Markert, Viola; Zimmermann, Heinz

Working Paper
The Relationship between Risk-Premium and Convenience-Yield Models

WWZ Working Paper, No. 19/07

Provided in Cooperation with:
Center of Business and Economics (WWZ), University of Basel

Suggested Citation: Markert, Viola; Zimmermann, Heinz (2007) : The Relationship between Risk-Premium and Convenience-Yield Models, WWZ Working Paper, No. 19/07, University of Basel, Center of Business and Economics (WWZ), Basel

This Version is available at:
http://hdl.handle.net/10419/123384

Terms of use:
Documents in EconStor may be saved and copied for your personal and scholarly purposes.

You are not to copy documents for public or commercial purposes, to exhibit the documents publicly, to make them publicly available on the internet, or to distribute or otherwise use the documents in public.

If the documents have been made available under an Open Content Licence (especially Creative Commons Licences), you may exercise further usage rights as specified in the indicated licence.
The Relationship between Risk-Premium and Convenience-Yield Models

WWZ Summary 19/07

Viola Markert, Heinz Zimmermann
CHAPTER XYZ

THE RELATIONSHIP BETWEEN RISK-PREMIUM AND
CONVENIENCE-YIELD MODELS

VIOLA MARKERT
DR. OEC. HSG, MANAGING DIRECTOR
CYD RESEARCH GMBH

HEINZ ZIMMERMANN
PROFESSOR OF FINANCE
WIRTSCHAFTSWISSENSCHAFTLICHES ZENTRUM WWZ
UNIVERSITY OF BASEL

Name: Dr. Viola Markert, Managing Director of CYD Research GmbH in Basel
Postal address: CYD Research GmbH, Bäumleingasse 10, CH-4051 Basel
Telephone number: +41 (0)79 263 39 26 (home), +41 (0)61 228 74 70 (work)
Email: viola.markert@cyd-research.com
Fax: +41 (0)61 228 74 71

Name: Prof. Dr. Heinz Zimmermann, Professor of Finance, University of Basel
Postal address: University of Basel, Department of Finance, Holbeinstrasse 12, CH-4051 Basel
Telephone number: +41 (0)61 267 33 16 (work)
Email: heinz.zimmermann@unibas.ch
Fax: +41 (0)61 267 08 98
SUMMARY

Arbitrage pricing cannot be applied to commodity futures because the physical commodity does not represent a pure asset: Since consumption and processing of the commodity can drive down inventories to zero, it is not always possible to construct a replicating portfolio for the futures contract, and commodity spot prices do not (fully) reflect price expectations and risk premiums.

The two alternative valuation principles for commodity futures are risk premium model (RPM) and convenience-yield model (CYM). Risk-premium models derive futures prices from expected commodity spot prices at maturity, and convenience-yield models derive futures prices from the current commodity spot price.

The chapter shows that the two valuation principles are mutually consistent if convenience yields are regarded as the deviation of the commodity spot price from its asset value (the present value of the expected commodity spot price at maturity). By combining risk-premium models and convenience-yield models, it can be shown that convenience yields reflect the proportion of the expected change in commodity spot prices which is not attributable to the risk premium and the riskfree rate (i.e. to the quasi asset value of the commodity).

All relationships are summarized in Exhibit 7.
The relationship between futures returns and convenience yields, or the term structure respectively, is of particular interest. Can futures returns be predicted based on the term structure or convenience yields? At first sight, equations (12a) and (12b) seem to suggest such a relationship. But it has been shown that convenience yields only reflect the temporary "consumption value" of the commodity and are, in general, independent from the expected risk premium. Again, convenience yields reflect the expected change in commodity spot prices which is not driven by the risk premium or the cost of carry. The same interpretation should be applied to roll returns, because they differ from (storage cost adjusted) convenience yields by the riskfree rate. Therefore, average roll yields reflect the expected deviation of the spot price change from the risk premium.

Our empirical illustrations confirm this view: The futures term structure, convenience yields and roll returns largely anticipate subsequent spot price changes. However, a small portion of roll returns, is not compensated by subsequent spot price changes, and could be explained time-varying risk premiums conditional on roll returns and expected spot price changes. This requires more detailed analysis.
### Exhibit 7 Summary

<table>
<thead>
<tr>
<th>Term Structure</th>
<th>Futures Returns</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \ln \frac{F_{t,T_2}}{F_{t,T_1}} )</td>
<td>( \tilde{r}_{F,t,t+1,T} )</td>
</tr>
<tr>
<td><strong>Risk Premium Model</strong></td>
<td><strong>Convenience Yield Model</strong></td>
</tr>
<tr>
<td>( \hat{\alpha}_S^C (t, T_1, T_2) - rp(T_2 - T_1) )</td>
<td>( - \frac{[r + m - cy]}{\sigma} + \tilde{r}_{S,t,t+1}^C )</td>
</tr>
<tr>
<td><strong>Relationship</strong></td>
<td><strong>Relationship</strong></td>
</tr>
<tr>
<td>( \hat{\alpha}_S^C (t, T_1, T_2) = \frac{[r + rp + m - cy]}{\sigma}(T_2 - T_1) )</td>
<td>( \tilde{\Delta} \ln E_{t,t+1,T} = -[r + rp + m - cy] + \tilde{r}_{S,t,t+1}^C )</td>
</tr>
<tr>
<td>( E_t[\tilde{\Delta} \ln E_{t,t+1,T}] = -[r + rp + m - cy] + E_t[\tilde{r}_{S,t,t+1}^C] )</td>
<td>( = -\frac{1}{2}\sigma^2 )</td>
</tr>
</tbody>
</table>

For \( T_1 = t + 1, \ T_2 = T \):

\[
\hat{\alpha}_S^C (t, t+1, T) = \left( E_t[\tilde{r}_{S,t,t+1}^C] + \frac{1}{2}\sigma^2 \right)(T - t - 1)
\]