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Decomposition of country-specific corporate bond spreads

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Non-technical summary

Research Question

In the financial crisis corporate bond spreads widened strongly especially for firms from euro-area periphery countries. A decomposition of the spreads into the expected loss, bond risk premium and liquidity premium can provide information that is relevant for assessing financing conditions from a monetary policy and financial stability view.

Contribution

This paper presents a new approach, based on the Merton model, to decomposing corporate bond spreads. We show how the bond risk premium can be represented in the Merton model depending on the hedge ratio (the sensitivity of debt to equity) and the equity risk premium. In the empirical section, we estimate the hedge ratios in a time-varying way via the volatilities on the equity and bond market and calculate the equity risk premiums. We focus on country-specific financing conditions of German, French, Spanish and Italian firms and also analyse its determinants.

Results

The results show that the bond risk premium accounts for a much larger share of the spreads than either the expected loss component or the liquidity premium. While the expected loss component made the greatest contribution to the strong widening of the spreads in the crisis period around the turn of 2008/09 (indicating that investors were distinctly worried about unfavourable fundamentals at the time), the spreads were then heavily dominated by the bond risk premium and investors received relatively low or, at times, no compensation for expected losses. This points to a relatively high valuation on the corporate bond markets. The results on the magnitude of the individual spread components also reveal a certain degree of heterogeneity between the countries considered. For instance, the bond risk premium for France and the liquidity premium for Spain account for a particularly large share of the spreads. The heterogeneity between the countries considered is also due to differences in sovereign CDS premiums which, together with the safe interest rate, are key determinants for the expected loss component and the bond risk premium.

Nichttechnische Zusammenfassung

Fragestellung

In der Finanzkrise haben sich die Renditeaufschläge auf EWU-Unternehmensanleihen vor allem in den Peripherieländern deutlich ausgeweitet. Eine Zerlegung der Renditeaufschläge in die Bestandteile erwartete Kreditausfallverluste, Bondrisikoprämie und Liquiditätsprämie kann Informationen liefern, die für die Beurteilung der Finanzierungsbedingungen aus geldpolitischer und finanzstabilitätspolitischer Sicht wichtig sind.

Beitrag

Das Papier stellt einen neuen, auf dem Merton-Modell basierenden Ansatz zur Zerlegung von Renditeaufschlägen auf Unternehmensanleihen vor. Wir zeigen, wie sich die Bondrisikoprämie in Abhängigkeit von der Hedge Ratio – der Sensitivität des Fremdkapitalwerts gegenüber dem Eigenkapitalwert – und der Aktienrisikoprämie darstellen lässt. Im empirischen Teil ermitteln wir zeitvariable Hedge Ratios über die Volatilitäten am Aktien- und Bondmarkt und berechnen die Aktienrisikoprämien. Die Untersuchung bezieht sich auf landesspezifische Finanzierungsbedingungen deutscher, französischer, spanischer und italienischer Unternehmen und analysiert auch wichtige Determinanten.

Ergebnisse

Die Ergebnisse zeigen, dass die Bondrisikoprämie einen merklich größeren Anteil der Spreads erklärt als die Expected-loss-Komponente oder die Liquiditätsprämie. Die Expected-loss-Komponente hat zwar zur kräftigen Ausweitung der Spreads in der Krisenphase um den Jahreswechsel 2008/2009 den größten Beitrag geleistet, was auf damals ausgeprägte Sorgen der Anleger vor ungünstigen Fundamentaldaten hindeutet. Anschließend wurden die Spreads aber stark von der Bondrisikoprämie dominiert, und die Anleger erhielten für erwartete Verluste eine relativ geringe oder sogar überhaupt keine Kompensation. Dies deutet auf eine relativ hohe Bewertung an den Corporate Bond-Märkten hin. Die Ergebnisse zu den Erklärungsbeiträgen der einzelnen Komponenten weisen außerdem auf eine gewisse Heterogenität zwischen den Ländern hin. Beispielsweise leistet die Bondrisikoprämie für Frankreich und die Liquiditätsprämie für Spanien einen besonders hohen Beitrag zu den Spreads. Zu der Heterogenität zwischen den Ländern haben auch unterschiedliche staatliche CDS-Prämien beigetragen, die zusammen mit dem sicheren Zins wichtige Bestimmungsgrößen der Expected-loss-Komponente und der Bondrisikoprämie sind.

Decomposition of country-specific corporate bond spreads¹

Niko Dötz

Abstract

This paper presents a new approach, based on the Merton model, to decomposing corporate bond spreads into the expected loss, bond risk premium and liquidity premium components. The approach focuses on establishing the bond risk premium using the equity risk premium and the hedge ratio, which are estimated using a dividend discount model and a BEKK-GARCH model. The analysis focuses on non-financial European BBB-rated corporate bonds and distinguishes explicitly between German, French, Spanish and Italian firms. The results show that the bond risk premium is the largest component. While the expected loss component made the greatest contribution to the strong widening of the spreads around the turn of 2008/09, the spreads were then heavily dominated by the bond risk premium and investors received relatively low or, at times, no compensation for expected losses. The safe interest rate and the sovereign CDS premiums are key determinants of the expected loss component and the bond risk premium.

Keywords: Structural models, credit spreads, risk premiums

JEL classification: G12, G15

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1. Introduction

Bond spreads for firms from euro-area periphery countries, which had been broadly similar to those for German companies before the financial crisis, widened strongly around the turn of 2008/09 and between autumn 2011 and the middle of 2012. As the financial markets grew calmer, however, yield spreads tightened again noticeably and the differences between countries also narrowed once more (see Figure 1). Nonetheless, the at times significant heterogeneity of corporate financing conditions has fuelled the debate on how far the monetary policy transmission process in the euro area and especially in the periphery countries has been impaired. The low levels of yield spreads at the end of 2013 increasingly raised the question of how indicators of setback potential can be identified in this market.

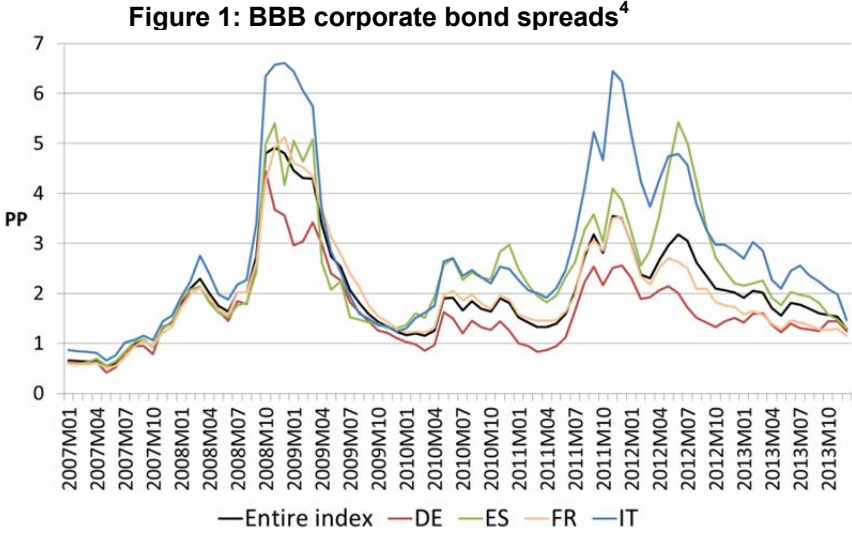
Against this background, a (country-specific) decomposition of the spreads can provide important information. To assess the effectiveness of monetary policy transmission, it is important to discover, for example, whether broader spreads mainly reflect higher expected default losses as a result of a gloomy economic outlook or rather heightened uncertainty, a reduced appetite for risk or an increased preference for liquidity by market participants. A breakdown of this kind helps to establish how far changes in the yield spreads are based on the real economy or how far they are attributable to changes in volatilities or market participants' preferences. First, this is important for assessing monetary policy reactions aimed at improving corporate financing conditions. Second, decomposing spreads gives a more accurate idea of how permanent the observed changes in financing costs are and what impact they have on financial market stability, firms' investment activity and aggregate demand.²

This study presents a new approach to decomposing corporate bond spreads into the expected loss, bond risk premium and liquidity premium components. The approach focuses on establishing the bond risk premium using the equity risk premium and the hedge ratio, which is derived from the Merton model.³ In comparison to existing studies on structural credit risk models, the methodology is relatively simple and the advantage is that there is no need to use variables which are difficult to quantify, such as the value of the firm's assets. Most existing studies on structural credit risk models do not include the equity risk premium (Huang/Huang 2012) even though the dividend discount models provide an established method for calculating this premium. The inclusion of the equity risk premium is also supported by empirical evidence that the stock markets incorporate new information quickly and efficiently. Unlike earlier studies, which concentrate mainly on US firms, this analysis focuses on non-financial European corporate bonds (BBB rated) and makes an explicit distinction

² For example, Gilchrist/Zakrajšek (2012) emphasise that the bond risk premium can provide important information about economic activity.

³ The hedge ratio is the sensitivity of debt to equity. It indicates how many shares need to be purchased for a replicating portfolio in order to replicate a corporate bond.

between German, French, Spanish and Italian firms. Using the calculated yield spread components, the second stage of the study analyses the extent to which the country-specific yield spread components are affected by the economic outlook in the euro area and the perceived creditworthiness of the firms' countries of origin (measured by CDS spreads).



2. Survey of the literature

Structural credit risk models based on the Merton (1974) model play a major role in the analysis and decomposition of yield spreads. Numerous empirical studies focus on the determinants of yield spreads (eg Collin-Dufresne/Goldstein/Martin, 2001, Eom/Helwege/Huang, 2004, Huang/Huang 2012). These studies show that, based on realistic assumptions, both the simple Merton model and various model extensions can only partially explain corporate bond spreads. Compared with theoretical credit risk model based spreads empirical spreads are too high – what is sometimes called the credit spread puzzle. Attempts to explain this discrepancy focus mainly on non-credit-risk components of the spreads, eg liquidity premiums or differences between corporate bonds and government bonds in terms of taxation or regulation – which are not captured by the Merton model.

An important group of empirical studies on the decomposition of yield spreads use data provided by rating agencies on the probability of default and the recovery rate to determine expected default losses and differentiate them from the other yield spread components (Elton/Gruber/Agrawal/Mann 2001, Amato/Remolona 2003). GARCH-in-mean models represent a different type of approach (Kounitis 2007, Flavin/Limosani 2007, Dötz/Fischer 2010). These models do not require data from rating agencies, but instead assume that appropriate fun-

⁴ Yield spreads over German Federal bonds of equivalent maturity. Based on non-financial firms in the broad Merrill Lynch BBB corporate bond index for which share price information is available. Excluding bonds for which the price is below 85% of the par amount.

damental determinants can be specified for the expected default losses and that the risk premium can be adequately explained using the estimated conditional variance of the residuals.

Non-credit-risk components are not the only factor to be taken into account when decomposing yield spreads. A further challenge is to break down the credit risk components into the element that represents compensation for expected losses (the expected loss component) and into the bond risk premium, which reflects the uncertainty associated with the expected loss component and also depends on investors' risk aversion. Although the Merton model can be resolved into the yield spread (see Annex 7.1), because the model is based on the no-arbitrage principle and is independent of risk preferences, the model-based theoretical yield spread reflects the total compensation for the credit risk, ie the sum of the expected loss component and the bond risk premium. Additional information about the market participants' risk preferences is therefore needed in order to determine the individual components. The present approach uses the equity risk premium for this purpose as it reflects market participants' risk preferences. The equity risk premium, together with the hedge ratio derived from the simple Merton model, forms the basis for calculating the bond risk premium.

In a similar paper, Churm/Panigirtzoglou (2005) use an extension of the Merton model by Leland and Toft (1996) to decompose US and UK corporate bond spreads during the observation period from 1997 to 2003. To determine the growth path of the value of the firm, they use the equity risk premium derived from a dividend discount model, meaning that the information on market participants' risk preferences contained in the equity risk premium is indirectly taken into account.⁵ They also use the implied equity volatility to calculate the volatility of total assets. On this basis, they isolate the bond risk premium from the expected loss component by comparing the risk-neutral and "real-world" probability density functions. In line with the present approach, Churm/Panigirtzoglou arrive at the conclusion that the expected loss component is closely correlated with the spread and that both variables rise considerably during times of crisis. As in the present approach, they also find that the bond risk premium is mostly higher than the expected loss component. However, in a departure from the present approach, they always calculate the expected loss component to be positive and their results reveal that the non-credit risk factors play a more significant role.

One key reason as to why the non-credit risk components account for a relatively high share of the spreads in Churm/Panigirtzoglou's approach is likely to lie in their calculation as a residual. Churm/Panigirtzoglou underline that these components contain not only a liquidity premium but also tax effects or differences in regulation between corporate and government bonds. The way in which the expected loss component is calculated in the two approaches also differs considerably. In Churm/Panigirtzoglou's approach, the expected loss component is the compensation required by risk-neutral investors for credit risk and is thus always posi-

⁵ In the model used by Leland/Toft (1996), the growth path of the assets is dependent on the firm's capital costs. The capital costs consist of the default-free interest rate and the asset risk premium, which, in turn, is a weighted (with the leverage ratio) average of the yield spread and the equity risk premium.

tive. Its value depends chiefly on the implied equity volatility. In the present approach, the expected loss component is calculated as a residual by removing the bond and liquidity premiums from the spread. The consequence of such an approach is, first, that it is more straightforward to calculate and that no data on implied equity volatility are required. Second, the expected loss component can take on a negative value when bond risk and liquidity premiums are relatively high. Negative values imply that investors receive practically no compensation for expected losses.

Two related papers (Chen/Guo/Zhang 2006, Campello/Chen/Zhang 2008) also focus on the link between the risk premium, the bond risk premium and the hedge ratio, but with the opposite objective: to calculate the equity risk premium from the bond risk premium. These studies are also similar to the rating-based approaches to decomposing the yield spreads because they base their calculations of the bond risk premium on probabilities of default provided by Moody's. Finally, our investigation is motivated by the results of a study by Schaefer/Strebulaev (2008), in particular, which concludes that even the hedge ratio derived from the simple Merton model largely corresponds to the empirical hedge ratio. This evidence provides an important argument in favour of using the hedge ratio derived from the classic Merton model to measuring the credit risk of corporate bonds.⁶ The use of the hedge ratio implies that the Merton model is not used to calculate the absolute value of equity or debt but to estimate how a one percent increase in the firm's value is reflected by percentage changes in the equity or debt value. As Schaefer/Strebulaev demonstrate, in this case, the "noise" created by the non-credit risk components plays a minor role although, as the credit puzzle shows, non-credit risk factors may reflect a significant portion of the yield spread.

While Chen/Guo/Zhang (2006), Campello/Chen/Zhang (2008) and Schaefer/Strebulaev (2008) calculate the empirical hedge ratios using a regression analysis of equity returns and bond yields, Bao/Pan (2012) base their calculations on the volatility of both markets. They interpret their evidence that the observed volatility on the credit market (ie on the bond and CDS market) is higher than the theoretical values derived from the Merton model ('excess volatility') primarily as the reflection of time-varying liquidity premiums on the credit markets. Their results, which are largely consistent with those of Schaefer/Strebulaev, provide an additional motivation for this analysis. First, they suggest that the hedge ratio derived from the Merton model may provide valuable insights into the relationship between equity and bond market prices. Second, they imply that the model-based volatilities can provide important information about this relationship if time-varying liquidity premiums are taken into account.

Section 3 of this paper shows how the bond risk premium is dependent on the hedge ratio and the equity risk premium in the Merton model. In order to calculate the empirical bond risk premiums, section 4 explains how the equity and bond volatilities and the equity risk premium are calculated for the observed firms and presents the underlying data. Section 5 anal-

⁶ Che/Kapadia (2012) demonstrate that the theoretical and empirical hedge ratios for equities and credit default swaps also largely correspond to one another, but emphasise the limited effectiveness of this type of hedging.

yses the relationship of the individual yield spread components with macro variables and sovereign CDS spreads, and section 6 concludes.

3. The Merton model

3.1. *Basic idea of the model*⁷

The basic idea of the Merton model is that investment in a corporate bond can be replicated by investment in a riskless bond and the sale of a put option (short put) on the firm with the nominal value of the corporate bond as the strike price. The short put position reflects the firm's credit risk, because if the value of the firm is lower than the nominal value of the corporate bond when the corporate bond matures (insolvency), the put option is exercised. In this case, the distressed firm is transferred to the seller of the put for the price of the nominal liabilities. As a result his losses, like a bondholder, amount to the difference between the nominal bond value and the recoverable amount. According to the model, the yield spread on a corporate bond therefore reflects the value of the put option and is determined by the same factors (see Annex 7.1). As the following sections show, the bond risk premium can also be determined from this model.

3.2. *Calculating the bond risk premium*

In Merton's credit risk model, the growth in the value of the firm (V) follows a geometric Brownian movement with drift:

$$1) \frac{dV}{V} = \mu dt + \sigma_V dW,$$

where μ is trend growth (drift), σ_V is the volatility of the corporate asset returns and W is a standard Wiener process. The value of the firm (V) consists of equity (E) and debt in the form of a zero-coupon bond (D):

$$2) V = E + D$$

Both equity and debt are only affected by changes in the value of the firm:

$$3) \frac{\partial E}{\partial V} + \frac{\partial D}{\partial V} = 1$$

⁷ Annex 7.1 presents the Merton model in more detail and shows how the equation for the yield spread is derived.

The value of equity and debt are assumed to be a function of firm value and time. Ito's Lemma produces the following representation of the volatility of equity and debt returns (σ_E, σ_D):⁸

$$4a) \sigma_E = \frac{V}{E} \frac{\partial E}{\partial V} \sigma_V \quad \text{and} \quad 4b) \sigma_D = \frac{V}{D} \frac{\partial D}{\partial V} \sigma_V$$

It follows from this that the relationship between σ_D and σ_E is equal to the sensitivity of debt to equity. Following Schaefer/Strebulaev (2008), this sensitivity is defined as hedge ratio δ below:

$$5) \frac{\sigma_D}{\sigma_E} = \frac{\partial D / \partial V}{\partial E / \partial V} \frac{E}{D} = \frac{\partial D}{\partial E} \frac{E}{D} = \delta$$

The hedge ratio is based on the concept that a corporate bond can be modelled using a replicating portfolio consisting of riskless bonds and equities. It indicates how many stocks need to be purchased in order to replicate a corporate bond. Campello/Chen/Zhang (2008) show that, based on the assumptions of the simple Merton model, the equity risk premium (ERP) is a linear function of the bond risk premium (BRP), with the inverse of the hedge ratio as the scaling factor:

$$6) ERP = \frac{\partial E}{\partial D} \frac{D}{E} BRP$$

The underlying intuition is that both equities and corporate bonds are contingent claims written on the corporate assets and therefore depend on a common systematic risk factor. The relationship between the risk premiums corresponds to the hedge ratio. For the BRP, following from 5) and 6),

$$7) BRP = ERP \frac{\sigma_D}{\sigma_E} .$$

3.3. Implications for decomposing the corporate bond spread

When decomposing the spread, it must be considered that the Merton model is based on highly simplified assumptions. The yield spread is assumed to reflect only the credit risk, with non-credit risk factors being omitted. Furthermore, the modelling of equity and debt is very simple as it assumes that they are dependent on solely one factor: firm value.⁹ There is no doubt that these simplifications impair the suitability of the Merton model for determining eq-

⁸ According to Ito's Lemma, the change in the function of an underlying and of time (ie in the price of a derivative) also follows an Ito process if the price of the underlying follows an Ito process. Under the assumptions of the Merton model, this means that the processes of the equity and debt value have different drift terms and Wiener process parameters to the process of the assets, but depend on the same random variable dW.

⁹ Extensions of the simple model include, for example, stochastic interest rates, an endogenously derived default, a dynamic capital structure or a jump in the firm value process; see, for example, Huang/Huang (2012).

uity and debt. However, as demonstrated by Schaefer/Strebulaev (2008), such restrictions are not as severe for determining the sensitivity of equity to debt. Thus, a crucial factor for the empirical meaningfulness of the theoretical hedge ratio is likely to be the extent to which participants in the equity and bond markets value risk in the same way – which the model assumes they do. If the two markets were fully integrated, this would always be the case. However, as market integration is more likely to be incomplete and to vary over time,¹⁰ the following empirical results should be interpreted with more caution. In particular, equation 7 should be assumed to be true on average over a longer period of time – in line with Schaefer/Strebulaev (2008) – rather than at any given time. Notwithstanding this caveat, the decomposition of spreads can aid in evaluating the valuation level of bond markets.

Calculating the empirical bond risk premium using the simple relationship in equation 7 has a number of benefits. The calculations do not require any information about determinants of the put options (which are partly difficult to measure), about historical default rates or about (intransparent) valuations by rating agencies.¹¹ The volatilities of the equity and debt returns, σ_E and σ_D , can be determined at any given time on the basis of market prices. Including equity markets in the calculation also acknowledges empirical evidence that the stock markets incorporate new information relatively quickly and efficiently (Forte/Peña 2009). Lastly, dividend discount models, which are based on regular updates of analysts' estimates of corporate earnings, are a widely established approach to establishing the equity risk premium.¹²

4. Decomposition of yield spreads

4.1. Methodology

Overview

The first step in decomposing yield spreads is to identify the bond risk premium. Then, in a second step, a simple linear regression is used to calculate the liquidity premium and finally, as a residual, the expected loss component.

Enterprises in the entire bond index

To establish the bond risk premium for the enterprises included in the entire index, the volatilities σ_D and σ_E must first be calculated. Following Schaefer/Strebulaev (2008), to do this we calculate the aggregate excess return on the bonds, weighted according to their nominal val-

¹⁰ For instance, the degree of market integration is likely to depend chiefly on the extent to which investors and firms are restricted by regulations: those governing investment decisions of the former and financing decisions of the latter; see Titman (2002).

¹¹ The value and the volatility of a firm's assets or the value of a firm's liabilities are deemed to be difficult to measure if neither the assets nor the liabilities are traded on the markets.

¹² The analysts' estimates used here are I/B/E/S estimates (Institutional Brokers Estimate System).

ue.¹³ The excess returns on the corresponding shares are also weighted according to the nominal value of the bonds. The excess returns on the bonds and shares are the logarithmic price differentials minus the yield on three-month Bubills (the latter converted into monthly values).¹⁴ Then, the volatilities of the aggregate share and bond excess returns are estimated using a diagonal bivariate BEKK-GARCH model.¹⁵ The application of a BEKK model implies that, as well as the time-varying variances, the time-varying covariance between the bond and share excess returns is also estimated.

The corresponding equity risk premium is calculated in two steps. First, the equity risk premium for the broad Euro Stoxx index is established using a three-stage dividend discount model.¹⁶ Then, a simple CAPM is estimated for the shares covered by the bond index. To do this, the aggregate excess returns on the shares are regressed on a constant and the excess returns for the Euro Stoxx. The equity risk premium for the enterprises in the bond index is then equal to the product of the beta factor and the Euro Stoxx equity risk premium.

To take account of the empirical indications of a “credit spread puzzle”, the present analysis factors in investors’ liquidity preferences. We use the bid/ask spreads on the bonds to measure liquidity risk below; the Annex (7.4) sets out an alternative measure in the form of the yield spread on bonds issued by the government-guaranteed *Kreditanstalt für Wiederaufbau* (KfW). To calculate the aggregate liquidity premium at index level, the aggregate yield spreads are first regressed on a constant and the aggregate bid/ask spreads for the bonds.¹⁷ The liquidity premium is then calculated as the product of the corresponding regression coefficients and the bid/ask spreads. Finally, the aggregate expected loss component is established, as a residual, as the discrepancy between the yield spread and the bond and liquidity premium.

Country-specific sub-indices

For the country-specific analysis, bond sub-indices weighted according to the nominal value of the corporate bonds are created for the individual countries under consideration (DE, ES, FR, IT). Apart from the calculation of the bond and equity volatilities σ_D and σ_E the country-

¹³ Following Brooks (2008), the excess returns for the selected bonds and shares are established against three-month Bubill returns. In calculating the excess returns, and thus the bond volatility σ_D , the fact that the bond prices also include liquidity premiums is initially abstracted out. The Annex (7.3) investigates how the use of liquidity-adjusted bond prices affects the estimated bond volatility σ_D and the bond risk premium. On average, the bond risk premium for the country-specific sub-indices calculated using the liquidity-adjusted bond prices is 25 bps above the unadjusted bond risk premium.

¹⁴ The share prices used include dividend payments (total return prices).

¹⁵ In the literature, multivariate GARCH models such as the BEKK model play an important role in calculating the optimal hedge ratio between spot paper and futures; see Brooks (2008). In the general BEKK model, the variance-covariance matrix H_t is $H_t = C + A[\varepsilon_{t-1} \varepsilon'_{t-1}]A' + B H_{t-1} B'$. In a diagonal BEKK model, the elements of the coefficient matrices A and B not lying on the diagonal are equal to zero. For a detailed explanation of the BEKK model, see Engle/Kroner (1995).

¹⁶ For details of the three-stage dividend discount model, see Deutsche Bundesbank, Monthly Report, March 2003, p 35.

¹⁷ To account for autocorrelation, we include two lags of the spread. Since there are no bid/ask spreads available for a small number of bonds, the weighting of the individual bonds is adjusted accordingly when calculating the aggregate bid/ask spreads.

specific bond risk premiums, liquidity premiums and expected loss components are identified in the same way as for the entire bond index. For the country-specific bond and equity volatilities, two market-specific diagonal BEKK models are estimated, ie a four-country model each for the bond and equity market. This approach is based on the consideration that the individual variances can best be estimated not on a country-specific basis but in combination with the market-specific covariances between the individual countries.

4.2. Data sources

The central data source on which the present analysis is based is the Merrill Lynch corporate bond index for euro-denominated, BBB-rated bonds issued by non-financial corporations. The sample covers all bonds of enterprises for which share price data are available. To prevent extreme price movements that are attributable to impending insolvency or restructuring from distorting the sample, the sample includes only bonds for which the price is at least 85% of the par amount. Overall, in the period under observation – January 2006 to December 2013 (monthly data) – this involves 724 bonds issued by 163 enterprises from 14 countries with an average effective duration of around 4½ years. Germany accounts for 146 bonds (43 enterprises), Spain 92 bonds (16 enterprises), France 291 bonds (59 enterprises) and Italy 110 bonds (23 enterprises). The data on nominal value, price, yield and effective duration are supplied by Merrill Lynch; the bid/ask spreads for the bonds and the share prices are obtained from Bloomberg. The bond yield spreads are calculated against the five-year yield on German government bonds.

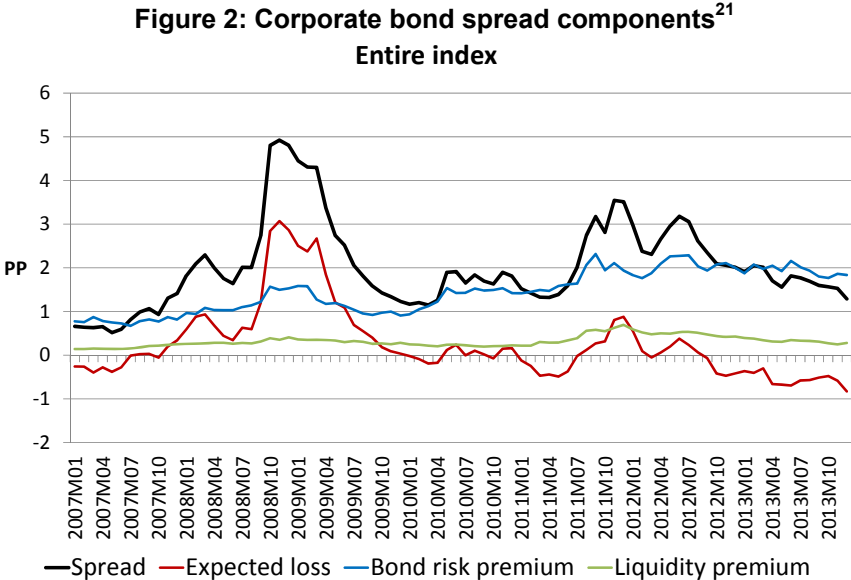
4.3. Results

Enterprises in the entire bond index

The estimated hedge ratio for enterprises in the entire bond index is between 0.22 and 0.33 in the period under observation.¹⁸ The corresponding equity risk premium is between 2.8% and 9.8% (Tables 1, 2 and Figure 1A in the Annex, section 7.2). The estimation of the liquidity premium reveals, that the bid/ask spreads have a significant positive influence on the yield spreads, as expected. Decomposing the spreads shows that the bond risk premium as a whole accounts for a much larger share of the spreads than the expected loss component or the liquidity premium. While the expected loss component made the greatest contribution to the strong widening of the spreads in the crisis period around the turn of 2008/09 (indicating that investors were distinctly worried about unfavourable fundamentals at the time), the spreads were then heavily dominated by the bond risk premium, and the expected loss component was, at times, negative due to the fact that it is calculated as a residual. Such values

¹⁸ The BEKK model is also used to estimate the time-varying conditional covariance between the monthly excess returns on bonds and equity. It is between -1.4 BP and 2.5 BP.

imply that investors are receiving practically no compensation for expected losses. On average in the period under observation, the bond risk premium accounted for the largest share of the spread (68%), followed by the expected loss component (17%) and the liquidity premium (15%) (Figure 2).¹⁹ The liquidity premium comes out somewhat higher if the KfW spread is used as an alternative measure of liquidity risk (Annex, section 7.4). The finding that the bond risk premium as a whole dominates the expected loss component is in line with earlier studies (Amato/Remolona 2003, Churm/Panigirtzoglou 2005). One major factor behind the fact that the bond risk premium accounts for such a large share of spreads is that credit risk is generally very difficult to diversify.²⁰ In contrast to the crisis period around the turn of 2008/09, the rise in yield spreads at the end of 2011 was primarily driven by the bond risk premium (and to a lesser extent, the liquidity premium), whereas the expected loss component initially remained at a relatively low level. Against a backdrop of falling spreads, the values of the expected loss component (which were actually negative between mid-2012 and end-2013) indicate that bond market valuations were again relatively high.



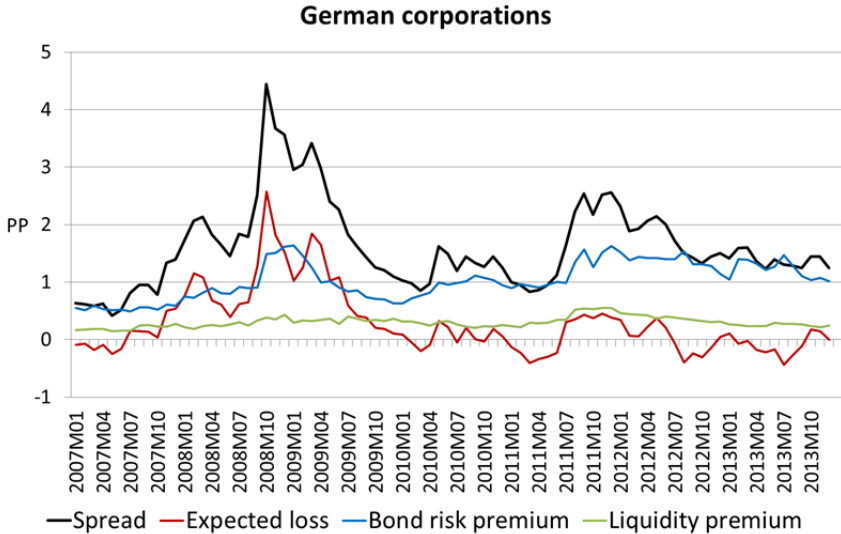
Country-specific yield spread components

The estimated hedge ratios for the country-specific sub-indices have average values similar to those for the entire index but, with the exception of France, a wider range of fluctuation. The country-specific equity risk premiums range between 2.4% and 12.9% in the period under observation (Tables 1, 2 and Figure 1A in the Annex, section 7.2). As for the entire bond index, the estimation of country-specific liquidity premiums also shows that all bid/ask spreads under consideration exert a significant positive influence on the relevant yield

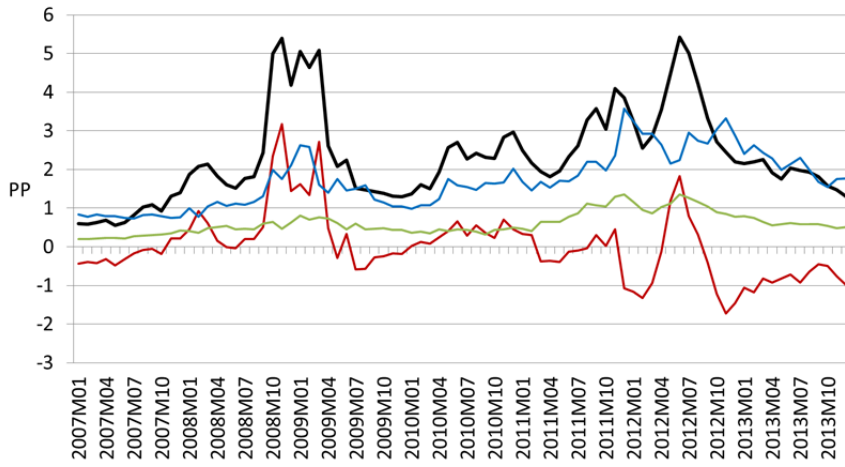
¹⁹ Here and in the country-specific analysis below, negative values of the expected loss component were taken to be zero.
²⁰ Amato/Remolona (2003) emphasise that the distribution of returns on corporate bonds is highly negative skewed. Such skewness would require an extraordinarily large portfolio to achieve full diversification.
²¹ Owing to its calculation as a residual, the expected loss component may assume negative values when bond risk premiums and liquidity premiums are relatively high. Such values indicate that investors are receiving practically no compensation for expected losses.

(66%, 63% and 62% respectively; see Figure 3). The strong widening of the spreads around the turn of 2008/09 in all four countries considered was mainly driven by the expected loss component. This is likely to reflect the fact that no country under consideration was immune to investors' worries about economic woes across Europe. However, as is also shown by the results for the entire index, in all countries considered the spreads were then heavily dominated by the bond risk premium. At the same time, the compensation required by investors for expected losses was at a low level and, at the beginning of 2012 in particular, was often negative, implying that investors received practically no compensation for expected losses. The high bond risk premiums, or rather the low compensation for expected losses, mainly reflect the different ways in which the equity risk premiums and spreads have been developing. As the financial markets began to calm following the insolvency of Lehman Brothers, the spreads initially narrowed by more than the equity risk premiums. Later on, too, the former remained relatively low or recorded only a moderate rise, whereas the latter started to increase notably again from as early as end-2009 and, since 2011, have even overshoot the level recorded in autumn 2008 (Figure 1A in the Annex, section 7.2). The relatively high bond risk premiums of French firms and the low – or, at times, even negative – compensation for expected losses reflect that the differing developments of the equity risk premiums and the bond spreads are particularly pronounced for France. The expected loss component plays a minor role for Spanish firms, which carry high bond risk premiums and a relatively high liquidity premium (amounting to 1.4 PP at its peak). Overall, at the end of the period under observation, compensation for expected losses is very low for all countries considered. In view of the generally negative correlation between expected losses and the euro-area economic outlook (section 5.1), an outlook which was, however, still quite modest at the end of 2013, this points to relatively high valuations on the relevant bond markets at that time.

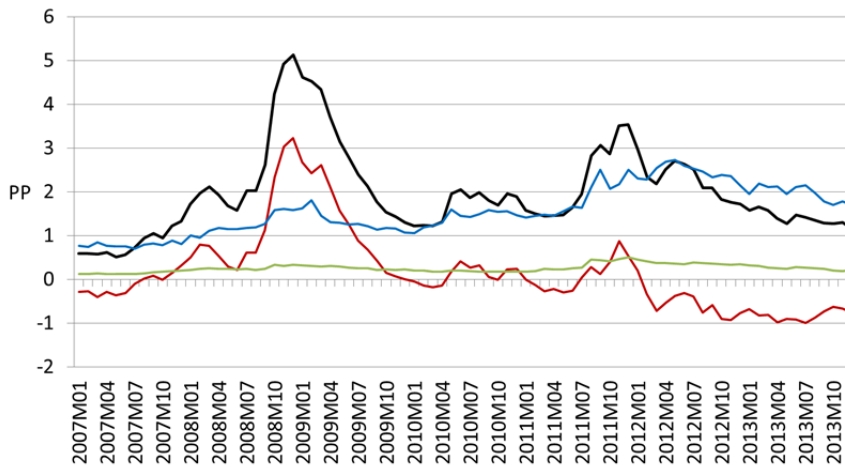
Figure 3: Country-specific yield spread components



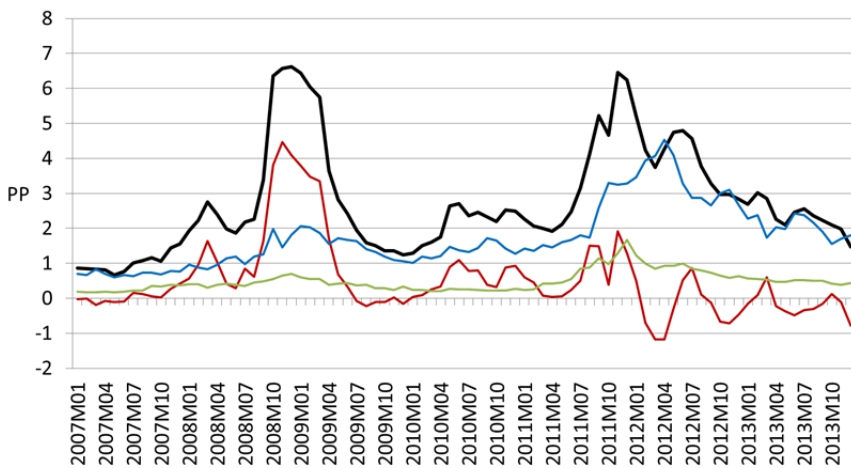
Spanish corporations



French corporations



Italian corporations



— Spread — Expected loss — Bond risk premium — Liquidity premium

5. Relationship between the yield spread components and macro variables as well as sovereign CDS premiums

Clearly, a suitable evaluation of financing conditions on the corporate bond markets needs to include an assessment of the specific yield spread components in relation to the macroeconomic environment. To measure the market participants' expectations for the economy we use the euro-area purchasing managers' index (PMI) for the manufacturing sector, a widely used leading indicator of economic activity. The yield on ten-year Bunds is used as a measure of the safe interest rate. The analysis also includes sovereign CDS premiums (duration: 5 years; source: Markit). This considers recent literature which shows that a worsening in government financing conditions has a negative impact on domestic enterprises, through rating downgrades (Almeida/Cunha/Ferreira/Restrepo 2014) or through higher CDS spreads (Bedendo/Colla 2013).

This section shows the relationship between these variables and the expected loss component as well as the bond risk premium using a simple vector autoregressive model (VAR).²² Granger causality tests based on the VAR models indicate that yields on Bunds have a major impact on the expected default losses, whereas the sovereign CDS premiums appear to influence the bond risk premiums (Tables 3 and 4 in the Annex, section 7.5). The Granger causality tests do not provide robust results for the PMI.

Impulse response sequences can be used to demonstrate the dynamics of the impact of the variables considered on the expected loss component and the bond risk premium (Figure 4).²³ As expected, the economic expectations (measured by the PMI) and sovereign CDS premiums both have a significant impact on the expected loss component. Both effects are more pronounced for Spain and Italy than for Germany and France. This suggests that Spanish and Italian firms' earnings and probability of insolvency are more dependent on the euro-area economy than is the case for German and French firms. Furthermore, the fact that Spanish and Italian firms are particularly sensitive to sovereign CDS premiums could reflect market participants' expectations, for instance, that a sovereign downgrade will have a detrimental effect on firms in the future. Examples of such a detrimental effect are higher taxes, increased government consolidation efforts and a weakened economy. Overall, the results indicate that the perceived improvement in government creditworthiness, as demonstrated by lower sovereign CDS premiums, played a major role in the decline in the expected default losses since mid-2012.

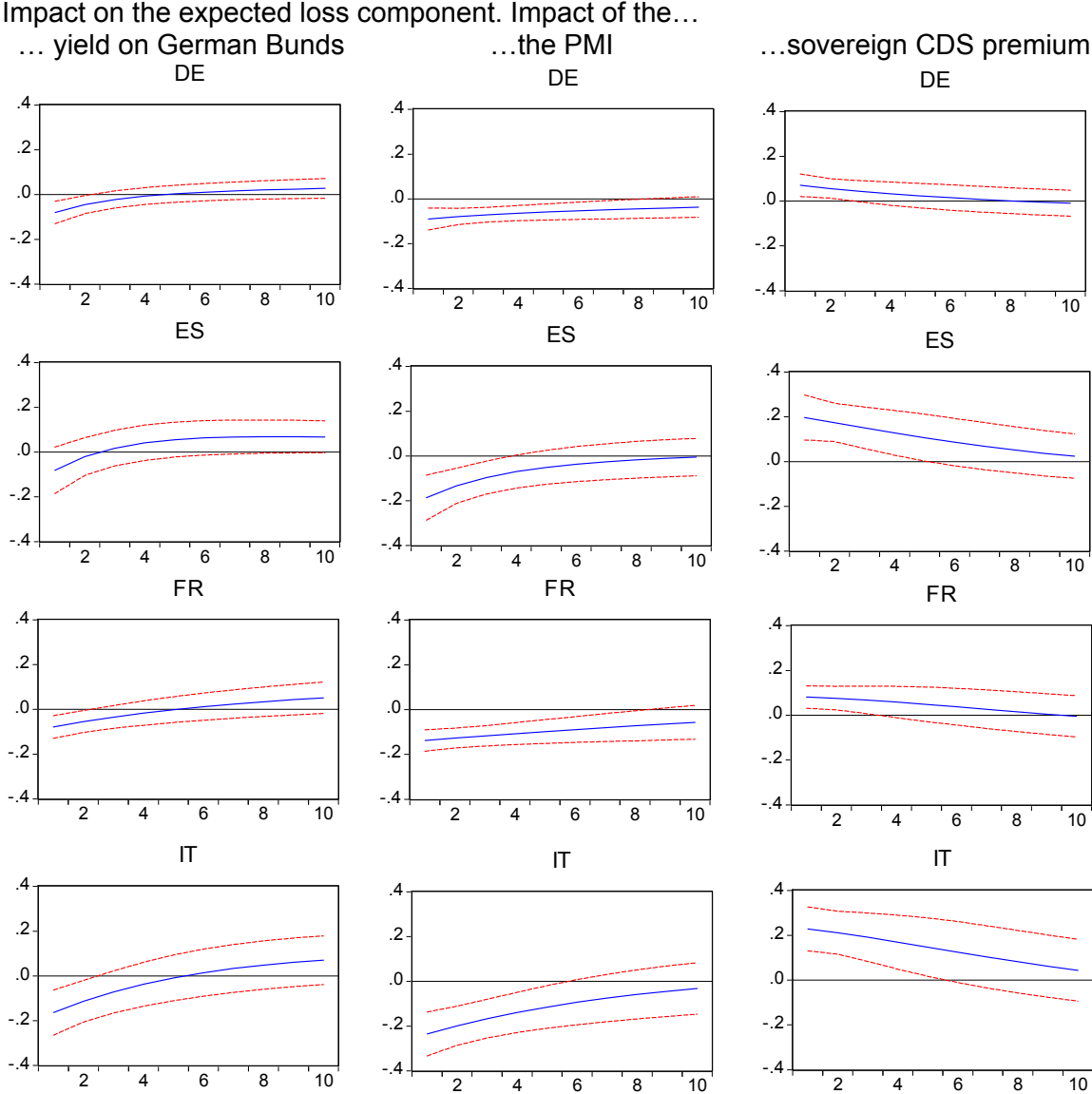
Furthermore, a fall in the safe interest rate (measured by the yield on Bunds) initially results in higher expected default losses. This negative effect is significant for Germany, France and Italy. The negative effect is in line with the Merton model, where a lower safe interest rate implies a flatter growth path for corporate assets and thus a higher probability of default. However, as shown in Figure 4, this effect is only short-lived. This may indicate that lower in-

²² Following the information criteria of Schwarz and Hannan-Quinn, the VAR models are estimated with one lag.

²³ We use generalised impulse responses as described by Pesaran/Shin (1998).

terest rates stimulate investment and economic growth over the longer term, which would, in turn, contain expected default losses. Relevant cointegration analyses (Morris/Neal/Rolph 1998) point to the existence of such differences between the short and long-term effects of changes in safe interest rates.

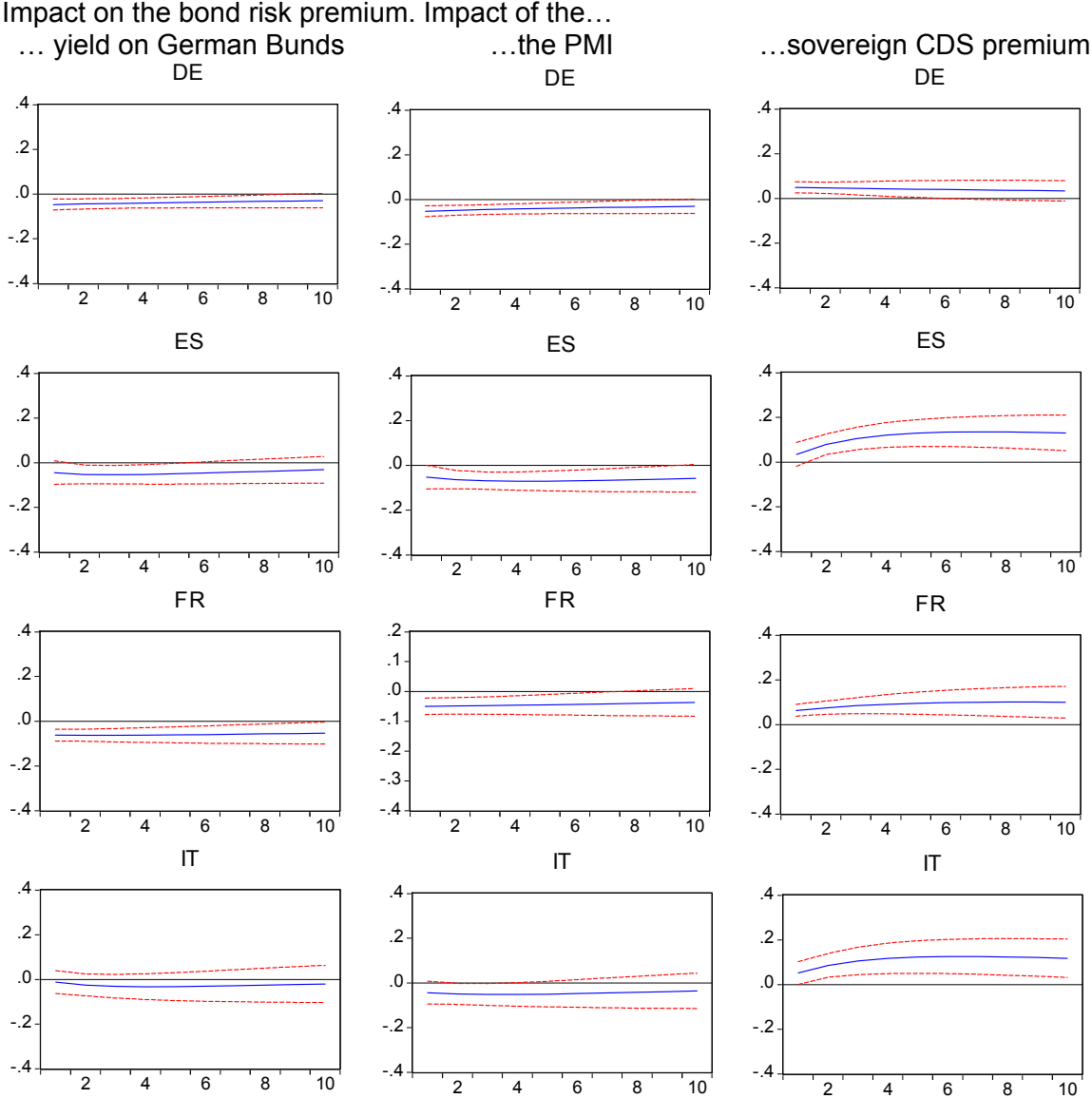
Figure 4: Impulse response sequence for the expected loss component



With respect to the explanation of the bond risk premium the impulse response sequences suggest that sovereign CDS premiums are a major determinant for bond risk premiums but that the PMI and safe interest rate are less so (Figure 5). The sovereign CDS premiums have a significant positive effect on the bond risk premium for all countries considered. Furthermore, this effect is of relatively long duration. As with the expected loss component, the effect of the sovereign CDS premiums is particularly pronounced for Spanish and Italian firms. This indicates that the conditions on the CDS market are also to some degree reflected in the uncertainty and risk aversion of players on the corporate bond markets. It also lends support to the interpretation that, if a government’s credit rating is downgraded, this results in not just

a detrimental effect on firms but also heightened uncertainty which, in turn, causes financing costs to rise. This uncertainty probably reflects the fact that many of the potential detrimental effects, such as the potential effect on firms of a government intensifying its consolidation policy, are extremely difficult to gauge.

Figure 5: Impulse response sequence for the bond risk premium



6. Conclusion

The present paper has set forth a new approach, based on the Merton model, to decomposing yield spreads on corporate bonds into the expected loss, bond risk premium and liquidity premium components. The approach focuses on establishing the bond risk premium, which, in the Merton model, depends on the hedge ratio and the equity risk premium. To calculate

the empirical bond risk premiums, the hedge ratios are estimated in a time-varying way via the volatilities on the equity and bond markets using BEKK-GARCH models, while the equity risk premiums are calculated through a three-stage dividend discount model. The empirical bond risk premiums then form the basis for decomposing yield spreads. Using the broad Merrill Lynch BBB corporate bond index as the central source of data, we focus on non-financial European corporations, with the analysis distinguishing explicitly between enterprises based in Germany, France, Spain and Italy. We also investigate how the expected loss component and the bond risk premium are affected by the economic outlook in the euro area, the safe interest rate and sovereign CDS-markets.

The results show that the bond risk premium accounts for a markedly larger share of the spreads than either the expected loss component or the liquidity premium. While the expected loss component made the greatest contribution to the strong widening of the spreads in the crisis period around the turn of 2008/09 (indicating that investors were distinctly worried about unfavourable fundamentals at the time), the spreads were then heavily dominated by the bond risk premium and investors received relatively low or, at times, no compensation for expected losses. This points to relatively high valuations on the corporate bond markets. The results on the magnitude of the individual spread components also reveal a certain degree of heterogeneity between the countries considered. For instance, the bond risk premium for France and the liquidity premium for Spain account for a particular large share of the spreads. The heterogeneity between the countries considered is also due to differences in sovereign CDS premiums which, together with the safe interest rate, are important determinants of the expected loss component and the bond risk premium.

7. Annex

7.1. Yield spread in the Merton model

In Merton's credit risk model, an enterprise is considered to be in default if its market value (V) falls below the nominal value of the liabilities (L) at the time that the bond matures (time T). Its assets are then transferred to the creditors. Upon maturity, the value of the zero-coupon bond (D_T) is thus

$$2) D_T = \min(L, V_T).$$

This cash flow corresponds to the difference between the payment of a safe bond and a European put option on the enterprise with the nominal value of the liabilities (L) as the strike price. The corporate bond can thus be interpreted as a bundle comprising a safe bond and the sale of a put option (short put position).

The price of the zero-coupon bond at the time of issue (D) is

$$3) D = Le^{-yT} = Le^{-rT} - P,$$

where y is the yield, r the safe interest rate and P the value of the put option.

The yield spread s is calculated as

$$4) s = y - r = -\frac{\ln(D/L)}{T} - r.$$

The value of the put option P is determined using the Black-Scholes formula

$$5) P = Le^{-rT}N(-d_2) - VN(-d_1)$$

with

$$d_1 = \frac{\ln(V/L) + (r + 0,5\sigma_V^2)T}{\sigma_V\sqrt{T}}$$

and

$$d_2 = d_1 - \sigma_V\sqrt{T},$$

where $N(.)$ is the cumulative density of the standard normal distribution and σ_V is the volatility of corporate asset returns. By substituting equation 5) in equation 3) and then in equation 4), the yield spread can be determined as follows

$$6) \quad s = -\frac{1}{T} \ln(e^{-rT} N(d_2) + \frac{V}{L} N(-d_1)) - r.$$

Equation 6) shows that the yield spread depends on the maturity date of the bond (T), the safe interest rate (r), the volatility of corporate asset returns (σ_V) and the leverage ratio (L / V).

7.2 Hedge ratios, equity risk premiums and corporate bond spreads

Table 1: Descriptive statistics for the estimated hedge ratio (δ)

The hedge ratio is the estimated volatility of the excess return on debt capital divided by the estimated volatility of the excess return on equity capital: $\delta = \sigma_D / \sigma_E$

| Hedge ratio for the ... | entire index | country-specific sub-index | | | |
|-------------------------|--------------|----------------------------|-------|-------|-------|
| | | DE | ES | FR | IT |
| Mean | 0.243 | 0.204 | 0.296 | 0.193 | 0.250 |
| Maximum | 0.333 | 0.272 | 0.485 | 0.253 | 0.509 |
| Minimum | 0.215 | 0.167 | 0.205 | 0.167 | 0.162 |
| Standard deviation | 0.021 | 0.024 | 0.056 | 0.018 | 0.071 |

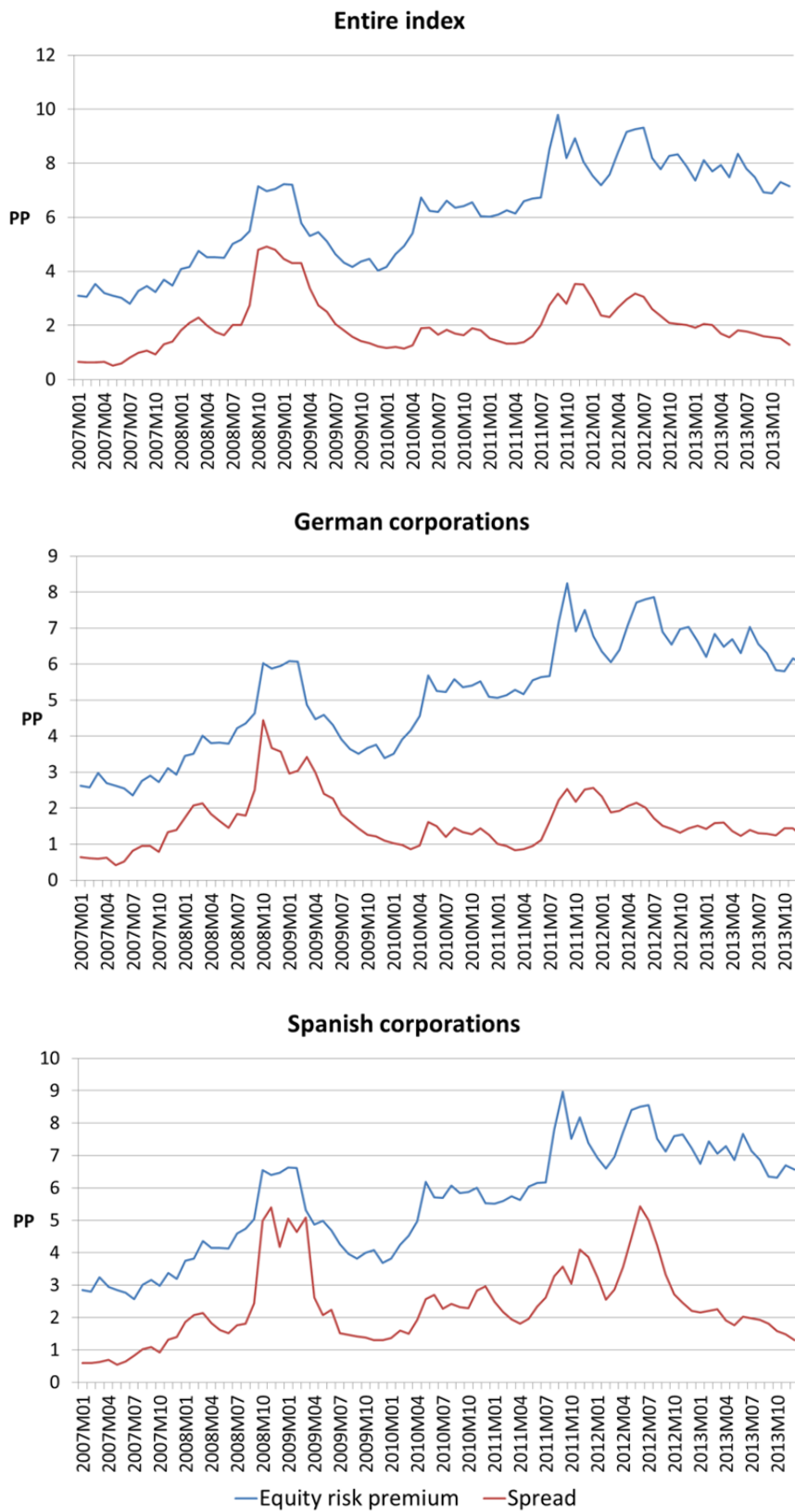
The estimated volatilities are based on diagonal BEKK models with the variance-covariance matrix $H_t = C + A[\varepsilon_{t-1} \varepsilon'_{t-1}]A' + B H_{t-1} B'$. The elements of the coefficient matrices A and B that are not on the diagonal are equal to zero.

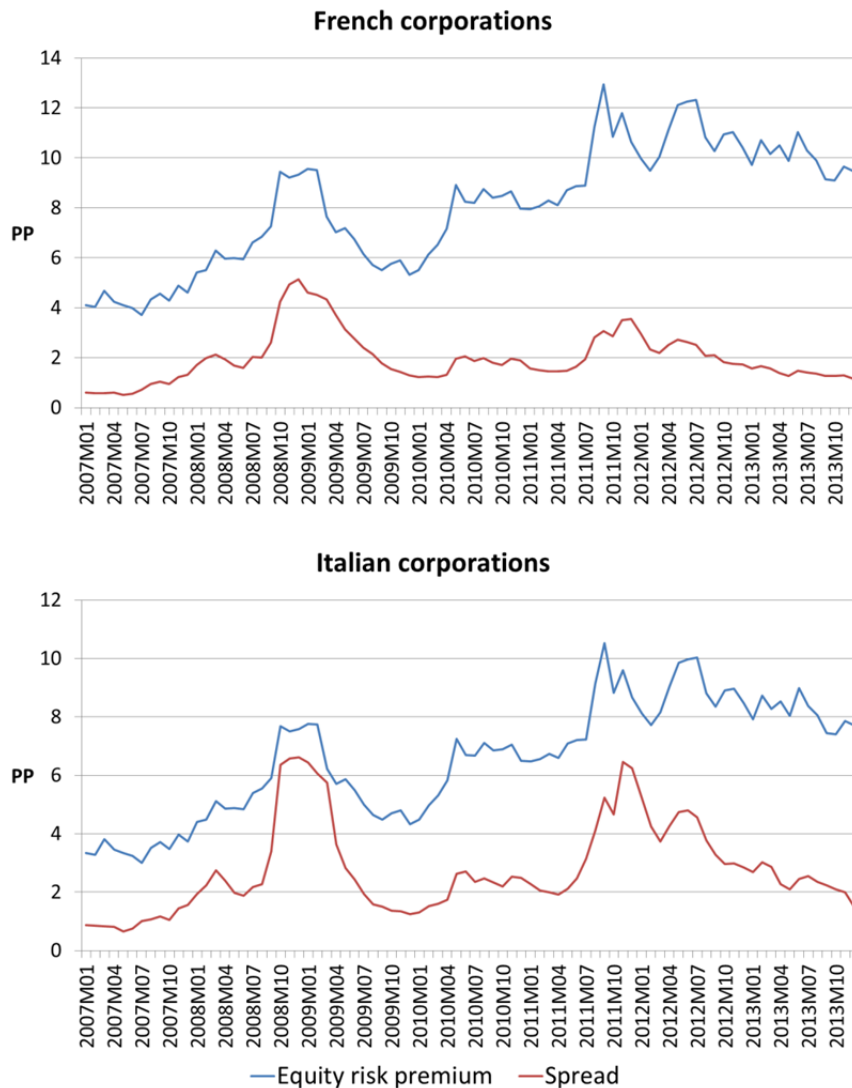
Table 2: Descriptive statistics for the estimated equity risk premium

| Equity risk premium for the... | entire index | country-specific sub-index | | | |
|--------------------------------|--------------|----------------------------|-------|-------|-------|
| | | DE | ES | FR | IT |
| Mean | 0.058 | 0.049 | 0.053 | 0.077 | 0.062 |
| Maximum | 0.098 | 0.082 | 0.090 | 0.129 | 0.105 |
| Minimum | 0.028 | 0.024 | 0.026 | 0.037 | 0.030 |
| Standard deviation | 0.019 | 0.016 | 0.017 | 0.025 | 0.020 |

The estimated equity risk premiums are based on the three-stage dividend discount model for Euro Stoxx and CAPM models for each index.

Figure 1A: Equity premium and corporate bond spread





7.3 Estimation of liquidity-adjusted bond volatilities

Although the liquidity premium does not go a long way to explaining the yield spread, when calculating the bond risk premium by computing the ratio of equity volatility to bond volatility, we have to pay attention to the fact that the bond volatility σ_D – and thus also the bond risk premium – could be notably distorted by the time-varying liquidity premiums contained in the bond prices.

The relationship between volatility on the bond market and liquidity risk has been examined from various angles in the literature. Bao/Pan (2012) cite time-varying liquidity premiums as a possible reason for their findings that the empirical bond market volatility of enterprises in the USA is higher than the volatility derived using the Merton model. This indicates that the bond risk premium calculated using the empirical bond market volatility may be biased upwards. Other studies underline the positive correlation between the volatility of bond yields and various liquidity proxies, indicating that it may be difficult to distinguish between the bond risk premium and the liquidity premium (Bao/Pan/Wang, 2011; Dick-Nielsen/Feldhütter/Lando,

2012; Friewald/Jankowitsch/Subrahmanyam, 2012). There are also indications that the liquidity proxies used may – at least partially – capture credit risk (Grass/Ward, 2012).

To evaluate the potential effect of time-varying liquidity premiums on the estimated bond volatility σ_D and the bond risk premium, the bond volatilities are then additionally estimated on the basis of liquidity-adjusted excess returns. The returns are adjusted as follows. The excess returns on bonds are first regressed on the corresponding bid-ask spread (measured in differences). The bid-ask spread is then multiplied by its coefficients and deducted from the excess returns on bonds. On average, the bond risk premium for the country-specific sub-indices calculated using the liquidity-adjusted bond prices is 25 bps above the unadjusted bond risk premium. Due to the residual calculation of the expected loss component, this component falls by the same amount.

7.4 KfW spread as an alternative proxy for liquidity risk

In addition to the bond-specific bid-ask spread and based on earlier studies, the yield differential between ten-year bonds issued by the government-guaranteed *Kreditanstalt für Wiederaufbau* (KfW) and long-term German Federal bonds (KfW spread) is used as a general proxy for market participants' liquidity preferences (see Longstaff (2004) for a study for the USA). As with calculations of the liquidity premium based on the bid-ask spread, the country-specific aggregated yield spreads are initially regressed on a constant and the KfW spread. The liquidity premium is then calculated as the product of the corresponding regression coefficient and the KfW spread.

As expected, the KfW spread has a significant positive effect for all country-specific yield spreads. The country-specific liquidity premiums predominantly demonstrate a similar pattern to the liquidity premiums calculated on the basis of the bid-ask spread, but were generally at a somewhat higher level. On average, they were around 5 bps higher for the four countries analysed and over the entire period of observation. Due to the residual calculation of the expected loss component, this component falls by the same amount.

7.5 Granger causality tests

Table 3: Impact on the expected loss component

| Country | Yield on Bunds $H_0 : \delta^1 = 0$ | PMI $H_0 : \delta^2 = 0$ | Sovereign CDS $H_0 : \delta^3 = 0$ |
|---------|--|-----------------------------|---------------------------------------|
| DE | *** | ** | - |
| ES | ** | - | - |
| FR | ** | - | - |
| IT | * | - | - |

The Granger causality tests are based on the following equation of the one-lag VAR model:

$$ELOSS_{country,t} = c_1 + \beta ELOSS_{country,t-1} + \delta^1 YIELD_{DE,t-1} + \delta^2 PMI_{t-1} + \delta^3 CDS_{country,t-1} + \varepsilon_t$$

where $ELOSS$, $YIELD_{DE}$, PMI and CDS stand for the expected loss component, the yield on ten-year German Bunds, the PMI and the sovereign CDS premium.

***, ** and * represent a rejection of H_0 at a significance level of 1%, 5% and 10%, respectively.

Table 4: Impact on the bond risk premium

| Country | Yield on Bunds $H_0 : \delta^1 = 0$ | PMI $H_0 : \delta^2 = 0$ | Sovereign CDS $H_0 : \delta^3 = 0$ |
|---------|--|-----------------------------|---------------------------------------|
| DE | - | - | - |
| ES | - | ** | *** |
| FR | - | - | * |
| IT | - | - | ** |

The Granger causality tests are based on the following equation of the one-lag VAR model:

$$ELOSS_{country,t} = c_1 + \beta ELOSS_{country,t-1} + \delta^1 YIELD_{DE,t-1} + \delta^2 PMI_{t-1} + \delta^3 CDS_{country,t-1} + \varepsilon_t$$

where $ELOSS$, $YIELD_{DE}$, PMI and CDS stand for the expected loss component, the yield on ten-year German Bunds, the PMI and the sovereign CDS premium.

***, ** and * represent a rejection of H_0 at a significance level of 1%, 5% and 10%, respectively.

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