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Forschungsinstitut zur Zukunft der Arbeit Institute for the Study of Labor

# **Optimal Data Collection for Randomized Control Trials**

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# ABSTRACT

# **Optimal Data Collection for Randomized Control Trials**<sup>\*</sup>

In a randomized control trial, the precision of an average treatment effect estimator can be improved either by collecting data on additional individuals, or by collecting additional covariates that predict the outcome variable. We propose the use of pre-experimental data such as a census, or a household survey, to inform the choice of both the sample size and the covariates to be collected. Our procedure seeks to minimize the resulting average treatment effect estimator's mean squared error, subject to the researcher's budget constraint. We rely on a modification of an orthogonal greedy algorithm that is conceptually simple and easy to implement in the presence of a large number of potential covariates, and does not require any tuning parameters. In two empirical applications, we show that our procedure can lead to substantial gains of up to 58%, measured either in terms of reductions in data collection costs or in terms of improvements in the precision of the treatment effect estimator.

JEL Classification: C55, C81

Keywords: randomized control trials, big data, data collection, optimal survey design, orthogonal greedy algorithm, survey costs

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# I Introduction

This paper is motivated by the observation that empirical research in economics increasingly involves the collection of original data through laboratory or field experiments (see, e.g. Duflo, Glennerster, and Kremer, 2007; Banerjee and Duflo, 2009; Bandiera, Barankay, and Rasul, 2011; List, 2011; List and Rasul, 2011; Hamermesh, 2013, among others). This observation carries with it a call and an opportunity for research to provide econometrically sound guidelines for data collection.

We consider the decision problem faced by a researcher designing the survey for a randomized control trial (RCT). We assume that the goal of the researcher is to obtain precise estimates of the average treatment effect using the experimental data. Data collection is costly and the researcher is restricted by a budget, which limits how much data can be collected. We focus on optimally trading off the number of individuals included in the RCT and the choice of covariates elicited as part of the data collection process.

There are, of course, other factors potentially influencing the choice of covariates to be collected in a survey for an RCT. For example, one may wish to learn about the mechanisms through which the RCT is operating, check whether treatment or control groups are balanced, or measure heterogeneity in the impacts of the intervention being tested. In practice, researchers place implicit weights on each of the main objectives they consider when designing surveys, and consider informally the different trade-offs involved in their choices. We show that there is substantial value to making this decision process more rigorous and transparent through the use of data-driven tools that optimize a well-defined objective. Instead of attempting to formalize the whole research design process, we focus on one particular trade-off that we think is of firstorder importance and particularly conducive to data-driven procedures.

We assume the researcher has access to pre-experimental data from the population from which the experimental data will be drawn or at least from a population that shares similar second moments of the variables to be collected. The data set includes all the potentially relevant variables that one would consider collecting for the analysis of the experiment. The researcher faces a fixed budget for the implementation of the RCT. Given this budget, the researcher chooses the survey's sample size and set of covariates so as to optimize the resulting treatment effect estimator's precision. This choice takes place before the implementation of the RCT and could, for example, be part of a pre-analysis plan in which, among other things, the researcher specifies outcomes of interest, covariates to be selected, and econometric techniques to be used. In principle, the trade-offs involved in this choice involve basic economic reasoning. For each possible covariate, one should be comparing the marginal benefit and marginal cost of including it in the survey, which in turn, depend on all the other covariates included in the survey. As we discuss below, in simple settings it is possible to derive analytic and intuitive solutions to this problem. Although these are insightful, they only apply in unrealistic formulations of the problem. In general, for each covariate, there is a discrete choice of whether to include it or not, and for each possible sample size, one needs to consider all possible combinations of covariates within the budget. This requires a solution to a computationally difficult combinatorial optimization problem. This problem is especially challenging when the set of potential variables to choose from is large, a case that is increasingly encountered in today's big data environment. Fortunately, with the increased availability of high-dimensional data, methods for the analysis of such data sets have received growing attention in several fields, including economics (Belloni, Chernozhukov, and Hansen, 2014). This literature makes available a rich set of new tools, which can be adapted to our study of optimal survey design.

In this paper, we propose the use of a computationally attractive algorithm based on the orthogonal greedy algorithm (OGA) – also known as the orthogonal matching pursuit; see, for example, Tropp (2004) and Tropp and Gilbert (2007) among many others. To implement the OGA, it is necessary to specify the stopping rule, which in turn generally requires a tuning parameter. One attractive feature of our algorithm is that, once the budget constraint is given, there is no longer the need to choose a tuning parameter to implement the proposed method, as the budget constraint plays the role of a stopping rule. In other words, we develop an automated OGA that is tailored to our own decision problem. Furthermore, it performs well even when there are a large number of potential covariates in the pre-experimental data set.

There is a large and important body of literature on the design of experiments, starting with Fisher (1935). There also exists an extensive body of literature on sample size (power) calculations; see, for example, McConnell and Vera-Hernández (2015) for a practical guide. Both bodies of literature are concerned with the precision of treatment effect estimates, but neither addresses the problem that concerns us. For instance, McConnell and Vera-Hernández (2015) have developed methods to choose the sample size when cost constraints are binding, but they neither consider the issue of collecting covariates nor its trade-off with selecting the sample size.

Both our paper and the standard literature on power calculations rely on the availability of information in pre-experimental data. The calculations we propose can be seen as a substantive reformulation and extension of the more standard power calculations, which are an important part of the design of any RCT. When conducting power calculations, one searches for the sample size that allows the researcher to detect a particular effect size in the experiment. The role of covariates can be accounted for if one has pre-defined the covariates that will be used in the experiment, and one knows (based on some pre-experimental data) how they affect the outcome. Then, once the significance level and power parameters are determined (specifying the type I and type II errors one is willing to accept), all that matters is the impact of the sample size on the variance of the treatment effect.

Suppose that, instead of asking what is the minimum sample size that allows us to detect a given effect size, we asked instead how small an effect size we could detect with a particular sample size (this amounts to a reversal of the usual power calculation). In this simple setting with pre-defined covariates, the sample size would define a particular survey cost, and we would essentially be asking about the minimum size of the variance of the treatment effect estimator that one could obtain at this particular cost, which would lead to a question similar to the one asked in this paper. Therefore, one simple way to describe our contribution is that we adapt and extend the information in power calculations to account for the simultaneous selection of covariates and sample size, explicitly considering the costs of data collection.

To illustrate the application of our method we examine two recent experiments for which we have detailed knowledge of the process and costs of data collection. We ask two questions. First, if there is a single hypothesis one wants to test in the experiment, concerning the impact of the experimental treatment on one outcome of interest, what is the optimal combination of covariate selection and sample size given by our method, and how much of an improvement in the precision of the impact estimate can we obtain as a result? Second, what are the minimum costs of obtaining the same precision of the treatment effect as in the actual experiment, if one was to select covariates and sample size optimally (what we call the "equivalent budget")?

We find from these two examples that by adopting optimal data collection rules, not only can we achieve substantial increases in the precision of the estimates (statistical importance) for a given budget, but we can also accomplish sizeable reductions in the equivalent budget (economic importance). To illustrate the quantitative importance of the latter, we show that the optimal selection of the set of covariates and the sample size leads to a reduction of about 45 percent (up to 58 percent) of the original budget in the first (second) example we consider, while maintaining the same level of the statistical significance as in the original experiment.

To the best of our knowledge, no paper in the literature directly considers our data

collection problem. Some papers address related but very different problems (see Hahn, Hirano, and Karlan, 2011; List, Sadoff, and Wagner, 2011; Bhattacharya and Dupas, 2012; McKenzie, 2012; Dominitz and Manski, 2016). They study some issues of data measurement, budget allocation or efficient estimation; however, they do not consider the simultaneous selection of the sample size and covariates for the RCTs as in this paper. Because our problem is distinct from the problems studied in these papers, we give a detailed comparison between our paper and the aforementioned papers in Section VI.

More broadly, this paper is related to a recent emerging literature in economics that emphasizes the importance of micro-level predictions and the usefulness of machine learning for that purpose. For example, Kleinberg, Ludwig, Mullainathan, and Obermeyer (2015) argue that prediction problems are abundant in economic policy analysis, and recent advances in machine learning can be used to tackle those problems. Furthermore, our paper is related to the contemporaneous debates on pre-analysis plans which demand, for example, the selection of sample sizes and covariates before the implementation of an RCT; see, for example, Coffman and Niederle (2015) and Olken (2015) for the advantages and limitations of the pre-analysis plans.

The remainder of the paper is organized as follows. In Section II, we describe our data collection problem in detail. In Section III, we propose the use of a simple algorithm based on the OGA. In Section IV, we discuss the costs of data collection in experiments. In Section V, we present two empirical applications, in Section VI, we discuss the existing literature, and in Section VII, we give concluding remarks. Online appendices provide details that are omitted from the main text.

## II Data Collection Problem

Suppose we are planning an RCT in which we randomly assign individuals to either a treatment (D = 1) or a control group (D = 0) with corresponding potential outcomes  $Y_1$  and  $Y_0$ , respectively. After administering the treatment to the treatment group, we collect data on outcomes Y for both groups so that  $Y = DY_1 + (1 - D)Y_0$ . We also conduct a survey to collect data on a potentially very high-dimensional vector of covariates Z (e.g. from a household survey covering demographics, social background, income etc.) that predicts potential outcomes. These covariates are a subset of the universe of predictors of potential outcomes, denoted by X. Random assignment of D means that D is independent of potential outcomes and of X.

Our goal is to estimate the average treatment effect  $\beta_0 := E[Y_1 - Y_0]$  as precisely as possible, where we measure precision by the finite sample mean-squared error (MSE) of a treatment effect estimator. Instead of simply regressing Y on D, we want to make use of the available covariates Z to improve the precision of the resulting treatment effect estimator. Therefore, we consider estimating  $\beta_0$  in the regression

$$Y = \alpha_0 + \beta_0 D + \gamma'_0 Z + U, \tag{1}$$

where  $(\alpha_0, \beta_0, \gamma'_0)'$  is a vector of parameters to be estimated and U is an error term. The implementation of the RCT requires us to make two decisions that may have a significant impact on the resulting treatment effect estimator's precision:

- 1. Which covariates Z should we select from the universe of potential predictors X?
- 2. From how many individuals (n) should we collect data on (Y, D, Z)?

Obviously, a large experimental sample size n improves the precision of the treatment effect estimator. Similarly, collecting more covariates, in particular strong predictors of potential outcomes, reduces the variance of the residual U which, in turn, also improves the precision of the estimator. At the same time collecting data from more individuals and on more covariates is costly so that, given a finite budget, we want to find a combination of sample size n and covariate selection Z that leads to the most precise treatment effect estimator possible.

In this section, we propose a procedure to make this choice based on a pre-experimental data set on Y and X, such as a pilot study or a census from the same population from which we plan to draw the RCT sample.<sup>1</sup> The combined data collection and estimation procedure can be summarized as follows:

- 1. Obtain pre-experimental data  $\mathcal{S}_{\text{pre}}$  on (Y, X).
- 2. Use data in  $\mathcal{S}_{pre}$  to select the covariates Z and sample size n.
- 3. Implement the RCT and collect the experimental data  $S_{exp}$  on (Y, D, Z).
- 4. Estimate the average treatment effect using  $S_{exp}$ .
- 5. Compute standard errors.

 $<sup>^1\</sup>mathrm{In}$  fact, we do not need the populations to be identical, but only require second moments to be the same.

We now describe the five steps listed above in more detail. The main component of our procedure consists of a proposal for the optimal choice of n and Z in Step 2, which is described more formally in Section III.

- Step 1. Obtain pre-experimental data. We assume the availability of data on outcomes  $Y \in \mathbb{R}$  and covariates  $X \in \mathbb{R}^M$  for the population from which we plan to draw the experimental data. We denote the pre-experimental sample of size N by  $S_{\text{pre}} := \{Y_i, X_i\}_{i=1}^N$ . Our framework allows the number of potential covariates, M, to be very large (possibly much larger than the sample size N). Typical examples would be census data, household surveys, or data from other, similar experiments. Another possible candidate is a pilot experiment that was carried out before the larger-scale role out of the main experiment, provided that the sample size N of the pilot study is large enough for our econometric analysis in Step 2.
- Step 2. Optimal selection of covariates and sample size. We want to use the pre-experimental data to choose the sample size, and which covariates should be in our survey. Let  $S \in \{0,1\}^M$  be a vector of ones and zeros of the same dimension as X. We say that the *j*th covariate  $(X^{(j)})$  is selected if  $S_j = 1$ , and denote by  $X_S$  the subvector of X containing elements that are selected by S. For example, consider  $X = (X^{(1)}, X^{(2)}, X^{(3)})$  and S = (1, 0, 1). Then  $X_S = (X^{(1)}, X^{(3)})$ . For any vector of coefficients  $\gamma \in \mathbb{R}^M$ , let  $\mathcal{I}(\gamma) \in \{0, 1\}^M$  denote the nonzero elements of  $\gamma$ . Suppose X contains a constant term. We can then rewrite (1) as

$$Y = \beta_0 D + \gamma'_{\mathcal{I}(\gamma)} X_{\mathcal{I}(\gamma)} + U(\gamma), \qquad (2)$$

where  $\gamma \in \mathbb{R}^M$  and  $U(\gamma) := Y - \beta_0 D - \gamma'_{\mathcal{I}(\gamma)} X_{\mathcal{I}(\gamma)}$ . For a given  $\gamma$  and sample size n, we denote by  $\hat{\beta}(\gamma, n)$  the OLS estimator of  $\beta_0$  in a regression of Y on D and  $X_{\mathcal{I}(\gamma)}$  using a random sample  $\{Y_i, D_i, X_i\}_{i=1}^n$ .

Data collection is costly and therefore constrained by a budget of the form  $c(S,n) \leq B$ , where c(S,n) are the costs of collecting the variables given by selection S from n individuals, and B is the researcher's budget.

Our goal is to choose the experimental sample size n and the covariate selection S so as to minimize the finite sample MSE of  $\hat{\beta}(\gamma, n)$ , i.e., we want to choose n and  $\gamma$  to minimize

$$MSE\left(\hat{\beta}(\gamma,n) \mid D_1,\ldots,D_n\right) := E\left[\left(\hat{\beta}(\gamma,n) - \beta_0\right)^2 \mid D_1,\ldots,D_n\right].$$

subject to the budget constraint. The following lemma characterizes the MSE of the estimator under the homoskedasticity assumption that  $\operatorname{Var}(U(\gamma)|D=1) =$  $\operatorname{Var}(U(\gamma)|D=0)$  for any  $\gamma \in \mathbb{R}^M$ . This assumption is satisfied, for example, if the treatment effect is constant across individuals in the experiment.

**Lemma 1.** Assume that  $Var(U(\gamma)|D=1) = Var(U(\gamma)|D=0)$  for any  $\gamma \in \mathbb{R}^M$ . Then, letting  $\overline{D}_n := n^{-1} \sum_{i=1}^n D_i$ ,

$$MSE\left(\hat{\beta}(\gamma,n) \mid D_1,\dots,D_n\right) = \frac{Var(Y-\gamma'X \mid D=0)}{n\,\bar{D}_n(1-\bar{D}_n)}.$$
(3)

The proof of this Lemma can be found in the appendix. Note that for each  $(\gamma, n)$ , the MSE is minimized by the equal splitting between the treatment and control groups. Hence, suppose that the treatment and control groups are of exactly the same size (i.e.,  $\bar{D}_n = 0.5$ ). By Lemma 1, minimizing the MSE of the treatment effect estimator subject to the budget constraint,

$$\min_{n \in \mathbb{N}_+, \, \gamma \in \mathbb{R}^M} MSE\left(\hat{\beta}(\gamma, n) \mid D_1, \dots, D_n\right) \qquad \text{s.t.} \qquad c(\mathcal{I}(\gamma), n) \le B, \quad (4)$$

is equivalent to minimizing the residual variance in a regression of Y on X (conditional on D = 0), divided by the sample size,

$$\min_{n \in \mathbb{N}_+, \gamma \in \mathbb{R}^M} \frac{1}{n} \operatorname{Var} \left( Y - \gamma' X \mid D = 0 \right) \qquad \text{s.t.} \qquad c(\mathcal{I}(\gamma), n) \le B, \tag{5}$$

Importantly, the MSE expression depends on the data only through  $\operatorname{Var}(Y - \gamma' X | D = 0)$ , which can be estimated before the randomization takes place, i.e. using the pre-experimental sample  $S_{\text{pre}}$ . Therefore, the sample counterpart of our population optimization problem (4) is

$$\min_{n \in \mathbb{N}_+, \gamma \in \mathbb{R}^M} \frac{1}{nN} \sum_{i=1}^N (Y_i - \gamma' X_i)^2 \qquad \text{s.t.} \qquad c(\mathcal{I}(\gamma), n) \le B.$$
(6)

The problem (6), which is based on the pre-experimental sample, approximates the population problem (5) for the experiment if the second moments in the pre-experimental sample are close to the second moments in the experiment.

In Section III, we describe a computationally attractive OGA that approximates the solution to (6). The OGA has been studied extensively in the signal extraction literature and is implemented in most statistical software packages. Appendices A and D show that this algorithm possesses desirable theoretical and practical properties.

The basic idea of the algorithm (in its simplest form) is straightforward. Fix a sample size n. Start by finding the covariate that has the highest correlation with the outcome. Regress the outcome on that variable, and keep the residual. Then, among the remaining covariates, find the one that has the highest correlation with the residual. Regress the outcome onto both selected covariates, and keep the residual. Again, among the remaining covariates, find the one that has the highest correlation with the new residual, and proceed as before. We iteratively select additional covariates up to the point when the budget constraint is no longer satisfied. Finally, we repeat this search process for alternative sample sizes, and search for the combination of sample size and covariate selection that minimizes the MSE. Denote the OGA solution by  $(\hat{n}, \hat{\gamma})$  and let  $\hat{\mathcal{I}} := \mathcal{I}(\hat{\gamma})$  denote the selected covariates. See Section III for more details.

Note that, generally speaking, the OGA requires us to specify how to terminate the iterative procedure. One attractive feature of our algorithm is that the budget constraint plays the role of the stopping rule, without introducing any tuning parameters.

- Step 3. Experiment and data collection. Given the optimal selection of covariates  $\hat{\mathcal{I}}$  and sample size  $\hat{n}$ , we randomly assign  $\hat{n}$  individuals to either the treatment or the control group (with equal probability), and collect the covariates  $Z := X_{\hat{\mathcal{I}}}$  from each of them. This yields the experimental sample  $\mathcal{S}_{\exp} := \{Y_i, D_i, Z_i\}_{i=1}^{\hat{n}}$  from  $(Y, D, X_{\hat{\mathcal{I}}})$ .
- Step 4. Estimation of the average treatment effect. We regress  $Y_i$  on  $(1, D_i, Z_i)$  using the experimental sample  $S_{exp}$ . The OLS estimator of the coefficient on  $D_i$  is the average treatment effect estimator  $\hat{\beta}$ .
- Step 5. Computation of standard errors. Assuming the two samples  $S_{\text{pre}}$  and  $S_{\text{exp}}$  are independent, and that treatment is randomly assigned, the presence of the covariate selection Step 2 does not affect the asymptotic validity of the standard errors that one would use in the absence of Step 2. Therefore, asymptotically valid standard errors of  $\hat{\beta}$  can be computed in the usual fashion (see, e.g., Imbens and Rubin, 2015).

#### II.A Discussion

In this subsection, we discuss some of conceptual and practical properties of our proposed data collection procedure.

Availability of Pre-Experimental Data. As in standard power calculations, preexperimental data provide essential information for our procedure. The availability of such data is very common, ranging from census data sets and other household surveys to studies that were conducted in a similar context as the RCT we are planning to implement. In addition, if no such data set is available, one may consider running a pilot project that collects pre-experimental data. We recognize that in some cases it might be difficult to have the required information readily available. However, this is a problem that affects any attempt to a data-driven design of surveys, including standard power calculations. Even when pre-experimental data are imperfect, such calculations provide a valuable guide to survey design, as long as the available pre-experimental data are not very different from the ideal data. In particular, our procedure only requires second moments of the pre-experimental variables to be similar to those in the population of interest.

The Optimization Problem in a Simplified Setup. In general, the problem in equation (6) does not have a simple solution. To gain some intuition about the trade-offs in this problem, in Appendix C we consider a simplified setup in which all covariates are orthogonal to each other, and the budget constraint has a very simple form. We show that if all covariates have the same price, then one wants to choose covariates up to the point where the percentage increase in survey costs equals the percentage reduction in the MSE from the last covariate. Furthermore, the elasticity of the MSE with respect to changes in sample size should equal the elasticity of the MSE with respect to an additional covariate. If the costs of data collection vary with covariates, then this conclusion is slightly modified. If we organize variables by type according to their contribution to the MSE, then we want to choose variables of each type up to the point where the percent marginal contribution of each variable to the MSE equals its percent marginal contribution to survey costs.

**Imbalance and Re-randomization.** In RCTs, covariates typically do not only serve as a means to improving the precision of treatment effect estimators, but also for checking whether the control and treatment groups are balanced. See, for example,

Bruhn and McKenzie (2009) for practical issues concerning randomization and balance. To rule out large biases due to imbalance, it is important to carry out balance checks for strong predictors of potential outcomes. Our procedure selects the strongest predictors as long as they are not too expensive (e.g. household survey questions such as gender, race, number of children etc.) and we can check balance for these covariates. However, in principle, it is possible that our procedure does not select a strong predictor that is very expensive (e.g. baseline test scores). Such a situation occurs in our second empirical application (Section V.B). In this case, in Step 2, we recommend running the OGA a second time, forcing the inclusion of such expensive predictors. If the MSE of the resulting estimate is not much larger than that from the selection without the expensive predictor, then we may prefer the former selection to the latter so as to reduce the potential for bias due to imbalance at the expense of slightly larger variance of the treatment effect estimator.

An alternative approach to avoiding imbalance considers re-randomization until some criterion capturing the degree of balance is met (e.g., Bruhn and McKenzie (2009), Morgan and Rubin (2012, 2015)). Our criterion for the covariate selection procedure in Step 2 can readily be adapted to this case: we only need to replace our variance expression in the criterion function by the modified variance in Morgan and Rubin (2012), which accounts for the effect of re-randomization on the treatment effect estimator.

**Expensive, Strong Predictors.** When some covariates have similar predictive power, but respective prices that are substantially different, our covariate selection procedure may produce a suboptimal choice. For example, if the covariate with the highest price is also the most predictive, OGA selects it first even when there are other covariates that are much cheaper but only slightly less predictive. In Section V.B, we encounter an example of such a situation and propose a simple robustness check for whether removing an expensive, strong predictor may be beneficial.

Properties of the Treatment Effect Estimator. Since the treatment indicator is assumed independent of X, standard asymptotic theory of the treatment effect estimator continues to hold for our estimator (despite the addition of a covariate selection step). For example, it is unbiased, consistent, asymptotically normal, and adding the covariates X in the regression in (1) cannot increase the asymptotic variance of the estimator. In fact, inclusion of a covariate strictly reduces the estimator's asymptotic variance as long as the corresponding true regression coefficient is not zero. All these results hold regardless of whether the true conditional expectation of Y given D and X is in fact linear and additive separable as in (1) or not. In particular, in some applications one may want to include interaction terms of D and X (see, e.g., Imbens and Rubin, 2015). Finally, the treatment effect can be allowed to be heterogeneous (i.e. vary across individuals i) in which case our procedure estimates the average of those treatment effects.

An Alternative to Regression. Step 4 consists of running the regression in (1). There are instances when it is desirable to modify this step. For example, if the selected sample size  $\hat{n}$  is smaller than the number of selected covariates, then the regression in (1) is not feasible. However, if the pre-experimental sample  $S_{\text{pre}}$  is large enough, we can instead compute the OLS estimator  $\hat{\gamma}$  from the regression of Y on  $X_{\hat{I}}$  in  $S_{\text{pre}}$ . Then use Y and Z from the experimental sample  $S_{\text{exp}}$  to construct the new outcome variable  $\hat{Y}_i^* := Y_i - \hat{\gamma}' Z_i$  and compute the treatment effect estimator  $\hat{\beta}$  from the regression of  $\hat{Y}_i^*$  on  $(1, D_i)$ . This approach avoids fitting too many parameters when the experimental sample is small and has the additional desirable property that the resulting estimator is free from bias due to imbalance in the selected covariates.

# III A Simple Greedy Algorithm

In practice, the vector X of potential covariates is typically high-dimensional, which makes it challenging to solve the optimization problem (6). In this section, we propose a computationally feasible algorithm that is both conceptually simple and easy to implement.

We split the joint optimization problem in (6) over n and  $\gamma$  into two nested problems. The outer problem searches over the optimal sample size n, which is restricted to be on a grid  $n \in \mathcal{N} := \{n_0, n_1, \ldots, n_K\}$ , while the inner problem determines the optimal selection of covariates for each sample size n:

$$\min_{n \in \mathcal{N}} \frac{1}{n} \min_{\gamma \in \mathbb{R}^M} \frac{1}{N} \sum_{i=1}^N (Y_i - \gamma' X_i)^2 \qquad \text{s.t.} \qquad c(\mathcal{I}(\gamma), n) \le B.$$
(7)

To convey our ideas in a simple form, suppose for the moment that the budget constraint has the following linear form,

$$c(\mathcal{I}(\gamma), n) = n \cdot |\mathcal{I}(\gamma)| \le B_{2}$$

where  $|\mathcal{I}(\gamma)|$  denotes the number of non-zero elements of  $\gamma$ . Note that the budget constraint puts the restriction on the number of selected covariates, that is,  $|\mathcal{I}(\gamma)| \leq B/n$ .

It is known to be NP-hard (non-deterministic polynomial time hard) to find a solution to the inner optimization problem in (7) subject to the constraint that  $\gamma$  has m non-zero components, also called an m-term approximation, where m is the integer part of B/n in our problem. In other words, solving (7) directly is not feasible unless the dimension of covariates, M, is small (Natarajan, 1995; Davis, Mallat, and Avellaneda, 1997).

There exists a class of computationally attractive procedures called greedy algorithms that are able to approximate the infeasible solution. See Temlyakov (2011) for a detailed discussion of greedy algorithms in the context of approximation theory. Tropp (2004), Tropp and Gilbert (2007), Barron, Cohen, Dahmen, and DeVore (2008), Zhang (2009), Huang, Zhang, and Metaxas (2011), Ing and Lai (2011), and Sancetta (2016), among many others, demonstrate the usefulness of greedy algorithms for signal recovery in information theory, and for the regression problem in statistical learning. We use a variant of OGA that can allow for selection of groups of variables (see, for example, Huang, Zhang, and Metaxas (2011)).

To formally define our proposed algorithm, we introduce some notation. For a vector v of N observations  $v_1, \ldots, v_N$ , let  $||v||_N := (1/N \sum_{i=1}^N v_i^2)^{1/2}$  denote the empirical  $L^2$ -norm and let  $\mathbf{Y} := (Y_1, \ldots, Y_N)'$ .

Suppose that the covariates  $X^{(j)}$ , j = 1, ..., M, are organized into p pre-determined groups  $X_{G_1}, ..., X_{G_p}$ , where  $G_k \subseteq \{1, ..., p\}$  indicates the covariates of group k. We denote the corresponding matrices of observations by bold letters (i.e.,  $\mathbf{X}_{G_k}$  is the  $N \times |G_k|$  matrix of observations on  $X_{G_k}$ , where  $|G_k|$  denotes the number of elements of the index set  $G_k$ ). By a slight abuse of notation, we let  $\mathbf{X}_k := \mathbf{X}_{\{k\}}$  be the column vector of observations on  $X_k$  when k is a scalar. One important special case is that in which each group consists of a single regressor. Furthermore, we allow for overlapping groups; in other words, some elements can be included in multiple or even all groups. The group structure occurs naturally in experiments where data collection is carried out through surveys whose questions can be grouped in those concerning income, those concerning education, and so on.

Suppose that the largest group size  $J_{\max} := \max_{k=1,\dots,p} |G_k|$  is small, so that we can implement orthogonal transformations within each group such that  $(\mathbf{X}'_{G_j}\mathbf{X}_{G_j})/N =$  $\mathbf{I}_{|G_j|}$ , where  $\mathbf{I}_d$  is the *d*-dimensional identity matrix. In what follows, assume that  $(\mathbf{X}'_{G_j}\mathbf{X}_{G_j})/N = \mathbf{I}_{|G_j|}$  without loss of generality. Let  $|\cdot|_2$  denote the  $\ell_2$  norm. The following procedure describes our algorithm.

STEP 1. Set the initial sample size  $n = n_0$ .

STEP 2. Group OGA for a given sample size n:

- (a) initialize the inner loop at k = 0 and set the initial residual  $\hat{\mathbf{r}}_{n,0} = \mathbf{Y}$ , the initial covariate indices  $\hat{\mathcal{I}}_{n,0} = \emptyset$  and the initial group indices  $\hat{\mathcal{G}}_{n,0} = \emptyset$ ;
- (b) separately regress  $\hat{\mathbf{r}}_{n,k}$  on each group of regressors in  $\{1, \ldots, p\} \setminus \hat{\mathcal{G}}_{n,k}$ ; call  $\hat{j}_{n,k}$  the group of regressors with the largest  $\ell_2$  regression coefficients,

$$\hat{j}_{n,k} := \arg \max_{j \in \{1,\dots,p\} \setminus \hat{\mathcal{G}}_{n,k}} \left| \mathbf{X}_{G_j}' \hat{\mathbf{r}}_{n,k} \right|_2;$$

add  $\hat{j}_{n,k}$  to the set of selected groups,  $\hat{\mathcal{G}}_{n,k+1} = \hat{\mathcal{G}}_{n,k} \cup \{\hat{j}_{n,k}\};$ 

- (c) regress  $\mathbf{Y}$  on the covariates  $\mathbf{X}_{\hat{\mathcal{I}}_{n,k+1}}$  where  $\hat{\mathcal{I}}_{n,k+1} := \hat{\mathcal{I}}_{n,k} \cup G_{\hat{j}_{n,k}}$ ; call the regression coefficient  $\hat{\gamma}_{n,k+1} := (\mathbf{X}'_{\hat{\mathcal{I}}_{n,k+1}} \mathbf{X}_{\hat{\mathcal{I}}_{n,k+1}})^{-1} \mathbf{X}'_{\hat{\mathcal{I}}_{n,k+1}} \mathbf{Y}$  and the residual  $\hat{\mathbf{r}}_{n,k+1} := \mathbf{Y} \mathbf{X}_{\hat{\mathcal{I}}_{n,k+1}} \hat{\gamma}_{n,k+1};$
- (d) increase k by one and continue with (b) as long as  $c(\hat{\mathcal{I}}_{n,k}, n) \leq B$  is satisfied;
- (e) let  $k_n$  be the number of selected groups; call the resulting submatrix of selected regressors  $\mathbf{Z} := \mathbf{X}_{\hat{\mathcal{I}}_{n,k_n}}$  and  $\hat{\gamma}_n := \hat{\gamma}_{n,k_n}$ , respectively.
- STEP 3. Set n to the next sample size in  $\mathcal{N}$ , and go to Step 2 until (and including)  $n = n_K$ .

STEP 4. Set  $\hat{n}$  as the sample size that minimizes the MSE:

$$\hat{n} := \arg\min_{n \in \mathcal{N}} \frac{1}{nN} \sum_{i=1}^{N} \left( Y_i - \mathbf{Z}_i \hat{\gamma}_n \right)^2.$$

The algorithm above produces the selected sample size  $\hat{n}$ , the selection of covariates  $\hat{\mathcal{I}} := \hat{\mathcal{I}}_{\hat{n},k_{\hat{n}}}$  with  $k_{\hat{n}}$  selected groups and  $\hat{m} := m(\hat{n}) := |\hat{\mathcal{I}}_{\hat{n},k_{\hat{n}}}|$  selected regressors. Here,  $\hat{\gamma} := \hat{\gamma}_{\hat{n}}$  is the corresponding coefficient vector on the selected regressors Z.

Remark 1. Theorem A.1 in Appendix A gives the finite-sample bound on the MSE of the average treatment effect estimator resulting from our OGA method. The natural target for this MSE is an infeasible MSE when  $\gamma_0$  is known *a priori*. Theorem A.1 establishes conditions under which the difference between the MSE resulting from our method and the infeasible MSE decreases at a rate of 1/k as k increases, where k is the number of the steps in the OGA. It is known in a simpler setting than ours that this rate 1/k cannot generally be improved (see, e.g., Barron, Cohen, Dahmen, and DeVore, 2008). In this sense, we show that our proposed method has a desirable property. See Appendix A for further details.

Remark 2. There are many important reasons for collecting covariates, such as checking whether randomization was carried out properly and identifying heterogeneous treatment effects, among others. If a few covariates are essential for the analysis, we can guarantee their selection by including them in every group  $G_k$ ,  $k = 1, \ldots, p$ .

# IV The Costs of Data Collection

In this section, we discuss the specification of the cost function c(S, n) that defines the budget constraint of the researcher. In principle, it is possible to construct a matrix containing the value of the costs of data collection for every possible combination of S and n without assuming any particular form of relationship between the individual entries. However, determination of the costs for every possible combination of S and n is a cumbersome and, in practice, probably infeasible exercise. Therefore, we consider the specification of cost functions that capture the costs of all stages of the data collection process in a more parsimonious fashion.

We propose to decompose the overall costs of data collection into three components: administration costs  $c_{admin}(S)$ , training costs  $c_{train}(S, n)$ , and interview costs  $c_{interv}(S, n)$ , so that

$$c(S,n) = c_{\text{admin}}(S) + c_{\text{train}}(S,n) + c_{\text{interv}}(S,n).$$
(8)

In the remainder of this section, we discuss possible specifications of the three types of costs by considering fixed and variable cost components corresponding to the different stages of the data collection process. The exact functional form assumptions are based on the researcher's knowledge about the operational details of the survey process. Even though this section's general discussion is driven by our experience in the empirical applications of Section V, the operational details are likely to be similar for many surveys, so we expect the following discussion to provide a useful starting point for other data collection projects.

We start by specifying survey time costs. Let  $\tau_j$ ,  $j = 1, \ldots, M$ , be the costs of collecting variable j for one individual, measured in units of survey time. Similarly, let  $\tau_0$  denote the costs of collecting the outcome variable, measured in units of survey time.

Then, the total time costs of surveying one individual to elicit the variables indicated by S are

$$T(S) := \tau_0 + \sum_{j=1}^M \tau_j S_j.$$

### IV.A Administration and Training Costs

A data collection process typically incurs costs due to administrative work and training prior to the start of the actual survey. Examples of such tasks are developing the questionnaire and the program for data entry, piloting the questionnaire, developing the manual for administration of the survey, and organizing the training required for the enumerators.

Fixed costs, which depend neither on the size of the survey nor on the sample size of survey participants, can simply be subtracted from the budget. We assume that B is already net of such fixed costs.

Most administrative and training costs tend to vary with the size of the questionnaire and the number of survey participants. Administrative tasks such as development of the questionnaire, data entry, and training protocols are independent of the number of survey participants, but depend on the size of the questionnaire (measured by the number of positive entries in S) as smaller questionnaires are less expensive to prepare than larger ones. We model those costs by

$$c_{\text{admin}}(S) := \phi T(S)^{\alpha},\tag{9}$$

where  $\phi$  and  $\alpha$  are scalars to be chosen by the researcher. We assume  $0 < \alpha < 1$ , which means that marginal costs are positive but decline with survey size.

Training of the enumerators depends on the survey size, because a longer survey requires more training, and on the number of survey participants, because surveying more individuals usually requires more enumerators (which, in turn, may raise the costs of training), especially when there are limits on the duration of the fieldwork. We therefore specify training costs as

$$c_{\text{train}}(S,n) := \kappa(n) T(S), \tag{10}$$

where  $\kappa(n)$  is some function of the number of survey participants.<sup>2</sup> Training costs are

<sup>&</sup>lt;sup>2</sup>It is of course possible that  $\kappa$  depends not only on *n* but also on T(S). We model it this way for simplicity, and because it is a sensible choice in the applications we discuss below.

typically lumpy because, for example, there exists only a limited set of room sizes one can rent for the training, so we model  $\kappa(n)$  as a step function:

$$\kappa(n) = \begin{cases} \overline{\kappa}_1 & \text{if } 0 < n \le \overline{n}_1 \\ \overline{\kappa}_2 & \text{if } \overline{n}_1 < n \le \overline{n}_2 \\ \vdots \end{cases}$$

Here,  $\overline{\kappa}_1, \overline{\kappa}_2, \ldots$  is a sequence of scalars describing the costs of sample sizes in the ranges defined by the cut-off sequence  $\overline{n}_1, \overline{n}_2, \ldots$ 

#### **IV.B** Interview Costs

Enumerators are often paid by the number of interviews conducted, and the payment increases with the size of the questionnaire. Let  $\eta$  denote fixed costs per interview that are independent of the size of the questionnaire and of the number of participants. These are often due to travel costs and can account for a substantive fraction of the total interview costs. Suppose the variable component of the interview costs is linear so that total interview costs can be written as

$$c_{\text{interv}}(S,n) := n\eta + np T(S), \tag{11}$$

where T(S) should now be interpreted as the average time spent per interview, and p is the average price of one unit of survey time. We employ the specification (8) with (9)– (11) when studying the impact of free day-care on child development in Section V.A.

Remark 3. Because we always collect the outcome variable, we incur the fixed costs  $n\eta$  and the variable costs  $np\tau_0$  even when no covariates are collected.

*Remark* 4. Non-financial costs are difficult to model, but could in principle be added. They are primarily related to the impact of sample and survey size on data quality. For example, if we design a survey that takes more than four hours to complete, the quality of the resulting data is likely to be affected by interviewer and interviewee fatigue. Similarly, conducting the training of enumerators becomes more difficult as the survey size grows. Hiring high-quality enumerators may be particularly important in that case, which could result in even higher costs (although this latter observation could be explicitly considered in our framework).

#### **IV.C** Clusters

In many experiments, randomization is carried out at a cluster level (e.g., school level), rather than at an individual level (e.g., student level). In this case, training costs may depend not only on the ultimate sample size  $n = c n_c$ , where c and  $n_c$  denote the number of clusters and the number of participants per cluster, respectively, but on a particular combination  $(c, n_c)$ , because the number of required enumerators may be different for different  $(c, n_c)$  combinations. Therefore, training costs (which now also depend on c and  $n_c$ ) may be modeled as

$$c_{\text{train}}(S, n_c, c) := \kappa(c, n_c) T(S).$$
(12)

The interaction of cluster and sample size in determining the number of required enumerators and, thus, the quantity  $\kappa(c, n_c)$ , complicates the modeling of this quantity relative to the case without clustering. Let  $\mu(c, n_c)$  denote the number of required survey enumerators for c clusters of size  $n_c$ . As in the case without clustering, we assume that the training costs is lumpy in the number of enumerators used:

$$\kappa(c, n_c) := \begin{cases} \overline{\kappa}_1 & \text{if} \quad 0 < \mu(c, n_c) \le \overline{\mu}_1 \\ \overline{\kappa}_2 & \text{if} \quad \overline{\mu}_1 < \mu(c, n_c) \le \overline{\mu}_2 \\ \vdots \end{cases}$$

The number of enumerators required,  $\mu(c, n_c)$ , may also be lumpy in the number of interviewees per cluster,  $n_c$ , because there are bounds to how many interviews each enumerator can carry out. Also, the number of enumerators needed for the survey typically increases in the number of clusters in the experiment. Therefore, we model  $\mu(c, n_c)$  as

$$\mu(c, n_c) := \lfloor \mu_c(c) \cdot \mu_n(n_c) \rfloor,$$

where  $\lfloor \cdot \rfloor$  denotes the integer part,  $\mu_c(c) := \lambda c$  for some constant  $\lambda$  (i.e.,  $\mu_c(c)$  is assumed to be linear in c), and

$$\mu_n(n_c) := \begin{cases} \overline{\mu}_{n,1} & \text{if } 0 < n_c \le \overline{n}_1 \\ \overline{\mu}_{n,2} & \text{if } \overline{n}_1 < n_c \le \overline{n}_2 \\ \vdots \end{cases}$$

In addition, while the variable interview costs component continues to depend on the overall sample size n as in (11), the fixed part of the interview costs is determined by the number of clusters c rather than by n. Therefore, the total costs per interview become

$$c_{\text{interv}}(S, n_c, c) := \psi(c)\eta + cn_c p T(S), \tag{13}$$

where  $\psi(c)$  is some function of the number of clusters c.

#### IV.D Covariates with Heterogeneous Prices

In randomized experiments, the data collection process often differs across blocks of covariates. For example, the researcher may want to collect outcomes of psychological tests for the members of the household that is visited. These tests may need to be administered by trained psychologists, whereas administering a questionnaire about background variables such as household income, number of children, or parental education, may not require any particular set of skills or qualifications other than the training provided as part of the data collection project.

Partition the covariates into two blocks, a high-cost block (e.g., outcomes of psychological tests) and a low-cost block (e.g., standard questionnaire). Order the covariates such that the first  $M_{\text{low}}$  covariates belong to the low-cost block, and the remaining  $M_{\text{high}} := M - M_{\text{low}}$  together with the outcome variable belong to the high-cost block. Let

$$T_{\text{low}}(S) := \sum_{j=1}^{M_{\text{low}}} \tau_j S_j \quad \text{and} \quad T_{\text{high}}(S) := \tau_0 + \sum_{j=M_{\text{low}}+1}^{M} \tau_j S_j$$

be the total time costs per individual of surveying all low-cost and high-cost covariates, respectively. Then, the total time costs for all variables can be written as  $T(S) = T_{\text{low}}(S) + T_{\text{high}}(S)$ .

Because we require two types of enumerators, one for the high-cost covariates and one for the low-cost covariates, the financial costs of each interview (fixed and variable) may be different for the two blocks of covariates. Denote these by  $\psi_{\text{low}}(c, n_c)\eta_{\text{low}} + cn_c p_{\text{low}}T_{\text{low}}(S)$  and  $\psi_{\text{high}}(c, n_c)\eta_{\text{high}} + cn_c p_{\text{high}}T_{\text{high}}(S)$ , respectively.

The fixed costs for the high-cost block are incurred regardless of whether highcost covariates are selected or not, because we always collect the outcome variable, which here is assumed to belong to this block. The fixed costs for the low-cost block, however, are incurred only when at least one low-cost covariate is selected (i.e., when  $\sum_{j=1}^{M_{\text{low}}} S_j > 0$ ). Therefore, the total interview costs for all covariates can be written as

$$c_{\text{interv}}(S,n) := \mathbb{1}\left\{\sum_{j=1}^{M_{\text{low}}} S_j > 0\right\} (\psi_{\text{low}}(c,n_c)\eta_{\text{low}} + cn_c p_{\text{low}}T_{\text{low}}(S)) + \psi_{\text{high}}(c,n_c)\eta_{\text{high}} + cn_c p_{\text{high}}T_{\text{high}}(S).$$
(14)

The administration and training costs can also be assumed to differ for the two types of enumerators. In that case,

$$c_{\text{admin}}(S) := \phi_{\text{low}} T_{\text{low}}(S)^{\alpha_{\text{low}}} + \phi_{\text{high}} T_{\text{high}}(S)^{\alpha_{\text{high}}},\tag{15}$$

$$c_{\text{train}}(S,n) := \kappa_{\text{low}}(c,n_c) T_{\text{low}}(S) + \kappa_{\text{high}}(c,n_c) T_{\text{high}}(S).$$
(16)

We employ specification (8) with (13)-(16) when, in Section V.B, we study the impact on student learning of cash grants which are provided to schools.

# V Empirical Applications

#### V.A Access to Free Day-Care in Rio

In this section, we re-examine the experimental design of Attanasio et al. (2014), who evaluate the impact of access to free day-care on child development and household resources in Rio de Janeiro. In their dataset, access to care in public day-care centers, most of which are located in slums, is allocated through a lottery, administered to children in the waiting lists for each day-care center.

Just before the 2008 school year, children applying for a slot at a public day-care center were put on a waiting list. At this time, children were between the ages of 0 and 3. For each center, when the demand for day-care slots in a given age range exceeded the supply, the slots were allocated using a lottery (for that particular age range). The use of such an allocation mechanism means that we can analyze this intervention as if it was an RCT, where the offer of free day-care slots is randomly allocated across potentially eligible recipients. Attanasio et al. (2014) compare the outcomes of children and their families who were awarded a day-care slot through the lottery, with the outcomes of those not awarded a slot.

The data for the study were collected mainly during the second half of 2012, four and a half years after the randomization took place. Most children were between the ages of 5 and 8. A survey was conducted, which had two components: a household questionnaire, administered to the mother or guardian of the child; and a battery of health and child development assessments, administered to children. Each household was visited by a team of two field workers, one for each component of the survey.

The child assessments took a little less than one hour to administer, and included five tests per child, plus the measurement of height and weight. The household survey took between one and a half and two hours, and included about 190 items, in addition to a long module asking about day-care history, and the administration of a vocabulary test to the main carer of each child.

As we explain below, we use the original sample, with the full set of items collected in the survey, to calibrate the cost function for this example. However, when solving the survey design problem described in this paper we consider only a subset of items of these data, with the original budget being scaled down properly. This is done for simplicity, so that we can essentially ignore the fact that some variables are missing for part of the sample, either because some items are not applicable to everyone in the sample, or because of item non-response. We organize the child assessments into three indices: cognitive tests, executive function tests, and anthropometrics (height and weight). These three indices are the main outcome variables in the analysis. However, we use only the cognitive tests and anthropometrics indices in our analysis, as we have fewer observations for executive function tests.

We consider only 40 covariates out of the total set of items on the questionnaire. The variables not included can be arranged into four groups: (i) variables that can be seen as final outcomes, such as questions about the development and the behavior of the children in the household; (ii) variables that can be seen as intermediate outcomes, such as labor supply, income, expenditure, and investments in children; (iii) variables for which there is an unusually large number of missing values; and (iv) variables that are either part of the day-care history module, or the vocabulary test for the child's carer (because these could have been affected by the lottery assigning children to daycare vacancies). We then drop four of the 40 covariates chosen, because their variance is zero in the sample. The remaining M = 36 covariates are related to the respondent's age, literacy, educational attainment, household size, safety, burglary at home, day care, neighborhood, characteristics of the respondent's home and its surroundings (the number of rooms, garbage collection service, water filter, stove, refrigerator, freezer, washer, TV, computer, Internet, phone, car, type of roof, public light in the street, pavement, etc.). We drop individuals for whom at least one value in each of these covariates is missing, which leads us to use a subsample with 1,330 individuals from the original experimental sample, which included 1,466 individuals.

Calibration of the cost function. We specify the cost function (8) with components (9)–(11) to model the data collection procedure as implemented in Attanasio et al. (2014). We calibrate the parameters using the actual budgets for training, administrative, and interview costs in the authors' implementation. The contracted total budget of the data collection process was R\$665,000.<sup>3</sup>

For the calibration of the cost function, we use the originally planned budget of R\$665,000, and the original sample size of 1,466. As mentioned above, there were 190 variables collected in the household survey, together with a day-care module and a vocabulary test. In total, this translates into a total of roughly 240 variables.<sup>4</sup> Appendix B provides a detailed description of all components of the calibrated cost function.

**Implementation.** In implementing the OGA, we take each single variable as a possible group (i.e., each group consists of a singleton set). We studentized all covariates to have variance one. To compare the OGA with alternative approaches, we also consider LASSO and POST-LASSO for the inner optimization problem in Step 2 of our procedure. The LASSO solves

$$\min_{\gamma} \frac{1}{N} \sum_{i=1}^{N} \left( Y_i - \gamma' X_i \right)^2 + \lambda \sum_j |\gamma_j| \tag{17}$$

with a tuning parameter  $\lambda > 0$ . The POST-LASSO procedure runs an OLS regression of  $Y_i$  on the selected covariates (non-zero entries of  $\gamma$ ) in (17). Belloni and Chernozhukov (2013), for example, provide a detailed description of the two algorithms. It is known that LASSO yields biased regression coefficient estimates and that POST-LASSO can mitigate this bias problem. Together with the outer optimization over the sample size using the LASSO or POST-LASSO solutions in the inner loop may lead to different selections of covariate-sample size combinations. This is because POST-LASSO re-estimates the regression equation which may lead to more precise estimates of  $\gamma$  and thus result in a different estimate for the MSE of the treatment effect estimator.

<sup>&</sup>lt;sup>3</sup>There were some adjustments to the budget during the period of fieldwork.

<sup>&</sup>lt;sup>4</sup>The budget is for the 240 variables (or so) actually collected. In spite of that, we only use 36 of these as covariates in this paper, as the remaining variables in the survey were not so much covariates as they were measuring other intermediate and final outcomes of the experiment, as we have explained before. The actual budget used in solving the survey design problem is scaled down to match the use of only 36 covariates.

In both LASSO implementations, the penalization parameter  $\lambda$  is chosen so as to satisfy the budget constraint as close to equality as possible. We start with a large value for  $\lambda$ , which leads to a large penalty for non-zero entries in  $\gamma$ , so that few or no covariates are selected and the budget constraint holds. Similarly, we consider a very small value for  $\lambda$  which leads to the selection of many covariates and violation of the budget. Then, we use a bisection algorithm to find the  $\lambda$ -value in this interval for which the budget is satisfied within some pre-specified tolerance.

Table 1: Day-care (outcome: cognitive test)

Method	$\hat{n}$	$ \hat{I} $	$\operatorname{Cost}/\operatorname{B}$	RMSE	EQB	Relative EQB
Experiment	1,330	36	1	0.025285	R\$562,323	1
OGA	$2,\!677$	1	0.9939	0.018776	R\$312,363	0.555
LASSO	2,762	0	0.99475	0.018789	R\$313,853	0.558
POST-LASSO	$2,\!677$	1	0.9939	0.018719	R\$312,363	0.555

Table 2: Day-care (outcome: health assessment)

Method	$\hat{n}$	$ \hat{I} $	$\operatorname{Cost}/\operatorname{B}$	RMSE	EQB	Relative EQB
Experiment	1,330	36	1	0.025442	R\$562,323	1
OGA	2,762	0	0.99475	0.018799	R\$308,201	0.548
LASSO	2,762	0	0.99475	0.018799	R\$308,201	0.548
POST-LASSO	$2,\!677$	1	0.9939	0.018735	R\$306,557	0.545

**Results.** Tables 1 and 2 summarize the results of the covariate selection procedures. For the cognitive test outcome, OGA and POST-LASSO select one covariate (" $|\hat{I}|$ "),<sup>5</sup> whereas LASSO does not select any covariate. The selected sample sizes (" $\hat{n}$ ") are 2,677 for OGA and POST-LASSO, and 2,762 for LASSO, which are almost twice as large as the actual sample size in the experiment. The performance of the three covariate selection methods in terms of the precision of the resulting treatment effect estimator is measured by the square-root value of the minimized MSE criterion function ("RMSE")

<sup>&</sup>lt;sup>5</sup>For OGA, it is an indicator variable whether the respondent has finished secondary education, which is an important predictor of outcomes; for POST-LASSO, it is the number of rooms in the house, which can be considered as a proxy for wealth of the household, and again, an important predictor of outcomes.

from Step 2 of our procedure. The three methods perform similarly well and improve precision by about 25% relative to the experiment. Also, all three methods manage to exhaust the budget, as indicated by the cost-to-budget ratios ("Cost/B") close to one. We do not put any strong emphasis on the selected covariates as the improvement of the criterion function is minimal relative to the case that no covariate is selected (i.e., the selection with LASSO). The results for the health assessment outcome are very similar to those of the cognitive test with POST-LASSO selecting one variable (the number of rooms in the house), whereas OGA and LASSO do not select any covariate.

To assess the economic gain of having performed the covariate selection procedure after the first wave, we include the column "EQB" (abbreviation of "equivalent budget") in Tables 1 and 2. The first entry of this column in Table 1 reports the budget necessary for the selection of  $\hat{n} = 1,330$  and all covariates, as was carried out in the experiment. For the three covariate selection procedures, the column shows the budget that would have sufficed to achieve the same precision as the actual experiment in terms of the minimum value of the MSE criterion function in Step 2. For example, for the cognitive test outcome, using the OGA to select the sample size and the covariates, a budget of R\$312,363 would have sufficed to achieve the experimental RMSE of 0.025285. This is a huge reduction of costs by about 45 percent, as shown in the last column called "relative EQB". Similar reductions in costs are possible when using the LASSO procedures and also when considering the health assessment outcome.

Appendix D presents the results of Monte Carlo simulations that mimic this dataset, and shows that all three methods select more covariates and smaller sample sizes as we increase the predictive power of some covariates. This finding suggests that the covariates collected in the survey were not predicting the outcome very well and, therefore, in the next wave the researcher should spend more of the available budget to collect data on more individuals, with no (or only a minimal) household survey. Alternatively, the researcher may want to redesign the household survey to include questions whose answers are likely better predictors of the outcome.

#### V.B Provision of School Grants in Senegal

In this subsection, we consider the study by Carneiro et al. (2015) who evaluate, using an RCT, the impact of school grants on student learning in Senegal. The authors collect original data not only on the treatment status of schools (treatment and control) and on student learning, but also on a variety of household, principal, and teacher characteristics that could potentially affect learning. The dataset contains two waves, a baseline and a follow-up, which we use for the study of two different hypothetical scenarios. In the first scenario, the researcher has access to a pre-experimental dataset consisting of all outcomes and covariates collected in the baseline survey of this experiment, but not the follow-up data. The researcher applies the covariate selection procedure to this pre-experimental dataset to find the optimal sample size and set of covariates for the randomized control trial to be carried out after the first wave. In the second scenario, in addition to the pre-experimental sample from the first wave the researcher now also has access to the post-experimental outcomes collected in the follow-up (second wave). In this second scenario, we treat the follow-up outcomes as the outcomes of interest and include baseline outcomes in the pool of covariates that predict follow-up outcomes.

As in the previous subsection, we calibrate the cost function based on the full dataset from the experiment, but for solving the survey design problem we focus on a subset of individuals and variables from the original questionnaire. For simplicity, we exclude all household variables from the analysis, because they were only collected for 4 out of the 12 students tested in each school, and we remove covariates whose sample variance is equal to zero. Again, for simplicity, of the four outcomes (math test, French test, oral test, and receptive vocabulary) in the original experiment, we only consider the first one (math test) as our outcome variable. We drop individuals for whom at least one answer in the survey or the outcome variable is missing. This sample selection procedure leads to sample sizes of N = 2,280 for the baseline math test outcome. For the second scenario discussed above where we use also the follow-up outcome, the sample size is smaller (N = 762) because of non-response in the follow-up outcome and because we restrict the sample to the control group of the follow-up. In the first scenario in which we predict the baseline outcome, dropping household variables reduces the original number of covariates in the survey from 255 to M = 142. The remaining covariates are school- and teacher-level variables. In the second scenario in which we predict follow-up outcomes, we add the three baseline outcomes to the covariate pool, but at the same time remove two covariates because they have variance zero when restricted to the control group. Therefore, there are M = 143 covariates in the second scenario.

Calibration of the cost function. We specify the cost function (8) with components (14)–(16) to model the data collection procedure as implemented in Carneiro et al. (2015). Each school forms a cluster. We calibrate the parameters using the costs faced by the researchers and their actual budgets for training, administrative, and in-

terview costs. The total budget for one wave of data collection in this experiment, excluding the costs of the household survey, was approximately \$192,200.

For the calibration of the cost function, we use the original sample size, the original number of covariates in the survey (except those in the household survey), and the original number of outcomes collected at baseline. The three baseline outcomes were much more expensive to collect than the remaining covariates. In the second scenario, we therefore group the former together as high-cost variables, and all remaining covariates as low-cost variables. Appendix B provides a detailed description of all components of the calibrated cost function.

**Implementation.** The implementation of the covariate selection procedures is identical to the one in the previous subsection except that we consider here two different specifications of the pre-experimental sample  $S_{pre}$ , depending on whether the outcome of interest is the baseline or follow-up outcome.

**Results.** Table 3 summarizes the results of the covariate selection procedures. Panel (a) shows the results of the first scenario in which the baseline math test is used as the outcome variable to be predicted. Panel (b) shows the corresponding results for the second scenario in which the baseline outcomes are treated as high-cost covariates and the follow-up math test is used as the outcome to be predicted.

For the baseline outcome in panel (a), the OGA selects only  $|\hat{I}| = 14$  out of the 145 covariates with a selected sample size of  $\hat{n} = 3,018$ , which is about 32% larger than the actual sample size in the experiment. The results for the LASSO and POST-LASSO methods are similar. As in the previous subsection, we measure the performance of the three covariate selection methods by the estimated precision of the resulting treatment effect estimator ("RMSE"). The three methods improve the precision by about 7% relative to the experiment. Also, all three methods manage to essentially exhaust the budget, as indicated by cost-to-budget ratios ("Cost/B") close to one. As in the previous subsection, we measure the economic gains from using the covariate selection procedures by the equivalent budget ("EQB") that each of the method requires to achieve the precision of the experiment. All three methods require equivalent budgets that are 7-9% lower than that of the experiment.

All variables that the OGA selects as strong predictors of baseline outcome are plausibly related to student performance on a math test:<sup>6</sup> They are related to important

 $<sup>^6\</sup>mathrm{Online}$  Appendix E shows the full list and definitions of selected covariates for the baseline outcome.

Method	$\hat{n}$	$ \hat{I} $	Cost/B	RMSE	EQB	Relative EQB		
(a) Baseline outcome								
experiment	$2,\!280$	142	1	0.0042272	\$30,767	1		
OGA	$3,\!018$	14	0.99966	0.003916	\$28,141	0.91		
LASSO	$2,\!985$	18	0.99968	0.0039727	\$28,669	0.93		
POST-LASSO	$2,\!985$	18	0.99968	0.0038931	\$27,990	0.91		
(b) Follow-up outcome								
experiment	762	143	1	0.0051298	\$52,604	1		
OGA	6,755	0	0.99961	0.0027047	\$22,761	0.43		
LASSO	6,755	0	0.99961	0.0027047	\$22,761	0.43		
POST-LASSO	6,755	0	0.99961	0.0027047	\$22,761	0.43		
(c) Follow-up outcome, no high-cost covariates								
experiment	762	143	1	0.0051298	\$52,604	1		
OGA	$5,\!411$	140	0.99879	0.0024969	\$21,740	0.41		
LASSO	$5,\!444$	136	0.99908	0.00249	\$22,082	0.42		
POST-LASSO	$6,\!197$	43	0.99933	0.0024624	\$21,636	0.41		
(d) Follow-up outcome, force baseline outcome								
experiment	762	143	1	0.0051298	\$52,604	1		
OGA	$1,\!314$	133	0.99963	0.0040293	\$41,256	0.78		
LASSO	2,789	1	0.9929	0.0043604	\$42,815	0.81		
POST-LASSO	2,789	1	0.9929	0.0032823	\$32,190	0.61		

Table 3: School grants (outcome: math test)

aspects of the community surrounding the school (e.g., distance to the nearest city), school equipment (e.g., number of computers), school infrastructure (e.g., number of temporary structures), human resources (e.g., teacher–student ratio, teacher training), and teacher and principal perceptions about which factors are central for success in the school and about which factors are the most important obstacles to school success.

For the follow-up outcome in panel (b), the budget used in the experiment increases due to the addition of the three expensive baseline outcomes to the pool of covariates. All three methods select no covariates and exhaust the budget by using the maximum feasible sample size of 6,755, which is almost nine times larger than the sample size in the experiment. The implied precision of the treatment effect estimator improves by about 47% relative to the experiment, which translates into the covariate selection methods requiring less than half of the experimental budget to achieve the same precision as in the experiment. These are substantial statistical and economic gains from using our proposed procedure.

Sensitivity Checks. In RCT's, baseline outcomes tend to be strong predictors of the follow-up outcome. One may therefore be concerned that, because the OGA first selects the most predictive covariates which in this application are also much more expensive than the remaining low-cost covariates, the algorithm never examines what would happen to the estimator's MSE if it first selects the most predictive low-cost covariates instead. In principle, such selection could lead to a lower MSE than any selection that includes the very expensive baseline outcomes. As a sensitivity check we therefore perform the covariate selection procedures on the pool of covariates that excludes the three baseline outcomes. Panel (c) shows the corresponding results. In this case, all methods indeed select more covariates and smaller sample sizes than in panel (b), and achieve a slightly smaller MSE. The budget reductions relative to the experiment as measured by EQB are also almost identical to those in panel (b). Therefore, both selections of either no covariates and large sample size (panel (b)) and many low-cost covariates with somewhat smaller sample size (panel (c)) yield very similar and significant improvements in precision or significant reductions in the experimental budget, respectively.<sup>7</sup>

As discussed in Section II.A, one may want to ensure balance of the control and treatment group, especially in terms of strong predictors such as baseline outcomes. Checking balance requires collection of the relevant covariates. Therefore, we also perform the three covariate selection procedures when we force each of them to include the baseline math outcome as a covariate. In the OGA, we can force the selection of a covariate by performing group OGA as described in Section III, where each group contains a low-cost covariate together with the baseline math outcome. For the LASSO procedures, we simply perform the LASSO algorithms after partialing out the baseline math outcome from the follow-up outcome. The corresponding results are reported in panel (d). Since baseline outcomes are very expensive covariates, the selected sample sizes relative to those in panels (b) and (c) are much smaller. OGA selects a sample size of 1,314 which is almost twice as large as the experimental sample size, but about

<sup>&</sup>lt;sup>7</sup>Note that there is no sense in which need to be concerned about identification of the minimizing set of covariates. There may indeed exist several combinations of covariates that yield similar precision of the resulting treatment effect estimator. Our objective is highest possible precision without any direct interest in the identities of the covariates that achieve that minimum.

4-5 times smaller than the OGA selections in panels (b) and (c). In contrast to OGA, the two LASSO procedures do not select any other covariates beyond the baseline math outcome. As a result of forcing the selection of the baseline outcome, all three methods achieve an improvement in precision, or reduction of budgets respectively, of around 20% relative to the experiment. These are still substantial gains, but the requirement of checking balance on the expensive baseline outcome comes at the cost of smaller improvements in precision due to our procedure.

# **VI** Relation to the Existing Literature

In this section, we discuss related papers in the literature. We emphasize that the research question in our paper is different from those studied in the literature and that our paper is a complement to the existing work.

In the context of experimental economics, List, Sadoff, and Wagner (2011) suggest several simple rules of thumb that researchers can apply to improve the efficiency of their experimental designs. They discuss the issue of experimental costs and estimation efficiency but did not consider the problem of selecting covariates.

Hahn, Hirano, and Karlan (2011) consider the design of a two-stage experiment for estimating an average treatment effect, and proposed to select the propensity score that minimizes the asymptotic variance bound for estimating the average treatment effect. Their recommendation is to assign individuals randomly between the treatment and control groups in the second stage, according to the optimized propensity score. They use the covariate information collected in the first stage to compute the optimized propensity score.

Bhattacharya and Dupas (2012) consider the problem of allocating a binary treatment under a budget constraint. Their budget constraint limits what fraction of the population can be treated, and hence is different from our budget constraint. They discuss the costs of using a large number of covariates in the context of treatment assignment.

McKenzie (2012) demonstrates that taking multiple measurements of the outcomes after an experiment can improve power under the budget constraint. His choice problem is how to allocate a fixed budget over multiple surveys between a baseline and followups. The main source of the improvement in his case comes from taking repeated measures of outcomes; see Frison and Pocock (1992) for this point in the context of clinical trials. In the set-up of McKenzie (2012), a baseline survey measuring the outcome is especially useful when there is high autocorrelation in outcomes. This would be analogous in our paper to devoting part of the budget to the collection of a baseline covariate, which is highly correlated with the outcome (in this case, the baseline value of the outcome), instead of just selecting a post-treatment sample size that is as large as the budget allows for. In this way, McKenzie (2012) is perhaps closest to our paper in spirit.

In a very recent paper, Dominitz and Manski (2016) proposed the use of statistical decision theory to study allocation of a predetermined budget between two sampling processes of outcomes: a high-cost process of good data quality and a low-cost process with non-response or low-resolution interval measurement of outcomes. Their main concern is data quality between two sampling processes and is distinct from our main focus, namely the simultaneous selection of the set of covariates and the sample size.

# VII Concluding Remarks

We develop data-driven methods for designing a survey in a randomized experiment using information from a pre-existing dataset. Our procedure is optimal in a sense that it minimizes the mean squared error of the average treatment effect estimator, and can handle a large number of potential covariates as well as complex budget constraints faced by the researcher. We have illustrated the usefulness of our approach by showing substantial improvements in precision of the resulting estimator or substantial reductions in the researcher's budget in two empirical applications.

We recognize that there are several other potential reasons guiding the choice of covariates in a survey. These may be as important as the one we focus on, which is the precision of the treatment effect estimator. We show that it is possible and important to develop practical tools to help researchers make such decisions. We regard our paper as part of the broader task of making the research design process more rigorous and transparent.

Some important issues remain as interesting future research topics. First, in principle, one could also consider the optimization of other criteria, e.g., the joint minimization of type-I and type-II errors of a test of the null hypothesis of no-treatment effect. Second, we have assumed that the pre-experimental sample  $S_{pre}$  is large, and therefore the difference between the minimization of the sample average and that of the population expectation is negligible. However, if the sample size of  $S_{pre}$  is small (e.g., in a pilot study), one may be concerned about over-fitting, in the sense of selecting too many covariates. A straightforward solution would be to add a term to the objective function that penalizes a large number of covariates via some information criteria (e.g., the Akaike information criterion (AIC) or the Bayesian information criterion (BIC)).

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# Appendix A: Large-Budget Properties of the Algorithm

In this appendix, we provide non-asymptotic bounds on the empirical risk of the OGA approximation  $\hat{\mathbf{f}} := \mathbf{Z}\hat{\gamma}$ . Following Barron, Cohen, Dahmen, and DeVore (2008), we define

$$||f||_{\mathcal{L}_1^N} := \inf \Big\{ \sum_{k=1}^p |\beta_k|_2 : \beta_k \in \mathbb{R}^{|G_k|} \text{ and } f = \sum_{k=1}^p X'_{G_k} \beta_k \Big\}.$$

When the expression  $f = \sum_{k=1}^{p} X'_{G_k} \beta_k$  is not unique, we take the true f to be one with the minimum value of  $||f||_{\mathcal{L}_1^N}$ . This gives  $f := \gamma'_0 X$  and  $\mathbf{f} := \mathbf{X}\gamma_0$  for some  $\gamma_0$ . Note that  $\mathbf{f}$  is defined by  $\mathbf{X}$  with the true parameter value  $\gamma_0$ , while  $\hat{\mathbf{f}}$  is an OGA estimator of  $\mathbf{f}$  using only  $\mathbf{Z}$ . The following theorem bounds the finite sample approximation to the MSE of the treatment effect estimator

$$\widehat{MSE}_{\hat{n},N}(\hat{\mathbf{f}}) := \|\mathbf{Y} - \hat{\mathbf{f}}\|_N^2 / \hat{n},$$

which is equal to the objective function in (6). Note that  $\widehat{MSE}_{\hat{n},N}(\hat{\mathbf{f}})$  can also be called the "empirical risk".

The following theorem is a modification of Theorem 2.3 of Barron, Cohen, Dahmen, and DeVore (2008). Our result is different from Barron, Cohen, Dahmen, and DeVore (2008) in two respects: (i) we pay explicit attention to the group structure, and (ii) our budget constraint is different from their termination rule.

**Theorem A.1.** Assume that  $(\mathbf{X}'_{G_j}\mathbf{X}_{G_j})/N = \mathbf{I}_{|G_j|}$  for each j = 1, ..., p. Suppose  $\mathcal{N}$  is a finite subset of  $\mathbb{N}_+$ ,  $c : \{0, 1\}^M \times \mathbb{N}_+ \to \mathbb{R}$  some function, and B > 0 some constant. Then the following bound holds:

$$\widehat{MSE}_{\hat{n},N}(\hat{\mathbf{f}}) - \widehat{MSE}_{\hat{n},N}(\mathbf{f}) \le \frac{4\|f\|_{\mathcal{L}^{N}_{1}}^{2}}{\hat{n}} \left(\frac{1}{\min\{p,k_{\hat{n}}\}}\right).$$
(A.1)

The theorem provides a non-asymptotic bound on the empirical risk of the OGA approximation, but the bound also immediately yields asymptotic consistency in the following sense. Suppose  $||f||_{\mathcal{L}_1^N} < \infty$  (Remark A.1 discusses this condition). Then, the empirical risk of  $\hat{\mathbf{f}}$  is asymptotically equivalent to that of the true predictor  $\mathbf{f}$  either if the selected sample size  $\hat{n} \to \infty$  or if both the total number of groups p and the

number of selected groups  $k_{\hat{n}}$  diverge to infinity. Consider, for example, the simple case in which, for a given sample size n, data collection on every covariate incurs the same costs (i.e.,  $\tilde{c}(n)$ ) and each group consists of a single covariate. Then the total data collection costs are equal to the number of covariates selected multiplied by  $\tilde{c}(n)$  (i.e.,  $c(S,n) = \tilde{c}(n) \sum_{j=1}^{M} S_j$ ). Assuming that  $\tilde{c}(n)$  is non-decreasing in n, we then have

$$\frac{1}{\hat{n}\min\{p,k_{\hat{n}}\}} = \frac{1}{\hat{n}\min\{M,\hat{m}\}} = \frac{1}{\hat{n}\min\{M,\lfloor B/\tilde{c}(\hat{n})\rfloor\}},$$

where  $\lfloor x \rfloor$  denotes the largest integer smaller than x. Therefore, we obtain consistency if  $\hat{n}M \to_p \infty$  and  $\hat{n}B/\tilde{c}(\hat{n}) \to_p \infty$ . Continue to assume that  $\tilde{c}(n)$  is increasing in nand  $\mathcal{N}$  contains sample sizes bounded away from zero. Then, both rate conditions are satisfied, for example, as the budget increases,  $B \to \infty$ , and the costs per covariate does not increase faster than linearly in the sample size.<sup>8</sup> Note that consistency can hold irrespectively of whether the number of covariates M is finite or infinite.

Remark A.1. The condition  $||f||_{\mathcal{L}_1^N} < \infty$  is trivially satisfied when p is finite. In the case  $p \to \infty$ , the condition  $||f||_{\mathcal{L}_1^N} < \infty$  requires that not all groups of covariates are equally important in the sense that the coefficients  $\beta_k$ , when their  $\ell_2$  norms are sorted in decreasing order, need to converge to zero fast enough to guarantee that  $\sum_{k=1}^{\infty} |\beta_k|_2 < \infty$ .

Remark A.2. If suitable laws of large numbers apply, we can also replace the condition  $||f||_{\mathcal{L}^N_1} < \infty$  by its population counterpart.

Remark A.3. The minimal sample size  $n_0$  in  $\mathcal{N}$  could, for example, be determined by power calculations (see, e.g. Duflo, Glennerster, and Kremer, 2007; McConnell and Vera-Hernández, 2015) that guarantee a certain power level for an hypothesis test of  $\beta = 0$ .

### Proofs

Proof of Lemma 1. Let  $U_i(\gamma) := Y_i - \gamma' X_i - \beta_0 D_i$ . The homoskedastic error assumption implies that conditional on  $D_1, \ldots, D_n$ , the finite-sample MSE of  $\hat{\beta}(\gamma)$  is

$$\operatorname{Var}\left(\hat{\beta}(\gamma) \mid D_1, \dots, D_n\right)$$

<sup>&</sup>lt;sup>8</sup>In fact, the costs could be allowed to increase with n at any rate as long as  $B \to \infty$  at a faster rate, so that we have  $\hat{n}B/\tilde{c}(\hat{n}) \to_p \infty$ .

$$= \frac{1}{n} \operatorname{Var} \left( U_i(\gamma) \mid D_1, \dots, D_n \right) \left\{ \left( n^{-1} \sum_{i=1}^n D_i \right) \left( 1 - n^{-1} \sum_{i=1}^n D_i \right) \right\}^{-1}$$
  
$$= \frac{1}{n} \operatorname{Var} \left( U_i(\gamma) \mid D_i \right) \left\{ \left( n^{-1} \sum_{i=1}^n D_i \right) \left( 1 - n^{-1} \sum_{i=1}^n D_i \right) \right\}^{-1}$$
  
$$= \frac{1}{n} \operatorname{Var} \left( Y_i - \gamma' X_i \mid D_i = 0 \right) \left\{ \left( n^{-1} \sum_{i=1}^n D_i \right) \left( 1 - n^{-1} \sum_{i=1}^n D_i \right) \right\}^{-1}.$$
  
Q.E.D.

Proof of Theorem A.1. This theorem can be proved by arguments similar to those used in the proof of Theorem 2.3 in Barron, Cohen, Dahmen, and DeVore (2008). In the subsequent arguments, we fix n and leave indexing by n implicit.

First, letting  $\hat{\mathbf{r}}_{k-1,i}$  denote the *i*th component of  $\hat{\mathbf{r}}_{k-1}$ , we have

$$\begin{aligned} \|\hat{\mathbf{r}}_{k-1}\|_{N}^{2} &= N^{-1} \sum_{i=1}^{N} \hat{\mathbf{r}}_{k-1,i} Y_{i} \\ &= N^{-1} \sum_{i=1}^{N} \hat{\mathbf{r}}_{k-1,i} U_{i} + N^{-1} \sum_{i=1}^{N} \hat{\mathbf{r}}_{k-1,i} \sum_{j=1}^{\infty} X'_{G_{j},i} \beta_{j} \\ &\leq \|\hat{\mathbf{r}}_{k-1}\|_{N} \left\| \mathbf{Y} - \sum_{k=1}^{\infty} \mathbf{X}'_{G_{k}} \beta_{k} \right\|_{N} + \left[ \sum_{j=1}^{\infty} |\beta_{j}|_{2} \right] N^{-1} |\hat{\mathbf{r}}'_{k-1} \mathbf{X}_{G_{k}}|_{2} \\ &\leq \frac{1}{2} \left( \|\hat{\mathbf{r}}_{k-1}\|_{N}^{2} + \left\| \mathbf{Y} - \sum_{k=1}^{\infty} \mathbf{X}'_{G_{k}} \beta_{k} \right\|_{N}^{2} \right) + \left[ \sum_{j=1}^{\infty} |\beta_{j}|_{2} \right] N^{-1} |\hat{\mathbf{r}}'_{k-1} \mathbf{X}_{G_{k}}|_{2}, \end{aligned}$$

which implies that

$$\|\hat{\mathbf{r}}_{k-1}\|_{N}^{2} - \left\|\mathbf{Y} - \sum_{k=1}^{\infty} \mathbf{X}_{G_{k}}^{\prime} \beta_{k}\right\|_{N}^{2} \le 2 \left[\sum_{j=1}^{\infty} |\beta_{j}|_{2}\right] N^{-1} |\hat{\mathbf{r}}_{k-1}^{\prime} \mathbf{X}_{G_{k}}|_{2}.$$
 (A.2)

Note that if the left-hand side of (A.2) is negative for some  $k = k_0$ , then the conclusion of the theorem follows immediately for all  $m \ge k_0 - 1$ . Hence, we assume that the left-hand side of (A.2) is positive, implying that

$$\left(\|\hat{\mathbf{r}}_{k-1}\|_{N}^{2} - \left\|\mathbf{Y} - \sum_{k=1}^{\infty} \mathbf{X}_{G_{k}}^{\prime} \beta_{k}\right\|_{N}^{2}\right)^{2} \leq 4 \left[\sum_{j=1}^{\infty} |\beta_{j}|_{2}\right]^{2} N^{-2} |\hat{\mathbf{r}}_{k-1}^{\prime} \mathbf{X}_{G_{k}}|_{2}^{2}.$$
 (A.3)

Let  $P_k$  denote the projection matrix  $P_k := \mathbf{X}_{G_k} (\mathbf{X}'_{G_k} \mathbf{X}_{G_k})^{-1} \mathbf{X}'_{G_k} = N^{-1} \mathbf{X}_{G_k} \mathbf{X}'_{G_k}$ 

where the second equality comes from the assumption that  $(\mathbf{X}'_{G_k}\mathbf{X}_{G_k})/N = \mathbf{I}_{|G_k|}$ . Hence, it follows from the fact that  $P_k$  is the projection matrix that

$$\|\hat{\mathbf{r}}_{k-1} - P_k \hat{\mathbf{r}}_{k-1}\|_N^2 = \|\hat{\mathbf{r}}_{k-1}\|_N^2 - \|P_k \hat{\mathbf{r}}_{k-1}\|_N^2.$$
(A.4)

Because  $\hat{\mathbf{r}}_k$  is the best approximation to  $\mathbf{Y}$  from  $\hat{\mathcal{I}}_{n,k}$ , we have

$$\|\hat{\mathbf{r}}_{k}\|_{N}^{2} \leq \|\hat{\mathbf{r}}_{k-1} - P_{k}\hat{\mathbf{r}}_{k-1}\|_{N}^{2}.$$
(A.5)

Combining (A.5) with (A.4) and using the fact that  $P_k^2 = P_k$ , we have

$$\begin{aligned} \|\hat{\mathbf{r}}_{k}\|_{N}^{2} &\leq \|\hat{\mathbf{r}}_{k-1}\|_{N}^{2} - \|P_{k}\hat{\mathbf{r}}_{k-1}\|_{N}^{2} \\ &= \|\hat{\mathbf{r}}_{k-1}\|_{N}^{2} - \|N^{-1}\mathbf{X}_{G_{k}}\mathbf{X}_{G_{k}}'\hat{\mathbf{r}}_{k-1}\|_{N}^{2} \\ &= \|\hat{\mathbf{r}}_{k-1}\|_{N}^{2} - N^{-2}|\hat{\mathbf{r}}_{k-1}'\mathbf{X}_{G_{k}}|_{2}^{2}, \end{aligned}$$
(A.6)

Now, combining (A.6) and (A.3) together yields

$$\|\hat{\mathbf{r}}_{k}\|_{N}^{2} \leq \|\hat{\mathbf{r}}_{k-1}\|_{N}^{2} - \frac{1}{4} \Big(\|\hat{\mathbf{r}}_{k-1}\|_{N}^{2} - \left\|\mathbf{Y} - \sum_{k=1}^{\infty} \mathbf{X}_{G_{k}}^{\prime}\beta_{k}\right\|_{N}^{2} \Big)^{2} \Big[\sum_{j=1}^{\infty} |\beta_{j}|_{2}\Big]^{-2}.$$
(A.7)

As in the proof of Theorem 2.3 in Barron, Cohen, Dahmen, and DeVore (2008), let  $a_k := \|\hat{\mathbf{r}}_k\|_N^2 - \|\mathbf{Y} - \sum_{k=1}^{\infty} \mathbf{X}'_{G_k} \beta_k\|_N^2$ . Then (A.7) can be rewritten as

$$a_k \le a_{k-1} \left( 1 - \frac{a_{k-1}}{4} \left[ \sum_{j=1}^{\infty} |\beta_j|_2 \right]^{-2} \right).$$
 (A.8)

Then the induction method used in the proof of Theorem 2.1 in Barron, Cohen, Dahmen, and DeVore (2008) gives the desired result, provided that  $a_1 \leq 4 [\sum_{j=1}^{\infty} |\beta_j|_2]^2$ . As discussed at the end of the proof of Theorem 2.3 in Barron, Cohen, Dahmen, and DeVore (2008), the initial condition is satisfied if  $a_0 \leq 4 [\sum_{j=1}^{\infty} |\beta_j|_2]^2$ . If not, we have that  $a_0 > 4 [\sum_{j=1}^{\infty} |\beta_j|_2]^2$ , which implies that  $a_1 < 0$  by (A.8). Hence, in this case, we have that  $\|\hat{\mathbf{r}}_1\|_N^2 \leq \|\mathbf{Y} - \sum_{k=1}^{\infty} \mathbf{X}'_{G_k} \beta_k\|_N^2$  for which there is nothing else to prove.

Then, we have proved that the error of the group OGA satisfies

$$\|\hat{\mathbf{r}}_m\|_N^2 \le \left\|\mathbf{Y} - \sum_{k=1}^p \mathbf{X}'_{G_k}\beta_k\right\|_N^2 + \frac{4}{m} \left[\sum_{j=1}^p |\beta_j|_2\right]^2, \ m = 1, 2, \dots$$

Equivalently, we have, for any  $n \in \mathcal{N}$  and any  $k \ge 1$ ,

$$\|\mathbf{Y} - \hat{\mathbf{f}}_{n,k}\|_N^2 - \|\mathbf{Y} - \mathbf{f}\|_N^2 \le \frac{4\|f\|_{\mathcal{L}_1^N}^2}{k}.$$

Because  $\mathcal{N}$  is a finite set, the desired result immediately follows by substituting in the definition of  $\hat{\mathbf{f}}$  and  $k_{\hat{n}}$ . Q.E.D.

## Appendix B: Cost Functions Used in Section V

In this appendix, we provide detailed descriptions of the cost functions used in Section V.

## Calibration of the Cost Function in Section V.A

Here, we give a detailed description of components of the cost function used in Section V.A.

• Administration costs. The administration costs in the survey were R\$10,000 and the average survey took two hours per household to conduct (i.e., T(S) = 120 measured in minutes). Therefore,

$$c_{\text{admin}}(S,n) = \phi(120)^{\alpha} = 10,000.$$

If we assume that, say,  $\alpha = 0.4$  (which means that the costs of 60 minutes are about 75.8 percent of the costs of 120 minutes), we obtain  $\phi \approx 1,473$ .

• Training costs. The training costs in the survey were R\$25,000, that is,

$$c_{\text{train}}(S,n) = \kappa(1,466) \cdot 120 = 25,000,$$

so that  $\kappa(1, 466) \approx 208$ . It is reasonable to assume that there exists some lumpiness in the training costs. For example, there could be some indivisibility in hotel rooms that are rented, and in the number of trainers required for each training

session. To reflect this lumpiness, we assume that

$$\kappa(n) = \begin{cases} 150 & \text{if} \quad 0 < n \le 1,400\\ 208 & \text{if} \quad 1,400 < n \le 3,000\\ 250 & \text{if} \quad 3,000 < n \le 4,500\\ 300 & \text{if} \quad 4,500 < n \le 6,000\\ 350 & \text{if} \quad 6,000 < n \end{cases}$$

Note that, in this specification,  $\kappa(1,466) \approx 208$ , as calculated above. We take this as a point of departure to calibrate  $\kappa(n)$ . Increases in sample size n are likely to translated into increases in the required number of field workers for the survey, which in turn lead to higher training costs. Our experience in the field (based on running surveys in different settings, and on looking at different budgets for different versions of this same survey) suggests that, in our example, there is some concavity in this cost function, because an increase in the sample size, in principle, will not require a proportional increase in the number of interviewers, and an increase in the number of interviewers will probably require a less than proportion increase in training costs. For example, we assume that a large increase in the size of the sample, from 1,500 to 6,000, leads to an increase in  $\kappa(n)$  from 208 to 300 (i.e., an increase in overall training costs of about 50 percent).

• Interview costs. Interview costs were R\$630,000, accounting for the majority of the total survey costs, that is,

$$c_{\text{interv}}(S, n) = 1,466 \cdot \eta + 1,466 \cdot p \cdot 120 = 630,000,$$

so that  $\eta + 120p \approx 429.74$ . The costs of traveling to each household in this survey were approximately half of the total costs of each interview. If we choose  $\eta = 200$ , then the fixed costs  $\eta$  amount to about 47 percent of the total interview costs, which is consistent with the actual costs of the survey. Then we obtain the price per unit of survey time as  $p \approx 1.91$ . It is also reasonable to assume that half of the variable costs per individual are due to the collection of the three outcomes in the survey, because their administration was quite lengthy. The costs of collecting the outcomes could also be seen as fixed costs (equal to  $0.955 \times 120 = 114.6$ ), which means that the price per unit of survey time for each of the remaining covariates is about 0.955. In sum, we can rewrite interview costs as

 $c_{\text{interv}}(S,n) = 1,466 \times (200 + 114.6) + 1,466 \times 0.955 \times 120 = 630,000.$ 

- Price per covariate. We treat the sample obtained from the original experiment as  $S_{\text{pre}}$ , a pilot study or the first wave of a data collection process, based on which we want to decide which covariates and what sample size to collect in the next wave. We perform the selection procedure for each outcome variable separately, and thus adjust  $T(S) = \tau(1 + \sum_{j=1}^{M} S_j)$ . For simplicity, we assume that to ask each question on the questionnaire takes the same time, so that  $\tau_0 = \tau_j = \tau$ for every question; therefore,  $T(S) = \tau(1 + \sum_{j=1}^{M} S_j) = 120$ . Note that we set  $\tau_0 = \tau$  here, but the high costs of collecting the outcome variables are reflected in the specification of  $\eta$  above. This results in  $\tau = 120/(1 + \sum_{j=1}^{M} S_j)$ . The actual number of covariates collected in the experiment was 40; so  $\sum_{j=1}^{M} S_j = 40$ , and thus  $\tau \approx 3$ .
- Rescaled budget. Because we use only a subsample of the original experimental sample, we also scale down the original budget of R\$665,000 down to R\$569,074, which corresponds to the costs of selecting all 36 covariates in the subsample; that is,  $c(\mathbf{1}, 1, 330)$  where  $\mathbf{1}$  is a 36-dimensional vector of ones and c(S, n) is the calibrated cost function.

### Calibration of the Cost Function in Section V.B

Here, we present a detailed description of components of the cost function used in Section V.B.

• Administration costs. The administration costs for the low- and high-cost covariates were estimated to be about \$5,000 and \$24,000, respectively. The high-cost covariates were four tests that took about 15 minutes each (i.e.,  $T_{\text{high}}(S) = 60$ ). For the low-cost covariates (teacher and principal survey), the total survey time was around 60 minutes, so  $T_{\text{low}}(S) = 60$ . High- and low-cost variables were collected by two different sets of enumerators, with different levels of training and skills. Therefore,

$$\phi_{\text{low}}(60)^{\alpha_{\text{low}}} = 5,000$$
 and  $\phi_{\text{high}}(60)^{\alpha_{\text{high}}} = 24,000.$ 

If we assume that, say,  $\alpha_{\text{low}} = \alpha_{\text{high}} = 0.7$ , we obtain  $\phi_{\text{low}} \approx 285$  and  $\phi_{\text{high}} \approx 1,366$ .

• Training costs.  $\mu_{\text{high}}$  and  $\mu_{\text{low}}$  are the numbers of enumerators collecting highand low-cost variables, respectively. The training costs for enumerators in the high and low groups increase by 20 for each set of additional 20 low-cost enumerators, and by 12 for each set of 4 high-cost enumerators:

$$\kappa_{\text{low}}(c, n_c) := 20 \sum_{k=1}^{19} k \cdot \mathbb{1} \{ 20(k-1) < \mu_{\text{low}}(c, n_c) \le 20k \}$$

and

$$\kappa_{\text{high}}(c, n_c) := 12 \sum_{k=1}^{17} k \cdot \mathbb{1}\{4(k-1) < \mu_{\text{high}}(c, n_c) \le 4k\}.$$

This is reasonable because enumerators for low-cost variables can be trained in large groups (i.e., groups of 20), while enumerators for high-cost variables need to be trained in small groups (i.e., groups of 4). However, training a larger group demands a larger room, and, in our experience, more time in the room. The lumpiness comes from the costs of hotel rooms and the time of the trainers. The numbers 20 and 12 as the average costs of each cluster of enumerators were chosen based on our experience with this survey (even if the design of the training and the organization of the survey was not exactly the same as the stylized version presented here), and reflect both the time of the trainer and the costs of hotel rooms for each type of enumerators. Because the low-cost variables are questionnaires administered to principals and teachers, in principle the number of required enumerators only depends on c (i.e.,  $\mu_{\text{low}}(c, n_c) = \lfloor \lambda_{\text{low}} c \rfloor$ ). Highcost variables are collected from students, and therefore the number of required enumerators should depend on c and  $n_c$ , so  $\mu_{\text{high}}(c, n_c) = |\lambda_{\text{high}} c \mu_{n,\text{high}}(n_c)|$ . We assume that the latter increases again in steps, in this case of 10 individuals per cluster, that is,

$$\mu_{n,\text{high}}(n_c) := \sum_{k=1}^7 k \cdot \mathbb{1}\{10(k-1) < n_c \le 10k\}.$$

We let  $\lambda_{\text{low}} = 0.14$  (capturing the idea that one interviewer could do about seven schools) and  $\lambda_{\text{high}} = 0.019$  (capturing the idea that one enumerator could perhaps work with about 50 children). The training costs in the survey were \$1,600 for

the low-cost group of covariates and \$1,600 for the high-cost group of covariates.

• Interview costs. We estimate that interview costs in the survey were \$150,000 and \$10,000 for the high- and low-cost variables, respectively, i.e.

$$\psi_{\text{low}}(350)\eta_{\text{low}} + 350 \cdot p_{\text{low}} \cdot 60 = 10,000$$

and

$$\psi_{\text{high}}(350, 24)\eta_{\text{high}} + 350 \cdot 24p_{\text{high}} \cdot 60 = 150,000.$$

We set  $\psi_{\text{low}}(c) = \mu_{\text{low}}(c)$  and  $\psi_{\text{high}}(c, n_c) = \mu_{\text{high}}(c, n_c)$ , the number of required enumerators for the two groups, so that  $\eta_{\text{low}}$  and  $\eta_{\text{high}}$  can be interpreted as fixed costs per enumerator. From the specification of  $\mu_{\text{low}}(c)$  and  $\mu_{\text{high}}(c, n_c)$  above, we obtain  $\mu_{\text{low}}(350) = 50$  and  $\mu_{\text{high}}(350, 24) = 20$ . The fixed costs in the survey were about  $\psi_{\text{low}}(350)\eta_{\text{low}} = 500$  and  $\psi_{\text{high}}(350, 24)\eta_{\text{high}} = 1,000$  for low- and highcost covariates. Therefore,  $\eta_{\text{low}} = 500/50 = 10$  and  $\eta_{\text{high}} = 1,000/20 = 50$ . Finally, we can solve for the prices  $p_{\text{low}} = (10,000 - 500)/(350 \times 60) \approx 0.45$  and  $p_{\text{high}} = (150,000 - 1,000)/(350 \times 24 \times 60) \approx 0.3$ .

- Price per covariate. For simplicity, we assume that to ask each low-cost question takes the same time, so that  $\tau_j = \tau_{\text{low}}$  for every low-cost question (i.e.,  $j = 1, \ldots, M_{\text{low}}$ ), and that each high-cost question takes the same time (i.e.,  $\tau_j = \tau_{\text{high}}$ ) for all  $j = M_{\text{low}} + 1, \ldots, M$ . The experimental budget contains funding for the collection of one outcome variable, the high-cost test results at follow-up, and three high-cost covariates at baseline. We modify  $T_{\text{high}}(S)$  accordingly:  $T_{\text{high}}(S) = \tau_{\text{high}}(1 + \sum_{j=M_{\text{low}}+1}^{M} S_j) = 4\tau_{\text{high}}$  so that  $\tau_{\text{high}} = 60/4 = 15$ . Similarly, originally there were 255 low-cost covariates, which leads to  $\tau_{\text{low}} = 120/255 \approx 0.47$ .
- Rescaled budget. As in the previous subsection, we use only a subsample of the original experimental sample. Therefore, we scale down the original budget to the amount that corresponds to the costs of collecting all covariates used in the subsample. As a consequence, the rescaled budget is \$25,338 in the case of baseline outcomes and \$33,281 in the case of the follow-up outcomes.

## Appendix C: A Simple Formulation of the Problem

#### Uniform Cost per Covariate

Take the following simple example where: (1) all covariates are orthogonal to each other; (2) all covariates have the same price, and the budget constraint is just B = nk, where n is sample size and k is the number of covariates. Order the covariates by the contribution to the MSE, so that the problem is to choose the first k covariates (and the corresponding n).

Define  $\sigma^2(k) = (1/N) \sum_{i=1}^{N} (Y_i - \gamma'_{0,k}X_i)^2$ , where  $\gamma_{0,k}$  is the same as the vector of true coefficients  $\gamma_0$  except that all coefficients after the (k+1)th coefficient are set to be zeros, and let  $MSE(k,n) = (1/n)\sigma^2(k)$ . For the convenience of using simple calculus, suppose that k is continuous, ignoring that k is a positive integer, and that  $\sigma^2(k)$  is twice continuously differentiable. This would be a reasonable first-order approximation when there are a large number of covariates, which is our set-up in the paper. Because we ordered the covariates by the magnitude of their contribution to a reduction in the MSE, we have  $\partial \sigma^2(k)/\partial k < 0$ , and  $\partial^2 \sigma^2(k)/\partial k^2 > 0$ .

The problem we solve in this case is just

$$\min_{n,k} \frac{1}{n} \sigma^2(k) \quad \text{s.t.} \quad nk \le B.$$

Assume we have an interior solution and that n is also continuous. Replace the budget constraint in the objective function and we obtain

$$\min_{n,k} \frac{k}{B} \sigma^2(k)$$

This means that k is determined by

$$\sigma^2(k) + k \frac{\partial \sigma^2(k)}{\partial k} = 0,$$

or

$$\frac{\sigma^2(k)}{k} + \frac{\partial \sigma^2(k)}{\partial k} = 0, \tag{C.1}$$

which in this particular case does not depend on B. Then, n is given by the budget constraint (i.e., n = B/k).

Another way to see where this condition comes from is just to start from the budget

constraint. If we want to always satisfy it then, starting from a particular choice of n and k yields

$$n \cdot dk + k \cdot dn = 0,$$

or

$$\frac{dn}{dk} = -\frac{n}{k}.$$

Now, suppose we want to see what happens when k increases by a small amount. In that case, keeping n fixed, the objective function falls by

$$\frac{1}{n}\frac{\partial\sigma^2(k)}{\partial k}dk.$$

This is the marginal benefit of increasing k. However, n cannot stay fixed, and needs to decrease by (n/k)dk to keep the budget constraint satisfied. This means that the objective function will increase by

$$\left(-\frac{1}{n^2}\right)\sigma^2\left(k\right)\left(-\frac{n}{k}\right)dk$$

This is the marginal cost of increasing k.

At the optimum, in an interior solution, marginal costs and marginal benefits need to balance out, so

$$\frac{1}{nk}\sigma^{2}\left(k\right)dk = -\frac{1}{n}\frac{\partial\sigma^{2}\left(k\right)}{\partial k}dk$$

or

$$\frac{\sigma^{2}(k)}{k} + \frac{\partial\sigma^{2}(k)}{\partial k} = 0,$$

which reproduces (C.1).

There are a few things to notice in this simple example.

- (1) The marginal costs of an increase in k are increasing in  $\sigma^2(k)$ . This is because increases in n are more important role for the MSE when  $\sigma^2(k)$  is large than when it is small.
- (2) The marginal costs of an increase in k are decreasing in k. This is because when k is large, adding an additional covariate does not cost much in terms of reductions in n.
- (3) A large n affects the costs and benefits of increasing k in similar way. Having a large n reduces benefits of additional covariates because it dilutes the decrease in

 $\sigma^2(k)$ . Then, on one hand, it increases costs through the budget constraint, as a larger reduction in n is needed to compensate for the same change in k. However, on the other hand, it reduces costs, because when n is large, a particular reduction in n makes much less difference for the MSE than in the case where n is small.

(4) We can rewrite this condition as

$$\frac{1}{k} + \frac{\partial \sigma^2(k)/\partial k}{\sigma^2(k)} = 0,$$

where the term  $(\partial \sigma^2(k)/\partial k)/\sigma^2(k)$  is the percentage change in the unexplained variance from an increase in k.

If we combine

$$\frac{dn}{n} = \frac{dk}{k},$$

which comes from the budget constraint, and

$$\frac{1}{MSE\left(n,k\right)}\frac{\partial MSE\left(n,k\right)}{\partial n}=-\frac{1}{n},$$

we notice that the percentage decrease in MSE from an increase in n is just (dn)/n, the percentage change in n, which in turn is just equal to (dk)/k. So what the condition above says is that we want to equate the percentage change in the unexplained variance from a change in k to the percentage change in the MSE from the corresponding change in n.

Perhaps even more interesting is to notice that k is the survey cost per individual in this very simple example. Then this condition says that we want to choose k to equate the percentage change in the survey costs per individual ((dk)/k) to the percentage change in the residual variance

$$\frac{\partial \sigma^2(k)/\partial k}{\sigma^2\left(k\right)}dk.$$

This condition explicitly links the impacts of k on the survey costs and on the reduction in the MSE.

Adding fixed costs F of visiting each individual is both useful and easy in this very simple framework. Suppose there are a fixed costs F of going to each individual, so the budget constraint is n(F + k) = B. Proceeding as above, we can rewrite our problem as

$$\min_{n,k} \frac{F'+k}{B} \sigma^2(k) \,.$$

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This means that k is determined by

$$\sigma^{2}(k) + (F+k)\frac{\partial\sigma^{2}(k)}{\partial k} = 0,$$

or

$$\frac{1}{F+k} + \frac{\partial \sigma^2(k)/\partial k}{\sigma^2(k)} = 0.$$

Note that, when there are large fixed costs of visiting each individual, increasing k is not going to be that costly at the margin. It makes it much easier to pick a positive k. However, other than that, the main lessons (1)–(4) of this simple model remain unchanged.

#### Variable Cost per Covariate

If covariates do not have uniform costs, then the problem is much more complicated. Consider again a simple set-up where all the regressors are orthogonal, and we order them by their contribution to the MSE. However, suppose that the magnitude of each covariate's contribution the MSE takes a discrete finite number of values. Let  $\mathcal{R}$  denote the set of these discrete values. Let r denote an element of  $\mathcal{R}$  and  $R = |\mathcal{R}|$  (the total number of all elements in  $\mathcal{R}$ ). There are many potential covariates within each r group, each with a different price p. The support of p could be different for each r. So, within each r, we will then order variables by p. The problem will be to determine the optimal k for each r group. Let  $\mathbf{k} \equiv \{k_r : r \in \mathcal{R}\}$ .

The problem is

$$\min_{n,\mathbf{k}} \frac{1}{n} \sigma^2(\mathbf{k}) \quad \text{s.t.} \sum_{r \in \mathcal{R}} c_r(k_r) \le B,$$

where  $c_r(k_r) = \sum_{l=1}^{k_r} p_l$  are the costs of variables of type r used in the survey. We can also write it as  $c_r(k_r) = p_r(k_r) k_r$ , where  $p_r(k_r) = (\sum_{l=1}^{k_r} p_l)/k_r$ . Because we order the variables by price (from low to high),  $\partial p_r(k_r) / \partial k_r > 0$ . Let  $\sigma_r^2 = \partial \sigma^2(\mathbf{k}) / \partial k_r$ , which is a constant (this is what defines a group of variables).

Then, assume we can approximate  $p_l(k_r)$  by a continuous function and that we have an interior solution. Then, substituting the budget constraint in the objective function:

$$\min_{n,\mathbf{k}} \frac{1}{B} \left[ \sum_{r \in \mathcal{R}} c_r(k_r) \right] \sigma^2(\mathbf{k}) \, .$$

From the first-order condition for  $k_r$ ,

$$\frac{\partial c_r \left(k_r\right)}{\partial k_r} \sigma^2 \left(\mathbf{k}\right) + \left[\sum_{r \in \mathcal{R}} c_r(k_r)\right] \frac{\partial \sigma^2 \left(\mathbf{k}\right)}{\partial k_r} = 0,$$
$$\frac{\partial c_r \left(k_r\right) / \partial k_r}{\sum_{r \in \mathcal{R}} c_r(k_r)} = -\frac{\partial \sigma^2 \left(\mathbf{k}\right) / \partial k_r}{\sigma^2 \left(\mathbf{k}\right)}.$$

or

What this says is that, for each r, we choose variables up to the point where the percent marginal contribution of the additional variable to the residual variance equals the percent marginal contribution of the additional variable to the costs per interview, just as in the previous subsection.

## **Appendix D: Simulations**

In this appendix, we study the finite sample behavior of our proposed data collection procedure, and compare its performance to other variable selection methods. We consider the linear model from above,  $Y = \gamma' X + \varepsilon$ , and mimic the data-generating process in the day-care application of Section V.A with the cognitive test outcome variable.

First, we use the dataset to regress Y on X. Call the regression coefficients  $\hat{\gamma}_{emp}$  and the residual variance  $\hat{\sigma}_{emp}^2$ . Then, we regress Y on the treatment indicator to estimate the treatment effect  $\hat{\beta}_{emp} = 0.18656$ . We use these three estimates to generate Monte Carlo samples as follows. For the pre-experimental data  $S_{pre}$ , we resample X from the empirical distribution of the M = 36 covariates in the dataset and generate outcome variables by  $Y = \gamma' X + \varepsilon$ , where  $\varepsilon \sim N(0, \hat{\sigma}_{emp}^2)$  and

$$\gamma = \hat{\gamma}_{\rm emp} + \frac{1}{2} {\rm sign}(\hat{\gamma}_{\rm emp}) \kappa \bar{\gamma}.$$

We vary the scaling parameter  $\kappa \in \{0, 0.3, 0.7, 1\}$  and  $\bar{\gamma} := (\bar{\gamma}_1, \dots, \bar{\gamma}_{36})'$  is specified in three different fashions, as follows:

• "lin-sparse", where the first five coefficients linearly decrease from 3 to 1, and all others are zero, that is,

$$\bar{\gamma}_k := \begin{cases} 3 - 2(k-1)/5, & 1 \le k \le 5\\ 0, & \text{otherwise} \end{cases};$$

• "lin-exp", where the first five coefficients linearly decrease from 3 to 1, and the remaining decay exponentially, that is,

$$\bar{\gamma}_k := \begin{cases} 3 - 2(k-1)/5, & 1 \le k \le 5\\ e^{-k}, & k > 5 \end{cases};$$

• "exp", where exponential decay  $\bar{\gamma}_k := 10e^{-k}$ .

When  $\kappa = 0$ , the regression coefficients  $\gamma$  are equal to those in the empirical application. When  $\kappa > 0$ , we add one of the three specifications of  $\bar{\gamma}$  to the coefficients found in the dataset, thereby increasing (in absolute value) the first few coefficients<sup>9</sup>

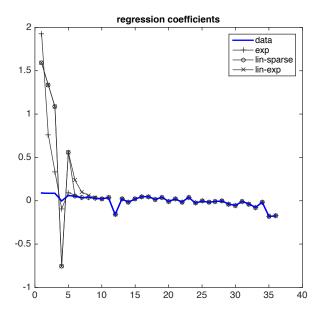


Figure 1: Regression coefficients in the simulation when  $\kappa = 0.3$ 

<sup>&</sup>lt;sup>9</sup>Because all estimated coefficients in the dataset ( $\hat{\gamma}_{emp}$ ) are close to zero and roughly of the same magnitude, we simply pick the first five covariates that have the highest correlation with the outcome variable.

more than the others, and thus increasing the importance of the corresponding regressors for prediction of the outcome. Figure 1 displays the regression coefficients in the dataset (i.e., when  $\kappa = 0$ , denoted by the blue line labeled "data"), and  $\gamma$  for the three different specifications when  $\kappa = 0.3$ .

For each Monte Carlo sample from  $S_{pre}$ , we apply the OGA, LASSO, and POST-LASSO methods, as explained in Section V.A. The cost function and budget are specified exactly as in the empirical application. We store the sample size and covariate selection produced by each of the three procedures, and then mimic the randomized experiment  $S_{exp}$  by first drawing a new sample of X from the same data-generating process as in  $S_{pre}$ . Then we generate random treatment indicators D, so that outcomes are determined by

$$Y = \hat{\beta}_{\rm emp} D + \gamma' X + \varepsilon,$$

where  $\varepsilon$  is randomly drawn from  $N(0, \hat{\sigma}_{emp}^2)$ . We then compute the treatment effect estimator  $\hat{\beta}$  of  $\beta$  as described in Step 4 of Section II.

The results are based on 500 Monte Carlo samples, N = 1,330, which is the sample size in the dataset, and  $\mathcal{N}$  a fine grid from 500 to 4,000. All covariates, those in the dataset as well as the simulated ones, are studentized so that their variance is equal to one.

For the different specifications of  $\bar{\gamma}$ , Tables D.1–D.3 report the selected sample size  $(\hat{n})$ , the selected number of covariates  $(|\hat{I}|)$ , the ratio of costs for that selection divided by the budget B, the square root of the estimated MSE,  $\sqrt{\widehat{MSE}_{\hat{n},N}(\hat{\mathbf{f}})}$ , the bias and standard deviation of the estimated average treatment effect  $(bias(\hat{\beta}) \text{ and } sd(\hat{\beta}))$ , and the RMSE of  $\hat{\beta}$  across the Monte Carlo samples of the experiment.

Overall, all three methods perform similarly well across different designs and the number of selected covariates tends to increase as  $\kappa$  becomes large. No single method dominates other methods, although POST-LASSO seems to perform slightly better than LASSO. In view of the Monte Carlo results, we argue that the empirical findings reported in Section V.A are likely to result from the lack of highly predictive covariates in the empirical example.

# Appendix E: Variables Selected in the School Grants Example

Scale	Scale Method	'n	$ \hat{I} $	Cost/B	$\sqrt{\widehat{MSE}}_{\hat{n},N}(\hat{\mathbf{f}})$	$bias(\hat{eta})$	$sd(\hat{eta})$	$\mathrm{RMSE}(\hat{\beta})$	EQB
0	Experiment	1,330	36		0.02498	-0.0034284	0.049981	0.050048	\$56,9074
	OGA	2,508	1.4	0.99543	0.019249	0.00034598	0.038838	0.038801	\$34,8586
	LASSO	2,587	0.1	0.99278	0.019418	0.0020874	0.039372	0.039388	\$35,6781
	POST-LASSO	2,529	1.0	0.99457	0.019222	0.00069394	0.037758	0.037727	\$35,1659
0.3	Experiment	1,330	36	1	0.02494	0.00036992	0.049501	0.049453	\$56,9074
	OGA	2,350	3.9	0.99443	0.019751	0.0013905	0.038275	0.038262	\$37,7076
	LASSO	2,228	5.9	0.988	0.020346	-0.00093089	0.041713	0.041682	\$39,3017
	POST-LASSO	2,320	4.4	0.99321	0.019696	-0.0020751	0.038746	0.038763	\$37,1730
0.7	Experiment	1,330	36	<del>, -</del> 1	0.024953	-0.00086563	0.050992	0.050948	\$56,9074
	OGA	2,346	4.0	0.99433	0.020552	-0.0020151	0.041475	0.041483	\$39,7722
	LASSO	2,218	6.1	0.98747	0.021145	0.00057516	0.043957	0.043917	\$42,3971
	POST-LASSO	2,246	5.7	0.98929	0.020177	0.0019693	0.042683	0.042686	\$38,7095
H	Experiment	1,330	36	<del>, -</del> 1	0.024938	-0.0021535	0.051146	0.05114	\$56,9074
	OGA	2,346	4.0	0.99433	0.021566	0.00044162	0.043389	0.043348	\$43,8536
	LASSO	2,172	6.9	0.98513	0.021383	-0.00058106	0.045378	0.045336	\$43,1589
	POST-LASSO	2,172	6.9	0.98513	0.019956	-0.0048726	0.040967	0.041215	\$38,0053

Table D.1: Simulation results: lin-sparse

Scale	Scale Method	ŷ	Ĵ	Cost/B	$\sqrt{\widehat{MSE}_{\hat{n},N}(\hat{\mathbf{f}})}$	$bias(\hat{eta})$	$sd(\hat{eta})$	$RMSE(\hat{\beta})$	EQB
0	Experiment	1,330	36		0.024965	0.0027033	0.051564	0.051583	\$569,074
	OGA	2,509	1.3	0.99541	0.019249	-0.00042961	0.03723	0.037195	\$348,682
	$\mathbf{LASSO}$	2,588	0.1	0.99275	0.01941	-0.003374	0.03845	0.03856	357,261
	POST-LASSO	2,530	1.0	0.9946	0.019215	0.00076956	0.037924	0.037894	\$351,755
0.3	Experiment	1,330	36	Η	0.02492	-0.0015645	0.049457	0.049432	\$569,074
	OGA	2,343	4.0	0.99421	0.019868	-0.0014349	0.040197	0.040182	\$379,540
	LASSO	2,186	6.7	0.98569	0.020652	0.0019377	0.04084	0.040845	\$403,004
	POST-LASSO	2,313	4.5	0.99288	0.019816	-0.0025812	0.039587	0.039631	\$377,876
0.7	Experiment	1,330	36	Η	0.024936	0.0041527	0.050436	0.050556	\$569,074
	OGA	2,301	4.7	0.99247	0.020805	-0.0017267	0.041303	0.041297	\$408,990
	LASSO	2,134	7.7	0.98551	0.02162	-0.00071182	0.042716	0.042679	\$440,232
	POST-LASSO	2,206	6.5	0.98955	0.020522	0.0013055	0.043358	0.043334	\$400,219
<del>,</del> 1	Experiment	1,330	36	1	0.024964	-0.0034064	0.049484	0.049551	\$569,074
	OGA	2,286	5.0	0.99187	0.021874	-0.0025106	0.042304	0.042336	\$451,756
	$\mathbf{LASSO}$	2,080	9.0	0.98793	0.021987	-0.0015746	0.044218	0.044201	\$454,765
	POST-LASSO	2,078	9.0	0.98787	0.020374	0.00077488	0.041977	0.041942	\$396,218

Table D.2: Simulation results: lin-exp

Scale	Scale Method	$\hat{n}$	Î	Cost/B	$\sqrt{\widehat{MSE}}_{\hat{n},N}(\hat{\mathbf{f}})$	$bias(\hat{eta})$	$sd(\hat{eta})$	$RMSE(\hat{\beta})$	EQB
0	Experiment	1,330	36		0.024953	0.00083077	0.054043	0.053996	\$569,074
	OGA	2,511	1.3	0.99538	0.019234	0.0016616	0.037237	0.037236	\$348,426
	LASSO	2,588	0.1	0.99278	0.019394	-0.00049328	0.038849	0.038813	\$356,941
	POST-LASSO	2,529	1.0	0.99452	0.019203	-0.00044404	0.039549	0.039512	\$351,403
0.3	Experiment	1,330	36		0.024947	-0.00089522	0.051246	0.051202	\$569,074
	OGA	2,411	2.9	0.99605	0.019426	0.0016951	0.038729	0.038727	\$359,950
	LASSO	2,291	4.9	0.9911	0.020184	-0.0022094	0.040243	0.040263	\$389,560
	POST-LASSO	2,380	3.5	0.99514	0.019377	0.0014552	0.039996	0.039982	\$359,662
0.7	Experiment	1,330	36		0.024946	-0.0012694	0.050947	0.050912	\$569,074
	OGA	2,408	3.0	0.99605	0.019457	0.0015399	0.040789	0.040778	\$362, 287
	LASSO	2,279	5.1	0.99039	0.020233	0.0011166	0.042491	0.042463	\$391,128
	POST-LASSO	2,376	3.5	0.99515	0.019405	-0.0023208	0.037252	0.037287	\$361,903
	Experiment	1,330	36		0.024948	-0.0034014	0.051898	0.051957	\$569,074
	OGA	2,407	3.0	0.99603	0.019494	0.0022031	0.038846	0.038869	\$364,015
	LASSO	2,271	5.2	0.99008	0.020298	0.0016393	0.039024	0.039019	\$392,857
	POST-LASSO	2,377	3.5	0.99516	0.019448	-0.00085645	0.039135	0.039106	\$363,023

Table D.3: Simulation results: exp

Table E.1: School grants (outcome: math test): selected covariates in panel (a) of Table 3

OGA	LASSO	POST-LASSO
Child is male	Child is male	Child is male
Village pop.	Dist. to Dakar	Dist. to Dakar
Piped water	Dist. to city	Dist. to city
Teach-stud	Village pop.	Village pop.
No. computers	Piped water	Piped water
Req. (h) teach. qual.	No. computers	No. computers
Req. (h) teach. att.	Req. (h) teach-stud	Req. (h) teach-stud
Obs. (h) manuals	Hrs. tutoring	Hrs. tutoring
Books acq. last yr.	Books acq. last yr.	Books acq. last yr.
Any parent transfer	Provis. struct.	Provis. struct.
Teacher bacc. plus	NGO cash cont.	NGO cash cont.
Teach. train. math	Any parent transfer	Any parent transfer
Obst. (t) class size	NGO promised cash	NGO promised cash
Measure. equip.	Avg. teach. exp.	Avg. teach. exp.
	Teacher bacc. plus	Teacher bacc. plus
	Obs. (t) student will.	Obs. (t) student will
	Obst. (t) class size	Obst. (t) class size
	Silence kids	Silence kids

Table E.2: Definition of variables in Table E.1

Variable	Definition
Child is male	Male student
Village pop.	Size of the population in the village
Piped water	School has access to piped water
Teach-stud	Teacher–student ratio in the school
No. computers	Number of computers in the school
Req. (h) teach. qual.	Principal believes teacher quality is a major requirement
	for school success
Req. (h) teach. att.	Principal believes teacher attendance is a major requirement
	for school success
Obs. (h) manuals	Principal believes the lack of manuals is a major obstacle
	to school success
Books acq. last yr.	Number of manuals acquired last year
Any parent transfer	Cash contributions from parents
Teacher bacc. plus	Teacher has at least a baccalaureate degree
Teach. train. math	Teacher received special training in math
Obst. (t) class size	Teacher believes class size is a major obstacle to school succes
Measure. equip.	There is measurement equipment in the classroom
Dist. to Dakar	Distance to Dakar
Dist. to city	Distance to the nearest city
Req. (h) teach–stud	Principal believe teacher-student ratio is a major requirement
- ( )	for school success
Hrs. tutoring	Hours of tutoring by teachers
Provis. struct.	Number of provisional structures in school
NGO cash cont.	Cash contributions by NGO
NGO promised cash	Promised cash contributions by NGO
Avg. teach. exp.	Average experience of teachers in the school
Obst. (t) student will.	Teacher believes the lack of student willpower is one of the
	main obstacles to learning in the school
Obst. (t) class size	Teacher believes the lack of classroom size is one of the main
× /	obstacles to learning in the school
Silence kids	Teacher has to silence kids frequently