under assumption 3 and normalization  $K_1 = K_k = 1$ ; becomes:

$$G(\mu; 1; K_{w}) = A(b_{s})_{i} B(b_{w}) + \left[\frac{1_{i} 2\mu}{1_{i} \mu} + \frac{1}{1_{i} \mu} K_{w}\right] b_{w}^{i^{-2}} + (42)$$

$$+ \left[\frac{1_{i} 2\mu}{\mu} + \frac{1}{\mu} K_{w}\right] b_{s}^{i^{-2}}$$

In Figure 1 we have also traced the net gain function  $G(\mu; 1; K_w) = 0$  using dashed line GG. The values of the relevant parameters follow Dixit (1989): the operating cost of the productive activity amounts to 30% of the capital exit cost (i.e.  $c = 0.3K_k(K_l)$ ); the discount rate is ½ = 0.1. To avoid paradoxical results due to presence of in‡ation in the price process but not on the side of costs, we set ® = 0. The price's instantaneous volatility is ¾ = 0.25 (for instance 25% per year) so that the price elasticity of the shut down option becomes  $\frac{\pi}{2}$  is 3:

Above and on the right of GG the gain shareholders obtain by deciding to exit is larger than what workers would get in the same role, i.e. G > 0: Below and on the left of GG it is just the opposite, i.e. G < 0. Noting that G(0.5; 1; 0) = 0; from Figure 1 we can distinguish three areas within the feasible set.

The ...rst one, indicated by the parallelogram ABCE; where G>0: If shareholders own the exit decision (benchmark case) they have a greater advantage than what workers would have in the same role. The time horizon of shareholders is longer than that of workers (and consequently also the life of the ...rm), i.e.  $b_w>b_s$ .

payo¤ maximization. However, as the workers' net bonus is negative the ...rm's expected life is shorter than what it would be under workers' control.

These results and in particular the one highlighted by the second area that constitute the core of the paper can be summarized in the following proposition:

Proposition 3 Under assumption that both physical and human capital have the same degree of speci...city ( $K_k = K_l$ ) we ...nd that: There are combinations of pro...t distributions and exit costs where the traditional conduct of shareholders deciding to exit does not maximize the total payo¤. In this case laid-o¤ workers receive an exit compensation lower than their exit sunk cost ( $K_w < K_l$ ); which induce them to desire a longer life for the ...rm to recover losses. It would be better for the players to negotiate and avoid the deadweight loss associated with carrying out the threat of closing too soon.

## 4.2 Capital non speci...c, labor speci...c

In this case there is a strong asymmetry in favor of shareholders. Capital is reversible while labor can be deployed elsewhere by bearing a sunk cost. Labor receives a positive compensation when the ...rm stops production.

Assumption 4.  $K_k = 0$ ;  $K_1 > 0$  and  $K_w > 0$ :

Under assumptions 1, 2 and 4, the feasible set where the exit option is viable for both actors can be split into two subsets according to whether the shareholders' trigger value is higher or lower than the workers' trigger value. From (41), when  $K_w > K_I$  workers wish to exit earlier than shareholders for the entire set of parameters. If  $K_w < K_I$  workers would like to exit earlier only if  $\frac{K_w}{K_I} > \mu$ :

Normalizing  $K_1 = 1$ ; the feasible set for the trigger prices can be represented by the area ABCD in Figure 2 wherein both trigger prices  $b_s$  and  $b_w$ 

$$+[\frac{1}{u}K_{w}+1]b_{s}^{i}$$

Noting that G(0;1;0)=0 and that G>0 to the right of the line GG in Figure 2, we can distinguish two areas. The ...rst one is on the left of GG and below AB; where G<0: If workers decide to exit they gain more than what shareholders lose. Unlike the previous case, here  $b_w>b_s$ : Workers receive a negative net bonus  $(K_w<K_I)$ , but the low level of the share parameter  $\mu$  speaks in favor of shareholders, who have a larger (per unit of time) exit cost  $\frac{\nu_k}{\mu}K_w$  (even if  $K_k=0$ ) than their contenders. Then they would let the ...rm live longer than workers (see equation (41)). The second area is indicated by the remainder of the parameter set on the right of GG; where shareholders show a higher gain: G>0, inside the triangle ACD: The owners do not let the ...rm live longer since  $b_w< b_s$ : Aggregate payox maximization does not go hand in hand with the longest possible life expectancy of the ...rm.

#### FIGURE 2 ABOUT HERE

We then summarize:

Proposition 4 Under the assumptions that labor is speci...c while capital is not, we ...nd that: There is a small area at low levels of  $\mu$  and  $K_w$  where ecciency would require letting workers take over the exit policy. Laid-ox workers receive a compensation lower than their exit cost  $(K_w < K_l)$ , while, if they stay active they receive a high pro...t share  $(1_i \ \mu)$  which reduces substantially their per unit of time exit cost  $\frac{\hbar}{1_i \ \mu} (K_w \ i \ K_l)$ : They, then, exit earlier than shareholders. A similar short sightedness is shown by shareholders in a near area where G > 0. In both cases maximization of the total payox does not coincide with the ...rm's longest life expectancy.

Assumption 5.  $K_k > 0$ ;  $K_l = 0$  and  $K_w > 0$ :

From (41) we see that the level of the trigger set by workers is larger than the one set by shareholders, i.e.  $\frac{b_w}{b_s} > 1$ : Then, under assumptions 1, 2 and 5, the feasible set where the exit option is viable for both actors is given by the triangle ABC in Figure 3. Setting  $K_k = 1$ , the net gain function (40) becomes:

$$G(\mu; 1; K_w) = A(b_s)_i B(b_w) + [1 + \frac{1}{1_i \mu} K_w] b_w^{i-2} + (44)$$
$$+ [\frac{1_i \mu}{\mu} + \frac{1}{\mu} K_w] b_s^{i-2}$$

In this case we just get one area, the triangle ABC where G>0: If shareholders decide to exit they do so e $\Phi$ ciently and this is consistent with a longer ...rm's expected life, since  $b_w>b_s$ . This is the traditional case analyzed by Moretto and Rossini (1995).

#### FIGURE 3 ABOUT HERE

Then we write:

Proposition 5 When labor is not ...rm speci...c and the cost of exit is born entirely by shareholders, e $\oplus$ ciency requires that shareholders control exit. Yet, life expectancy of the ...rm is longer since  $b_w > b_s$ :

# 5 Towards an agreed upon e¢cient exit policy

the joint organizational rent. We have seen in the previous section that the ...rm may stay on the eccient frontier if ownership by shareholders is in some circumstances delinked from control over the ...rm's life expectancy.

Even if we take for granted the traditional institutional environment with closure in the hands of owners, there seems to be a possibility for the shareholders themselves to be better ox if they switch to a dixerent allocation of the decision to exit. Take for instance the case seen in Proposition 3 where  $b_w < b_s$ . If shareholders controlled exit they would stop production earlier than workers. In this case the loss of workers is higher (in absolute value) than the shareholders's gain. It may be in the interest of workers to make an oxer to shareholders to let the ...rm live longer by increasing the well being of workers and shareholders at the ...rm. But, in the absence of a binding commitment any lump sum transfer will be inecient (Klein and O'Flaherty, 1993 and Shavell and Spier, 1996). The victims, workers, know that the threateners, shareholders, have an incentive to carry out the threat, stopping the activity, the ...rst time the price hits the lower barrier b<sub>s</sub>. This is intuitively apparent since closing the ...rm is equivalent to putting an end to the game played by shareholders and workers. Shareholders have the power to set the time horizon of the game, while workers do not share this power. If the payment by workers is made the ...rst time p<sub>t</sub> hits b<sub>s</sub> immediately after shareholders would strictly prefer to carry out the threat regardless of the (previous) payment made by workers, unless  $p_t > b_s$ . On the contrary, if the parties agree that the payment is due just when p<sub>t</sub> hits b<sub>w</sub> then workers won't make any payment. By backward induction the same outcome appears for any scheme with a ...nite number of compensations. Workers do not have any incentive to pay in order to delay closure. Threateners do not expect to receive any compensation, and then it is optimal for them to carry out the threat the ...rst time the price hits b<sub>s</sub>: In game-theoretic terms this means that the unique subgame-perfect equilibrium is ine¢cient since the threat is carried out despite the fact that the victim's loss may or may not be greater than the threatener's payox. 11

for workers to "subsidize continuously the shareholders" till the price hits the workers' optimal lower barrier  $b_w$ ; and then exit. In terms of operating pro…ts (losses), as long as the market price  $p_t$  stays above  $b_s$  nothing is done. If ever  $p_t$  goes below  $b_s$  workers should give up part of their organizational rent in favor of shareholders: workers pay a compensation  $s_t \ \ \, 0$  to keep shareholders indi¤erent with respect to exit. This compensation should go on, until the (exogenous) price process  $p_t$  hits, for the …rst time, the workers' lower barrier  $b_w$ : When  $b_w$  is touched the compensation stops and both contenders should be at their indi¤erence position, i.e.  $S(b_s; \mu) = i \ K_s$  and  $W(b_w; \mu) = K_{wi} \ K_l$ : Compensation is triggered at  $T_s$  and stops at  $T_w$ : closure maximizes the total payo¤ of the two contenders. 12

This is the scheme proposed, in a discrete-time and constant-payo¤s game, by Shavell and Spier (1996). It is quite easy to show the e⊄ciency of their scheme if the threateners use a simple trigger strategy with maximal punishments: Constant payment streams over time a are made by the victim and threats are never carried out in equilibrium (proposition 2, p.12).<sup>13</sup>

Although referring to the Shavell and Spier's scheme can be appealing, the framework where here shareholders and workers make their decisions is quite di¤erent. First, decisions must be taken in continuous time. This requires a re…nement of the notion of trigger strategy to deal with a continuous time repeated game.<sup>14</sup> Continuous time can be seen as discrete-time with a length

 $<sup>^{12}</sup>$ It may be easy to design a compensation when  $b_w > b_s$  (see proposition 4). Workers would exit at  $b_w$ : However, the decision is in the hands of shareholders and they must wait till the price falls to  $b_s$ : In this case the compensation is simply a lump sum transfer to keep the shareholders indi¤erent at  $b_w$ ; i.e.  $S(b_w; \mu) + s = S(b_s; \mu)$ :

<sup>&</sup>lt;sup>13</sup> The simple trigger strategy with maximal punishment used by Shavell and Spier (1996) requires that if the victim deviates by paying less than the equilibrium subsidy, the threathner belives that the victim will pay nothing in the future, and the victim belives that the threathner will carry out the treat at his ...rst opportunity. After a single deviation, the continuation equilibrium becomes the ine⊄cient stationary equilibrium.

In Shavell and Spier, the eccient subgame-perfect equilibrium is characterized by a constant per-period payment within a range which depends on the magnitude of the discount factor. When the per-period payment is at its lower bound, the threatener is as well or as

of reaction (or information lag) that becomes in...nitely negligible to allow the threateners to respond immediately to the workers' actions.<sup>15</sup>

Second, the compensation takes place within a ...nite (yet stochastic) timespan,  $(T_{w\ i}\ T_s)$ , but in continuous time. Therefore a participation constraint by workers must be determined: Their payo¤ must be larger with the compensation scheme than if they exit at  $b_s$ :

Third, by the stochastic nature of the game, neither player is able to perfectly predict the value of the state variable  $p_t$  at each date: Therefore the payment made by workers is contingent upon realizations of  $p_t$  and may depend on the price history. Yet, since the market price follows a random walk there is, for each time interval of small length dt; a constant probability that the price will move up or down, i.e. that the game will continue one more period. That is, the game ends in ...nite (stochastic) time with prob-

A p\_! A p\_!

<sup>&</sup>lt;sup>15</sup>We may refer either to Simon and Stinchcombe (1989) or to Bergin and MacLeod (1993) contributions. In the former a class of continuous strategies is de...ned so that any increasingly narrow sequence of discrete-time grids generates a convergent sequence of game's outcomes whose limit is independent of the sequence of the grid. In the latter a class of inertia strategies represent a delay in response: that is an action an agent chooses at time t must also be chosen by the agent for some small period of time after t; with this small period of time tending to zero.

<sup>&</sup>lt;sup>16</sup>The idea behind a stochastic game is that the history of the game at each period can be summarized by a state variabale (price) that follows a Markov process, and current payo¤ depends on current action (subsidy). A perfect equilibrium of a stochastic game allows the strategies of each player to be functions of the (entire) history of the game while a Markov perfect equilibrium concerns a smaller class of strategies where the past in‡uences current actions only through the current realization of the state variable.(Fudenberg and Tirole, 1991, p. 503-504).

 $<sup>^{17}</sup>$  Applying Itô's lemma to  $P_t=\ln p_t$ ; where dp\_t is de...ned by (1) we get that, for initial condition  $P_{t_0}=\ln p_{t_0}$  and for any time t>0,  $P_t$  is normally distributed with mean ( $P_{t_0}+^1t$ ); where  $^1=^{\circledR}i$   $\frac{1}{2}\%^2$ ; and variance  $\%^2t$ : Yet, dP\_t is derived as the continuous limit of a discrete-time random walk, where in each small time interval of length  $\Phi t$  the variable P either moves up or down by  $\Phi h$  with probabilties (Cox and Miller, 1965, pp. 205-206):

ability one, but everything is as if the horizon were in...nite. Workers ...nd convenient at each instant t to continue the game paying a compensation to shareholders until the participation constraint bites. This may happen before  $T_w$  is touched. Workers will then stop the payment and let the shareholders close the ...rm.

Several compensation mechanisms can be devised, once the participation constraint is satis...ed, where the initial holder of the decision is able to obtain a rent as a result of a lack of a market allocation of the shut-down decision. In the Appendix a compensation scheme is devised, applying a one-sided regulator  $s_t$  0 to the state variable  $p_t$ : Referring to the formalization of regulated stochastic processes (Brownian Motion) by Harrison and Taksar (1983), and Harrison (1985), the subsidized price  $p_t$   $p_t$   $p_t$   $p_t$  is obtained from  $p_t$  by imposition of a lower control barrier at  $p_t$  with the compensation de...ned as:

 $1 + s_t \cdot \max_{T_{s} \cdot v \cdot t} \frac{\mu}{p_v} \P$ 

The subsidy  $s_s$  increases faster enough to keep  $p_t$  always greater than  $b_s$ ; and indicates the cumulative amount of control (subsidy) exerted on the sample path of  $p_t$  up to time t: That is, the subsidized price  $p_t$  equals the amount by which  $p_t$  exceeds the minimum value of  $p_t$  over the interval  $[T_s;t]$  (see ...q.4): The Appendix also shows the eCeiency and the subgame-perfectness

 $Pr[\Phi p = (e^{i \Phi h} i 1)p] = \frac{1}{2} n \frac{\mu}{1 i \Phi h}$ 

<sup>18</sup> It is well known that in...nitely repeated games are equivalent to repeated games that terminate in ...nite time. At each period there is a constant probability that the game continues (Fudenberg and Tirole, 1991, p.148). Consider again the price process P<sub>+</sub> = In p<sub>+</sub>:

of the equilibrium where the magnitude of the subsidy is related to the history of the game and to past price realizations.

All these schemes dixer by the extent of the rent shareholders are able to reap. The rent is due to the commitment of employees to pay a subsidy to shareholders. The closing decision has a cost for the contender not controlling it who may be willing to "buy" the decision. The possessor of the decision to close receives a rent.

These compensation devices may become important since, as we pointed out in the introduction, there are many cases in which workers have directly or indirectly a voice in the closing decision. The extreme situation may be that in which workers have some veto power on the shareholders' closing decision. This leads just to the opposite of what was seen above. If workers would like to exit earlier they may do so by guitting. In that case it could be in the interest of shareholders to make an oxer to workers to let the ...rm live longer by avoiding massive guitting. There results an increase in the well being of workers and shareholders (for example in the ...rst area with equal speci...city between the two factors or proposition 5). In a world in which workers share pro...ts and losses the ...rm may be faced with massive quitting. Workers may be halted by increasing K<sub>w</sub> (since this is received if the ...rm closes but not if they voluntarily guit). Lowering K<sub>1</sub> through retraining that makes employment elsewhere less costly is not in the interest of the ...rm. In other words, as Lazear and Freeman (1996) have observed, it is possible to design ‡exible organizations with the consent of workers even when they have some conditioning power.

However these compensation schemes are far from being easily implemented since, whenever we change  $\mu$  and/or  $K_w$  also trigger prices change and the optimal plans are revised by both contenders.

We must actually say that once the allocation of the exit decision is in the hands of one of the two contenders it may be quite di¢cult to avoid falling into ine¢cient practices unless we are able to ...nd the proper compensation mechanism to shift responsibility to the other contender who is contingently

on endogenous ...rm's ownership structure, in this case employees are better ox by self-management (Dow, 1993). If self-management seems too a radical solution, letting closure be decided jointly may be a clear improvement.

## 6 Conclusions

We have tried to answer a question concerning the optimal organization of the ...rm as far as closing is concerned. The issue is complementary to the literature on the optimal ...rm's ownership structure. We have con...ned our attention to the cases in which employees get a ...xed share of the organizational rent or pro...t. Closing down axects the welfare of workers and shareholders in dixerent ways. The control over the closing decision has different opportunity costs according to who holds it. Respective sunk costs of shareholders and employees, i.e. the relative degree of factor speci...city, and the institutional environment represented by severance rules are crucial. Outside options make each agent prefer to stay rather than leave before or after the other contender. The decision to close plays the role of a threat that may in‡uence the pro...t share distribution within the ...rm, as shown by Moretto and Rossini (1995).

Taking for granted that owners are the sole subject entitled with the closing decision implies assuming away an ine⊄ciency in ...rm organization that may be quite large and comparable to that of principal-agent kind. To show that we set up a taxonomy in terms of the maximization of the total payo¤ of both contenders as to the decision to close. We ...nd that if we were to design an optimal distribution of the decision to close, in some cases we would have to take it away from shareholders, as, for instance, when the degree of speci...city of human capital is fairly high vis à vis physical capital. Otherwise an ine⊄ciency arises.

We take for granted that the most common institutional setting associates property with the right to close. Several compensation schemes can be designed as a way out of the inettiency that this may give rise in par-

There are no handy escape routes from ine¢cient allocation of the exit decision once it has been taken for granted. In some cases the given allocation of the decision to close gives rise to a deadweight loss. Avoiding this makes the holder of the decision able to reap a rent out of most compensation schemes. In this sense history matters. Present institutional settings are justi...ed because most ...rms start their activity with highly speci...c physical capital and non speci...c human capital. Human capital becomes speci...c afterwards while physical capital is speci...c from the beginning.

An open strand of research comes from the fact that the credibility of the shut down threat should not be taken for granted because it implies that the ...ght for ownership of the decision to close has already taken place while it may, in some context, be an open struggle that may take place simultaneously with determination of the share parameter.

# A Appendix

This appendix proposes a compensation mechanism by which workers subsidize shareholders to avoid them closing the ...rm, when closure implies a loss to workers larger (in absolute value) than the gain shareholders get. This is the case expressed in proposition 3, when  $b_w < b_s$ :

The compensation scheme corresponds a perfect equilibrium belonging to the class of e $\$ cient perfect equilibria (which may be very large) for the continuous time threat-game described in the text. The compensation mechanism ...Ils workers' desire of capturing part of the deadweight loss by keeping shareholders at their indi $\$ erent position  $S(b_s;\mu) = i$  ( $K_k + K_w$ ); until the price hits the workers' optimal lower barrier  $b_w$ :

To avoid complications we see the continuous-time representation as discrete-time with a reaction (or information) lag that becomes in...nitely negligible. That is, the treatheners are able to respond immediately to the workers' actions. <sup>19</sup> Finally, we begin assuming that the participation constraint is never binding.

Let us start describing the compensation mechanism.

As long as the market price  $p_t$  stays above  $b_s$  nothing is done. If ever  $p_t$  goes below  $b_s$  workers give up part of their organizational rent in favor of shareholders. The transfer is the negative increment  $dp_t$  that allows the price process  $p_t$  to stay at  $b_s$ : Formally, we de…ne<sup>20</sup> a regulated process  $p_t$ ; as:

$$p_t \cdot p_t Z_t$$
; for  $p_t 2 [b_s; 1)$  (45)

or in terms of compensation:

$$s_t(p_t; Z_t) = p_t i p_t (Z_t i 1)p_t$$

where:

<sup>2</sup> i)  $Z_t$  is an increasing and continuous process, with  $Z_0 = 1$ ;

A crucial feature of this setup is that as the regulator  $Z_t$  depends only on the primitive exogenous process  $p_t$  also for the endogenous regulated process  $p_t$  the strong Markov property hold (Harrison, 1985, proposition 7, pp.80-81).

The shareholders' expected sum of discounted pro...ts with compensation paid by workers, up to the shut down, becomes (Harrison, 1985, p. 84; Moretto, 1995, p. 100):

$$dp_t = {}^{\circledR}p_t dt + {}^{\ggg}\!\!\!/ p_t dz_t + \frac{p_t}{Z_t} dZ_t \quad with \ p_0 = p_0 = p$$

The process  $Z_t$  describes the price compensation. Then  $\frac{p_t}{Z_t}dZ_t$  is the in...nitesimally small level of organizational rent given up by workers to let the current pro...t distributed to shareholders to stay above the level  $\mu(b_{s\;i}\;c)$ : In fact, by (45), if  $p_t=b_s$ ; we get  $dp_t=0$  and the rate of variation of  $Z_t$  is equal to that of  $p_t$  to keep  $p_t$  constant.

<sup>&</sup>lt;sup>21</sup>By Itô's Lemma applied to (45) we get:

or:22

$$S^{c}(p; p; \mu) = g(p; \mu) i g(p_{T_{w}}; Z_{T_{w}}; \mu) i E_{0} K_{s}e^{i \frac{1}{2}T_{w}} = \frac{2}{34}$$

$$= E_{0} \mu(p_{t i} c)e^{i \frac{1}{2}t}dt i$$

$$i E_{0} \mu(p_{t i} c)e^{i \frac{1}{2}t}dt i E_{0} K_{s}e^{i \frac{1}{2}T_{w}}$$

$$(48)$$

where, the stopping time can now be speci…ed as  $T_w = \inf(t \ \ 0 \ j \ p_t \cdot b_s; \ Z_t \ \ \ p_t = p_t \cdot b_s = b_w)$ , in order to account for the compensation Both trigger levels  $p_{T_w} = b_s$  and  $p_{T_w} = b_w$  determine the stopping time from which we can immediately see the dependence of  $S^c$  on the two processes  $p_t$  and  $p_t$  .

The ...rst integral,  $g(p;\mu)$ ; on the r.h.s. of (48) indicates the shareholders' expected sum of discounted pro...ts, if the price does not go below the retecting barrier  $b_s$  when there is no absorbing barrier. The second integral,  $g(p_{T_w}; Z_{T_w}; \mu)$ ; accounts for the loss due to absorbing at time  $T_w$ : By the strong Markev property of  $p_t$  it can be proved that  $g(p_{T_w}; Z_{T_w}; \mu) = E_0$   $g(b_s; \mu)e^{i\frac{k}{2}T_w}$  and therefore (48) reduces  $to^{23}$ :

$$S^{c}(p; p; \mu) = g(p; \mu)_{i} E_{0}^{e} [g(b_{s}; \mu) + K_{s}]e^{i \frac{\pi}{k}T_{w}} = \frac{\sqrt{2}Z_{1}}{\sqrt{2}} \frac{\sqrt{2}}{\sqrt{2}} e^{i \frac{\pi}{k}T_{w}} = \frac{\sqrt{2}Z_{1}}{\sqrt{2}} \frac{\sqrt{2}Z_{1}}{\sqrt{2}} e^{i \frac{\pi}{k}T_{w}} e^{i \frac{\pi}{k}T_{w}} = \frac{\sqrt{2}Z_{1}}{\sqrt{2}} e^{i \frac{\pi}{k}T_{w}} e^{i \frac{\pi}{k}T_{w}}$$

$$= E_{0} \mu(p_{t}; c)e^{i \frac{\pi}{k}t}dt \quad i \quad E_{0}^{e} [g(b_{s}; \mu) + K_{s}]e^{i \frac{\pi}{k}T_{w}}$$

$$(49)$$

Equation (49) shows how the expected discounted value of pro...ts accruing to shareholders, when a retecting and an absorbing barrier are considered, is represented by the dixerence between two terms depending upon the joint evolution of the two processes  $p_t$  and  $p_t$ : The ...rst,  $g(p; \mu)$ ; indicates the

 $<sup>^{22}</sup>$  If we divide the life time of the ...rm into two parts, before  $b_s$  is touched for the ...rst time,  $T_s$ ; and the period between  $T_s$  and  $T_w$ ; we can write:

expected value of pro...ts with only the lower barrier  $b_s$  beyond which pro...ts do not go. The second,  $E_0$  [g( $b_s$ ;  $\mu$ ) +  $K_s$ ]ei  $^{1/2}T_w$  is the cost of exit at  $T_w$  with the inclusion of pro...ts lost because of the decision.

Considering only the retecting barrier and going through the usual asset equilibrium condition, the shareholders' well-being is the solution of the following dixerential equation:

$$\frac{1}{2} \frac{1}{4} {}^{2} p^{2} g^{0} + {}^{\otimes} p g^{0} ; \quad \frac{1}{2} g = \mu(p_{i} c) \text{ for } p 2 [b_{s}; 1); \tag{50}$$

yet boundary conditions change:

$$\lim_{p! \ 1} [g(p; \mu)_{i} \ \mu \frac{p}{\frac{p}{k_{i}} \mathbb{R}}_{i} \frac{c}{\frac{p}{k}}] = 0$$
 (51)

$$g^{\emptyset}(b_s; \mu) = 0 \tag{52}$$

The smooth pasting condition (52) is the ...rst order derivative of the expected present value of a function of a Brownian motion. It does not involve any optimizing role of the barrier and requires only the continuity of the ...rst derivative of s in  $b_s$  (Dixit, 1993, p. 27). Finally we need an overall value matching condition saying that the shareholders at the exit are indizerent with and without compensation.

$$S^{c}(b_{w};b_{s};\mu) = S(b_{s};\mu) = i K_{s}$$
 (53)

By the linearity of the dixerential equation (50) and making use of (51), (52) and (53), the general solution of (49) takes the form:

$$S^{c}(p; p; \mu) = g(p; \mu)_{i} [g(b_{s}; \mu) + K_{s}] \frac{\mu}{b_{w}} \P_{-2}$$
 (54)

where:

That is, as long as the compensation period is stochastic, the expected loss during the subsidization is zero. At each time t  $_s$   $T_s$  the compensation keeps shareholders better ox (at least indixerent) between exiting now or putting ox the decision. Compensation starts at  $T_s$  and the value of the ...rm to shareholders will be greater, i.e.  $S^c(p_t; p_t; \mu)_i$   $S(b_s; \mu)$   $g(p_t; \mu)_i$   $S(b_s; \mu)$   $g(p_t; \mu)_i$   $S(b_s; \mu)$ .

While the compensation keeps shareholders at least indixerent between exiting now or keeping on, workers are not in the same condition. Indicating with  $W^c(p;p;\mu)$  the workers' well-being less the compensation they pay, we get:

Whilst the ...rst integral represents the workers' well-being without compensation, the second accounts for the transfer. Using again the strong Markov property of  $\mathfrak{p}_t$ ; it can be proved that:

$$\begin{split} W\left(p;\mu\right)_{i} & W^{c}(p;\beta;\mu) = m_{1}(\beta;\mu)_{i} & E_{0} & m_{1}(b_{s};\mu)e^{i\frac{\hbar}{2}T_{w}} \\ & \frac{\hbar}{2} & \frac{3}{4} & \frac{\hbar}{2} & \frac{3}{4} \\ & = E_{0} & (1_{i} \ \mu)\beta_{t}e^{i\frac{\hbar}{2}t}dt \quad i \quad E_{0} & (1_{i} \ \mu)\beta_{t}e^{i\frac{\hbar}{2}t}dt \end{split}$$

with boundary conditions:

$$\lim_{p! \ 1} [m_1(p; \mu)_i \ (1_i \ \mu) \frac{p}{\frac{1}{2} i^{\otimes}}] = 0; \tag{60}$$

$$\mathsf{m}_1^{\,0}(\mathsf{b}_\mathsf{S};\mu) = 0; \tag{61}$$

 $m_2(p; \mu)$  is the solution of:

$$\frac{1}{2} \frac{3}{4} p^{2} m_{2}^{0} + {}^{\text{@}} p m_{2}^{0} ; \quad \frac{1}{2} m_{2} = (1; \mu) p \text{ for p 2 [b_{w}; 1)}; \tag{62}$$

with boundary condition:

$$\lim_{p!} [m_2(p; \mu)_i (1_i \mu) \frac{p}{\frac{1}{1/2} i^{-\frac{n}{8}}}] = 0:$$
 (63)

Finally, as for shareholders, we need an overall value matching condition:

$$W(b_w; \mu) i W^c(b_w; b_s; \mu) = 0$$
 (64)

By the linearity of the two dixerential equations (59) and (62), and making use of the boundary conditions, the general solution of (58) becomes:

$$W(p;\mu)_{i} W^{c}(p;p;\mu) = M(p;p;\mu)^{-1} m_{1}(p;\mu)_{i} m_{1}(b_{s};\mu) \frac{\mu}{b_{w}} \frac{\eta^{-1}}{p_{w}} m_{2}(p;\mu)$$
(65)

where:

$$m_1(p; \mu) = B_1^c p^{-2} + (1_i \mu) \frac{p}{\frac{1}{2} i \cdot m};$$

$$m_2(p; \mu) = B_2^c p^{-2} + (1_i \mu) \frac{p}{\frac{1}{12} i \cdot \mathbb{R}};$$

future subsidies. Therefore, in game-theoretic terms it may be represented, in the strategy space of shareholders, as:

$$\begin{tabular}{lll} \bf 8 \\ & \begin{tabular}{l} \bf 8 \\ & \begin{tabular}{$$

Where  $A(p_t; Z_t) = [Exit, Non Exit]$  is the action chosen by shareholders at time t with history  $(p_t; Z_t)$ : In our formulation of the shareholders's "trigger" strategy the threat is exercised if the victims deviate paying less than  $s_t$  or by abandoning  $s_t = (Z_{t \mid t}) p_t$  as decision rule to evaluate future subsidies. Carrying out the threat depends on the expected sum of future discounted pro...ts (i.e. up to the shut down). Then, shareholders must believe that the compensation rule viewed from the initial date and state  $(T_s; b_s)$ ; will be kept in use for all the (stochastic) planning horizon. If workers deviate the threateners believe that the victims will use a diærerent rule in the future, and then the workers believe that the threateners will carry out the threat at their ...rst opportunity, that is immediately. In this way, workers are punished for deviating of using the announced subsidy rule.

On the other hand, workers do not have any incentive to pay more than s<sub>t</sub>

shareholders do not exit, i.e.  $\acute{A}(p_t; Z_t) =$  "Non Exit" for all t  $_s$   $T_s$ . This situation is equivalent to one in which at the initial date  $T_s$  workers choose a decision rule that speci…es which subsidy is to be taken at each realization of  $p_t$  and for any date t 2  $[T_s; T_w)$  (Fudenberg and Tirole, 1991, ch.13).<sup>24</sup>

Moreover, as the strategy  $\acute{A}$  is e $\frak{C}$ cient for any subgame starting at an intermediate date and state (t; p<sub>t</sub>) pair at which the option to exit has not been exercised yet (as any subgame beginning at a point at which exit has not taken place is equivalent to the whole game), then we may conclude that it is also subgame perfect.

We are now able to introduce the workers' participation constraint. Although the value matching condition (64) assures that, at time  $T_w$ ,  $W^c(b_w;b_s;\mu) = K_w$  i  $K_l$ ; there is no condition that a priori warrants that the loss from having the threat carried out at  $T_s$ ; i.e.  $W(b_s;\mu)$  i  $\hat{W}(b_s;\mu)$  is smaller than the (expected) present discounted value of the payment  $E_{T_s}$   $E_{T_s}$   $E_t$  in the compensation scheme may be interrupted before reaching the terminal time  $E_t$ . However, by the random evolution of the subsidized price  $E_t$  at each date  $E_t$   $E_t$  there is no reasons for both players to commit for a stochastic period of length lower than  $E_t$   $E_t$   $E_t$   $E_t$  they discover that  $E_t$   $E_t$ 

So far we have implicitly assumed that, once started at time  $T_s$ ; the compensation ‡ow goes on until the state variable  $p_t$  touches the lower barrier  $b_w$  at time  $T_w$ : Earlier interruption can only be due to the participation constraint. However, by the characteristics of optimal Brownian paths, there always exists a probability, starting at an interior point of the range ( $b_s$ ;  $b_w$ ) between the two barrier, that the state  $p_t$  touches again  $b_s$  before reaching  $b_w$ : In this case, workers may be willing to stop compensating shareholders.

option to exit since they are at their indixerent position.

Not only the participation constraint but also the rise of the price above  $b_s$  seem to imply a sudden end of the compensation ‡ow and of the game before touching  $T_w$ : However, as shareholders anticipate this and the decision rule strategy  $\acute{A}$  depends on the history of the game (is not a Markov strategy),  $s_t$  is not subgame perfect any longer.

If we consider the possibility that workers' compensation terminates before reaching  $T_w$ , the shareholders' expected sum of discounted pro...ts starting at any t 2  $[T_s; T_w)$ ; becomes:

$$(z_{T_s^0 \land T_w}), \text{ becomes.}$$

$$S^c(p_t; p_t; \mu) = E_t \qquad \mu(p_v \mid c)e^{i\frac{\lambda}{2}(v_i \mid t)}dv \quad \text{i} \quad E_t \quad K_s e^{i\frac{\lambda}{2}(T_s^0 \land T_w \mid t)};$$

$$(66)$$

where  $T_s^0 \wedge T_w \cap \min[T^0(b_s); T(b_w)]$ ; and  $T_s^0 = \inf(t_s, T_s j p_t \cdot b_s)$  indicates the ...rst hitting time of  $b_s$  when the compensation scheme is in operation (the prime indicates that  $b_s$  has been already touched).  $E_t$  represents the expected value operator conditional to all the random variables with the inclusion of the stopping time  $T_s^0 \wedge T_w$ : Triggers  $b_s$  and  $b_w$  play the role of absorbing barriers for the primitive process  $p_t$ .

The probability of reaching  $b_s$  before  $b_w$  is equal to (Cox and Miller, 1965, pp.232-234; Dixit, 1993, p.54.):

$$Pr(T_s^{\emptyset} < T_w j p_t) \hat{P}(p_t) = \frac{(p_t)^{i} 2^{1-\frac{3}{4}^2} j (b_w)^{i} 2^{1-\frac{3}{4}^2}}{(b_s)^{i} 2^{1-\frac{3}{4}^2} j (b_w)^{i} 2^{1-\frac{3}{4}^2}};$$

with  $^{1} = (^{\circ}_{i} \frac{1}{2} \%^{2})^{25}$ . Then the shareholders' well-being can be rewritten as:

$$(\mathbf{z}_{\mathsf{T}_s^0})$$

$$\mathsf{S}^c(\mathsf{p}_t;\mathsf{p}_t;\mu) = \mathsf{P}(\mathsf{p}_t)\mathsf{E}_t \qquad \mu(\mathsf{p}_{\mathsf{v}|\mathsf{i}} \mathsf{c})\mathsf{e}^{\mathsf{i}\,\frac{\mathsf{v}_i(\mathsf{v}_i\;\mathsf{t})}{\mathsf{d}}\mathsf{v}\,\mathsf{i}} \;\;\mathsf{K}_s\mathsf{e}^{\mathsf{i}\,\frac{\mathsf{v}_i(\mathsf{T}_s^0\;\mathsf{i}\;\mathsf{t})}{\mathsf{t}}} \;\;+$$

we get:

$$S^{c}(p_{t}; p_{t}; \mu) = g(p_{t}; \mu)_{i} P(p_{t}) g(p_{T_{s}^{0}}; \mu) + K_{s} \frac{p_{t}}{b_{s}}^{\eta_{-1}};$$
(67)

where  $^-_1 > 1$  is the positive root of  $^{\circ}(^-)$ : Although (67) satis...es the overall value matching condition  $S^c(b_s; p_{T_s^0}; \mu) = S(b_s; \mu) = {}_i K_s$ ; this is not true for all t 2  $[T_s; T_s^0)$ : To see this consider the case in ...g. 4.

## FIGURE 4 ABOUT HERE

By (45), at t the subsidy is such that  $\mathfrak{p}_t = \mathfrak{b}_s$ ; and the shareholders will not exercise the option to exit if their well-being is at least equal to  $\mathfrak{j} \ \mathsf{K}_s$ : In addition, as  $\mathfrak{p}_{\mathsf{T}_s^0} = (\mathfrak{b}_s = \mathfrak{p}_{t^0})\mathfrak{b}_s > \mathfrak{b}_s$  we may write  $g(\mathfrak{p}_{\mathsf{T}_s^0}; \mu) = \mathfrak{j} \ \mathsf{K}_s + 4$ "; with 4" > 0: Then substituting into (67) the well-being becomes:

$$S^{c}(p_{t};b_{s};\mu) = i K_{s} i P(p_{t})4" \frac{\mu}{b_{s}} \P_{1} < i K_{s}$$

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