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Persistence and nominal inertia in a generalized Taylor economy: how longer contracts dominate shorter contracts

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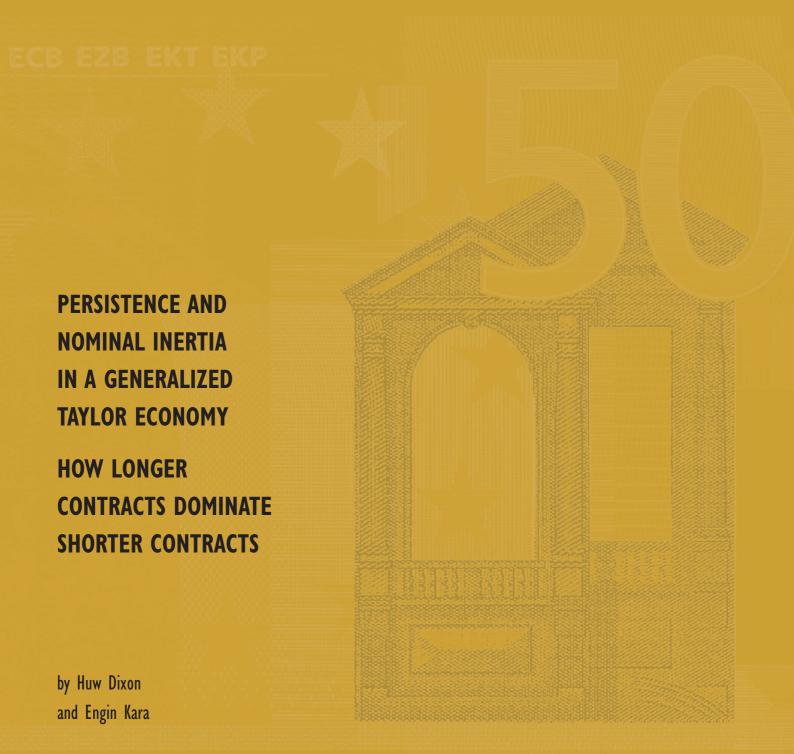
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PERSISTENCE AND NOMINAL INERTIA IN A GENERALIZED TAYLOR ECONOMY

HOW LONGER CONTRACTS DOMINATE SHORTER CONTRACTS 1

by Huw Dixon² and Engin Kara³

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Abstract

In this paper we develop the Generalized Taylor Economy (GTE) in which there are many sectors with overlapping contracts of different lengths. In economies with the same average contract length, monetary shocks will be more persistent when longer contracts are present. We are able to solve the puzzle of why Calvo contracts appear to be more persistent than simple Taylor contracts: it arises because of the distribution of contract lengths. When we choose a GTE with the same distribution of completed contract lengths as the Calvo, the economies behave in a similar manner.

JEL: E50, E24, E32, E52

Keywords: Persistence, Taylor contract, Calvo.

Non-Techinal Summary

This paper develops the concept of the Generalized Taylor Economy (GTE), in which there can be many sectors with different contract lengths. This has the simple Taylor economy as a special case: there is only one contract length in the economy. This framework can be used to model either wage or price-setting behaviour. There is clear evidence of heterogeneity of contract lengths within and between economies.

We apply this concept to wage-setting behaviour in a Dynamic Stochastic General Equilibrium Setting. We look at the issue of persistence in an impulse-response setting. In this literature, there is something of a consensus in theory-consistent parameterizations of DSGE with Taylor contracts, nominal wage or price rigidity does not generate as much persistence as is seen in the data.

We find that even the presence of a small proportion of longer contracts can significantly increase the persistence of output in response to a monetary shock. In two economies with the same mean contract length, the one with more dispersion will exhibit more persistence.

We apply this to an empirical distribution of contract lengths for the US compiled by John B Taylor. We show that when we use this in a DSGE model with standard calibrations the persistence is similar to the empirical persistence.

We then apply the GTE approach to solve another puzzle. We can calibrate the GTE using the distribution of completed contract levels generated by the Calvo model of price-wage setting. In the existing literature, it has long been noted that a Calvo economy appears to be significantly more persistent than a simple Taylor economy with the same mean contract length. We solve this puzzle.

First, we show that the standard calibration of Calvo and Taylor has been wrong: it has confused the age of a contract with the completed or lifetime duration of the contract. In steady state, the average age is about half the corresponding average completed lifetime. So, Calvo economies are compared with Taylor economies which have almost half the average completed contract length. This is one source of the larger persistence in Calvo models.

Second, we show that even if you calibrate the Taylor and Calvo to have the same mean contract length, Calvo is still more persistent. That is because of the distribution of contract lengths which includes a long tail of long contracts. We construct the Calvo-GTE: it is an economy where the wage-setting in each sector is Taylor, but the distribution of contract lengths is exactly the same as the Calvo. The persistence of the two economies is almost the same.

The slight differences between the Calvo and Calvo-GTE occur because of the wage-setting decisions. The Calvo-GTE wage-setting is more myopic. This is because when there is a distribution of contract lengths, the shorter contracts show up more amongst the firm-unions who reset wages. This explains why the output response in the Calvo-GTE is a little larger earlier on and a little less later on.

The intuitive explanation of why longer contracts tend to dominate is because of a sort of spillover effect through the general price-level. The general price level aggregates prices of each sector, which depend primarily on wages in that sector. When setting wages, wage-setters look at the trajectory of prices in the future. If longer contracts are present, they tend to make the general price more sluggish. This then affects the wage-setting of shorter contracts who react by less since the general price level is more sluggish. Hence the sluggishness of long contracts is infectious.

We believe that the GTE has a wide range of applications, wherever the diversity of wage or price setting is thought to be important. It will also help us to understand the implications of using the Calvo model and suggests a unifying framework that embraces both the Taylor and Calvo models.

1 Introduction

"There is a great deal of heterogeneity in wage and price setting. In fact, the data suggest that there is as much a difference between the average lengths of different types of price setting arrangements, or between the average lengths of different types of wage setting arrangements, as there is between wage setting and price setting. Grocery prices change much more frequently than magazine prices - frozen orange juice prices change every two weeks, while magazine prices change every three years! Wages in some industries change once per year on average, while others change per quarter and others once every two years. One might hope that a model with homogenous representative price or wage setting would be a good approximation to this more complex world, but most likely some degree of heterogeneity will be required to describe reality accurately."

Taylor (1999).

There are two main approaches to modelling nominal wage and price rigidity in the dynamic general equilibrium (DGE) macromodels: the staggered contract setting of Taylor (Taylor (1980)) and the Calvo model of random contract lengths generated by a constant hazard (reset) probability (Calvo (1983)). This paper proposes a generalization of the standard Taylor model to allow for an economy with many different contract lengths: we call this a Generalized Taylor Economy - *GTE* for short. The standard approach in the literature has been to adopt a simple Taylor economy, in which there is a single contract length in the economy: for example 2 or 4 quarters¹. As the above quote from John Taylor indicates, in practice there is a wide range of wage and price setting behavior resulting in a variety of contract lengths. We can use the *GTE* framework to evaluate whether the hope expressed by John Taylor that a representative sector approach "is a good approximation to this more complex world".

An additional advantage of the GTE framework is that it includes the Calvo model as a special case, in the sense that we can set up the GTE to

¹This is not to ignore some recent papers that have allowed for two sectors with different contract durations, such as Aoki (2001), Erceg and Levin (2002), Carlstrom, Fuerst and Ghironi (2003) or with multi-sectors such as Mankiw and Reis (2003). However, these studies are mainly concerned with computing optimal monetary policy in a Dynamic Equlibrium Setting.

have the same distribution of contract lengths as the Calvo model. This is an important contribution in itself since the two approaches have until now appeared to be distinct and incompatible at the theoretical level even if they are sometimes claimed to be empirically similar (see for example Kiley (2002) for a discussion). As we shall show, a simple Taylor economy can indeed be a good approximation to a Calvo model, but only if the two are calibrated in a consistent manner.

We develop our approach in a DGE setting following the approach of Ascari (2000). The issue we focus on is the way a monetary shock can generate changes in output through time, and in particular the degree of persistence of deviations of output from steady-state. Much recent attention has been devoted to the ability of the staggered contract approach of Taylor to generate enough persistence in the sense of being quantitatively able to generate the persistence observed in the data. Two influential papers in this are Chari, Kehoe and McGrattan (2000) (CKM herafter) and Ascari (2000). Both papers are pessimistic for staggered contracts. CKM develop a microfounded model of staggered price-setting and find that they do not generate enough persistence and conclude that the "mechanism to solve persistence problem must be found elsewhere". Ascari focusses on staggered wage setting, and finds that whilst nominal wage rigidities lead to more persistent output deviations than with price setting, they are still not enough to explain the Based on these conclusions, it is commonly inferred that in a dynamic equilibrium framework, staggered contracts cannot generate enough persistence.

In this paper, we follow Ascari in focussing on staggered wage-contracts. However, we show that by allowing for an economy with a range of contract lengths, the presence of longer contracts can significantly increase the degree of persistence in output following a monetary shock. We calibrate the model in a way that in either the CKM or Ascari setting would not generate much persistence. We show that even a small proportion of longer contracts can significantly increase the degree of persistence. For example, we consider the case of a economy where 90% of the economy consist of simple 2-period Taylor contracts, and 10% have 8-period Taylor contracts (the average is 2.6 quarters) and show that the economy has a marked increase in output persistence. We also take an empirical distribution of contract lengths (from 1-8 quarters) for the US taken from Taylor (1993) and show that this will generate a significant degree of persistence. The intuition behind this finding is that there is a spillover effect or strategic complementarity in terms of wage-

setting through the price level. The presence of longer contracts means that the general price level is held back in response to monetary shocks. This in turn means that the wage setting of shorter contracts is influenced and hence they adjust by less than they otherwise would.

It has long been observed that in the Calvo setting there can be a significant backlog of old contracts: for example, with a reset probability of $\omega = 0.25$ (a common value used with quarterly data), there is a probability of over 10% that a contract will survive for 8 periods (see for example Erceg (1997), Wolman (1999)). We construct a *GTE* which has exactly the same distribution of completed contract lengths as the Calvo distribution (as derived in Dixon and Kara (2005)). We find that this Calvo-GTE has similar persistence to the Calvo economy. The remaining difference between the Calvo economy and the Calvo-GTE is in the wage-setting decision. We find that calvo reset firms are more forward looking on average than in the Calvo-GTE. This is because short contracts are more predominant amongst wage-resetters in the Calvo-GTE than in the economy as a whole, simply because wage-setters with long contracts reset wages less frequently. However, for the calibrated values this does not make a big difference and indicates that the two approaches of Taylor and Calvo can be brought together in the framework of the GTE.

The outline of the paper is as follows. In section 2 we outline the basic structure of the Economy. The main innovation here is to allow for the GTE contract structure. In section 3 we present the log-linearized general equilibrium and discuss the calibration of the model in relation to recent literature. In section 4 we explore the influence of longer term contracts on persistence as compared to the simple Taylor economy, and in section 5 we apply our methodology to evaluating persistence in the Calvo model.

2 The Model Economy

The approach of this paper is to model an economy in which there can be many sectors with different wage setting processes, which we denote a Generalized Taylor Economy. (GTE). As we will show later, an advantage of the GTE approach is that it includes as special cases not only the standard Taylor case of an economy where all wage contracts are of the same length, but also the Calvo process.

The model in this section is an extension of Ascari (2000) and includes a

number of features essential to understanding the impact of monetary shock on output in a dynamic equilibrium setting. The exposition aims to outline the basic building blocks of the model. However, the novel aspects of this paper only begin with the wage setting process. Firstly, we describe the behavior of firms which is standard. Then we describe the structure of the contracts in a GTE, the wage-setting decision and monetary policy.

2.1 Firms

There is a continuum of firms $f \in [0, 1]$, each producing a single differentiated good Y(f), which are combined to produce a final consumption good Y. The production function here is CES with constant returns and corresponding unit cost function P

$$Y_t = \left[\int_0^1 Y_t(f)^{\frac{\theta - 1}{\theta}} df \right]^{\frac{\theta}{\theta - 1}} \tag{1}$$

$$P_t = \left[\int_0^1 P_{ft}^{1-\theta} df \right]^{\frac{1}{1-\theta}} \tag{2}$$

The demand for the output of firm f is

$$Y_{ft} = \left(\frac{P_{ft}}{P_t}\right)^{-\theta} Y_t \tag{3}$$

Each firm f sets the price P_{ft} and takes the firm-specific wage rate W_{ft} as given. Labor L_{ft} is the only input so that the inverse production function is

$$L_{ft} = \left(\frac{Y_{ft}}{\alpha}\right)^{\frac{1}{\sigma}} \tag{4}$$

Where $\sigma \leq 1$ represents the degree of diminishing returns, with $\sigma = 1$ being constant returns. The firm chooses $\{P_{ft}, Y_{ft}, L_{ft}\}$ to maximize profits subject to (3,4), yields the following solutions for price, output and employment at the firm level given $\{Y_t, W_{ft}, P_t\}$

$$P_{ft} = \left(\frac{\theta - 1}{\theta}\right) \frac{\alpha^{-1/\sigma}}{\sigma} W_{ft} Y_{ft}^{\frac{1 - \sigma}{\sigma}} \tag{5}$$

$$Y_{ft} = \kappa_1 \left(\frac{W_{ft}}{P_t}\right)^{-\sigma\varepsilon} Y_t^{\frac{\varepsilon\sigma}{\theta}} \tag{6}$$

$$L_{ft} = \kappa_2 \left(\frac{W_{ft}}{P_t}\right)^{-\varepsilon} Y_t^{\frac{\varepsilon}{\theta}} \tag{7}$$

where
$$\varepsilon = \frac{\theta}{\theta(1-\sigma)+\sigma} > 1$$
 $\kappa_1 = \left(\frac{\theta-1}{\theta}\right)^{-\sigma\varepsilon} \sigma^{-\sigma\varepsilon} \alpha^{-\varepsilon}$ $\kappa_2 = \left(\frac{\theta-1}{\theta}\right)^{-\varepsilon} \sigma^{\varepsilon} \alpha^{\varepsilon(\frac{\theta-1}{\theta})}$. Price is a markup over marginal cost, which depends on the wage rate

Price is a markup over marginal cost, which depends on the wage rate and the output level (when $\sigma < 1$): output and employment depend on the real wage and total output in the economy.

2.2 The Structure of Contracts in a GTE

In this section we outline an economy in which there are potentially many sectors with different types of wage-setting processes. Within each sector there is a more or less standard Taylor process (i.e. overlapping contracts of a specified length). The economy is called a Generalized Taylor Economy (GTE). Corresponding to the continuum of firms f there is a unit interval of household-unions (one per firm). The economy consists N sectors i=1...N. The budget shares of the N sectors with uniform prices (when prices p_f are equal for all $f \in [0,1]$) are given by α_i with $\sum_{i=1}^N \alpha_i = 1$, the N vector $(\alpha_i)_{i=1}^N$ being denoted α , where $\alpha \in \Delta^{N-1}$.

We can partition the unit interval into sub-intervals representing each sector. Let us define the cumulative budget share of sectors k = 1...i.

$$\hat{\alpha}_i = \sum_{k=1}^i \alpha_k$$

with $\hat{\alpha}_0 = 0$ and $\hat{\alpha}_N = 1$. The interval for sector i is then $[\hat{\alpha}_{i-1}, \hat{\alpha}_i]$.

Within each sector, each firm is matched with a firm-specific union: there are N_i cohorts of unions and firms in sector i. Again, we can partition the interval $[\hat{\alpha}_{i-1}, \hat{\alpha}_i]$ into cohort intervals: let the share of each cohort within the sector be λ_{ij} so that $\sum_{j=1}^{N_i} \lambda_{ij} = 1$, with the N_i -vector $\lambda_i \in \Delta^{N_i-1}$. Again, we can define the cumulative share $\hat{\lambda}_{ij}$ analogously to $\hat{\alpha}_k$. The interval of firm-unions corresponding to cohort j in sector i is then

$$\left[\hat{\alpha}_{i-1} + \hat{\lambda}_{ij-1}\alpha_i, \hat{\alpha}_{i-1} + \hat{\lambda}_{ij}\alpha_i\right]$$

Clearly, if symmetry is assumed (cohorts are of equal size) $\lambda_{ij} = N_i^{-1}$ and $\hat{\lambda}_{ij} = j N_i^{-1}$.

The sectors are differentiated by the integer² contract length $T_i \in Z_{++}$, which is the same for all cohorts within a sector. The timing of the wage

²We work in discrete time in this paper, although the model obviously generalises to continuous time.

setting process within the sector can be summarized by an N_i – 1-tuple of integers $\{T_{ij}\}_{j=2}^{N_i}$ which specifies when in the wage-setting cycle cohort j moves. It is assumed that cohort 1 moves first (period 1): this defines the beginning of the cycle, so that $1 \leq T_{ij} \leq N_i$. If $T_{ij} = 3$, it means that cohort j sets its wage in period 3 periods after the first. By convention, we assume that the js are ordered so that T_{ij} is strictly increasing. Clearly, we have the restriction of $N_i \leq T_i$: there cannot be more cohorts than contract periods. If $N_i = T_i$, then one cohort moves in each period: if in addition the the cohorts are of equal size $\lambda_{ij} = N_i^{-1}$, we define a uniform wage setting process in sector i. If $N_i < T_i$, then there will be some periods when no cohort moves. For example, we can consider a sector with 8 period contracts in which there are two cohorts in which the second cohort moves 4 periods after the first, $T_{i2} = 4$. Alternatively, there might be three cohorts, with timing $\{2,6\}$ so that the second cohort moves in period 2 and third in period 6.

In order to fully characterize the economy with non-uniform wage setting, we also need to specify the calender date t_i when the wage-setting process starts³ for each contract length T_i . In the case of an economy with uniform wage setting processes in all sectors, the start dates are irrelevant, since each period is exactly the same in all sectors (i.e. the same proportion of wages are reset).

We can therefore characterize the wage setting process in a GTE by $(\mathbf{T}, \boldsymbol{\alpha}) \in \mathbb{Z}_{++}^N \times \Delta^{N-1}$, which gives the contract lengths and sizes of the N sectors, and $(N_i, \lambda_i, t_i) \in Z_{++} \times \Delta^{N_i-1} \times Z_{++}$ which describes the number and relative size of the cohorts in each sector i, and the timing/synchronization of cohorts in that sector:

$$GTE := \left\{ \left(\boldsymbol{T}, \boldsymbol{\alpha} \right), \left\{ N_{i, \boldsymbol{\lambda}_{i}}, t_{i} \right\}_{i=1}^{N} \right\}$$

In the case where each sector has a uniform wage setting process, we have a uniform GTE which is more simply parameterized by $(\mathbf{T}, \boldsymbol{\alpha})$ since $(N_i, \boldsymbol{\lambda}_i) =$ (T_i, T_i^{-1}) and t_i is irrelevant (each period looks the same). A homogenous or simple Taylor economy is one where there is just one sector with a uniform wage-setting process.

³Of course, this is not unique: all that is required for each sector is the start date of one cycle, since then the start date of all cycles is given.

The general price index P can be defined in terms of sectors, or subintervals $[\hat{\alpha}_{i-1}, \hat{\alpha}_i]$ for each sector i.

$$P = \left[\sum_{i=1}^{N} \int_{\hat{\alpha}_{i-1}}^{\hat{\alpha}_i} P_f^{1-\theta} df \right]^{\frac{1}{1-\theta}}$$

This can be further broken down into intervals for each cohort, where we note that all firms in the same cohort face the same wage and hence set the same price $p_f = p_{ij}$ for $f \in \left[\hat{\alpha}_{i-1} + \hat{\lambda}_{ij-1}\alpha_i, \hat{\alpha}_{i-1} + \hat{\lambda}_{ij}\alpha_i\right]$

$$P = \left[\sum_{i=1}^{N} \sum_{j=1}^{N_i} \int_{\hat{\alpha}_{i-1} + \hat{\lambda}_{ij} - 1\alpha_i}^{\hat{\alpha}_{i-1} + \hat{\lambda}_{ij} - \alpha_i} P_{ij}^{1-\theta} df \right]^{\frac{1}{1-\theta}}$$
(8)

We can log linearize the price equations around the steady state, given the wages. All firms with the same wage will set the same price: define P_{ij} as the price set by firms in sector i cohort j. This yields the following log-linearization in terms of deviations from the steady state (where we assume $P^* = 1$):

$$p = \sum_{i=1}^{N} \sum_{j=1}^{N_i} \alpha_i \lambda_{ij} p_{ij} \tag{9}$$

Note that there is an important property of CES technology. The demand for an individual firm depends only on its own price and the general price index (see 3). There is no sense of location: whilst we divide the unit interval into segments corresponding to sectors and cohorts within sectors, this need not reflect any objective factor in terms of sector or cohort specific aspects of technology or preferences. The sole communality within a sector is the length of the wage contract: the sole communality within a cohort is the timing of the contract. The vectors α and λ_i are best be thought of as simply measures of sector and cohort size. This is an important property which will become useful when we show that a Calvo economy can be represented by a GTE.

2.3 Household-Unions and Wage Setting

Households $h \in [0, 1]$ have preferences defined over consumption, labour, and real money balances. The expected life-time utility function takes the form

$$U_h = E_t \left[\sum_{t=0}^{\infty} \beta^t u(C_{ht}, \frac{M_{ht}}{P_t}, \underbrace{1 - H_{ht}}_{L_{ht}}) \right]$$
 (10)

where C_{ht} , $\left(\frac{M_{ht}}{P_t}\right)$, H_{ht} , L_{ht} are household h's consumption, end-of period real money balances, hours worked, and leisure respectively, t is an index for time, $0 < \beta < 1$ is the discount factor, and each household has the same flow utility function u, which is assumed to take the form

$$U(C_{ht}) + \delta \ln(\frac{M_{ht}}{P_t}) + V\left(1 - H_{ht}\right) \tag{11}$$

Each household-union belongs to a particular sector and wage-setting cohort within that sector (recall, that each household is twinned with firm f = h). Since the household acts as a monopoly union, hours worked are demand determined, being given by the (7).

The household's budget constraint is given by

$$P_t C_{ht} + M_{ht} + \sum_{s_{t+1}} Q(s^{t+1} \mid s^t) B_h(s^{t+1}) \le M_{ht-1} + B_{ht} + W_{ht} H_{ht} + \pi_{ht} + T_{ht}$$
 (12)

where $B_h(s^{t+1})$ is a one-period nominal bond that costs $Q(s^{t+1} \mid s^t)$ at state s^t and pays off one dollar in the next period if s^{t+1} is realized. B_{ht} represents the value of the household's existing claims given the realized state of nature. M_{ht} denotes money holdings at the end of period t. W_{ht} is the nominal wage, π_{ht} is the profits distributed by firms and $W_{ht}H_{ht}$ is the labour income. Finally, T_t is a nominal lump-sum transfer from the government.

The households optimization breaks down into two parts. First, there is the choice of consumption, money balances and one-period nominal bonds to be transferred to the next period to maximize expected lifetime utility (10) given the budget constraint (12). The first order conditions derived from the consumer's problem are as follows:

$$u_{ct} = \beta R_t E_t \left(\frac{P_t}{P_{t+1}} u_{ct+1} \right) \tag{13}$$

$$\sum_{s_{t+1}} Q(s^{t+1} \mid s^t) = \beta E_t \frac{u_{ct+1} P_t}{u_{ct} P_{t+1}} = \frac{1}{R_t}$$
 (14)

$$\delta \frac{P_t}{M_t} = u_{ct} - \beta E_t \frac{P_t}{P_{t+1}} u_{ct+1} \tag{15}$$

Equation (13) is the Euler equation, (14) gives the gross nominal interest rate and (15) gives the optimal allocation between consumption and real balances. Note that the index h is dropped in equations (13) and (15), which reflects our assumption of complete contingent claims markets for consumption and implies that consumption is identical across all households in each period $(C_{ht} = C_t)^4$.

The reset wage is for household h in sector i is chosen to maximize lifetime utility given labour demand (7) and the additional constraint that nominal wage will be fixed for T_i periods in which the aggregate output and price level are given $\{Y_t, P_t\}$. >From the unions point of view, we can collect together all of the terms in (7) which the union treats as exogenous by defining the constant K_t where:

$$K_t = \kappa_2 P_t^{\varepsilon} Y_t^{\frac{\varepsilon}{\overline{\theta}}}$$

Since the reset wage at time t will only hold for T_i periods, we have the following first-order condition:

$$X_{it} = \left(\frac{\varepsilon}{\varepsilon - 1}\right) \left[\frac{E_t \sum_{s=0}^{T_i - 1} \beta^s \left[V_L \left(1 - H_{t+s}\right) \left(K_{t+s}\right)\right]}{E_t \sum_{s=0}^{T_i - 1} \beta^s \left[\frac{u_c \left(C_{t+s}\right)}{P_{t+s}} K_{t+s}\right]}\right]$$
(16)

Where E_t represents the conditional expectation taken only over states of nature in which the household is unable to reset its wage contract. Equation (16) shows that the optimal wage is a constant "mark-up" (given by $\frac{\varepsilon}{\varepsilon-1}$) over the ratio of marginal utilities of leisure and marginal utility from consumption within the contract duration, from t to $t+T_i-1$ When $T_i=2$, this equation reduces to the first order condition in Ascari (2000).

2.4 Government

There is a government that conducts monetary policy via lump-sum transfer, that is,

⁴See Ascari (2000).

$$T_t = M_t - M_{t-1} (17)$$

The money supply M_t grows at a rate μ_t so that $M_t = \mu_t M_{t-1}$. To focus on the role of the GTE in generating the output persistence, following Huang and Liu (2001), we assume that there are no serial correlation in the money growth process and therefore $\ln(\mu_t)$ follows a white noise process, i.e., $\ln(\mu_t) = \xi_t$, where ξ_t is a white noise process with a zero mean and a finite variance σ_{ξ}^2 . More specifically, we assume that the money supply follows a random walk, i.e., $m_t = m_{t-1} + \xi_t$.

3 General Equilibrium

In this section, we characterize equilibrium of the economy. We first describe the equilibrium conditions for sector i and then the equilibrium conditions for the aggregate economy. To compute an equilibrium, we reduced the equilibrium conditions to four equations, including the household's first order condition for setting its contract wage, the pricing equation, the household's money demand equation, and an exogenous law of motion for the growth rate of money supply. We then log-linearize this equilibrium conditions around a steady state. The steady state which we choose is the zero-inflation steady state, which is a standard assumption in this literature. The linearized version of the equations are listed and discussed below. We follow the notational convention that lower-case symbols represents log-deviations of variables from the steady state.

The linearized wage decision equation (16) for sector i is given by

$$x_{it} = \frac{1}{\sum_{s=0}^{T_i - 1} \beta^s} \left[\sum_{s=0}^{T_i - 1} \beta^s \left[p_{t+s} + \gamma y_{t+s} \right] \right]$$
(18)

The coefficients on output in the wage setting equation in all sectors is given by

$$\gamma = \frac{\eta_{LL} + \eta_{cc}(\sigma + \theta(1 - \sigma))}{\sigma + \theta(1 - \sigma) + \theta\eta_{LL}}$$
(19)

Where $\eta_{cc} = \frac{-U_{cc}C}{U_c}$ is the parameter governing risk aversion, $\eta_{LL} = \frac{-V_{LL}H}{V_L}$ is the inverse of the labour elasticity, θ is the elasticity of substitution of consumption goods.

Using equation (9) and aggregating for sector i, we get

$$p_{it} = w_{it} + \left(\frac{1-\sigma}{\sigma}\right) y_{it} \tag{20}$$

where

$$w_{it} = \sum_{i=1}^{N_i} \lambda_{ijt} w_{ijt}$$

Using equation (3) and aggregating for sector i yields

$$y_{it} = \theta(p_t - p_{it}) + y_t \tag{21}$$

Given the money demand equation (15), log-linerazing this equation yields the following;

$$y_t = m_t - p_t \tag{22}$$

Finally, the linearized price index in the economy is simply a weighted average of the ongoing prices in all sectors and is given by

$$p_t = \sum_{i=1}^{N} \alpha_i p_{it} \tag{23}$$

4 The Calibration of Simple Taylor Economies with Price and Wage setting

In this section, we examine whether our model can account for a contract multiplier. Since the novel aspect of our paper is the incorporation of generalized wage setting, it is useful to compare our results with identical models that makes the standard assumption of a simple Taylor economy. However, before presenting our main results by using the chosen parameter values, it useful to discuss possible alternatives found in the literature and illustrate their implications in simple Taylor economies. The parameters of the model include the discount factor, β , the elasticity of substitution of labour, η_{LL} , the elasticity of substitution of consumption, η_{CC} , the elasticity of substitution of consumption goods, θ , the monetary policy parameter, ξ_t .

The utility is additively separable and for simplicity, we assume $\beta=1$. Empirical studies reveal that intertemporal labour supply elasticity, $1/\eta_{LL}$, is low and is at most 1. In particular, the survey by Pencavel (1986) suggests that η_{LL} is between 2.2 and infinity. Following the literature, we set $\eta_{LL}=4.5$, which implies that intertemporal labour supply elasticity, $1/\eta_{LL}$, is 0.2. Following Ascari (2000), we set $\theta=6$. Finally, we set $\eta_{CC}=1$ and $\sigma=1$, which are all standard values used in the literature (see for example Huang and Liu (2002)). Finally, we assume that at time t there is 1% shock to the distrubance term corresponding to the money growth rate, ξ_t , so that $\xi(t)=1$ and $\xi(s)=0$ for all s>t.

4.1 The Choice of γ

The key parameter determining aggregate dynamics is γ . The magnitude of γ is important since it governs how responsive household-unions are to current and future changes in output (see equation 18). When there is an increase in aggregate demand, households face higher demand for their labour and therefore the marginal disutility of labour increases. With higher income they consume more and marginal utility of consumption falls. The combination of an increase in the marginal disutility of labour and the fall in the marginal utility of consumption leads household-unions to increase their wage. The coefficient γ determines how wages change in response to changes in current and future output. If γ is large, then wages respond a lot to changes in output which implies faster adjustments and a short-lived response of output. On the other hand, if γ is small, then unions are not sensitive to changes in current and future output. In response to an increase in aggregate demand, the wage would not change very much and hence wages are more rigid. In the limit, if $\gamma = 0$, there will be no relationship between output and wages, so that shocks are permanent. Hence the smaller γ , the more wages are rigid and hence the more persistent are output responses.

Estimating γ as an unconstrained parameter, Taylor found that for the US γ is between 0.05 and 0.1. However, in a general equilibrium framework γ is derived so as to conform to micro-foundations. CKM find that with reasonable parameter values, γ will be bigger than one in a staggered price setting, whilst with staggered wage setting Ascari finds the value of γ to be 0.2. Both CKM and Ascari argue that the microfounded value of γ is too high generate the observed persistence following a monetary shock, hence raising doubts over the Taylor model in this respect. In a general equilib-

rium setting, γ is determined by the fundamental parameters of the model according to (19). In particular, its magnitude depends on the parameter governing risk aversion, η_{cc} , the labour supply elasticity, η_{ll}^{-1} and the elasticity of substitution of consumption goods θ (which determines the elasticity of firm demand and the markup from (3) and hence the markup (5)).

With staggered price setting, CKM find that with reasonable parameter values, the value of γ is bigger than one: in particular with $\sigma = 1$

$$\gamma^{CKM} = \eta_{LL} + \eta_{cc} = 1.2 > 1$$

However, for CKM the value of γ^{CKM} could reasonably be much higher⁵: for example with $\eta_{LL}=4.5$ and $\eta_{cc}=1, \ \gamma^{CKM}=5.5$. Huang and Liu (2002) choose to set $\eta_{LL}=2$, so that $\gamma^{CKM}=2$.

The value of γ with wage-setting is much smaller. In our model, as in Ascari, with $\sigma = 1$,

$$\gamma^A = \frac{\eta_{\scriptscriptstyle LL} + \eta_{cc}}{1 + \theta \eta_{\scriptscriptstyle LL}} = \frac{\gamma^{CKM}}{1 + \theta \eta_{\scriptscriptstyle LL}}$$

Under our preferred calibration, $\gamma^{CKM}=5.5$, and $1+\theta\eta_{LL}=27$, so that $\gamma^A=0.2$. The value of γ under wage setting could arguably be much smaller: some authors set $\theta=10$ and combined with a smaller $\eta_{LL}=2$, $\gamma=1/7=0.14$. The lower value of γ is significant and means that with staggered wages the aggregate price level changes more slowly than with staggered prices. This contradicts with the common view that both wage and price-setting have similar implications for persistence. Altough the equations are esentially the same, the the value of γ differs across the two settings (see Huang and Liu (2002) for further discussion). Whilst Ascari (2000) shows that output is more persistent with the staggered wage setting, he shows it is still not persistent enough to generate the observed persistence in output.

We can illustrate how the magnitude of γ can affect the result by comparing the impulse responses using the values of γ from CKM and Ascari (2000) and Taylor (1980). We assume a simple Taylor economy with T=2 (wages last 6 months). All other decisions are made quarterly. We display the

⁵Since CKM were aiming to show that the staggered price model did not generate enough peristence, they chose a value of γ^{CKM} which was low to make the model as persistent as it could reasonably be.

impulse-response functions for output after a one percent monetary shock. As we can see from Figure 1, in response to the one percent monetary shock, output displays similar patterns in the case of $\gamma^{CKM} = 1.22$ and $\gamma^A = 0.20$. For both cases, output increases when the shock hits and quickly returns to its steady state level. For the case of $\gamma = 1.22$, output returns to steady state level when both unions have had the chance to reset wages, i.e. two quarters. Output is certainly more persistent with $\gamma = 0.20$, but not significantly. Finally, the impulse response of output in the case with $\gamma = 0.05$ originally used by Taylor (1980), which yields a level of persistence more in line with the evidence, but not the microfoundations.

5 Persistence in a GTE

The existing literature has tended to focus on the value γ in generating persistence. We want to explore another dimension: for a given γ , we allow for different contract lengths in the GTE framework we have developed. Having more than one type of contract length thus is necessary if the model is to generate output persistence beyond the initial contract period. In what follows, we show that including longer term contracts can significantly increase persistence. Of course, this is in a sense obvious: longer contracts lead to more persistence, and we can achieve any level of persistence if contracts are long enough (so long as $\gamma > 0$). However, we want to show that even a small proportion of long-term contracts can lead to a significant increase. Throughout this section, we will take the value of $\gamma = 0.2$ and explore how persistence changes when we allow for a range of contract lengths. this in three stages: first we simply illustrate our case with a simple two sector example. Second, we use Taylor's 1993 calibrated model of the US economy allowing for contract lengths from 1-8 quarters. Lastly, we consider the Calvo contract process with the corresponding distribution of contract lengths from 1 to infinity.

5.1 Two-sector GTEs

First, let us consider the simple case of a two sector uniform GTE, $\{\mathbf{T}, \boldsymbol{\alpha}\} = \{(2,8), (0.9,0.1)\}$: in sector 1 there are two period contracts, in sector 2 there are 8 period contracts: the short contract sectors produce 90% of the

economies output, the long-contracts 10%. The average contract length in the whole economy (weighted by α_i) is 2.6 quarters.

In Figure 2 we show both the simple Taylor economy with only 2-period contracts alongside the GTE with 10% share of 8-period contracts. We report the impulse response of aggregate output after a one-percent shock in money supply as in Figure 1⁶. As can be seen from the Figure 2, the GTE and simple Taylor economy have dramatically different implications for persistence. In the simple Taylor economy with 2-quarter contracts, changes in money supply have a potentially large but short-lived effect on output. In the GTE, the presence of long-term contracts means that not only does aggregate output rise following a increase in the money supply, but it is considerably more persistent.

What is the intuition behind this finding? We believe that the presence of the longer term contracts influences the wage-setting behaviour of the short-term contracts. This can be seen as a sort of "strategic complementarity". A monetary expansion means that the new steady state price is higher. When setting wages, unions trade off the current price level and the future. The fact that the long-contracts will adjust sluggishly means that the shorter contracts will also react more sluggishly, since their wage setting is influenced by the general price level which includes the prices of the more sluggish sectors. There is a spillover effect from the sluggish long-contract sectors to the short-contract sectors via the price level, a mechanism identified previously in Dixon (1994).

We can perhaps best illustrate the contrast in terms of mean-equivalent GTEs. In Figure 3a we have the output response compared in two GTEs with a mean contract length of 2: one is a simple Taylor economy, the other consists of mainly flexible wages and 1/7 are 8 period contracts. The presence of the perfectly flexible one period contracts leads to a dampened impact relative to the 2-period Taylor. However, it is clear that although the economy consists mainly of flexible wages, the output dies away slowly and after the second quarter output is larger in the mixed economy. This is because the 8 period contracts are holding back the general price level

⁶We use Dynare to compute the impulse response functions. See Juillard (1996).

and hence influencing the wage-setting of the flexible sector. In Figure 3b we have a simple 3 Taylor economy with a mixed one of 2 and 8 period contracts. Again the impact is less in the mixed economy but soon becomes more persistent.

5.2 Taylor's US Economy

In this section we use the study by Taylor (1993). Taylor Calibrates the US economy as $\mathbf{T} = (1, 2, 3, 4, 5, 6, 7, 8)$, with sector shares being: $\alpha_1 = 0.07$, $\alpha_2 = 0.19$, $\alpha_3 = 0.23$, $\alpha_4 = 0.21$, $\alpha_5 = 0.15$, $\alpha_6 = 0.08$, $\alpha_7 = 0.04$, $\alpha_8 = 0.03$. We can note that the largest sector is 3-period contracts, the three contract lengths (3, 4, 5) each have about 20%, with a fat tail of longer contracts (as many 7 and 8 quarter contracts as 1 quarter contracts). The average contract length in this economy is 3.6 periods.

In Figure 4, we show the impulse response function for output in Taylor's US economy. We find a persistent response in output. In particular, the effect of a monetary shock on output lasts roughly three years. It is evident that incorporating generalized wage setting into a dynamic equilibrium model has a significant effect on dynamic responses of output. We compare this economy with the corresponding simpler GTE with an average contract length of 3.5 periods ($\mathbf{T} = (3,4), \boldsymbol{\alpha} = (0.5,0.5)$). We can see that Taylor's US economy is more persistent: this is because it includes longer contracts despite having almost the same mean.

To summarize this section, in Figure 5 we plot the output responses for 4 different GTEs. The responses are normalized in the sense that the impact is set at 1. From Figure 4 we have Taylor's US economy and the 2-sector GTE, from Fig 2 we have the simple Taylor with 2-period contracts and the case with 10% 8 period contracts. We can also read off the half lives (and quarter lives) of the impulse-response functions, which gives us a quantitative measure of the degree of persistence. For example, when there is simple Taylor economy with only 2-period contracts alongside the GTE with 10% share of 8-period contracts, the half-life increases from 0.74 periods to 1.25 periods. This is also the case when we compare Taylor's US economy with the corresponding Simple Taylor Economy. In particular, half-life increases from 1.98 periods to 2.53 periods.

6 Comparison with a Calvo Economy

It has long been noted that Calvo contracts appear to be far more persistent than Taylor contracts. In this section, we will show that if we focus on the structure of contracts (as opposed to the wage-setting rule), the Calvo economy is a special case of the GTE. Two main features of the Calvo setup stand out as different form the standard Taylor setup. First its "stochastic" nature: at the firm or household level, the length of the wage contract is random. Second, that the model is described in terms of the "age" of contracts (which includes uncompleted durations) and the hazard rate (the reset probability ω). On the first issue, the stochastic nature of the Calvo model at the firm level does affect the wage setting decision. However, apart form the wage setting decision we can describe the Calvo process in deterministic terms at the aggregate level because the firm level randomness washes out. At the aggregate level, the precise identity of individual firms does not matter: what matters is population demographics in terms of proportions of firms setting contracts of particular lengths at particular times. there is a continuum of firms, the behavior of contracts at the aggregate level can be seen as a purely deterministic process.

The second feature is easy to remedy: we can look at either Taylor or Calvo contracts and describe them in terms of either the distribution of completed contract durations (lifetimes) or in terms of the distribution of ages - all durations (complete and incomplete): it is simply two ways of describing the same process. First, we set aside the precise level of wages and observe the duration of wages. We focus on the "demographics" of the contract lengths in a Calvo process⁷. If we take a snapshot of the economy in period t we will observe a proportion ω of wages being reset and the remaining $(1-\omega)$ proportion not being reset. We observe the distribution of durations: a proportion $\omega(1-\omega)^{s-1}$ have been been in place for s periods: of these, a propotion ω will reset in period s+1 (their duration was completed at time s) and a proportion $(1-\omega)$ survive until s+1 (their duration was incomplete at time s).

⁷For a discussion of "life span" and "age", in the unemployment duration literature, see Salant (1977), Carlson and Horrigan (1983). These studies present some examples and show that $E[T \mid s] = 2\omega^{-1}$. However, in discrete time specification needs to be a small adjustment in this formula, as pointed out by Carlson and Horrigan (1983) (cf. Luckett (1979))

The steady-state cross-section of contract ages can be described by the proportions α_i^s of firms surviving at least s periods:

$$\alpha_i^s = \omega \left(1 - \omega \right)^{i-1} : i = 1..\infty \tag{24}$$

with mean $\bar{s} = \omega^{-1}$. In demographic terms, s is the age of the contract: α_i^s is the proportion of the population of age s; \bar{s} is the average age of the population.

The corresponding distribution of *completed* contract lengths i is given by⁸:

$$\alpha_i = \omega^2 i \left(1 - \omega \right)^{i-1} \tag{25}$$

with mean $\bar{T} = \frac{2-\omega}{\omega}$. In demographic terms, α_i gives the distribution of ages at death (for example as reported by the registrar of deaths): α_i being the proportion of the steady state population who will live to die at age T_i .

Assuming that we are in steady state (which is implicit in the use of the Calvo model), we can assume that there are in fact ex ante fixed contract lengths. We can classify household-unions by the duration of their "contract". The fact that the contract length is fixed is perfectly compatible with the notion of a reset probability if we assume that the wage-setter does not know the contract length. We can think of the wage-setter having a probability distribution over contract lengths given by α_i^s in (24): Nature chooses the contract length, but the wage-setters do not know this when they have to set the wage (when the contract begins)⁹.

Having redefined the Calvo economy in terms of completed contract lengths, we can now describe it as a *GTE*. There are an infinite number of sectors, each strictly positive integer corresponding to a contract length:

$$N = \infty$$
 $T_i = i, i = 1...\infty$

The proportions of each completed contract length are given by (25). The wage setting process in each sector is uniform: there are T_i^{-1} cohorts of equal size.

$$N_i = T_i^{-1}, \lambda_{ij} = \frac{1}{T_i}$$

Let us just check that this will yield a contract structure equivalent to the Calvo process. Since the wage setting process is uniform, we can consider the

⁸See Dixon and Kara (2005), Proposition 1.

⁹In game-theory terms wage-setting is done under incomplete information.

representative period. In the sector with T_i period contracts, a proportion α_i/T_i contracts come to an end. Hence, using (25) and summing across all sectors the total measure of all contracts in the economy coming to an end in any period is ω , since:

$$\sum_{i=1}^{\infty} \frac{\alpha_i}{T_i} = \sum_{i=1}^{\infty} \omega^2 \left(1 - \omega\right)^{i-1} = \omega \tag{26}$$

If we look at this Calvo-GTE, the average observed duration of contacts (completed and non-completed) will be ω^{-1} . To see why, let us derive the average age from the distribution of contract lengths. The proportion of contracts age i is obtained by summing across all cohorts who reset wages i periods ago. Clearly, this means we sum only over sectors with completed contract lengths $T \geq i$

$$\alpha_i^s = \sum_{T \ge i}^{\infty} \omega^2 (1 - \omega)^{T-1}$$

$$= \omega^2 (1 - \omega)^{i-1} \sum_{T=1}^{\infty} (1 - \omega)^{T-1}$$

$$= \omega (1 - \omega)^{i-1}$$

Hence, as in Calvo, the average age of contracts in a Calvo-GTE is ω^{-1} and a proportion ω of firms reset their wages each period. The contract demographics of Calvo and Calvo-GTE are indeed the same.

In Figure 6 we have the distribution of completed contract lengths in the Calvo model with $\omega=0.25$, the distribution of contract ages (i.e. steady-state durations, complete and incomplete), and for reference the distribution of contract lengths in Taylor's US economy. As can be seen, the modal completed contract lengths are 3 and 4 quarters which have exactly the same proportions (just over 10%), and the distribution beyond that tails off, with the mean being 7 quarters.

6.1 Wage-setting in the Calvo-GTE

We have defined the Calvo-GTE in terms of the structure of completed contract lengths. The only difference between the Calvo economy and the

Calvo-GTE is in the wage-setting decision (exactly the same arguments and observations apply of price-setting). In the Calvo economy, the wage-setter is uncertain of the contract length: the wage-setting decision must be made "ex ante", that is before the firm knows which length nature has chosen. This yields the standard Calvo wage-setting decision. Once the wage is set, the firm finds out its contract length in due course¹⁰. By contrast, in the Calvo-GTE, the wage-setters know which sector they belong to when they set the wage. Hence, wages in each sector of the Calvo-GTE will be different. Taking the simple case of $\beta = 1$, from (18) the reset wage in sector i with a T_i contract is then the average "optimal" price over the T_i periods is

$$x_{it} = \frac{1}{T_i} \sum_{s=0}^{T_i} (p_{t+s} + \gamma y_{t+s})$$
 (27)

We can calculate the mean reset wage in two ways. First, we define the unconditional mean reset wage, weighting the reset wages in each sector x_{it} with the sectoral weight α_i

$$\hat{x}_t = \sum_{i=1}^{\infty} \alpha_i x_{it} \tag{28}$$

However, if we take the mean conditional on the wage being reset (i.e. leaving out all those who do not reset wages at time t) we get something rather different:

$$\bar{x}_t = \frac{1}{\omega} \sum_{i=1}^{\infty} \frac{\alpha_i}{i} x_{it} = \sum_{i=1}^{\infty} \omega \left(1 - \omega \right)^{i-1} x_{it}$$
 (29)

Within the sector with i period contracts only i^{-1} reset their prices each period. Hence we weight each sector using the proportions resetting using (26). Clearly, if we look at the firms that reset their price, then the less frequent price setters are under-represented relative to their share in the total population. A union that resets every period (i = 1) is counted every period, whilst a firm that resets every 10 periods is only counted once every 10 periods. Note that the weights on the sector i contract x_{it} is the same as the Calvo weight for t + i periods ahead.

There are thus two main differences between the Calvo and the Calvo-GTE wage-setting rules. First, in the Calvo-GTE there is a distribution of

 $^{^{10}}$ It does not matter when: either straight after the pricing decision or at the last moment when it gets the Calvo phone call that it is time to reset the wage.

sector specific reset wages x_{it} in each period. Hence, in addition to the distribution of prices across cohorts (defined by when they last reset prices) as in the Calvo model, the GTE has a distribution across sectors within the cohort.

Second, the Calvo-GTE puts more weight on the immediate future than the Calvo rule. If we expand (29) using (27), we can write the conditional and unconditional mean reset wages in terms of current and future outputs and prices $(p_{t+s} + \gamma y_{t+s})$.

Proposition 1 Let $\beta = 1$.

(a) The unconditional mean reset wage at time t in the Calvo-GTE is

$$\hat{x}_{t} = \sum_{s=0}^{\infty} C_{s} \left(p_{t+s} + \gamma y_{t+s} \right)$$

$$C_{s} = \omega \left(1 - \omega \right)^{s}$$

(b) The conditional mean reset price is

$$\bar{x}_t = \sum_{s=0}^{\infty} b_s \left(p_{t+s} + \gamma y_{t+s} \right)$$

$$b_s = \omega \sum_{T=s+1}^{\infty} \frac{(1-\omega)^{T-1}}{T}$$

Clearly, the unconditional mean reset wage in the Calvo-GTE is equal to the standard Calvo reset wage, with familiar Calvo weights C_s . However, whilst this is a useful reference point, it is not the correct comparison, because it is weighting by sector size, including those who do not reset wages. The conditional mean gives the average reset wage across those who are resetting the wage. The weights of the conditional mean reset reset wage are b_s and can be expressed in terms of the corresponding Calvo weights C_s :

$$b_s = C_s - \frac{s}{s+1}C_s + \sum_{i=s+1}^{\infty} \frac{C_i}{i}$$

If we look at the Calvo-GTE weights b_s , they are a simple transformation of the Calvo weights. Calvo weights on future prices are "passed back" along the line. The general term b_s has three elements: the Calvo weight C_s ;

the weight it passes back equally to all the previous s weights $\frac{s}{s+1}C_j$; and the weight it receives from the subsequent Calvo weights $\sum_{i=s+1}^{\infty} \frac{C_i}{i}$. Thus we can see that the Calvo-GTE puts a much bigger weight on the more immediate future than the Calvo rule. This is intuitive: in every sector $i \geq 1$ there is a proportion i^{-1} weight on the current period t: in every sector $i \geq 2$ there is a weight of i^{-1} period t+1 and so on.

This is best illustrated by the *cumulative weights*: the Calvo-GTE weights up to J are simply the corresponding sum of Calvo weights plus the total weight on dates beyond J passed back to all of the weights s=0...J:

$$\sum_{s=0}^{J} b_s = \sum_{s=0}^{J} C_s + \sum_{k=0}^{J} \sum_{i=k}^{\infty} \frac{C_i}{i+1}$$

In Figure 7 we show the distributions of weights C_s and b_s with $\omega = 0.25$. As we can see, the weight for the first 2 quarters is larger than Calvo, and subsequently less.

We can define the degree of forward-lookingness as the weighted mean of future dates in the reset wage. In Calvo this is simply¹¹ ω^{-1} :

$$FL^{C} = \sum_{s=0}^{\infty} C_{s} (s+1) = \frac{1}{\omega}$$

In the Calvo-GTE this is derived from (29). Note that the wage set by the sector i cohort x_{it} is the mean over periods 1...i,so that the mean forward lookingness in sector i is (i + 1)/2. Hence, from (29) the mean forward-lookingness in the Calvo-GTE is

$$FL^{CGTE} = \sum_{i=1}^{\infty} C_{i-1} \left(\frac{i+1}{2} \right) = \frac{1+\omega}{2\omega}$$

Note that since $\omega < 1$, $FL^C > FL^{CGTE}$. Hence in the Calvo-GTE, the forward-lookingness of wage-resetters as a whole is less than in the equivalent Calvo, with the ratio $FL^C/FL^{CGTE} = \frac{2}{1+\omega}$. With $\omega = 0.25$, the Calvo reset price looks forward on average 4 periods, whilst the Calvo-GTE, the average reset wage looks forward 2.5 quarters.

¹¹We follow the convention of saying that the present (s=0) is period 1 and so on.

If we choose a uniform Taylor process with contract lengths $T = 2\omega^{-1} - 1$, the mean forward-lookingness of the cohort that resets its wage is

$$FL^T = \frac{T+1}{2} = \frac{1}{\omega}$$

Hence $FL^T = FL^C$. This reinforces the insight that the reason that wage-setting in the Calvo-GTE is more myopic than both the simple Taylor and Calvo economies with the same mean contract length, is that in the Calvo-GTE the longer contracts are "under-represented" in the wage-resetters because they reset wages less frequently.

6.2 Persistence in the Calvo and Calvo-GTE compared

We now compare the Calvo-GTE and the standard Calvo economy in terms of the impuls-response functions. In theory, the Calvo-GTE and the Calvo economy are exactly the same in terms of contract structure. However, for computational purposes whilst the Calvo economy effectively has an infinite lag structure (via the Koyck transform), the Calvo-GTE has to be truncated. Hence we also introduce a Calvo-Calvo-GTE: that is the GTE with the same contract structure and wage-setting rule as the Calvo model, but truncated as in the Calvo-GTE. For the simulations, we truncated the distribution of contract lengths to 20 quarters T=1,...20. with the 20 period contracts absorbing all of the weight from the longer contracts. When we apply the standard Calvo pricing rule to this truncated distribution, it yields a perceptible but negligible difference; hence all of the visually apparent differences between the Calvo-GTE and the standard Calvo model are due almost entirely to the difference in wage-setting behaviour.

In Figure 8 we compare the impulse response for the Calvo-GTE which has the same distribution of completed contract lengths as the Calvo distribution, with the standard Calvo economy for $\omega=0.25$. We find that Calvo-GTE has very similar persistence to the Calvo economy. The effect is as little larger for 6 quarters and a little less subsequently, reflecting the less forward looking pricing behaviour. We also show the standard Taylor economy with the same mean contract length $\bar{T}=7$. Although the effect is a greater for the first 5 quarters, the effect dies down and is significantly less

thereafter. This reflects the fact that although the mean contract lengths are the same, the longer contracts in the Calvo and Calvo-GTE generate the extra persistence.

To understand the difference between the Calvo and Calvo-GTE we can focus on wage-setting behavior as depicted in Figure 9. In Fig 9a, we depict the price level in the two cases. We see that the price level rises a bit more in the Calvo case early on (for the first 6 quarters) and a bit less later on (hence mirroring the comparison in terms of output we saw in Figure 8). In Fig 9b we depict the trajectory of the reset wage in both cases: again the Calvo reset wage is a little higher early on (for the first 4 quarters) and a little lower later on. The effect of the permanent increase in the money supply is to lead to an upward trajectory in prices. In the Calvo economy the wage-resetters are more forward looking and so raise wages more in the initial period in anticipation of the future price rises. This leads to a slightly smaller increase in output in the first few periods. As the new steady state is approached, the Calvo resetters slow down the increase in wages, whilst the more myopic calvo-GTE wage resetters keep up the momentum of wage increases, so that the output becomes a little larger in the Calvo case.

7 Conclusions

In this paper we have developed a general framework, the *GTE* which unifies the previously disparate approaches of modelling dynamic price and wage setting: Calvo and Taylor. The approach is a generalization of the simple Taylor model to take into account the presence of a range of different contract lengths. We use this approach to focus on the effect of the presence longer term contracts on the persistence of impulse-response functions generated by a monetary shock. Our conclusions are the following:

- A small proportion of long-term contracts can generate a significant increase in persistence.
- As shown in Kara and Dixon (2005), the average length of contracts in the Calvo model has been seriously underestimated, because the age and life-time of contracts have been confused. If modelers want an average contract length of 4-quarters, they should choose a reset

probability of $\omega = 0.4$. The often used value of 0.25 generates an average contract length of 7 quarters.

- When we compare the standard Calvo model with the corresponding Calvo-*GTE*, we find that although the wage-setting behavior differs, the persistence of the two is very similar.
- The main difference in wage or price setting behaviour between Calvo and Calvo-GTE is in the forward-lookingness of the wage or price setting decision. In the GTE setting, longer contracts reset wages less frequently and so are under-represented amongst wage-resetters relative to their share in the economy. This means reset wages are on average less forward looking than in either the Calvo or simple Taylor economy with same mean contract life.
- In general, if we want to model an economy with many different contract lengths using a simple Taylor economy, we should choose a contract length which is greater than the average. This is because the presence of contracts with longer duration leads to more persistence despite having a similar mean.

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8 Appendix

Proof of Proposition 1(a)

$$\hat{x}_{t} = \sum_{T=1}^{\infty} \omega^{2} T (1 - \omega)^{T-1} \left[\sum_{s=0}^{T} \frac{(p_{t+s} + \gamma y_{t+s})}{T} \right]$$

$$= \sum_{T=1}^{\infty} \omega^{2} (1 - \omega)^{T-1} \left[\sum_{s=0}^{T-1} (p_{t+s} + \gamma y_{t+s}) \right]$$

$$= \omega^{2} (p_{t} + \gamma y_{t}) \sum_{T=1}^{\infty} (1 - \omega)^{T-1} + \omega^{2} (p_{t+1} + \gamma y_{t+1}) \sum_{T=2}^{\infty} (1 - \omega)^{T-1}$$

$$= \omega (p_{t} + \gamma y_{t}) + \omega^{2} (1 - \omega) (p_{t+1} + \gamma y_{t+1}) \sum_{T=1}^{\infty} (1 - \omega)^{T-1}$$

$$= \sum_{s=1}^{\infty} \omega (1 - \omega)^{s-1} (p_{t+s} + \gamma y_{t+s})$$

Proof of Proposition 1(b)

$$\bar{x}_{t} = \sum_{T=1}^{\infty} \omega (1 - \omega)^{T-1} \left[\sum_{s=0}^{T-1} \frac{(p_{t+s} + \gamma y_{t+s})}{T} \right]$$

$$= \omega (p_{t} + \gamma y_{t}) + \omega (1 - \omega) \left[\sum_{s=0}^{1} \frac{(p_{t+s} + \gamma y_{t+s})}{2} \right]$$

$$+ \omega (1 - \omega)^{2} \left[\sum_{s=0}^{2} \frac{(p_{t+s} + \gamma y_{t+s})}{3} \right] + \dots$$

$$= (p_{t} + \gamma y_{t}) \omega \sum_{T=1}^{\infty} \frac{(1 - \omega)^{T-1}}{T} + (p_{t+1} + \gamma y_{t+1}) \omega \sum_{T=2}^{\infty} \frac{(1 - \omega)^{T-1}}{T} + \dots$$

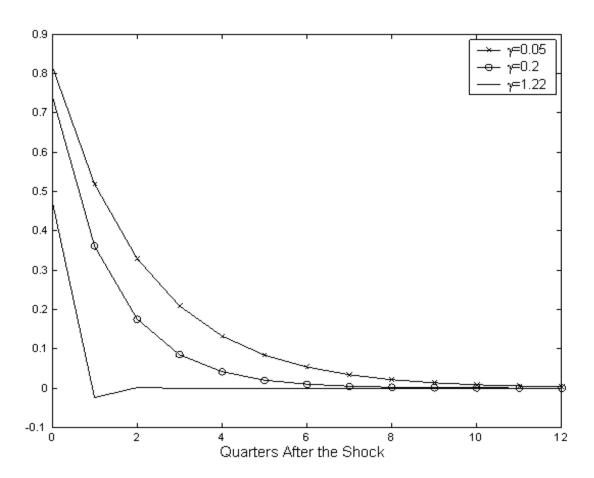


Figure 1: Output Response for Alternative $\gamma's$

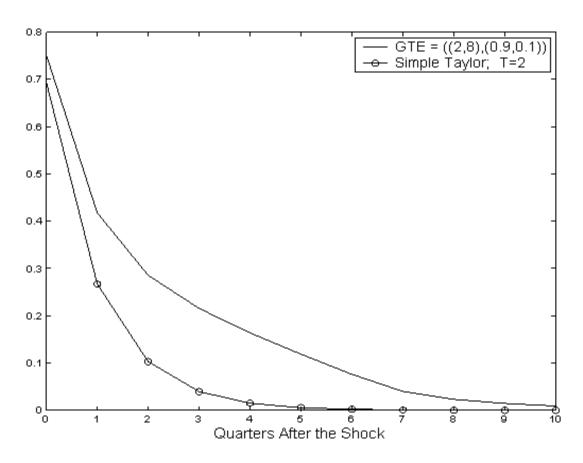
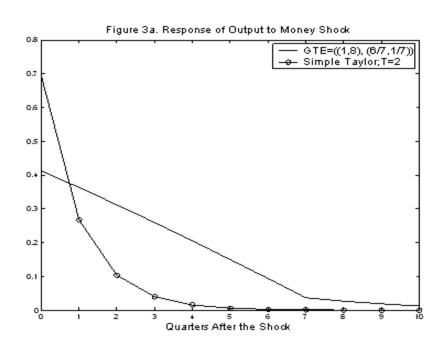


Figure 2: Output Response in Different Settings



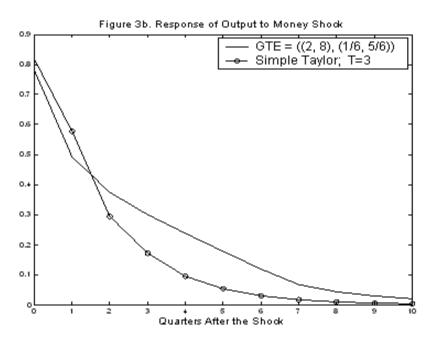


Figure 3: Response of Output in two GTEs with a mean contract length of 2 and 3

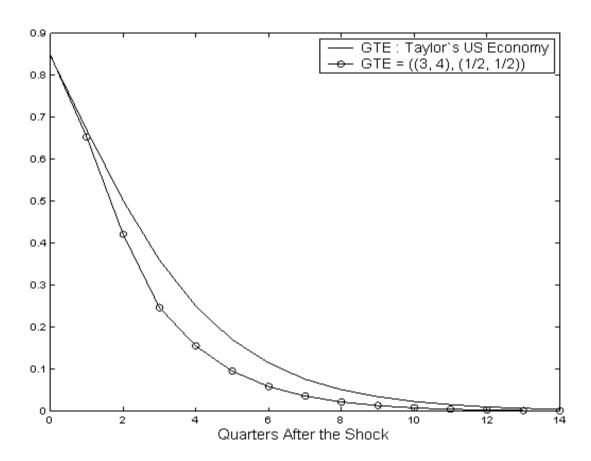


Figure 4: Output response in Taylor's US economy

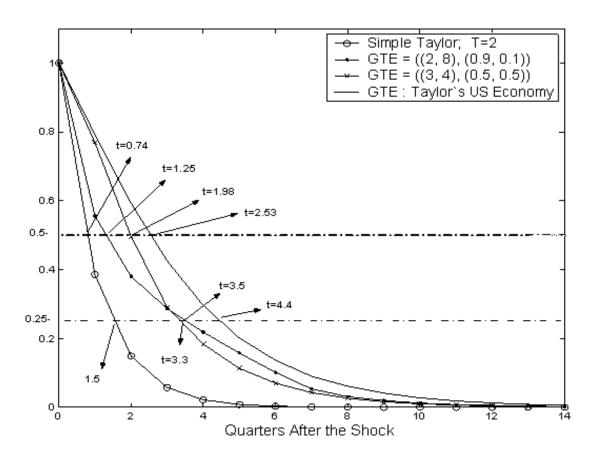


Figure 5: Normalized Responses

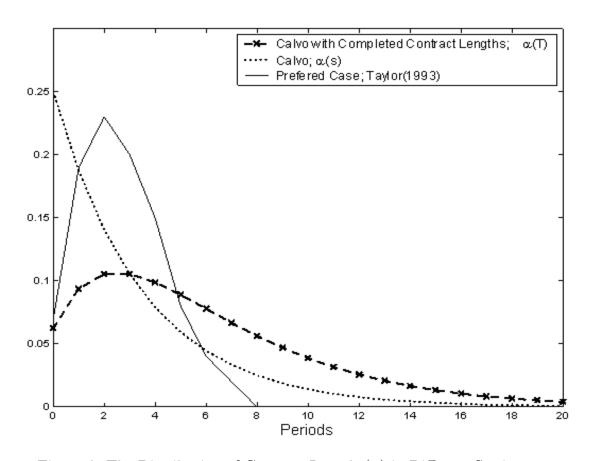


Figure 6: The Distribution of Contract Lengths(α) in Different Settings

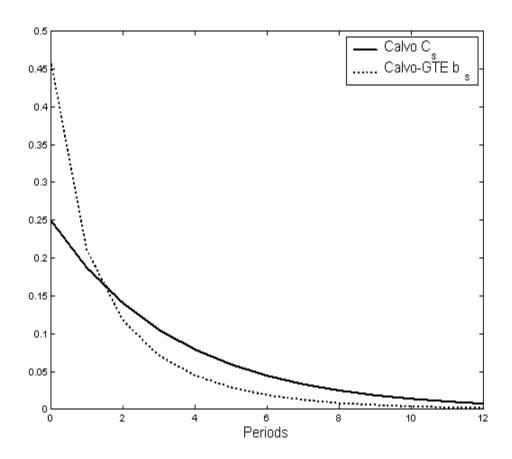


Figure 7: The Weights on future $(p_{t+s}+\gamma y_{t+s})$ for Calvo C_s and Calvo-GTE b_s with $\omega=0.25$

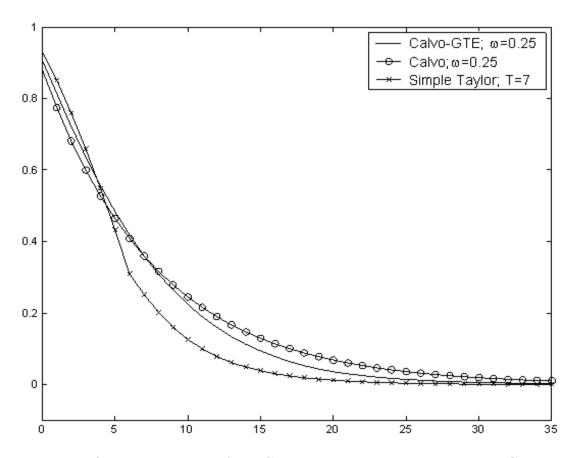
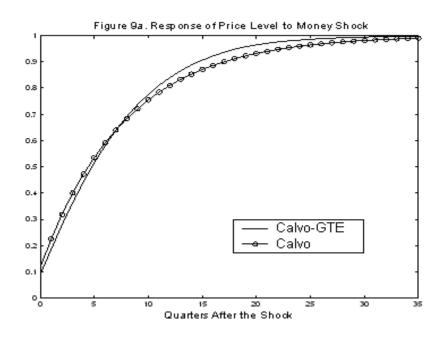


Figure 8: Output responses of the Calvo Economy, the corresponding GTE and simple Taylor economy with same mean contract length



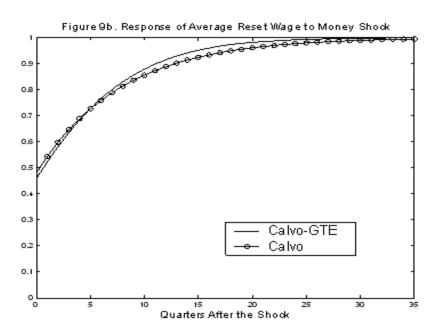


Figure 9: Responses of price level and average reset wage for standard Calvo Economy and Calvo-GTE with $\omega=0.25$

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