ECONSTOR
Make Your Publications Visible.

A Service of

ZBW Leibniz-Informationszentrum Wirtschaft
Leibniz Information Centre for Economics

Delgado, Ana Paula; Godinho, Isabel Maria

Conference Paper

Long Term Evolution of the Size Distribution of Portuguese Cities

45th Congress of the European Regional Science Association: "Land Use and Water Management in a Sustainable Network Society", 23-27 August 2005, Amsterdam, The Netherlands

Provided in Cooperation with:

European Regional Science Association (ERSA)

Suggested Citation: Delgado, Ana Paula; Godinho, Isabel Maria (2005) : Long Term Evolution of the Size Distribution of Portuguese Cities, 45th Congress of the European Regional Science Association: "Land Use and Water Management in a Sustainable Network Society", 23-27 August 2005, Amsterdam, The Netherlands, European Regional Science Association (ERSA), Louvain-la-Neuve

This Version is available at:
https://hdl.handle.net/10419/117831

Standard-Nutzungsbedingungen:

Die Dokumente auf EconStor dürfen zu eigenen wissenschaftlichen Zwecken und zum Privatgebrauch gespeichert und kopiert werden.

Sie dürfen die Dokumente nicht für öffentliche oder kommerzielle Zwecke vervielfältigen, öffentlich ausstellen, öffentlich zugänglich machen, vertreiben oder anderweitig nutzen.

Sofern die Verfasser die Dokumente unter Open-Content-Lizenzen (insbesondere CC-Lizenzen) zur Verfügung gestellt haben sollten, gelten abweichend von diesen Nutzungsbedingungen die in der dort genannten Lizenz gewährten Nutzungsrechte.

Terms of use:

Documents in EconStor may be saved and copied for your personal and scholarly purposes.

You are not to copy documents for public or commercial purposes, to exhibit the documents publicly, to make them publicly available on the internet, or to distribute or otherwise use the documents in public.

If the documents have been made available under an Open Content Licence (especially Creative Commons Licences), you may exercise further usage rights as specified in the indicated licence.

WWW.ECONSTOR.EU

Mitglied der Leibniz-Gemeinschaft

45th Congress of the European Regional Science Association
23-27 August 2005, Vrije Universiteit Amsterdam
Land Use and Water Management in a Sustainable Network Society

LONG TERM EVOLUTION OF THE SIZE DISTRIBUTION OF PORTUGUESE CITIES

Ana Paula Delgado[a]

Isabel Maria Godinho[b]

Abstract

In this paper we study the evolution of the Portuguese urban system from 1864 to 2001. We apply the rank-size model and use rank-size estimates to describe the evolution of city-size hierarchy.

Non paretian behavior of the distribution is examined by adding a quadratic term to the basic equation of the model. Our results enhance two different processes in the evolution of urban system: until the middle of the twentieth century urban growth was accompanied by population concentration in the largest cities; afterwards growth benefits middle size cities, reinforced in the last decades by heavy population losses in the two largest cities.

From the association between the characteristics and evolving pattern of city size distribution and the spatial pattern of urban growth, it appears that the non paretian behavior of city size distribution in the last decades can be linked to the particular growth process of cities located in the proximity of the central cities of the two metropolitan areas of Portugal's mainland.

In order to obtain a better understanding of the dynamics of the Portuguese urban system we examine the movements in the ranking of cities, through a Markov chain process. We also analyze the existence of spatial correlation in the process of urban hierarchy restructuring.

Keywords: Urban hierarchy, rank-size distribution, urban growth, Markov processes

JEL classification: O18, R11, R12

On going work – do not quote

[a] CEDRES / Faculdade de Economia do Porto, Rua Dr. Roberto Frias, 4200-464 Porto, Portugal.
Fax: + 351 225 505 050 E-mail: apaula@fep.up.pt
[b] CEDRES and Escola Secundária de Oliveira Martins, Rua Major David Magno, 4000-191 Porto, Portugal.
E-mail: isa_godinho@hotmail.com

We thank our colleague Rui Alves for helping us compute the ergodic probabilities.

1. Introduction

The aim of this paper is to analyse the long term evolution of the Portuguese urban system, from 1864 to 2001. Studies in this vein have been conducted, for example, by Guérin-Pace (1995) for France, Eaton and Eckstein (1997) for France and Japan, Dobkins and Ioannides (2000), Black and Henderson (2003) for the USA and by Lanaspa et al. (2003) for Spain. All of them revisit the rank-size model, which has been recognized as one of those stylized facts in spatial economics, existing a general acceptance of that model as a good synthetic description of the hierarchical organization of urban systems.

In a previous paper we have provided empirical evidence for the evolution of the rank size exponent and examined the effect of varying city size cut-offs on its estimated value. We studied further the deviations of the rank size distribution from linearity, which is seen as a violation of Gibrat's Law, since in order to generate a log-normal distribution, city growth rates must be independent of initial city size and also independence from one period to another. We concluded that, in Portugal, more than the relationship between size and growth rates, deviation from linearity seemed to arise from autocorrelation in successive growth rates. From our results, we detected a pattern of urban growth characterised by concentration of population in the early phases of the period considered, followed by a decrease in concentration that appeared to result, in the last decades, from a process of selective growth beneficial to the same cities, in particular those that are closer to the central cities of the metropolitan areas of Lisboa and Porto. In this paper we develop that study and take a Markov chain process to describe mobility of cities within city size distribution, examining also the existence of spatial autocorrelation in the movements of cities.

In section 2 we present and compare the datasets that we employ and discuss some of the drawbacks arising from the concepts of urban unit that are used. In the following section we apply the rank size model to the analysis of evolution of the Portuguese urban system. We start by a brief characterisation of that system, enhancing its specific traits. We then use a Pareto distribution to estimate, in each census date, the size distribution of cities. We discuss slope sensitivity to sample threshold and to urban definition. We extend the rank size model by adding a quadratic term to the basic equation and analyse the long term evolution of the estimated parameter and the sensibility of this estimates to sample threshold. In section 4, we applied a Markov chain process to describe the inter-census movements of cities within the distribution. We compute year to year transition matrix, from which we calculate the average transition matrix and the associated ergodic probability vector.

In section 5, we study the spatial pattern of movements within the distribution between 1864 and 1991. Since, during the more than a century period of our analysis, an important number of upward or downward movements occur and as there seems to occur a spatial pattern in these movements, we test for spatial autocorrelation. Finally in the last section we present the main conclusions.

2. Description of the data set

Studies on urban hierarchy and rank size distribution are contingent on the definition of the unit of analysis. Thus, the characteristics of the urban system resulting from the analysis of the rank-size parameter estimates depend on the definition of urban units. From a theoretical perspective the adequate definition would be one considering the urban place as an integrated economic and functional unit. But as a rule, researchers are constrained by the lack of appropriate data.

Another problem concerns the definition of urban units and its consistency over time. In this paper we use two city-proper databases for mainland Portugal, where cities are defined according to administrative criteria. A drawback with a sample based on administrative definitions is that city boundaries may not coincide with functional and economical boundaries of urban places. However, applying city definitions to prior decades in a single country study, instead of contemporaneous administrative definitions, minimizes the problem of city definition and that of building consistent definitions over time[1].

Portugal is a country with long established national borders whose mainland urban system dates back to some centuries ago: many of the cities have several hundred years and a number of them are even older than the nation. Through time some of the older cities may have lost population and various urban functions. Still, they retain their administrative status. On the other side, in early dates, some cities had zero population or were too small to be considered urban units. So, in order to define whether a place qualifies as a city, we use an absolute cut-off of 2000 inhabitants, in each census date.

The data set for the 1864-1991 period was developed by Albergaria (1999) and uses a consistent definition of cities, calculating the population for each city and each census using the 1998's administrative cities. In order to analyze the recent evolution of the urban system, we use another city proper database[2], for the 1991-2001 period. This last database uses the 2001 administrative classification of cities. As a consequence the number of cities, for 1991, grows from

[1] We must note that in Portugal, as in many other countries, data constraints do not allow alternative approaches to city definition over time.

[2] This data base was built by Ferreira, Cardoso and Silva (2003) based on INE (2002) - Instituto Nacional de Estatística (INE) / National Statistics Institute

111 to 123 and, as we observed inconsistency between the two data sets, we considered them separately.

In sum, our sample obeys to two criteria: 1) urban places which have in 1998 or 2001 the administrative status of "city"; and 2) have at least 2000 inhabitants, in each census date.

For the 1991-2001 period we also analyse the sensibility of the results to the definition of urban units, using data supplied by INE and referring to urban places[3], with at least 2 000 inhabitants. Differences between city proper and urban place databases arise mainly from the criteria that a place must observe in order to qualify as a city[4] and are reflected in the size of both data sets. In fact, for urban places database, the number of urban units rises to 450, in 1991, and 531, in 2001.

3. Rank-size evolution of the Portuguese urban system

3.1. Some basic facts about Portuguese urban system

The Portuguese urban system is characterized by a large number of very small cities – 50% of the cities had, in 1991, less than 14000 inhabitants - and two dominant cities which are the central cities of Portugal's two metropolitan areas (Table 1). The long term evolution shows a slow increase in the number of cities, between 1864 and 1991, while city population more than quadruplicates in the same period. As a consequence, average city size increased from 8829 inhabitants, in 1864, to 29087, in 1991. In general, urban population grew faster than total population and the urbanization rate[5], although moderate, increased from around 19%, in 1864, to 34% in 1991.

The growth of urban population is faster than that of the number of cities, suggesting an urbanization process characterized above all by population concentration in existing cities. This process of concentration favors the two main cities, Lisboa and Porto. After 1940, the decline in the primacy index[6] portrays a process of decentralization of urban growth, reinforced in the last decades by heavy population losses in the central cities of the Lisboa and Porto metropolitan areas. However, in 2001, 57% of the Portuguese urban population lived in the 28 cities that belong to the metropolitan areas of Lisboa and Porto.

[3] Places are defined as continuous built up areas with at least 10 or more dwellings and having an own assignment, independently of belonging or not the same basic administrative unit of the country ("freguesia").
[4] Nowadays in order to qualify as a city, places must have at least 8000 voters and possess a certain minimum set of functions and social infrastructure; the acquisition of that administrative status depends also on political criteria.
[5] Defined as the ratio of total city population (urban population) to total population, in a given year, expressed in percentage.
[6] Defined as the ratio of resident population in top two cities to total urban population, expressed in percentage.

Table 1 - Basic data about Portuguese Urban System (Full sample), 1864-2001

Data Source	Census date	Number of Cities	Average size	Median Size	Minimum Size	Maximum Size	Urban Population	Urbanization rate (%)	Top Two Primacy Index (%)
Albergaria data base	1864	85	8829	4563	2013	190311	750496	18,83	37,26
	1890	91	11791	5469	2172	300964	1072970	23,02	41,70
	1900	97	12397	5815	2044	351210	1202476	24,05	43,07
	1920	101	14688	6851	2054	484664	1483455	26,17	46,31
	1940	105	19502	9277	2075	694389	2047756	28,37	46,54
	1950	108	21571	9755	2009	783226	2329644	29,41	45,70
	1960	109	23278	10206	2092	802230	2537248	30,60	43,58
	1970	108	25057	10520	2141	769044	2706118	33,31	39,73
	1981	110	29637	12457	2189	807937	3260069	34,92	34,82
	1991	110	29087	13248	2789	663394	3199601	34,14	30,19
Atlas Data base	1991	122	29546	13638	2487	661966	3604563	38,46	26,65
	2001	122	30895	15382	2578	564657	3769214	38,19	21,96

Source: Delgado and Godinho, 2004:9

The image of the Portuguese urban system portrayed by the urban places data set is quite different (Table 2). Urbanization rate, in 2001, rises from 38% to 55% when we consider urban places instead of administrative cities. As expected, the top two primacy index decreases[7]. The number of urban units is substantially higher, with an average size around 10000 inhabitants that is about one third of the average size for the Atlas data base. These differences can be imputed to the legal requirements that a place must fulfill in order to qualify as a city. However as Carter (1981: 20) points out: *"In older countries many towns which have long decayed retain their former status and chartered rights and fight energetically to maintain them; likewise newly grown towns find it a lengthy and cumbersome process to obtain the articles of recognition."* As a consequence, although the Atlas data base contains urban units that do not conform to the size implicit criteria of 8000 voters, the relative importance of very small towns is lower.

The effect of urban definition in sample size is drastic: when we consider a 5000 inhabitants threshold we lose more than sixty percent of the number of urban units in the 2000 inhabitants sample for the urban places data set, whereas for the Atlas data set the reduction in the sample size is less than 10% of the initial size. On the other hand, the effectiveness of *bureaucratic* and political barriers to access city status reflects in the fact that, for the 10000 inhabitants threshold, the number of urban units is significantly higher when we consider the urban place data set.

[7] We must note that in both data sets the two top urban units (Lisboa and Porto) have roughly the same size. In fact, in both cases, urban place and administrative city are synonymous.

Table 2 - Basic data about Portuguese urban places, 1991-2001

Data Source	Census date	Number of Cities	Average size	Median Size	Minimum Size	Maximum Size	Urbanization rate (%)	Top two primacy index (%)
INE Urban Places	1991	450	10103	3934	2004	662782	48,51	21,23
	2001	531	10270	4323	2001	563818	55,26	15,16

3.2. The rank-size model

According to the rank-size model, the size distribution of cities follows a Pareto distribution:

(1) $R_{it} = AP_{it}^{-a}$ or, in logarithmic form, (1') $\log R_{it} = \log A - a \log P_{it}$

where R_{it} is the rank of the ith city in time period t, P_{it} is the size (population) of the ith city in time period t, A is a constant and a is the Pareto/Zipf's exponent. This formulation is known as the Pareto equation[8].

City size distribution is then characterised by the number of cities and two parameters: the exponent (a) and the constant term (A). The exponent is a measure of city size inequality in a given urban system and time period. Using Pareto's formulation, when $a > 1$ the rank-size curve is flatter and city sizes are more evenly distributed than that predicted by Zipf's law ($a = 1$). In particular, considering the limiting value of $a \to \infty$ all cities would have the same size. On the other hand, when $0 < a < 1$, the rank-size curve becomes steeper. In this case, urban hierarchy is more contrasted than in Zipf's case and cities in the top of the hierarchy are larger. Here we obtain a more heterogeneous distribution of city sizes. In the limiting case of $a \to 0$, there would be just one city in the urban system.

3.3.The long-term evolution of city size distribution: 1864-2001

To study the long term evolution of city size distribution, we began by constructing a rank-size graph, observing how the shape of that distribution evolved through time. Next we estimated the rank size model by ordinary least squares (OLS) and analyse the long term evolution of slope

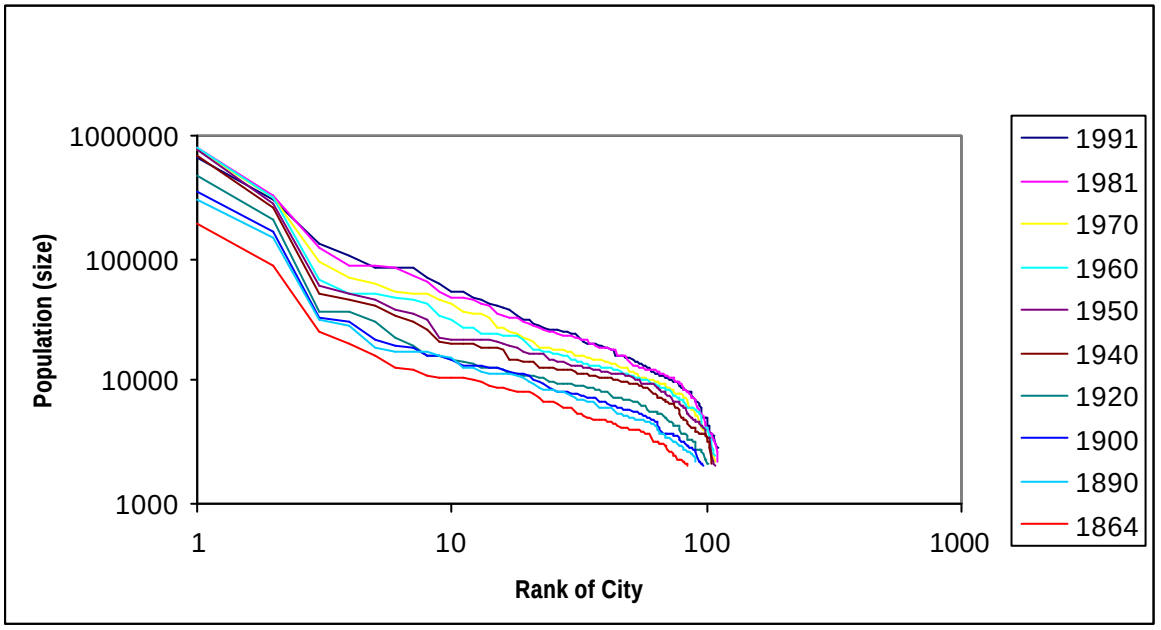
[8] Another formulation is that of Lotka (1924), which is given by the following equation: $P_{it} = BR_{it}^{-\beta}$ or, in logarithmic form, $\log P_{it} = \log B - b \log R_{it}$ where B is a constant and $ß$ is the inverse of Pareto exponent. The two formulations can further be related to as $B = A^{ß}$.

estimates and the sensibility of these estimates to sample threshold. Then we study the deviations from rank-size linearity, following the approach of Rosen and Resnick (1980).

The rank-size graph[9]

From Figure 1 we can conclude that, on the whole, the shape of the rank-size distribution has remained stable until the eighties, shifting up in the course of time, as a result of urban growth. This does not mean that individual city ranking has remained unchanged; in fact, excluding Lisboa and Porto, cities relative position in urban hierarchy has changed. The rank-size graph shows a significant increase in its height and a slight enlargement in the bottom. This result points to an urban growth process characterized by a considerable growth in the size of the largest city and a slow increase in the number of cities. Generally, the rank-size line shows an upward concavity between the 3rd and the 20th city, as a consequence of the under-dimension of middle size cities. It presents also a downward concavity in the lower tail of the distribution, translating the excess of small cities.

Figure 1 – Rank-size distributions of Portuguese cities, 1864-1991: Full sample

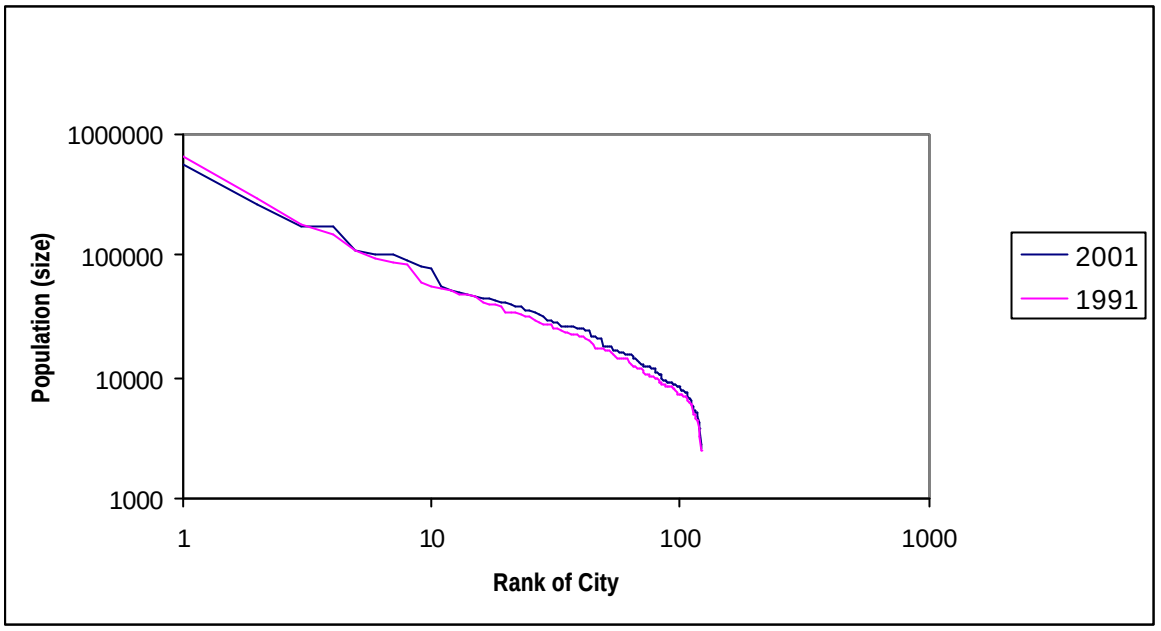


Source: Delgado and Godinho, 2004:11

In the last decade, we denote a downward counter clockwise movement of the rank-size line, due to the decline in the size of the two largest cities. There is a more even distribution of city sizes, as the two top cities have lost population, whereas middle size cities have experienced population gains and the dimension of the smallest cities in our sample has remained roughly stable (Figure 2).

[9] We must note that the graph refers to Lotka's formulation.

Figure 2 - Rank-size distributions of Portuguese cities, 1991-2001: Full sample (Atlas)



Source: Delgado and Godinho, 2004:11

Results from the estimation of the model

The estimation of the rank-size model requires the ordering of cities from the largest down to the smallest. We applied OLS to equation 1'. In order to examine the sensibility of the slope estimates to the choice of sample threshold we defined several sample cut-offs, chosen taking into account the dimension of the Portuguese city system[10] and current cut-offs for urban definition in the Portuguese statistical system. The estimates of rank-size parameters are all statistically significant at 5% significance level. The quality of the adjustment is quite good, since R^2 are high and close to unity (Table 3).

When the entire distribution is used, from 1864 till 1960, the slope is higher than one and decreasing, indicating that city size distribution is, at the beginning of the period, more evenly distributed than predicted by Zipf's law, becoming increasingly divergent and resulting in a more contrasted urban hierarchy. From 1970 onwards a is less than one and tends to decrease. However, in the last two decades, we observe a reverse in that tendency, reflecting a process of decreasing inequality.

[10] We did not consider sample thresholds of at least 50 000 inhabitants or higher because the number of cities obeying that criteria is too small.

Table 3 - Results of OLS estimation, 1864-2001

Data base	Census Date	Cities with 2000 inhs. or more			Cities with 5000 inhs. or more		
		Number of cities	Slope	R^2	Number of cities	Slope	R^2
Albergaria	1864	85	1,189	0,946	35	1,081	0,895
	1890	91	1,120	0,947	51	1,105	0,911
	1900	97	1,098	0,936	58	1,127	0,901
	1920	101	1,082	0,907	69	1,140	0,878
	1940	105	1,061	0,908	80	1,158	0,897
	1950	108	1,022	0,899	88	1,155	0,915
	1960	109	1,026	0,921	95	1,144	0,946
	1970	108	0,963	0,927	92	1,113	0,966
	1981	110	0,937	0,931	97	1,073	0,973
	1991	110	0,953	0,947	100	1,054	0,979
Atlas	1991	122	0,970	0,961	112	1,050	0,988
	2001	122	0,977	0,950	115	1,051	0,977
Data base	Census Date	Cities with 10000 inhs. or more			Cities with 20000 inhs. or more		
		Number of cities	Slope	R^2	Number of cities	Slope	R^2
Albergaria	1864	12	0,761	0,919	4	0,557	0,949
	1890	19	0,839	0,875	4	0,495	0,917
	1900	21	0,842	0,862	5	0,500	0,932
	1920	23	0,806	0,881	6	0,517	0,928
	1940	45	1,006	0,874	11	0,632	0,924
	1950	53	1,069	0,879	16	0,726	0,896
	1960	57	1,089	0,917	19	0,813	0,882
	1970	59	1,094	0,955	21	0,894	0,931
	1981	75	1,132	0,978	36	1,066	0,959
	1991	73	1,130	0,989	36	1,107	0,979
Atlas	1991	77	1,120	0,993	42	1,138	0,989
	2001	85	1,152	0,991	48	1,221	0,989

This results must be interpreted with caution as Portugal has an urban system with primatial characteristics. For instance, if we take the 1991 city size distribution in the Albergaria's database and compare the observed sizes with the expected size of equivalent rank for a top city of 663394 inhabitants and $\alpha = 1$, all the cities from the 2nd to the 25th rank are under-dimensioned. In particular, population deficit is more notorious for cities ranking from the 3rd to 10th position. The opposite situation occurs from the 26th until the 87th position, where cities are bigger than expected. Finally, for all the remaining positions in the bottom of the distribution, cities are smaller than predicted by rank-size rule – some of them having less than 50% of their expected population.

When smaller cities are excluded (sample thresholds of 10000 inhabitants or more), slope estimates tend to increase over time, starting from values lesser than one, indicating a reduction in city size inequality. This distinct evolution, in comparison with the full sample, mirrors the changes

in growth behavior of middle sized cities vis-à-vis the first city. At the beginning of our study period intermediate cities, in the class size of 30000-100000 inhabitants, developed more slowly than Lisboa, growing at a faster rate, after the fifties.

Since we are studying the long term evolution of the urban system an absolute cut-off does not account for the change in typical city size with the urbanization process. So we consider an upper tail distribution which includes cities in the top one third of size distribution, in each census date, and re-estimated the model (Table 4). Slope estimates exhibit a long term U shaped pattern, with a minimum value in 1920-1940, indicating an urbanization process characterized by increasing city size inequality, for the upper tail distribution, until the middle of the last century. Afterwards, the reversing of the tendency points to a diminishing inequality, reinforced in the last decades.

Table 4 - Results of OLS estimation: upper 1/3 of the cities, 1864-2001

Data base	Census Date	Top third - upper 1/3 of cities			
		Number of cities	Minimum size	Slope	R^2
Albergaria	1864	28	6046	1,020	0,882
	1890	30	7156	0,969	0,886
	1900	32	7591	0,962	0,877
	1920	34	8798	0,924	0,857
	1940	35	10802	0,927	0,884
	1950	36	12307	0,949	0,882
	1960	36	13091	0,969	0,909
	1970	36	14837	0,998	0,946
	1981	37	19318	1,071	0,960
	1991	37	19990	1,110	0,980
Atlas	1991	41	21416	1,135	0,989
	2001	41	24481	1,209	0,988

The sensibility of the slope estimates to sample cut-offs is well illustrated in Figure 3, and is higher in the beginning of the observation period. From 1864 to the middle of the 20th century, as sample threshold increases slope estimates decrease and differences are more important for higher sample cut-offs. The distribution gets more uneven as we impose higher thresholds. For the last decades, slope estimates tend to increase with the sample threshold.

In conclusion, in the first part of the period smaller cities tend to generate a more even distribution whereas in the last decades the rise in a values with sample threshold seem to indicate that medium and larger cities are the source of a more equal distribution. This tendency is also evident when we confront the full sample with the upper tail distribution (Figure 4).

Figure 3 – Sensibility of slope estimates to sample threshold

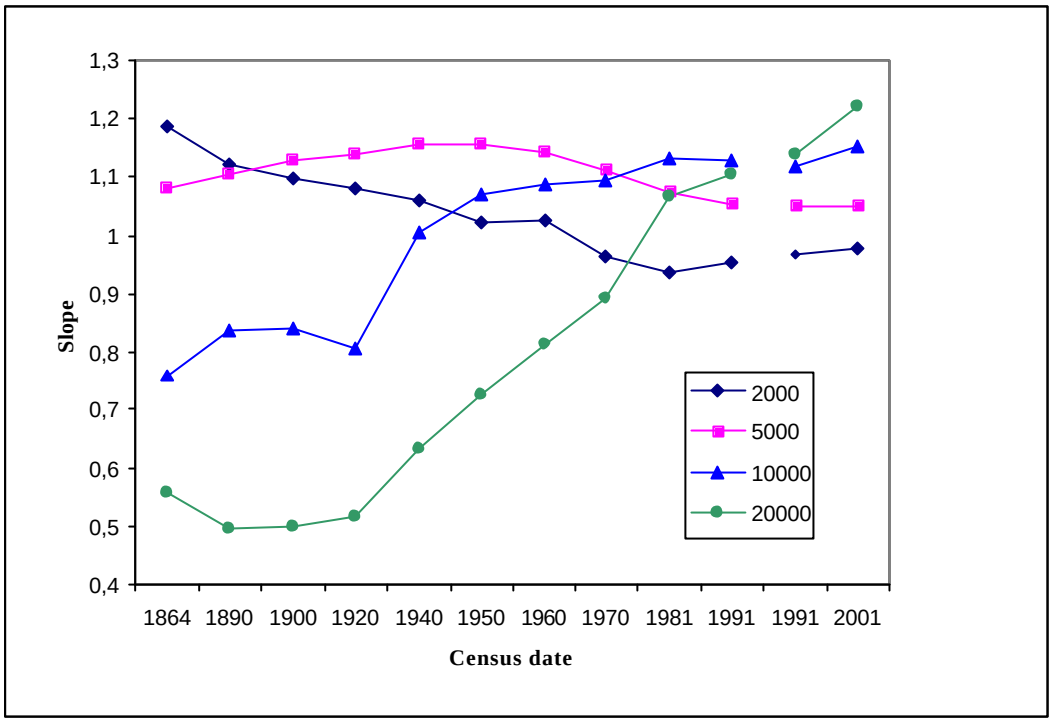
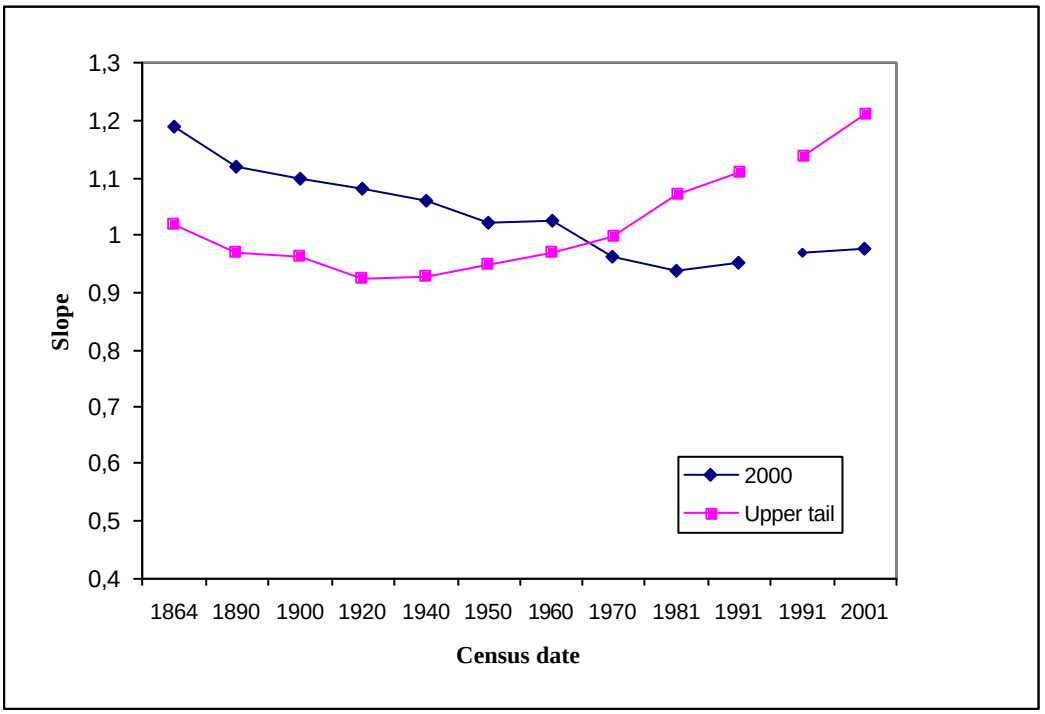


Figure 4- Sensibility of slope estimates: full sample versus upper 1/3 of cities



Deviations from rank-size regularity

The fact that slope estimates are sensitive to sample size signals a non-paretian behaviour of the distribution. Therefore, we examine the deviations of the rank-size distribution from linearity by adding a quadratic term to equation 1', following the standard approach in literature. Thus, we estimate the following equation:

$$(2) \quad log\, R_{it} = a + b\, log\, P_{it} + c(log\, P_{it})^2 \ .$$

The value of the parameter *c* characterises the curvature: when *c*>0, the rank-size curve is strictly convex (upward concavity) and when *c*<0 it is strictly concave (downward concavity). An upward concavity is obtained when the city size distribution has a smaller number of middle-sized cities than predicted by Zipf's Law. In this case, there is a deficit of intermediate cities in favour of largest cities dimension or the number of small cities. A downward concavity means that there is a larger number of middle-sized cities than expected. In this case, there is an excess of intermediate cities relatively to the dimension of the largest cities or to the number of small cities. In rank-size distributions with an upward concavity, the largest city will be larger and smaller cities will be more numerous than expected in a linear relationship between the logarithm of city size and the logarithm of its order. On the other hand, in rank-size distributions with a downward concavity, middle-sized cities are larger than expect in a linear relationship between the logarithms of size and order.

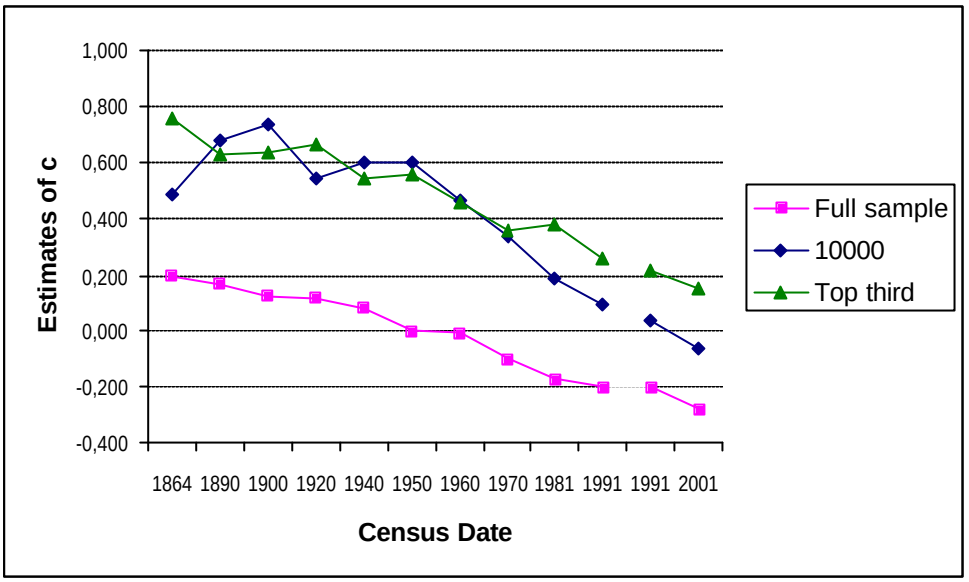
The long term evolution of parameter *c* is depicted in Figure 7.[11] Considering the full sample, until the middle of the 20th century, urban growth favours the largest cities. In 1950 and 1960, the value of *c* is not significantly different from zero meaning that the rank-size distribution tends to conform to linearity. From 1970 onwards, the value of the quadratic parameter is negative reflecting the growth of middle-sized cities, reinforced in the last decades. When we exclude small cities from the sample (10 000 inhabitants and upper tail distributions), the estimates of *c* remain positive for the 1864-1991 period indicating that middle-sized cities are smaller than expected in a linear relationship. Since *c* is decreasing, this characteristic is less accentuated in recent years, signifying that urban growth has been concentrated in cities of that size class.

Our results for the long term evolution of *c* are similar to those of Guérin-Pace's for France in 1831-1990 period and the 2000 inhabitant's threshold; but they differ from those of Moriconi-Ébrard (1993), for 1981, and Soo (2002), for 2001[12], reinforcing the idea that the estimates of *c* are sensitive to city and threshold definition. In fact, Moriconi-Ébrard (1993) uses urban agglomerations

[11] The estimates of *c* parameter are all statistically significant at 5% significance level, except in 1950 and 1960, for the full sample, and for the 10 000 inhabitants threshold in 1991 (Atlas database).
[12] In both studies c is positive: 0,468 (Moriconi-Ébrard) and 0, 124 (Soo).

with at least 10000 inhabitants, while Soo (2002) uses Brinkhoff's data base,[13] with a threshold of 15000 inhabitants.

Figure 5 - Long term evolution of *c* estimates

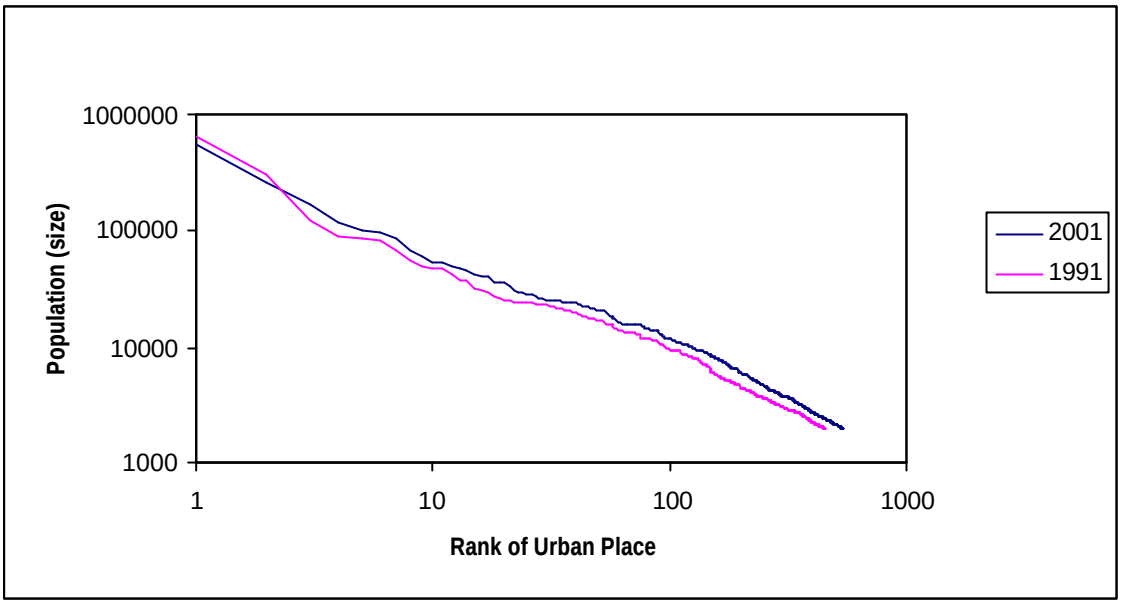


3.4.Comparative analysis of rank size distribution: cities *versus* urban places in the nineties

The proliferation of very small cities in the urban places data base, reflected on a median size about 28% of the corresponding value for the Atlas data base, results on a rank-size distribution for urban places that is more scattered than the one that we have obtained when considering cities (Figure 6). As for the Atlas data base, the heavy population losses of Lisboa and Porto produces a downward counter clockwise movement of the rank-size line and a more even distribution.

[13] Comparing the cities in this data base with INE's list of legal cities, we conclude that Brinkhoff's definition includes places that are not classified as cities.

Figure 6 – Rank-size distributions of Portuguese urban places, 1991-2001



In order to analyse the sensibility of parameter estimates to city definition, sample thresholds are the same for both data sets. Table 5 shows the estimates of rank size parameters for both datasets, as well as sample size and R^2 values.

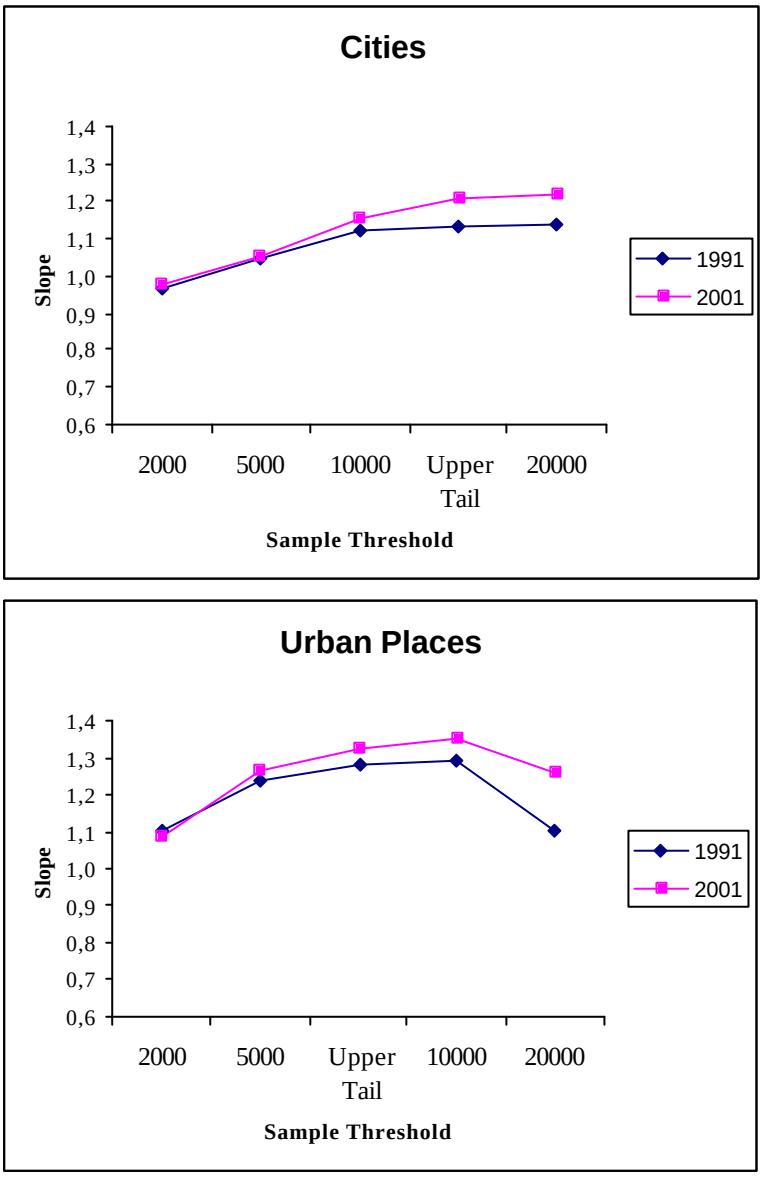
Table 5 - Results of OLS estimation: urban places versus cities (1991-2001)

Sample threshold	Census Date	Urban Places			Atlas data base		
		Number of cities	Slope	R2	Number of cities	Slope	R2
=2000	1991	450	1,106	0,985	122	0,970	0,961
	2001	531	1,090	0,983	122	0,977	0,950
=5000	1991	179	1,241	0,979	112	1,050	0,988
	2001	233	1,264	0,988	115	1,051	0,977
=10000	1991	97	1,293	0,968	77	1,120	0,993
	2001	123	1,352	0,988	85	1,152	0,991
=20000	1991	38	1,105	0,957	42	1,138	0,989
	2001	52	1,262	0,979	48	1,221	0,989
Upper tail	1991	150	1,284	0,979	41	1,135	0,989
	2001	178	1,324	0,991	41	1,209	0,988

Confronting the slope estimates for both data bases we can observe that, for cities, their values increase with the sample threshold, reflecting a reduction in city size inequality as smaller cities are excluded. For urban places, slope estimates increase with sample threshold until 10000 inhabitants and decrease afterwards. The evolution from 1991 to 2001 shows a decrease in city size inequality which is more important for higher sample cut-offs (Figure 7). In both samples, the

behavior of the slope for higher cut-offs in 2001, comparing with 1991, reflects the growth of middle size urban units and the decrease in the size of the two top units (Lisboa and Porto). Generally, slope estimates for urban places are bigger than those obtained for the city data base.

Figure 7 – Sensibility of slope estimates to urban definition



4. City movements within city size distribution

The precedent analysis of the long term evolution of city size distribution did not account for the movements that occur within the distribution. By following the position of each city relative to the others we can examine the movements of cities up or down the city size distribution, through

time. For that purpose we use a Markov Chain to describe changes within city size distribution, from 1864 up to date.

Although the first economic applications of Markov Chain Process go back to the 1950's, urban economists refer usually to the work of Quah (1993) as the keystone reference. In the context of empirical analysis of convergence or divergence between regions or countries, Quah uses a stationary first order Markov Chain to infer about patterns of "inter-temporal evolution of the entire cross section distribution" (Dobkins and Ioannides, 2000, 232). Following this methodology, Eaton and Eckstein (1997) examine the predicted evolution of the size distribution of cities in France and Japan. The same methodology was applied to study the dynamics of the evolution of city size distributions by Dobkins and Ioannides (2000) and Black and Henderson (2003), in the USA , and by Lanaspa *et al.* (2003), in Spain.

4.1 Methodology

Take F_t as the cross section distribution of city sizes at time t. In order to provide a discrete approximation of that distribution we must consider a set of K different size classes or states and calculate the frequency of cities in each state at time t. The evolution of city size distribution is represented by a (K,K) transition probability matrix, M. Each element of this matrix (p_{ij}) indicates the probability that a city belonging to state i in time period t reaches state j in the next period. The transition probabilities are given by:

$$(3)\ p_{ij} = \frac{m_{ij}}{\sum_{j=1}^{n} m_{ij}},\ \text{and}\ \sum_{j=1}^{n} p_{ij} = 1$$

where m_{ij} is the observed number of cities that belonging initially to state i are in state j in the next period, and n represents the number of possible states. The elements of M are estimated from the relative frequencies of changing of state between to subsequent periods. They are only an approximation of the true probability but, as Anderson and Goodman (1957) show (3) is the maximum likelihood estimate of the true p_{ij}.

The frequency of cities in each size class in time $t+1$, given by a $(K,1)$ vector F_{t+1}, is described by the following equation:

$$(4)\quad F_{t+1} = M\,F_t$$

where the $(K,1)$ vector F_t denotes the frequency of cities in each class, at time t.

Admitting that the probabilities between two states are constant over time, then the transition probability matrix is stationary and:

$$(5) \quad F_{t+s} = M^s F_t$$

If the M matrix is regular, the long-term distribution of F_t (or ergodic probability distribution[14]) is obtained taking s to 8 in equation (5).

$$(6) \quad F_8 = M^8 F_t$$

where the resulting $(K,1)$ vector, F_8, represents the equilibrium distribution of cities obtained under the assumption that the movements observed from t to $t+1$ are repeated as $t? \ 8$.

Considering $M_{t, t+1}$ as the transition matrix for the $(t, t+1)$ period we calculate this matrix for all periods in the sample (T) and obtained each element of the estimated average period to period transition matrix ($\overline{M}$), by computing the average of p_{ij} for all the T periods. The ergodic probability distribution is estimated using the ($\overline{M}$) matrix.

4.2. Empirical results

The use of a Markov transition matrix requires the definition of a discrete set of states. Following Eaton and Eckstein (1997) and Lanaspa *et al.* (2003) we defined cell upper points in the size distribution of cities according to their size relative to the average city size in each census date. We obtained seven states, corresponding to the following intervals: more than twice the average (state 1); between the average and twice the average (state 2); between 0.75 and the average (state 3); between 0.50 and 0.75 of the average (state four); between 0.30 and 0.50 of the average (state five); less than 0.30 of the average (state six) and a residual state (state seven) accounting for cities that, in each census date, enter or leave the sample. As our samples were obtained from population census, each period is define by consecutive census dates and has a variable length[15].

We estimate the matrix in Table 6 by computing the average of the relative frequency of cities in each state, from the 1864 to 1991[16] inter-census transition matrix. In the average transition matrix, large values in diagonal cells and low values or zeros in the off diagonal cells indicate the persistence of the relative position of cities within the distribution; zero values in cells far from the diagonal indicate that there are no drastic movements in the relative position/size of a city from one period to another. In this last case mobility is a gradual process that occurs between contiguous states.

[14] Also known as the equilibrium or steady state distribution.
[15] Since the middle of the 20th century, inter-census periods correspond to a decennium.
[16] The nature of the data does not allow equal length time periods.

For Portugal the diagonal terms are higher for larger cities (state 1) and for smaller cities (state 6), that is the probability of moving from the initial state is lower for the cities in the extremes of the distribution. These results indicate that the largest and the smallest cities are less likely to modify their relative position over time. Mobility seems to be higher in intermediate states. In fact, cities having sizes between 0.75 of the average and the average have a 53% probability of remaining in the same state, and cities in the class of 0.50 and 0.75 of the average have a 68% probability of persistence in the same state.

Movements for the adjacent higher state are more probable for small cities (with sizes below 0.50 of the average) whereas cities having between 0.75 and twice the average are more probable to move to the next lower state than to climb in the hierarchy. Finally, cities having less than 2000 inhabitants (state 7) have a 70% probability of remaining out of the sample and a 29% probability of entering in the class of cities having less than 0.30 of the average. On the other hand for smaller cities (state 6) the probability of dropping out (that is passing from state 6 to state 7) is about zero[17].

Table 6 - Average transition matrix for Portuguese cities, 1864 to 1991

Cell's upper end points	Cell's upper end points						
	8	2	1	0.75	0.50	0.30	Out of the sample
8	**0.986**	0.014	0.000	0.000	0.000	0.000	0.000
2	0.049	**0.798**	0.133	0.020	0.000	0.000	0.000
1	0.012	0.199	**0.530**	0.259	0.000	0.000	0.000
0.75	0.000	0.020	0.118	**0.680**	0.182	0.000	0.000
0.50	0.000	0.004	0.003	0.130	**0.787**	0.076	0.000
0.30	0.000	0.000	0.000	0.000	0.119	**0.877**	0.004
Out of the sample	0.000	0.000	0.000	0.000	0.011	0.291	**0.698**

The transition matrix for the Atlas data base, in Table 7, refers to the last inter-census period. The large number of zeros in the off-diagonal cells and the high values in the main diagonal show a high persistence of the city size distribution of Portuguese cities. As in the previous case, the probability of remaining in the same state is higher for larger and smaller cities than for medium size

[17] In fact our sample considers urban places that have the administrative status of "city" and at least 2000 inhabitants. So, the probability of dropping out, taking in account the age of the urban units and the criteria for becoming a city, is necessarily very small.

ones, that is, mobility is more likely to occur in cities having between 0,30 and the average size. Cities changing their relative position within the hierarchy, tend to move up to the next state.

Table 7 - Transition matrix for Portuguese cities, 1991 to 2001

	Cell's upper end points						
	∞	2	1	0.75	0.50	0.30	Out of the sample
∞	**1**	0.000	0.000	0.000	0.000	0.000	0.000
2	0.063	**0.938**	0.000	0.000	0.000	0.000	0.000
1	0.000	0.167	**0.750**	0.083	0.000	0.000	0.000
0.75	0.000	0.000	0.333	**0.556**	0.111	0.000	0.000
0.50	0.000	0.000	0.032	0.226	**0.645**	0.097	0.000
0.30	0.000	0.000	0.000	0.000	0.167	**0.833**	0.000
Out of the sample	0.000	0.000	0.000	0.000	0.000	0.000	**1.000**

The ergodic distribution (Table 8) is usually seen as the long run equilibrium distribution of city sizes. It gives an indicator of the tendencies at work within the distribution. The size distribution implied by the ergodic probability is a projection of the distribution of city sizes if the observed pattern of movement continued. The ergodic probability vector shows that the most probable state, in the long term distribution of Portuguese cities, is the first one ("∞"). Thus, there is a tendency towards the reinforcement of the number of cities that have more than twice the average size. On the other hand, for all the remaining states, but for the residual one, there is a lesser probability of remaining in a given state comparatively to the initial distribution. If the above tendencies persist city-size distribution will be gradually biased towards the relative larger cities

Table 8 – Ergodic probabilities

	Cell's upper end points						
	∞	2	1	0.75	0.50	0.30	Out of the sample
Ergodic probability	0,4302	0,1075	0,0629	0,1253	0,1664	0,1062	0,0014

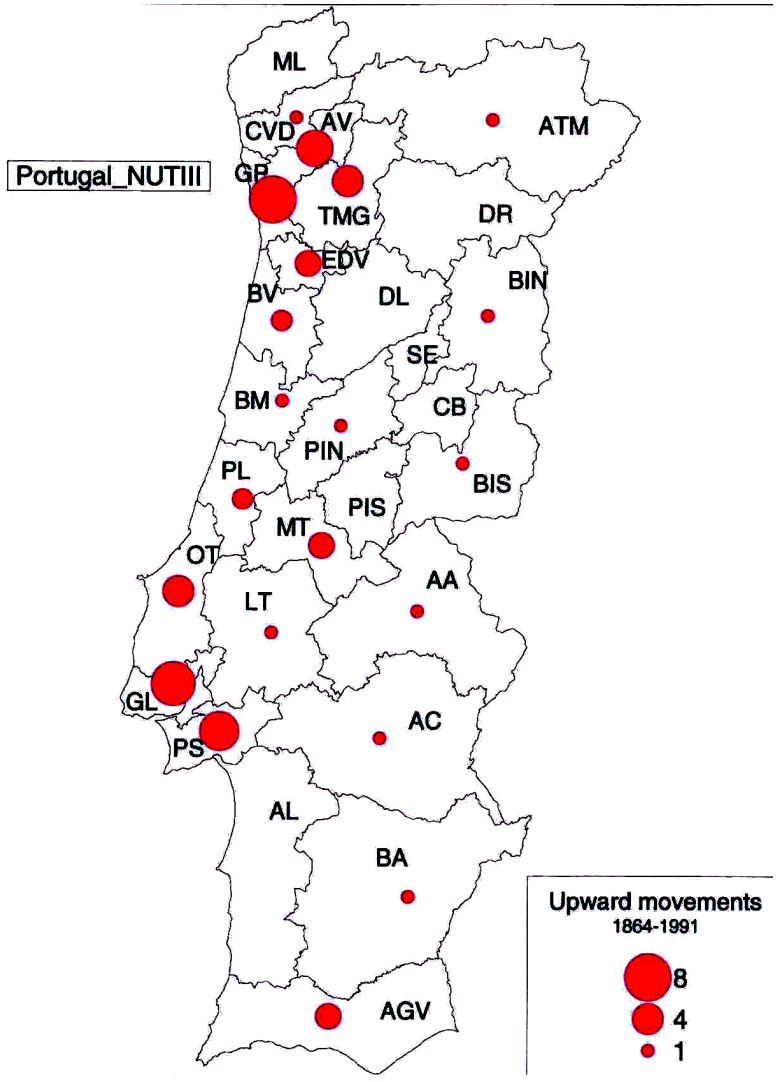
5. Spatial pattern of "winners" and "losers"

In order to analyze the spatial pattern of movements in the Portuguese urban system we confronted the distribution of cities by size classes in 1864 and 1991, identifying cities that move up

in their relative position (winners) and cities that move down (losers). From Figure 8[18] we can conclude that the number of upward movements is more than the double of the number of downward movements. The graph indicates the net gain (or loss) from 1864 to 1991. Some cities have registered a 6 or 5 point gain.

The inspection of the geographical location of urban places moving up in city size distribution suggests the existence of a spatial pattern. Winners seem to concentrate in the littoral and specially in and around the two main metropolitan areas (Figure 9). In fact, out of the 57 cities that registered positive changes in their relative position from 1864 to 1991, 40% belong to the metropolitan areas of Lisboa and Porto.

Figure 9 – NUT III distribution of cities registering upward movements (1864-1991)

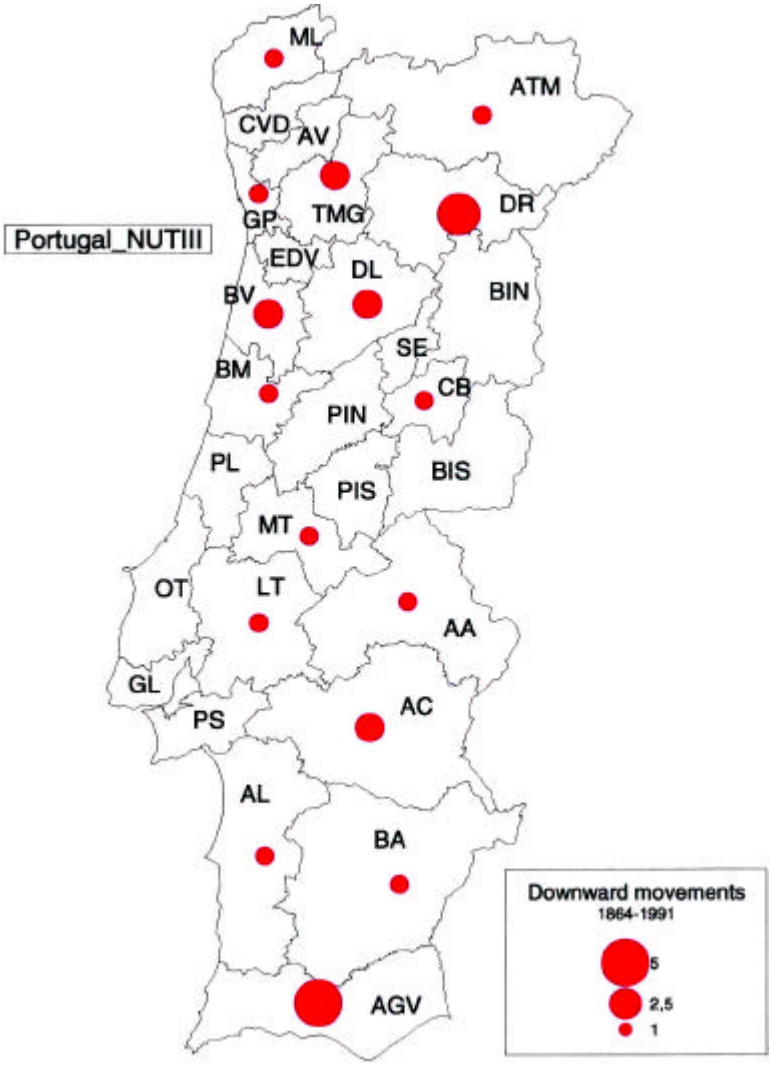


Legend

ML – Minho-Lima
CVD – Cávado
AV- Ave
ATM – Alto Trás-os-Montes
GP – Grande Porto
TMG – Tâmega
DR – Douro
EDV – Entre Douro e Vouga
BV – Baixo Vouga
DL – Dão-Lafões
BIN – Beira Interior Norte
SE – Serra da Estrela
CB – Cova da Beira
BM – Baixo Mondego
PIN – Pinhal Interior Norte
PIS – Pinhal Interior Sul
PL – Pinhal Litoral
MT – Médio tejo
BIS – Beira Interior Sul
OT – Oeste
LT – Lezíria do Tejo
Gl _ Grande Lisboa
PS – Península de Setúbal
AA – Alto Alentejo
AC – Alentejo Central
AL – Alentejo Litoral
BA – Baixo Alentejo
AGV - Algarve

[18] Reproduced in Annex 1

As for cities moving down the size classes (Figure 10), there is a more scattered geographical pattern, although 9 of these are concentrated in just two NUT III (Algarve and Douro).



Legend
ML – Minho-Lima
CVD – Cávado
AV- Ave
ATM – Alto Trás-os-Montes
GP – Grande Porto
TMG – Tâmega
DR – Douro
EDV – Entre Douro e Vouga
BV – Baixo Vouga
DL – Dão-Lafões
BIN – Beira Interior Norte
SE – Serra da Estrela
CB – Cova da Beira
BM – Baixo Mondego
PIN – Pinhal Interior Norte
PIS – Pinhal Interior Sul
PL – Pinhal Litoral
MT – Médio tejo
BIS – Beira Interior Sul
OT – Oeste
LT – Lezíria do Tejo
Gl _ Grande Lisboa
PS – Península de Setúbal
AA – Alto Alentejo
AC – Alentejo Central
AL – Alentejo Litoral
BA – Baixo Alentejo
AGV - Algarve

Figure 10 – NUT III distribution of cities registering downward movements (1864-1991)

The geographical location of winners and losers, suggests the existence of a spatial dependency in the evolution of the urban system. In order to test for spatial dependency we defined X_i as a variable that takes value 1 if the city registers a net gain (net loss) from 1864 to 1991 and 0 otherwise. The contiguity matrix was constructed considering that city i and city j are contiguous cities if they belong to the same NUT III. Given the nature of the variable, we applied the methodology of Cliff and Ord to test for spatial autocorrelation and computed their H statistic for

both sets of cities[19]. After normalizing, the appropriate values of *H* for upward and downward movements are, respectively, 2,55 and 0,92. In the first case we reject the null hypotheses of spatial independence, at the 5 per cent level of significance. So we can conclude that the distribution of cities registering upward movements from 1864 to 1991 is not spatially random. As for downward movements, the value of the Cliff and Ord's statistic does not allow the rejection of the null hypotheses, for the same level of significance.

6. Conclusions

This paper presents evidence about urban evolution in Portugal over more than a century, focusing on the characteristics and evolving pattern of city size distribution. One limitation of our study relates to the nature of our basic sample. The use of administrative cities conducts to the inclusion of very small places and to the exclusion of urban places with considerable population, but lacking the administrative status of city.

The following aspects emerge from our study:

- ✓ The Portuguese urban system is characterized by the proliferation of small cities and two dominant cities, Lisboa and Porto, which are the central cities of Portugal's two metropolitan areas. The long term evolution shows a slow increase in the number of cities. The growth of urban population was faster than that of the number of cities, urban growth resulting mainly from the concentration of population in existing cities. In the last decades, the two top cities have experienced heavy population losses, whereas intermediate cities, specially those in the their periphery, have registered significant population gains. As a result we observe a decrease in the top two primacy index;
- ✓ For the 1991-2001 period we obtain a different image of the Portuguese urban system if we take the urban place data base. Urbanization rate rises and the number of urban units is substantially higher. The proliferation of very small towns is reflected on a median size of 3934 and 4323 inhabitants, in 1991 and 2001, respectively. At the same time, we observe the emergence of 81 new urban units with 2000 inhabitants or more in a decade;
- ✓ The rank size line shifts up in the course of time as a result of urban growth and became smoother, expressing the development of the urban system as a whole, accompanied by a reduction of inequality between city sizes in the upper tail of the distribution;

[19] A more detailed description of the *H* statistics is presented in Annex II.

- ✓ For the basic sample and a 2000 inhabitants cut-off, the Pareto exponent is higher than one but decreasing, which generates a more contrasted urban hierarchy; from 1970 onwards it is less than one and tends to decrease; however, in the last two decade, we detect a reverse in this tendency, pointing to a process of decreasing inequality. When smaller cities are excluded from the sample, slope estimates tends to increase over time, starting from values lesser than one, reflecting a reduction in city size inequality. In comparison with the full sample, this distinct evolution portrays the changes in growth behaviour of middle-sized cities vis-à-vis the two top cities. The sensibility of slope estimates to sample threshold is higher in the beginning of our study period; on the other hand, their behaviour permits to conclude that, in the first part of the period, smaller cities tends to generate a more even distribution, whereas in more recent dates it appears that medium and larger cities are the source of a more equal distribution;
- ✓ For the urban places data base slope estimates are higher than one, indicating that city sizes are more evenly distributed than that predicted by Zipf's law. As smaller places are excluded we observe a reduction in city size inequality, since the values of the exponent are always superior and increase with sample threshold until 10000 inhabitants;
- ✓ Deviations from rank-size regularity enhance two different processes in the evolution of the urban system: until the middle of the twenty century, urban growth was accompanied by population concentration in the largest cities; afterwards, growth benefits intermediate cities, reinforced in the last decades by heavy population losses in the two top cities;
- ✓ Despite the observed pattern of urban growth - increased concentration in the early phases of the urbanization process, followed by a tendency of decreased concentration afterwards - we must bear in mind that we are using a city proper data base and that the rank size model does not take in account the location of the cities. As a result, the process of decentralization of urban growth can not be entirely viewed as an inter-urban decentralization process, since the parameter estimates captures the suburbanization process of population in the larger cities. In fact, the change in the growth behaviour of the two top cities *vis-à-vis* the middle size cities points to a process of selective growth since it favours mainly cities located closer to the central cities in the metropolitan areas of Lisboa and Porto;
- ✓ The use of a Markov chain process to describe movements within the distribution indicates that mobility is a gradual process that occurs mainly between contiguous size classes; mobility is more likely in intermediate states; there is a persistence of the relative position of cities within the distribution, given that in the average transition matrix we obtain large

values in diagonal cells. The long run equilibrium distribution of city sizes reflects a tendency toward the reinforcement of the number of the larger cities;

- ✓ The spatial pattern of "winners" and "losers" between 1864 and 1991 shows that the "winners" tends to concentrate in the littoral and especially in and around the two metropolitan areas. The test for spatial autocorrelation leads to the conclusion that the distribution of cities registering upward movements is not spatially random, reinforcing the idea of a selective growth process;
- ✓ On the other hand, the observed pattern of the 81 new urban places with 2000 or more inhabitants that emerge from 1991 to 2001, strengthens that idea. In fact, they are mostly located in the littoral and in the two metropolitan areas, as well as in the urban nebula that we can perceive from them.

The evolution of the Portuguese urban system mirrors structural changes that took place mainly in the second half of the 20th century: modern industrialization, in the fifties, export oriented since the sixties, and economic restructuring in the seventies and the eighties, following severe political changes and the integration in the European Union. It reflects also the evolution from a centralized political regime, administrating vast colonial territories, to a democratic regime, with a more decentralized administrative organization and confined to its European borders.

Bibliography

Albergaria, H. (1999), "A Dinâmica Populacional das Cidades do Continente Português", *Revista de Estatística*, Vol. 2, 47-66

Allen, G.R. (1954), "The 'Courbe des populations', a further analysis", *Bulletin of the Oxford University Institute of Statistics*, Vol. 16, 179-189

Auerbach, F. (1913), "Das gesetz der Bevölkerungskonzentration", Petermans Geographische Mitteilungen, 59, No.1, 74-76

Berry, B.J.L. (1961), « City size distribution and economic development", Economic Development and Cultural Change, Vol. IX, No. 4, 573-587

Bessi-Pietri, P.(2000), "Les formes récentes de la croissance urbaine « , Economie et Statistique, No. 336, 35-52

Black, D. and V. Henderson (2003), "Urban Evolution in the USA", *Journal of Economic Geography*, 3, 343-372

Brakman, S., H. Garretsen, C. Van Marrewijk and M. van den Berg (1999), "The Return of Zipf's: Towards a further understanding of the Rank-Size Distribution", *Journal of Regional Science*, Vol. 39, No. 1, 183-213

Carroll, G. (1982), "National city-size distributions: What do we know after 67 years of research?", *Progress in Human Geography*, Vol. 6, 1-43

Carter, H. (1981), *The Study of Urban Geography*, London, Edward Arnold

Cheshire, P. (1999), "Trends in sizes and structures of urban areas", in P. Cheshire and E.S. Mills (eds), *Handbook of Regional and Urban Economics*, Vol. 3, Amsterdam, Elsevier Science B. V., pp. 1339-1373

Chevailler, J.-C.(1978), *Eléments d'Économétrie Spatiale*, Paris, Editions Sirey

Clark, J.S. and J.C. Stabler (1991), "Gibrat's Law and the Growth of Canadian Cities", *Urban Studies*, Vol. 28, No. 4, 635-639

Córdoba, J.-C. (2003), "On the Distribution of City Sizes", *Working Paper*, Rice University

Delgado, A.P. and I.M. Godinho, 2004, The evolution of city size distribution in Portugal: 1864-2001, Working paper No. 151, Faculdade de Economia do Porto

Dobkins, L.H. and Y.M. Ioannides (2000), "The Evolution of Size Distribution: U.S. Cities", in *Economics of Cities: Theoretical Perspectives*, J.M. Huriot and J.-F. Thisse (eds), Cambridge, UK: Cambridge University Press

Duranton, G. (2002), "City Size Distribution As A Consequence of the Growth Process", Centre for Economic Performance, in http://cep.lse. ac.uk/pubs accessed in December 2003

Eaton, J. and Z. Eckstein (1997), "Cities and growth: Theory and evidence from France and Japan", *Regional Science and Urban Economics*, Vol. 27, 443-474

Eaton, J. and Z. Eckstein (1994), "Cities and Growth: Theory and Evidence from France and Japan", *Working Paper* No. 4612, National Bureau of Economic Research

Fan, C.C. and E. Casetti (1994), "*The spatial and temporal dynamics of US regional income inequality*", Annals of Regional Science, Vol. 28, 177-196

Ferreira, L., M.C. Cardoso and S.A.Silva (2003), *Evolução do Sistema Urbano Português*, Faculdade de Economia do Porto, unpublished

Fujita, M., P. Krugman and A. Venables (1999), *The Spatial Economy. Cities, Regions and International Trade*, Cambridge, Mass.:The M.I.T. Press

Gabaix, X. (1999a), "Zipf's Law and the growth of cities", *American Economic Review* (AEA Papers and Proceedings), Vol. 89, 129-132

Gabaix, X. (1999b), "Zipf's Law for Cities: An Explanation", *The Quarterly Journal of Economics*, Vol. CXIV, No. 3, 739-767

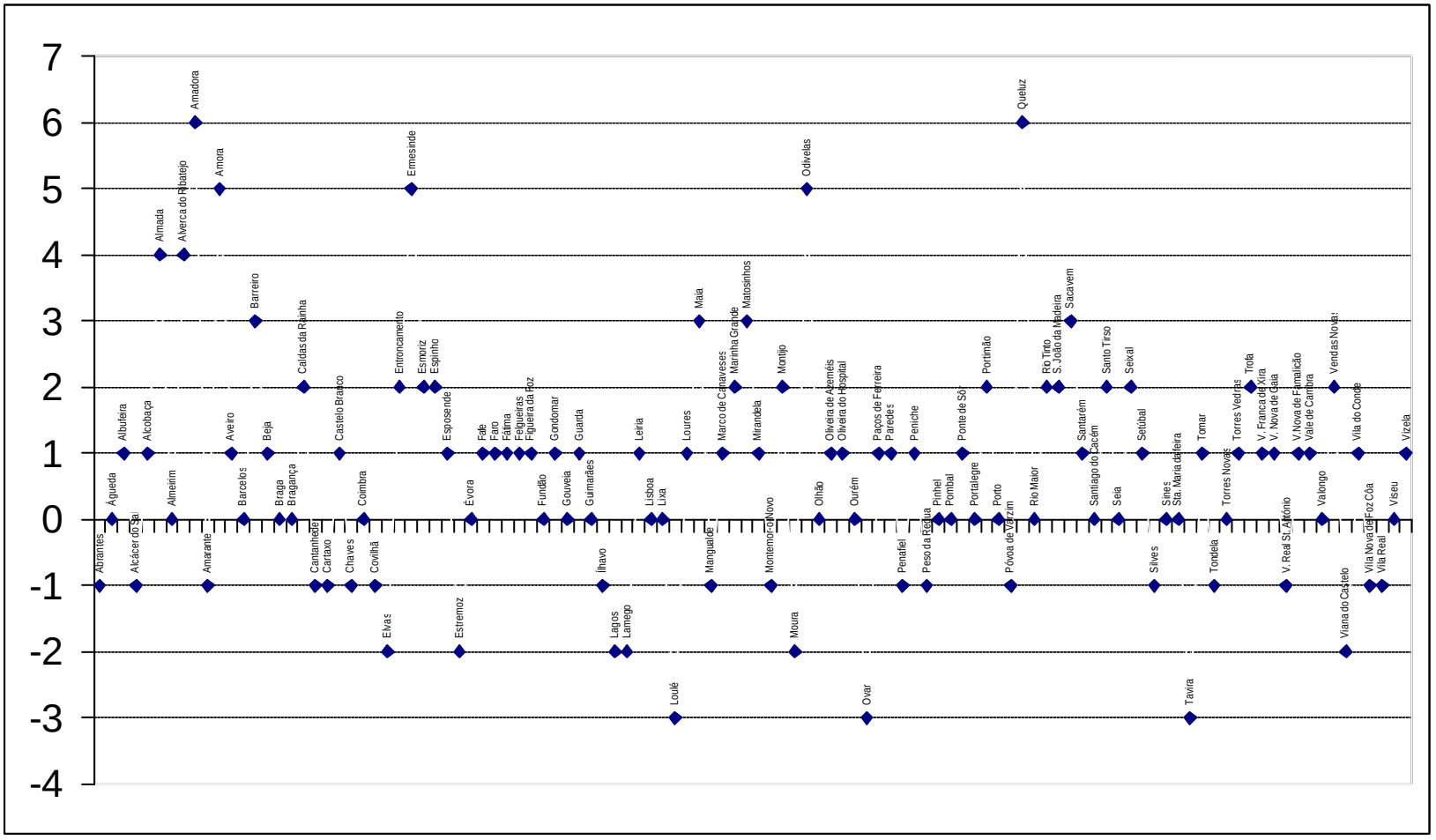
Gabaix, X. and Y.M. Ioannides (2003), "The Evolution of City Size Distributions", *Working*

Paper 2003, Tufts University, in http://ase.tufts.edu/econ/papers , accessed in December 2003
Gabaix, X. and Y.M. Ioannides (2003), "The Evolution of City Size Distributions", in J.V-Henderson and J.-F. Thisse (eds) *Handbook of Urban and Regional Economics*, in http://www.core.ucl.ac.be/staff/ThisseHandbook/Handbook/html, accessed in December 2003
Gibrat, R. (1931), *Les inégalités économiques*, Paris : Librairie du Recueil Sirey
Girão, A.A. and F.O.L. Velho (1944), *Evolução Demográfica e Ocupação do Solo Continental (1890-1940)*, Centro de Estudos Geográficos, Faculdade de Letras, Universidade de Coimbra, Coimbra
Goodrich, E.P., (1926), *The Statistical Relationship Between Population and the City Plan*, Chicago: The Urban Community.
Guérin-Pace, F. (1995), "Rank-Size Distributions and the Process of Urban Growth", *Urban Studies*, Vol. 32, No. 3, pp. 551-562
Henderson, J.V. (1974), "The sizes and types of cities", The American Economic Review, Vol. 64, No.4, 640-656
INE (2002), *Atlas das Cidades*, Lisboa, Instituto Nacional de Estatística
Ioannides, Y.M. and L.H. Dobkins (1999), "Dynamic Evolution of the U.S. City Size Distribution", *Working Paper* 1999-16, Tufts University, in http://ase.tufts.edu/econ/papers accessed in December 2003
Ioannides, Y.M. and H.G. Overman (2003), "Zipf's law for cities: an empirical examination", *Regional Science and Urban Economics*, 33, 127-137
Ioannides, Y.M. and H.G. Overman (2000), "Spatial Evolution of the US Urban System", *Working Paper* 2000-18, Tufts University, in http://ase.tufts.edu/econ/papers accessed in December 2003
Ioannides, Y.M. and H.G. Overman (1999), "Dynamic Evolution of the U.S. City Size Distribution", *Working Paper* No. 99-16, Tufts University, in http://ase.tufts.edu/econ/papers accessed in December 2003
Jayet, H. (1993), *Analyse Spatiale Quantitative. Une Introduction*, Paris, Economica
Knudsen, T. (2001), "Zipf's law for cities and beyond: The case of Denmark", ", Jan. 2001
Krugman, P. (1996), "Confronting the Mystery of Urban Hierarchy", *Journal of the Japanese and International Economies*, Vol. 10, 399-418
Krugman, P. (1995), "Innovation and Agglomeration: Two parables suggested by city-size distributions", *Japan and World Economy*, Vol. 7, 371-390
Lanaspa, L., A.M. Perdiguero and F. Sanz (2004), "La distribución del tamaño de las ciudades en España, 1900-1999", *Revista de Economia Aplicada*, No. 34 (vol. XII), 5-16
Lanaspa, L., F. Pueyo and F. Sanz (2003), "The evolution of Spanish urban structure during the twentieth century", *Urban Studies*, Vol. 40, No. 3, 567-580
Lasuén, J.R., A. Lorca and J. Oria (1967), "City-size distributions and economic growth", *Ekistics*, Vol. 24, 221-226
Le Gallo, J. (2001), "Space-time Analysis of GDP Disparities among European Regions: A Markov chains approach", 2001-06, LATEC, Laboratoire d'Analyse des Techniques Economiques, Université de Bourgogne
Lembo, A.J. Jr., "Spatial Autocorrelation", in http://www.css.cornell.edu/courses/620/lecture10, accessed in 2005/04/25
Lopes, A.S. (1979), *Desenvolvimento Regional*, Lisboa: Fundação Calouste Gulbenkian
Lopes, A.S. (1971), *As Funções Económicas dos Pequenos Centros*, Lisboa: Instituto Gulbenkian de Ciências.
Lotka, A. (1925), *Elements of Physical Biology*, Baltimore: Williams & Wilkins
Mills, E.S. and B.W. Hamilton (1994), *Urban Economics*, New York: HarperCollins College Publishers
Moriconi-Ebrard, F. (1993), *L'Urbanisation du Monde depuis 1950*, Paris: Anthropos

Overman, H.G. and Y.M. Ioannides (2000), "Cross-Sectional Evolution of the US City Size Distribution", in http://cep.lse.ac.uk/pubs/ accessed in December 2003
Parr, J. (1976), "A Class of Deviations from Rank-Size Regularity: Three Interpretations", *Regional Studies*, Vol. 10, 285-292
Parr, J. (1985), "A Note on the Size Distribution of Cities over Time", *Journal of Urban Economics*, Vol. 19, 535-546
Quah, D. (1993), "Empirical cross-section dynamics in economic growth", *European Economic Review*, 37, 426-434
Reed, W. J. (2002), "On the Rank-Size Distribution for Human Settlements", *Journal of Regional Science*, Vol. 42, No. 1, 1-17
Reed, W.J. (2001), "The Pareto, Zipf and other power laws", *Economics Letters*, 74, 15-19
Richardson, H. W. (1973), "Theory of the distribution of city sizes: Review and prospects2, *Regional Studies*, Vol. 7, 239-251
Rosen, K.T. and M. Resnick (1980), "The Size Distribution of Cities: An Examination of the Pareto Law and Primacy", *Journal of Urban Economics*, Vol. 8, 165-186
Salgueiro, T.B. (1992), *A Cidade em Portugal. Uma Geografia Urbana*, Porto: Edições Afrontamento
Simon, H. (1955), "On a class of skew distribution functions", *Biometrika*, Vol. 42, 425-440
Singer, H.W. (1936), "The 'courbe des populations.'A parallel to Pareto's Law", *The Economic Journal*, Vol. XLVI, No. 182, 254-263
Soo, K. T. (2002), "Zipf's Law for Cities: A Cross Country Investigation", *Working Paper*, Centre for Economic Performance, London School of Economics
Suarez-Villa, L. (1988), "Metropolitan evolution, sectoral economic change and the city size distribution", *Urban Studies*, Vol.25, 1-20
Tabuchi, T., J.-F. Thisse and D.-Z. Zeng (2003), "On the Number and Size of Cities", *Discussion papers*, Centre for Economic Policy Research, in http://www.core.ucl.ac.be/staff/thissePapers/NR61.pdf, accessed in December 2003
Urzúa, C.M. (2000), "A simple and efficient test for Zipf's law", *Economics Letters*, 66, 257-260
Zipf, G.K. (1949), *Human Behaviour and the Principle of Least Effort*, Reading, M.A.: Addison-Wesley

Annex I

Figure 8 – Net movements, 1864-1991



Annex 2

Testing for spatial autocorrelation

Consider a set of spatial units, cities, characterized by a binary variable X_i, that takes the value 1 if city *i* registers a net gain (a net loss) in its relative position from period *t* to period *t+n*, and zero if not.

Let $C=\{c_{ij}\}$ be the contiguity matrix whose elements are defined as follows: if city *i* and city *j* belong to the same *NUT III* then $c_{ij} = 1$, if they belong to different *NUT III*, $c_{ij} = 0$. In this matrix $c_{ij}=c_{ji}$ and $c_{ii}=0$, $\forall$ *i*.

We can compute $\sum_{j=1}^{n} c_{ij} = L_i$ as the total number of cities that belong to the same *NUT III* as city *i* (total number of contiguities for city *i*), and $\sum_{i=1}^{n} L_i = \mathrm{A}$. We defined $L=A/2$ as the total number of contiguous cities or join-counts in the set of cities.

If we have *n* cities, with n_1 cities registering a net gain (net loss) and n_2 registering a loss (gain) or maintaining their relative position ($n=n_1 + n_2$), the probability of a winning (losing) city is:

$$p(n_1) = n_1 / n$$

and the probability of a loss (gain) or non change in relative position of a city is:

$$p(n_2) = n_2 / n, \text{ with } p(n_1) + p(n_2) = 1$$

The probability of having two contiguous cities registering a net gain (net loss) is:

$$p(n_1) * p(n_1) \text{ or } [p(n_1)]^2$$

With *L* contiguous cities, the expected number of winning (losing) cities that are contiguous is given by

$$E(WW) = [p(n_1)]^2 L$$

and the correspondent standard deviation is:

$$s(WW) = \sqrt{[p(n_1)]^2 L + [p(n_1)]^3 K - [p(n_1)]^4 (L+K)}, \text{ where } K = \frac{1}{2}\sum_{i=1}^{n} c_i (c_i - 1)$$

In order to test for spatial autocorrelation, given the nature of X_i, we must calculate the Cliff and Ord's (1981) statistic *H*:

$$H = \frac{1}{2}\sum_{i \neq j}^{n}\sum_{j=1}^{n} c_{ij} x_i x_j,$$

where x_i and x_j are cities and c_{ij} is the correspondent value of the contiguity matrix. H is the number of times that two winning (losing) cities are located in the same *NUT III*.

The appropriate test statistic, the normalized value of H, is:

$$t = \frac{H - E(WW)}{s(WW)}$$

The relevant null hypothesis (H_0) is the existence of no spatial structure. If $|t| > |t_a|$, where t_a is given by the table of the standardized normal, we can reject H_0 at the a per cent level of significance. In this case we can conclude that the distribution of winning (losing) cities is not spatially random.