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**Conference Paper**

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39th Congress of the European Regional Science Association: "Regional Cohesion and Competitiveness in 21st Century Europe", August 23 - 27, 1999, Dublin, Ireland

**Provided in Cooperation with:**

European Regional Science Association (ERSA)

*Suggested Citation:* Campos, M. Isabel; Herrera, Julio; Jimenez-Ridruejo, Zenon (1999) : Censured Exchange Rates in a Discrete Time Target Zones Model: The Spanish Peseta/Deutsche Mark Case, 39th Congress of the European Regional Science Association: "Regional Cohesion and Competitiveness in 21st Century Europe", August 23 - 27, 1999, Dublin, Ireland, European Regional Science Association (ERSA), Louvain-la-Neuve

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# Censured Exchange Rates in a Discrete Time Target Zones Model: The Spanish Peseta/Deutsche Mark Case

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June 30, 1999

## Abstract

The literature on "Target Zones" is characterized by a continuous stochastic time modelization, where the exchange rate is a non-censored dependent variable. In this paper we propose a discrete time target zones model, taking into account the censored disposition of the exchange rate, whose parameters will be estimated by the FIML method. The settled theoretical model is a simplified version of Dornbusch's (1976) model, applied in a two countries environment. It will be tested into a peseta/deutsche mark exchange rate frame, from june 1989 to may 1998. The period is split in two sub-samples thinking over the enlargement of bands decided in august 1993. The estimation procedure of the model is based on the limited dependent rational expectation technique developed by Pesaran and Ruge-Murcia (1999). The results point out weightily differences between the two considered sample periods.

**Keywords:** Target Zones, LD-RE Models, Credibility, Realignment Probability

**JEL:** F31-Foreign Exchange

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<sup>‡</sup>This paper is an outgrowth of a research project [SEC97-1379] sponsored by the Spanish Consejo Interministerial de Ciencia y Tecnología.

# 1 Introduction

The recently developed literature known as "Target Zones" since the initial papers by Flood and Garber (1983), Williamson and Miller (1987), or the well-known Krugman's (1991) paper, models, in continuous time, the exchange rate behavior inside a floating band. The basic idea of these models can be represented in Figure 1, and point out the fact that the band, if credible, plays a stabilizing effect [the "honeymoon effect"] on the exchange rate which exhibits less variability than in the free float case [line FF in Figure 1]. The stabilizing effect comes from the monetary authority, who will intervene when necessary [with marginal or intramarginal intervention], or from the moderation effect that the band implies on exchange rate expectations. In a simple two countries monetary model, in continuous time, the typical expression for the exchange rate behavior is the following:

$$e_t = e(h_t) = h_t + c E_t(de_t=dt) \quad (1.1)$$

where  $e_t$  is the log of exchange rate,  $h_t$  represents the "fundamentals" or basic variables that determine  $e_t$ ,  $c$  is the semi-elasticity of money demand with respect to interest rate, and  $E_t(de_t=dt)$  is the expected variation of exchange rate in period  $t$ . The fundamentals are given by the following stochastic process:

$$dh_t = dm_t + d\hat{A}_t \quad (1.2)$$

where  $dm_t$  represents the monetary authorities intervention in the exchange rate market and  $\hat{A}_t$  is a shock on the velocity of money. This money velocity is modeled according to a brownian movement with drift expressed as:

$$d\hat{A}_t = \theta dt + \sigma d\epsilon_t; \quad \theta > 0 \quad (1.3)$$

the drift  $\theta$  represents the trend movements in  $\hat{A}_t$ , and, as a result of  $h_t$ ,  $\epsilon_t$  is modeled as a Wiener process that, in general, is described by  $\epsilon_t \sim N(0; \sigma^2 t)$ .

To solve the equation (1.1) we must use the Ito lemma. The expected exchange rate depreciation rate is:

$$E_t(de_t=dt) = \theta e'(h_t) + \frac{\sigma^2}{2} e''(h_t) \quad (1.4)$$

where  $e'$  and  $e''$  represent the first and second derivatives of the function "e(h<sub>t</sub>)" respectively.

Substituting (1:4) into (1:1) we obtain:

$$e_t = e(h_t) = h_t + c \int e'(h_t) + \frac{c^2}{2} e''(h_t) \quad (1.5)$$

The general solution of this equation is:

$$e_t = h_t + c \int + M_1 \exp(\lambda_1 h_t) + M_2 \exp(\lambda_2 h_t) \quad (1.6)$$

where  $M_1$  and  $M_2$  represent the integral constants, and  $\lambda_1$  and  $\lambda_2$  are the roots of the characteristic equation:

$$\frac{c^2}{2} \lambda^2 + c \int \lambda + 1 = 0 \quad (1.7)$$

Once solved, we obtain:

$$\lambda_1 = \frac{-\int c + \sqrt{\int^2 c^2 - 2c}}{c} < 0 \quad (1.8.a)$$

$$\lambda_2 = \frac{-\int c - \sqrt{\int^2 c^2 - 2c}}{c} > 0 \quad (1.8.b)$$

To get a concrete value of integral constants  $M_1$  and  $M_2$  that determine the SS curve, and to get a unique solution, this curve must be tangent to the edges of the band, as the slope of the curve tends to zero in the edges of the band. This result represents the Dornbusch's condition of "smooth pasting". The smooth pasting is a concept taken from options theory, which, in this case, can be expressed as:<sup>1</sup>

$$e'(h_{\max}) = 0 \quad \text{when} \quad e_{\max} = e(h_{\max}) \quad (1.9.a)$$

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<sup>1</sup>[34, Vid. Sodal, 1998]

$$e^l(h_{\min}) = 0 \quad \text{when} \quad e_{\min} = e(h_{\min}) \quad (1.9.b)$$

and implies the following system of equations when can solve  $M_1$  and  $M_2$ :

$$1 + M_1 \lambda_1 \exp(\lambda_1 h_{\min}) + M_2 \lambda_2 \exp(\lambda_2 h_{\min}) = 0 \quad (1.10.a)$$

$$1 + M_1 \lambda_1 \exp(\lambda_1 h_{\max}) + M_2 \lambda_2 \exp(\lambda_2 h_{\max}) = 0 \quad (1.10.b)$$

The solution is:

$$e_t = e(h_t) = h_t + c^{\otimes} + N \quad (1.11)$$

where:

$$N = \frac{f \lambda_2 \exp(\lambda_2 h_{\max} + \lambda_1 h_t) i \lambda_2 \exp(\lambda_2 h_{\min} + \lambda_1 h_t) g}{\lambda_1 \lambda_2 \exp(\lambda_2 h_{\min} + \lambda_1 h_{\max}) i \lambda_1 \lambda_2 \exp(\lambda_2 h_{\max} + \lambda_1 h_{\min})} +$$

$$+ \frac{f \lambda_1 \exp(\lambda_1 h_{\min} + \lambda_2 h_t) i \lambda_1 \exp(\lambda_1 h_{\max} + \lambda_2 h_t) g}{\lambda_1 \lambda_2 \exp(\lambda_2 h_{\min} + \lambda_1 h_{\max}) i \lambda_1 \lambda_2 \exp(\lambda_2 h_{\max} + \lambda_1 h_{\min})}$$

The graphic representation [..gure 1] is a curve with "S" shape that implies a reduction in exchange rate volatility as far as the exchange rate gets closer to the edges of the band.

One of the aspects deeply studied by target zones literature has been the evaluation of credibility degree of the target zone.<sup>2</sup>

There are different methodologies to estimate the expected depreciation of exchange rate in a target zone. They use a mix of assumptions like perfect and imperfect target zone credibility and/or infinitesimal or marginal, or intramarginal intervention.<sup>3</sup> The common characteristic of all of them is the

<sup>2</sup>Vid: the survey by Gámez and Torres (1996)

<sup>3</sup>From the so called "Basic Model" developed by Krugman (1991), taking into account the poor results of his empirical tests, several ways of development have arisen out addressed to improve the flexibility of the assumptions about perfect credibility of the bands and infinitesimal intervention. Vid: Bertola and Caballero (1992.a, 1992.b), Svensson (1991), Bertola and Svensson (1993), Svensson (1992) or Tristani (1994), among others.

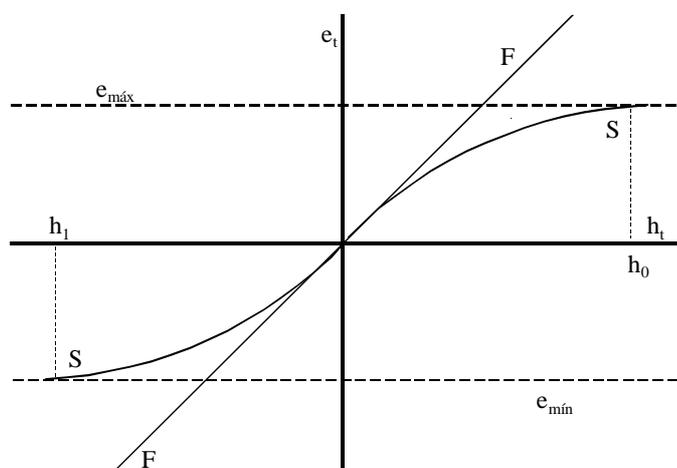


Figure 1: The exchange rate in a target zone with infinitesimal intervention and full credibility.

introduction of a stochastic continuous time modelling, taking the exchange rate like a no-censored dependent variable.<sup>4</sup>

However, the limited nature of exchange rate can't be ignored in a system when that variable is submitted to the edges of the band, neither can be ignored the fact that economic agents includes in their expectations such limited nature; as this aspect can, on some way, influence on the estimation an significance level of studies on the target zone subject. We propose a model of target zone in discrete time where we take into account the censored nature of the exchange rate an in which the parameters of the model will be estimated by maximum likelihood.

There are a lot of papers about the econometric estimation of models with censored dependent variables.<sup>5</sup> This work developed from initial paper by Tobin

<sup>4</sup>Since the edition of Bertola and Svensson (1993) paper, a lot of new methods have been developed to pull up information about market expectations. We can emphasize the papers by Mizrach (1995), Ayuso and Pérez Jurado (1997), Gómez Puig and Montalvo (1997), Söderlind and Svensson (1997) or Bekaert and Gray (1998), which detail target zones models with stochastic devaluation jumps, constants or variables along time.

<sup>5</sup>A model with truncate dependent variables is identified by the presence of unknown

(1958), who suggested an iterative process to solve this kind of equations and to estimate by maximum likelihood. This work was followed by the papers by Chanda and Maddala (1983), Shonkweiler and Maddala (1985), Pesaran (1989) or Holt and Johnson (1989). Recent developments can be encountered in the papers by Pesaran and Samiei (1992.a, 1992.b, 1995), Donald and Maddala (1992), Lee (1994) or Pesaran and Ruge-Murcia (1996, 1998).

The theoretical model of exchange rate determination that we use in this paper is an extension of Dornbusch (1976) model for two countries, and it is estimated for the Spanish peseta/German mark exchange rate from June 1989 to May 1998. We divide the time period in two subperiods due to the amplification of band. This is the case of peseta/mark exchange rate: the exchange rate band was initially  $\pm 6\%$  and evolved to a  $\pm 15\%$  on August 2nd 1993. The estimation technique we are going to use in the paper is the one formulated by Pesaran and Ruge-Murcia (1999) to find a unique solution to limited dependent variable model, subject to stochastic jumps in the target zone.

## 2 The LD-RE<sup>6</sup> Exchange Rate Determination Model

### 2.1 The Theoretical Model

The model of exchange rate determination that we use in the paper is a dynamic exchange rate model with two countries and predetermined prices. This model is an extension of Dornbusch's (1976) model, adding variable output and without considering that the economy is always in the potential output. We include in the model an equation explaining price adjustment. The money supplies are endogenously determined. Following Papell (1984.a, 1984.b), the

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observations that are placed out of a specific rank. On the other hand, the observational character of the exogenous variables can describe a model with censored variables. [1, Vid: Amemiya, 1984]

<sup>6</sup> "Limited Dependent Rational Expectations Model"

equations are the following:

$$\begin{aligned} m_t - p_t &= \alpha_1 r_t + \alpha_2 y_t + \alpha_0 \\ m_t^* - p_t^* &= \alpha_1 r_t^* + \alpha_2 y_t^* + \alpha_0^* \end{aligned} \quad \begin{array}{l} \text{Subtracting both equations,} \\ \text{we get:} \end{array}$$

$$(m_t - m_t^*) = (p_t - p_t^*) + \alpha_1 (r_t - r_t^*) + \alpha_2 (y_t - y_t^*) + \Delta_0 \quad (2.1.1)$$

that represents money market equilibrium.

The output in a time period could be different to full employment level and the adjustment equation, expressed for each country, is:

$$\begin{aligned} y_t &= \alpha_0 + \alpha_3 (e_t - p_t + p_t^*) + \alpha_4 i_t + \alpha_1 \\ y_t^* &= \alpha_0^* + \alpha_3^* (e_t - p_t + p_t^*) + \alpha_4^* i_t + \alpha_1^* \end{aligned} \quad \begin{array}{l} \text{Subtracting both equations,} \\ \text{we get:} \end{array}$$

$$(y_t - y_t^*) = (\alpha_0 - \alpha_0^*) + \alpha_3 (i_t - i_t^*) + \alpha_5 (e_t - p_t + p_t^*) + \Delta_1 \quad (2.1.2)$$

The prices are predetermined and respond to excess of demand by:

$$\begin{aligned} p_{t+1} - p_t &= \alpha_6 (y_t - \bar{y}) + \alpha_2 \\ p_{t+1}^* - p_t^* &= \alpha_6^* (y_t^* - \bar{y}^*) + \alpha_2^* \end{aligned} \quad \begin{array}{l} \text{Subtracting both equations,} \\ \text{we get:} \end{array}$$

$$\mathbb{E}_t [p_{t+1} - p_{t+1}^* - (p_t - p_t^*)] = \alpha_6 (y_t - y_t^*) + \alpha_6^* (\bar{y} - \bar{y}^*) + \Delta_2 \quad (2.1.3)$$

The following equation express the conditions of UIP to exchange rate:

$$\mathbb{E}_t (e_{t+1} - e_t) = (r_t - r_t^*) + PR_t \quad (2.1.4)$$

The real interest rate follows the Fisher equation for each country:

$$\begin{aligned} i_t &= r_t - (p_{t+1} - p_t) \\ i_t^* &= r_t^* - (p_{t+1}^* - p_t^*) \end{aligned} \quad \begin{array}{l} \text{Subtracting both equations,} \\ \text{we get:} \end{array}$$

$$(i_t - i_t^*) = (r_t - r_t^*) - \mathbb{E}_t [p_{t+1} - p_{t+1}^* - (p_t - p_t^*)] \quad (2.1.5)$$

$$\text{where } \begin{cases} \dot{A}_{0t} = \dot{1}_{0t} i \dot{1}_{0t}^* \\ \dot{\pi}_5 = \dot{\pi}_3 + \dot{\pi}_3^* \\ \dot{A}_{1t} = \dot{1}_{1t} i \dot{1}_{1t}^* \\ \dot{A}_{2t} = \dot{1}_{2t} i \dot{1}_{2t}^* \end{cases}$$

The equations of money and good markets equilibrium are standard. Equation (2:1:1) represents the money market equilibrium with predetermined prices in the short run, where  $y_t$  is the log of output,  $r_t$  is the nominal interest rate,  $p_t$  is the log of prices,  $\dot{1}_{jt}$  is a error term [shock] and the asterisk denotes foreign country.

Equation (2:1:2) represents aggregate demand function. In the case of predetermined prices we assume that in the short run the output is demand determined.<sup>7</sup> The aggregate demand depends on real exchange rate,  $(e_t i p_t + p_t^*)$ , and on the real interest rate  $i_t$ .<sup>8</sup>

Equation (2:1:4) is the UIP condition where  $e_t$  is the log of exchange rate,  $I_t$  is a information set used by economic agents in period  $t$ , and  $PR_t$  is the risk premium. With perfect capital mobility, the UIP condition implies that interest rates differential plus the risk premium equals the expected depreciation of exchange rate.

The last equation (2:1:5) express the Fisher condition under the assumption of predetermined prices.

To get the equation that describes the equilibrium level of exchange rate, ...rst, we substitute (2:1:5) into (2:1:2) and we obtain:

$$\begin{aligned} \dot{\pi}_5 i p_{t+1} i p_{t+1}^* i (p_t i p_t^*)^a &= \frac{1}{\dot{\pi}_4} (y_t i y_t^*) i \frac{1}{\dot{\pi}_4} (\dot{\pi}_0 i \dot{\pi}_0^*) i \\ &i \frac{\dot{\pi}_5}{\dot{\pi}_4} (e_t i p_t + p_t^*) i (r_t i r_t^*) i \dot{A}_{1t} \end{aligned} \quad (2.1.6)$$

<sup>7</sup>The seminal Dornbusch (1976) model would suppose that the production is placed always at the full employment level.

<sup>8</sup>This function can be modelled including the real interest rate instead of the nominal one. [23, Vid: Mathieson, 1977] and [3, Vid: Bhandari, 1982]

Substituting (2:1:6) into (2:1:3), we get:

$$\begin{aligned}
 (p_t \text{ i } p_t^*) &= \frac{1}{\mathbb{R}_5} (\mathbb{R}_0 \text{ i } \mathbb{R}_0^*) \text{ i } \frac{\mathbb{R}_1 \text{ i } \mathbb{R}_6 \mathbb{R}_4}{\mathbb{R}_5} (y_t \text{ i } y_t^*) + e_t + \frac{\mathbb{R}_4}{\mathbb{R}_5} (r_t \text{ i } r_t^*) + \\
 &+ \frac{\mathbb{R}_6 \mathbb{R}_4}{\mathbb{R}_5} (y_t \text{ i } y_t^*) + \frac{\mathbb{R}_4}{\mathbb{R}_5} (\dot{A}_{1t} + \dot{A}_{2t}) \quad (2.1.7)
 \end{aligned}$$

Mixing the expressions (2:1:7) and (2:1:4), and substituting into (2:1:1) we get the equation that describes the evolution of exchange rate as a function of its fundamentals like:

$$\begin{aligned}
 \text{I } e_t &= \frac{\frac{1}{2} (\mathbb{R}_0 \text{ i } \mathbb{R}_0^*)}{(\mathbb{R}_4 \text{ i } \mathbb{R}_1 \mathbb{R}_5 \text{ i } \mathbb{R}_5)} + \frac{\mathbb{R}_6 \mathbb{R}_4}{(\mathbb{R}_4 \text{ i } \mathbb{R}_1 \mathbb{R}_5 \text{ i } \mathbb{R}_5)} (y_t \text{ i } y_t^*)^{\frac{3}{4}} + \\
 + \frac{\frac{1}{2} (\mathbb{R}_4 \text{ i } \mathbb{R}_1 \mathbb{R}_5)}{(\mathbb{R}_4 \text{ i } \mathbb{R}_1 \mathbb{R}_5 \text{ i } \mathbb{R}_5)} E_t (e_{t+1} | I_t) \text{ i } \frac{\frac{1}{2} \mathbb{R}_5}{(\mathbb{R}_4 \text{ i } \mathbb{R}_1 \mathbb{R}_5 \text{ i } \mathbb{R}_5)} (m_t \text{ i } m_t^*) + \\
 + \frac{\frac{1}{2} (\mathbb{R}_2 \mathbb{R}_5 \text{ i } 1 + \mathbb{R}_4 \mathbb{R}_6)}{(\mathbb{R}_4 \text{ i } \mathbb{R}_1 \mathbb{R}_5 \text{ i } \mathbb{R}_5)} (y_t \text{ i } y_t^*)^{\frac{3}{4}} + \frac{\frac{1}{2} (\mathbb{R}_4 \text{ i } \mathbb{R}_1 \mathbb{R}_5)}{(\mathbb{R}_4 \text{ i } \mathbb{R}_1 \mathbb{R}_5 \text{ i } \mathbb{R}_5)} PR_t + \\
 + \frac{\frac{1}{2} \mathbb{R}_5}{(\mathbb{R}_4 \text{ i } \mathbb{R}_1 \mathbb{R}_5 \text{ i } \mathbb{R}_5)} \dot{A}_{0t} + \frac{\frac{1}{2} \mathbb{R}_4}{(\mathbb{R}_4 \text{ i } \mathbb{R}_1 \mathbb{R}_5 \text{ i } \mathbb{R}_5)} (\dot{A}_{1t} + \dot{A}_{2t}) \text{ i } \\
 \text{ i } \frac{\frac{1}{2} (\mathbb{R}_1 \mathbb{R}_5 \text{ i } \mathbb{R}_4)}{(\mathbb{R}_4 \text{ i } \mathbb{R}_1 \mathbb{R}_5 \text{ i } \mathbb{R}_5)} 1_{3t} \quad (2.1.8)
 \end{aligned}$$

To simplifying, the notation, we call:

$$-_0 = \frac{(\mathbb{R}_0 \text{ i } \mathbb{R}_0^*) + \mathbb{R}_6 \mathbb{R}_4 (y_t \text{ i } y_t^*)}{(\mathbb{R}_4 \text{ i } \mathbb{R}_1 \mathbb{R}_5 \text{ i } \mathbb{R}_5)}$$

$$-_1 = \frac{(\mathbb{R}_4 \text{ i } \mathbb{R}_1 \mathbb{R}_5)}{(\mathbb{R}_4 \text{ i } \mathbb{R}_1 \mathbb{R}_5 \text{ i } \mathbb{R}_5)}$$

$$-_2 = \frac{\mathbb{R}_5}{(\mathbb{R}_4 \text{ i } \mathbb{R}_1 \mathbb{R}_5 \text{ i } \mathbb{R}_5)}$$

$$-_3 = \frac{(\mathbb{R}_2 \mathbb{R}_5 \text{ i } 1 + \mathbb{R}_4 \mathbb{R}_6)}{(\mathbb{R}_4 \text{ i } \mathbb{R}_1 \mathbb{R}_5 \text{ i } \mathbb{R}_5)}$$

$$\epsilon_t = \frac{\alpha_5 \hat{A}_{0t} + \alpha_4 (\hat{A}_{1t} + \hat{A}_{2t}) + (\alpha_1 \alpha_5 + \alpha_4) \epsilon_{3t}}{(\alpha_4 + \alpha_1 \alpha_5 + \alpha_5)}$$

and we get the following expression:

$$e_t = {}^{-1}E_t(e_{t+1}=I_t) + \hat{A}h_t + \epsilon_t \quad (2.1.9)$$

\*  $\hat{A} = [\alpha_0; \alpha_2; \alpha_3; \alpha_1]$  is a 1 x 4 vector of coefficients

where:  $h_t^0 = [1; (m_t; m_t^a); (y_t; y_t^a); PR_t]$  such  $h_t$  is a 4 x 1 vector of fundamentals

In a target zone regime there are a maximum and a minimum limits that the exchange rate can get with respect to the central parity,  $o_t$ , that we call  $e_{max}$  and  $e_{min}$ , respectively. Without generality lost, we can assume that the band is symmetric. Let  $\frac{1}{2}$  be the band width.

In this case, we can assume that the exchange rate is described by the following non linear process:

$$e_t = \begin{cases} e_{max;t} & \text{if } {}^{-1}E_t(e_{t+1}=I_t) + \hat{A}h_t + \epsilon_t > e_{max;t} \\ \hat{e}_t^a & \text{if } e_{min;t} < {}^{-1}E_t(e_{t+1}=I_t) + \hat{A}h_t + \epsilon_t < e_{max;t} \\ e_{min;t} & \text{if } {}^{-1}E_t(e_{t+1}=I_t) + \hat{A}h_t + \epsilon_t < e_{min;t} \end{cases} \quad (2.1.10)$$

where:

$$\hat{e}_t^a = {}^{-1}E_t(e_{t+1}=I_t) + \hat{A}h_t + \epsilon_t$$

$$e_{max;t} = o_t + \frac{1}{2}; \quad e_{min;t} = o_t - \frac{1}{2}$$

To solve this equation we must take expectations over an infinite sequential set of censored variables, analytically described by a finite set of integrals and unsolved mathematically.<sup>9</sup> To obtain a unique and stable solution to our model we use the approach proposed by Pesaran and Ruge-Murcia (1999) and it is

<sup>9</sup>This aspect was studied by Pesaran and Samiei (1995) finding an exact solution in a LD-RE model with perfect credibility of the band and  $h_t$  composed by variables serially independent.

based on previous works done by Pesaran and Samiei (1992.a, 1992.b). In the appendix of their paper, Pesaran and Ruge-Murcia shown that the stable solution to a mathematical model with future expectation is equivalent to a model with current expectations.

The solution to the model with current expectations and target zones force us to reformulate equation (2:1:9) as follows:

$$e_t = {}^{-1}E_{t_i-1}(e_t=I_{t_i-1}) + \pm f_t + "t \quad (2.1.11)$$

where  $\pm$  is a  $1 \times n$  vector of parameters and  $f_t = [h_t; \Phi h_{t-1}; \dots]$  is a  $n \times 1$  vector of fundamentals.

Starting from equation (2:1:11) we can express the exchange rate in a target zone as:

$$e_t = \begin{cases} s & \\ < e_{m(x);t} & \text{if } \hat{e}_t > e_{m(x);t} \\ \hat{e}_t & \text{if } e_{m(n);t} < \hat{e}_t < e_{m(x);t} \\ & \\ : & \\ e_{m(n);t} & \text{if } \hat{e}_t < e_{m(n);t} \end{cases} \quad (2.1.12)$$

where:

$$\hat{e}_t = {}^{-1}E_{t_i-1}(e_t=I_{t_i-1}) + \pm f_t + "t$$

## 2.2 Identification of the Stochastic Process of the Variables

To obtain a unique and stable solution to the exchange rate equation (2:1:12) we need to specify the stochastic process followed by the variables in the model.

We use a similar process that Pesaran and Ruge-Murcia (1999), because we are going to use their econometric approach to estimate the model.

<sup>2</sup> The expression to the fundamentals are the following:

$$f_t = E_1!_{1;t_i-1} + u_t \quad (2.2.1)$$

where  $f_t$  is a  $n \times 1$  vector of fundamentals,  $\Gamma_1$  is a  $n \times j$  matrix of coefficients,  $\lambda_{1;t_i-1}$  is a  $j \times 1$  vector of predetermined variables including lagged values of  $f_t$  and  $e_t$ ; and  $u_t$  is a  $n \times 1$  vector of shocks.

- <sup>2</sup> The rational expectations solution of equation (2.1:11), when we do not take into account the band, is expressed by the following linear function:

$$E_{t_i-1}(e_t | I_{t_i-1}) = \frac{\pm f_t^e}{1 - \lambda_{1;t_i-1}} \quad \text{where} \quad f_t^e = E_{t_i-1}(f_t | I_{t_i-1}) = \Gamma_1 \lambda_{1;t_i-1} \quad (2.2.2)$$

- <sup>2</sup> We assume that the central parity,  $o_t$ , is normally fixed, but can make discrete jumps occasionally. Then:

$$e_{i;t} = e_{i;t_i-1} + a_t (b_t + z_t) \quad \text{for} \quad e_{i;t} = e_{max}; 0; e_{min} \quad (2.2.3)$$

where  $a_t$  is 1 or 0 depending on whether there is a realignment in central parity or not. The size of realignment, when it happens ( $a_t = 1$ ), is measured by  $(b_t + z_t)$ .  $z_t$  represents the non-predictable component [shock] and  $b_t$  is the predictable, follow the law:

$$b_t = \Gamma_2 \lambda_{2;t_i-1} \quad (2.2.4)$$

being  $\Gamma_2$  a  $1 \times k$  vector of fixed coefficients and  $\lambda_{2;t_i-1}$  a  $k \times 1$  vector of fundamentals included in  $I_{t_i-1}$ .

- <sup>2</sup> We assume that economic agents, when take their expectations, consider as stochastic the nature of the band as well as the monetary authorities intervention inside of the band. As the band is known in  $(t_i - 1)$ , the agents take in  $I_{t_i-1}$  the value of  $a_{t_i-1}$ . Besides, they need to incorporate in their exchange rate expectations a prediction about  $a_t$ . We assume that  $a_t$  depends only on  $a_{t_i-1}$  following a Markov Chain<sup>10</sup> with transition probability matrix:

$$P(t) = \begin{matrix} \mu & & \pi \\ \begin{pmatrix} P_{00}(t) & P_{01}(t) \\ P_{10}(t) & P_{11}(t) \end{pmatrix} & & \end{matrix} \quad (2.2.5)$$

<sup>10</sup>In a Markov chain, the value of a variable in period "t" depends only on the value of this variable in "(t\_i - 1)", and does not depend on any other value in the historical series. [36, Vid: Stokey and Lucas, con Prescott, 1989]

where  $\begin{cases} P_{i,j}(t) = \text{prob}(a_t = j | a_{t-1} = i); i, j = 0, 1 \\ P_{i,0}(t) + P_{i,1}(t) = 1; i = 0, 1 \end{cases}$

This formulation allow us to impose additional restrictions on the elements of  $P(t)$ . In this case,  $P_{i,j}(t)$  could be expressed like:

$$P_{i,j}(t) = \alpha(I_{3;t_i-1}) \quad (2.2.6)$$

where  $\alpha(z) \in [0, 1]$ , and  $I_{3;t_i-1}$  represents predetermined variables included in  $I_{t_i-1}$ .<sup>11</sup>

<sup>2</sup> The shocks  $\epsilon_t$ ,  $u_t$  and  $z_t$  are normally distributed with zero mean and a constant variance-covariance matrix:

$$\text{Cov} \begin{pmatrix} \epsilon_t \\ z_t \\ u_t \end{pmatrix} = \begin{pmatrix} \sigma_\epsilon^2 & 0_{1 \times j} & 0 \\ 0_{1 \times 1} & \Sigma_z & 0_{1 \times j} \\ 0_{j \times 1} & 0_{j \times 1} & -\Sigma_u \end{pmatrix} \quad (2.2.7)$$

where  $0_{1 \times j}$  is a  $1 \times j$  vector of zeros and  $\Sigma_u$  is a positive-definite variance-covariance matrix of  $u_t$ .

As we have incorporated a dummy variable  $a_t$  which takes 1 or 0 depending on whether there is a band realignment, we can reformulate the exchange rate equation (2:1:12) to take this fact into account. Besides, we make a set of transformations to get an expression of the LD-RE model as a function of the shocks. To do this, we substitute  $f_t^e$  from equation (2:2:2) into (2:2:1):

$$f_t = f_t^e + u_t \quad (2.2.8)$$

Substituting (2:2:8) into (2:1:11):

$$e_t = E_{t-1}(e_t | I_{t-1}) + \alpha f_t^e + \alpha u_t + \epsilon_t \quad (2.2.9)$$

Calling  $\hat{\epsilon}_t = \alpha u_t + \epsilon_t$ , such  $\text{Var}(\hat{\epsilon}_t) = \sigma_\epsilon^2 + \alpha \Sigma_u$ , and substituting in the last equation, we obtain:

$$e_t = E_{t-1}(e_t | I_{t-1}) + \alpha f_t^e + \hat{\epsilon}_t \quad (2.2.10)$$

<sup>11</sup>We will include lagged values of  $e_t$  and  $f_t$ , but not of  $E_{t-1}(e_t | I_{t-1})$ .

Operating:

$$\hat{\epsilon}_t = e_{t,i}^{-1} E_{t-1}(e_{t=I_{t-1}})_i \pm f_t^e \quad (2.2.11)$$

If we call now  $\#_t = \frac{\hat{\epsilon}_t}{\sigma_{\epsilon}^2}$ , to typify  $\hat{\epsilon}_t$  and substituting in (2:2:11):

$$\#_t = \frac{e_{t,i}^{-1} E_{t-1}(e_{t=I_{t-1}})_i \pm f_t^e}{\sigma_{\epsilon}^2} \quad (2.2.12)$$

If there is not band realignment  $a_t = 0$ , the equation (2:2:3) is transformed in:

$$e_{i;t} = e_{i;t-1}; \quad \text{for } e_i = e_{\max}; 0; e_{\min} \quad (2.2.13)$$

Taking this equation into account, we express  $\#_t$  as:

$$\#_{i;t} = \frac{e_{i;t-1}^{-1} E_{t-1}(e_{t=I_{t-1}})_i \pm f_t^e}{\sigma_{\epsilon}^2}, \quad \text{for } i = \max; \min \quad (2.2.14)$$

Following the same procedure, when  $a_t = 1$  and defining  $\epsilon_t = \pm u_t + \epsilon_{t-1} Z_t$ , with  $\text{Var}(\epsilon_t) = \sigma_{\epsilon}^2 = \sigma_{\epsilon}^2 + \pm \pm \sigma_z^2$ , and calling  $\mu_t = \frac{\hat{\epsilon}_t}{\sigma_{\epsilon}^2}$ , we can express  $\mu_t$  as:

$$\mu_{i;t} = \frac{e_{i;t-1}^{-1} E_{t-1}(e_{t=I_{t-1}})_i \pm f_t^e}{\sigma_{\epsilon}^2}, \quad \text{where } i = \max; \min \quad (2.2.15)$$

Then, we can formulate equation (2:1:12) distinguishing whether there is a realignment [ $a_t = 1$ ], or not, [ $a_t = 0$ ]. The LD-RE proposed model could be applied with perfect credibility case as well as with imperfect credibility. The model specification is:

$$e_t = \begin{cases} e_{\max;t-1} & \text{if } \#_t > \#_{\max;t} \\ e_{\min;t-1} & \text{if } \#_{\min;t} < \#_t < \#_{\max;t} \\ e_{\min;t-1} & \text{if } \#_t < \#_{\min;t} \end{cases} \quad \text{when } a_t = 0 \quad (2.2.16.a)$$

$$e_t = \begin{cases} e_{\max;t-1} + b_t + Z_t & \text{si } \mu_t > \mu_{\max;t} \\ e_{\min;t-1} + b_t + Z_t & \text{si } \mu_{\min;t} < \mu_t < \mu_{\max;t} \\ e_{\min;t-1} + b_t + Z_t & \text{si } \mu_t < \mu_{\min;t} \end{cases} \quad \text{when } a_t = 1 \quad (2.2.16.b)$$

## 2.3 Resolution of Rational Expectations in the Model

To solve the model specified in equations (2:2:16:a) and (2:2:16:b) we need to determine before the solution for the exchange rate expectations  $E_{t-1}(e_t | I_{t-1})$ .

Assuming that in the period  $(t-1)$  economic agents know the value of  $a_{t-1} = i; \forall i = 0, 1$ , the conditional exchange rate expectation could be expressed like:

$$E_{t-1}(e_t | I_{t-1}) = E_{t-1}(e_t | I_{t-1}; a_t = 0) \cdot P_{i0}(t) + E_{t-1}(e_t | I_{t-1}; a_t = 1) \cdot P_{i1}(t) \quad (2.3.1)$$

$\forall i = 0, 1$ , where the values of  $P_{i0}(t)$  and  $P_{i1}(t)$  are given for the  $i$ -esima row of  $P(t)$  matrix, and verify the restriction  $P_{i0}(t) + P_{i1}(t) = 1$ .

Taken into account equations (2:2:16:a) and (2:2:16:b) we can express the conditional exchange rate expectations as:

$$\begin{aligned} I \quad E_{t-1}(e_t | I_{t-1}; a_t = 0) &= E_{t-1}(e_t | I_{t-1}; \#_{t-1}, \#_{max;t}) \cdot \text{prob}(\#_{t-1}, \#_{max;t}) + \\ &+ E_{t-1}(e_t | I_{t-1}; \#_{min;t} < \#_{t-1} < \#_{max;t}) \cdot \text{prob}(\#_{min;t} < \#_{t-1} < \#_{max;t}) + \\ &+ E_{t-1}(e_t | I_{t-1}; \#_{t-1}, \#_{min;t}) \cdot \text{prob}(\#_{t-1}, \#_{min;t}) \end{aligned} \quad (2.3.2.a)$$

$$\begin{aligned} I \quad E_{t-1}(e_t | I_{t-1}; a_t = 1) &= E_{t-1}(e_t | I_{t-1}; \mu_{t-1}, \mu_{max;t}) \cdot \text{prob}(\mu_{t-1}, \mu_{max;t}) + \\ &+ E_{t-1}(e_t | I_{t-1}; \mu_{min;t} < \mu_{t-1} < \mu_{max;t}) \cdot \text{prob}(\mu_{min;t} < \mu_{t-1} < \mu_{max;t}) + \\ &+ E_{t-1}(e_t | I_{t-1}; \mu_{t-1}, \mu_{min;t}) \cdot \text{prob}(\mu_{t-1}, \mu_{min;t}) \end{aligned} \quad (2.3.2.b)$$

<sup>2</sup> And:

$$\begin{aligned} I \quad & \text{prob}(\#_{t-1}, \#_{max;t}) = 1 - F(\#_{max;t}) \\ & \text{prob}(\#_{min;t} < \#_{t-1} < \#_{max;t}) = F(\#_{max;t}) - F(\#_{min;t}) \\ & \text{prob}(\#_{t-1}, \#_{min;t}) = F(\#_{min;t}) \end{aligned} \quad (2.3.3.a)$$

$$\begin{aligned}
& \text{prob}(\mu_t > \mu_{m\#x;t}) = 1 - G(\mu_{m\#x;t}) \\
& \text{prob}(\mu_{m\#n;t} < \mu_t < \mu_{m\#x;t}) = G(\mu_{m\#x;t}) - G(\mu_{m\#n;t}) \\
& \text{prob}(\mu_t < \mu_{m\#n;t}) = G(\mu_{m\#n;t})
\end{aligned} \tag{2.3.3.b}$$

where  $F^{(2)}$  and  $G^{(2)}$  denote cumulative distribution functions of  $\#_t$  and  $\mu_t$  respectively.

From an econometric point of view and following Pesaran and Ruge-Murcia (1999), sometimes it is convenient to suppose that shocks are normally distributed.<sup>12</sup> The standardized variables  $\#_t$  and  $\mu_t$  will be  $N(0, 1)$ , and  $H^{(2)}$  and  $L^{(2)}$  will denote, respectively, the density functions. The value of  $E_{t_i-1}(e_t | I_{t_i-1})$  that will solve equation (2:3:1) will be the following rational expectations solution:

$$\begin{aligned}
E_{t_i-1}(e_t | I_{t_i-1}) &= f_{e_{m\#x;t_i-1}} [1 - H(\#_{m\#x;t})] + \frac{3}{4} \cdot [L(\#_{m\#n;t}) - L(\#_{m\#x;t})] + \\
&+ [-1 E_{t_i-1}(e_t | I_{t_i-1}) + \pm f_t^e] [H(\#_{m\#x;t}) - H(\#_{m\#n;t})] + e_{m\#n;t_i-1} H(\#_{m\#n;t}) g E \\
E_{t_i-1}(e_t) &+ f_{e_{m\#x;t_i-1} + b_t} [1 - H(\mu_{m\#x;t})] + \frac{3}{4} \cdot [L(\mu_{m\#n;t}) - L(\mu_{m\#x;t})] + \\
&+ [-1 E_{t_i-1}(e_t | I_{t_i-1}) + \pm f_t^e] [H(\mu_{m\#x;t}) - H(\mu_{m\#n;t})] + \\
&+ (e_{m\#n;t_i-1} + b_t) H(\mu_{m\#n;t}) g E_{t_i-1}(e_t)
\end{aligned} \tag{2.3.5}$$

$\#_i = 0; 1.$

We look for a unique solution to (2:3:5). We propose as a sufficient condition the following proposition, which can be proved showing the equivalence between this proposition and the formulated by Lee (1994) and Pesaran and Ruge-Murcia (1996, 1998).

<sup>12</sup>The results are valid also when we suppose a more general specification, for example assuming heteroskedastic shocks. In the empirical application that we include in the paper we assume that the conditional variance of the shock in the exchange rate equation is a function of squared deviation of exchange rate from central parity. In the case of fundamentals we assume homoskedastic shocks.

**Proposition 1** For any  $\alpha_1 \in (0, 2)$ , and assuming that  $F(\cdot)$  and  $G(\cdot)$  are continuous and first-order differentiable probability distribution functions, then the rational expectations solution for the two-sided band with occasional jumps exists. If  $\alpha_1 > 1$ , then the solution is also unique.

If this sufficient condition is verified we can find a unique solution to expression (2.3.5). The problem is that both equations are implicit solutions and, therefore, we need employ iterative procedures to calculate  $E_{t-1}(e_t | I_{t-1})$ . In our case, we employ the Newton-Raphson algorithm.<sup>13</sup>

### 3 Empirical Application of LD-RE Model

We choose the peseta/deutsche mark bilateral exchange rate as the dependent variable to estimate. The number of observations are 102, starting when Spain came into the Agreement of Exchange and Intervention of European Monetary System [June 1989] until last available data [May 1998]. During this period, the width of the band was modified from  $\pm 6\%$  to  $\pm 15\%$  on August, 2nd 1993. This fact forces us to subdivide the total period in two subperiods.

In the total period four realignments occurred for the peseta: September, 17th 1992, November, 23rd 1992, May, 14th 1993 and, March, 6th 1995; three realignments happened in the first subperiod and one in the second.

With respect to the fundamentals, the output in each country is measured by the Index of Industrial Production seasonally unadjusted.<sup>14</sup> The money supply is the  $M_1$  series seasonally unadjusted and the interest rate is the three-month interbank money market rates. All the data were extracted from the Main Economic Indicators series of OECD. The central parity exchange rate

<sup>13</sup>Vid: Wallis (1980), Hansen and Sargent (1981) or Fair and Taylor (1983).

<sup>14</sup>Always we can argue, but we follow Espasa and Cancelo (1993): "In an econometrics model, when we try to study the dynamic relation among two or more variables, the analysis must be done using the observed variables, never the extracted signals over the basis of eliminate stochastic seasonality" [11, Ch. 4, pp. 318]. [41, Vid: Wallis, 1974]

is extracted from the Cuentas Financieras de la Economía Española (Spain Financial Accounts) published by Banco de España (Spain Central Bank).

### 3.1 Description of the Likelihood Function

To solve the proposed model, we have to estimate the parameters of the model: We use the Full Information Maximum Likelihood [FIML] method to do it.

To estimate the parameters, we assume that we have a stationary series with  $T$  elements  $f_{j_t}g$  just as  $t = 1; \dots; T$ , where  $j_t = ff_t; a_t; o_t; e_tg$ . Besides, in period "t" economic agents incorporate the elements  $j_1; j_2; \dots; j_t$  to the information set  $I_t$ , then:

$$\begin{aligned} \text{prob}(j_1; j_2; \dots; j_t; \dots; j_T) &= \text{prob}(j_1) : \text{prob}(j_2=I_1) : \text{prob}(j_3=I_2) : \dots \\ &::: \text{prob}(j_t=I_{t-1}) : \dots : \text{prob}(j_T=I_{T-1}) \end{aligned} \quad (3.1.1)$$

where:

$$\begin{aligned} \text{prob}(j_t=I_{t-1}) &= \text{prob}(f_t=I_{t-1}) : \text{prob}(a_t=f_t; I_{t-1}) : \text{prob}(o_t=a_t; f_t; I_{t-1}) : \\ &: \text{prob}(e_t=o_t; a_t; f_t; I_{t-1}) \end{aligned} \quad (3.1.2)$$

Considering the characterization of the model variables given in two previous parts, we can write the likelihood function like:

$$L(\$) = L_f(\$_1) + L_a(\$_2) + L_o(\$_3) + L_e(\$_4) \quad (3.1.3)$$

where:

$$^2 L_f(\$_1):$$

$$L_f = \sum_{t=1}^T \log(2^{j_t}) + \sum_{t=1}^T \log j_t - \sum_{t=1}^T \frac{1}{2} (f_t - E_{1|1:t-1})^2 - \frac{1}{2} (f_t - E_{1|1:t-1}) \quad (3.1.4)$$

$L_a (\$2)$ :

$$L_a = \log \text{prob}(a_1) + \log \text{prob}(a_2=1) + \dots + \log \text{prob}(a_T=1) \quad (3.1.5)$$

$L_o (\$3)$ :

$$L_o = \sum_{t=2}^T \log \frac{1}{2^{j_t}} + \sum_{t=2}^T \frac{1}{2^{j_t}} [(o_t - o_{t-1}) - E_{2|2:t-1}]^2 \quad (3.1.6)$$

where  $\log[\text{prob}(o_t=a_t=0; f_t; I_{t-1})] = \log(1) = 0$ .

$L_e (\$4)$ :

$$L_e = \sum_{t=2}^T \log[1 - H(\#m_{x:t})] + \sum_{t=2}^T \log[H(\#m_{n:t})] + \sum_{t=2}^T \log \frac{1}{2^{j_t}} + \sum_{t=2}^T \frac{1}{2^{j_t}} [e_t - E_{t-1}(e_t=I_{t-1}) - f_t]^2 \quad (3.1.7)$$

The estimation of the exact likelihood in equation (3:1:3) raises a non linear optimization system that we have to solve. The estimates obtained when maximizing the likelihood function are the FIML.

To solve this non linear optimization problems, the most effective method of is to use iterative algorithms.<sup>15</sup> Generally there apply the called "Gradient Methods", and specially the "Newton Method", which is a linear approach to the maximum using Taylor series.<sup>16</sup>

<sup>15</sup>[17, Vid: Greene (1998), pp. 175-187]

<sup>16</sup>In our case, we started the iterations using Newton algorithm, but to get the final results we changed to a "Quasi-Newton Algorithm". Specially, we analyze the iterative process using "Davidon-Fletcher-Powell [DFP] Algorithm".

### 3.2 Econometric Identification

First, we will make an approach to the method we are going to use to solve equation (2:1:9). Before, we describe the analytic expressions of estimating equations we have shown if there exist autocorrelation in the residuals. We have tested and there are due to exchange rate behavior as a random walk,<sup>17</sup> and thus, we are going to estimate exchange rate equation including, like an additional variable, the lagged exchange rate. The procedure was used before by Bajo (1986, 1987) who tested the existence of autocorrelation in the residuals in the peseta/mark exchange rate from 1977 to 1984, and there are corrected with the incorporation of lagged exchange rate.

The expression of fundamentals  $h_t$  that we are going to use assumes that  $h_t$  follows an autorregressive process that in our case will be an AR(1) with parameter  $P$ . Taking  $e_{t-1}$  as an additional variable, and assuming that a stable future rational expectation solution is equivalent to a stable current rational expectation solution, we can write the exchange rate process as:

$$\begin{aligned}
 e_t &= \alpha_1 E_{t-1}(e_t) + z_1(1 - \alpha_1)e_{t-1} + \tilde{A}h_t + \frac{\mu}{1 - \alpha_1} \tilde{P}^{-1} \Phi h_t + \epsilon_t = \\
 &= \alpha_1 E_{t-1}(e_t) + \epsilon_t + \epsilon_t \quad (3.2.1)
 \end{aligned}$$

where  $f_t^0 = [e_{t-1}; h_t; \Phi h_t]$  and  $z_1$  is the root of the equation  $\tilde{A}z + \alpha_1 z^{-1} = 1$ , such  $|z_j| < 1$ .

Then, the econometric specification that we will do is the following:

<sup>2</sup>  $h_t^0 = [(m_t; m_t^a); (y_t; y_t^a); PR_t]$  will be approach by the following vector  $f_t$ :

$$f_t^0 = [(m_t; m_t^a); (y_t; y_t^a); x_t] \quad (3.2.2)$$

<sup>17</sup>We have tested using ADF [Augmented Dickey-Fuller] and Phillips-Perron tests, and we can not reject the existence of an unit root.

with:

$$x_t^0 = \begin{pmatrix} 1; e_{t_i-1}; r_{t_i-1}; r_{t_i-1}^a; (e_{t_i-1}; o_{t_i-1}); \\ \phi^i m_{t_i-1}; m_{t_i-1}^a; \phi^i y_{t_i-1}; y_{t_i-1}^a; \phi^i m_{t_i-2}; m_{t_i-2}^a; \\ \phi^i y_{t_i-2}; y_{t_i-2}^a; \phi^i r_{t_i-2}; r_{t_i-2}^a; \phi (e_{t_i-2}; o_{t_i-2}) \end{pmatrix}$$

where we have included  $r_{t_i-1}$  and  $(e_{t_i-1}; o_{t_i-1})$  as a proxy variable to the risk premium. Besides, we have incorporated lags in the variable in order to correct the possibility of error in the estimation for approaching the solution of future rational expectations to the current ones.

<sup>2</sup> To estimate the exchange rate expectations,  $E_{t_i-1}(e_t = I_{t_i-1})$ ,<sup>18</sup> the specification of  $(m_t; m_t^a)$  and  $(y_t; y_t^a)$  is, respectively, the following:<sup>19</sup>

$$\begin{aligned} I \phi (m_t; m_t^a) = & \%_0 + \%_1 \phi^i m_{t_i-1}; m_{t_i-1}^a + \%_2 \phi^i m_{t_i-2}; m_{t_i-2}^a + \\ & + \%_{12} \phi^i m_{t_i-12}; m_{t_i-12}^a + \Upsilon_{1t} \end{aligned} \quad (3.2.3)$$

where  $\Upsilon_{1t}$  is white noise.

$$I (y_t; y_t^a) = o + \%_1 y_{t_i-1}; y_{t_i-1}^a + \%_2 y_{t_i-12}; y_{t_i-12}^a + \Upsilon_{2t} \quad (3.2.4)$$

where the shock  $\Upsilon_{2t}$  is white noise.

<sup>2</sup> The realignment process of central parity can be write as:

$$o_t = o_{t_i-1} + a_t (b_t + z_t) \quad (3.2.5)$$

where we assume that  $b_t$  is constant, because only three realignments took place in the ...rst period and only one in the second.

<sup>18</sup>If we don't take into account the target zone, the expression to estimate  $E_{t_i-1}(e_t = I_{t_i-1})$  will be:

$$E_{t_i-1}(e_t = I_{t_i-1}) = \frac{[\%_1 (m_t; m_t^a) + \%_2 (y_t; y_t^a) + x_t]}{(1 - \%_1)}$$

where  $(m_t; m_t^a)$  and  $(y_t; y_t^a)$  follow the expressions (3:2:3) and (3:2:4), respectively.

<sup>19</sup>We test the stationary nature of  $(m_t; m_t^a)$  and  $(y_t; y_t^a)$  using ADF test [Augmented Dickey-Fuller]. We can not reject the unit root in  $(m_t; m_t^a)$ , and we can reject in  $(y_t; y_t^a)$  after correct the seasonal nature.

<sup>2</sup> The matrix of transition probabilities will be:

$$P(t) = \begin{pmatrix} P_{00}(t) & P_{01}(t) \\ P_{10}(t) & P_{11}(t) \end{pmatrix} \quad (3.2.6)$$

where  $P_{11}(t)$  is zero, because we can't find two successive periods when a realignment of central parity took place. Depending of the model used for estimation,  $P_{01}$  will be zero, constant or a variable function that depends on  $r_{t-1}^i$ ,  $r_{t-1}^a$ ,  $(e_{t-1} - o_{t-1})$ ,  $m_{t-1}^i$ ,  $m_{t-1}^a$ ,  $m_{t-2}^i$ ,  $m_{t-2}^a$  and  $y_{t-1}^i$ ,  $y_{t-1}^a$ .

<sup>2</sup> We represent the shock  $\epsilon_t$  in the exchange rate equation such that its variance express the possible effect of a reduction in exchange rate volatility, as target zones models predict.

$$\sigma_{\epsilon_t}^2 = \lambda_0 + \lambda_1 (e_{t-1} - o_{t-1})^2 \quad (3.2.7)$$

With respect to the variances of the shocks  $\epsilon_{1t}$  and  $\epsilon_{2t}$  we assume that there are homoskedastic.

<sup>2</sup> We got the variance-covariance matrix of the maximum likelihood estimator by calculating the estimator called "BHHH".<sup>20</sup>

### 3.3 Estimation Results

We have done the estimation using four different models in the two subperiods respectively. The Mod<sub>1</sub> model makes reference to a lineal rational expectations model, where the existence of the band doesn't matter in the economic agents expectations. Models Mod<sub>2</sub>, Mod<sub>3</sub> and Mod<sub>4</sub> are non linear rational expectations models in which the band influences agent expectations and their differences arise from the probability value:  $P_{01} = 0$  in Z<sub>2</sub>,  $P_{01}$  is a constant different from zero in Mod<sub>3</sub>, and  $P_{01}$  is a variable function

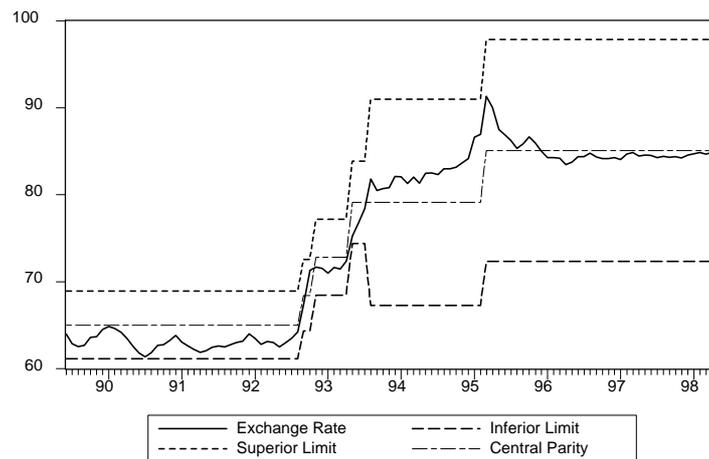
<sup>20</sup>Like Greene (1998) [17, pp. 123-125] explains the variance-covariance matrix of maximum likelihood estimator depends on the parameters. We have apply two alternative methods to estimate: First, the estimator used by Pesaran and Ruge-Murcia (1998), evaluating the second derivatives matrix of maximum likelihood estimator; second, using the BHHH matrix. Like Greene (1998) [17, pp. 124] says, to make use of this matrix is very convenient in some cases because we don't need any additional calculations to get it.

in  $Mod_4$  that depends on  $i_{t-1}$ ,  $r_{t-1}^{\$}$ ,  $(e_{t-1} - o_{t-1})$ ,  $y_{t-1}$ ,  $y_{t-1}^{\$}$  and  $\epsilon_{t-1}$ .

Figure 2 shows the evolution of exchange rate in the sample period, where there aren't values out of the band. The figure shows besides, the edges of the band and the central parity. Then, could be seen, clearly, the four realignments that taken place in the period and the enlargement of the band en august 1993.

A look of the figure, infers us to think, a priori, on a different behavior of the exchange rate between the two subperiods [september 1989 to july 1993, and november 1993 to may 1998].

Figure 2: Evolution of peseta/deutsche mark exchange rate



Then, we are going to study which of those models is the best in order to explain the behavior of the peseta/mark exchange rate. We will show this behavior from different viewpoints. First, we will study the values of the estimated coefficients in the alternative models. Second, we will illustrate it through the conditional variance of the exchange rate shock. Third, we will estimate the realignment probability of the bands in  $Mod_3$  and  $Mod_4$  models.

Finally, we will apply different selecting's criteria.

The estimated coefficient value in the alternative models, with their significance levels for the two subperiods are in tables 1 and 2, respectively.<sup>21</sup> In the first period [september 1989 to july 1993] only the Mod<sub>4</sub> model shows parameters with significance levels different from zero, using the t-statistic. Such parameters will explain better the exchange rate behavior in the period and they are the lagged exchange rate, expectation, lagged money supply and lagged interest rate differential as a variable approaching to the risk premium.

In the second subperiods [november 1993 to may 1998] the results, in significance terms, are not as conclusive as in the first one. In the lineal rational expectations model Mod<sub>1</sub> the parameter of exchange rate expectations is significant, as in Mod<sub>4</sub> model, but it's not less than one.<sup>22</sup> Lagged exchange rate is significant in the Mod<sub>3</sub> model.

With respect to the estimated conditional variance of the exchange rate shock,  $\sigma_{\epsilon_t}^2$ , showed in tables 3 and 4, which equation was  $\sigma_{\epsilon_t}^2 = \zeta_0 + \zeta_1 (\epsilon_{t-1} + \sigma_{\epsilon_{t-1}})^2$ , the differences between subperiods are clear. In the first period, the variance,  $\sigma_{\epsilon_t}^2$ , is constant and then homoskedastic. This result implies that, in the first subperiods, exchange rate variability doesn't depend on exchange rate position with respect to the central parity, and then doesn't verify the honeymoon effect as predicted by the target zones literature, and represented by a shape curve between exchange rate and fundamentals.

In the second subperiods, all estimated coefficients values are close to zero and are not significant. We can deduce a reduced exchange rate variability, at least since 1996 like can be shown in figure 2.

In the econometric specification of the rational expectations solution, we assume that this has a saddle path when the parameter  $z_1$  takes the values

<sup>21</sup> Analyzed the correlation among the variables used in the estimation, and, taking into account to find two economic variable not correlated, we have observed same multicollinearity problems but not too much to be very significant.

<sup>22</sup> If  $z_1$  is not less than one, rational expectations solution could not be unique.

of 1:000, 1:008, 1:005 and 1:021 in Mod<sub>1</sub>, Mod<sub>2</sub>, Mod<sub>3</sub> and Mod<sub>4</sub> models respectively.<sup>23</sup> Then, the estimated value is not less than one in any model, suggesting that exchange rate follows a explosive path. In the ...rst subperiods, we can say that there are not mean reversion as target zone models predict. Once the ...nancial markets assign devaluation expectations to the peseta, the continuous intramarginal or in...nitesimal interventions of monetary authorities won't get intercept capital movements in the markets, usually in much more amount than interventions, and will drive to inevitable devaluation, and then a new central parity of exchange rate.

In the second subperiods, the estimated values of  $z_1$  are, respectively, 0:967, 1:002, 0:995 and 0:997. In this case, the coefficient is less than one except in Mod<sub>2</sub> model. However, this value is close to 1 and then, with a quasi-explosive path.

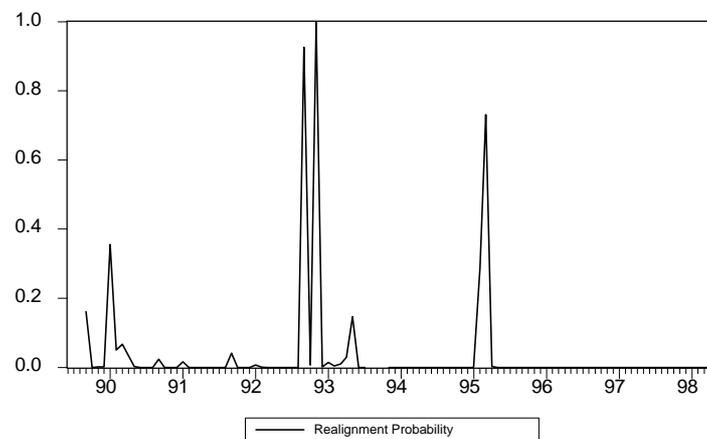
We have estimated the realignment probability of the band in Mod<sub>3</sub> and Mod<sub>4</sub>. The tables 5 and 6 take the estimated values up in the two considered subperiods. In the nonlinear rational expectations Mod<sub>3</sub> model we assume a constant probability. A ...rst approach to this value can be calculated taken into account the number of observations in the sample and the number of realignments happened and dividing both.<sup>24</sup> If we consider the ...rst subperiods, the number of realignments were three and 47 the number of effective observations  $\frac{3}{47} = 0:0638$ . The constant estimated value in the model was 0:0422. One possible explanation for this difference could be the highest proximity between the two ...rst realignments and we can approach the number of realignment to two. In this case,  $\frac{2}{47} = 0:0425$ , that is a value near to the estimated one. In the second subperiods, the number of observations are 55 and there is only one realignment; then,  $\frac{1}{55} = 0:0182$ . The estimated value was 0:0186.

<sup>23</sup>The values are calculated but not show in tables.

<sup>24</sup>That is, applying Laplace Rule:

$$P(z) = \frac{\text{favorables}}{\text{possibles}}$$

Figure 3: Estimated realignment probability



The Mod<sub>4</sub> model assumes that realignment probability depends on a constant, on  $i_{t-1}^r$ ,  $r_{t-1}^c$ ,  $(e_{t-1} - o_{t-1})$ ,  $i_{t-1}^y$ ,  $y_{t-1}^c$  and  $\Phi i_{t-1}^m$ . In the first subperiods, the constant and output differentials are significantly different from zero. In the second subperiods either coefficients are significant. We can see the justification of this results in figure 3 which shows the realignments probabilities in the two subperiods. As a general rule, the observed peaks in probability corresponds to realignments;<sup>25</sup> first, in the beginning of 90's, which corresponds with tensions produced by the dollar fall and rumors about a revaluation of the deutsche mark that didn't happen, and the entrance of Italian lira to the narrow bands of EMS. Then, as was pointed out by Bekaert and Gray (1998), the exchange rate jumps must be modeled depending on the realignments, or on the movements inside the band, because most of the jumps inside the band are of the same amount than realignments.

In our case, the estimated probability in January 1990 [0:3556] is bigger than in May 1993 [0:1467], date when a realignment took place. The other tree peaks

<sup>25</sup>It may be taken into account that, due to lags in estimation, the real sample start in September 1989 and not in June; The second sample start in November 1993 and not in August. Figure 3 reflect the probability in the real sample.

correspond to realignments: september 1992 [0:9258], november 1992 [0:9989] and march 1995 [0:7309]. Then, the estimated probability adjust to the evidence shown in figure 2; when besides, we can see a smooth raise in the probability when the sterling pound incorporates to EMS and the opposite position with respect to the peseta desestabilizing the last one.

The only thing we miss in the estimation of the probability is the measure the possible effect on the probability of band enlargement due to information loss for dividing the sample in two.

To verify which model better explain the behavior of realignment probability [the Mod<sub>3</sub> model with constant probability or Mod<sub>4</sub> model with variable] we contrast both models using the likelihood ratio test, which is shown in table 7 for first period and 8 for the second. The likelihood ratio test is given by  $LR = \frac{L^3(\beta)}{L^4(\beta)}$  and is distributed like a  $\chi^2$  with four degrees of freedom. For the first subperiods, the value of LR-Test is 41:724, and allows us not to reject Mod<sub>4</sub> model to a significative level of 99%. In the second subperiods the value is 7:228 and the significative level is 87%.

However, our intention is not only to study which model interprets better the probability, but also to find which one better explains exchange rate behavior. For this reason, we compare the four estimated models with two others that model the exchange rate behavior in a simple way. We modeled the exchange rate like a Random walk, RW, and like a GARCH(1,1) [Generalized Autorregressive Conditional Heteroscedasticity] process, RW<sub>GARCH</sub>. The results and the different criteria used are compiled for both subperiods in tables 7 and 8 respectively.

The criteria used are the following:

<sup>2</sup> AIC [Akaike Information Criterion]: calculated like Pesaran and Ruge-Murcia (1999), that is the difference between the maximized value of the

likelihood function associated to the exchange rate and the number of estimated parameters in each equation. [15 parameters in Mod<sub>1</sub> and Mod<sub>2</sub> models, 16 in Mod<sub>3</sub>, 20 in Mod<sub>4</sub>, 2 in RW and 4 in RW<sub>GARCH</sub> model]<sup>26</sup>

<sup>2</sup> RMSFE [Root Mean Squared Forecast Errors] defined like:

$$\text{RMSFE} = \frac{\sum_{t=1}^T [e_{t+1} - E_{t+1}(e_{t+1})]^2}{T} \quad (3.3.1)$$

where T represents the observations number in the sample.

<sup>2</sup> AMFE [Absolute Mean Forecast Errors] defined like:

$$\text{AMFE} = \frac{\sum_{t=1}^T |e_{t+1} - E_{t+1}(e_{t+1})|}{T} \quad (3.3.2)$$

where T represents the same than RMSFE.

In the first subperiods, the three criteria show that the better model is nonlinear rational expectations with variable probability of band realignment [Mod<sub>4</sub>]. Then, the model which better explains the peseta/deutsche mark bilateral exchange rate is a model which incorporates the band in economic agents expectations and that are influenced by lagged exchange rate, the differential in the money supply and the risk premium approached by interest rate differential and in which the realignment probability exists with values different from zero and is function of output differentials between Germany and Spain.

With respect to the second subperiods the results are not as conclusive as in the first subperiods. We pointed out that, with the exception of march 1995 devaluation. This period can be represented by a stability in the exchange rate, at least since mid 1996. From the chosen criteria point of view, the RMSFE choose Mod<sub>2</sub> model follow by Mod<sub>1</sub> model. If we use AIC or AMFE criteria,

<sup>26</sup>About selection criteria of models see Lütkepohl (1991) [22, pp. 118-166]

the best model is Mod<sub>1</sub>. In this model, economic agents don't take into account the band when form their expectations and the realignment probability of the band is zero. This result points out that with a band of 30% the economic agents act like a quasi-flexible exchange rate system and where a contractive fiscal stance with a control on public deficit since march 1996 and the fulfillment of convergence criteria have a positive influence over exchange rate stability. The perspectives of incorporation of Spain in the first phase of EMU have made that realignment probability has been zero for the most of period.<sup>27</sup>

## 4 Conclusions

The argue about exchange rate behavior has been the object of special interest, academic and politic, with respect to the excessive volatility and realignments. A theoretical proposal driven to try to reduce the exchange rate volatility, and over all, its sudden movements has been the called " Target Zones Models" in continuous time. In this paper we developpe a theoretical modelization their rational expectations, in discrete time, in the line with the LD-RE and we estimate it for the peseta/deutsche mark exchange rate. We employ such a model because, in difference with amplified target zone model, we have, not only the possibility of intramarginal intervention, stochastic realignment expectations and predetermined prices, but also that the existence of the band is taken into account when economic agents take expectations.

The estimation results show a clear difference between the period before and after the modification of the band width. The results, on the other band, can be surprising, at least for the first path of the sample, because don't verify the regularities found for other exchange rates in the EMS. However, they explain coherently the peseta/deutsche mark exchange rate evolution in the sample.

We find the following regularities:

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<sup>27</sup> Like can find in figure 3, of 55 observations that enter in the second subperiod, only nine takes a value different from zero.

<sup>2</sup> The sample from June 1989 to July 1993 is characterized by a strong volatility in the peseta/deutsche mark exchange rate, sometimes near to the maximum appreciation, and sometimes in the maximum limit of depreciation and besides the three central parity realignments. We find new regularities for the Spanish case different from Pesaran and Ruge-Murcia (1999) for French franc/deutsche mark exchange rate. These are the following:

- There are not a shape curve between the exchange rate and fundamentals, and then, there is not honeymoon effect like target zones literature predicts. On the contrary, like suggest Bertola and Caballero (1992.a, 1992.b), the realignment expectations in the band can invert the Krugman (1991) SS curve.
- Once the agents expect that the peseta/deutsche mark exchange rate is going to devaluate, press with speculative attacks in such amount that either intramarginal or infinitesimal interventions can impede devaluation.
- The realignment probability of the band have existed and there has been not constant. Such realignment probability took positive values as inside take band as when the band is realigned.
- The model that better explains the exchange rate evolution is this part of the sample is a LD-RE model with variable probability. This realignment probability depends on exchange rate expectations, the differential in money supply and the risk premium approached by lagged interest rate differential.

<sup>2</sup> The sample from August 1993 to May 1998 is characterized by a low volatility in the peseta/deutsche mark exchange rate, with the exception of devaluation on March 1995. This period wasn't analyzed by Pesaran and Ruge-Murcia (1999) and the results are totally new. This result has been the following:

- The results are not conclusive with respect to maintenance of the "S" relation between exchange rate and fundamentals.

- Neither about the existence of mean reversion because  $z_1$  takes values near to 1.
- The realignment probability of the band has been constant and near to zero with the exception of the period just before the devaluation in march 1995.
- We can not characterize exchange rate evolution with a model because the results are not conclusive. However, there are nearer to a linear rational expectations model than a nonlinear model with variable realignment probability. When we use the probability, on the other hand, the second one is better than the ...rst one to predict the probability.

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Table 1: Estimated Parameters in the ...rst sample (September 1989-July 1993)

Explanatory Variables	Mod <sub>1</sub>	Mod <sub>2</sub>	Mod <sub>3</sub>	Mod <sub>4</sub>
Constant	0:068 (0:022)	i 0:825 (i 0:245)	i 0:326 (i 0:149)	i 0:535 (i 0:124)
$e_{t_i-1}$	i 0:819 (i 0:590)	0:518 (0:344)	0:622 (0:650)	0:168 <sup>***</sup> (1:883)
$E_{t_i-1}(e_{t_i-1})$	1:818 (1:295)	0:487 (0:341)	0:381 (0:451)	0:810 <sup>***</sup> (11:572)
$(m_{t_i}   m_{t_i}^a)$	i 0:099 (i 0:040)	i 1:193 (i 1:590)	0:024 (0:040)	i 2:220 <sup>***</sup> (i 1:943)
$(y_{t_i}   y_{t_i}^a)$	0:925 (0:541)	i 1:026 (i 0:584)	0:504 (i 0:051)	i 0:015 (i 0:002)
$i r_{t_i-1}   i r_{t_i-1}^a$	i 0:344 (i 0:259)	i 0:567 (i 0:450)	i 0:323 (i 0:317)	i 1:218 <sup>***</sup> (i 3:210)
$(e_{t_i-1}   o_{t_i-1})$	i 0:012 (i 0:065)	0:027 (0:214)	0:070 (0:008)	i 0:018 (i 0:021)
$\Phi i m_{t_i-1}   m_{t_i-1}^a$	i 1:305 (i 0:395)	0:978 (0:466)	0:997 (0:721)	i 0:394 (i 0:134)
$\Phi i y_{t_i-1}   y_{t_i-1}^a$	i 0:091 (i 0:051)	i 1:158 <sup>**</sup> (i 1:714)	i 0:086 (i 0:080)	0:371 (0:484)
$\Phi i m_{t_i-2}   m_{t_i-2}^a$	i 1:344 (i 0:341)	0:165 (0:033)	0:593 (0:314)	0:365 (0:028)
$\Phi i y_{t_i-2}   y_{t_i-2}^a$	0:169 (0:212)	i 1:110 (i 1:344)	i 0:268 (i 0:772)	i 0:219 (i 0:693)
$\Phi i r_{t_i-2}   r_{t_i-2}^a$	0:056 (0:019)	0:653 (0:221)	0:385 (0:239)	0:056 (0:031)
$\Phi (e_{t_i-2}   o_{t_i-2})$	i 0:073 (i 0:073)	0:100 (1:610)	0:055 (0:630)	0:003 (0:0004)

Note: Mod<sub>1</sub> refers a linear RE model that does not take into account the effect of the band on expectations. Mod<sub>2</sub>, Mod<sub>3</sub> and Mod<sub>4</sub> are non linear RE models where the band affects agents' expectations and different realignment probabilities.

$P_{01} = 0$  in Mod<sub>2</sub>,  $P_{0\Phi}$  is a constant different from zero in Mod<sub>3</sub> and  $P_{01}$  is a function of  $i r_{t_i-1} | i r_{t_i-1}^a$ ,  $(e_{t_i-1} | o_{t_i-1})$ ,  $\Phi i m_{t_i-1} | m_{t_i-1}^a$  and  $\Phi i y_{t_i-1} | y_{t_i-1}^a$  in Mod<sub>4</sub>. The value into a parenthesis is the t-statistic and <sup>\*</sup>, <sup>\*\*</sup> and <sup>\*\*\*</sup> denotes the significance of 10, 5 or 1 % respectively.

Table 2: Estimated Parameters in the second sample (November 1993-May 1998)

Explanatory Variables	Mod <sub>1</sub>	Mod <sub>2</sub>	Mod <sub>3</sub>	Mod <sub>4</sub>
Constant	i 0:951 (i 1:209)	0:007 (0:0006)	0:142 (0:363)	0:105 (0:328)
$e_{t_i-1}$	i 0:068 (i 0:317)	0:256 (0:449)	0:899 <sup>***</sup> (3:177)	0:129 (0:443)
$E_{t_i-1}(e_{t_i-1})$	1:070 <sup>***</sup> (4:623)	0:745 (1:324)	0:096 (0:338)	0:870 <sup>***</sup> (2:967)
$(m_{t_i}   m_{t_i}^a)$	i 0:222 (i 0:010)	i 0:784 (i 0:629)	0:246 (0:146)	0:273 (0:281)
$(y_{t_i}   y_{t_i}^a)$	0:038 (0:035)	i 0:157 (i 0:247)	i 0:046 (i 0:001)	i 0:054 (i 0:004)
$i r_{t_i-1}   r_{t_i-1}^a$	i 0:008 (i 0:008)	i 0:495 (i 1:358)	i 0:002 (i 0:0008)	i 0:012 (i 0:007)
$(e_{t_i-1}   o_{t_i-1})$	i 0:004 (i 0:003)	0:016 (0:014)	0:006 (0:0008)	0:009 (0:010)
$\Phi i m_{t_i-1}   m_{t_i-1}^a$	0:214 (0:014)	i 0:075 (i 0:067)	i 0:275 (i 0:016)	i 0:347 (i 0:046)
$\Phi i y_{t_i-1}   y_{t_i-1}^a$	0:007 (0:010)	i 0:080 (i 0:020)	i 0:011 (i 0:0008)	i 0:022 (i 0:0007)
$\Phi i m_{t_i-2}   m_{t_i-2}^a$	i 0:131 (i 0:031)	0:823 (0:321)	0:200 (0:058)	0:348 (0:274)
$\Phi i y_{t_i-2}   y_{t_i-2}^a$	0:084 (0:069)	i 0:320 (i 0:321)	i 0:115 (i 0:007)	i 0:161 (i 0:018)
$\Phi i r_{t_i-2}   r_{t_i-2}^a$	1:540 (0:077)	i 1:641 <sup>***</sup> (i 3:277)	i 2:109 (i 0:079)	i 2:788 (i 0:108)
$\Phi (e_{t_i-2}   o_{t_i-2})$	0:003 (0:003)	i 0:044 (i 0:012)	i 0:004 (i 0:003)	i 0:007 (i 0:0005)

Note: Mod<sub>1</sub> refers a linear RE model that does not take into account the effect of the band on expectations. Mod<sub>2</sub>, Mod<sub>3</sub> and Mod<sub>4</sub> are non linear RE models where the band affects agents' expectations and different realignment probabilities.

$P_{01} = 0$  in Mod<sub>2</sub>,  $P_{01}$  is a constant different from zero in Mod<sub>3</sub> and  $P_{01}$  is a function of  $r_{t_i-1}$ ,  $r_{t_i-1}^a$ ,  $(e_{t_i-1} | o_{t_i-1})$ ,  $\Phi i m_{t_i-1} | m_{t_i-1}^a$  and  $\Phi i m_{t_i-2} | m_{t_i-2}^a$  and  $y_{t_i-1} | y_{t_i-1}^a$  in Mod<sub>4</sub>. The value into a parenthesis is the t-statistic and <sup>\*</sup>, <sup>\*\*</sup> and <sup>\*\*\*</sup> denotes the significance of 10, 5 or 1 % respectively.

Table 3: Estimation of conditional variance of exchange rate shocks in the first sample (September 1989-July 1993)

Models	Constant	$(e_{t-1} - o_{t-1})^2$
Mod <sub>1</sub>	1:900 (1:503)	0:000 (0:000)
Mod <sub>2</sub>	1:445 <sup>***</sup> (5:162)	0:000 (0:000)
Mod <sub>3</sub>	1:576 <sup>***</sup> (6:065)	0:000 (0:000)
Mod <sub>4</sub>	1:219 (0:286)	0:000 (0:000)

Table 4: Estimation of conditional variance of exchange rate shocks in the second sample (November 1993-May 1998)

Models	Constant	$(e_{t-1} - o_{t-1})^2$
Mod <sub>1</sub>	0:065 (0:007)	0:069 (0:004)
Mod <sub>2</sub>	0:104 (0:008)	0:076 (0:008)
Mod <sub>3</sub>	0:066 (0:0002)	0:067 (0:0002)
Mod <sub>4</sub>	0:066 (0:007)	0:068 (0:005)

Note: Mod<sub>1</sub> refers a linear RE model that does not take into account the effect of the band on expectations. Mod<sub>2</sub>, Mod<sub>3</sub> and Mod<sub>4</sub> are non linear RE models where the band affects agents' expectations and different realignment probabilities.

$P_{01} = 0$  in Mod<sub>2</sub>,  $P_{01}$  is a constant different from zero in Mod<sub>3</sub> and  $P_{01}$  is a function of  $r_{t-1}$ ,  $r_{t-1}^*$ ,  $(e_{t-1} - o_{t-1})$ ,  $m_{t-1}$  and  $m_{t-1}^*$  in Mod<sub>2</sub> and  $y_{t-1}$  and  $y_{t-1}^*$  in Mod<sub>4</sub>. The value into a parenthesis is the t-statistic and <sup>\*</sup>, <sup>\*\*</sup> and <sup>\*\*\*</sup> denotes the significance of 10, 5 or 1 % respectively.

Table 5: Estimation of Realignment Probability of the Band in the first sample (September 1989-July 1993)

Explanatory Variables	Mod <sub>3</sub>	Mod <sub>4</sub>
Constant	0:042 (0:478)	i 5:170 <sup>***</sup> (i 2:042)
$i r_{t_i-1} \quad i r_{t_i-1}^{\alpha}$		8:290 (0:849)
$(e_{t_i-1} \quad o_{t_i-1})$		2:098 (0:869)
$i y_{t_i-1} \quad i y_{t_i-1}^{\alpha}$		i 18:407 <sup>***</sup> (i 2:715)
$\epsilon \quad i m_{t_i-1} \quad m_{t_i-1}^{\alpha} \quad i \quad i m_{t_i-2} \quad m_{t_i-2}^{\alpha}$		10:675 (0:788)
$L_0$	i 11:264	i 2:926

Table 6: Estimación de la probabilidad de reajuste de las bandas de fluctuación en la segunda submuestra (Noviembre 1993-Mayo 1998)

Explanatory Variables	Mod <sub>3</sub>	Mod <sub>4</sub>
Constant	0:018 (0:005)	i 27:00 (i 0:320)
$i r_{t_i-1} \quad i r_{t_i-1}^{\alpha}$		i 1:423 (i 0:013)
$(e_{t_i-1} \quad o_{t_i-1})$		3:071 (0:005)
$i y_{t_i-1} \quad i y_{t_i-1}^{\alpha}$		i 14:382 (i 0:241)
$\epsilon \quad i m_{t_i-1} \quad m_{t_i-1}^{\alpha} \quad i \quad i m_{t_i-2} \quad m_{t_i-2}^{\alpha}$		12:563 (0:036)
$L_0$	i 4:980	i 0:654

Note: The value into a parenthesis is the t-statistic and <sup>\*</sup>, <sup>\*\*</sup> and <sup>\*\*\*</sup> denotes the significance of 10, 5 or 1 % respectively.  $L_0$  is the maximized value of log-likelihood function associated with changes in central parity.

Table 7: Selection Models Criteria in the first sample (September 1989-July 1993)

Models	$L_e$	AIC	RMSFE	AMFE	L (\$)	$\frac{1}{2}$
Mod <sub>1</sub>	-40.084	-55.084	1.429	0.991	-	1
Mod <sub>2</sub>	-37.233	-52.233	1.328	0.986	-	12.00
Mod <sub>3</sub>	-39.671	-55.671	1.406	1.016	216.348	12.00
Mod <sub>4</sub>	-27.139	-47.139	1.078	0.790	237.210	12.00
RW	-79.936	-81.936	1.375	0.988	-	1
RW <sub>GARCH</sub>	-75.929	-79.929	1.389	0.978	-	1

Table 8: Selection Models Criteria in the second sample (November 1993-May 1998)

Models	$L_e$	AIC	RMSFE	AMFE	L (\$)	$\frac{1}{2}$
Mod <sub>1</sub>	7.795	-7.205	0.1491	0.5542	-	1
Mod <sub>2</sub>	0.232	-14.768	0.1465	0.5923	-	30.00
Mod <sub>3</sub>	6.731	-9.269	0.150	0.5697	352.956	30.00
Mod <sub>4</sub>	6.645	-13.355	0.1498	0.5709	356.570	30.00
RW	-87.006	-89.006	1.0845	0.6392	-	1
RW <sub>GARCH</sub>	-68.768	-72.768	1.0929	0.6292	-	1

Note: Mod<sub>1</sub> refers a linear RE model that does not take into account the effect of the band on expectations. Mod<sub>2</sub>, Mod<sub>3</sub> and Mod<sub>4</sub> are non linear RE models where the band affects agents' expectations and different realignment probabilities.

$P_{01} = 0$  in Mod<sub>2</sub>,  $P_{01}$  is a constant different from zero in Mod<sub>3</sub> and  $P_{01}$  is a function of  $r_{t-1}$ ,  $r_{t-1}^a$ ,  $(e_{t-1} - o_{t-1})$ ,  $\phi_1 m_{t-1}$ ,  $m_{t-1}^a$ ,  $\phi_2 m_{t-2}$ ,  $m_{t-2}^a$  and  $y_{t-1}$ ,  $y_{t-1}^a$  in Mod<sub>4</sub>. The RW and RW<sub>GARCH</sub> models express exchange rate behavior like a random walk with drift, RW, with homoskedastic variance, and a conditional variance like a GARCH(1,1), RW<sub>GARCH</sub>, respectively.  $L_e$  represents the value of maximized log-likelihood function associated with exchange rate and  $L(\$) = L_f(\$_1) + L_a(\$_2) + L_o(\$_3) + L_e(\$_4)$  is the maximized value of log-likelihood.