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Yue, Xiao-Guang; Cao, Yong; McAleer, Michael

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From Disorder to Order

Xiao-Guang Yue¹ Yong Cao² Michael McAleer³

¹ Wuhan University, Wuhan, China;

² Southwest Forestry University, Kunming, China;

³ National Tsing Hua University, Taiwan; Erasmus School of Economics, Erasmus University Rotterdam, Tinbergen Institute, the Netherlands; Complutense University of Madrid, Spain.

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Tel.: +31(0)20 525 1600

Tinbergen Institute Rotterdam Burg. Oudlaan 50 3062 PA Rotterdam The Netherlands

Tel.: +31(0)10 408 8900 Fax: +31(0)10 408 9031

From Disorder to Order*

Xiao-Guang Yue

Department of Engineering Management School of Civil Engineering Wuhan University Wuhan, China

Yong Cao**

Department of Computer Science School of Computer and Information Southwest Forestry University Kunming, China

Michael McAleer

Department of Quantitative Finance
National Tsing Hua University, Taiwan
and
Econometric Institute
Erasmus School of Economics
Erasmus University Rotterdam
and
Tinbergen Institute
The Netherlands
and
Department of Quantitative Economics
Complutense University of Madrid

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^{**} Corresponding author: Yong Cao (842836263@qq.com)

Abstract

In the physical sciences, order and disorder refer to the presence or absence of some

symmetry or correlation in a many-particle system. It follows that it is important to

examine whether there is any regularity hidden in the phase transition of the disorder-

order relationship. In this paper a series of experiments are devised and executed to

reveal the power law relationship between order and disorder, and to determine that the

power law is indeed an important regular pattern in the phase transition from disorder

to order.

Keywords: Order, disorder, power law, scale invariance, symmetry, regularity,

physical sciences.

JEL: C12, C18, C92.

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1. Introduction

In the physical sciences, order and disorder refer to the presence or absence of some symmetry or correlation in a many-particle system. Order is a necessary condition for any issue that the human mind might wish to understand. Arrangements such as the layout of a city or building, a set of tools, a display of merchandise, the verbal exposition of facts or ideas, or a painting or piece of music, are called orderly when an observer or listener can grasp their overall structure and the ramification of the structure in some detail.

Order makes it possible to focus on what is alike and what is different, what belongs together, and what should be separated. When nothing superfluous is included and nothing indispensable is omitted, one can understand the interrelation of the whole and its parts, as well as the hierarchical scale of importance and power by which some structural features are dominant, and others are subordinate. The perceivable order tends to be manifested and understood as a reflection of an underlying order, whether physical, social, or cognitive.

Disorder means a physical condition in which there is a disturbance of normal functioning, a condition in which things are not in their expected places, or a disturbance of the peace or of public order. In fact, the term disorder, when used by physicists in this connection, is intended to mean that the single elements, with which the statistical approach operates, behave independently from one another. For example, thermal movement and white noise are manifestations of disorder.

Scientists have researched order and disorder for millennia. Physicists defined entropy as the quantitative measure of the degree of disorder in a system. In information theory, entropy is also a measure of unpredictability of information content. There exist

interesting problems of what a regular pattern relationship might be between disorder and order, and what mechanism might underlie the transition from disorder to order.

Biological systems are typically heterogeneous as individuals vary in their characteristics, their response to the external environment, and to each other. Ariel, Rimer and Ben-Jacob examined the effect of heterogeneity in the context of the well-known scalar noise model. This model shows numerically that the system undergoes a phase transition between an ordered phase at low temperature/high density, and a disordered phase at high temperature/low density [1].

Woloszyn, Stauffer and Kulakowski investigated the network model of community by Watts, Dodds and Newman as a hierarchy of groups [2]. They used Glauber dynamics to investigate the order-disorder transition, and found the transition temperature. The results provided a mathematical illustration of the social ability to a collective action via weak ties, as discussed in Granovetter in 1973 [3].

Lorinczi, Georgii and Lukkarinen investigated the continuum q-Potts model at its transition point from the disordered to the ordered regime. They argued that the occurrence of phase transition can be seen as a percolation in the related random cluster representation, and argued that the occurrence of a phase transition can be seen as percolation in the related random cluster representation [4].

Symbolic sequences have been analysed for an extended period in many areas, including physics, biology, information science, economics, and linguistics. There is an old saying in many cultures that says if billions of monkeys were to have tapped keyboards for billions of years, they are very likely to have written a Shakespearean masterpiece, or maybe even the Bible. This implies there are some discernible patterns in the phase from disorder to order.

This paper designs an experiment-based method about symbolic sequences to research

the regularity between order and disorder. About 128 students are asked to play monkeys to continue to tap keyboards thousands of times, and a power law is found in these experiments. It seems that a power law is indeed an emerging pattern from disorder to order.

The outline of the paper is as follows. Section 2 describes the power law. Section 3 describes a series of experiments to reveal the regular patterns in the phase from disorder to order, and obtains the experimental results. Section 4 draws a conclusion that the power law is an important regular pattern that can be determined in the transition from disorder to order.

2. Power Law

Some classical distributions, such as the normal distribution, can be characterized by the mean and variance, but not all distributions are as straightforward to characterize. Among others, the power law has attracted particular attention over the years for its mathematical properties, which sometimes lead to surprising physical consequences, and for its appearance in a diverse range of natural and artificial phenomena.

The populations of cities, the intensities of earthquakes, volcanic activity and tsunami, and the sizes of power outages, for example, are all viewed as having power law distributions. Quantities such as these are not well characterized by their typical or average values [5]. The power law describes the objects as self-similar under some change in scale, either strictly, or statistically.

Mathematically, a quantity x obeys a power law if it is drawn from a probability distribution:

$$p(x) \propto x$$
, (1)

namely a power law is a relationship between two scalar variables, x and y = p(x), which can be written as follows:

$$p(x) = C \cdot x^{\alpha}, \tag{2}$$

where C is the constant of proportionality and α is the exponent of the power law. Such a power law relationship shows as a straight line on a logarithmic graph as a logarithmic transformation of both sides of equation (2) is equivalent to:

$$\log p(x) = \alpha \log(x) + \log C, \tag{3}$$

which has the same form as the equation for a straight line:

$$Y = \alpha X + C \tag{4}$$

The equation $p(x) = C \cdot x^{\alpha}$ has a property that relative scale change $p(sx)/p(x) = s^{\alpha}$ is independent of x. In this sense, p(x) lacks a characteristic scale. The constant α is an unknown exponent or scaling parameter of the distribution, and is scale invariant. As α and C are unknown constants, in practice they would be estimated from available data using standard estimation methods such as least squares..

3. A Regular Pattern Between Order and Disorder

Consider allowing students to play the above mentioned monkeys and ask them to continue to tap keyboards arbitrarily. The input random character sequence represents the disorder state, and the words that appear in the input sequence imply the order state.

Any regularity between order and disorder can be analysed, with the experiments

devised as follows:

- First, 128 students are asked to randomly tap the keyboard to input letters, and each student inputs 6000 letters arbitrarily.
- Next the words in an electronic Oxford dictionary (more than 30000) are input to a text file, and they are split by tab key in order that regular expression methods can be applied easily.
- Then the number of words (according to the above text file of the Oxford dictionary), which appear in the input random character sequences of 2, 4, 8, 16, ..., 128 students will be counted.
- Finally, it can be determined whether a regular pattern such as a power law is found.

Of course, the power law requires varied scales. Here 2, 4, 8, ..., 128 represent the nth power of 2 (n = 1, 2, 3, ..., 7), and they are varied scales in the power law. The little corner of one input random character sequence is shown in following Fig.1. The text file of the electronic Oxford dictionary is shown in Figure 2. The number of words (according to the above text file of Oxford dictionary) appearing in input random character sequences of students is shown in Figure 3.

ylxqeqsxbvghbtvdzajmtmihqsgh ptmfcuwnopizxcdfndobqxzwzsjb gpmfjwtvvnoqqnthalffrsllfklu myqfkitzaixpmmfhkwuvctxnyxue qgvxrjfatsaraiulblrzutslqwlq mtlethebkizszhevegiuwsoellzc hwfiddhuwatsegjdjyxdpqanpdbq fuvwdbpuucmsqrccsgoptbkkihxl nijpvfpbwhcxjzlcifzumzshsmtw eilasuotcfxhmzbfkbuiehqfxptb

Figure 1

Part of one input random character sequence and the total of sequences is 128

a	AA	AAA	AB	aback			
abashed	abate	abatemen	nt	abattoir			
abdicate		abdication abdomen					
abeam	aberrant	t	aberrati	on			
abiding		ability					
able	ably	able-boo	died	ablution			
abnormal		Abo	aboard	abode			
abominably		Abominable Snowman					
aborigine		abort	aborted				
about	above	abracada	abra	abrade			

Figure 2

Text file of Oxford dictionary which includes words that occur more than 30000 times.

abut	1	ace	3	add	10
aft	11	after	1	ago	2
aid	59	aide	2	ail	15
air	19	ajar	1	aka	37
alas	3	album	1	ale	24
alp	6	am	153	and	64
ant	6	anus	1	any	6

Figure 3

Number of words that appear in the input random character sequences

Then the number of words appearing in input random character sequences of 2, 4, ..., 64, 128 students, respectively, are counted. Next the logarithm of the number of the input random sequences, the logarithm of the number of words appearing in random sequences (if the word appears repeatedly, it will be counted only once), and the logarithm of the cumulative number of words appearing in random sequences (if the word appears repeatedly, the cumulative number will be counted) are computed. The results are shown in Table.1.

Table 1

Logarithm of input random sequence number, number of words appearing and cumulative number of words appearing

Number of input sequences	2	4	8	16	32	64	128
Logarithm of input sequence number	1	2	3	4	5	6	7
The number of words appearing	365	432	499	688	865	1175	1714
Logarithm of number of words appearing	8.51	8.75	8.96	9.43	9.76	10.20	10.74
Cumulative number of words appearing	1713	4073	7601	15837	33711	58057	124385
Logarithm of cumulative number of words appearing	10.74	11.99	12.89	13.95	15.04	15.83	16.92

We select 2 as a scale and take account of $N(\epsilon)$, which is the number of words appearing in the input random sequences. Then we change the scale with the nth power of 2 (n = 2, 3, ..., 7) to obtain a new $N(\epsilon)$, and repeat the above steps to obtain a series of ϵ - $N(\epsilon)$ pairs. Then we treat the ϵ - $N(\epsilon)$ pair of series as a point in the logarithmic coordinate, and draw a $\log \epsilon$ - $\log N(\epsilon)$ chart to analyze the data.

It can be seen that the logarithmic points are almost in a straight line in Figure 4. The relationships between the number, cumulative number of words appearing and the number of input random sequences follow a power law. However, the logarithmic relationship between the cumulative number of words appearing and the number of input sequences fits the power law more accurately.

Next we count the number and the cumulative number of 2-, 3-, 4- and 5-letter words appearing in input random sequences, and obtain the new logarithmic relationships, which are shown in Figures 5-8.

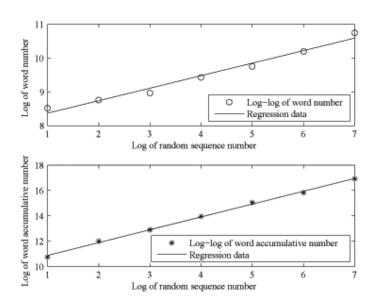


Figure 4
Logarithmic number of input random sequences.

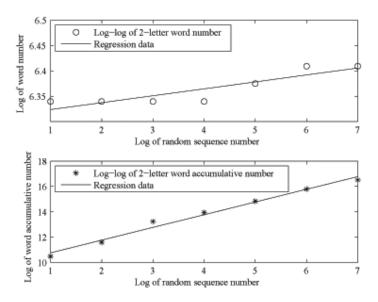


Figure 5

Logarithmic relationships between the number and the accumulative number of 2-letter appearing words and the number of input random sequences.

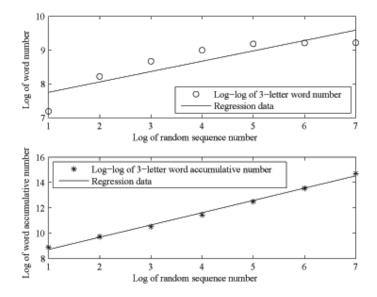


Figure 6

Logarithmic relationships between the number and the cumulative number of 3-letter words and the number of input random sequences.

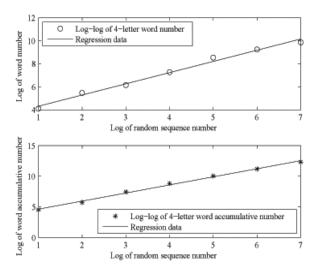


Figure 7

Logarithmic relationships between the number and the cumulative number of 4-letter words and the number of input random sequences

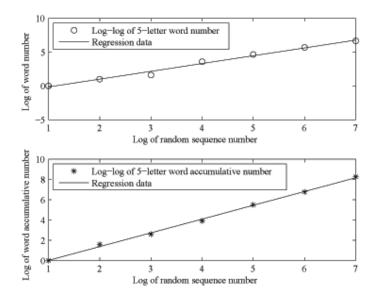


Figure 8

Logarithmic relationships between the number and the cumulative number of 5-letter words and the number of input random sequences.

Table 2
The respective power law exponent and coefficient C of 2-, 3-, 4- and 5-letter words, namely the slope and the intercept of a log-log relationship in Figures 5-8

Number of letters in the word	2	3	4	5
Exponent α of power law	1.0026	0.9679	1.3179	1.3583
Coefficient C of power law	866.17	214.30	9.92	0.39

It can be seen that the relationships between the number of the input random sequences and the number of 2-, 3-, 4- and 5-letter words appearing (if the word occurs repeatedly, we count it only once) do not follow the power law well. However, the relationships between the number of the input random sequences and the cumulative number of 2-, 3-, 4- and 5-letter words appearing (if the word occurs repeatedly, we count the number of occurrences) follow power law very well. It follows that the power law is an important regular pattern between order and disorder. The respective power law exponent α and coefficient C of 2-, 3-, 4- and 5-letter words are shown in Table.2.

4. Conclusion

The study of power laws spans many scientific disciplines, including physics, biology, engineering, computer science, earth sciences, economics, political science, sociology, and statistics. In this paper we devised and executed a series of experiments to reveal power law regularities between order and disorder, and obtained some experimental results. We counted the number of the input random character sequences and the accumulative number of words appearing in the input random sequences, and found that they follow the power law rather well.

The experimental results showed that the power law is indeed an important regular pattern in the phase transition procedure from disorder to order. The mechanism underlying the power law requires further research in the future.

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