

Chang, Chia-Lin; McAleer, Michael; Tian, Jiarong

Working Paper

Modelling and Testing Volatility Spillovers in Oil and Financial Markets for USA, UK and China

Tinbergen Institute Discussion Paper, No. 16-053/III

Provided in Cooperation with:

Tinbergen Institute, Amsterdam and Rotterdam

Suggested Citation: Chang, Chia-Lin; McAleer, Michael; Tian, Jiarong (2016) : Modelling and Testing Volatility Spillovers in Oil and Financial Markets for USA, UK and China, Tinbergen Institute Discussion Paper, No. 16-053/III, Tinbergen Institute, Amsterdam and Rotterdam

This Version is available at:

<https://hdl.handle.net/10419/145360>

Standard-Nutzungsbedingungen:

Die Dokumente auf EconStor dürfen zu eigenen wissenschaftlichen Zwecken und zum Privatgebrauch gespeichert und kopiert werden.

Sie dürfen die Dokumente nicht für öffentliche oder kommerzielle Zwecke vervielfältigen, öffentlich ausstellen, öffentlich zugänglich machen, vertreiben oder anderweitig nutzen.

Sofern die Verfasser die Dokumente unter Open-Content-Lizenzen (insbesondere CC-Lizenzen) zur Verfügung gestellt haben sollten, gelten abweichend von diesen Nutzungsbedingungen die in der dort genannten Lizenz gewährten Nutzungsrechte.

Terms of use:

Documents in EconStor may be saved and copied for your personal and scholarly purposes.

You are not to copy documents for public or commercial purposes, to exhibit the documents publicly, to make them publicly available on the internet, or to distribute or otherwise use the documents in public.

If the documents have been made available under an Open Content Licence (especially Creative Commons Licences), you may exercise further usage rights as specified in the indicated licence.

TI 2016-053/III
Tinbergen Institute Discussion Paper



Modelling and Testing Volatility Spillovers in Oil and Financial Markets for USA, UK and China

*Chia-Lin Chang*¹

*Michael McAleer*²

*Jiarong Tian*³

¹ National Chung Hsing University, Taiwan;

² National Tsing Hua University, Taiwan; Erasmus School of Economics, Erasmus University Rotterdam; Complutense University of Madrid, Spain;

³ National Tsing Hua University, Taiwan.

Tinbergen Institute is the graduate school and research institute in economics of Erasmus University Rotterdam, the University of Amsterdam and VU University Amsterdam.

More TI discussion papers can be downloaded at <http://www.tinbergen.nl>

Tinbergen Institute has two locations:

Tinbergen Institute Amsterdam
Gustav Mahlerplein 117
1082 MS Amsterdam
The Netherlands
Tel.: +31(0)20 525 1600

Tinbergen Institute Rotterdam
Burg. Oudlaan 50
3062 PA Rotterdam
The Netherlands
Tel.: +31(0)10 408 8900
Fax: +31(0)10 408 9031

Modelling and Testing Volatility Spillovers in Oil and Financial Markets for USA, UK and China*

Chia-Lin Chang

Department of Applied Economics
Department of Finance
National Chung Hsing University
Taiwan

Michael McAleer

Department of Quantitative Finance
National Tsing Hua University
Taiwan
and
Econometric Institute
Erasmus School of Economics
Erasmus University Rotterdam
and
Department of Quantitative Economics
Complutense University of Madrid

Jiarong Tian

Department of Quantitative Finance
National Tsing Hua University
Taiwan

Revised: June, 2016

* The authors are grateful to Leh-Chyan So for helpful comments and suggestions. For financial support, the first author wishes to thank the National Science Council, Taiwan, and the second author acknowledges the Australian Research Council and the National Science Council, Taiwan.

Abstract

The primary purpose of the paper is to analyze the conditional correlations, conditional covariances, and co-volatility spillovers between international crude oil and associated financial markets. The paper investigates co-volatility spillovers (namely, the delayed effect of a returns shock in one physical or financial asset on the subsequent volatility or co-volatility in another physical or financial asset) between the oil and financial markets. The oil industry has four major regions, namely North Sea, USA, Middle East, and South-East Asia. Associated with these regions are two major financial centers, namely UK and USA. For these reasons, the data to be used are the returns on alternative crude oil markets, returns on crude oil derivatives, specifically futures, and stock index returns in UK and USA. The paper will also analyze the Chinese financial markets, where the data are more recent. The empirical analysis will be based on the diagonal BEKK model, from which the conditional covariances will be used for testing co-volatility spillovers, and policy recommendations. Based on these results, dynamic hedging strategies will be suggested to analyze market fluctuations in crude oil prices and associated financial markets.

Keywords: Co-volatility spillovers, crude oil, financial markets, spot, futures, diagonal BEKK, optimal dynamic hedging.

JEL Classifications: C58, D53, G13, G31, O13.

1. Introduction

Crude oil is the most influential commodity in energy markets. In industrialized nations, crude oil drives machinery, generates heat, fuels domestic and commercial vehicles, and allows commercial air travel for businesses, and private travel and transportation for domestic and international tourists.

Moreover, crude oil components can produce almost all chemical products, such as plastics and detergents. Refined energy products, such as gasoline and diesel, are also widely used in industry and commerce. As a consequence, crude oil prices affect many industries simultaneously. Crude oil and its derivative products, such as options, futures and forward prices, and associated index and volatility indices, such as Exchange Traded Funds (ETF) and VIX, respectively, are traded widely in international markets.

Crude oil is generally sold near the origin of production, and is transferred from the loading terminal to the free on board (FOB) shipping point. Therefore, spot prices are quoted as FOB prices for immediate delivery of crude oil. Futures prices are quoted for delivering crude oil at a specified time in the future, in a specified quantity, and at a particular trading center. Forward prices of crude oil are agreed on from counterparties in forward contracts. Options are more legal and technical, and are one of the most widely traded financial derivative products.

As shown in Figure 1, the historical price of spot and futures prices of crude oil in UK and USA have has enormous fluctuations since 2007, which coincided with the beginning of the Global Financial Crisis (GFC). Thus analyzing the correlations and spillovers between crude oil markets and financial markets seems to be super useful for making investment strategies.

A stock index is a weighted average of stock prices of selected listed companies. Weights mostly depend on market capitalization. Stock indices give investors insights into decision making by providing an historical perspective of stock market performance.

Investors can invest in index mutual funds to expect as good performance as the market index. Stock index also provides a yardstick for investors to compare with their individual stock portfolios. Stock index can also be used in forecasting movements in the market. The historical prices of financial indices in UK, USA and China are presented in Figures 2 and 3.

[Insert Figures 1-3 here]

Volatility is essential in analyzing any markets with high frequency (daily and weekly data) or ultra-high frequency data (second, minute or hourly data), but it is usually unobservable in commodity and financial markets. Volatility spillovers seem to be widespread in both crude oil and financial markets. A volatility spillover is the lagged effect on one market due to changes of return shocks in another market. Unfortunately, the analysis of volatility and co-volatility spillovers is typically conducted in a confused and confusing manner, with incorrect definitions and inappropriate models being used, mainly with no standard statistical properties underlying the empirical analysis.

The findings of Arouri, Jouini and Nguyen (2009) show significant volatility spillovers between oil price and stock returns. Thus, volatility spillovers and asymmetric effects in crude oil markets and financial markets play important roles in calculating optimal hedge ratios and optimal portfolios.

In an early analysis on the topic of volatility spillovers, Sadorsky (1999) uses a vector autoregression to show that oil price returns and oil price volatility both play important roles in influencing real stock returns in financial markets. Oil price fluctuations and interest rates were shown to account for approximately 5% - 6% of the stock return forecast error variance in the USA.

Faff and Brailsford (1999) find the pervasiveness of an oil price factor, beyond the influence of the market, is detected across some Australian industries. Significant positive oil price sensitivity is found in the Oil and Gas and Diversified Resources

industries, and significant negative oil price sensitivity is found in the Paper and Packaging and Transport industries.

A multivariate vector autoregression was used by Cong, Wei, Jiao and Fan (2008) to investigate the interactive relationships between oil price shocks and the Chinese stock market. The empirical results show that an increase in oil volatility does not affect most stock returns, but may increase the speculative behavior in the mining index and petrochemicals index, which would lead to an increase in their stock returns.

In analyzing 6 OECD countries, Miller and Ratti (2009) show that stock market indices respond negatively to increases in the oil price in the long run. The empirical findings support a conjecture of change in the relationship between real oil prices and real stock prices in the last decade compared with earlier years, which may suggest the presence of several stock market bubbles and/or oil price bubbles since the turn of the Century.

Aloui and Jammazi (2009) use a two-regime Markov-switching EGARCH model to analyze the relationship between crude oil and stock market returns. Unfortunately, the EGARCH model is well-known not to have any regularity conditions, and hence is not invertible and has no asymptotic properties, specifically consistency and asymptotic normality (see McAleer and Hafner (2014)). The paper detects two episodes of Markov-switching time series behavior, specifically, one related to a low mean/high variance regime, and the other related to a high mean/low variance regime.

Given the high chance that the expansion is followed by a recession, Jammazi and Aloui (2009) find that the stock market variables respond negatively and temporarily to crude oil changes during moderate phases in France, and expansion phases in UK and France, but not at levels that would plunge them into a recession phase.

Kilian and Park (2009) show that the reaction of US real stock returns to an oil price shock differ greatly, depending on whether the change in the price of oil is driven by demand or supply shocks in oil markets. Fundamental supply and demand shocks are

identified as underlying the innovations to the real price of crude oil. These shocks together explain one-fifth of the long-term variation in US real stock returns.

The effects of oil price shocks on stock returns in a major oil-exporting country, namely Norway, are analyzed in Bjørnland (2009). The author shows that increasing of oil prices had a stimulating effect on the economy in Norway, which is consistent with the expectation for a country that exports large amount of crude oil. Specifically, following a 10% increase in oil prices, stock returns increased by 2.5%. The maximum effect is reached after 14–15 months (having increased by 4%–5%), after which the effect gradually subsides.

Chang et al. (2013) investigate the crude oil and financial markets by examining the effect of conditional correlations on volatility spillovers. The alternative models used in the empirical analysis are the CCC model of Bollerslev (1990), VARMA-GARCH model of Ling and McAleer (2003), VARMA-AGARCH model of McAleer, Hoti, and Chan (2008), and DCC model of Engle (2002).

The paper will digress slightly from the extant literature by applying the diagonal version of the multivariate extension of the univariate GARCH model, namely the diagonal BEKK as presented in Baba et al. (1985) and Engle and Kroner (1995). Chang et al. (2015) analyzed the literature on volatility and co-volatility spillovers between the energy and agricultural markets, providing and defining useful methodology for testing the effects of such spillovers.

2. Financial Econometrics Methodology

There are alternative multivariate volatility models of conditional covariance for accommodating volatility spillover effects. For example, the Baba, Engle, Kraft, and Kroner (1985) (BEKK) multivariate GARCH model, the diagonal model of Bollerslev et al. (1988), the constant conditional correlation (CCC) (specifically, multiple univariate rather than multivariate) GARCH model of Bollerslev (1990), the *vech* and diagonal *vech*

models of Engle and Kroner (1995), the Tse and Tsui (2002) varying conditional correlation (VCC) model, the Engle (2002) dynamic conditional correlation (technically, dynamic conditional covariance rather than correlation model) (DCC), the Ling and McAleer (2003) vector ARMA- GARCH (VARMA-GARCH) model, and the VARMA–asymmetric GARCH (VARMA- AGARCH) model of McAleer et al. (2009). For further details on these multivariate static and dynamic conditional covariance models see, for example, McAleer (2005).

In order to estimate multivariate models, it is necessary to estimate and acquire the standardized shocks from the conditional mean returns shocks. Therefore, univariate conditional volatility model GARCH and the multivariate conditional covariance models, Diagonal BEKK and the special case of scalar BEKK, will be presented briefly.

Consider the conditional mean of returns, which may be univariate or multivariate, as follows:

$$y_t = E(y_t|I_{t-1}) + \varepsilon_t \quad (1)$$

where the returns, $y_t = \Delta \log P_t$, represent the log-difference in commodity or financial indices prices, P_t , I_{t-1} is the information set available at time $t-1$, and ε_t is an unconditionally homoscedastic, but conditionally heteroskedastic, random error term. In order to derive conditional volatility specifications, it is necessary to specify the stochastic process underlying the returns shocks, ε_t . Much of the following section follows closely the presentation in McAleer (2005), McAleer et al. (2008), and Chang et al. (2015).

2.1. Univariate Conditional Volatility Models

Various univariate conditional volatility models are used in single index models to describe individual financial assets and markets. Univariate conditional volatilities can also be used as standardization of the conditional covariances in different multivariate

conditional volatility models to estimate conditional correlations, which are especially useful in developing optimal dynamic hedging strategies. The GARCH model, as the most popular univariate conditional volatility model, is discussed below.

Consider the random coefficient autoregressive process of order one:

$$\varepsilon_t = \phi_t \varepsilon_{t-1} + \eta_t \quad (2)$$

where

$$\phi_t \sim iid(0, \alpha),$$

$$\eta_t \sim iid(0, \omega),$$

and $\eta_t = \varepsilon_t / \sqrt{h_t}$ is the standardized residual.

Tsay (1987) derived the ARCH(1) model of Engle (1982) from equation (2) as:

$$h_t = E(\varepsilon_t^2 | I_{t-1}) = \omega + \alpha \varepsilon_{t-1}^2 \quad (3)$$

where h_t is conditional volatility, and I_{t-1} is the information set at time $t-1$. The use of an infinite lag length for the random coefficient autoregressive process in equation (2), with appropriate geometric restrictions (or stability conditions) on the random coefficients, leads to the GARCH model of Bollerslev (1986). From the specification of equation (2), it is clear that both ω and α should be positive as they are the unconditional variances of two separate stochastic processes.

The Quasi Maximum Likelihood Estimator (QMLE) of the parameters of ARCH and GARCH have been shown to be consistent and asymptotically normal in several papers. For example, Ling and McAleer (2003) showed that the QMLE for GARCH(p, q) is consistent if the second moment is finite. Moreover, a weak sufficient log-moment

condition for the QMLE of GARCH(l, l) to be consistent and asymptotically normal is given by:

$$E(\log(\alpha\eta_t^2 + \beta)) < 0, \quad |\beta| < 1$$

which is not easy to check in practice as it involves two unknown parameters and a random variable. The more restrictive second moment condition, namely $\alpha + \beta < 1$, is much easier to check in practice.

In general, the proofs of the asymptotic properties follow from the fact that ARCH and GARCH can be derived from a random coefficient autoregressive process. In this context, McAleer et al. (2008) provide a general proof of the asymptotic properties of multivariate conditional volatility models that are based on proving that the regularity conditions satisfy the regularity conditions given in Jeantheau (1998) for consistency, and the conditions given in Theorem 4.1.3 in Amemiya (1985) for asymptotic normality.

2.2 Multivariate Conditional Volatility Models

The multivariate extension of the univariate GARCH model is given in Baba et al. (1985) and Engle and Kroner (1995). In order to establish volatility spillovers in a multivariate framework, it is useful to define the multivariate extension of the relationship between the returns shocks and the standardized residuals, that is, $\eta_t = \varepsilon_t / \sqrt{h_t}$.

The multivariate extension of equation (1), namely $y_t = E(y_t | I_{t-1}) + \varepsilon_t$, can remain unchanged by assuming that the three components are now $m \times 1$ vectors, where m is the number of crude oil or financial assets. The multivariate definition of the relationship between ε_t and η_t is given as:

$$\varepsilon_t = D_t^{1/2} \eta_t \tag{4}$$

where $D_t = \text{diag}(h_{1t}, h_{2t}, \dots, h_{mt})$ is a diagonal matrix comprising the univariate conditional volatilities. Define the conditional covariance matrix of ε_t as H_t . As the $m \times 1$ vector, η_t , is assumed to be *iid* for all m elements, the conditional correlation matrix of ε_t , which is equivalent to the conditional correlation matrix of η_t , is given by Γ_t . Therefore, the conditional expectation of (4) is defined as:

$$H_t = D_t^{1/2} \Gamma_t D_t^{1/2} . \quad (5)$$

Equivalently, the conditional correlation matrix, Γ_t , can be defined as:

$$\Gamma_t = D_t^{-1/2} H_t D_t^{-1/2} . \quad (6)$$

Equation (5) is useful if a model of Γ_t is available for purposes of estimating H_t , whereas equation (6) is useful if a model of H_t is available for purposes of estimating Γ_t .

Equation (5) is convenient for a discussion of volatility spillover effects, while both equations (5) and (6) are instructive for a discussion of asymptotic properties, especially for the full BEKK model without appropriate parametric restrictions. As the elements of D_t are consistent and asymptotically normal, the consistency of H_t in (5) depends on consistent estimation of Γ_t , whereas the consistency of Γ_t in (6) depends on consistent estimation of H_t . As both H_t and Γ_t are products of matrices, and the inverse of the matrix D is not asymptotically normal, even when D is asymptotically normal, neither the QMLE of H_t nor Γ_t will be asymptotically normal, especially based on the definitions that relate the conditional covariances and conditional correlations given in equations (5) and (6).

2.2.1 Diagonal and Scalar BEKK

The vector random coefficient autoregressive process of order one is the multivariate extension of equation (2), and is given as:

$$\varepsilon_t = \Phi_t \varepsilon_{t-1} + \eta_t \quad (7)$$

where ε_t and η_t are $m \times 1$ vectors, Φ_t is an $m \times m$ matrix of random coefficients, and

$$\begin{aligned} \Phi_t &\sim iid(0, A), \\ \eta_t &\sim iid(0, HH'). \end{aligned}$$

Technically, a vectorization of a full (that is, non-diagonal or non-scalar) matrix A to vec A can have dimension as high as $m^2 \times m^2$, whereas vectorization of a symmetric matrix A to $vech$ A can have dimension as low as $m(m-1)/2 \times m(m-1)/2$. Neither of these possibilities is as small in dimension as $m \times m$, which is required to generate an appropriate BEKK model with any regularity conditions or asymptotic properties.

In a case where A is either a diagonal matrix, or the special case of a scalar matrix, $A = \alpha I_m$, McAleer et al. (2008) showed that the multivariate extension of GARCH($1, 1$) from equation (7), incorporating an infinite geometric lag in terms of the returns shocks, is given as the diagonal (or scalar) BEKK model, namely:

$$H_t = HH' + A\varepsilon_{t-1}\varepsilon'_{t-1}A' + BH_{t-1}B' \quad (8)$$

where A and B is a diagonal (or scalar) matrix.

McAleer et al. (2008) showed that the QMLE of the parameters of the diagonal, and hence also the scalar, BEKK models are consistent and asymptotically normal, so that standard statistical inference on testing hypotheses is valid. Moreover, as H_t in equation (8) can be estimated consistently, Γ_t in equation (6) can also be estimated consistently. However, as explained above, asymptotic normality cannot be proved given the definitions in equations (5) and (6).

In terms of volatility spillovers, as the off-diagonal terms in the second term on the right-hand side of equation (8), $\varepsilon_{t-1}\varepsilon'_{t-1}A'$, have typical (i,j) elements $a_{ii}a_{jj}\varepsilon_{it-1}\varepsilon_{jt-1}$, $i \neq j$, $i, j = 1, \dots, m$, there are no full volatility or full co-volatility spillovers. However, partial co-volatility spillovers are not only possible, but they can also be tested using valid statistical procedures.

2.3 Spillovers

Conditional correlations and spillovers between international crude oil and associate financial markets describe the delayed effect of a returns shock in one commodity or financial asset on the subsequent volatility or co-volatility in another commodity or financial asset.

Define H_t as the conditional covariance matrix of ε_{t-1} . It follows that:

- Full volatility spillovers: $\frac{\partial H_{ii}}{\partial \varepsilon_{kt-1}}$, $k \neq i$;
- Full co-volatility spillovers: $\frac{\partial H_{ij}}{\partial \varepsilon_{kt-1}}$, $k \neq i, j$;
- Partial co-volatility spillovers: $\frac{\partial H_{ij}}{\partial \varepsilon_{kt-1}}$, $i \neq j, k = \text{either } i \text{ or } j$.

where $i, j, k = 1 \dots m$; ε_t is returns shocks, and H_t is the conditional covariance matrix of ε_t .

Full volatility spillovers occur when the returns shock from financial asset k affects the volatility of a different financial asset i .

Full co-volatility spillovers occur when the returns shock from financial asset k affects the co-volatility between two different financial assets, i and j .

Partial co-volatility spillovers occur when the returns shock from financial asset k affects the

co-volatility between two financial assets, i and j , one of which can be asset k .

When $m = 2$, only full volatility spillovers and partial co-volatility spillovers are possible as full co-volatility spillovers depend on the existence of a third financial asset.

2.4 Dynamic Optimal Hedging Strategies

As investors trade massively in both commodity and financial assets, spillovers can provide investors with a basis to understand and hedge optimally using derivatives in both markets. The optimal dynamic hedge ratio is the size of the futures contract relative to the cash transaction.

According to Chang et al. (2011), consider the case of an oil company, which seeks to protect their exposure in the crude oil spot price by taking a position in a futures financial markets. The return on the oil company's portfolio of spot and futures position can be denoted as:

$$R_{H,t} = R_{S,t} - \gamma_t R_{F,t}, \quad (9)$$

where $R_{H,t}$ is the return on holding the portfolio between $t-1$ and t , $R_{S,t}$ and $R_{F,t}$ are the returns on holding spot and futures positions between t and $t-1$, and γ_t is the dynamic hedge ratio, that is, the number of futures contracts that the hedger must sell for each unit of a spot commodity on which price risk is borne.

According to Johnson (1960), the variance of the returns of the hedged portfolio, conditional on the information set available at time $t-1$, is given by

$$\text{var}(R_{H,t}|\Omega_{t-1}) = \text{var}(R_{S,t}|\Omega_{t-1}) - 2\gamma_t \text{cov}(R_{S,t}, R_{F,t}|\Omega_{t-1}) + \gamma_t^2 \text{var}(R_{F,t}|\Omega_{t-1}) \quad (10)$$

where $\text{var}(R_{S,t}|\Omega_{t-1})$, $\text{var}(R_{F,t}|\Omega_{t-1})$, and $\text{cov}(R_{S,t}, R_{F,t}|\Omega_{t-1})$ are the conditional variances and covariance of the spot and futures returns, respectively. The Optimal

Hedging Ratios (*OHR*) are defined as the value of γ_t which minimizes the conditional variance (risk) of the hedged portfolio returns.

Taking the partial derivative of equation (10) with respect to γ_t , setting it equal to zero, and solving for γ_t , yields the OHR_t conditional on the information available at $t-1$ (see, for example, Baillie and Myers (1991)):

$$\gamma_t^* | \Omega_{t-1} = cov(R_{S,t}, R_{F,t} | \Omega_{t-1}) / var(R_{F,t} | \Omega_{t-1}), \quad (11)$$

where returns are defined as the logarithmic differences of spot and futures prices. Estimates of dynamic conditional volatility and co-volatility for purposes of testing spillover effects will be undertaken using alternative univariate and multivariate conditional volatility models, as discussed above.

3. Data and Variables

As the topic of the paper is to test co-volatility spillovers in the crude oil and financial markets, important indices in both markets are taken into consideration and will be discussed below.

3.1. Crude oil markets

Two key indices used in crude oil markets are West Texas Intermediate (WTI) in the USA and Brent Blend Oil Index in the UK. Daily spot and futures price of WTI, and the futures price of Brent, are available during from 24 June 1988 to 13 May 2016, but there is no spot price available for Brent. All the crude oil indices used in the paper are expressed in US dollars and in cents per barrel.

WTI refers to oil extracted from wells in the USA and sent via pipeline to Cushing, Oklahoma. The transportation price of WTI is relatively expensive because supplies are land-locked, and cannot be transported in large quantities, as can be done where large

container ships are used. WTI oil is very light and sweet, which makes it ideal for the refining of gasoline.

The New York Mercantile Exchange (NYMEX) designates petroleum with less than 0.42% Sulphur as sweet. Higher levels of Sulphur content are called sour crude oil. NYMEX defines light crude oil for domestic USA oil as having an American Petroleum Institute (API) gravity between 37° API (840 kg/m³) and 42° API (816 kg/m³). API gravity is a measure of how heavy or light a petroleum liquid is compared with water. If its API gravity is greater than 10, it is lighter and floats on water; if it is less than 10, it is heavier and sinks. Light crude oil produces a higher percentage of gasoline and diesel, so the price is higher than that of heavy crude oil.

The daily spot price of WTI is available using “Bloomberg West Texas Intermediate (WTI) Cushing Crude Oil Spot Price”. It uses benchmark WTI crude at Cushing, Oklahoma, and other USA crude oil grades trade on a price spread differential to WTI, Cushing. Prices are on a free-on-board basis. WTI crude oil at Cushing, Oklahoma typically trades in pipeline lots of 1,000 to 5,000 barrels a day, for delivery between the 25th day in one month to the 25th of the following month. These prices are for physical shipments. API gravity is 39°, while the sulfur content is 0.34%. The number of barrels per ton is 7.640.

Daily futures price of WTI is available under the designation “CL1 COMDTY” in Bloomberg. It is Generic 1st ‘CL’ Future, which is one-month-front contract, traded at NYMEX. The contract trades in units of 1,000 barrels, and the delivery point is Cushing, Oklahoma.

Brent Blend refers to oil from four different fields in the North Sea, namely Brent, Forties, Oseberg and Ekofisk. Crude oil from this region is less “light” and “sweet” than that of WTI, but it is still an excellent product for the refining of diesel fuel, gasoline and other high-demand products. As the supply is water borne, it is relatively easy to transport large quantities to distant locations.

The daily futures Price of Brent Blend is available under the designation “CO1 COMDTY” in Bloomberg. It is Generic 1st ‘CO’ Future, which is also one-month-front contract, traded at the Intercontinental Exchange (ICE) in the UK. The unit of trading is one or more lots of 1,000 net barrels of Brent crude oil.

3.2. Financial Markets

The paper examines three leading financial markets internationally, namely USA, the UK and China. Daily data are used for eight indices, namely S&P 500 Spot, S&P 500 Futures, FTSE 100 Spot, FTSE 100 Futures, SSE Composite Spot, SZSE Composite Spot, China A50 Spot, and China A50 Futures.

For the US market, both daily spot and daily futures prices of the widely-used Standard & Poor’s 500 Composite Index (S&P 500) is accessible from 24 June 1988 to 13 May 2016. S&P 500 is based on the market capitalizations of 500 large companies listed on the NYSE or NASDAQ. It is one of the most suitable representations available of the stock market in the USA, which is expressed in US dollars.

For the UK market, daily spot and daily futures prices of the Financial Times Stock Exchange 100 Index (FTSE 100) are available from 24 June 1988 to 13 May 2016. FTSE 100 is an index of the 100 companies with the largest capitalization listed on the London Stock Exchange. The index is considered a benchmark of prosperity for business under the company law of UK, which is calculated in GdP.

Regarding the Chinese markets, both domestic and non-domestic indices are considered. In domestic Chinese financial markets, the daily spot price of the Shanghai Stock Exchange Composite Index (SSE Composite) and Shenzhen Stock Exchange Composite Index (SZSE Composite) are seen as the leading indicators of financial market trends in China. The SSE Composite includes all stocks (A shares and B shares) that are traded at

the Shanghai Stock Exchange, and SZSE Composite calculates all stocks listed on the Shenzhen Stock Exchange.

A shares are denominated in CNY traded by domestic investors, whereas B shares are denominated in foreign currencies traded by qualified international investors. Until 13 May 2016, there were 1,140 listed companies are included in SSE Composite, and 1,808 companies were available in SZSE Composite. Both spot prices are calculated in CNY. SSE Composite is available from 19 December 1990, and SZSE Composite is available from 2 January 1992.

Another important index is the FTSE China A50, which is the benchmark for international investors to access China's domestic financial market through A Shares. The index incorporates the 50 largest A share companies by market capitalization. Daily spot and futures price of FTSE China A50 are available from 5 January 2007 to 13 May 2016, and are denominated in CNY. As the paper emphasizes hedging strategies in both spot and futures markets, for Chinese financial markets, only data after 5 January 2007 are used when China A50 futures price were initiated.

The paper uses daily time series data from 24 June 1988 to 13 May 2016, where all the data are downloaded from Bloomberg. Three time periods are also analyzed from the whole period due to the Global Financial Crisis (GFC) that occurred between 2007 and 2009, namely Pre-GFC (from 24 June 1988 to 4 January 2007), GFC (from 5 January 2007 to 5 March 2009), and Post-GFC (from 6 March 2009 to 13 May 2016).

The initial date of the GFC is widely regarded as having started somewhere between November 2007 (the high point of the S&P 500 Composite Index prior to the GFC) to August 2009 (after Lehmann Brothers entered bankruptcy). In the paper, the starting point of the GFC is taken to be the date when the futures price of China A50 became available, namely August 2007. By adding seven months of data, the prices and returns move with slightly lower volatility.

3.3. Descriptive Statistics and Unit Root Tests

The returns of crude oil prices and financial market indices are calculated on a continuous compound basis, defined as:

$$r_{ij,t} = 100 \times \log\left(\frac{P_{ij,t}}{P_{ij,t-1}}\right)$$

where $P_{ij,t}$ and $P_{ij,t-1}$ are the closing prices i of market j for days t and $t-1$, respectively. WTI-s, WTI-f, BRENT-f, SP500-s, SP500-f, FTSE-s, FTSE-f, SH-s, SZ-s, CNA50-s, CNA50-f denote returns of WTI spot prices, returns of WTI futures prices, returns of BRENT futures prices, returns of S&P 500 spot prices, returns of S&P futures prices, returns of FTSE 100 spot prices, returns of FTSE 100 futures prices, returns of SSE Composite, returns of SZSE Composite, returns of FTSE China A50 spot prices, and returns of FTSE China A50 futures prices, respectively.

The descriptive statistics for crude oil returns and financial index returns in UK and USA for four time periods, which are whole sample (1988-2007), Pre-GFC (1988-2007), GFC (2007-2009) and Post-GFC (2009-2016), are reported in Table 1.

[Insert Table 1 here]

All the series present large negative mean returns for the During-GFC period, whereas mean returns for each of the variables are positive for Pre-GFC, Post-GFC and the Whole Period. Crude oil returns show a larger standard deviation than financial index returns for all periods, indicating that crude oil markets are more volatile than financial markets, in general, at the aggregate level. Not surprisingly, all the variables have the largest standard deviations for all variables During-GFC.

However, except for futures returns of BRENT, all the maximum values exist During-GFC, indicating that, although crude oil markets and financial markets are volatile

During-GFC, large positive returns can be obtained during the same period. As for the minimum value, crude oil returns display large negative returns Pre-GFC, due to the fact that, on 16 January 1991, USA began an air attack against Iraqi military targets, as well as the drawdown of Strategic Petroleum Reserves (SPR) in the USA.

The normal distribution has skewness of zero and kurtosis of 3. Spot and futures returns of WTI show positive skewness During-GFC and Post-GFC. Futures returns of BRENT also have positive skewness. These statistics show that Post-GFC, crude oil markets have more extreme positive returns. Nevertheless, financial index returns always present negative skewness, except futures returns of S&P 500 During-GFC, indicating that compared with crude oil markets, financial markets are more likely to have extreme negative returns.

All the return series have high kurtosis, suggesting the existence of fat tails. The Jarque-Bera Lagrange Multiplier statistics of all series of returns are statistically significant, indicating non-normality in the distribution of returns.

As shown in Table 2, descriptive statistics for China During-GFC and Post-GFC display similar results to those in Table 1. SSE Composite, China A50 spot and futures show negative mean returns During-GFC, and positive mean returns Post-GFC. SZSE Composite has positive mean returns for the During-GFC and Post-GFC periods, indicating that, in general, the companies listed on SZSE performed well During-GFC and Post-GFC. All returns During-GFC and Post-GFC show negative skewness, large kurtosis, and large Jarque-Bera Lagrange Multiplier statistics, indicating that it is likely to have negative returns in Chinese financial markets, on average, and that the returns are not normally distributed.

[Insert Table 2 here]

Table 3 presents the correlation matrix for crude oil and financial markets in UK and USA for the Pre-GFC, During-GFC and Post-GFC periods. Most of the correlation

coefficients between pairs of variables show an increasing trend from Pre-GFC to Post-GFC, indicating that spot and futures returns for crude oil and financial markets have been more closely tied together in recent years. This empirical regularity strengthens the need and importance of testing for co-volatility spillovers between indices in crude oil and financial markets.

[Insert Table 3 here]

The highest correlation coefficient in the whole sample is between the spot and futures returns of S&P 500, at 0.974, followed by the spot and futures return correlation coefficient of 0.963. The spot and futures returns are also highly correlated in WTI, at 0.901, and with BRENT, at 0.804. The correlation coefficient between WTI spot returns and BRENT futures returns is 0.795, indicating that returns of oil markets are relatively highly correlated between UK and USA.

The financial markets in UK and USA are only moderately correlated. The correlation coefficient between spot returns of S&P 500 and FTSE 100 is 0.491. However, by examining the whole sample, returns from crude oil markets and financial markets are slightly correlated. Specifically, the highest correlation coefficient is 0.147 between futures returns of WTI and spot returns of FTSE 100.

Pre-GFC, the correlation coefficients are all negative and close to 0 between the crude oil and financial markets. During-GFC and Post-GFC, the two markets become moderately correlated. Specifically, the highest correlation between crude oil and financial markets Post-GFC is 0.430, which is between the spot or futures returns of WTI and spot returns of S&P 500.

Table 4 shows the correlations of crude oil in UK and USA, and financial markets in China During-GFC and Post-GFC. Focusing on the financial markets in China During-GFC and Post-GFC, the highest correlation coefficient is 0.948 between SSE Composite

returns and China A50 spot returns, followed by 0.930 between spot and futures returns of China A50.

Interestingly, the correlation coefficient between SSE Composite returns and SZSE Composite returns is 0.902, whereas SZSE Composite returns and China A50 spot returns have a correlation coefficient of only 0.783. The reason behind the statistics might be the fact that there are only 7 SZSE-listed companies in China A50, so the leading companies in SSE Composite are also included in China A50.

[Insert Table 4 here]

The correlation coefficients between crude oil in UK and USA, and financial markets in China, are generally very low. The highest coefficient is 0.132, which is between futures returns of BRENT and SSE Composite returns Post-GFC. Comparing this number with the correlation coefficients between crude oil and financial markets in UK and USA, it is only one-third of those in UK and USA. These results indicate that China has limited experience regarding trading in international crude oil markets.

In the interests of saving space, the unit root tests of all the variables for all time periods are not reported. In order to summarize the unit root tests results, all prices are found to be nonstationary, while all return series are found to be stationary.

4. Empirical Results

By testing the significance of the estimates of matrix A in the Diagonal BEKK model, the co-volatility spillover effects can be obtained directly. Specifically, if the null hypothesis is rejected, there will exist spillovers from the returns shock of commodity or financial index j at $t-1$ to the co-volatility between commodities or financial indices i and j at t that depends only on the returns shock of commodity or financial index i at $t-1$. Estimation of the model in equations (1) and (2) by QMLE is accomplished by using the EViews 8 econometric software package.

4.1. UK and USA

Tables 5-10 report the empirical results of the estimates of matrix A of the Diagonal BEKK model, with various dimensions for the UK and US markets. The estimates of the coefficients in matrix A can be interpreted as the weights that each variable have on the co-volatility. Mean return shocks and mean co-volatility spillovers are calculated in order to obtain a more precise interpretation and understanding of the two markets.

Table 5 shows the estimates of matrix A using 2 x 2 Diagonal BEKK for spot markets for UK and USA for four periods. Specifically, spot returns of WTI are tested with spot returns of S&P 500 and spot returns of FTSE 100, respectively. Thus for each period, there are two pairs of mean co-volatility spillovers.

[Insert Table 5 here]

From the estimates of matrix A of the Diagonal BEKK model in Table 5, all the coefficients are statistically significant at the 1% level. For example, the coefficients are 0.236 and 0.248 for WTI spot and S&P 500 spot prices during the whole sample. The empirical results show that there are spillover effects from the spot returns of WTI at $t-1$ to the co-volatility between WTI spot and S&P 500 spot prices, and from the spot returns of S&P 500 at $t-1$ to the co-volatility between WTI spot and S&P 500 spot prices. Similar empirical results and interpretations hold for the Pre-GFC, During-GFC and Post-GFC sub-periods.

As highlighted in bold in Table 5, there are 2 of 8 scalar matrices A , which are WTI spot and S&P 500 spot prices for the whole period, and WTI spot and FTSE spot prices Pre-GFC. The scalar matrix A shows that the two variables have similar weights on the co-volatility between the pair. If the two variables have different effects on their respective co-volatility, a diagonal matrix A will be interpreted as appropriate weights. In Table 5, there are 4 of 8 diagonal matrices A , which are highlighted in italics.

The mean return shocks for all pairs of variables are shown alongside the estimates of the weight matrix A . The highest difference in mean return shocks is between WTI spot and S&P 500 spot prices Pre-GFC at 0.036. The partial co-volatility spillovers effects are calculated according to the definition presented in Section 2. The columns of mean co-volatility spillover effects show that there are significant co-volatility spillovers in all the cases presented.

The largest absolute value of mean co-volatility spillovers in Table 5 is from spot returns of FTSE 100 to the mean co-volatility between WTI spot and FTSE 100 spot prices During-GFC. It can also be found that the mean co-volatility spillovers have the largest absolute values During-GFC as compared with Pre-GFC and Post-GFC. These empirical results correspond with the fact that During-GFC, the volatility in crude oil markets and financial markets is higher than in the Pre-GFC and Post-GFC sub-periods.

Table 5 shows that Pre-GFC, the mean co-volatility spillovers have different signs in each of the testing pairs, whereas the mean co-volatility spillovers all have negative signs in the pairs During-GFC and Post-GFC. Optimal hedging strategies can be considered if the product of the two mean return shocks is negative. Therefore, there are little or no hedging opportunities between the oil spot and financial spot markets During-GFC and Post-GFC, as indicated by the 2 x 2 Diagonal BEKK model, whereas dynamic hedging is possible in the Pre-GFC sub-period.

Table 6 demonstrates the estimates of the weight matrix A using the 2 x 2 Diagonal BEKK model for futures markets for UK and USA for the four periods. In each period, WTI futures returns are analyzed in combination with S&P 500 returns and FTSE 100 returns. BRENT futures returns are also tested in related to the futures returns of the two financial markets. Therefore, there are four pairs of spillovers tests to be considered for each period.

[Insert Table 6 here]

As shown in Table 6, all the estimates of the weight matrix A are significant at the 1% level, indicating that each of the variables has significant impacts on the co-volatility in alternative pairs. Among 16 pairs that are considered, 4 pairs show scalar matrices A . WTI futures and FTSE 100 futures, BRENT futures and FTSE 100 futures Pre-GFC both demonstrate scalar weights in matrix A . Of 16 pairs, 7 are found to have diagonal matrices A .

The results of the signs for futures mean co-volatility spillovers are similar to those of the spot prices. Positive and negative signs of mean co-volatility spillovers can be seen Pre-GFC. The signs are always the same for each pair During-GFC and Post-GFC. When the products of the mean return shocks are examined, optimal hedging strategies can only be applied Pre-GFC.

A 3 x 3 Diagonal BEKK model can be used if three spot returns, namely WTI spot, S&P 500 spot and FTSE 100 spot prices, are estimated simultaneously. Table 7 shows the results of the weight matrix A in the 3 x 3 Diagonal BEKK model, the mean return shocks, and mean co-volatility spillovers for all sets of three spot prices. All the estimates of matrix A are statistically significant at the 1% level. For the whole sample period, the coefficients are scalar, whereas the estimates of matrix A are diagonal in the separate sub-periods Pre-GFC, During-GFC, and Post-GFC.

[Insert Table 7 here]

The mean co-volatility spillovers have similar results as for the 2 x 2 Diagonal BEKK model. Examination of the whole sample and Pre-GFC sub-period, optimal hedging strategies can be considered between WTI spot and S&P 500 spot prices, and WTI spot and FTSE 100 spot prices. However, there is little or no opportunity of hedging between these two pairs During-GFC and Post-GFC.

Table 8 presents the results of the weight matrix A in the 4 x 4 Diagonal BEKK model, the mean return shocks, and mean co-volatility spillovers for UK and US futures markets in the four periods. It is notable that in the Post-GFC sub-period, WTI futures, BRENT futures and FTSE 100 futures have similar estimates of the weights, namely 0.217, 0.222, and 0.225, respectively, but S&P 500 futures provide a distinctly different coefficient at 0.291). As for the results of mean co-volatility spillovers, it confirms the interpretation of the results in Tables 5-7. Optimal dynamic hedging is not possible between crude oil futures markets and financial futures markets During-GFC and Post-GFC by using a 4 x 4 Diagonal BEKK model.

[Insert Table 8 here]

It would be interesting to analyze the spot and futures markets in pairs. Tables 9 and 10 provide the results of a 7 x 7 Diagonal BEKK model consisting of 3 crude oil returns, namely WTI spot, WTI futures and BRENT futures, and 4 financial index returns, namely S&P 500 spot, S&P 500 futures, FTSE 100 spot and FTSE 100 futures. As can be seen from the estimates of the weights of matrix A , all the matrices are found to be diagonal. Although spot and futures markets are analyzed together to determine mean co-volatility spillovers, similar results are found to hold as in the cases of lower dimensions, namely the crude oil and financial markets in UK and USA cannot be hedged using a 7 x 7 Diagonal BEKK model.

[Insert Tables 9-10 here]

4.2. China

Tables 11 and 12 present the estimates of the weight matrix A in the Diagonal BEKK model, mean return shocks, and mean co-volatility spillovers, for the crude oil markets in UK and USA, and financial markets in China, for the During-GFC and Post-GFC sub-periods.

Table 11 shows the results of the 2 x 2 Diagonal BEKK model. All the coefficients of matrix A are statistically significant at the 1% level. Among the 15 pairs of spillovers that are analyzed, there are 9 pairs of variables that display estimates of diagonal matrices A . It is worth mentioning that for the Post-GFC period, diagonal matrix A exists in each pair of variables, indicating that Post-GFC, Chinese financial markets and crude oil markets in the UK and USA have nearly the same impacts on the co-volatility among any pair of commodities and markets.

[Insert Table 11 here]

Interestingly, the results of the mean co-volatility spillovers in Chinese markets are quite different from the empirical results presented for UK and USA. Positive and negative mean co-volatility spillovers pairs can be seen Post-GFC, indicating that there is an opportunity that optimal dynamic hedging strategies can be obtained by using a 2 x 2 Diagonal BEKK model.

Table 12 shows the results of a 5 x 5 Diagonal BEKK model, using three crude oil indices, namely WTI spot, WTI futures and BRENT futures, and two financial indices in China, namely China A50 spot and China A50 futures. The estimates of matrix A are all statistically significant at the 1% level, and all the matrices are diagonal. In addition, the resulting mean co-volatility spillovers are consistent with the results presented in Table 9, which demonstrate that it is possible to hedge by using a 5 x 5 Diagonal BEKK model in Chinese financial markets, together with UK and US crude oil markets Post-GFC.

[Insert Table 12 here]

5. Concluding Remarks

The main purpose of the paper was to analyze the conditional correlations, conditional covariances, and spillovers between international crude oil and associated financial markets.

The oil industry has four major regions, namely the North Sea, USA, Middle East, and South-East Asia. Associated with these four regions are three major financial centers, namely those centred in UK, USA and China, for which the data are more recent. The paper examined the co-volatility spillover effects between crude oil and financial markets among these three countries by partitioning the whole sample time period from 1988 to 2016 into three representative time periods that are associated with the Global Financial crisis (GFC), namely Pre-GFC, GFC and Post-GFC.

The paper analyzed three crude oil indices returns and eight financial indices returns using various dimensions of the multivariate conditional covariance Diagonal BEKK model, from which the conditional covariances were used for testing co-volatility spillovers. Based on these results, dynamic hedging strategies could be suggested to analyze market fluctuations in crude oil prices and associated financial markets.

The empirical findings revealed that, for markets in UK and USA, there were significant negative co-volatility spillover effects for any pairs of crude oil and financial indices During-GFC and Post-GFC, whereas for Pre-GFC and for the whole sample period, most of the pairs had different signs of co-volatility effects. These empirical results suggested opportunities for optimal dynamic hedging.

However, for China, there were significant negative co-volatility effects for numerous pairs of crude oil indices and financial indices During-GFC, but positive and negative signs of co-volatility spillovers in the Post-GFC period. The empirical results for China also suggested numerous opportunities for optimal dynamic hedging across the oil and financial markets, as well as with UK and USA.

References

- Aloui, C. and R. Jammazi (2009), The effects of crude oil shocks on stock market shifts behavior: A regime switching approach, *Energy Economics*, 31(5), 789-799.
- Amemiya, T. (1985), *Advanced Econometrics*, Harvard University Press, Cambridge, MA, USA.
- Arouri, M.E.H., J. Jouini and D.K. Nguyen (2012), On the impacts of oil price fluctuations on European equity markets: Volatility spillover and hedging effectiveness, *Energy Economics*, 34(2), 611-617.
- Baba, Y., R.F. Engle, D. Kraft and K.F. Kroner (1985), Multivariate simultaneous generalized ARCH, Unpublished manuscript, Department of Economics, University of California, San Diego, CA.
- Baillie, R. and R. Myers (1991), Bivariate GARCH estimation of the optimal commodity futures hedge, *Journal of Applied Econometrics*, 6, 109–124.
- Bjørnland, H.C. (2009), Oil price shocks and stock market booms in an oil exporting country, *Scottish Journal of Political Economy*, 56(2), 232-254.
- Bollerslev, T. (1990), Modelling the coherence in short-run nominal exchange rate: A multivariate generalized ARCH approach, *Review of Economics and Statistics*, 72, 498-505.
- Bollerslev, T., R. Engle and J. Wooldridge (1988), A capital asset pricing model with time varying covariance, *Journal of Political Economy*, 96, 116-131.
- Caporin, M. and M. McAleer (2013), Ten things you should know about the dynamic conditional correlation representation, *Econometrics*, 1(1), 115-126.
- Chang, C.-L., Y.-Y. Li and M. McAleer (2015), Volatility spillovers between energy and agricultural markets: A critical appraisal of theory and practice, Discussion Paper 15-077/III, Tinbergen Institute, The Netherlands.
- Chang, C.-L., M. McAleer and R. Tansuchat (2009), Modelling conditional correlations for risk diversification in crude oil markets, *Journal of Energy Markets*, 2(4), 29-51.
- Chang, C.-L., M. McAleer and R. Tansuchat (2010), Analyzing and forecasting volatility spillovers, asymmetries and hedging in major oil markets, *Energy Economics*, 32(6), 1445-1455.
- Chang, C.-L., M. McAleer and R. Tansuchat (2011), Crude oil hedging strategies using dynamic multivariate GARCH, *Energy Economics*, 33(5), 912-923.

Chang, C.-L., M. McAleer and R. Tansuchat (2013), Conditional correlations and volatility spillovers between crude oil and stock index returns, *North American Journal of Economics and Finance*, 25, 116-138.

Chang, C.-L., M. McAleer and Y.-A. Wang (2016), Modelling volatility spillovers for bio-ethanol, sugarcane and corn, *Tinbergen Institute Discussion Papers 16-014/III*, The Netherlands.

Cong, R.-G., Y.-M. Wei, J.-L. Jiao and Y. Fan (2008), Relationships between oil price shocks and stock market: An empirical analysis from China, *Energy Policy*, 36(9), 3544-3553.

Engle, R. (2002), Dynamic conditional correlation: A simple class of multivariate generalized autoregressive conditional heteroskedasticity models, *Journal of Business and Economic Statistics*, 20, 339-350.

Engle, R.F. and K.F. Kroner (1995), Multivariate simultaneous generalized ARCH, *Econometric Theory*, 11(1), 122-150.

Faff, R.W., and T.J. Brailsford (1999), Oil price risk and the Australian stock market, *Journal of Energy Finance & Development*, 4(1), 69-87.

Hafner, C. and M. McAleer (2014), A one line derivation of DCC: Application of a vector random coefficient moving average process, *Tinbergen Institute Discussion Paper 14-087*, The Netherlands.

Jammazi, R. and C. Aloui (2010), Wavelet decomposition and regime shifts: Assessing the effects of crude oil shocks on stock market returns, *Energy Policy*, 38(3), 1415-1435.

Johnson, L.L. (1960), The theory of hedging and speculation in commodity futures, *Review of Economic Studies*, 27, 139-151.

Kilian, L. and C. Park (2009), The impact of oil price shocks on the US stock market, *International Economic Review*, 50(4), 1267-1287.

Ling, S. and M. McAleer (2003), Asymptotic theory for a vector ARMA-GARCH model, *Econometric Theory*, 19, 278-308.

Manera, M., M. McAleer and M. Grasso (2006), Modelling time-varying conditional correlations in the volatility of Tapis oil spot and forward returns, *Applied Financial Economics*, 16(7), 525-533.

McAleer, M. (2005), Automated inference and learning in modeling financial volatility, *Econometric Theory*, 21(1), 232-261.

McAleer, M., F. Chan, S. Hoti and O. Lieberman (2008), Generalized autoregressive conditional correlation, *Econometric Theory*, 24(6), 1554-1583.

McAleer, M. and C. Hafner (2014), A one line derivation of EGARCH, *Econometrics*, 2, 92-97.

McAleer, M., S. Hoti and F. Chan (2009), Structure and asymptotic theory for multivariate asymmetric conditional volatility, *Econometric Reviews*, 28, 422-440.

Miller, J. Isaac and R.A. Ratti (2009), Crude oil and stock markets: Stability, instability, and bubbles, *Energy Economics*, 31(4), 559-568.

Sadorsky, P. (1999), Oil price shocks and stock market activity, *Energy Economics*, 21(5), 449-469.

Tse, Y.K. and A.K.C. Tsui (2002), A multivariate GARCH model with time-varying correlations, *Journal of Business and Economic Statistics*, 20, 351-362.

Table 1
Descriptive Statistics for UK and USA

Returns	Mean	SD	Max	Min	Skewness	Kurtosis	Jarque-Bera
Whole Sample: 1988-2016							
WTI-s	0.015	2.450	21.277	-40.826	-0.698	18.586	74240.627
WTI-f	0.014	2.392	16.410	-40.048	-0.756	18.278	71460.620
BRENT-f	0.015	2.212	13.151	-42.722	-1.096	25.787	158879.705
SP500-s	0.028	1.100	10.957	-9.470	-0.263	12.131	25358.268
SP500-f	0.027	1.130	13.197	-10.400	-0.196	13.935	36296.838
FTSE-s	0.016	1.087	9.384	-9.266	-0.140	9.252	11874.199
FTSE-f	0.016	1.139	9.580	-9.699	-0.147	8.414	8911.304
Pre-GFC: 1998-2007							
WTI-s	0.026	2.431	14.886	-40.826	-1.240	23.935	89533.234
WTI-f	0.025	2.354	13.572	-40.048	-1.294	24.574	95114.659
BRENT-f	0.026	2.214	13.151	-42.722	-1.650	35.390	213547.316
SP500-s	0.034	0.965	5.573	-7.113	-0.154	7.422	3957.782
SP500-f	0.034	1.009	5.755	-8.730	-0.300	8.414	5976.879
FTSE-s	0.025	0.982	5.904	-5.885	-0.133	6.368	2299.857
FTSE-f	0.025	1.070	6.373	-6.557	-0.094	6.090	1930.618
During GFC: 2007-2009							
WTI-s	-0.043	3.333	21.277	-13.065	0.472	8.331	690.083
WTI-f	-0.043	3.307	16.410	-13.065	0.223	6.918	366.075
BRENT-f	-0.041	2.836	12.707	-10.946	-0.195	5.712	176.732
SP500-s	-0.129	1.978	10.957	-9.470	-0.210	9.272	930.089
SP500-f	-0.130	1.998	13.197	-10.400	0.123	11.687	1777.879
FTSE-s	-0.102	1.835	9.384	-9.266	-0.018	8.439	696.510
FTSE-f	-0.103	1.825	9.580	-9.699	-0.109	8.423	693.530
Post-GFC: 2009-2016							
WTI-s	0.004	2.169	11.621	-10.794	0.108	6.158	783.537
WTI-f	0.004	2.151	11.621	-10.794	0.116	6.139	774.799
BRENT-f	0.006	1.982	10.416	-8.963	0.207	6.099	764.396
SP500-s	0.059	1.054	6.837	-6.896	-0.093	7.550	1621.836
SP500-f	0.058	1.057	6.731	-7.496	-0.155	7.763	1781.712
FTSE-s	0.029	1.041	5.032	-4.779	-0.077	5.199	380.064
FTSE-f	0.029	1.037	4.854	-4.950	-0.099	5.316	422.473

Note: There are 7277, 4835, 565 and 1877 observations for four periods, respectively. The Jarque-Bera Lagrange Multiplier test is asymptotically chi-squared, and is based on testing skewness and kurtosis against the normal distribution.

Table 2
Descriptive Statistics for China

Returns	Mean	SD	Max	Min	Skewness	Kurtosis	Jarque-Bera
During & Post-GFC: 2007-2016							
SH-s	0.002	1.787	9.034	-9.256	-0.612	6.894	1695.525
SZ-s	0.049	2.001	8.515	-8.930	-0.743	5.535	878.809
CNA50-s	0.000	1.912	9.198	-9.861	-0.196	6.381	1209.280
CNA50-f	-0.001	2.063	16.106	-15.979	-0.196	9.997	5023.172
During GFC: 2007-2009							
SH-s	-0.036	2.485	9.034	-9.256	-0.256	4.331	47.890
SZ-s	0.046	2.645	8.515	-8.930	-0.546	3.987	51.064
CNA50-s	-0.029	2.667	9.198	-9.861	-0.206	4.084	31.672
CNA50-f	-0.031	2.779	10.110	-10.359	-0.107	4.392	46.731
Post-GFC: 2009-2016							
SH-s	0.013	1.516	5.604	-8.873	-0.927	7.927	2167.348
SZ-s	0.049	1.762	6.320	-8.601	-0.859	5.890	883.716
CNA50-s	0.009	1.618	6.827	-9.744	-0.418	7.125	1385.175
CNA50-f	0.009	1.793	16.106	-15.979	-0.493	15.185	11687.501

Note: There are 2442, 565 and 1877 observations for the three periods, respectively. The Jarque-Bera Lagrange Multiplier test is asymptotically chi-squared, and is based on testing skewness and kurtosis against the normal distribution.

Table 3

Correlations of Crude Oil and Financial Markets for UK and USA

Whole Sample	WTI-s	WTI-f	BRENT-f	SP500-s	SP500-f	FTSE-s	FTSE-f
WTI-s	1.000						
WTI-f	0.901	1.000					
BRENT-f	0.795	0.804	1.000				
SP500-s	0.105	0.098	0.103	1.000			
SP500-f	0.104	0.096	0.097	0.974	1.000		
FTSE-s	0.146	0.147	0.139	0.491	0.487	1.000	
FTSE-f	0.140	0.140	0.131	0.475	0.473	0.963	1.000
Pre-GFC	WTI-s	WTI-f	BRENT-f	SP500-s	SP500-f	FTSE-s	FTSE-f
WTI-s	1.000						
WTI-f	0.874	1.000					
BRENT-f	0.759	0.775	1.000				
SP500-s	-0.065	-0.079	-0.073	1.000			
SP500-f	-0.060	-0.077	-0.076	0.965	1.000		
FTSE-s	-0.018	-0.017	-0.037	0.401	0.383	1.000	
FTSE-f	-0.014	-0.017	-0.035	0.385	0.372	0.952	1.000
GFC	WTI-s	WTI-f	BRENT-f	SP500-s	SP500-f	FTSE-s	FTSE-f
WTI-s	1.000						
WTI-f	0.914	1.000					
BRENT-f	0.861	0.845	1.000				
SP500-s	0.252	0.249	0.282	1.000			
SP500-f	0.265	0.264	0.284	0.982	1.000		
FTSE-s	0.386	0.370	0.430	0.537	0.570	1.000	
FTSE-f	0.393	0.386	0.434	0.536	0.570	0.989	1.000
Post-GFC	WTI-s	WTI-f	BRENT-f	SP500-s	SP500-f	FTSE-s	FTSE-f
WTI-s	1.000						
WTI-f	0.977	1.000					
BRENT-f	0.872	0.872	1.000				
SP500-s	0.430	0.430	0.429	1.000			
SP500-f	0.422	0.420	0.423	0.984	1.000		
FTSE-s	0.402	0.404	0.400	0.643	0.642	1.000	
FTSE-f	0.396	0.397	0.397	0.639	0.634	0.972	1.000

Table 4

Correlations of Crude Oil in UK and USA, and Financial Markets in China

During & Post-GFC	WTI-s	WTI-f	BRENT-f	SH-s	SZ-s	CNA50-s	CNA50-f
WTI-s	1.000						
WTI-f	0.951	1.000					
BRENT-f	0.867	0.861	1.000				
SH-s	0.084	0.094	0.117	1.000			
SZ-s	0.066	0.080	0.098	0.902	1.000		
CNA50-s	0.086	0.093	0.114	0.948	0.783	1.000	
CNA50-f	0.089	0.093	0.114	0.894	0.746	0.930	1.000
GFC	WTI-s	WTI-f	BRENT-f	SH-s	SZ-s	CNA50-s	CNA50-f
WTI-s	1.000						
WTI-f	0.914	1.000					
BRENT-f	0.861	0.845	1.000				
SH-s	0.092	0.097	0.096	1.000			
SZ-s	0.047	0.064	0.058	0.927	1.000		
CNA50-s	0.096	0.099	0.098	0.975	0.892	1.000	
CNA50-f	0.100	0.100	0.098	0.927	0.855	0.947	1.000
Post-GFC	WTI-s	WTI-f	BRENT-f	SH-s	SZ-s	CNA50-s	CNA50-f
WTI-s	1.000						
WTI-f	0.977	1.000					
BRENT-f	0.872	0.872	1.000				
SH-s	0.078	0.091	0.132	1.000			
SZ-s	0.079	0.092	0.124	0.884	1.000		
CNA50-s	0.079	0.089	0.126	0.925	0.704	1.000	
CNA50-f	0.081	0.088	0.124	0.870	0.671	0.918	1.000

Table 5

Matrix *A* in Diagonal BEKK, Mean Return Shocks, and Mean Co-volatility Spillovers for UK and US Spot Markets, Four Periods (2 x 2)

Periods	Variables	<i>A</i>	Mean Return Shocks	Mean Co-volatility Spillovers	Variables	<i>A</i>	Mean Return Shocks	Mean Co-volatility Spillovers
Whole Sample	WTI-s	0.236*	0.006	-0.0012	WTI-s	0.239*	-0.003	-0.0011
	SP500-s	0.248*	-0.021	0.0004	FTSE-s	0.264*	-0.017	-0.0002
Pre-GFC	WTI-s	<i>0.263*</i>	0.026	-0.0005	WTI-s	0.242*	0.020	-0.0008
	SP500-s	<i>0.170*</i>	-0.010	0.0012	FTSE-s	0.246*	-0.013	0.0012
GFC	WTI-s	<i>0.211*</i>	-0.207	-0.0093	WTI-s	<i>0.205*</i>	-0.231	-0.0078
	SP500-s	<i>0.276*</i>	-0.159	-0.0121	FTSE-s	<i>0.362*</i>	-0.105	-0.0171
Post-GFC	WTI-s	<i>0.235*</i>	-0.028	-0.0010	WTI-s	0.232*	-0.009	-0.0002
	SP500-s	<i>0.325*</i>	-0.014	-0.0021	FTSE-s	0.266*	-0.003	-0.0005

Notes: 1. * significant 1%.

2. Scalar weight matrices *A* are in bold, while diagonal weights are in italics.

3. Mean Co-volatility Spillover = $\partial H_{ij} / \partial \varepsilon_{kt-1}$, $i \neq j$, $k = \text{either } i \text{ or } j$.

4. Pairs with different signs of Mean Co-volatility Spillovers are in color.

Table 6
Matrix A in Diagonal BEKK, Mean Return Shocks, and Mean Co-volatility Spillovers for UK and US Futures Markets,
Four Periods (2 x 2)

Periods	Variables	A	Mean Return Shocks	Mean Co-volatility Spillovers	Variables	A	Mean Return Shocks	Mean Co-volatility Spillovers
Whole Sample	WTI-f	0.224*	-0.002	-0.0014	WTI-f	0.228*	-0.010	-0.0010
	SP500-f	0.265*	-0.023	-0.0001	FTSE-f	0.258*	-0.018	-0.0006
	BRENT-f	0.232*	0.001	-0.0016	BRENT-f	0.238*	-0.004	-0.0011
	SP500-f	0.270*	-0.025	0.0001	FTSE-f	0.253*	-0.019	-0.0002
Pre-GFC	WTI-f	0.231*	0.012	-0.0005	WTI-f	0.225*	0.007	-0.0008
	SP500-f	0.194*	-0.010	0.0005	FTSE-f	0.243*	-0.015	0.0004
	BRENT-f	0.253*	0.007	-0.0006	BRENT-f	0.251*	0.008	-0.0010
	SP500-f	0.199*	-0.012	0.0004	FTSE-f	0.235*	-0.016	0.0004
GFC	WTI-f	0.204*	-0.203	-0.0094	WTI-f	0.217*	-0.224	-0.0076
	SP500-f	0.296*	-0.155	-0.0122	FTSE-f	0.357*	-0.098	-0.0173
	BRENT-f	0.194*	-0.173	-0.0094	BRENT-f	0.209*	-0.195	-0.0077
	SP500-f	0.295*	-0.164	-0.0099	FTSE-f	0.360*	-0.103	-0.0147
Post-GFC	WTI-f	0.233*	-0.029	-0.0014	WTI-f	0.228*	-0.008	0.0000
	SP500-f	0.355*	-0.017	-0.0024	FTSE-f	0.261*	0.001	-0.0005
	BRENT-f	0.225*	-0.009	-0.0010	BRENT-f	0.220*	0.005	0.0001
	SP500-f	0.333*	-0.013	-0.0007	FTSE-f	0.250*	0.002	0.0003

- Notes:** 1. * significant 1%.
2. Scalar weight matrices *A* are in bold, while diagonal weights are in italics.
3. Mean Co-volatility Spillover = $\partial H_{ij} / \partial \epsilon_{kt-1}$, $i \neq j$, $k = \text{either } i \text{ or } j$.
4. Pairs with different signs of Mean Co-volatility Spillovers are in color.

Table 7
Matrix A in Diagonal BEKK, Mean Return Shocks, and Mean Co-volatility Spillovers for UK and US Spot Markets,
Four Periods (3 x 3)

Periods	Variables	A	Mean Return Shocks	Pairs	Mean Co-volatility Spillovers
Whole Sample	WTI-s	0.219*	0.004	WTI-s	-0.0010
	SP500-s	0.228*	-0.021	SP500-s	0.0002
	FTSE-s	0.237*	-0.013	WTI-s	-0.0007
				FTSE-s	0.0002
Pre-GFC	WTI-s	<i>0.232*</i>	0.022	WTI-s	-0.0004
	SP500-s	<i>0.166*</i>	-0.009	SP500-s	0.0008
	FTSE-s	<i>0.231*</i>	-0.012	WTI-s	-0.0006
				FTSE-s	0.0050
GFC	WTI-s	<i>0.199*</i>	-0.194	WTI-s	-0.0082
	SP500-s	<i>0.260*</i>	-0.158	SP500-s	-0.0100
	FTSE-s	<i>0.267*</i>	-0.054	WTI-s	-0.0028
				FTSE-s	-0.0103
Post-GFC	WTI-s	<i>0.217*</i>	-0.019	WTI-s	-0.0007
	SP500-s	<i>0.281*</i>	-0.011	SP500-s	-0.0011
	FTSE-s	<i>0.246*</i>	-0.005	WTI-s	-0.0003
				FTSE-s	-0.0010

Note: 1. * significant 1%.

2. Scalar weight matrices *A* are in bold, while diagonal weights are in italics.

3. Mean Co-volatility Spillover = $\partial H_{ijl} / \partial \epsilon_{kt-1}$, $i \neq j$, $k = \text{either } i \text{ or } j$.

4. Pairs with different signs of Mean Co-volatility Spillovers are in color.

Table 8
Matrix A in Diagonal BEKK, Mean Return Shocks, and Mean Co-volatility Spillovers for UK and US Futures Markets,
Four Periods (4 x 4)

Periods	Variables	<i>A</i>	Mean Return Shocks	Pairs	Mean Co-volatility Spillovers	Pairs	Mean Co-volatility Spillovers
Whole Sample	WTI-f	0.240*	0.004	WTI-f	-0.0012	BRENT-f	-0.0011
	BRENT-f	0.217*	0.001	SP500-f	0.0002	SP500-f	0.0001
	SP500-f	0.228*	-0.022	WTI-f	-0.0007	BRENT-f	-0.0007
	FTSE-f	0.213*	-0.014	FTSE-f	0.0002	FTSE-f	0.0001
Pre-GFC	WTI-f	<i>0.290*</i>	0.011	WTI-f	-0.0004	BRENT-f	-0.0003
	BRENT-f	<i>0.228*</i>	0.007	SP500-f	0.0005	SP500-f	0.0003
	SP500-f	<i>0.165*</i>	-0.009	WTI-f	-0.0008	BRENT-f	-0.0006
	FTSE-f	<i>0.198*</i>	-0.014	FTSE-f	0.0006	FTSE-f	0.0003
GFC	WTI-f	<i>0.319*</i>	-0.233	WTI-f	-0.0123	BRENT-f	-0.0092
	BRENT-f	<i>0.238*</i>	-0.228	SP500-f	-0.0179	SP500-f	-0.0130
	SP500-f	<i>0.240*</i>	-0.160	WTI-f	-0.0046	BRENT-f	-0.0034
	FTSE-f	<i>0.229*</i>	-0.063	FTSE-f	-0.0171	FTSE-f	-0.0124
Post-GFC	WTI-f	<i>0.217*</i>	-0.012	WTI-f	-0.0007	BRENT-f	-0.0008
	BRENT-f	<i>0.222*</i>	-0.002	SP500-f	-0.0008	SP500-f	-0.0001
	SP500-f	<i>0.291*</i>	-0.012	WTI-f	-0.0001	BRENT-f	-0.0001
	FTSE-f	<i>0.225*</i>	-0.002	FTSE-f	-0.0006	FTSE-f	-0.0001

- Notes:** 1. * significant 1%.
2. Scalar weight matrices *A* are in bold, while diagonal weights are in italics.
3. Mean Co-volatility Spillover = $\partial H_{ij} / \partial \varepsilon_{kt-1}$, $i \neq j$, $k = \text{either } i \text{ or } j$.
4. Pairs with different signs of Mean Co-volatility Spillovers are in color.

Table 9
Matrix A in Diagonal BEKK and Mean Return Shocks for UK and US Spot and Futures Markets,
Four Periods (7 x 7)

Periods	Variables	A	Mean Return Shocks	Periods	Variables	A	Mean Return Shocks
Whole Sample	WTI-s	<i>0.266*</i>	0.016	GFC	WTI-s	<i>0.253*</i>	-0.307
	WTI-f	<i>0.220*</i>	0.007		WTI-f	<i>0.315*</i>	-0.297
	BRENT-f	<i>0.248*</i>	0.009		BRENT-f	<i>0.284*</i>	-0.270
	SP500-s	<i>0.155*</i>	-0.013		SP500-s	<i>0.209*</i>	-0.185
	SP500-f	<i>0.157*</i>	-0.015		SP500-f	<i>0.217*</i>	-0.182
	FTSE-s	<i>0.138*</i>	-0.007		FTSE-s	<i>0.075*</i>	-0.111
	FTSE-f	<i>0.139*</i>	-0.008		FTSE-f	<i>0.071*</i>	-0.109
Pre-GFC	WTI-s	<i>0.319*</i>	0.012	Post-GFC	WTI-s	<i>0.218*</i>	-0.014
	WTI-f	<i>0.350*</i>	0.038		WTI-f	<i>0.229*</i>	-0.017
	BRENT-f	<i>0.253*</i>	0.016		BRENT-f	<i>0.209*</i>	-0.009
	SP500-s	<i>0.104*</i>	-0.007		SP500-s	<i>0.159*</i>	-0.021
	SP500-f	<i>0.103*</i>	-0.008		SP500-f	<i>0.182*</i>	-0.017
	FTSE-s	<i>0.125*</i>	-0.010		FTSE-s	<i>0.403*</i>	-0.016
	FTSE-f	<i>0.130*</i>	-0.013		FTSE-f	<i>0.379*</i>	-0.021

Notes: 1. * significant 1%.

2. Scalar weight matrices *A* are in bold, while diagonal weights are in italics.

Table 10
Mean Co-volatility Spillovers for UK and US Spot and Futures Markets,
Four Periods (7 x 7)

Periods	Pairs	Mean Co-volatility Spillovers	Pairs	Mean Co-volatility Spillovers	Pairs	Mean Co-volatility Spillovers
Whole Sample	WTI-s	-0.0006	WTI-f	-0.0005	BRENT-f	-0.0005
	SP500-s	0.0006	SP500-s	0.0003	SP500-s	0.0003
	WTI-s	-0.0006	WTI-f	-0.0005	BRENT-f	-0.0006
	SP500-f	0.0007	SP500-f	0.0003	SP500-f	0.0003
	WTI-s	-0.0003	WTI-f	-0.0002	BRENT-f	-0.0002
	FTSE-s	0.0006	FTSE-s	0.0002	FTSE-s	0.0003
Pre-GFC	WTI-s	-0.0003	WTI-f	-0.0003	BRENT-f	-0.0003
	FTSE-f	0.0006	FTSE-f	0.0002	FTSE-f	0.0003
	WTI-s	-0.0002	WTI-f	-0.0002	BRENT-f	-0.0002
	SP500-s	0.0004	SP500-s	0.0014	SP500-s	0.0004
	WTI-s	-0.0003	WTI-f	-0.0003	BRENT-f	-0.0002
GFC	SP500-f	0.0004	SP500-f	0.0014	SP500-f	0.0004
	WTI-s	-0.0004	WTI-f	-0.0004	BRENT-f	-0.0003
	FTSE-s	0.0005	FTSE-s	0.0016	FTSE-s	0.0005
	WTI-s	-0.0005	WTI-f	-0.0006	BRENT-f	-0.0004
	FTSE-f	0.0005	FTSE-f	0.0017	FTSE-f	0.0005
Post-GFC	WTI-s	-0.0098	WTI-f	-0.0122	BRENT-f	-0.0110
	SP500-s	-0.0163	SP500-s	-0.0195	SP500-s	-0.0161
	WTI-s	-0.0100	WTI-f	-0.0124	BRENT-f	-0.0112
	SP500-f	-0.0168	SP500-f	-0.0202	SP500-f	-0.0166
	WTI-s	-0.0021	WTI-f	-0.0026	BRENT-f	-0.0024
	FTSE-s	-0.0058	FTSE-s	-0.0070	FTSE-s	-0.0057
Post-GFC	WTI-s	-0.0020	WTI-f	-0.0024	BRENT-f	-0.0022
	FTSE-f	-0.0055	FTSE-f	-0.0067	FTSE-f	-0.0055
	WTI-s	-0.0007	WTI-f	-0.0008	BRENT-f	-0.0007
	SP500-s	-0.0005	SP500-s	-0.0006	SP500-s	-0.0003
	WTI-s	-0.0007	WTI-f	-0.0007	BRENT-f	-0.0006
Post-GFC	SP500-f	-0.0005	SP500-f	-0.0007	SP500-f	-0.0003
	WTI-s	-0.0014	WTI-f	-0.0015	BRENT-f	-0.0014
	FTSE-s	-0.0012	FTSE-s	-0.0015	FTSE-s	-0.0008
	WTI-s	-0.0017	WTI-f	-0.0018	BRENT-f	-0.0017
FTSE-f	-0.0011	FTSE-f	-0.0014	FTSE-f	-0.0007	

Notes: 1. Mean Co-volatility Spillover = $\partial H_{iji} / \partial \varepsilon_{k-1}$, $i \neq j$, $k = \text{either } i \text{ or } j$.
2. Pairs with different signs of Mean Co-volatility Spillovers are in color.

Table 11
Matrix A in Diagonal BEKK, Mean Return Shocks, and Mean Co-volatility Spillovers
for UK and US Crude Oil Markets, and Chinese Financial Markets,
Three Periods (2 x 2)

Periods	Variables	A	Mean Return Shocks	Mean Co-volatility Spillovers	Variables	A	Mean Return Shocks	Mean Co-volatility Spillovers
During & Post-GFC	WTI-s	<i>0.248*</i>	-0.063	-0.0001	WTI-f	0.238*	-0.056	-0.0001
	SH-s	<i>0.193*</i>	-0.002	-0.0030	CNA50-f	0.221*	-0.001	-0.0029
	WTI-s	<i>0.249*</i>	-0.057	0.0001	BRENT-f	0.221*	-0.038	0.0001
	SZ-s	<i>0.197*</i>	0.002	-0.0028	CNA50-f	0.223*	0.003	-0.0019
	WTI-s	<i>0.246*</i>	-0.061	0.0001				
	CNA50-s	<i>0.202*</i>	0.001	-0.0031				
GFC	WTI-s	<i>0.275*</i>	-0.271	-0.0039	WTI-f	<i>0.270*</i>	-0.277	-0.0050
	SH-s	<i>0.192*</i>	-0.073	-0.0143	CNA50-f	<i>0.184*</i>	-0.100	-0.0138
	WTI-s	0.256*	-0.274	-0.0066	BRENT-f	0.230*	-0.205	-0.0002
	SZ-s	0.281*	-0.093	-0.0197	CNA50-f	0.228*	-0.004	-0.0108
	WTI-s	<i>0.266*</i>	-0.277	-0.0032				
	CNA50-s	<i>0.165*</i>	-0.072	-0.0122				
Post-GFC	WTI-s	0.228*	-0.024	0.0005	WTI-f	0.222*	-0.016	0.0008
	SH-s	0.214*	0.011	-0.0012	CNA50-f	0.228*	0.016	-0.0008
	WTI-s	0.229*	-0.016	0.0004	BRENT-f	0.217*	-0.001	0.0010
	SZ-s	0.211*	0.008	-0.0008	CNA50-f	0.229*	0.021	0.0000
	WTI-s	0.228*	-0.021	0.0007				
	CNA50-s	0.219*	0.013	-0.0011				

Notes: 1. * significant 1%.

2. Scalar weight matrices *A* are in bold, while diagonal weights are in italics.

3. Mean Co-volatility Spillover = $\partial H_{ij} / \partial \varepsilon_{kt-1}$, $i \neq j$, $k = \text{either } i \text{ or } j$.

4. Pairs with different signs of Mean Co-volatility Spillovers are in color.

Table 12
Matrix A in Diagonal BEKK, Mean Return Shocks, and Mean Co-volatility Spillovers
for UK and US Crude Oil Markets, and Chinese Financial Markets,
Three Periods (5 x 5)

Periods	Variables	A	Mean Return Shocks	Pairs	Mean Co-volatility Spillovers	Pairs	Mean Co-volatility Spillovers	Pairs	Mean Co-volatility Spillovers
During & Post-GFC	WTI-s	<i>0.236*</i>	-0.042	WTI-s	0.0000	WTI-f	0.0000	BRENT-f	0.0000
	WTI-f	<i>0.281*</i>	-0.034	CNA50-s	-0.0015	CNA50-s	-0.0015	CNA50-s	-0.0012
	BRENT-f	<i>0.265*</i>	-0.028	WTI-s	0.0001	WTI-f	0.0002	BRENT-f	0.0002
	CNA50-s	<i>0.157*</i>	0.000	CNA50-f	-0.0018	CNA50-f	-0.0018	CNA50-f	-0.0014
	CNA50-f	<i>0.187*</i>	0.003						
GFC	WTI-s	<i>0.262*</i>	-0.334	WTI-s	-0.0060	WTI-f	-0.0070	BRENT-f	-0.0063
	WTI-f	<i>0.308*</i>	-0.341	CNA50-s	-0.0208	CNA50-s	-0.0249	CNA50-s	-0.0206
	BRENT-f	<i>0.276*</i>	-0.314	WTI-s	-0.0060	WTI-f	-0.0070	BRENT-f	-0.0063
	CNA50-s	<i>0.237*</i>	-0.096	CNA50-f	-0.0215	CNA50-f	-0.0256	CNA50-f	-0.0212
	CNA50-f	<i>0.245*</i>	-0.093						
Post-GFC	WTI-s	<i>0.225*</i>	-0.021	WTI-s	0.0001	WTI-f	0.0001	BRENT-f	0.0001
	WTI-f	<i>0.214*</i>	-0.024	CNA50-s	-0.0006	CNA50-s	-0.0007	CNA50-s	-0.0003
	BRENT-f	<i>0.217*</i>	-0.011	WTI-s	0.0002	WTI-f	0.0002	BRENT-f	0.0002
	CNA50-s	<i>0.140*</i>	0.002	CNA50-f	-0.0009	CNA50-f	-0.0010	CNA50-f	-0.0005
	CNA50-f	<i>0.190*</i>	0.005						

- Notes:** 1. * significant 1%.
2. Scalar weight matrices *A* are in bold, while diagonal weights are in italics.
3. Mean Co-volatility Spillover = $\partial H_{ij} / \partial \varepsilon_{kt-1}$, $i \neq j$, $k = \text{either } i \text{ or } j$.
4. Pairs with different signs of Mean Co-volatility Spillovers are in color.

Figure 1

Spot and Futures Price of WTI, and Futures Price of BRENT, 1988-2016

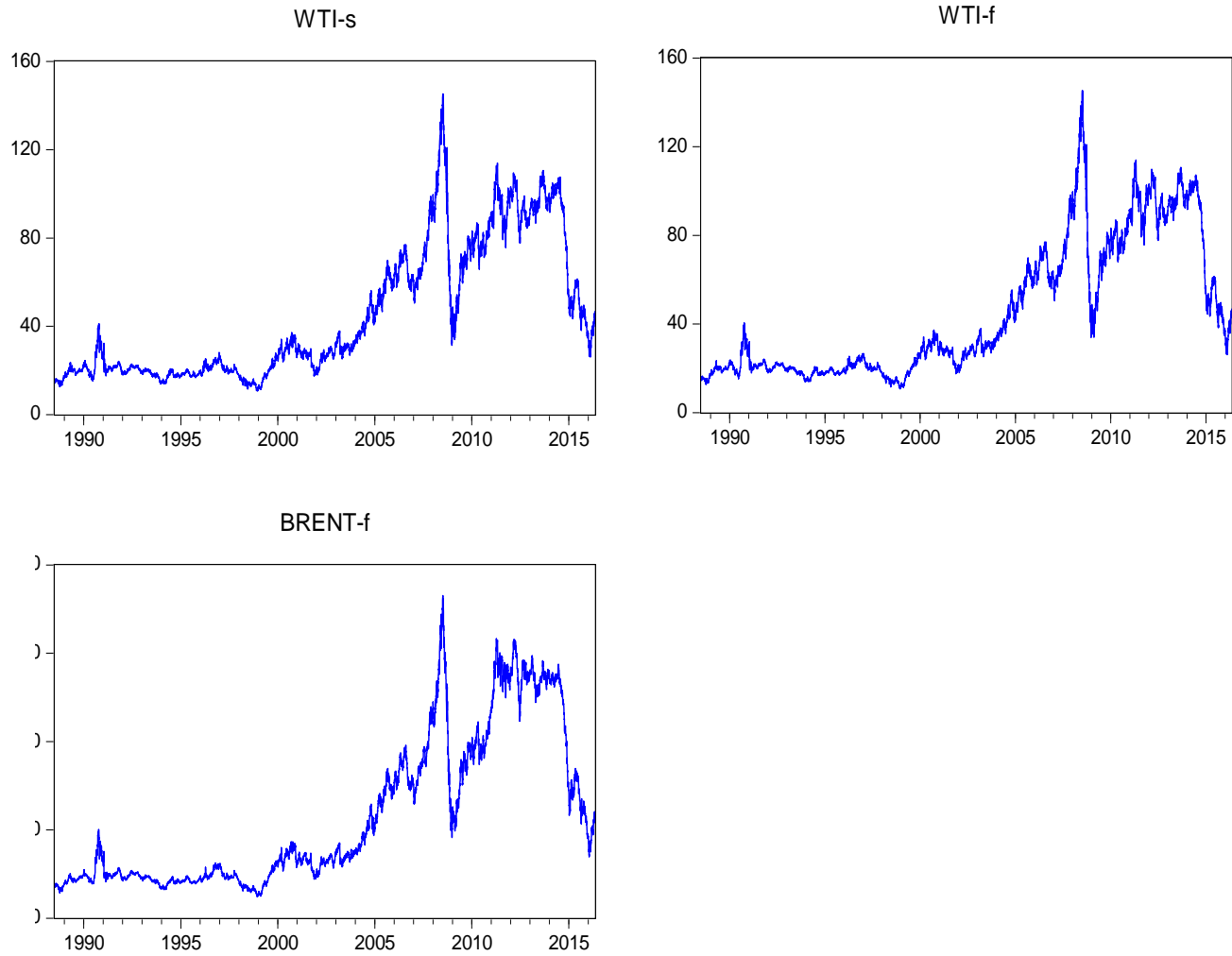


Figure 2

Spot and Futures Price of S&P 500, Spot and Futures Price of FTSE 100, 1988-2016

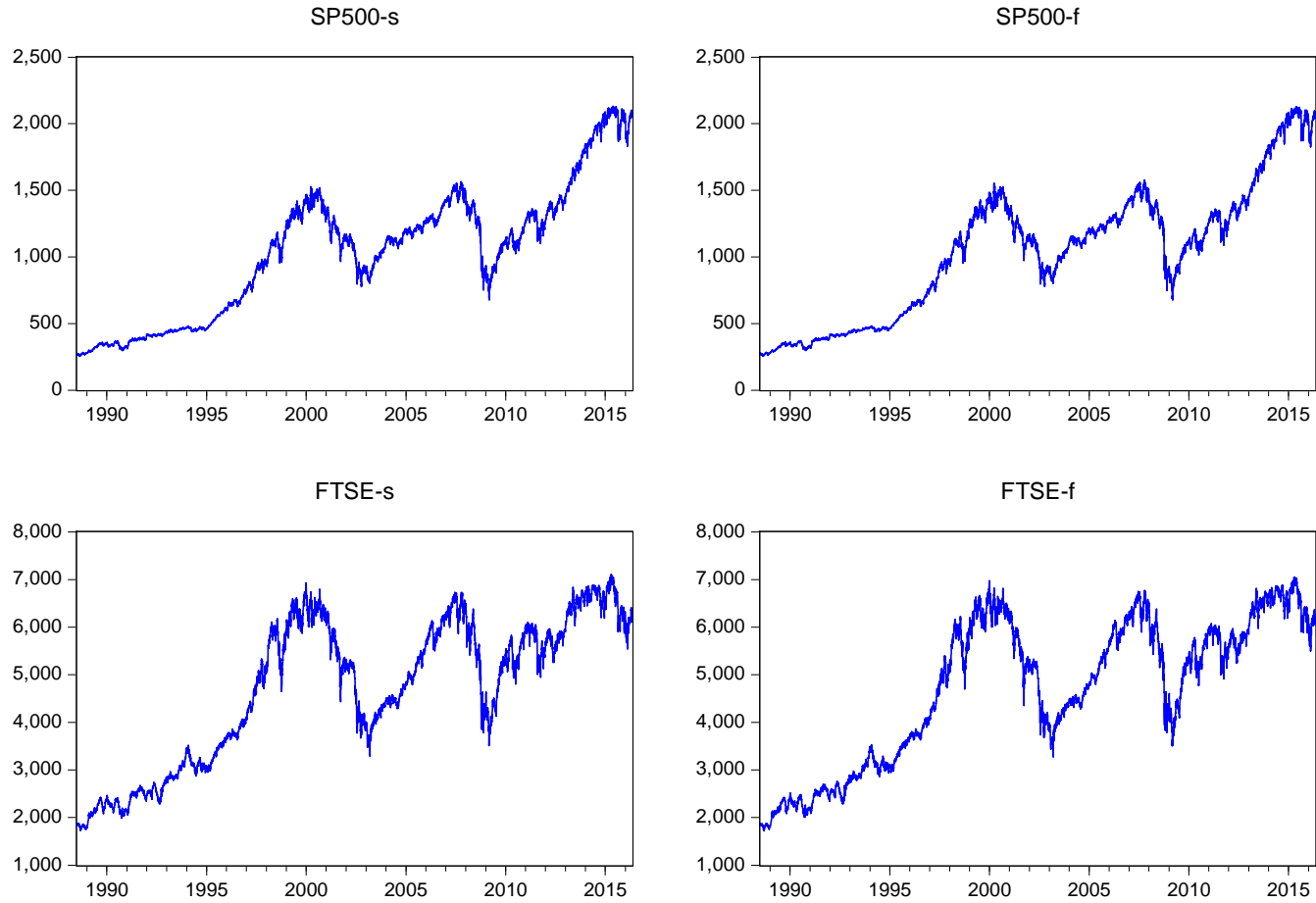


Figure 3

Spot Prices of SSE Composite, SZSE Composite, China A50, Futures Price of China A50, 2007-2016

