

A Service of



Leibniz-Informationszentrum Wirtschaft Leibniz Information Centre

Xepapadeas, Anastasios; Vardas, Giannis

Working Paper

Uncertainty Aversion, Robust Control and Asset Holdings

Nota di Lavoro, No. 66.2004

Provided in Cooperation with:

Fondazione Eni Enrico Mattei (FEEM)

Suggested Citation: Xepapadeas, Anastasios; Vardas, Giannis (2004): Uncertainty Aversion, Robust Control and Asset Holdings, Nota di Lavoro, No. 66.2004, Fondazione Eni Enrico Mattei (FEEM), Milano

This Version is available at: https://hdl.handle.net/10419/117940

Standard-Nutzungsbedingungen:

Die Dokumente auf EconStor dürfen zu eigenen wissenschaftlichen Zwecken und zum Privatgebrauch gespeichert und kopiert werden.

Sie dürfen die Dokumente nicht für öffentliche oder kommerzielle Zwecke vervielfältigen, öffentlich ausstellen, öffentlich zugänglich machen, vertreiben oder anderweitig nutzen.

Sofern die Verfasser die Dokumente unter Open-Content-Lizenzen (insbesondere CC-Lizenzen) zur Verfügung gestellt haben sollten, gelten abweichend von diesen Nutzungsbedingungen die in der dort genannten Lizenz gewährten Nutzungsrechte.

Terms of use:

Documents in EconStor may be saved and copied for your personal and scholarly purposes.

You are not to copy documents for public or commercial purposes, to exhibit the documents publicly, to make them publicly available on the internet, or to distribute or otherwise use the documents in public.

If the documents have been made available under an Open Content Licence (especially Creative Commons Licences), you may exercise further usage rights as specified in the indicated licence.



Uncertainty Aversion, Robust Control and Asset Holdings

Giannis Vardas and Anastasios Xepapadeas

NOTA DI LAVORO 66.2004

APRIL 2004

ETA - Economic Theory and Applications

Giannis Vardas and Anastasios Xepapadeas, Department of Economics, University of Crete

This paper can be downloaded without charge at:

The Fondazione Eni Enrico Mattei Note di Lavoro Series Index: http://www.feem.it/Feem/Pub/Publications/WPapers/default.htm

Social Science Research Network Electronic Paper Collection: http://ssrn.com/abstract=XXXXXX

The opinions expressed in this paper do not necessarily reflect the position of Fondazione Eni Enrico Mattei

Uncertainty Aversion, Robust Control and Asset Holdings

Summary

Optimal portfolio rules are derived under uncertainty aversion by formulating the portfolio choice problem as a robust control problem. The robust portfolio rule indicates that the total holdings of risky assets as a proportion of the investor's wealth could increase as compared to the holdings under the Merton rule, which is the standard risk aversion case. With two risky assets an increase in the holdings of the one risky asset is accompanied by a reduction in the holdings of the other asset. Furthermore, in the optimal robust portfolio the investor may increase the holdings of the asset for which there is or less ambiguity, and reduce the holding of the asset for which there is more ambiguity, a result that might provide an explanation of the home bias puzzle.

Keywords: Uncertainty aversion, Model misspecification, Robust control, Portfolio choice models

JEL Classification: G11, D81

Address for correspondence:

Anastasios Xepapadeas
Department of Economics
University of Crete
University Campus
74 100 Rethymno
Crete
Greece
E-mail: xepapad@econ.soc.uoc.gr

1 Introduction

The assumption that asset prices are generated by a geometric Brownian motion and that consumers-investors know the associated true probability law has been central in the analysis of portfolio choice models (Merton [15], [16]). In economics the assumption that the true probability distribution associated with an event is known, and thus the expected utility framework can be used as a methodological framework, has come under some criticism because of its failure to explain certain "puzzles" such as the observed equity premium puzzle, or the investors home-bias puzzle. In trying to explain these puzzles attention has been focused on the case where the decision maker faces pure uncertainty in the Knightian sense, or ambiguity, and its preference relationship is characterized by uncertainty aversion (Gilboa and Schmeidler [12])

There are two main approaches to the problem of choices when the agent is assumed to be uncertainty averse. In the first, the multiple priors model, the decision maker may formulate his/her objective by attaching a probability, say e, to a baseline prior and a probability (1-e) to the infimum of a family of the disturbed priors around the baseline one. This is the so-called e-contamination approach (Epstein and Wang [9]), which is consistent with uncertainty or ambiguity aversion. In the second approach the agent considers model misspecification. In this approach the decision maker is unsure about his/her model, in the sense that there is a group of approximate models that are also considered as possibly true given a set of finite data. These approximate models are obtained by disturbing a benchmark model, and the admissible disturbances reflect the set of possible probability measures that the decision maker is willing to consider. The resulting problem is one of robust dynamic control, where the objective is to choose a rule that will work under a range of different model specifications. This methodology provides another tractable way to incorporate uncertainty aversion (e.g. Hansen and Sargent, [19], [20], [21], [23], Hansen et al [24]).

Portfolio choice theory has been a prominent area of application of the above approaches² (e.g. Dow and Werlang [5], Epstein and Wang [9], Chen and Epstein [7], Epstein and Miao [8], Uppal and Wang [31], Maenhout [25], Pathak [26], Liu [13], [14]). The idea behind the use of robust control methods in optimal portfolio choice is that the investor faces model uncertainty regarding the assets' price processes. Thus, although the available data used to estimate the probability law characterizing the evolution of asset prices allow for the estima-

¹Chen and Epstein [7], introduce ambiguity aversion to recursive multiple-prior models of utility by considering κ – Ignorance which is a concept that allows differentiation between ambiguous and pure risk cases.

²Monetary policy can be regarded as the initial area of application of these approaches (e.g., Brainard, [1] Hansen and Sargent [23], Onatski and Stock [17], Onatski and Williams [18], Soderstrom [29]). See also Brock and Durlauf [2], Brock, Durlauf and West [3] for similar approaches to policy design and policy evaluation under uncertainty. Another area of interest is environmental and resource management where uncertainty aversion can be used to formulate the concept of the Precautionary Principle (Brock and Xepapadeas [4], Roseta-Palma and Xepapadeas [27])

tion of a benchmark model, there is a set of alternative models describing the evolution of asset prices, which is also consistent with the data and could be regarded as possibly true. In this set up the investor seeks a portfolio rule that will work, in the sense of maximizing utility, under a range of different model specifications of the assets' price equations.

In recent attempts to study Merton's basic optimal portfolio choice problem in the context of the Hansen-Sargent robust control methodology, Maenhout [25] considers a two asset problem, a risky asset and a riskless asset for an investor maximizing a CRRA utility function. The derived robust portfolio rule is an adjusted Merton rule. When there is no preference for robustness, or to put it differently, there is no concern for model misspecification, which implies that the so-called robustness parameter $\theta \to \infty$, this rule tends to Merton's rule. Uppal and Wang [31] extend the problem to the n asset case and derive a generalized robust portfolio rule, which allows for different degrees of robustness associated with different subsets of the asset price process. A central result underlying the recent robust control literature in the portfolio selection context (Maenhout [25], Uppal and Wang [31]) suggests that model uncertainty implies cautiousness in the sense that the investor, under uncertainty aversion, will invest a smaller share of his/her wealth in the risky assets relative to the share implied by the standard Merton rule under risk aversion. In more general terms, model uncertainty seems to have been associated in the earlier literature with some kind of cautious or conservative behavior, ⁴ although more recent results in the area of monetary policy analysis under uncertainty seem to provide mixed findings, that is aggressiveness or robustness depending on the structure of the $\bmod {\rm el.^5}$

The present paper attempts to derive optimal portfolio rules under uncertainty aversion by following Hansen and Sargent's approach and formulating the portfolio choice problem as a robust control problem. We derive portfolio rules for the cases of two and multiple, i=1,...,n, risky assets. We also allow for uncertainty aversion, or preference for robustness, both with respect to the joint distribution of the assets, and, in the general model, with respect to the distribution of each risky asset. Our portfolio rules are parametrized by the robustness parameter θ . We show that as $\theta \to \infty$ the robust portfolio rule tends to Merton's rule in accordance with Maenhout's results. However, under uncertainty aversion, the associated robust portfolio rule indicates that the total holdings of risky assets as a proportion of the investor's wealth is not always

³The robustness parameter θ can be interpreted as the Lagrangian multiplier associated with an entropy constraint, which determines the maximum specification error in the asset price equation that the investor is willing to accept (Hansen and Sargent [21]). As such it is a fixed parameter and characterizes preferences consistent with Gilboa and Schmeidler's axiomatization of uncertainty aversion. When $\theta \to \infty$ there is no concern about model misspecification and we are in the usual risk aversion framework.

⁴For example Brainard's [1] results suggest caution in the face of model uncertainty in a Bayesian framework.

⁵See for example Onatski and Williams [18] and the papers cited by them.

⁶When we allow for different levels of ambiguity associated with different assets, the portfolio rule is parametrized by the vector $\boldsymbol{\theta} = (\theta_1, ..., \theta_n)$.

smaller as compared to the holdings under the Merton rule, which is the risk aversion case, and which is equivalent to no concerns about model misspecification and $\theta \to \infty$. This result seems to depart from the belief that uncertainty, or ambiguity aversion, and the associated robust control methods might result in more cautiousness or conservatism regarding portfolio choices, in the sense that holdings of the "risky - ambiguous" assets are reduced relative to the pure risk case. We derive conditions under which such an increase in the total holdings of risky assets takes place, which are independent of the form of the utility function and the value of the robustness parameter θ . With two risky assets we show that under certain condition uncertainty aversion could induce an increase in the holdings of the one risky asset as compared to risk aversion. When this happens the holding of the other asset is always reduced.

Next we examine the case when the investor has different preferences for robustness for each asset, or different levels of ambiguity regarding each asset. For the multiple asset case we derive again conditions under which the total holdings of assets increase under uncertainty aversion. For the two asset case we show that in the optimal robust portfolio the investor may increase the holdings of the asset for which there is less concern about model misspecification (high θ), or less ambiguity, and reduce the holding of the asset for which there is more concern about model misspecification (low θ), or more ambiguity, relative to the risk aversion case ($\theta = \infty$). If we associate the asset with less ambiguity with home assets and the asset with more ambiguity with foreign assets, this result could be regarded as an additional explanation of the home bias puzzle.

⁷The independence from the value of θ is desirable since θ is basically exogenous. There have been attempts to eliminate θ from the portfolio rule as shown by Pathak [26]. Maenhout's transformation of the robustness parameter θ to a time dependent function, with θ being proportional to the value function of the robust problem portfolio, in order to make the portfolio rule independent of θ , breaks down the consistency of preferences with Gilboa and Schmeidler's axiomatization of uncertainty aversion, and transforms the robust rule to Merton's rule with a lower drift of the asset price equations. Pathak shows also that the Uppal and Wang [31] rule depends on a normalization factor which is taken to be proportional to the value function as in Maenhout's transformation. Pathak [26] avoids the transformation that endogenizes the robustness parameter in terms of the value function by directly determining the worst possible distortion in terms of an instantaneous relative entropy constraint. In this case the robust portfolio problem is simply Merton's problem with a reduced mean return, the reduction defined in terms of the worse possible distortion. (See also Chen and Epstein [7]). It seems that since the exogeneity of θ is required in order for the problem to be consistent with uncertainty aversion, robust portfolios are parametrized by θ . To estimate θ in order to fully characterize the robust portfolio, Hansen and Sargent [19] suggest the use of detection error probabilities.

⁸The extent to which the net result of these two opposite effects will increase or decrease total holdings of risky assets depends on the conditions of the previous result which characterize the behavior of total holdings.

⁹There have been a number of arguments attempting to explain the home bias puzzle. Strong and Xu [30] explain the puzzle on the basis of optimism of fund managers towards their home equity market. Serrat [28] considers nontraded goods to operate as factors that shift the marginal utility of traded goods. This entails dynamic hedging policies which in turn are consistent with the home bias puzzle, while French and Poterba [11] consider information costs as an explanation of the puzzle. Our approach of providing a partial explanation to the puzzle through uncertainty aversion is along the lines of the approach used by Uppal and Wang[31] and Pathak [26].

2 Robust Portfolio Choices

We consider a market which consists of one riskless asset whose price evolves accordingly to:

$$dS(t) = rS(t)dt \qquad S(0) = S_0, \quad t \ge 0,$$

where r denotes the risk-free rate of return, and i = 1, ..., n risky assets. Denoting by $(\alpha_1, \alpha_2, ..., \alpha_n)$ the drift rates, or mean rates of return, and by $(\sigma_1, \sigma_2, ..., \sigma_n)$ the volatility rates, the evolution of the prices $P = [diag(P_1, P_2, ..., P_n)]$ of the n assets, is given by:

$$dP = P\mathcal{A}dt + P\Sigma RdB \tag{1}$$

where \mathcal{A}, Σ , are $n \times n$ diagonal matrices with diagonal elements α_i, σ_i respectively, R^{-10} is a matrix such that $\Sigma R(\Sigma R)^T$ is equal to the variance - covariance matrix and $B = [B_1, B_2, ..., B_n]^{T-11}$ are n independent Brownian processes, defined on an underlying probability space (Ω, \mathcal{F}) , with measure $\mathcal{P} = \mathcal{P}_1 \otimes \mathcal{P}_2 \otimes ... \otimes \mathcal{P}_n$.

Merton's solution ([15], [16]) of the optimal portfolio allocation problem for an infinite time horizon and n risky assets, determines the optimal portfolio weights, w_i , that is the fraction of the investor's total wealth W allocated to asset i as:

$$w_i W = A \sum_{j=1}^n \Upsilon_{ij}^{-1}(\alpha_i - r) \qquad i = 1, ..., n$$

$$A = -\frac{V_W}{V_{WW}} = -\frac{U'(C)}{U''(C)\frac{\partial C}{\partial W}}$$
(2)

where V is the value function of the problem, V_W and V_{WW} are the first and the second partial derivatives respectively with respect to the wealth W, Υ^{-1} is the inverse of the variance - covariance matrix Υ , and U(C) is a standard utility function.

Following Hansen and Sargent [22] and Hansen et al. [24], model (1) is regarded as a benchmark model. If the consumer-investor was sure about the benchmark model, then there would be no concerns about robustness regarding model misspecification. Otherwise, these concerns can be reflected by a family of stochastic perturbations. Because there are n independent Brownian motions, ¹² each one can be perturbed separately, so that:

$$B_i(t) = \hat{B}_i(t) + \int_0^t h_i(s)ds$$
, $i = 1, ..., n$ (3)

where $\{\hat{B}_i(t): t \geq 0\}$ are Brownian motions and $\{h_i(t): t \geq 0\}$ are measurable drift distortions. Therefore the probabilities implied by (1) are distorted. The

 $^{^{10}\}mathrm{A}$ typical element of matrix R can be seen in the next section when we examine the case of two risky assets.

¹¹Superscript T denotes the transpose of a matrix.

¹²This is the reason for the use of the specific form of equation (1).

measure \mathcal{P} is replaced by another probability measure $\mathcal{Q} = \mathcal{Q}_1 \otimes \mathcal{Q}_2, ..., \otimes \mathcal{Q}_n$. As shown by Hansen et al. [24], the discrepancy between the distribution \mathcal{P} and \mathcal{Q} is measured as the relative entropy, $R(\mathcal{Q} \parallel \mathcal{P})$. At this stage we consider distortions to the joint distribution of assets so we impose an overall entropy constraint for all the n assets. Based on Corollary C3.3 of Dupuis and Ellis [6], the entropy constraint becomes:

$$R(\mathcal{Q} \parallel \mathcal{P}) = \sum_{i=1}^{n} R(\mathcal{Q}_i \parallel \mathcal{P}_i) = \sum_{i=1}^{n} \int_{0}^{\infty} e^{-\delta u} \mathbb{E}_{\mathcal{Q}} \left(\frac{h_i^2}{2} \right) du.$$
 (4)

The above equation allows us to consider n separate distortion terms, one for each asset. However in order to reduce the complexity of the model, we initially assume symmetric distorted measures Q_i , and examine the case with the same distortion terms h_i . In this specific case, the equation for wealth dynamics becomes:

$$dW = \left(rW - c + \sum_{i=1}^{n} w_i(\alpha_i - r)W + h \sum_{i=1}^{n} \sigma_i R_{ri} w_i W\right) dt$$

$$+ \sum_{i=1}^{n} \sum_{j=1}^{n} w_j \sigma_j W R_{ij} d\hat{B}_i$$
(5)

where $R_{ri} = \sum_{j=1}^{n} R_{ij}$, is the i^{th} element of the matrix, each of whose elements is equal to the sum of the elements of the ith row of matrix R. Under model misspecification, a multiplier robust control problem can be associated with the problem of maximizing the present value of lifetime expected utility, or:

$$\max_{w_i, C} \mathbb{E}_0 \int_0^\infty e^{-\delta t} U(C) dt \tag{6}$$

In this case the multiplier robust control problem becomes:

$$J(\theta) = \sup_{w_i, C} \inf_{h} \mathbb{E}_{\mathcal{Q}} \int_0^\infty e^{-\delta t} \left[U(C) + \theta_n \frac{h^2}{2} \right] dt$$
 (7)

In the above equation because of (4), $\theta_n = n\theta$ where θ denotes the robustness parameter which takes values greater than or equal to zero. Thus it is assumed that concerns about model misspecification are the same for the price processes of all assets. As shown by Hansen and Sargent [22] θ is the Lagrangian multiplier at the optimum, associated with the entropy constraint $\mathcal{Q}(\tau) = \{Q \in \mathcal{Q} : R_t(\mathcal{Q} \parallel \mathcal{P}) \leq \tau \ \forall t\}$. A value of $\theta = \infty$, indicates that we are absolutely sure about the measure \mathcal{P} , with no preference for robustness. This case can be regarded as the risk aversion case and the problem is reduced to

¹³ For two assets we will see (in the next section) that: $R_{r1} = 1$, $R_{r2} = \rho + \sqrt{1 - \rho^2}$, where ρ is the correlation coefficient.

the standard Merton problem with the objective function given by (6). Lower values for θ indicate preference for robustness under model misspecification, or uncertainty aversion, where a value of $\theta = 0$ indicates that we have no knowledge about the measure \mathcal{P} .

Using the results of Fleming and Souganidis [10] regarding the existence of a recursive solution to the multiplier problem, Hansen et al. [24] show that problem (7) can be transformed into a stochastic infinite horizon two-player game between the investor and Nature. Nature plays the role of a "mean agent" and chooses a reduction h in the mean return of assets to reduce the investor's life time utility. The Bellman-Isaacs conditions for this game implies that the value function $V(W, \theta)$ satisfies the following equation:

$$\delta V = \max_{w_i, C} \min_{h} \left\{ U(C) + \left(rW - c + \sum_{i=1}^{n} w_i (\alpha_i - r) W \right) + h \sum_{i=1}^{n} \sigma_i R_{ri} w_i W \right) V_W + \theta_n \frac{h^2}{2} + \frac{1}{2} V_{WW} \sum_{i=1}^{n} \sum_{j=1}^{n} w_i w_j \sigma_{ij} W^2 \right\}.$$
(8)

The first-order conditions which describe the solution of the above two-player game are:

$$U'(C) = V_W (9)$$

$$h = -\frac{V_W W \sum_{i=1}^n w_i \sigma_i R_{ri}}{\theta_r} \tag{10}$$

$$\sum_{i=1}^{n} w_{j} W \sigma_{ij} = A(\alpha_{i} - r) + A \sigma_{i} R_{ri} h , i = 1, ..., n$$
 (11)

$$A = -\frac{V_W}{V_{WW}} = -\frac{U'(C)}{U''(C)\frac{\partial C}{\partial W}}$$
 (12)

From the above system of equations, it can be seen that as $\theta \to \infty$ the solution reduces to that of Merton's standard problem given by (2). Using (10) to eliminate h from (11), we obtain the robust portfolio weights, or equivalently, the fraction of the wealth invested in each asset, as:

$$w_i^* W = A \sum_{j=1}^n v_{ij}^{-1}(\alpha_j - r) , i = 1, ..., n$$
 (13)

where v^{-1} is the inverse of the matrix:

$$[v_{ij}] = [(\Sigma D \Sigma)_{ij}] \tag{14}$$

$$D_{ij} = \left(\rho_{ij} - \frac{V_W^2}{\theta_n V_{WW}} R_{ri} R_{rj}\right) \tag{15}$$

and ρ_{ij} is the correlation coefficient of the benchmark model, between assets i and j ($\sigma_{ij} = \sigma_i \sigma_j \rho_{ij}$). In order to determine the change in portfolio weights

induced by uncertainty aversion relative to the risk aversion weights, we subtract from (2) the relationship (13) to obtain:¹⁴

$$W(w_i - w_i^*) = W\Delta w_i = A \sum_{j=1}^n [\Sigma^{-1}(\Pi^{-1} - D^{-1})\Sigma^{-1}]_{ij}(\alpha_j - r) , i = 1, ..., n$$
(16)

where $\Pi = RR'$, is the correlation coefficient matrix. If $\Delta w_i \leq 0$, then uncertainty aversion, as reflected in robust control portfolio choices, increases (decreases) the holding of asset i as a fraction of wealth invested in this asset, relative to risk aversion.

The change in the total holdings of risky assets as a fraction of wealth between uncertainty and risk aversion is obtained by using (16) as:

$$W\Delta W = W \sum_{i=1}^{n} \Delta w_i = A \sum_{i=1}^{n} \sum_{j=1}^{n} [\Sigma^{-1} (\Pi^{-1} - D^{-1}) \Sigma^{-1}]_{ij} (\alpha_j - r)$$
 (17)

If $\Delta W \leq 0$, then uncertainty aversion increases (decreases) the total holdings of risky assets i as a fraction of wealth relative to risk aversion.

To derive conditions under which the signs Δw_i , ΔW can be determined and which are relatively simpler to interpret and present, we consider the special case of two risky assets.

2.1 Two Risky Assets

We consider one risk free asset and two correlated risky assets, where ρ denotes the correlation coefficient at the benchmark model. In this case $B = [B_1, B_2]^T$ is a vector of independent Brownian processes defined on an underlying probability space (Ω, \mathcal{F}) , with measure $\mathcal{P} = \mathcal{P}_1 \otimes \mathcal{P}_2$. Because of $\mathbb{E}(dB_1d\hat{B}_2) = \rho dt$, where \mathbb{E} denotes expected value and $dB_1, d\hat{B}_2$ are correlated Brownian motions on $\mathcal{P}_1, \mathcal{P}_2$ respectively, the evolution of the prices of the assets based on (1) is given by:¹⁵

$$dP_1(t) = \alpha_1 P_1(t) dt + \sigma_1 P_1(t) dB_1(t) \qquad t \ge 0 \tag{18}$$

$$dP_2(t) = \alpha_2 P_2(t) dt + \sigma_2 P_2(t) \rho dB_1(t) + \sigma_2 P_2(t) \sqrt{1 - \rho^2} dB_2(t)$$
 (19)

Merton's solution for the maximization problem (6) in the two risky assets

¹⁴For infinitesimal changes in θ , this is basically a comparative statics exercise that characterizes the derivative $\partial w_i^*/\partial \theta$.

¹⁵We have that for independent Brownian motions B_1, B_2 : $\mathbb{E}(dB_1dB_2) = 0$, $\mathbb{E}(dB_1dB_1) = dt$ so we write $d\hat{B}_2 = \rho dB_1 + \sqrt{1 - \rho^2} dB_2$.

case is:

$$w_1 W = \frac{A(\alpha_1 - r)\sigma_2^2}{\sigma_1^2 \sigma_2^2 (1 - \rho_{12}^2)} - \frac{A(\alpha_2 - r)\sigma_{12}}{\sigma_1^2 \sigma_2^2 (1 - \rho_{12}^2)}$$
(20)

$$w_2W = -\frac{A(\alpha_1 - r)\sigma_{12}}{\sigma_1^2\sigma_2^2(1 - \rho_{12}^2)} + \frac{A(\alpha_2 - r)\sigma_2^2}{\sigma_1^2\sigma_2^2(1 - \rho_{12}^2)}$$
(21)

$$A = -\frac{V_W}{V_{WW}} = -\frac{U'(C)}{U''(C)\frac{\partial C}{\partial W}}$$
 (22)

If we perturb each Brownian motion separately, the wealth equation becomes:

$$dW = w_1(\alpha_1 - r + \sigma_1 h)Wdt + w_2(\alpha_2 - r + \sigma_2(\rho h + h\sqrt{1 - \rho^2}))Wdt + (rW - C)dt + W\sigma_1 w_1 d\hat{B}_1 + W\sigma_2 \rho w_2 d\hat{B}_1 + \sigma_2 \sqrt{1 - \rho^2} w_2 d\hat{B}_2.$$
(23)

In this specific case the Bellman equation for problem (7) subject to (23) is:

$$\delta V = \max_{w_i, C} \min_{h} \left\{ U(C) + \left(w_1(\alpha_1 - r + \sigma_1 h)W + (rW - c) + \theta_2 \frac{h^2}{2} + w_2(\alpha_2 - r + \sigma_2(\rho + \sqrt{1 - \rho^2})h)W \right) V_W + \frac{1}{2} V_{WW} \sum_{i=1}^2 \sum_{j=1}^2 w_i w_j \sigma_{ij} W^2 \right\},$$
(24)

where $\theta_2 = 2\theta$ and θ this time refers to the robustness parameter in the two assets case. The first order conditions which describe the solution of the above two-player game are:

$$U'(C) = V_W (25)$$

$$h = -\frac{V_W W \left(\sigma_1 w_1^* + \sigma_2 (\rho + \sqrt{1 - \rho^2}) w_2^*\right)}{\theta_2}$$
 (26)

$$\sum_{j=1}^{2} w_{j}^{*} W \sigma_{1j} = A(\alpha_{1} - r) + A \sigma_{1} h$$
(27)

$$\sum_{j=1}^{2} w_{j}^{*} W \sigma_{2j} = A(\alpha_{2} - r) + A\sigma_{2}(\rho + \sqrt{1 - \rho^{2}})h$$
 (28)

$$A = -\frac{V_W}{V_{WW}} = -\frac{U'(C)}{U''(C)\frac{\partial C}{\partial W}}.$$
 (29)

Using matrix notation the solution of the above problem can be described by the following equation:

$$\begin{bmatrix} w_1^* W & w_2^* W \end{bmatrix} \Lambda = \begin{bmatrix} A(\alpha_1 - r) & A(\alpha_2 - r) \end{bmatrix}$$
 (30)

where.

$$\Lambda = \begin{bmatrix}
\sigma_{11} \left(1 - \frac{V_W^2}{\theta_2 V_{WW}}\right) & \sigma_{12} \left(1 - \frac{V_W^2}{\theta_2 V_{WW}} \frac{\rho + \sqrt{1 - \rho^2}}{\rho}\right) \\
\sigma_{12} \left(1 - \frac{V_W^2}{\theta_2 V_{WW}} \frac{\rho + \sqrt{1 - \rho^2}}{\rho}\right) & \sigma_{22} \left(1 - \frac{V_W^2}{\theta_2 V_{WW}} (1 + 2\rho\sqrt{1 - \rho^2})\right)
\end{bmatrix}. (31)$$

If Σ denotes the diagonal matrix with elements σ_1 , σ_2 then:

$$\Lambda = \Sigma \left[\begin{array}{cc} (1 - \frac{V_W^2}{\theta_2 V_{WW}}) & \left(\rho - \frac{V_W^2}{\theta_2 V_{WW}} (\rho + \sqrt{1 - \rho^2})\right) \\ \left(\rho - \frac{V_W^2}{\theta_2 V_{WW}} (\rho + \sqrt{1 - \rho^2})\right) & \left(1 - \frac{V_W^2}{\theta_2 V_{WW}} (1 + 2\rho\sqrt{1 - \rho^2})\right) \end{array} \right] \Sigma.$$
(32)

Solving the above system we determine the fraction of the wealth invested in the first and second asset under robust portfolio choices as:

$$\begin{bmatrix} w_1^* W & w_2^* W \end{bmatrix} = \frac{1}{(1 - \rho^2) \left(1 - 2\frac{V_W^2}{\theta_2 V_{WW}}\right)} \begin{bmatrix} A(\alpha_1 - r) & A(\alpha_2 - r) \end{bmatrix}$$

$$\Sigma^{-1} \begin{bmatrix} \left(1 - \frac{V_W^2}{\theta_2 V_{WW}} (1 + 2\rho\sqrt{1 - \rho^2}) & -\rho + \frac{V_W^2}{\theta_2 V_{WW}} (\rho + \sqrt{1 - \rho^2}) \\ -\rho + \frac{V_W^2}{\theta_2 V_{WW}} (\rho + \sqrt{1 - \rho^2}) & \left(1 - \frac{V_W^2}{\theta_2 V_{WW}}\right) \end{bmatrix} \Sigma (33)$$

Next we examine, as in the previous section, the changes in the robust portfolio weights $\Delta w_i = w_i - w_i^*$, i = 1, 2 between risk aversion $(\theta \to \infty)$ and uncertainty aversion $(\theta < \infty)$. Using (20),(21),(33) we obtain:

$$\begin{bmatrix} W\Delta w_1 & W\Delta w_2 \end{bmatrix} = \frac{1}{(1-\rho^2)} \begin{bmatrix} A(\alpha_1 - r) & A(\alpha_2 - r) \end{bmatrix} \Sigma^{-1} \Xi \Sigma^{-1}$$
 (34)

where:

$$\Xi = \begin{bmatrix} 1 & -\rho \\ -\rho & 1 \end{bmatrix} - \frac{1}{\left(1 - 2\frac{V_W^2}{\theta_2 V_{WW}}\right)}$$

$$\begin{bmatrix} \left(1 - \frac{V_W^2}{\theta_2 V_{WW}} (1 + 2\rho\sqrt{1 - \rho^2}) & -\rho + \frac{V_W^2}{\theta_2 V_{WW}} (\rho + \sqrt{1 - \rho^2}) \\ -\rho + \frac{V_W^2}{\theta_2 V_{WW}} (\rho + \sqrt{1 - \rho^2}) & \left(1 - \frac{V_W^2}{\theta_2 V_{WW}}\right) \end{bmatrix}$$
(35)

After some manipulations we have that:

$$\begin{bmatrix} W\Delta w_1 & W\Delta w_2 \end{bmatrix} = \tag{36}$$

$$\frac{AV_W^2 \begin{bmatrix} \alpha_1 - r & \alpha_2 - r \end{bmatrix}}{(1 - \rho^2)(\theta_2 V_{WW} - V_W^2)} \Sigma^{-1} \begin{bmatrix} 2\rho\sqrt{1 - \rho^2} - 1 & \rho - \sqrt{1 - \rho^2} \\ \rho - \sqrt{1 - \rho^2} & -1 \end{bmatrix} \Sigma^{-1}.$$

Therefore the solution becomes:

$$W\Delta w_1 = \frac{\kappa}{\sigma_1} \left[\frac{\alpha_1 - r}{\sigma_1} (2\rho\sqrt{1 - \rho^2} - 1) + \frac{\alpha_2 - r}{\sigma_2} (\rho - \sqrt{1 - \rho^2}) \right]$$
(37)

$$W\Delta w_2 = \frac{\kappa}{\sigma_2} \left[\frac{\alpha_1 - r}{\sigma_1} (\rho - \sqrt{1 - \rho^2}) - \frac{\alpha_2 - r}{\sigma_2} \right]$$
(38)

$$\kappa = \frac{AV_W^2}{(1 - \rho^2)(\theta_2 V_{WW} - V_W^2)}. (39)$$

In the above equation, κ is always a negative number, so denoting the relative price of risk by:

$$\lambda = \frac{\frac{\alpha_2 - r}{\sigma_2}}{\frac{\alpha_1 - r}{\sigma_1}} \tag{40}$$

we obtain

$$W\Delta w_1 < 0 \quad \text{if} \quad \frac{\rho - \sqrt{1 - \rho^2}}{1 - 2\rho\sqrt{1 - \rho^2}} > \frac{1}{\lambda}$$
 (41)

$$W\Delta w_2 < 0 \quad \text{if} \quad \rho - \sqrt{1 - \rho^2} > \lambda.$$
 (42)

It can be seen that independent of the specific form of utility function and the value of the robustness parameter θ , the fraction of the wealth invested in the first asset increases relative to Merton's weight if $\frac{\rho-\sqrt{1-\rho^2}}{1-2\rho\sqrt{1-\rho^2}}>\frac{1}{\lambda}$, while the fraction of the wealth invested in the second asset increases relative to Merton's weight if $\rho-\sqrt{1-\rho^2}>\lambda$. If we combine (42) and (41), it can be seen that it is not possible to have:

$$\frac{1 - 2\rho\sqrt{1 - \rho^2}}{\rho - \sqrt{1 - \rho^2}} < \lambda < \rho - \sqrt{1 - \rho^2}.$$
 (43)

So both weights cannot increase at the same time due to uncertainty aversion. If the fraction of the wealth invested in the first asset increases relative to Merton's weight, then the fraction of the wealth invested in the second asset has to decrease relative to Merton's weight. Furthermore, the holdings of both assets decrease relative to Merton's weights if $\rho < \sqrt{2}/2$, thus uncertainty aversion results in an increase in the holdings of one asset for sufficiently high and positive correlation between the two risky assets.

The effect of uncertainty aversion on the total holdings of both risky assets is obtained by combining (41) and (42) as:

$$W\Delta W = W\Delta w_{1} + W\Delta w_{2} =$$

$$\kappa \frac{\alpha_{1} - r}{\sigma_{1}} \frac{1}{\sigma_{2}} \left[(2\rho\sqrt{1 - \rho^{2}} - 1)\sigma + \lambda\sigma(\rho - \sqrt{1 - \rho^{2}}) + \frac{(\rho - \sqrt{1 - \rho^{2}}) - \lambda}{(\rho - \sqrt{1 - \rho^{2}}) - \lambda} \right] < 0 \quad if$$

$$(\lambda\sigma + 1)(\rho - \sqrt{1 - \rho^{2}}) > \lambda + \sigma(1 - 2\rho\sqrt{1 - \rho^{2}})$$

$$\hat{\lambda}(\rho - \sqrt{1 - \rho^{2}} - \frac{1}{\sigma}) > \sigma(1 - 2\rho\sqrt{1 - \rho^{2}}) - (\rho - \sqrt{1 - \rho^{2}})$$

$$\text{with } \hat{\lambda} = \frac{a_{2} - r}{a_{1} - r}, \ \sigma = \frac{\sigma_{2}}{\sigma_{1}}$$

$$(45)$$

If (45) is satisfied then asset holdings increase under uncertainty aversion. These results can be summarized in the following proposition: **Proposition 1** With λ , $\hat{\lambda}$, σ , and ρ as defined above, robust portfolio choices under uncertainty aversion imply, for a market consisting of one riskless and two risky assets, the following:

- 1. If $\hat{\lambda} > \frac{\sigma^2(1-2\rho\sqrt{1-\rho^2})-\sigma(\rho-\sqrt{1-\rho^2})}{\sigma(\rho-\sqrt{1-\rho^2})-1}$, there is an increase in the holdings of risky assets, relative to risk aversion, or $\Delta W < 0$.
- 2. If $\lambda > \frac{1-2\rho\sqrt{1-\rho^2}}{\rho-\sqrt{1-\rho^2}}$, there is an increase in the holdings of the first risky asset, relative to risk aversion, or $\Delta w_1 < 0$.
- 3. If $\lambda < \rho \sqrt{1 \rho^2}$, there is an increase in the holdings of the second risky asset, relative to risk aversion, or $\Delta w_2 < 0$.
- 4. An increase in the holdings of one risky asset under robust portfolio choices implies a reduction in the holdings of the other risky asset.
- 5. When concerns about model misspecification do not exist, or $\theta \to \infty$, then the difference in portfolio choices between uncertainty aversion and risk aversion vanish. $\Delta W \to 0$, $(\Delta w_1, \Delta w_2) \to 0$.
- 6. If $\rho < \sqrt{2}/2$, the holdings of both assets decrease relative to Merton's weights.

Figures 1 and 2 provide a graphical exposition of these results. In figure 1 for parameter constellations such that the value of $\hat{\lambda}$ is above the surface $\phi\left(\sigma,\rho\right)=\frac{\sigma^2(1-2\rho\sqrt{1-\rho^2})-\sigma(\rho-\sqrt{1-\rho^2})}{\sigma\left(\rho-\sqrt{1-\rho^2}\right)-1}$, robust control implies an increase in asset holdings. In figure 2 for parameter constellations such that the value of λ is above the line $\psi\left(\rho\right)=\frac{1-2\rho\sqrt{1-\rho^2}}{\rho-\sqrt{1-\rho^2}}$, robust control implies an increase in the holdings of asset one and a decrease in the holdings of asset two.

3 Differences in Preferences for Robustness

In this section we generalize our model to allow for differences in preferences for robustness, or differences in concern about model misspecification among the different assets. These differences can also be interpreted as differences in the levels of ambiguity associated with the price processes of each asset. ¹⁶

Following the robust control methodology, we solve the same problem as in section 2, placing n different penalty terms h_i , i=1,...,n and considering n

¹⁶Uppal and Wang [31] develop a framework that allows for ambiguity about the joint distribution for all stocks being considered for the portfolio and also for different levels of ambiguity for the marginal distribution for any subset of the stocks.

different robustness parameters θ_i , one for each asset. Our results regarding changes in asset holdings between uncertainty and risk aversion in the generalized model are summarized in the following proposition.

Proposition 2 Robust portfolio choices under uncertainty aversion imply, for a market consisting of one riskless and multiple risky assets with differences in ambiguity among assets, the following:

1. The change in the fraction of wealth invested in each asset, between uncertainty and risk aversion, is: $W\Delta w_i = \sum_{j=1}^n [\Sigma^{-1}(\Pi^{-1} - \hat{D}^{-1})\Sigma^{-1}]_{ij}(\alpha_j - r)$, i = 1,...,n.

2. The change in the total holdings of risky assets as a fraction of wealth between uncertainty and risk aversion is:

$$W\Delta W = \sum_{i=1}^{n} \Delta w_{i} = \sum_{i=1}^{n} \sum_{j=1}^{n} [\Sigma^{-1}(\Pi^{-1} - \hat{D}^{-1})\Sigma^{-1}]_{ij}(\alpha_{j} - r), \text{ where } \hat{D}_{ij} = (\rho_{ij} - \frac{V_{W}^{2}}{V_{WW}} \sum_{\kappa=1}^{n} \frac{R_{i\kappa}R_{jk}}{\theta_{\kappa}}).$$

For the proof see Appendix.

If we compare the above result with the corresponding one derived in section 2, we see that the only difference is that matrix D has been replaced by matrix D, which incorporates the heterogeneity in robustness parameters.

3.1 The Special Case of Two Risky Assets

In this subsection we examine the case of two risky assets, with different penalty terms, h_1, h_2 , and robustness parameters, θ_1, θ_2 . Following the proof of the previous section, we obtain the following proposition:

Proposition 3 Robust portfolio choices under uncertainty aversion imply, for a market consisting of one riskless and two risky assets with differences in ambiguity among the two assets, the following:

1.
$$W\Delta w_1 = \frac{\kappa}{\sigma_1} \left[\frac{\alpha_1 - r}{\sigma_1} \left(\frac{\theta_1 - \theta_2}{\theta_2} \frac{1 - \rho^2}{1 - \frac{V_W^2}{V_W W}} - 1 \right) + \frac{\alpha_2 - r}{\sigma_2} \rho \right] < 0$$
, if $\frac{\theta_1 - \theta_2}{\theta_2} \mu > \frac{1 - \rho \lambda}{1 - \rho^2}$

$$W\Delta w_2 = \frac{\kappa}{\sigma_2} \left[\frac{\alpha_1 - r}{\sigma_1} \rho - \frac{\alpha_2 - r}{\sigma_2} \right] < 0$$
, if $\rho > \lambda$

- 2. We never increase the holdings of both assets at the same time, relative to risk aversion.
- 3. $W\Delta W < 0$, if $\rho\lambda\sigma + \rho \lambda = \hat{\lambda}\left(\rho \frac{1}{\sigma}\right) + \rho > \sigma\left[1 \frac{\theta_1 \theta_2}{\theta_2}\mu(1 \rho^2)\right]$

where
$$\mu = \frac{1}{1 - \frac{V_W^2}{V_W W}}$$
, $\sigma = \frac{\sigma_2}{\sigma_1}$, $\lambda = \frac{\frac{\alpha_2 - r}{\sigma_2}}{\frac{\alpha_1 - r}{\sigma_1}}$, $\hat{\lambda} = \frac{a_2 - r}{a_1 - r}$

For the proof see Appendix.

The first condition of this proposition implies that if preferences for robustness for asset one are low (high θ_1) or the ambiguity associated with the price process for this asset is small, while preferences for robustness for asset two are high (low θ_2) or the ambiguity associated with the price process for this asset is large, then it very likely that the holdings of the first asset will increase under uncertainty aversion. If asset one is a home asset and asset two is a foreign asset, then this result provides some explanation for the home bias puzzle. Uppal and Wang [31] derive a similar result regarding the home puzzle bias. They, however, use the normalization that essentially endogenizes the robustness parameter and then breaks down the consistency of preferences with the Gilboa and Schmeidler axiomatization of uncertainty aversion. Pathak [26] also provides an explanation of the home bias puzzle using a two-asset model and a κ – Ignorance framework, where the worst-case scenario is used to reduce the mean return of the asset price process. There is a subtle difference between our result and the κ – Ignorance, worst case scenario approach. In the latter approach the worst case scenario means that the reduction in the mean return of the asset price process is determined at the level where the entropy constraint $Q(\tau) = \{Q \in Q : R_t(Q \parallel \mathcal{P}) < \tau \ \forall t\}$ is binding. In the robust control model developed in this paper, the robustness parameter associated with the penalty terms is the Lagrangian multiplier associated with the entropy constraint. In the two-player game between the investor and Nature (the mean agent) described by (8), the choice of the penalty term h by Nature, which reduces the mean return, is not necessarily set at the constraint constants of the entropy constraints but is chosen in a "penalty maximizing way" as shown in (50) of the Appendix in the proof of proposition 2. Thus our result may be interpreted as an additional explanation of the home bias puzzle using a different angle for incorporating uncertainty aversion. Furthermore since the holdings in each asset depend on the θ s, this approach could associate the magnitude of the puzzle with differences in uncertainty aversion between home and foreign assets.

4 Concluding Remarks

Robust portfolio rules suggest that total holdings of risky assets may increase under uncertainty aversion relative to the risk aversion case, which is a result that can be contrasted to results suggesting that robust methods in portfolio selection imply a reduction in the total holdings of risky assets. Furthermore under heterogeneity with respect to preference for robustness, robust portfolio rules suggest that the investor might increase the holdings of the less ambiguous asset and reduce the holdings of the more ambiguous asset, a result that might provide an additional explanation for the home bias puzzle.

The robust portfolio rules derived in this paper are parametrized by the robustness parameter θ , which is not endogenized in order to keep the model consistent with the Gilboa Schmeilder axiomatization of uncertainty aversion.¹⁷ Thus our results should be regarded mainly as comparative static results in-

¹⁷Thus the full characterization of the robust portfolio rule requires estimation of θ , using for example detection probabilities [23].

dicating the direction of changes in risky asset holdings when preferences for robustness changes, with the limiting case being the no preference for robustness, which is equivalent to standard risk aversion. The fact that changes could go either way depending on the structure of the model parameters suggests that uncertainty aversion and adoption of robust portfolio rules should not be associated with smaller holdings of risky assets.

Appendix

Proof of Proposition 2

Suppose now, that we place n different penalty terms h_i for i = 1, ..., n and consider the corresponding robustness parameters θ_i . In this case, the equation for wealth dynamics takes the form:

$$dW = \left(rW - c + \sum_{i=1}^{n} w_i(\alpha_i - r)W + \sum_{i=1}^{n} \sum_{j=1}^{n} \sigma_i R_{ij} w_i W h_j\right) dt$$

$$+ \sum_{i=1}^{n} \sum_{j=1}^{n} w_j \sigma_j W R_{ij} d\hat{B}_i$$

$$(46)$$

and the corresponding multiplier robust control problem now becomes:

$$J(\theta) = \sup_{w_i, C} \inf_{h_i} \mathbb{E}_{\mathcal{Q}} \int_0^\infty e^{-\delta t} \left[U(C) + \sum_{i=1}^n \theta_i \frac{h_i^2}{2} \right] dt$$
 (47)

subject to (46).

The value function $V(W, \theta)$ satisfies the following equation:

$$\delta V = \max_{w_i, C} \min_{h_i} \left\{ U(C) + \left(rW - c + \sum_{i=1}^n w_i (\alpha_i - r)W \right) \right\}$$

$$\tag{48}$$

$$+ \sum_{i=1}^{n} \sum_{j=1}^{n} \sigma_{i} R_{ij} w_{i} W h_{j} W + \sum_{i=1}^{n} \theta_{i} \frac{h_{i}^{2}}{2} + \frac{1}{2} V_{WW} \sum_{i=1}^{n} \sum_{j=1}^{n} w_{i} w_{j} \sigma_{ij} W^{2} .$$

The first-order conditions are:

$$U'(C) = V_W (49)$$

$$h_i = -\frac{V_W W \sum_{j=1}^n w_j \sigma_j R_{ji}}{\theta_i}, i = 1, ..., n$$
 (50)

$$\sum_{j=1}^{n} w_{j} W \sigma_{ij} = A(\alpha_{i} - r) + A \sigma_{i} \sum_{j=1}^{n} h_{j} R_{ij} , i = 1, ..., n$$
 (51)

$$A = -\frac{V_W}{V_{WW}} = -\frac{U'(C)}{U''(C)\frac{\partial C}{\partial W}}.$$
 (52)

Replacing the second into the third relationship we obtain that:

$$w_i^* W = \sum_{j=1}^n \hat{v}_{ij}^{-1} (\alpha_j - r) , i = 1, ..., n$$
 (53)

where \hat{v}^{-1} is the inverse of the matrix:

$$[\hat{v}_{ij}] = [(\Sigma \hat{D}\Sigma)_{ij}] \tag{54}$$

$$\hat{D}_{ij} = \left(\rho_{ij} - \frac{V_W^2}{V_{WW}} \sum_{\kappa=1}^n \frac{R_{i\kappa} R_{jk}}{\theta_{\kappa}}\right). \tag{55}$$

So in order to compare again the change of wealth invested in each one of the assets, we subtract relationship (53) from (2). Therefore we obtain that:

$$W\Delta w_i = \sum_{j=1}^n \left[\Sigma^{-1} (\Pi^{-1} - \hat{D}^{-1}) \Sigma^{-1} \right]_{ij} (\alpha_j - r) , \ i = 1, ..., n$$
 (56)

From the previous equation we obtain:

$$W\Delta W = \sum_{i=1}^{n} \Delta w_i = \sum_{i=1}^{n} \sum_{j=1}^{n} [\Sigma^{-1} (\Pi^{-1} - \hat{D}^{-1}) \Sigma^{-1}]_{ij} (\alpha_j - r).$$
 (57)

Proof of Proposition 3

In this case the equation for wealth dynamics becomes:

$$dW = \left[w_1(\alpha_1 - r + \sigma_1 h_1) + w_2(\alpha_2 - r + \sigma_2(\rho h_1 + h_2 \sqrt{1 - \rho^2})) \right] W dt + (rW - C) dt + W \sigma_1 w_1 d\hat{B}_1 + W \sigma_2 \rho w_2 d\hat{B}_1 + \sigma_2 \sqrt{1 - \rho^2} w_2 d\hat{B}_2.$$
(58)

The multiplier robust control problem is defined as:

$$J(\theta) = \sup_{w_i, C} \inf_{h} \mathbb{E}_{\mathcal{Q}} \int_0^\infty e^{-\delta t} \left[U(C) + \theta_1 \frac{h_1^2}{2} + \theta_2 \frac{h_2^2}{2} \right] dt$$
 (59)

subject to (58).

The value function in this case satisfies:

$$\delta V = \max_{w_i, C} \min_{h_i} \left\{ U(C) + \left(w_1(\alpha_1 - r + \sigma_1 h_1) W + (rW - c) \right) + \theta_1 \frac{h_1^2}{2} + \theta_2 \frac{h_2^2}{2} + w_2(\alpha_2 - r + \sigma_2 \rho h_1 + \sigma_2 \sqrt{1 - \rho^2} h_2) W \right) V_W + \frac{1}{2} V_{WW} \sum_{i=1}^2 \sum_{j=1}^2 w_i w_j \sigma_{ij} W^2 \right\}.$$
(60)

For this two-player game the first-order conditions are:

$$U'(C) = V_W (61)$$

$$h_1 = -\frac{V_W W \left(\sigma_1 w_1^* + \sigma_2 \rho w_2^*\right)}{\theta_1} \tag{62}$$

$$h_2 = -\frac{V_W W \sqrt{1 - \rho^2} \sigma_2 w_2^*}{\theta_2} \tag{63}$$

$$\sum_{j=1}^{2} w_{j}^{*} W \sigma_{1j} = A(\alpha_{1} - r) + A \sigma_{1} h_{1}$$
(64)

$$\sum_{j=1}^{2} w_{j}^{*} W \sigma_{2j} = A(\alpha_{2} - r) + A \sigma_{2} (\rho h_{1} + \sqrt{1 - \rho^{2}} h_{2})$$
 (65)

$$A = -\frac{V_W}{V_{WW}} = -\frac{U'(C)}{U''(C)\frac{\partial C}{\partial W}}.$$
 (66)

Using matrices as in section 3, we are able to describe the solution of the above problem by the following equation:

$$[w_1^* W \quad w_2^* W] \Lambda = [A(\alpha_1 - r) \quad A(\alpha_2 - r)]$$
 (67)

where now Λ is the matrix:

$$\Lambda = \begin{bmatrix} \sigma_{11} \left(1 - \frac{V_W^2}{\theta_1 V_{WW}}\right) & \sigma_{12} \left(1 - \frac{V_W^2}{\theta_1 V_{WW}}\right) \\ \sigma_{21} \left(1 - \frac{V_W^2}{\theta_1 V_{WW}}\right) & \sigma_{22} \left(1 - \frac{V_W^2}{V_{WW}} \left(\frac{\rho^2}{\theta_1} + \frac{1 - \rho^2}{\theta_2}\right)\right) \end{bmatrix}.$$
(68)

In this case the solution is:

We examine the difference between the quantities given by (20),(21) and (69) and after manipulations we obtain:

$$\begin{bmatrix}
W\Delta w_1 & W\Delta w_2
\end{bmatrix} = \frac{AV_W^2 \begin{bmatrix} \alpha_1 - r & \alpha_2 - r \\ (1 - \rho^2)(\theta_2 V_{WW} - V_W^2) \end{bmatrix} \\
\Sigma^{-1} \begin{bmatrix} \frac{\theta_1 - \theta_2}{\theta_2} \frac{1 - \rho^2}{1 - \frac{V_W^2}{V_{WW}}} - 1 & \rho \\ \rho & -1 \end{bmatrix} \Sigma^{-1}.$$
(70)

Therefore the solution becomes:

$$W\Delta w_1 = \frac{\kappa}{\sigma_1} \left[\frac{\alpha_1 - r}{\sigma_1} \left(\frac{\theta_1 - \theta_2}{\theta_2} \frac{1 - \rho^2}{1 - \frac{V_W^2}{V_{WW}}} - 1 \right) + \frac{\alpha_2 - r}{\sigma_2} \rho \right]$$
(71)

$$W\Delta w_2 = \frac{\kappa}{\sigma_2} \left[\frac{\alpha_1 - r}{\sigma_1} \rho - \frac{\alpha_2 - r}{\sigma_2} \right]$$
 (72)

$$\kappa = \frac{AV_W^2}{(1 - \rho^2)(\theta_2 V_{WW} - V_W^2)}. (73)$$

Thus if λ as in (40) then:

$$W\Delta w_1 < 0 \qquad if \quad \frac{\theta_1 - \theta_2}{\theta_2} \mu > \frac{1 - \rho\lambda}{1 - \rho^2} \tag{74}$$

$$W\Delta w_2 < 0 \quad if \quad \rho > \lambda$$
 (75)

where $\mu = \frac{1}{1 - \frac{V_W^2}{V_{WW}}}$. If equation (75) holds then the right hand side of (74) is

always greater than one and the left less than one. So as in the case with the same levels of ambiguity, we never increase the holdings of both assets at the same time. In addition if we combine (71) - (72), we obtain:

$$W\Delta W = W\Delta w_1 + W\Delta w_2 = \tag{76}$$

$$\kappa \frac{\alpha_1 - r}{\sigma_1} \frac{1}{\sigma_2} \left[\sigma \frac{\theta_1 - \theta_2}{\theta_2} \mu (1 - \rho^2) - \sigma + \rho \lambda \sigma + \rho - \lambda \right] < 0 \quad if \tag{77}$$

$$\rho \lambda \sigma + \rho - \lambda > \sigma \left[1 - \frac{\theta_1 - \theta_2}{\theta_2} \mu (1 - \rho^2) \right]$$
 or

$$\hat{\lambda}(\rho - \frac{1}{\sigma}) + \rho > \sigma \left[1 - \frac{\theta_1 - \theta_2}{\theta_2} \mu (1 - \rho^2) \right]$$
 (78)

where again $\sigma = \frac{\sigma_2}{\sigma_1}$ and $\hat{\lambda} = \frac{a_2 - r}{a_1 - r}$.

References

- [1] W. Brainard, Uncertainty and the effectiveness of policy, Amer. Econom. Rev. 58 (1967) 411-425.
- [2] W.A. Brock, S. Durlauf, Elements of a theory of design limits to optimal policy, University of Wisconsin, SSRI Working Paper 2003-25, 2003.
- [3] W.A. Brock, S. Durlauf, K. West, Policy evaluation in uncertain economic environments, University of Wisconsin, SSRI Working Paper 2003-15, 2003.
- [4] W. A. Brock, A. Xepapadeas, Regulating nonlinear environmental Systems under Knightian uncertainty, in: R. Arnott, B. Greenwald, R. Kanbur, B. Nalebuff (Eds.), Economics for an Imperfect World: Essays In Honor of Joseph Stiglitz, MIT Press, Cambridge, Mass., 2003.
- [5] J. Dow, S. Werlang, Uncertainty aversion, risk aversion, and the optimal choice of portfolio, Econometrica 60 (1992) 197-204.
- [6] P. Dupuis, R. Ellis, A weak convergence approach to the theory of large deviations, Wiley Series in Probability and Statistics, John Wiley and Sons, New York, 1997.
- [7] Z. Chen, L. Epstein, Ambiguity risk and asset returns in continuous time, Econometrica 70 (2002) 1403-1443.
- [8] L. Epstein, J. Miao, A two-person dynamic equilibrium under ambiguity, J. Econom. Dynamics and Control, 27 (2003) 1253-1288.
- [9] L. Epstein, T. Wang, Intertemporal asset pricing under Knightian uncertainty, Econometrica 63 (1994) 283-322.
- [10] W.H. Fleming, P.E. Souganidis, On the existence of value function of twoplayer, zero sum stochastic differential games, Indiana Univ. Mathematics J. 3 (1989) 293-314.
- [11] K.R. French, J. M. Poterba, Investor diversification and international equity markets, Amer. Econom. Rev. Papers and Proceedings 81(2) (May 1991) 222-226.
- [12] I. Gilboa, D. Schmeidler, Maxmin expected utility with non-unique prior, J. Math. Econom. 18 (1989) 141-153.
- [13] W-F. Liu, Savings and portfolio decisions: Observable implications of Knightian uncertainty, Working Paper, Department of Economics, University of Washington, 2003.
- [14] W-F. Liu, Heterogeneous agents economics with Knightian uncertainty, Working Paper, Department of Economics, University of Washington, 2003.

- [15] R. Merton, Optimum consumption and portfolio rules in a continuous time model, J. Econom. Theory 3 (1971) 373-413.
- [16] R. Merton, An intertemporal capital asset pricing model, Econometrica 41 (1973) 867-887.
- [17] A. Onatski, J. Stock, Robust monetary policy under model uncertainty in a small model of the U.S. economy, Macroeconomic Dynamics 6 (2002) 85-110.
- [18] A. Onatski, N. Williams, Modeling model uncertainty, NBER Working Paper 9566, 2003.
- [19] L. Hansen, T. Sargent, Robust control and filtering for macroeconomics, unpublished manuscript, University of Chicago and Stanford University, 2001.
- [20] L. Hansen, T. Sargent, Robust control and model uncertainty, Amer. Econom. Rev. 91 (2001) 60–66.
- [21] L. Hansen, T. Sargent, Wanting robustness in macroeconomics, unpublished paper, University of Chicago and Stanford University, 2001.
- [22] L. Hansen, T. Sargent, Robust control and economic model uncertainty, unpublished paper, University of Chicago and Stanford University, 2002.
- [23] L. Hansen, T. Sargent, Misspecification in recursive macroeconomic theory, monograph, University of Chicago and Stanford University, 2003.
- [24] L. Hansen, T. Sargent, G. Turmuhambetova, N. Williams, Robust control and model uncertainty, unpublished paper, University of Chicago and Stanford University, 2002.
- [25] P. Maenhout, Robust portfolio rules, hedging and asset pricing, unpublished paper, INSEAD, 2001.
- [26] P. Pathak, Notes on robust portfolio choice, unpublished paper, Harvard University, 2002.
- [27] C. Roseta-Palma, A. Xepapadeas, Robust control in water management, J. Risk and Uncertainty, forthcoming.
- [28] A. Serrat, A dynamic equilibrium model of international portfolio holdings, Econometrica 69(6) (2001) 1467-1490.
- [29] U. Soderstrom, Monetary policy with uncertain parameters, Scandinavian J. Econom. 104 (2002) 125-145.
- [30] N. Strong, X. Xu, Understanding the equity home bias: Evidence from survey data, Rev. Econ. Statist. 85(2) (2003) 307 312.
- [31] R. Uppal, T. Wang, Model misspecification and underdiversification, J. Finance, forthcoming.

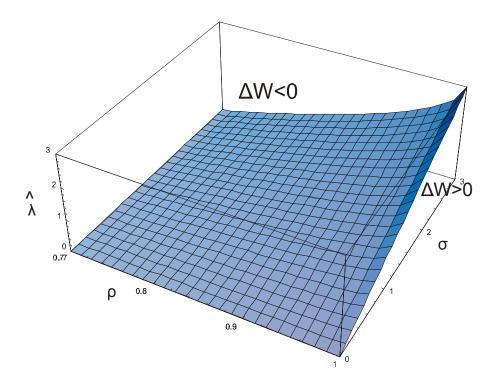


Figure 1: Changes in the total holdings of risky assets under uncertainty aversion

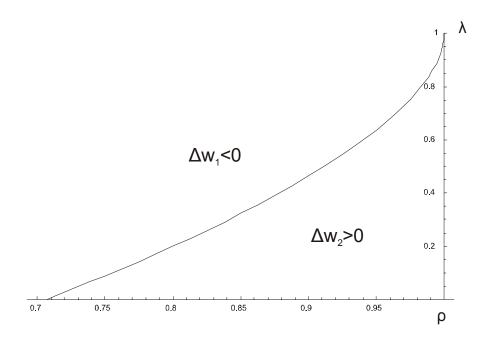


Figure 2: Changes in the holdings of each risky asset under uncertainty aversion

NOTE DI LAVORO DELLA FONDAZIONE ENI ENRICO MATTEI

Fondazione Eni Enrico Mattei Working Paper Series

Our Note di Lavoro are available on the Internet at the following addresses: http://www.feem.it/Feem/Pub/Publications/WPapers/default.htmlhttp://www.ssrn.com/link/feem.html

NOTE DI LAVORO PUBLISHED IN 2003

PRIV	1.2003	Gabriella CHIESA and Giovanna NICODANO: Privatization and Financial Market Development: Theoretical
		Issues
PRIV	2.2003	Ibolya SCHINDELE: Theory of Privatization in Eastern Europe: Literature Review
PRIV	3.2003	Wietze LISE, Claudia KEMFERT and Richard S.J. TOL: Strategic Action in the Liberalised German Electricity
	0.200	Market
CLIM	4.2003	Laura MARSILIANI and Thomas I. RENSTRÖM: Environmental Policy and Capital Movements: The Role of
CLIM	4.2003	Government Commitment
KNOW	5.2003	Reyer GERLAGH: Induced Technological Change under Technological Competition
ETA	6.2003	Efrem CASTELNUOVO: Squeezing the Interest Rate Smoothing Weight with a Hybrid Expectations Model
SIEV	7.2003	Anna ALBERINI, Alberto LONGO, Stefania TONIN, Francesco TROMBETTA and Margherita TURVANI: The
		Role of Liability, Regulation and Economic Incentives in Brownfield Remediation and Redevelopment:
		Evidence from Surveys of Developers
NRM	8.2003	Elissaios PAPYRAKIS and Reyer GERLAGH: Natural Resources: A Blessing or a Curse?
CLIM	9.2003	A. CAPARRÓS, JC. PEREAU and T. TAZDAÏT: North-South Climate Change Negotiations: a Sequential Game
		with Asymmetric Information
KNOW	10.2003	Giorgio BRUNELLO and Daniele CHECCHI: School Quality and Family Background in Italy
CLIM	11.2003	Efrem CASTELNUOVO and Marzio GALEOTTI: Learning By Doing vs Learning By Researching in a Model of
		Climate Change Policy Analysis
KNOW	12.2003	Carole MAIGNAN, Gianmarco OTTAVIANO and Dino PINELLI (eds.): Economic Growth, Innovation, Cultural
1211011	12.2003	Diversity: What are we all talking about? A critical survey of the state-of-the-art
KNOW	13.2003	Carole MAIGNAN, Gianmarco OTTAVIANO, Dino PINELLI and Francesco RULLANI (lix): Bio-Ecological
KNOW	13.2003	Diversity vs. Socio-Economic Diversity. A Comparison of Existing Measures
KNOW	14.2003	Maddy JANSSENS and Chris STEYAERT (lix): Theories of Diversity within Organisation Studies: Debates and
KNOW	14.2003	,
KNOW	15 2002	Future Trajectories The interpretation of the Future Trajectories and the Future Traj
KNOW	15.2003	Tuzin BAYCAN LEVENT, Enno MASUREL and Peter NIJKAMP (lix): Diversity in Entrepreneurship: Ethnic and
*******	4 6 0000	Female Roles in Urban Economic Life
KNOW	16.2003	Alexandra BITUSIKOVA (lix): Post-Communist City on its Way from Grey to Colourful: The Case Study from
		Slovakia
KNOW	17.2003	Billy E. VAUGHN and Katarina MLEKOV (lix): A Stage Model of Developing an Inclusive Community
KNOW	18.2003	Selma van LONDEN and Arie de RUIJTER (lix): Managing Diversity in a Glocalizing World
Coalition		
Theory	19.2003	Sergio CURRARINI: On the Stability of Hierarchies in Games with Externalities
Network		
PRIV	20.2003	Giacomo CALZOLARI and Alessandro PAVAN (lx): Monopoly with Resale
PRIV	21.2003	Claudio MEZZETTI (lx): Auction Design with Interdependent Valuations: The Generalized Revelation
		Principle, Efficiency, Full Surplus Extraction and Information Acquisition
PRIV	22.2003	Marco LiCalzi and Alessandro PAVAN (lx): Tilting the Supply Schedule to Enhance Competition in Uniform-
		· /
DD ***		Price Auctions
PRIV	23.2003	Price Auctions David ETTINGER (Ix): Bidding among Friends and Enemies
PRIV PRIV	23.2003 24.2003	David ETTINGER (lx): Bidding among Friends and Enemies
PRIV	24.2003	David ETTINGER (lx): Bidding among Friends and Enemies Hannu VARTIAINEN (lx): Auction Design without Commitment
		David ETTINGER (lx): Bidding among Friends and Enemies Hannu VARTIAINEN (lx): Auction Design without Commitment Matti KELOHARJU, Kjell G. NYBORG and Kristian RYDQVIST (lx): Strategic Behavior and Underpricing in
PRIV PRIV	24.2003 25.2003	David ETTINGER (lx): Bidding among Friends and Enemies Hannu VARTIAINEN (lx): Auction Design without Commitment Matti KELOHARJU, Kjell G. NYBORG and Kristian RYDQVIST (lx): Strategic Behavior and Underpricing in Uniform Price Auctions: Evidence from Finnish Treasury Auctions
PRIV PRIV PRIV	24.2003 25.2003 26.2003	David ETTINGER (lx): Bidding among Friends and Enemies Hannu VARTIAINEN (lx): Auction Design without Commitment Matti KELOHARJU, Kjell G. NYBORG and Kristian RYDQVIST (lx): Strategic Behavior and Underpricing in Uniform Price Auctions: Evidence from Finnish Treasury Auctions Christine A. PARLOUR and Uday RAJAN (lx): Rationing in IPOs
PRIV PRIV PRIV PRIV	24.2003 25.2003 26.2003 27.2003	David ETTINGER (lx): Bidding among Friends and Enemies Hannu VARTIAINEN (lx): Auction Design without Commitment Matti KELOHARJU, Kjell G. NYBORG and Kristian RYDQVIST (lx): Strategic Behavior and Underpricing in Uniform Price Auctions: Evidence from Finnish Treasury Auctions Christine A. PARLOUR and Uday RAJAN (lx): Rationing in IPOs Kjell G. NYBORG and Ilya A. STREBULAEV (lx): Multiple Unit Auctions and Short Squeezes
PRIV PRIV PRIV	24.2003 25.2003 26.2003	David ETTINGER (lx): Bidding among Friends and Enemies Hannu VARTIAINEN (lx): Auction Design without Commitment Matti KELOHARJU, Kjell G. NYBORG and Kristian RYDQVIST (lx): Strategic Behavior and Underpricing in Uniform Price Auctions: Evidence from Finnish Treasury Auctions Christine A. PARLOUR and Uday RAJAN (lx): Rationing in IPOs Kjell G. NYBORG and Ilya A. STREBULAEV (lx): Multiple Unit Auctions and Short Squeezes Anders LUNANDER and Jan-Eric NILSSON (lx): Taking the Lab to the Field: Experimental Tests of Alternative
PRIV PRIV PRIV PRIV PRIV	24.2003 25.2003 26.2003 27.2003 28.2003	David ETTINGER (lx): Bidding among Friends and Enemies Hannu VARTIAINEN (lx): Auction Design without Commitment Matti KELOHARJU, Kjell G. NYBORG and Kristian RYDQVIST (lx): Strategic Behavior and Underpricing in Uniform Price Auctions: Evidence from Finnish Treasury Auctions Christine A. PARLOUR and Uday RAJAN (lx): Rationing in IPOs Kjell G. NYBORG and Ilya A. STREBULAEV (lx): Multiple Unit Auctions and Short Squeezes Anders LUNANDER and Jan-Eric NILSSON (lx): Taking the Lab to the Field: Experimental Tests of Alternative Mechanisms to Procure Multiple Contracts
PRIV PRIV PRIV PRIV PRIV	24.2003 25.2003 26.2003 27.2003 28.2003 29.2003	David ETTINGER (lx): Bidding among Friends and Enemies Hannu VARTIAINEN (lx): Auction Design without Commitment Matti KELOHARJU, Kjell G. NYBORG and Kristian RYDQVIST (lx): Strategic Behavior and Underpricing in Uniform Price Auctions: Evidence from Finnish Treasury Auctions Christine A. PARLOUR and Uday RAJAN (lx): Rationing in IPOs Kjell G. NYBORG and Ilya A. STREBULAEV (lx): Multiple Unit Auctions and Short Squeezes Anders LUNANDER and Jan-Eric NILSSON (lx): Taking the Lab to the Field: Experimental Tests of Alternative Mechanisms to Procure Multiple Contracts TangaMcDANIEL and Karsten NEUHOFF (lx): Use of Long-term Auctions for Network Investment
PRIV PRIV PRIV PRIV PRIV PRIV	24.2003 25.2003 26.2003 27.2003 28.2003 29.2003 30.2003	David ETTINGER (lx): Bidding among Friends and Enemies Hannu VARTIAINEN (lx): Auction Design without Commitment Matti KELOHARJU, Kjell G. NYBORG and Kristian RYDQVIST (lx): Strategic Behavior and Underpricing in Uniform Price Auctions: Evidence from Finnish Treasury Auctions Christine A. PARLOUR and Uday RAJAN (lx): Rationing in IPOs Kjell G. NYBORG and Ilya A. STREBULAEV (lx): Multiple Unit Auctions and Short Squeezes Anders LUNANDER and Jan-Eric NILSSON (lx): Taking the Lab to the Field: Experimental Tests of Alternative Mechanisms to Procure Multiple Contracts TangaMcDANIEL and Karsten NEUHOFF (lx): Use of Long-term Auctions for Network Investment Emiel MAASLAND and Sander ONDERSTAL (lx): Auctions with Financial Externalities
PRIV PRIV PRIV PRIV PRIV	24.2003 25.2003 26.2003 27.2003 28.2003 29.2003	David ETTINGER (lx): Bidding among Friends and Enemies Hannu VARTIAINEN (lx): Auction Design without Commitment Matti KELOHARJU, Kjell G. NYBORG and Kristian RYDQVIST (lx): Strategic Behavior and Underpricing in Uniform Price Auctions: Evidence from Finnish Treasury Auctions Christine A. PARLOUR and Uday RAJAN (lx): Rationing in IPOs Kjell G. NYBORG and Ilya A. STREBULAEV (lx): Multiple Unit Auctions and Short Squeezes Anders LUNANDER and Jan-Eric NILSSON (lx): Taking the Lab to the Field: Experimental Tests of Alternative Mechanisms to Procure Multiple Contracts TangaMcDANIEL and Karsten NEUHOFF (lx): Use of Long-term Auctions for Network Investment Emiel MAASLAND and Sander ONDERSTAL (lx): Auctions with Financial Externalities Michael FINUS and Bianca RUNDSHAGEN: A Non-cooperative Foundation of Core-Stability in Positive
PRIV PRIV PRIV PRIV PRIV PRIV PRIV ETA	24.2003 25.2003 26.2003 27.2003 28.2003 29.2003 30.2003 31.2003	David ETTINGER (lx): Bidding among Friends and Enemies Hannu VARTIAINEN (lx): Auction Design without Commitment Matti KELOHARJU, Kjell G. NYBORG and Kristian RYDQVIST (lx): Strategic Behavior and Underpricing in Uniform Price Auctions: Evidence from Finnish Treasury Auctions Christine A. PARLOUR and Uday RAJAN (lx): Rationing in IPOs Kjell G. NYBORG and Ilya A. STREBULAEV (lx): Multiple Unit Auctions and Short Squeezes Anders LUNANDER and Jan-Eric NILSSON (lx): Taking the Lab to the Field: Experimental Tests of Alternative Mechanisms to Procure Multiple Contracts TangaMcDANIEL and Karsten NEUHOFF (lx): Use of Long-term Auctions for Network Investment Emiel MAASLAND and Sander ONDERSTAL (lx): Auctions with Financial Externalities Michael FINUS and Bianca RUNDSHAGEN: A Non-cooperative Foundation of Core-Stability in Positive Externality NTU-Coalition Games
PRIV PRIV PRIV PRIV PRIV PRIV ETA	24.2003 25.2003 26.2003 27.2003 28.2003 30.2003 31.2003 32.2003	David ETTINGER (lx): Bidding among Friends and Enemies Hannu VARTIAINEN (lx): Auction Design without Commitment Matti KELOHARJU, Kjell G. NYBORG and Kristian RYDQVIST (lx): Strategic Behavior and Underpricing in Uniform Price Auctions: Evidence from Finnish Treasury Auctions Christine A. PARLOUR and Uday RAJAN (lx): Rationing in IPOs Kjell G. NYBORG and Ilya A. STREBULAEV (lx): Multiple Unit Auctions and Short Squeezes Anders LUNANDER and Jan-Eric NILSSON (lx): Taking the Lab to the Field: Experimental Tests of Alternative Mechanisms to Procure Multiple Contracts TangaMcDANIEL and Karsten NEUHOFF (lx): Use of Long-term Auctions for Network Investment Emiel MAASLAND and Sander ONDERSTAL (lx): Auctions with Financial Externalities Michael FINUS and Bianca RUNDSHAGEN: A Non-cooperative Foundation of Core-Stability in Positive Externality NTU-Coalition Games Michael MORETTO: Competition and Irreversible Investments under Uncertainty
PRIV PRIV PRIV PRIV PRIV PRIV PRIV ETA	24.2003 25.2003 26.2003 27.2003 28.2003 29.2003 30.2003 31.2003	David ETTINGER (lx): Bidding among Friends and Enemies Hannu VARTIAINEN (lx): Auction Design without Commitment Matti KELOHARJU, Kjell G. NYBORG and Kristian RYDQVIST (lx): Strategic Behavior and Underpricing in Uniform Price Auctions: Evidence from Finnish Treasury Auctions Christine A. PARLOUR and Uday RAJAN (lx): Rationing in IPOs Kjell G. NYBORG and Ilya A. STREBULAEV (lx): Multiple Unit Auctions and Short Squeezes Anders LUNANDER and Jan-Eric NILSSON (lx): Taking the Lab to the Field: Experimental Tests of Alternative Mechanisms to Procure Multiple Contracts TangaMcDANIEL and Karsten NEUHOFF (lx): Use of Long-term Auctions for Network Investment Emiel MAASLAND and Sander ONDERSTAL (lx): Auctions with Financial Externalities Michael FINUS and Bianca RUNDSHAGEN: A Non-cooperative Foundation of Core-Stability in Positive Externality NTU-Coalition Games Michele MORETTO: Competition and Irreversible Investments under Uncertainty Philippe QUIRION: Relative Quotas: Correct Answer to Uncertainty or Case of Regulatory Capture?
PRIV PRIV PRIV PRIV PRIV PRIV ETA	24.2003 25.2003 26.2003 27.2003 28.2003 30.2003 31.2003 32.2003	David ETTINGER (lx): Bidding among Friends and Enemies Hannu VARTIAINEN (lx): Auction Design without Commitment Matti KELOHARJU, Kjell G. NYBORG and Kristian RYDQVIST (lx): Strategic Behavior and Underpricing in Uniform Price Auctions: Evidence from Finnish Treasury Auctions Christine A. PARLOUR and Uday RAJAN (lx): Rationing in IPOs Kjell G. NYBORG and Ilya A. STREBULAEV (lx): Multiple Unit Auctions and Short Squeezes Anders LUNANDER and Jan-Eric NILSSON (lx): Taking the Lab to the Field: Experimental Tests of Alternative Mechanisms to Procure Multiple Contracts TangaMcDANIEL and Karsten NEUHOFF (lx): Use of Long-term Auctions for Network Investment Emiel MAASLAND and Sander ONDERSTAL (lx): Auctions with Financial Externalities Michael FINUS and Bianca RUNDSHAGEN: A Non-cooperative Foundation of Core-Stability in Positive Externality NTU-Coalition Games Michael MORETTO: Competition and Irreversible Investments under Uncertainty
PRIV PRIV PRIV PRIV PRIV PRIV ETA KNOW PRIV	24.2003 25.2003 26.2003 27.2003 28.2003 30.2003 31.2003 32.2003 33.2003	David ETTINGER (lx): Bidding among Friends and Enemies Hannu VARTIAINEN (lx): Auction Design without Commitment Matti KELOHARJU, Kjell G. NYBORG and Kristian RYDQVIST (lx): Strategic Behavior and Underpricing in Uniform Price Auctions: Evidence from Finnish Treasury Auctions Christine A. PARLOUR and Uday RAJAN (lx): Rationing in IPOs Kjell G. NYBORG and Ilya A. STREBULAEV (lx): Multiple Unit Auctions and Short Squeezes Anders LUNANDER and Jan-Eric NILSSON (lx): Taking the Lab to the Field: Experimental Tests of Alternative Mechanisms to Procure Multiple Contracts TangaMcDANIEL and Karsten NEUHOFF (lx): Use of Long-term Auctions for Network Investment Emiel MAASLAND and Sander ONDERSTAL (lx): Auctions with Financial Externalities Michael FINUS and Bianca RUNDSHAGEN: A Non-cooperative Foundation of Core-Stability in Positive Externality NTU-Coalition Games Michael MORETTO: Competition and Irreversible Investments under Uncertainty Philippe QUIRION: Relative Quotas: Correct Answer to Uncertainty or Case of Regulatory Capture?
PRIV PRIV PRIV PRIV PRIV PRIV ETA KNOW PRIV	24.2003 25.2003 26.2003 27.2003 28.2003 30.2003 31.2003 32.2003 33.2003	David ETTINGER (lx): Bidding among Friends and Enemies Hannu VARTIAINEN (lx): Auction Design without Commitment Matti KELOHARJU, Kjell G. NYBORG and Kristian RYDQVIST (lx): Strategic Behavior and Underpricing in Uniform Price Auctions: Evidence from Finnish Treasury Auctions Christine A. PARLOUR and Uday RAJAN (lx): Rationing in IPOs Kjell G. NYBORG and Ilya A. STREBULAEV (lx): Multiple Unit Auctions and Short Squeezes Anders LUNANDER and Jan-Eric NILSSON (lx): Taking the Lab to the Field: Experimental Tests of Alternative Mechanisms to Procure Multiple Contracts TangaMcDANIEL and Karsten NEUHOFF (lx): Use of Long-term Auctions for Network Investment Emiel MAASLAND and Sander ONDERSTAL (lx): Auctions with Financial Externalities Michael FINUS and Bianca RUNDSHAGEN: A Non-cooperative Foundation of Core-Stability in Positive Externality NTU-Coalition Games Michael MORETTO: Competition and Irreversible Investments under Uncertainty Philippe QUIRION: Relative Quotas: Correct Answer to Uncertainty or Case of Regulatory Capture? Giuseppe MEDA, Claudio PIGA and Donald SIEGEL: On the Relationship between R&D and Productivity: A
PRIV PRIV PRIV PRIV PRIV PRIV ETA KNOW PRIV KNOW	24.2003 25.2003 26.2003 27.2003 28.2003 30.2003 31.2003 32.2003 33.2003 34.2003	David ETTINGER (lx): Bidding among Friends and Enemies Hannu VARTIAINEN (lx): Auction Design without Commitment Matti KELOHARJU, Kjell G. NYBORG and Kristian RYDQVIST (lx): Strategic Behavior and Underpricing in Uniform Price Auctions: Evidence from Finnish Treasury Auctions Christine A. PARLOUR and Uday RAJAN (lx): Rationing in IPOs Kjell G. NYBORG and Ilya A. STREBULAEV (lx): Multiple Unit Auctions and Short Squeezes Anders LUNANDER and Jan-Eric NILSSON (lx): Taking the Lab to the Field: Experimental Tests of Alternative Mechanisms to Procure Multiple Contracts TangaMcDANIEL and Karsten NEUHOFF (lx): Use of Long-term Auctions for Network Investment Emiel MAASLAND and Sander ONDERSTAL (lx): Auctions with Financial Externalities Michael FINUS and Bianca RUNDSHAGEN: A Non-cooperative Foundation of Core-Stability in Positive Externality NTU-Coalition Games Michael MORETTO: Competition and Irreversible Investments under Uncertainty Philippe QUIRION: Relative Quotas: Correct Answer to Uncertainty or Case of Regulatory Capture? Giuseppe MEDA, Claudio PIGA and Donald SIEGEL: On the Relationship between R&D and Productivity: A Treatment Effect Analysis

GG	36.2003	Matthieu GLACHANT: Voluntary Agreements under Endogenous Legislative Threats
PRIV	37.2003	Narjess BOUBAKRI, Jean-Claude COSSET and Omrane GUEDHAMI: Postprivatization Corporate
		Governance: the Role of Ownership Structure and Investor Protection
CLIM	38.2003	Rolf GOLOMBEK and Michael HOEL: Climate Policy under Technology Spillovers
KNOW	39.2003	Slim BEN YOUSSEF: Transboundary Pollution, R&D Spillovers and International Trade
CTN	40.2003	Carlo CARRARO and Carmen MARCHIORI: Endogenous Strategic Issue Linkage in International Negotiations
KNOW	41.2003	Sonia OREFFICE: Abortion and Female Power in the Household: Evidence from Labor Supply
KNOW	42.2003	Timo GOESCHL and Timothy SWANSON: On Biology and Technology: The Economics of Managing
ICT (O V	12.2003	Biotechnologies
ETA	43.2003	Giorgio BUSETTI and Matteo MANERA: STAR-GARCH Models for Stock Market Interactions in the Pacific
EIA	43.2003	Basin Region, Japan and US
CL D.	44.2002	
CLIM	44.2003	Katrin MILLOCK and Céline NAUGES: The French Tax on Air Pollution: Some Preliminary Results on its
		<u>Effectiveness</u>
PRIV	45.2003	Bernardo BORTOLOTTI and Paolo PINOTTI: The Political Economy of Privatization
SIEV	46.2003	Elbert DIJKGRAAF and Herman R.J. VOLLEBERGH: Burn or Bury? A Social Cost Comparison of Final Waste
		<u>Disposal Methods</u>
ETA	47.2003	Jens HORBACH: Employment and Innovations in the Environmental Sector: Determinants and Econometrical
		Results for Germany
CLIM	48.2003	Lori SNYDER, Nolan MILLER and Robert STAVINS: The Effects of Environmental Regulation on Technology
		Diffusion: The Case of Chlorine Manufacturing
CLIM	49.2003	Lori SNYDER, Robert STAVINS and Alexander F. WAGNER: Private Options to Use Public Goods. Exploiting
		Revealed Preferences to Estimate Environmental Benefits
CTN	50.2003	László Á. KÓCZY and Luc LAUWERS (lxi): The Minimal Dominant Set is a Non-Empty Core-Extension
CIII	30.2003	Euszio II. Roozi una zue Eiler Erio (IX).
CTN	51.2003	Matthew O. JACKSON (lxi): Allocation Rules for Network Games
CTN	52.2003	Ana MAULEON and Vincent VANNETELBOSCH (Ixi): Farsightedness and Cautiousness in Coalition Formation
CTN	53.2003	Fernando VEGA-REDONDO (lxi): Building Up Social Capital in a Changing World: a network approach
CTN	54.2003	Matthew HAAG and Roger LAGUNOFF (lxi): On the Size and Structure of Group Cooperation
CTN	55.2003	Taiji FURUSAWA and Hideo KONISHI (lxi): Free Trade Networks
CTN	56.2003	Halis Murat YILDIZ (lxi): National Versus International Mergers and Trade Liberalization
CTN	57.2003	Santiago RUBIO and Alistair ULPH (lxi): An Infinite-Horizon Model of Dynamic Membership of International
		Environmental Agreements
KNOW	58.2003	Carole MAIGNAN, Dino PINELLI and Gianmarco I.P. OTTAVIANO: ICT, Clusters and Regional Cohesion: A
		Summary of Theoretical and Empirical Research
KNOW	59.2003	Giorgio BELLETTINI and Gianmarco I.P. OTTAVIANO: Special Interests and Technological Change
ETA	60.2003	Ronnie SCHÖB: The Double Dividend Hypothesis of Environmental Taxes: A Survey
CLIM	61.2003	Michael FINUS, Ekko van IERLAND and Robert DELLINK: Stability of Climate Coalitions in a Cartel
	0 - 1 - 0 - 0	Formation Game
GG	62.2003	Michael FINUS and Bianca RUNDSHAGEN: How the Rules of Coalition Formation Affect Stability of
00	02.2003	International Environmental Agreements
SIEV	63.2003	Alberto PETRUCCI: Taxing Land Rent in an Open Economy
CLIM	64.2003	Joseph E. ALDY, Scott BARRETT and Robert N. STAVINS: Thirteen Plus One: A Comparison of Global Climate
CLIM	04.2003	Policy Architectures
CIEV	(5.2002	
SIEV	65.2003	Edi DEFRANCESCO: The Beginning of Organic Fish Farming in Italy
SIEV	66.2003	Klaus CONRAD: Price Competition and Product Differentiation when Consumers Care for the Environment
SIEV	67.2003	Paulo A.L.D. NUNES, Luca ROSSETTO, Arianne DE BLAEIJ: Monetary Value Assessment of Clam Fishing
		Management Practices in the Venice Lagoon: Results from a Stated Choice Exercise
CLIM	68.2003	ZhongXiang ZHANG: Open Trade with the U.S. Without Compromising Canada's Ability to Comply with its
		Kyoto Target
KNOW	69.2003	David FRANTZ (lix): Lorenzo Market between Diversity and Mutation
KNOW	70.2003	Ercole SORI (lix): Mapping Diversity in Social History
KNOW	71.2003	Ljiljana DERU SIMIC (lxii): What is Specific about Art/Cultural Projects?
KNOW	72.2003	Natalya V. TARANOVA (lxii): The Role of the City in Fostering Intergroup Communication in a Multicultural
		Environment: Saint-Petersburg's Case
KNOW	73.2003	Kristine CRANE (lxii): The City as an Arena for the Expression of Multiple Identities in the Age of
		Globalisation and Migration
KNOW	74.2003	Kazuma MATOBA (lxii): Glocal Dialogue- Transformation through Transcultural Communication
KNOW	75.2003	Catarina REIS OLIVEIRA (Ixii): Immigrants' Entrepreneurial Opportunities: The Case of the Chinese in
KNOW	13.2003	Portugal
KNOW	76 2002	
KNOW	76.2003	Sandra WALLMAN (Ixii): The Diversity of Diversity - towards a typology of urban systems
KNOW	77.2003	Richard PEARCE (Ixii): A Biologist's View of Individual Cultural Identity for the Study of Cities
KNOW	78.2003	Vincent MERK (lxii): Communication Across Cultures: from Cultural Awareness to Reconciliation of the
******		Dilemmas On the property of the permitted of the permitt
KNOW	79.2003	Giorgio BELLETTINI, Carlotta BERTI CERONI and Gianmarco I.P.OTTAVIANO: Child Labor and Resistance
		to Change
ETA	80.2003	Michele MORETTO, Paolo M. PANTEGHINI and Carlo SCARPA: Investment Size and Firm's Value under
		Profit Sharing Regulation

IEM	81.2003	Alessandro LANZA, Matteo MANERA and Massimo GIOVANNINI: Oil and Product Dynamics in International
CLIM	82.2003	Petroleum Markets Y. Hossein FARZIN and Jinhua ZHAO: Pollution Abatement Investment When Firms Lobby Against
CLIM	62.2003	Environmental Regulation
CLIM	83.2003	Giuseppe DI VITA: Is the Discount Rate Relevant in Explaining the Environmental Kuznets Curve?
CLIM	84.2003	Reyer GERLAGH and Wietze LISE: Induced Technological Change Under Carbon Taxes
NRM	85.2003	Rinaldo BRAU, Alessandro LANZA and Francesco PIGLIARU: How Fast are the Tourism Countries Growing?
		The cross-country evidence
KNOW	86.2003	Elena BELLINI, Gianmarco I.P. OTTAVIANO and Dino PINELLI: The ICT Revolution: opportunities and risks
		for the Mezzogiorno
SIEV	87.2003	Lucas BRETSCGHER and Sjak SMULDERS: Sustainability and Substitution of Exhaustible Natural Resources.
CLIM	88.2003	How resource prices affect long-term R&D investments Johan EYCKMANS and Michael FINUS: New Roads to International Environmental Agreements: The Case of
CLIM	88.2003	Global Warming
CLIM	89.2003	Marzio GALEOTTI: Economic Development and Environmental Protection
CLIM	90.2003	Marzio GALEOTTI: Environment and Economic Growth: Is Technical Change the Key to Decoupling?
CLIM	91.2003	Marzio GALEOTTI and Barbara BUCHNER: Climate Policy and Economic Growth in Developing Countries
IEM	92.2003	A. MARKANDYA, A. GOLUB and E. STRUKOVA: The Influence of Climate Change Considerations on Energy
		Policy: The Case of Russia
ETA	93.2003	Andrea BELTRATTI: Socially Responsible Investment in General Equilibrium
CTN	94.2003	Parkash CHANDER: The γ-Core and Coalition Formation
IEM	95.2003	Matteo MANERA and Angelo MARZULLO: Modelling the Load Curve of Aggregate Electricity Consumption
		<u>Using Principal Components</u>
IEM	96.2003	Alessandro LANZA, Matteo MANERA, Margherita GRASSO and Massimo GIOVANNINI: Long-run Models of
CTD I	07.000	Oil Stock Prices
CTN	97.2003	Steven J. BRAMS, Michael A. JONES, and D. Marc KILGOUR: Forming Stable Coalitions: The Process
KNOW	98.2003	<u>Matters</u> John CROWLEY, Marie-Cecile NAVES (lxiii): Anti-Racist Policies in France. From Ideological and Historical
KNOW	98.2003	Schemes to Socio-Political Realities
KNOW	99.2003	Richard THOMPSON FORD (lxiii): Cultural Rights and Civic Virtue
KNOW	100.2003	Alaknanda PATEL (Ixiii): Cultural Diversity and Conflict in Multicultural Cities
KNOW	101.2003	David MAY (lxiii): The Struggle of Becoming Established in a Deprived Inner-City Neighbourhood
KNOW	102.2003	Sébastien ARCAND, Danielle JUTEAU, Sirma BILGE, and Francine LEMIRE (Ixiii): Municipal Reform on the
		Island of Montreal: Tensions Between Two Majority Groups in a Multicultural City
CLIM	103.2003	Barbara BUCHNER and Carlo CARRARO: China and the Evolution of the Present Climate Regime
CLIM	104.2003	Barbara BUCHNER and Carlo CARRARO: Emissions Trading Regimes and Incentives to Participate in
		International Climate Agreements
CLIM	105.2003	Anil MARKANDYA and Dirk T.G. RÜBBELKE: Ancillary Benefits of Climate Policy
NRM	106.2003	Anne Sophie CRÉPIN (lxiv): Management Challenges for Multiple-Species Boreal Forests
NRM	107.2003	Anne Sophie CRÉPIN (lxiv): Threshold Effects in Coral Reef Fisheries
SIEV	108.2003 109.2003	Sara ANIYAR (lxiv): Estimating the Value of Oil Capital in a Small Open Economy: The Venezuela's Example
SIEV	109.2003	Kenneth ARROW, Partha DASGUPTA and Karl-Göran MÄLER(lxiv): Evaluating Projects and Assessing Sustainable Development in Imperfect Economies
NRM	110.2003	Anastasios XEPAPADEAS and Catarina ROSETA-PALMA(lxiv): Instabilities and Robust Control in Fisheries
NRM	111.2003	Charles PERRINGS and Brian WALKER (Ixiv): Conservation and Optimal Use of Rangelands
ETA	112.2003	Jack GOODY (lxiv): Globalisation, Population and Ecology
CTN	113.2003	Carlo CARRARO, Carmen MARCHIORI and Sonia OREFFICE: Endogenous Minimum Participation in
		International Environmental Treaties
CTN	114.2003	Guillaume HAERINGER and Myrna WOODERS: Decentralized Job Matching
CTN	115.2003	Hideo KONISHI and M. Utku UNVER: Credible Group Stability in Multi-Partner Matching Problems
CTN	116.2003	Somdeb LAHIRI: Stable Matchings for the Room-Mates Problem
CTN	117.2003	Somdeb LAHIRI: Stable Matchings for a Generalized Marriage Problem
CTN	118.2003	Marita LAUKKANEN: Transboundary Fisheries Management under Implementation Uncertainty
CTN	119.2003	Edward CARTWRIGHT and Myrna WOODERS: Social Conformity and Bounded Rationality in Arbitrary
CTN	120 2002	Games with Incomplete Information: Some First Results Give him in VERNASCA, Demonstration with Pains Adjustment Control of Product Differentiation
CTN CTN	120.2003	Gianluigi VERNASCA: Dynamic Price Competition with Price Adjustment Costs and Product Differentiation Myrna WOODERS, Edward CARTWRIGHT and Reinhard SELTEN: Social Conformity in Games with Many
CIN	121.2003	Players
CTN	122.2003	Edward CARTWRIGHT and Myrna WOODERS: On Equilibrium in Pure Strategies in Games with Many Players
CTN	123.2003	Edward CARTWRIGHT and Myrna WOODERS: Conformity and Bounded Rationality in Games with Many
	2.2005	Players
	1000	Carlo CARRARO, Alessandro LANZA and Valeria PAPPONETTI: One Thousand Working Papers

NOTE DI LAVORO PUBLISHED IN 2004

IEM	1.2004	Anil MARKANDYA, Suzette PEDROSO and Alexander GOLUB: Empirical Analysis of National Income and
ETA	2.2004	So2 Emissions in Selected European Countries Masahisa FUJITA and Shlomo WEBER: Strategic Immigration Policies and Welfare in Heterogeneous Countries
PRA	3.2004	Adolfo DI CARLUCCIO, Giovanni FERRI, Cecilia FRALE and Ottavio RICCHI: Do Privatizations Boost
		Household Shareholding? Evidence from Italy
ETA	4.2004	Victor GINSBURGH and Shlomo WEBER: Languages Disenfranchisement in the European Union
ETA	5.2004	Romano PIRAS: Growth, Congestion of Public Goods, and Second-Best Optimal Policy
CCMP	6.2004	Herman R.J. VOLLEBERGH: Lessons from the Polder: Is Dutch CO2-Taxation Optimal
PRA PRA	7.2004 8.2004	Sandro BRUSCO, Giuseppe LOPOMO and S. VISWANATHAN (Ixv): Merger Mechanisms Wolfgang AUSSENECC, Request PICILI ER and Alay STOMPER (Ivv): IPO Priving with Poolshuilding and a
		Wolfgang AUSSENEGG, Pegaret PICHLER and Alex STOMPER (lxv): IPO Pricing with Bookbuilding, and a When-Issued Market
PRA	9.2004	Pegaret PICHLER and Alex STOMPER (lxv): Primary Market Design: Direct Mechanisms and Markets
PRA	10.2004	Florian ENGLMAIER, Pablo GUILLEN, Loreto LLORENTE, Sander ONDERSTAL and Rupert SAUSGRUBER (lxv): The Chopstick Auction: A Study of the Exposure Problem in Multi-Unit Auctions
PRA	11.2004	Bjarne BRENDSTRUP and Harry J. PAARSCH (lxv): Nonparametric Identification and Estimation of Multi- Unit, Sequential, Oral, Ascending-Price Auctions With Asymmetric Bidders
PRA	12.2004	Ohad KADAN (lxv): Equilibrium in the Two Player, k-Double Auction with Affiliated Private Values
PRA	13.2004	Maarten C.W. JANSSEN (lxv): Auctions as Coordination Devices
PRA	14.2004	Gadi FIBICH, Arieh GAVIOUS and Aner SELA (lxv): All-Pay Auctions with Weakly Risk-Averse Buyers
PRA	15.2004	Orly SADE, Charles SCHNITZLEIN and Jaime F. ZENDER (lxv): Competition and Cooperation in Divisible
		Good Auctions: An Experimental Examination
PRA	16.2004	Marta STRYSZOWSKA (lxv): Late and Multiple Bidding in Competing Second Price Internet Auctions
CCMP	17.2004	Slim Ben YOUSSEF: R&D in Cleaner Technology and International Trade
NRM	18.2004	Angelo ANTOCI, Simone BORGHESI and Paolo RUSSU (Ixvi): Biodiversity and Economic Growth:
SIEV	19.2004	Stabilization Versus Preservation of the Ecological Dynamics Anna ALBERINI, Paolo ROSATO, Alberto LONGO and Valentina ZANATTA: Information and Willingness to
SILV	17.2004	Pay in a Contingent Valuation Study: The Value of S. Erasmo in the Lagoon of Venice
NRM	20.2004	Guido CANDELA and Roberto CELLINI (lxvii): Investment in Tourism Market: A Dynamic Model of
		Differentiated Oligopoly
NRM	21.2004	Jacqueline M. HAMILTON (Ixvii): Climate and the Destination Choice of German Tourists
NRM	22.2004	Javier Rey-MAQUIEIRA PALMER, Javier LOZANO IBÁÑEZ and Carlos Mario GÓMEZ GÓMEZ (lxvii):
		Land, Environmental Externalities and Tourism Development
NRM	23.2004	Pius ODUNGA and Henk FOLMER (lxvii): <u>Profiling Tourists for Balanced Utilization of Tourism-Based</u> Resources in Kenya
NRM	24.2004	Jean-Jacques NOWAK, Mondher SAHLI and Pasquale M. SGRO (lxvii): Tourism, Trade and Domestic Welfare
NRM	25.2004	Riaz SHAREEF (lxvii): Country Risk Ratings of Small Island Tourism Economies
NRM	26.2004	Juan Luis EUGENIO-MARTÍN, Noelia MARTÍN MORALES and Riccardo SCARPA (Ixvii): Tourism and
		Economic Growth in Latin American Countries: A Panel Data Approach
NRM	27.2004	Raúl Hernández MARTÍN (lxvii): Impact of Tourism Consumption on GDP. The Role of Imports
CSRM	28.2004	Nicoletta FERRO: Cross-Country Ethical Dilemmas in Business: A Descriptive Framework
NRM	29.2004	Marian WEBER (lxvi): Assessing the Effectiveness of Tradable Landuse Rights for Biodiversity Conservation:
NRM	30.2004	an Application to Canada's Boreal Mixedwood Forest Trond BJORNDAL, Phoebe KOUNDOURI and Sean PASCOE (lxvi): Output Substitution in Multi-Species
111111	50.2001	Trawl Fisheries: Implications for Quota Setting
CCMP	31.2004	Marzio GALEOTTI, Alessandra GORIA, Paolo MOMBRINI and Evi SPANTIDAKI: Weather Impacts on
		Natural, Social and Economic Systems (WISE) Part I: Sectoral Analysis of Climate Impacts in Italy
CCMP	32.2004	Marzio GALEOTTI, Alessandra GORIA ,Paolo MOMBRINI and Evi SPANTIDAKI: Weather Impacts on
	22 2004	Natural, Social and Economic Systems (WISE) Part II: Individual Perception of Climate Extremes in Italy
CTN	33.2004	Wilson PEREZ: Divide and Conquer: Noisy Communication in Networks, Power, and Wealth Distribution
KTHC	34.2004	Gianmarco I.P. OTTAVIANO and Giovanni PERI (Ixviii): The Economic Value of Cultural Diversity: Evidence from US Cities
KTHC	35.2004	Linda CHAIB (Ixviii): Immigration and Local Urban Participatory Democracy: A Boston-Paris Comparison
KTHC	36.2004	Franca ECKERT COEN and Claudio ROSSI (lxviii): Foreigners, Immigrants, Host Cities: The Policies of
KIIIC	30.2001	Multi-Ethnicity in Rome. Reading Governance in a Local Context
KTHC	37.2004	Kristine CRANE (lxviii): Governing Migration: Immigrant Groups' Strategies in Three Italian Cities – Rome,
		Naples and Bari
KTHC	38.2004	Kiflemariam HAMDE (lxviii): Mind in Africa, Body in Europe: The Struggle for Maintaining and Transforming
E/E 4	20.2004	Cultural Identity - A Note from the Experience of Eritrean Immigrants in Stockholm Alberta CAVALUEDE, Price Competition with Information Dispersition in a Vertically Differentiated Dynamoly
ETA	39.2004	Alberto CAVALIERE: Price Competition with Information Disparities in a Vertically Differentiated Duopoly
PRA	40.2004	Andrea BIGANO and Stef PROOST: The Opening of the European Electricity Market and Environmental Policy: Does the Degree of Competition Matter?
CCMP	41.2004	Micheal FINUS (lxix): International Cooperation to Resolve International Pollution Problems
CCIVII		moneur 1 11100 (1A1A). International Cooperation to Resolve International Foliation Floriens

KTHO	42.2004	Francesco CRESPI: Notes on the Determinants of Innovation: A Multi-Perspective Analysis
KTHC	43.2004	Sergio CURRARINI and Marco MARINI: Coalition Formation in Games without Synergies
CTN	44.2004	Marc ESCRIHUELA-VILLAR: Cartel Sustainability and Cartel Stability
CTN	45.2004	Sebastian BERVOETS and Nicolas GRAVEL (lxvi): Appraising Diversity with an Ordinal Notion of Similarity:
NRM	43.2004	An Axiomatic Approach
NRM	46.2004	Signe ANTHON and Bo JELLESMARK THORSEN (lxvi): Optimal Afforestation Contracts with Asymmetric
TUCH		Information on Private Environmental Benefits
NRM	47.2004	John MBURU (lxvi): Wildlife Conservation and Management in Kenya: Towards a Co-management Approach
NRM	48.2004	Ekin BIROL, Ágnes GYOVAI and Melinda SMALE (lxvi): Using a Choice Experiment to Value Agricultural
		Biodiversity on Hungarian Small Farms: Agri-Environmental Policies in a Transition al Economy
CCMP	49.2004	Gernot KLEPPER and Sonja PETERSON: The EU Emissions Trading Scheme. Allowance Prices, Trade Flows,
	50.2004	Competitiveness Effects
GG	50.2004	Scott BARRETT and Michael HOEL: Optimal Disease Eradication
CTN	51.2004	Dinko DIMITROV, Peter BORM, Ruud HENDRICKX and Shao CHIN SUNG: Simple Priorities and Core
CIEV	52.2004	Stability in Hedonic Games Francesco RICCI: Channels of Transmission of Environmental Policy to Economic Growth: A Survey of the
SIEV	32.2004	Theory
SIEV	53.2004	Anna ALBERINI, Maureen CROPPER, Alan KRUPNICK and Nathalie B. SIMON: Willingness to Pay for
SIL V		Mortality Risk Reductions: Does Latency Matter?
NRM	54.2004	Ingo BRÄUER and Rainer MARGGRAF (lxvi): Valuation of Ecosystem Services Provided by Biodiversity
		Conservation: An Integrated Hydrological and Economic Model to Value the Enhanced Nitrogen Retention in
		Renaturated Streams
NRM	55.2004	Timo GOESCHL and Tun LIN (lxvi): Biodiversity Conservation on Private Lands: Information Problems and
NRM	56.2004	Regulatory Choices Tom DEDEURWAERDERE (lxvi): Bioprospection: From the Economics of Contracts to Reflexive Governance
		· / - · ·
CCMP	57.2004	Katrin REHDANZ and David MADDISON: The Amenity Value of Climate to German Households
CCMP	58.2004	Koen SMEKENS and Bob VAN DER ZWAAN: Environmental Externalities of Geological Carbon Sequestration
	50.00.	Effects on Energy Scenarios
NRM	59.2004	Valentina BOSETTI, Mariaester CASSINELLI and Alessandro LANZA (Ixvii): Using Data Envelopment
NRM	60.2004	Analysis to Evaluate Environmentally Conscious Tourism Management Timo GOESCHL and Danilo CAMARGO IGLIORI (lxvi):Property Rights Conservation and Development: An
INIXIVI	00.2004	Analysis of Extractive Reserves in the Brazilian Amazon
CCMP	61.2004	Barbara BUCHNER and Carlo CARRARO: Economic and Environmental Effectiveness of a
		Technology-based Climate Protocol
NRM	62.2004	Elissaios PAPYRAKIS and Reyer GERLAGH: Resource-Abundance and Economic Growth in the U.S.
NRM	63.2004	Györgyi BELA, György PATAKI, Melinda SMALE and Mariann HAJDÚ (lxvi): Conserving Crop Genetic
		Resources on Smallholder Farms in Hungary: Institutional Analysis
NRM	64.2004	E.C.M. RUIJGROK and E.E.M. NILLESEN (lxvi): The Socio-Economic Value of Natural Riverbanks in the
		Netherlands
NRM	65.2004	E.C.M. RUIJGROK (lxvi): Reducing Acidification: The Benefits of Increased Nature Quality. Investigating the
ET A	((2004	Possibilities of the Contingent Valuation Method
ETA	66.2004	Giannis VARDAS and Anastasios XEPAPADEAS: <u>Uncertainty Aversion</u> , Robust Control and Asset Holdings

- (lix) This paper was presented at the ENGIME Workshop on "Mapping Diversity", Leuven, May 16-17, 2002
- (lx) This paper was presented at the EuroConference on "Auctions and Market Design: Theory, Evidence and Applications", organised by the Fondazione Eni Enrico Mattei, Milan, September 26-28, 2002
- (lxi) This paper was presented at the Eighth Meeting of the Coalition Theory Network organised by the GREQAM, Aix-en-Provence, France, January 24-25, 2003
- (lxii) This paper was presented at the ENGIME Workshop on "Communication across Cultures in Multicultural Cities", The Hague, November 7-8, 2002
- (lxiii) This paper was presented at the ENGIME Workshop on "Social dynamics and conflicts in multicultural cities", Milan, March 20-21, 2003
- (lxiv) This paper was presented at the International Conference on "Theoretical Topics in Ecological Economics", organised by the Abdus Salam International Centre for Theoretical Physics ICTP, the Beijer International Institute of Ecological Economics, and Fondazione Eni Enrico Mattei FEEM Trieste, February 10-21, 2003
- (lxv) This paper was presented at the EuroConference on "Auctions and Market Design: Theory, Evidence and Applications" organised by Fondazione Eni Enrico Mattei and sponsored by the EU, Milan, September 25-27, 2003
- (lxvi) This paper has been presented at the 4th BioEcon Workshop on "Economic Analysis of Policies for Biodiversity Conservation" organised on behalf of the BIOECON Network by Fondazione Eni Enrico Mattei, Venice International University (VIU) and University College London (UCL), Venice, August 28-29, 2003
- (lxvii) This paper has been presented at the international conference on "Tourism and Sustainable Economic Development Macro and Micro Economic Issues" jointly organised by CRENoS (Università di Cagliari e Sassari, Italy) and Fondazione Eni Enrico Mattei, and supported by the World Bank, Sardinia, September 19-20, 2003
- (lxviii) This paper was presented at the ENGIME Workshop on "Governance and Policies in Multicultural Cities", Rome, June 5-6, 2003
- (lxix) This paper was presented at the Fourth EEP Plenary Workshop and EEP Conference "The Future of Climate Policy", Cagliari, Italy, 27-28 March 2003

2003 SERIES

CLIM Climate Change Modelling and Policy (Editor: Marzio Galeotti)

GG Global Governance (Editor: Carlo Carraro)

SIEV Sustainability Indicators and Environmental Valuation (Editor: Anna Alberini)

NRM Natural Resources Management (Editor: Carlo Giupponi)

KNOW Knowledge, Technology, Human Capital (Editor: Gianmarco Ottaviano)

IEM International Energy Markets (Editor: Anil Markandya)

CSRM Corporate Social Responsibility and Management (Editor: Sabina Ratti)

PRIV Privatisation, Regulation, Antitrust (Editor: Bernardo Bortolotti)

ETA Economic Theory and Applications (Editor: Carlo Carraro)

CTN Coalition Theory Network

2004 SERIES

CCMP Climate Change Modelling and Policy (Editor: Marzio Galeotti)

GG Global Governance (Editor: Carlo Carraro)

SIEV Sustainability Indicators and Environmental Valuation (Editor: Anna Alberini)

NRM Natural Resources Management (Editor: Carlo Giupponi)

KTHC Knowledge, Technology, Human Capital (Editor: Gianmarco Ottaviano)

IEM International Energy Markets (Editor: Anil Markandya)

CSRM Corporate Social Responsibility and Management (Editor: Sabina Ratti)

PRA Privatisation, Regulation, Antitrust (Editor: Bernardo Bortolotti)

ETA Economic Theory and Applications (Editor: Carlo Carraro)

CTN Coalition Theory Network