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On the Estimation of the Volatility-Growth Link

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On the Estimation of the Volatility-Growth Link

Abstract

It is common practice to estimate the volatility-growth link by specifying a standard growth equation such that the variance of the error term appears as an explanatory variable in this growth equation. The variance in turn is modelled by a second equation. Hardly any of existing applications of this framework includes exogenous controls in this second variance equation. Our theoretical findings suggest that the absence of relevant explanatory variables in the variance equation leads to a biased and inconsistent estimate of the volatility-growth link. Our simulations show that this effect is large. Once the appropriate controls are included in the variance equation consistency is restored. In short, we suggest that the variance equation must include relevant control variables to estimate the volatility-growth link.

JEL-Code: E320, O470.

Keywords: volatility and growth, growth regression, endogenous variance, unbiased estimates.

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1 Introduction

The background – Understanding the link between volatility and growth is central to many empirical analyzes. A prominent approach includes the variance of the error term of a growth regression into the very same growth equation as an explanatory variable. This is the approach pioneered by Ramey and Ramey (1995), henceforth RR. This approach has been extremely influential and led to many valuable insights. Despite this huge success, endogeneity of growth volatility has been seldom discussed.

The problem – Although it has been established that growth volatility is endogenous to determinants of economic growth,² empirical modeling of such dependence has not been discussed in detail so far. We argue that failing to properly account for dependence of the error variance on exogenous factors in this type of modelling may substantially bias the parameter estimates. It has already been recognized by RR that the endogeneity of volatility is important. They make the variance of the error term in the growth regression dependent on the squared residuals taken from forecasting regressions for government expenditures. Their idea was to use forecast errors as a measure of unobserved shocks. RR do not discuss, however, the correct specification of variance endogeneity or consequences of its misspecification, leaving the issue of endogenous volatility basically implicit.

The problem with the standard specification is the absence of explanatory variables in the equation for the growth volatility. This suggests that more explanatory variables are needed in the conditional variance equation than just forecast errors. Since the volatility term appears among explanatory variables in the growth equation, omitted variables in the conditional variance equation potentially lead to correlation between explanatory variables and the error term in the growth equation. This renders estimation of the feedback effect on economic growth captured by the variance term in the growth equation inconsistent. Inconsistence persists even if there are no omitted variables in the growth equation and if all variables are measured without error.

Our proposal – This note discusses an extension of the original RR model and specifies it as a model of conditional heteroscedasticity in mean (henceforward CH-M). As in RR, there is a growth equation that contains the volatility term and a variance equation. The extension consists in explicit allowing for explanatory variables in the variance equation. Using these additional explanatory variables, the RR approach will continue to remain a highly useful framework to investigate the volatility-growth link.

We demonstrate theoretically that a bias arises in the CH-M model of output growth if relevant control variables are omitted from the conditional variance equation. Thus, for example, neglecting the RR prediction error of government expenditure shocks potentially leads to a systematic bias in the estimated parameters of interest, particularly the one that links volatility and growth. In a simulation based on an example borrowed from the literature

²For a discussion of the literature on economic growth see Temple (1999). An elaborated investigation on linking the endogeneity of macroeconomic volatility to weak institutions is in Acemoglu et al. (2003). Theoretical analysis of the joint endogeneity of long-run growth and short-run volatility are undertaken in the ‘natural volatility’ literature (see e.g. Matsuyama, 1999, Francois and Lloyd-Ellis, 2003, Wälde 2005 and Posch and Wälde, 2011). Aghion et al. (2010) underscore strong empirical negative dependence between volatility and growth. Fernández-Villaverde et al. (2011) document strong influence of volatility shocks on real variables like output, consumption, investment and hours worked.

(Posch 2011), we show that the above bias is of economic importance for the volatility-growth nexus.

The literature – The most recent literature that follows the empirical setup of RR includes Dawson et al. (2001), Imbs (2007), Edwards and Yang (2009), Ponomareva and Katayama (2010), Posch (2011) and Posch and Wälde (2011), among others. Of these only Edwards and Yang (2009), Posch (2011) and Posch and Wälde (2011) explicitly consider the conditional volatility. Edwards and Yang (2009) analyze spatial differences in the influence of volatility on growth, Posch (2011) and Posch and Wälde (2011) include tax rates and further controls. None of these papers, however, addresses the source of the potential bias in the estimates of the volatility-growth link and its quantitative importance. It is somewhat unfortunate that in the rest of the literature modelling conditional variance has passed unnoticed, whereas exactly this gives rise to the mentioned systematic bias of the estimated effect of volatility on growth.

Remarkably, Dawson et al. (2001) and Ponomareva and Katayama (2010) discuss a related bias which appears in the empirical RR model if some explanatory variables in the growth equation are measured with error. We show that the bias induced by omitted variables in the conditional variance equation can be alternatively represented as an errors-in-variables bias, where volatility term could be considered as a regressor measured with error. Thus both types of biases have similar manifestation. Still an important difference in our case is that if some relevant controls are omitted from the volatility equation the bias will arise even if all other variables included in the growth regression are measured without error.

Our model may be viewed as a special case of the original ARCH-M model of Engle et al. (1987) and Nelson (1991), where the coefficients in front of autoregressive terms in the variance equation are set to zero. As a consequence, only explanatory variables of a current period matter for the variance (see Engle et al., 1987, equation 9, with $\alpha = 0$). Without emphasizing the role of explanatory variables in the variance equation explicitly, Engle et al. (1987) provide the framework that accounts for the bias discussed here.

The outline – The next section presents an augmented CH-M model. Section 3 provides theoretical insights into the existence and the source of the bias. It also conducts Monte-Carlo simulations in order to show the quantitative importance of the bias for the RR estimate of the link between volatility and growth. Section 4 concludes.

2 A volatility-growth regression with controls in the conditional variance equation

2.1 The regression setup

Consider the following extension of Ramey and Ramey (1995) borrowed from Posch (2011). Our argument is not limited for the illustration at hand, in fact it holds for any CH-M model in which a feedback effect in the growth equation is present. We specify the following growth equation and conditional variance equation,

$$\Delta y_{it} = \nu \sigma_{it} + \theta X_{it} + \varepsilon_{it}, \quad \text{where} \quad \varepsilon_{it} \sim N(0, \sigma_{it}^2), \quad (1a)$$

$$\log(\sigma_{it}) = \alpha_i + \mu_t + \beta Z_{it}. \quad (1b)$$

In these equations, Δy_{it} is the growth rate of output for country i in year t , σ_{it} is the standard deviation of the error term in the growth equation; X_{it} is a vector of control variables (e.g., the Levine-Renelt variables); Z_{it} is a vector of control variables (e.g., a subset of X_{it}); α_i and μ_t are country and time fixed effects; θ and β are vectors of coefficients. The key parameter of interest in a volatility-growth analysis is ν , which links growth to volatility.

We will now show the importance of including additional controls in the conditional variance equation in two ways. First, we will demonstrate analytically that omitted control variables induce systematic bias into the maximum likelihood (ML) estimator of the volatility-growth link ν . Second, we will confirm by simulation that this bias is large quantitatively.

2.2 Analytical result

- ML estimation with neglected controls in variance equation

Consider the model in (1a)-(1b), where for simplicity we drop the subscript i and country/time fixed effects, as they do not alter the argument. Let the standard deviation of the error term in the correctly specified growth regression, σ_t , depend on explanatory variables as: $\sigma_t = \exp\{\alpha + \beta Z_t\}$. Once dependence on Z_t is neglected, the same standard deviation in the misspecified model, say $\tilde{\sigma}_t$, will be given just by: $\tilde{\sigma}_t = \exp\{\alpha\}$. Keeping this in mind, growth equation (1a) can be written as

$$\begin{aligned}\Delta y_t &= \nu \sigma_t \pm \nu \tilde{\sigma}_t + \theta X_t + \varepsilon_t \\ &= \nu \tilde{\sigma}_t + \theta X_t + (\varepsilon_t + \nu[\sigma_t - \tilde{\sigma}_t]) \\ &= \nu \tilde{\sigma}_t + \theta X_t + \tilde{\varepsilon}_t,\end{aligned}$$

where $\tilde{\varepsilon}_t \equiv \varepsilon_t + \nu[\sigma_t - \tilde{\sigma}_t]$ and ε_t is not correlated with X_t and Z_t by assumption. Inserting for both σ_t and $\tilde{\sigma}_t$ in this new error term $\tilde{\varepsilon}_t$ we get

$$\tilde{\varepsilon}_t = \varepsilon_t + \nu e^\alpha [e^{\beta Z_t} - 1].$$

Consider now estimation of the equation

$$\Delta y_t = \nu \tilde{\sigma}_t + \theta X_t + \tilde{\varepsilon}_t$$

where explicit dependence on Z_t in the variance equation is omitted. Omitting the dependence on Z_t amounts to specifying the error term in this equation identically to that of the original equation (1a), i.e.

$$\Delta y_t = \nu \tilde{\sigma}_t + \theta X_t + u_t, \quad \text{where } u_t \sim N(0, \tilde{\sigma}_t), \quad (2a)$$

$$\log(\tilde{\sigma}_t) = \alpha. \quad (2b)$$

It is straightforward to show (see Appendix) that the maximum likelihood estimator of the parameter ν in the misspecified model (2a)-(2b) has a form

$$\hat{\nu} = T^{-1} \sum_{t=1}^T \frac{\Delta y_t - \theta X_t}{\tilde{\sigma}_t}$$

Taking the expected value of $\hat{\nu}$ with respect to the distribution of the dependent variable in the correctly specified model we obtain

$$E(\hat{\nu}) = \nu T^{-1} \sum_{t=1}^T e^{\beta Z_t}$$

as shown in the Appendix. This expected value is not equal to the true parameter ν unless $\beta = 0$, meaning that $\hat{\nu}$ is biased. Furthermore, the bias does not disappear asymptotically, as

$$\text{plim } \hat{\nu} = \nu E e^{\beta Z},$$

meaning that unless the true β is equal to zero $\hat{\nu}$ is inconsistent.³

Clearly, in a correctly specified model which explicitly considers Z_t in the variance equation the ML estimator of ν has all the standard properties.

The result just demonstrated has one interesting practical implication. As Z_t need not always be a subset of X_t , even if some variables are not significant in the growth equation, they may still be significant in the conditional variance equation. Consequently these variables may influence growth only indirectly, via volatility. This influence must be accounted for, though, because otherwise the estimate of the volatility-growth link will become inconsistent.

- Alternative look at the source of the bias

The above demonstrated bias can also be interpreted as an errors-in-variables bias, where growth volatility could be seen as a regressor measured with error. Assume that by some chance we are able measure the volatility term in the data (e.g. via collecting multiple proxy variables for growth volatility and creating a composite index). Though, our measure can be only imperfect. Once the true measure, σ_t , in the growth equation is substituted by the available imperfect measure, $\tilde{\sigma}_t$, the error term immediately adjusts by the difference between the two, where the difference is completely attributed to the measurement error. Since this difference is a function of Z_t , as the true volatility is the function of Z_t , the new error term will be correlated with X_t , namely

$$\text{Cov}(X_t, \tilde{\varepsilon}_t) = \text{Cov}(X_t, \varepsilon_t) + \text{Cov}(X_t, \nu e^{\alpha}[e^{\beta Z_t} - 1]) = \nu e^{\alpha} \text{Cov}(X_t, e^{\beta Z_t}).$$

Whenever $\beta = 0$ or X_t and Z_t are not stochastically independent it follows that $\text{Cov}(X_t, \tilde{\varepsilon}_t) \neq 0$. Correlation between the error term and regressors is a common source of the endogeneity bias.

Also note that except of σ_t all other variables, namely X_t and Z_t , are implicitly assumed to be measured correctly, which is different from the analysis of Dawson et al. (2001).

2.3 Monte-Carlo simulation

To provide quantitative support for the above demonstrated bias we simulate our model. As in the analytical discussion we consider the model in (1a)-(1b) suppressing country and time

³Repeating the steps outlined in the Appendix it is likewise possible to show that the ML estimate of θ in the misspecified model is also biased and inconsistent.

fixed effects for simplicity.⁴ Furthermore, again to simplify the simulation, we assume that $X_t = Z_t$, i.e. both growth rate of output and variance of this growth rate are determined by the same set of explanatory variables. Once again, this assumption is purely for the ease of illustration, our argument would also apply if X_t was independent from Z_t . We assume Z_t to follow a structure displaying time-variation of the kind shown in Figure 1.⁵

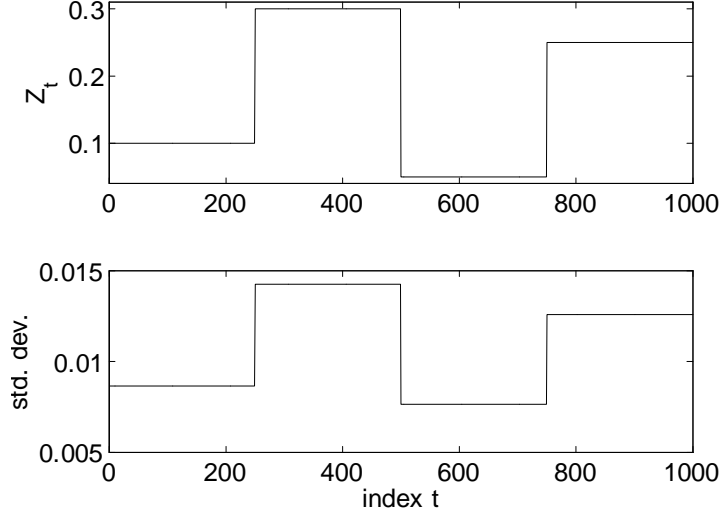


Figure 1 Our control variable Z_t and the implied standard deviation σ_t of the residuals

Under these assumptions our model for the simulation becomes

$$\begin{aligned} \Delta y_t &= \nu \sigma_t + \theta Z_t + \varepsilon_t, \quad \text{where } \varepsilon_t \sim N(0, \sigma_t^2), \\ \log(\sigma_t) &= \alpha + \beta Z_t. \end{aligned}$$

For a set of predetermined parameters ν , θ , α , and β , conditional on the tax vector Z_t and the vector of variances σ_t^2 at any time t , we draw a sample of $T = 1.000$ errors ε_t from the normal distribution $N(0, \sigma_t^2)$. This allows us computing T values for Δy_t . Having done so, we estimate the parameters of the above model by maximum likelihood using the simulated data. The resulting estimates constitute the estimates from a correctly specified model, of which we record the estimated value of ν . Next we consider the misspecified model ignoring Z_t in the variance equation. Estimating by maximum likelihood the misspecified model, we

⁴We also included lagged squared error terms $\varepsilon_{i,t-1}^2$ and/or lagged conditional variances $\log \sigma_{i,t-1}$ in the conditional variance equation (1b), extending our exponential CH-M model to the class of GARCH-M models (cf. Engle and Bollerslev, 1986). The inclusion of (generalized) autoregressive terms does not change our results.

⁵This structure was originally motivated by understanding the effect of taxes and tax reforms on growth and volatility. Such a tax vector could reflect three tax reforms over the length of time for which data is available. Tax rates are constant between reforms. The resulting standard deviations in the lower panel show that values are quantitatively reasonable. From a cross-sectional perspective, Z_t (or more precisely, Z_i) could reflect differences in tax rates accross countries i with tax rates that are time-invariant. Neglecting the cross-sectional variation would then also bias estimates.

obtain what we call biased parameters. Among these we again record the estimated value of the parameter ν . We repeat this procedure $N = 10.000$ times, which results in N pairs of estimates of ν , first element of this pair being the estimate from the correctly specified and second element - from the misspecified model. After that we plot these estimates of ν against the true values of ν chosen for the simulation. We do not vary the parameters α and β .

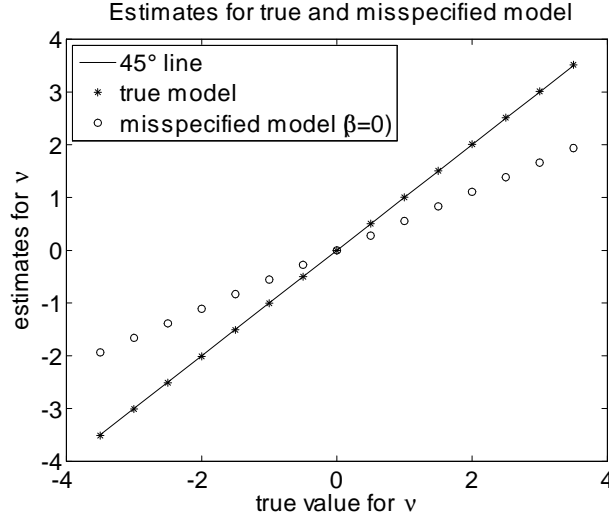


Figure 2 *Estimates for true and misspecified model for various ν*

Simulation results are summarized in fig. 2. The horizontal axis of this figure shows the true values for ν used in the simulation. On the vertical axis we plot the estimates from the correctly specified (asterisks) and misspecified (circles) models. In addition, we draw a 45° line to illustrate the equality to the true values of ν . We see that estimates from the correctly specified model are all stretching along the 45° line, whereas estimates from the misspecified model fail to replicate the 45° line by wide margin. N and T have been chosen such that confidence intervals around the estimated values are narrow enough to be neglected. A similar picture likewise emerges with smaller sample sizes (e.g. $T = 100$). Thus, fig. 2 shows that if Z is omitted from the variance equation, the estimates of the feedback effect of the volatility on growth can be substantially biased, confirming our analytical result.⁶

2.4 Outlook

Given the result above, the question of primary importance becomes: What are the right controls that need to be included in the variance equation?

In some trivial sense practical work should consider all plausible variables as candidates for the variance equation (notably, variables on economic institutions, in which respect Acemoglu et al., 2005, provide initial guidance). Sequential testing and elimination of jointly

⁶ Although lying beyond the scope of present discussion, we also find that estimates of θ in the misspecified model are biased even more than those of ν .

insignificant variables would subsequently be the least sophisticated way of dealing with the problem. A more sophisticated approach to retaining the right variables is the Bayesian averaging of ML estimates similar to that of Sala-i-Martin et al. (2004). This approach is also more advantageous inasmuch as it simultaneously informs about the robustness of the estimate of the volatility-growth link.

Since variable selection using the approach of Sala-i-Martin et al. (2004) is a project in itself, we refrain from setting it up in the present paper. Yet we do call for future research in this direction.

3 Conclusion

Economic theory suggests that the degree of volatility of an economy is endogenous. Empirical frameworks that do not account for this endogeneity imply that the estimate for the volatility-growth link is biased. We show this both theoretically and by Monte-Carlo simulations. We suggest that the growth-volatility link should only be estimated if the endogeneity of volatility is sufficiently controlled for by including explanatory variables also in the variance equation.

4 Appendix - ML estimation of the volatility-growth parameter in the misspecified model

Derivation of the estimator – Consider the misspecified model (2a)-(2b). The individual contribution to the likelihood is

$$\ell_t = \frac{1}{\tilde{\sigma}_t \sqrt{2\pi}} \exp \left\{ -\frac{1}{2} \left(\frac{\Delta y_t - (\nu \tilde{\sigma}_t + \theta X_t)}{\tilde{\sigma}_t} \right)^2 \right\},$$

and the total log-likelihood reads

$$\log \mathcal{L} = -\frac{T}{2} \log(2\pi) - T \log(\tilde{\sigma}_t) - \frac{1}{2} \sum_{t=1}^T \left(\frac{\Delta y_t - \theta X_t}{\tilde{\sigma}_t} - \nu \right)^2.$$

Taking first order condition with respect to ν we get

$$\frac{\partial \log \mathcal{L}}{\partial \nu} = -\frac{1}{2} \sum_{t=1}^T \frac{\partial}{\partial \nu} \left[\left(\frac{\Delta y_t - \theta X_t}{\tilde{\sigma}_t} - \nu \right)^2 \right] = \sum_{t=1}^T \left(\frac{\Delta y_t - \theta X_t}{\tilde{\sigma}_t} - \nu \right).$$

Setting this result to zero the ML estimate $\hat{\nu}$ of the true parameter ν in the misspecified model immediately follows

$$\hat{\nu} = T^{-1} \sum_{t=1}^T \frac{\Delta y_t - \theta X_t}{\tilde{\sigma}_t}.$$

In this result, the rest of the parameters are for the moment kept as their true unknown values.

Properties of the estimator – Taking the expected value of $\hat{\nu}$ with respect to the distribution of the dependent variable in the true model

$$\Delta y_t = \nu \sigma_t + \theta X_t + \varepsilon_t$$

we obtain

$$\begin{aligned} E(\hat{\nu}) &= T^{-1} \sum_{t=1}^T \frac{E(\Delta y_t) - \theta X_t}{\tilde{\sigma}_t} = T^{-1} \sum_{t=1}^T \frac{E(\nu \sigma_t + \theta X_t + \varepsilon_t) - \theta X_t}{\tilde{\sigma}_t} \\ &= T^{-1} \sum_{t=1}^T \left[\frac{\nu \sigma_t}{\tilde{\sigma}_t} + \frac{E(\varepsilon_t)}{\tilde{\sigma}_t} \right] = \nu T^{-1} \sum_{t=1}^T \frac{\exp\{\alpha + \beta Z_t\}}{\exp\{\alpha\}} = \nu T^{-1} \sum_{t=1}^T e^{\beta Z_t} \end{aligned}$$

This implies that $E(\hat{\nu}) \neq \nu$ unless $\beta = 0$ in the true model.

Furthermore, for any sequence of random variables $\{Z_t\}_{t=1}^T$ with appropriate conditions on the moments (and possibly distribution) of Z_t a corresponding law of large numbers applies and

$$T^{-1} \sum_{t=1}^T e^{\beta Z_t} \xrightarrow{p} E(e^{\beta Z}).$$

as $T \rightarrow \infty$. From this follows that

$$\text{plim } \hat{\nu} = \nu E e^{\beta Z} \neq \nu$$

unless $\beta = 0$ in the true model.

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