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Financial Market Imperfections and the Pricing Decision of Firms: Theory and Evidence

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# Financial Market Imperfections and the Pricing Decision of Firms: Theory and Evidence

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#### Abstract

This paper investigates how financial market imperfections and nominal rigidities interact. Based on new firm-level evidence for Germany, we document that financially constrained firms adjust prices more often than their unconstrained counterparts. In particular, financially constrained firms do not only increase prices, but also decrease prices more often. We show that these empirical patterns are consistent with a partial equilibrium menu-cost model with financial frictions. Our results suggest that tighter financial constraints are associated with higher nominal rigidities, higher prices and lower output. Furthermore, financial recessions may induce very different dynamics than normal recessions if the relative size of unexpected financial shocks is large relative to aggregate price shocks.

Keywords: Price distribution, financial frictions, menu cost model

JEL-Codes: E31, E44

## 1 Introduction

This paper investigates the interaction between financial frictions and the price setting of firms. Financial frictions and price setting may affect each other in two ways: On the one hand, being financially constrained may affect the pricing decision of a firm: firms with initially low prices that sell large quantities may not be able to finance their production inputs and may therefore find it optimal to scale down production and adjust prices up. On the other hand, firms seeking to gain market share may want to lower their prices. However, by doing so, they may run into financial constraints when expanding production. We show empirically and theoretically that both of these mechanisms are important for understanding the frequency, the direction, the size and the dispersion of individual firms' price changes. Moreover, the explicit interaction between financial frictions and the cross-sectional distribution of prices turns out to be of crucial relevance for the behavior of aggregate price rigidity over time and thus, for the transmission of macroeconomic shocks as well as the effectiveness of monetary policy.

We explore rich plant-level data for Germany: the ifo Business Survey, a monthly representative panel of 3600 manufacturing firms covering the years 2002-2014. The survey contains information about the extensive margin, i.e., whether and in what direction individual firms change prices, alongside two direct firm-specific measures of financial constraints. In particular firms give appraisals of their access to bank credit which is the predominant way of financing operational costs and investment. Firms also report whether they are experiencing production shortages due to financial constraints. In contrast, most of the existing literature has focused on price adjustment along the intensive margin, while, at the same time, relying on indirect measures of individual financial conditions such as the state of the business cycle or balance sheet measures. Since we have balance sheet information for a subset of firms in our sample, we can compare direct and indirect measures of financial constraints and document important differences.

Using our survey measures, we show that financially constrained firms adjust their prices more frequently than financially unconstrained firms. Moreover, constrained firms adjust their prices down more often than their unconstrained counterparts. In contrast, the existing studies highlight that financially constrained firms tend to decreases their prices less often (Bhaskar et al., 1993) or increase their prices more often than unconstrained firms (Gilchrist et al., 2013a), at least in recessions. We document that the latter effect is due to using balance sheet information, e.g. liquidity or cash flow ratios, in order to indirectly measure financial frictions. Generally, a low liquidity ratio can be the result of easy access to credit, while not affecting production possibilities of firms. It may therefore not measure financial constraints per se. For example, consider a firm experiencing a sudden decline in its marginal costs. Such a firm will typically decrease its prices and try to scale up the level of operation. If expanding the production capacity requires external funding, the firm may hit the upper limit of its financial constraint, but may still enjoy a relatively high liquidity ratio. Hence, one may wrongly conclude that it is financially unconstrained today.

Our interpretation of the empirical facts is guided by a partial-equilibrium menu cost model with financial frictions which provides an explicit rationale for the interactions between financial constraints and price setting. Here, we extend the standard menu-cost model<sup>3</sup> with heterogeneous firms by adding

<sup>&</sup>lt;sup>1</sup>See for example Chevalier and Scharfstein (1996) for the US or Gottfries (2002) and Asplund et al. (2005) for Sweden. An exception is Gilchrist et al. (2013b) in a study for the US.

<sup>&</sup>lt;sup>2</sup>The study closest to our paper that uses balance sheet measures is Gilchrist et al. (2013a). Only Bhaskar et al. (1993) use a small-sample cross-sectional survey for small firms in the UK.

<sup>&</sup>lt;sup>3</sup>Gilchrist et al. (2013a) calibrate a partial equilibrium menu-cost model to match US consumer price data. Most studies developing general equilibrium versions of the model with Ss pricing focus on the implied degree of monetary non-neutrality. For example Caplin and Spulber (1987), Dotsey et al. (1999) and Golosov and Lucas (2007) resort to the standard menu-cost model, extensions as stochastic idiosyncratic menu costs and leptokurtic productivity shocks are analysed in Dotsey and King (2005) and Midrigan (2005) respectively, multi-sector and multi-product versions of the model

a working capital constraint.<sup>4</sup> When financial frictions are present, the individual firm's profit function becomes more concave and asymmetric at the relative price below which the constraint binds. Since the shape of the profit function is a crucial determinant of the gains from price adjustment in a menu-cost environment, the presence of a financial constraint affects the pricing decisions of different firms differently depending on the current state of the firm. In particular, for relatively high levels of idiosyncratic productivity, the optimal price induces that the financial constraint binds, i.e., those firms that adjust prices (up or down) will be financially constrained. This implication is consistent with our empirical findings suggesting that the financially constrained firms adjust their prices more frequently, both up and down, compared to their unconstrained counterparts.

Our model simulations show that when more of the firms that adjust their price are constrained, unconstrained firms change their prices less often. If the latter are still many, nominal rigidities are higher in a situation with compared to without financial constraints. Moreover, tighter financial constraints induce higher average prices, lower average output and a lower dispersion of the cross-sectional distribution of prices. The output and price effects are stronger in a situation with compared to without menu costs, since for some firms it is now optimal not to change their prices when their prices are close to but above the constraint, but they will have to change their price when they are close to but below the constraint. In addition, firms for which the financial constraint binds find it optimal not to change their price, but to ration output instead. This poses a conflict of interest to the central bank, since traditional monetary policy might increase output, but push up prices even higher. In turn, reducing financial frictions might lead to lower nominal rigidities and may lead to monetary policy being less effective.

We further consider the response of the average price changes, average prices and price dispersion to shocks to the aggregate price level. In our partial-equilibrium model, these shocks can be interpreted as responses of a single sector to aggregate business cycle shocks. Doing so, we obviously ignore important general equilibrium effects, in particular the response of wages. We nevertheless believe this to be an instructive exercise as wages might be sticky in the short run. In particular, we consider the responses when negative price shocks are combined with an unexpected tightening of the financial constraint, i.e., a financial recession. When negative price shocks are large and financial tightening relatively small the dynamics resemble those in German manufacturing during the Great Recession. In particular, constrained firms decrease their prices more often, but overall nominal rigidities increase, since unconstrained firms change their prices less often. Hence, when financial constraints are present, monetary policy becomes less effective in recessions. In contrast, when financial shocks are large relative to aggregate price shocks, average prices fall by less with compared to without financial constraints. This model implication is very similar to what has been highlighted as the "cost channel" of financial frictions by Gilchrist et al. (2013a), albeit with a completely different mechanism. This effect is intensified in the presence of menu costs: Nominal rigidities decrease and firms do not only adjust prices up more often but also to even higher levels than without menu costs.

The remainder of the paper is organized as follows. Section 2 documents the data and the empirical relationship between financial frictions and the price setting of firms. Section 3 presents the model and quantitative results. Section 4 concludes.

are developed by Nakamura and Steinsson (2010) and Alvarez and Lippi (2013), while Vavra (2013) and Bachmann et al. (2013a) investigate the consequences of uncertainty shocks for the price distribution and the effectiveness of monetary policy.

<sup>&</sup>lt;sup>4</sup>In contrast, existing studies on the interaction between financial frictions and pricing decisions consider the intensive margin only, i.e., the fraction of firms that adjust prices is always equal to one, see e.g. Gottfries (1991), Chevalier and Scharfstein (1996) or Lundin and Yun (2009). Up to our knowledge, there so far exists no menu-cost model with financial frictions.

# 2 Empirical Evidence

#### 2.1 Data

We use data from the ifo Business Survey which is a representative sample of 3600 plants in the German manufacturing sector in 2002-2014. The survey starts as early as the 1950's, but our sample is restricted by the fact that the questions about financial constrainedness was added in 2002. The main advantages of the dataset relative to data used in other studies on price stickiness are twofold. First it enables us to link individual plant's pricing behavior both to direct survey-based measures of the plant-specific degree of financial constrainedness and to indirect proxies for the financial situation based on balance sheet information. Second, the survey is conducted on a monthly basis which enables us to track important aspects of a plant's actual behavior over time as it undergoes both, phases of easy and such of subdued access to credit while, at the same time, facing the alternating states of the business cycle. Since plants respond on a voluntary basis and, thus, not all plants respond every month, the panel is unbalanced.

In particular, we have monthly information about the extensive margin of price adjustment - i.e. whether and in what direction firms adjust prices.<sup>5</sup> More precisely, firms answer to the question: "Have you in the last month increased, decreased or left unchanged your prices?". We unfortunately do not have information about the intensive margin of price adjustment in our dataset. While our empirical analysis is limited to the extensive margin, our model in section 3 will have implications about size of price adjustments as well as price dispersion. More than 97% of the cross-sectional units in our sample are single-product plants. Additionally, some plants fill in a separate questionnaire for each product (product group) they produce. In what follows, we use the terms "firm", "plant" and "product" interchangeably.<sup>6</sup>

The ifo survey encompasses two questions regarding the financial constrainedness of firms. In the monthly survey, firms are asked about their access to bank lending: "Are you experiencing restrictive, normal or accommodating willingness of banks to lend?" We flag firms as financially constrained when they answer that bank lending is restrictive. Note that this answer might imply that firms experience restrictive bank lending in general, but do not necessarily need to borrow more, i.e., they are potentially not restricted in the way they invest, hire or produce. Figure A-1 in the Appendix shows a time-series plot of this measure of financial constraints. One can see that the fraction of constrained firms increases in a boom and decreases in a recession. A second question in the survey gets closer to this notion of financial constraints: "Are you experiencing production shortages due to financial constraints?". This question is very close to the actual definition of financial constraints in the economic model that we present below. However, it is only available at quarterly frequency.

Table 1 shows the relationship between price adjustments and being financially constrained. According to the bank lending question, 32% of all firms are financially constrained. According to the production shortage question, only 5% of firms are constrained on average. Clearly, the last measure can be viewed as a lower bound for the fraction of firms facing difficulties in obtaining external funds. In general few German firms adjust their prices on a monthly basis - a little more than 20%. However, if financially constrained, firms adjust their prices relatively more often. Furthermore, the fraction of price decreases is higher among financially constrained firms than among their unrestricted counterparts. This is true for both measures of financial constrainedness. With respect to price increases, the fraction of firms raising prices is higher for unconstrained than for constrained firms when using the bank lending

<sup>&</sup>lt;sup>5</sup>These prices are home country producer prices for all products of a particular firm. Bachmann et al. (2013b) have used the same dataset to assess the effect of uncertainty shocks on price setting.

<sup>&</sup>lt;sup>6</sup>Restricting our sample to the single-product cases only leaves our quantitative results unchanged. Results are available upon request.

Table 1: Financial Constraints and Price Setting

	unconstrained	constrained
$\underline{Bank\ lending}$		
Fractions	0.68	0.32
$\Delta p = 0$	0.80	0.76
$\Delta p < 0$	0.08	0.14
$\Delta p > 0$	0.13	0.10
$Production\ shortage$		
Fractions	0.95	0.05
$\Delta p = 0$	0.80	0.75
$\Delta p < 0$	0.08	0.12
$\Delta p > 0$	0.11	0.13

Source: ifo Business Survey, 2002-2014. Numbers shown are sample averages of fractions of constrained and unconstrained firms in all firms and fractions of price changes within unconstrained and constrained firms. Numbers for production shortage question are based on quarterly data, interpolated to monthly frequency.

measure, while the opposite is true when considering production shortages.

Based on this finding, one would like to know whether financially constrained and unconstrained firms are systematically different in some important aspect. The literature has discussed that small rather than large firms tend to be financially constrained. Table A-1 in the Appendix documents that this is not the case for our sample. In fact, the size distribution within financially constrained and unconstrained firms is very similar.

Figures A-2 to A-4 show time-series plots of pricing decisions of financially constrained and unconstrained firms respectively using the bank lending question. One can see that all firms decreases prices more often and increase prices less often in a recession. Over time, financially constrained firms decrease prices more often than unconstrained firms, regardless of the business cycle state. While the differences between price increases of constrained and unconstrained firms is small, more unconstrained firms leave prices constant relative to constrained firms in a recession compared to outside a recession. Clearly, the time series variation of pricing decisions may be driven by two facts: the business cycle itself and a possible selection of firms over the business cycle.

We further decompose the correlation between price changes and financial constrainedness into within and between firm effects using the following specification

$$P(\Delta p_{ijt} \le 0 | x_{ijt}) = \beta_0 + \beta_1 F C_{ijt} + c_j + \theta_t + u_{ijt}. \tag{1}$$

We estimate this equation using a Mlogit specification in which the dependent variable measures whether prices increase or decrease relative to no price changes. The right-hand side contains one of our two survey measures of financial constraints as well as sector and time fixed effects.<sup>8</sup> The coefficient  $\beta_1$  then measures the within-firm variation over time between being financially constrained and the probability of adjusting price up or down. Note that this coefficient should not be interpreted as causal, since it may well be that price adjustments influence whether a firm is financially constrained or not (as is motivated in the introduction and documented in detail in section 3 below). Instead, this specification seeks to

 $<sup>^{7}</sup>$  See Carpenter et al. (1994) for an early contribution on the topic.

<sup>&</sup>lt;sup>8</sup> To control for heteroscedasticity and within firm correlation of the residuals we compute robust standard errors clustered by firm. Clustering by sector delivers the same results regarding the significance of the estimated coefficients.

control for variation over time, i.e., business cycle effects, as well as possible selection of firms into being financially constrained or not that could have influenced the unconditional moments in Table 1.

Table 2 shows the results for this specification using either the question concerning restrictive bank lending (upper panel) or production shortages as measures of financially constrained firms (lower panel). One can see that in both cases, the finding that financially constrained firms decrease their prices more often than their unconstrained counterparts is robust with respect to the measure of the firm's financial situation as well as controlling for sector and time fixed effects. In the case of price increases, the results are more mixed. Nevertheless, when including time and sector fixed effects, financially constrained firms increase their prices more often than financially unconstrained firms. Overall, the results of the Mlogit estimation suggest that financially constrained firms change their prices significantly more often in both directions, upwards and downwards. Furthermore, linear regressions or separate logit models for price increases or price decreases deliver essentially the same results. Finally, estimating the link between the price change in the current month  $\Delta p_{ijt}$  and the access to bank lending in the previous month also confirm our baseline estimates.

Table 2: Financial Constraints and Price Setting: Within Firm Effects

				0	THIII Effects		
Restrictive bank lending							
		no	time	sector	time & sector		
price	variable	fixed effects	fixed effects	fixed effects	fixed effects		
$\downarrow$	FC	0.650***	0.473***	0.654***	0.476***		
*		(0.0256)	(0.0266)	(0.0271)	(0.0282)		
<b>↑</b>	FC	-0.225***	0.0345	-0.236***	0.0391		
I	10	(0.0265)	(0.0277)	(0.0279)	(0.0293)		
		Pro	duction shorta	øe.			
		110	duction bhorta	18°			
		no	$_{ m time}$	sector	time & sector		
price	variable	fixed effects	fixed effects	fixed effects	fixed effects		
1	FC	0.415***	0.308***	0.366***	0.251***		
<b>\</b>	10	(0.0517)	(0.0526)	(0.0543)	(0.0554)		

(0.0497) (0.0509) (0.0519) (0.0534)

Notes: MLOGIT estimation: Base outcome is prices unchanged. Sample: January 2002 - December 2013. Standard errors in parentheses: \*\*\* p < 0.01, \*\*\* p < 0.05, \* p < 0.1. Includes only observations for which balance sheet data are available. Monthly data for restrictive bank lending, quarterly data (interpolated) for production shortages.

0.261\*\*\*

FC

0.203\*\*\*

0.339\*\*\*

0.277\*\*\*

In a related paper, Gilchrist et al. (2013a) show that US firms that are financially constrained increase prices more often than their unconstrained counterparts, but do not decrease their prices more often. While the first finding is supported using our dataset, sample and specification, the second finding is not. A potential source of this difference is the measure of financial constrainedness of firms. While we use direct survey questions to identify financially constrained firms, Gilchrist et al. employ an indirect measure based on balance sheet information of firms. In line with Gilchrist, financial constraints may be measured in three possible ways: liquidity ratios (cash and other liquid assets over total assets), cash flow ratios (operating income over total assets) and interest coverage ratios (interest expenses over total

assets). The lower the liquidity and cash flow ratio and the higher the interest coverage ratio, the more constrained a firm. Constrained firms are then those with liquidity or cash flow ratios below, or interest rate coverage ratios above the median value of all firms.

For a subsample of the firms in our survey, we have access to balance sheet information and we can calculate the respective indicators on an annual basis<sup>9</sup>. Tables A-2 to A-4 in the Appendix show that liquidity and cash flow ratios are lower and interest coverage ratios higher for firms that are constrained according to our survey questions. However, the correlations between the balance sheet measures and our survey questions are very small. Moreover, of those firms that are unconstrained according to the production shortage question, close to 50% are constrained according to balance sheet measures. These may be firms that have already borrowed a lot, possibly due to good access to credit, but being indebted does not affect their production possibilities. Since this last aspect is usually key for most economic effects of financial frictions, our data suggest that using indirect balance sheet measures of financial frictions might be problematic.

Table A-5 in the Appendix shows that replacing the survey measures of financial constraints with the liquidity ratio measure in the Mlogit replicates the results of Gilchrist et al. for Germany. This means that the balance sheet measure picks up more of the price increases than of the price decreases compared to the survey measure. In our model in section 3, firms that decrease prices and are financially constrained are those with an initially high price and productivity. Even though not modelled explicitly, it makes sense that these firms do not exhibit low liquidity ratios and could therefore not be picked up by the respective measures. However, these firms are financially constrained in their pricing and production decisions and therefore qualify to be counted as financially constrained.

## 3 Model

In this section, we show that the documented empirical facts can be replicated in a simple partial-equilibrium menu cost model with a working capital constraint. We document our baseline model in section 3.1 and discuss our basic intuition which follows from the static equilibrium. We then calibrate and simulate the dynamic model in section 3.2. Finally, we simulate the response of the price distribution to aggregate shocks in section 3.3.

#### 3.1 Baseline model

**Firms problem.** Our model consists of a firms' problem only. There is a continuum of firms in the economy with idiosyncratic productivity z which is exogenous and stochastic. Firms produce output y(z) using the production technology  $y(z) = z\bar{k}h(z)^{\alpha}$ . Here, h(z) is variable labor input, while  $\bar{k}$  is fixed capital input and can be thought of as a normalizing constant. Assume that demand c(z) for the good produced by firm z is given by

$$c(z) = C \left(\frac{p(z)}{P}\right)^{-\theta},\tag{2}$$

where p(z) is the nominal price for this good and  $\theta$  is the elasticity of substitution between different goods and is assumed to be constant. Aggregate consumption C and the aggregate nominal price level

<sup>&</sup>lt;sup>9</sup>The data source here is the EBDC-BEP (2012): Business Expectations Panel 1/1980 12/2012, LMU-ifo Economics and Business Data Center, Munich, doi: 10.7805/ebdc-bep-2012. This dataset links firms' balance sheets from the Bureau van Dyk (BvD) Amadeus database and the Hoppenstedt database to a subset of the firms in the ifo Business Survey. See Kleemann and Wiegand (2014) for a detailed description of this data source.

P are exogenously given. Below, we will allow the aggregate price level to follow a random walk with drift, i.e., there will be inflation in the economy.

Firms start the period with a given price p and observe the exogenous realizations of aggregate prices and idiosyncratic productivity, P and z, respectively. Before producing they choose whether to change the price to  $q \neq p$  or whether not to change the price. Given the new price and the respective output, the firms then need to hire the necessary amount of labor h at wage w. Following Nakamura and Steinsson (2008), the real wage w is assumed to be constant and equal to

$$w = \frac{W}{P} = \frac{\theta - 1}{\theta},\tag{3}$$

where W denotes the nominal wage.<sup>10</sup>

We model financial frictions via a working capital constraint, i.e., we assume that payments of wages, wh, are made prior to the realization of revenues. This implies that the firm faces a cash flow mismatch during the period and the firm has to raise funds in form of a intra-period loan. To cover the cash flow mismatch, firms raise an intra-period loan l=wh which is repaid at the end of the period. Firms cannot borrow more than their liquidation value of capital

$$wh \le \xi \bar{k},\tag{4}$$

where  $0 \le \xi \le 1$  measures the tightness of the constraint. We allow  $\xi$  to be different for different firms and to follow an exogenous stochastic process. As in Jermann and Quadrini (2012), we assume that debt contracts are not enforceable as the firm can default. Default takes place at the end of the period before the intra-period loan has to be repaid. In case of default, the lender has the right to liquidate the firm's assets. However, the loan l are liquid funds that can be easily diverted by the firm in case of default. We assume that firms can divert all the revenues so lenders cannot access the cash-flow generated by the firm. The only asset left is then physical capital  $\bar{k}$ . The tighter the constraint, the less of  $\bar{k}$  can be liquidated. Our working capital constraint can therefore be viewed as an enforcement constraint.

The second friction we add to the model is a standard menu-cost, that is, the firm has to pay a fixed cost f in case it decides to adjust its price. For simplicity, we assume that a fixed cost f has to be paid at the end of the period after revenues have been realized.

Given  $(p, P, z, \xi)$ , the firm's real profits are then given by

$$\Pi(p, P, z, \xi) = \frac{p}{P}y(z) - wh = \frac{p}{P}z\bar{k}h^{\alpha} - wh.$$
(5)

The dynamic problem of the firm, taking the current values of  $P, z, \xi$  as given, is

$$V(p, P, z, \xi) = \max\{V^{A}(p, P, z, \xi), V^{NA}(p, P, z, \xi)\}$$
(6)

where

$$V^{A}(p, P, z, \xi) = \max_{h, q \neq p} \{ \Pi(q, P, z, \xi) - f + \beta E_{P', z', \xi'} V(q, P', z', \xi') \}$$
s.t.  $z\bar{k}h^{\alpha} \le c(z) \quad wh \le \xi\bar{k}$  (7)

<sup>&</sup>lt;sup>10</sup>This expression of the real wage would arise in a general equilibrium model with linear utility and flexible prices abstracting from financial frictions.

and

$$V^{NA}(p, P, z, \xi) = \max_{h} \left\{ \Pi(p, P, z, \xi) + \beta E_{P', z', \xi'} V(p, P', z', \xi') \right\}$$
s.t.  $z\bar{k}h^{\alpha} \le c(z) \quad wh \le \xi \bar{k}$  (8)

where  $V^A$  and  $V^{NA}$  are the value functions of the firm in case it decides to adjust or not adjust the prices respectively. In case of price adjustment, the fix cost f needs to be paid. Note that through  $y(z) \leq c(z)$  we allow the firm to not satisfy the demand for goods. As we show in the static model below, the situation can arise when the financing constraint is very tight and the firm does not adjust its price. In this case, the firms rations the supply due to the financial constraint.

As noted above the model also allows for two types of disturbances: firm-specific productivity shocks and firm-specific shocks to the financial constraint. The laws of motion for these two disturbances are given by

$$\ln z_t = \rho_z \ln z_{t-1} + \varepsilon_t \tag{9}$$

$$\ln \xi_t = \mu_{\xi} + \rho_{\xi} \ln \xi_{t-1} + u_t \tag{10}$$

In addition, and in line with Nakamura and Steinsson (2008), we allow for shocks to the aggregate price level

$$log(P_t) = \bar{\pi} + log(P_{t-1}) + \eta_t, \tag{11}$$

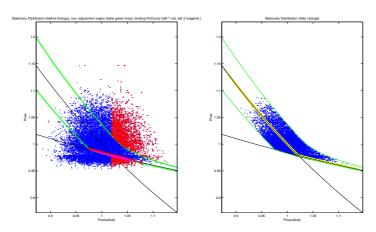
where  $\bar{\pi}$  is the average inflation rate in the economy.

**Intuition from the static model.** The most important insights from the model can already be discussed in a simpler, static version of the model. In this model, we set  $\beta = 0$  and we do not allow aggregate prices P to change.  $\xi$  is is fixed at  $\mu_{\xi}$  for all firms and there is not autocorrelation in the idiosyncratic productivity shock. The static model can be solved in closed form. 11 Figure 1 illustrates the static model for a given parametrisation (see our baseline calibration in subsection 3.2). The left hand side of the figure shows the situation before the price decision: Given P and  $\xi$ , firms start with a certain initial price p and a productivity level z. The right hand side graph shows the situation after price adjustment. The x-axis displays productivity levels z and the y-axis shows the real price of the firm  $\tilde{p} = p/P$  (or  $\tilde{q} = q/P$  if the price is changed). Each dot in this graph corresponds to a price-productivity combination that have some positive mass in the stationary distribution. Since we do not display the respective mass of firms, one should not think of each dot representing a single firm. 12 In the graph, the steeper black line exhibits the optimal relative price in an economy without financial constraints, while the flatter black line corresponds to relative price - productivity combinations at which a firm is financially constraint. One can see that the optimal price is no longer feasible for low price and high productivity firms. The yellow line in the right-hand side plot shows the optimally chosen price for each productivity level z in the presence of financial constraints. To the right of the intersection of the two black lines, it is optimal for firms to adjust prices up or down onto the financial constraint. We count

<sup>&</sup>lt;sup>11</sup> Please see Appendix A.1 for the respective equations.

 $<sup>^{12}</sup>$  Notice that a stationary distribution exists since firms still maximize the sum of expected future dividends. However, since they do not care about the future, the problem is essentially static. We can still obtain the stationary distribution by simulating the economy for a long time (or a large cross-section of firms) by starting with an initial draw of idiosyncratic productivity and using the policy function of the firm to obtain the joint stationary distribution of p, z given P and xi.

Figure 1: The static model with financial constraints



Notes: Left hand panel shows situation before pricing decision, but after realization of idiosyncratic productivity shock.

Right hand panel shows situation after price adjustment.

these firms as financially constrained. Price-productivity combinations for these firms are shown in red in the left-hand side plot.

As in the dynamic model, firms decide whether to adjust their prices or not given their initial price and productivity and given the fixed cost of adjustment. Without menu costs, firms will always adjust their price to the yellow line. One can show that when firms adjust their price, they will adjust the prices such that they always satisfy demand. Then, there are two cases: The financial constraint is binding or the financial constraint is not binding. For a given initial distribution of z and p, the number of constrained firms depends on the value of  $\xi$ . The higher  $\xi$ , the fewer firms are constrained. For a given value of  $\xi$ , firms with a high productivity z will be constrained. Out of the constrained firms, those with a low initial price sell and produce a lot and would like to increase their price. Since all firms need to finance the inputs used for production, these firms may not be able to finance output at their desired price and will be forced to increase their price by more than without financial constraints. Out of the constrained firms, those with a high initial price would like to decrease their price. However, they may not decrease their price down to the black, but only to the yellow line, i.e., they run into the financial constraint at some point. Likewise, for a given value of  $\xi$ , firms with a low productivity z will not be constrained. These firms do not produce enough such that financing the necessary inputs violates the financial constraint, regardless of wether they increase or decrease their price.

With menu costs, firms trade off the gain in revenue from changing the price and the cost of adjusting the price. If, given P, z and initial p, firms are not too far away from the optimal price and they will choose not to adjust their price. This is marked by the green region in Figure 1. Note that the graph depicts real prices  $\tilde{p} = p/P$ , but we refer to adjusting or not adjusting the nominal price p. Hence, the green region corresponds to the real prices of those price-productivity combinations for which firms do not change their nominal price p. Financial constraints shape the adjustment region of the firms. Compared to an economy without financial constraints, some firms that would not have adjusted their price previously, now have to adjust their prices (up). Some other firms that would have adjusted their prices down, now do not adjust their prices. In addition, the distribution of price and productivity of firms is different in the two economies. For a given  $\xi$ , the financial constraints will not be binding for some firms. These firms satisfy demand at their initial price. For other firms, the financial constraint is binding. Then, demand is not necessarily satisfied and the situation is called rationing. Price-productivity combinations

Table 3: Parametrization of the dynamic model

Parameter		Value	
discount factor	$\beta$	0.9966	NS(2010)
agg. consumption	C	1	NS (2010)
demand elast. of subst.	$\theta$	4	NS (2010)
fixed cost price adjust.	f	0.018	NS(2010)
average inflation	$\bar{\pi}$	0.001	Germany 1991-2014
sd price level innovations	$\sigma_{\eta}$	0.002	Germany 1991-2014
sd productivity	$\sigma_{arepsilon}$	0.067	
pers. productivity	$ ho_z$	0.66	
financial constraint	$\mu_{\xi}$	0.92	
sd fin. shock	$\sigma_{arepsilon}$	0.04	
pers. fin. shock	$\rho_{\xi}$	0.66	

for these firms are marked with magenta in the left-hand side plot of the figure.

In order to compare the output from the static (and later the dynamic) model to the empirical evidence, one then compares the fractions of financially constrained firms that adjust prices up or down relative to all financially constrained firms to the respective fractions within the unconstrained firms. Already in this static version, our model supports the empirical findings (see Table 4).

### 3.2 Quantitative results from the dynamic model

Compared to the static version, the first order conditions do change when prices are adjusted, and do not change when prices are not adjusted. When adjusting prices, firms now take into account the effect of their price change on next periods starting condition (i.e., the initial price next period) and its impact on future outcomes. Through adjusting their prices, they can also affect whether they are financially constrained or not. In the static model, it was not optimal to increase prices by more or decrease prices by less and, hence, to produce less than given by the constraint. Now, the foregone revenue this period is traded off with a possibly better initial price next period. Regardless of financial constraints, firms prefer to be located in the center of the non-adjustment region, since this decreases their chances to having to adjust their prices and paying the menu cost in the future. Hence, by setting their prices accordingly, some firms will choose not to be financially constrained and opt for a price in the center of the adjustment region. Hence, fewer firms will be financially constrained in the dynamic compared to the static model. The more productive the firms and the smaller the menu costs, the more likely are firms to be financially constrained in this setup. Figure A-5 in the Appendix illustrates this.

Table 3 shows our parametrization. In general, we stay very close to Nakamura and Steinsson (2008). In addition to the parameters in the table, this implies setting  $\bar{k}=1$  and  $\alpha=1$  in the production function. Average inflation and the standard deviation of price shocks targets German producer price developments in the manufacturing sector<sup>13</sup>. We set the standard deviation of productivity and the financial shock as well as the mean value of  $\xi$  such that we match the number of constrained firms as well as the fraction of financially constrained and unconstrained firms that do not change their price in the economy. Our baseline calibration targets the overall moments using the production shortage question from our survey.

Table 4 shows the moments in the data produced using both survey questions about financial constraints and the results from our simulation exercise. Even though not targeted, our baseline calibration

<sup>&</sup>lt;sup>13</sup>The data is provided by the German statistical office.

Table 4: Comparing moments in model and data

	FC firms	$\Delta p = 0$		$\Delta p$	< 0
		FC firms	$\operatorname{UC}$ firms	FC firms	$\operatorname{UC}$ firms
Data: 2001-2014					
Production shortage	0.05	0.75	0.80	0.12	0.08
Bank lending	0.32	0.76	0.80	0.14	0.08
Baseline model					
	0.05	0.75	0.80	0.20	0.08
Sensitivity of paramet	ers				
$\xi = 0.6$	0.32	0.70	0.86	0.13	0.03
no fin. shocks	0.05	0.84	0.80	0.13	0.08
no fin. constr.			0.79		0.10
no menu cost	0.22	0.03	0.03	0.66	0.41
Static model					
	0.10	0.34	0.82	0.64	0.04

matches the frequency of price decreases that we observe in the data relatively well. In addition to the baseline calibration, we consider how financial frictions and menu costs affect model outcomes. One can see that the fact that financially constrained firms decrease their prices more often than their unconstrained counterparts is driven by the financial constraint, not by the menu costs in the model. The reason is that the financial constraint compresses possible prices from below in the stationary distribution and it is more likely to end up above rather than below the constraint in the region where it is binding.

When tightening the financial constraint, more firms become constrained and more of these adjust their nominal price. The reason is that the financial constraint makes the adjustment region smaller in the area where it binds. Out of all firms that adjust their price, more are now financially constrained. As a consequence, the fraction of firms that are unconstrained and do not change their price increases. Overall, nominal rigidities increase when the financial constraint becomes tighter (see also Figure A-7).

When the financial constraint becomes tighter, but also due to the presence of financial shocks, unconstrained firms adjust their price up less often than constrained firms. When financial constraints vary for each firm, more firms will find themselves to be in a situation where given last periods price and current productivity, they cannot finance their production and need to adjust prices up. Hence, the fraction of financially constrained firms that increase their price increases, while the fraction of constrained firms that decrease their price is unaffected, and overall, financially constrained firms adjust price more often than financially unconstrained firms.

Table 5 shows the average price changes in the model. Financially constrained firms change their prices by less than unconstrained firms. This stems mainly from the fact that the constrained firms increase their prices by less than their unconstrained counterparts which is, again, due to the compression of the price distribution in the region where the constraint is effective. The difference between financially constrained and unconstrained firms increases without financial shocks. Comparing two economies with tight and lax financial constraints (low and high  $\mu_{\xi}$ ), prices are on average higher and price changes smaller in the economy with tight constraints. Consequently, the dispersion of prices decreases in economies with tighter financial constraints (see also Figure A-6).

Table 5: Average price changes

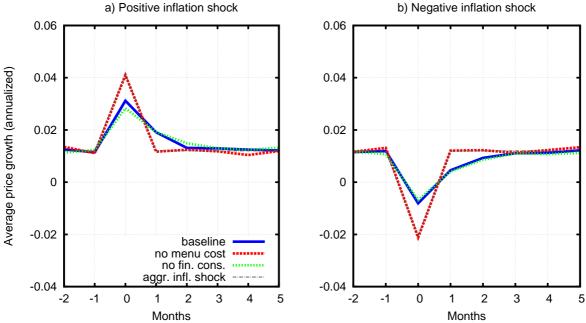
	Avg. $ \Delta p $		Avg. 4	Avg. $\Delta p > 0$		Avg. $\Delta p < 0$	
	FC firms	UC firms	FC firms	UC firms	FC firms	UC firms	
Baseline model							
	6.880	9.334	2.081	7.894	-7.986	-7.025	
Sensitivity of pe	arameters						
$\xi = 0.6$	4.295	4.449	2.510	3.692	-4.925	-2.189	
no fin. shocks	6.146	9.740	1.397	8.403	-7.437	-7.212	
no fin. constr.		11.258		9.313		-8.331	
no menu cost	3.562	5.500	1.565	5.548	-4.452	-5.427	
Static model							
	12.982	11.597	0.262	10.535	-13.231	-5.008	

### 3.3 Aggregate shocks

In this section we study the implications of aggregate inflation shocks on prices, the price dispersion and the fraction of price changes, averaged over financially constrained and unconstrained firms in the stationary distribution. In our partial equilibrium model, one can best view this exercise as the response of a single sector to an aggregate price level shock. We simulate the response of firm-specific prices to a one standard deviation shock to the aggregate price level in our baseline calibration. To study the relative contribution of nominal rigidities and financial constraints, respectively, we then report the responses for two counter-factual scenarios: one in which we shut down the nominal rigidities by setting the menu cost to zero (labeled 'no menu cost') and one in which we remove the financial constraints (labeled 'no fin. constr.'). The last scenario essentially represents the standard menu cost model. Figure 2 shows the response of the average price level to positive aggregate price level shocks in period 1 in panel (a) and to the corresponding negative shocks in panel (b). Figure 3 shows the corresponding response of nominal rigidities, i.e., the average fraction of price changes. Figures A-6 and A-7 in the Appendix further show the dispersion of prices as well as the responses of financially constrained and unconstrained firms price decisions separately.

Figure 2 documents that the model replicates the conventional business cycle pattern of average price decreases in a recession and price increases in a boom. In a model without menu costs, inflation shocks are offset one-to-one by the price changes of firms. This response is dampened when nominal rigidities are present. Comparing an economy with menu costs, but with and without financial constraints, there is hardly any difference in the response of average prices. If anything, financial constraints further dampen the response, i.e., prices are adjusted less and inflation is higher in a recession and lower in a boom compared to an economy without financial constraints. There is two offsetting effects here: First, nominal rigidities increase after a negative price shock in an economy with financial constraints (see Figure 3). Since the decreasing price level relaxes the financial constraint, the fraction of financial constraints decreases and those firms that become financially unconstrained are very likely to end up in the non-adjustment region and do not change their price. This will have a positive effect on average price growth. Those firms that have been inactive and have been shifted out of the inaction region by the price shock will now adjust their prices downward onto the financial constraint and, since the constraint lies at the lower boundary of the non-adjustment region, by more than the initial price shock. This has a

Figure 2: Average inflation response for unexpected aggregate inflation shock



negative effect on average price growth. Hence, even though average differences may be small, individual firms' price responses are very different in the two scenarios.

We further compare the responses to a negative inflation shock (normal recession) to the case in which a one-standard deviation negative financial shock hits the economy at the same time (financial recession). Figure 4 documents our various scenarios for the response of average price growth for a positive shock to the aggregate price level (panel (a)) and a corresponding negative shock (panel (b)). A financial tightening induces that firms decrease prices less in a recession and more in a boom. This result goes in the same direction as argued by Gilchrist et al. (2013a) for the Great Recession in the U.S.: tightening financial constraints in a recession counteract the deflationary pressures of a normal recession. The presence of menu costs intensifies this effect. Two things are important to note here: First, contrary to a normal recession, nominal rigidities decrease. Unlike in Gilchrist et al. this effect mainly stems from unconstrained firms increasing their prices more often. Put differently, the presence of (changing) financial constraints affects the behavior of both constrained and unconstrained firms. The latter are firms that have not adjusted their prices previously, but due to the tightening financial constraint now adjust the prices up. Since these firms are unconstrained, this means that they adjust their prices optimally such that their resulting price is higher than it would be on the constraint. Second, since prices are higher for both constrained and unconstrained firms, the corresponding output is even lower.

The depicted combination of negative aggregate price and financial shock explains the U.S. experience in the Great Recession well, albeit with a different mechanism than in Gilchrist et al. (2013a). Even though the fraction of financially constrained firms has increased in Germany, too, aggregate dynamics around 2009 have resembled a normal recession much more than a financial recession (see Figures A-1 to A-4 in the Appendix). In order to replicate the German business cycle facts, we combine the negative financial shock with a very large negative shock to the price level. In fact, producer prices have fallen dramatically in 2009, while the increase in financially constrained firms has been moderate. Figures A-8

a) Positive inflation shock b) Negative inflation shock 0.23 0.23 0.22 0.22 Fraction of price changes 0.21 0.21 0.2 0.2 0.19 0.19 baseline no fin. cons. joint shock 0.18 0.18 0 2 5 -2 -1 0 1 2 3 4 5

Figure 3: Response of frequency of price adjustment to aggregate inflation shock, all firms

Notes: This figure displays the response of frequencies of price adjustment following a one standard-deviation unexpected negative shock to aggregate inflation. Left panel: positive shock to aggregate inflation. Right panel: negative shock to aggregate inflation. Blue solid lines refer to the responses in the baseline model. Red dashed line refers to the joint shock scenario; that is, the negative shock to aggregate inflation is accompanied by an aggregate tightening of financial conditions. Green line refer to the model version where financial frictions are absent.

Months

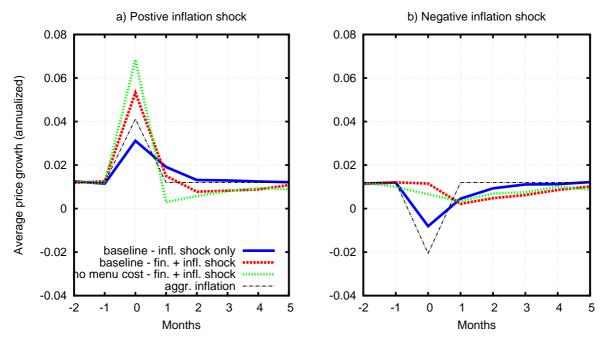
Months

and A-9 in the Appendix document the resulting dynamics and highlight that not only the presence of different shocks, but also their relative size matters for aggregate outcomes.

# 4 Conclusion

This paper investigates the interaction between financial frictions and the price setting of firms. Financial frictions and price setting may affect each other in two ways: On the one hand, being financially constrained may affect the pricing decision of a firm: firms with initially low prices that sell large quantities may not be able to finance their production inputs and may therefore find it optimal to scale down production and adjust prices up. On the other hand, firms seeking to gain market share may want to lower their prices. However, by doing so, they may run into financial constraints when expanding production. We show empirically and theoretically that both of these mechanisms are important for understanding the frequency, the direction, the size and the dispersion of individual firms' price changes.

Figure 4: Average response of firm price growth for unexpected aggregate inflation shock and contemporaneous tightening of financial conditions



Notes: This figure displays the response of firms' average price growth following a one standard-deviation unexpected shock to aggregate inflation. The left panel shows the response to a positive aggregate inflation shock. The right panel shows the responses for a negative aggregate inflation shock. In both panels it is assumed that the aggregate inflation shock comes together with an aggregate tightening of financial conditions, that is, a decrease in  $\xi$  for all firms.

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# A Appendix

#### A.1 The static model

#### A.1.1 Problem of the firm

Here for simplicity we assume that the aggregate price level P is normalized to one. Note that this implies so the firm's nominal price p is also its real price. In addition, we normalize the aggregate consumption level C=1. For the production function, we normalize  $\bar{k}=1$  and assume a constant return to scale technology, i.e.  $\alpha=1$ . To save on notation, denote by  $s=(z,\xi)$  the idiosyncratic state of the firm. The problem of the firm can then be written as

$$V(p,s) = \max\{V^A(p,s), V^{NA}(p,s)\}\$$

where

$$V^{A}(p,s) = \max_{h,q \neq p} \left\{ zh\left(q - \frac{w}{z}\right) - f \right\}$$

subject to

$$zh \le q^{-\theta} \tag{\phi}$$

$$wh \le \xi \tag{\mu}$$

and

$$V^{NA}(p,s) = \max_{h} zh\left(p - \frac{w}{z}\right)$$

subject to

$$zh \le p^{-\theta} \tag{\phi}$$

$$wh \le \xi \tag{\mu}$$

### A.1.2 No price adjustment.

Conditional on not adjusting the price, the firm chooses hours to maximize profits. The first order conditions read as

$$0 = \left(p - \frac{w}{z}\right) - \phi - \frac{w}{z}\mu$$
 
$$zh \le p^{-\theta} \quad \perp \quad \phi \ge 0$$
 
$$wh \le \xi \quad \perp \quad \mu \ge 0$$

for pz > w. Otherwise h = y = 0. Now, consider the following cases

1. Demand satisfied while the financial constraint is not binding. Complementary slackness requires

 $\mu = 0$ . From the demand equation we have

$$h = \frac{1}{z}p^{-\theta}$$
$$\phi = \left(p - \frac{w}{z}\right)$$

Note that in this case it has to be true that

$$z > \frac{w}{\xi} p^{-\theta}$$

which is satisfied for sufficiently high values of  $\xi$ , given p; or for given  $\xi$  for sufficiently high prices p.

2. Demand is (weakly) not satisfied while the financial constraint is binding. Then we have

$$h = \frac{\xi}{w}$$
$$\mu = \frac{z}{w} \left( p - \frac{w}{z} \right)$$

Note that in this case it has to be true that

$$z \le \frac{w}{\xi} p^{-\theta}$$

## A.1.3 Price adjustment

First order conditions for prices, hours, and output

$$\begin{split} 0 &= zh - \phi\theta q^{-\theta-1} \\ 0 &= \left(q - \frac{w}{z}\right) - \phi - \frac{w}{z}\mu \\ zh &\leq q^{-\theta} \perp \phi \geq 0 \\ wh &\leq \xi \perp \mu \geq 0 \end{split}$$

Consider the following cases

1. Financial constraint is not binding and demand is satisfied. This implies that  $\mu = 0$  and

$$h = \frac{1}{z}q^{-\theta}$$
$$0 = zh - \phi\theta q^{-\theta - 1}$$
$$\phi = \left(q - \frac{w}{z}\right)$$

so that

$$0 = 1 - \theta \left( q - \frac{w}{z} \right) q^{-1}$$

18

or

$$q = \frac{\theta}{\theta - 1} \frac{w}{z}$$

which is the standard result that price is a constant mark-up  $\theta/(\theta-1)$  over marginal costs w/z. For this case to arise, it must be the case that the parameter  $\xi$  that measures financial tightness is sufficiently large or

$$\xi > \left(\frac{\theta - 1}{\theta}\right)^{\theta} \left(\frac{w}{z}\right)^{1 - \theta}.$$

2. Both constraints are binding. Then

$$h = \frac{\xi}{w}$$

$$q = (zh)^{-\frac{1}{\theta}}$$

$$\phi = \frac{1}{\theta}zhq^{1+\theta}$$

$$\mu = \frac{z}{w}\left(\left(q - \frac{w}{z}\right) - \phi\right)$$

or

$$q = \xi^{-\frac{1}{\theta}} \left(\frac{w}{z}\right)^{\frac{1}{\theta}}$$

$$\phi = \frac{1}{\theta} \left(\frac{w}{z\xi}\right)^{\frac{1}{\theta}}$$

$$\mu = \frac{\theta - 1}{\theta} \left(\frac{w}{z\xi}\right)^{\frac{1}{\theta}} \frac{z}{w} - 1$$

For this case, it must be true that  $\phi, \mu \geq 0$ . Note that  $\phi > 0$  is always satisfied. For  $\mu \geq 0$ , it must be the case that

$$1 \le \frac{\theta - 1}{\theta} \left( \frac{w}{z\xi} \right)^{\frac{1}{\theta}} \frac{z}{w}$$

or

$$\xi \le \left(\frac{\theta - 1}{\theta}\right)^{\theta} \frac{w}{z\xi} \left(\frac{z}{w}\right)^{\theta}$$

3. The financial constraint is binding and the demand function is slack. In this case by hypothesis

 $\phi = 0$  and

$$h = \frac{\xi}{w}$$

$$0 = zh$$

$$0 = \left(q - \frac{w}{z}\right) - \frac{w}{z}\mu$$

Unless  $\frac{\xi}{w} = 0$  the optimality conditions lead to a contradiction, assuming that productivity is always positive z > 0. We exclude this case by assuming that  $w, \xi > 0$ .

#### A.1.4 Summary.

The previous discussion can be summarized as follows. In case the firm finds it optimal to adjust its price, it will always satisfy demand. When the working capital constraint is slack, this is the standard case and the prices is a constant mark-up over marginal costs. This scenario arises when the firm has access to sufficient funds to pay the hired workers, that is, given z for a sufficiently high  $\xi$  or - given  $\xi$  - for a sufficiently low z. On the other hand, if the working capital constraint is binding the firm can hire less workers, so output is lower. The firm then finds it optimal to increase the price further so that demand at this price is equal output that can be produced given the financial constraint. This situation arises, for given  $\xi$ , if the firm is very productive (large z) or - given z - faces tight financial conditions (low  $\xi$ ).

In case the firm finds it optimal not to adjust its price, there are two possible scenarios. In case the working capital constraint is slack, the firm hires labor so to produce the amount that satisfies demand at that price. On the other hand, if the constraint is binding, the firm cannot hire more labor than is prescribed by the constraint; in this case, the firm will not be able to satisfy demand.

The price adjustment decision is then made anticipating the possible scenarios as discussed above. Note that absent menu-costs the firm always finds it optimal to adjust the price.

# A.2 Additional Tables and Figures

Table A-1: Descriptive Statistics: Baseline sample

*		•
	unconstrained	constrained
Constrained status (1)		
Number of observations	47,788	$22,\!992$
Fraction of observations	0.68	0.32
$Firm\ size\ (employees)\ (2)$		
Average	542.2	572.9
Median	120.0	110.0
Small ( $\leq 50$ )	0.26	0.28
$SME \in 50,250$	0.44	0.41
$Medium \in 250, 500$	0.15	0.14
Large $(> 500)$	0.15	0.16
- ' '		

Notes: Sources: ifo Business Survey; (1) based on bank lending survey question, (2) Number of persons employed by the reporting firm/enterprise

Table A-2: Balance sheet information

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	${\it unconstrained}$	constrained
Total assets (1)	10,579,276	10,081,000
$Bank\ lending$		
Liquidity ratio (2)	0.061	0.034
Cash flow ratio (3)	0.055	0.010
Interest coverage ratio (4)	0.008	0.012
$Production\ shortage$		
Liquidity ratio $(2)$	0.046	0.017
Cash flow ratio (3)	0.044	0.000
Interest coverage ratio (4)	0.009	0.018

Sources: EBDC-BEP (2012): Business Expectations Panel 1980:1 to 2012:12; (1) total assets (end of year); (2) cash and cash equivalents over total assets (both end of year); (3) operating profit (end of year) over total assets (beginning of year); (4) interest expenses over sales (both end of year)

Table A-3: Correlations between different measures of financial constraints

Variables	Production	Restrictive	Liquidity	Cash flow
	$_{ m shortage}$	bank lending	$\operatorname{ratio}$	$\operatorname{ratio}$
Restrictive bank	0.262	1.000		
lending	(0.000)			
9	, ,			
Liquidity ratio	-0.065	-0.070	1.000	
1 0	(0.000)	(0.000)		
	(0.000)	(0.000)		
Cash flow ratio	-0.028	-0.041	-0.002	1.000
	(0.079)	(0.009)	(0.883)	1.000
	(0.010)	(0.003)	(0.000)	
Interest coverage	-0.013	-0.030	-0.036	0.251
ratio	(0.410)	(0.052)	(0.022)	(0.000)
1 at 10	(0.410)	(0.002)	(0.022)	(0.000)

Sources: ifo Business Survey and EBDC-BEP (2012)

Table A-4: Overlap between different measures of financial constraints

Production shortage:	${\it unconstrained}$	constrained
$Restrictive\ bank\ lending$		
Constrained (fraction)	0.281	0.827
Unconstrained (fraction)	0.719	0.173
$Fraction\ constrained$		
Liquidity ratio	0.490	0.671
Cash flow ratio	0.489	0.746
Interest coverage ratio	0.491	0.723
$Fraction \ unconstrained$		
Liquidity ratio	0.510	0.329
Cash flow ratio	0.511	0.254
Interest coverage ratio	0.509	0.277

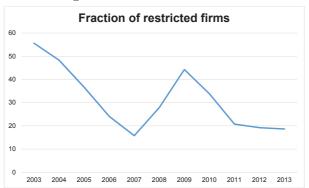
Sources: ifo Business Survey and EBDC-BEP (2012)

Table A-5: Financial Constraints and Price Setting: Within Firm Effects for Liquidity Ratios

	Liquidity ratio						
price	variable	no fixed effects	time fixed effects	sector fixed effects	time & sector fixed effects		
<b>+</b>	FC	-0.0449 (0.0278)	-0.0525* (0.0283)	0.00987 (0.0297)	-0.00503 (0.0303)		
<b>↑</b>	FC	0.140*** (0.0230)	0.172*** (0.0234)	0.0888*** (0.0244)	0.113*** (0.0249)		

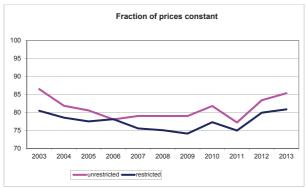
Notes: MLOGIT estimation: Base outcome is prices unchanged. Sample: January 2002 - December 2013. Standard errors in parentheses: \*\*\* p < 0.01, \*\* p < 0.05, \* p < 0.1. Includes only observations for which balance sheet data are available. Yearly data (interpolated).

Figure A-1: Fraction of restricted firms over time



Notes: Fraction of firms answering "restrictive" to bank lending survey question in all firms in a given month.

Figure A-2: Fraction of prices constant over time



Notes: Fraction of firms not changing prices within restricted and unrestricted firms using the bank lending survey question.

Figure A-3: Fraction of price increases over time

25
20
15
10
2003 2004 2005 2006 2007 2008 2009 2010 2011 2012 2013

—restricted firms —unrestricted firms

Fraction of price increases

Notes: Fraction of firms increasing prices within restricted and unrestricted firms using the bank lending survey question.

Figure A-4: Fraction of price decreases over time



Notes: Fraction of firms decreasing prices within restricted and unrestricted firms using the bank lending survey question.

Figure A-5: The dynamic model with financial constraints

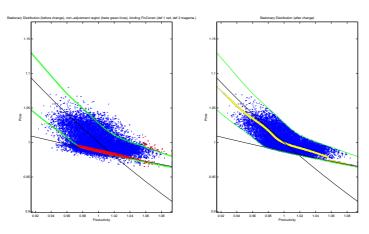
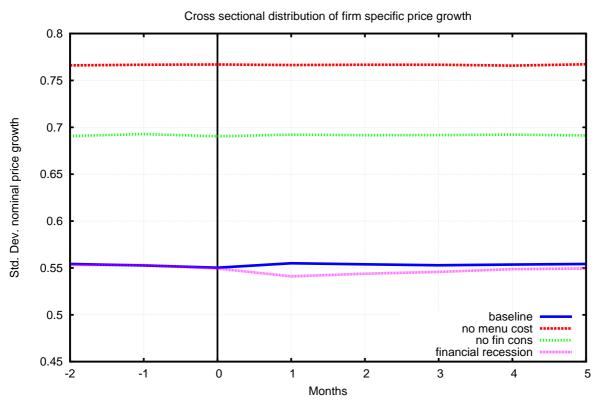
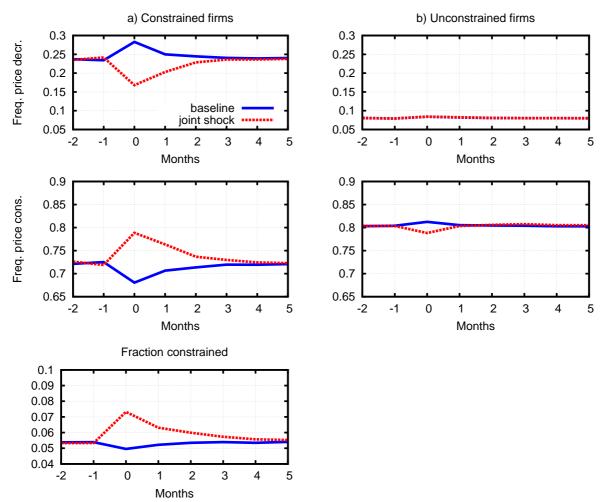


Figure A-6: Response to negative inflation shock: cross sectional distribution of firm specific inflation



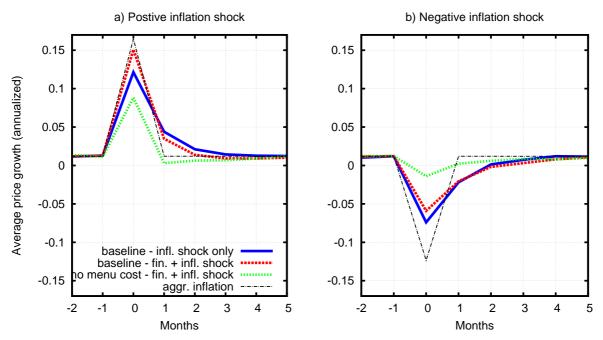
Notes: This figure displays the response of the cross sectional distribution of firm-specific inflation growth rates (annualized) following a one standard-deviation unexpected negative shock to aggregate inflation for different model specifications.

Figure A-7: Response of frequencies to a negative aggregate inflation shock



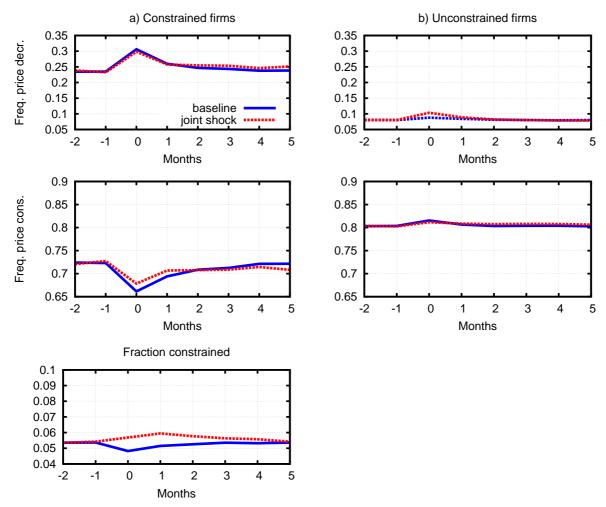
Notes: This figure displays the response of frequencies of price adjustment following a one standard-deviation unexpected negative shock to aggregate inflation. Left panel: financially constrained firms. Right panel: financially unconstrained firms. Blue solid lines refer to the responses in the baseline model. Red dashed line refers to the joint shock scenario; that is, the negative shock to aggregate inflation is accompanied by an aggregate tightening of financial conditions.

Figure A-8: Average response of firm price growth for large aggregate inflation shock and contemporaneous tightening of financial conditions



Notes: This figure displays the response of firms' average price growth following an unexpected shock to aggregate inflation of -15%. The left panel shows the response to a positive aggregate inflation shock. The right panel shows the responses for a negative aggregate inflation shock. In both panels it is assumed that the aggregate inflation shock comes together with an aggregate tightening of financial conditions, that is, a decrease in  $\xi$  for all firms.

Figure A-9: Response of frequencies to a large negative aggregate inflation shock



Notes: This figure displays the response of frequencies of price adjustment following an unexpected negative shock to aggregate inflation of -15%. Left panel: financially constrained firms. Right panel: financially unconstrained firms. Blue solid lines refer to the responses in the baseline model. Red dashed line refers to the joint shock scenario; that is, the negative shock to aggregate inflation is accompanied by an aggregate tightening of financial conditions.