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Abstract

We study the exclusionary properties of nonlinear price-quantity schedules in an Aghion-Bolton style model with elastic demand and product differentiation. We distinguish three regimes depending on whether and how the price of the incumbent good is linked to the quantity purchased from the rival firm. We find that the supply of rival good is distorted downwards. Moreover, given the quantity supplied from the rival, the buyer may opportunistically purchase inefficiently many units from the incumbent to pocket quantity rebates. We show that the possibility for the buyer to dispose of unconsumed units attenuates the opportunism problem and limits the exclusionary effects of nonlinear pricing.

JEL-Code: L120, L420, D820, D860.

Keywords: inefficient exclusion, buyer opportunism, disposal costs, quantity rebates, incomplete information.

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1 Introduction

In recent years, exclusionary conduct by firms with strong market power has become a highpriority issue on the agenda of antitrust agencies. For instance, the European Commission has made it clear that the emphasis of its enforcement activities is on "ensuring that undertakings which hold a dominant position do not exclude their competitors by other means than competing on the merits of the products or services they provide." The U.S. Department of Justice states that "whether conduct has the potential to exclude, eliminate, or weaken the competitiveness of equally efficient competitors can be a useful inquiry", and suggests that this inquiry "may be best suited to particular pricing practices."¹

In this article, we consider a wide range of pricing practices that fall under the general heading of nonlinear pricing, e.g. quantity or market-share rebates and exclusivity discounts. We organize a taxonomy of price schemes around the following main distinction: whether or not the price set by the dominant firm depends on the quantity supplied from rivals. When this is the case, we say that the dominant firm's price schedule is "conditional" (on rival quantities). Market-share discounts enter into this category. Because enforcing a conditional price may be unfeasible or legally prohibited, we also consider the situation where the firms are restricted to use "non-conditional" price schedules. Finally we define "exclusivity-based" schedules as conditional schedules for which the price depends on whether or not the buyer supplies exclusively from the dominant firm, but does not otherwise depend on the quantities sold by competitors.

Our analysis aims to understand how these different types of price-quantity schedules affect the way large buyers split their purchase requirements between the dominant firm and rival suppliers. It relies on a game close to Aghion and Bolton (1987) with three players – an incumbent firm, a rival, and a buyer – where contract offers are sequential: first a price schedule is decided by the buyer and the incumbent; only then have the rival and the buyer a chance to interact. In the present paper, the incumbent's market power is captured by the firstmover advantage and the corresponding commitment power. In a companion paper, Choné and Linnemer (2014), we introduce on top of incumbency the notion that the incumbent firm is, at least to some extent, an "unavoidable trading partner" – a key ingredient of dominance

¹See, respectively, European Commission (2009) and U.S. Department of Justice (2008). High-profile exclusionary cases involving pricing practices include *Virgin v British Airways* (S.D.N.Y. 1999 and 2nd Cir. 2001), *Concord Boat* (8th Cir. 2000), *Lepage's v 3M* (3d Cir. 2003) in the United States; *Virgin/British Airways* (2000/74/EC of 14 July 1999), *Michelin* (COMP/E-2/36.041/PO of 20 June 2001), *Tomra* (COMP/E-1/38.113, 2006), and *Intel* (COMP/C-3 /37.990, 2009) in Europe. Figueroa, Ide, and Montero (2014) present a Chilean case: *Chile v. Unilever*.

under European competition law at least since Hoffmann-La Roche.²

As in Aghion and Bolton (1987), we assume that the buyer and the incumbent contract at a time when the characteristics of the rival good are not yet known, i.e., the rival's cost and the buyer's willingness to pay for the rival good are uncertain. To concentrate on the exclusionary effects of nonlinear pricing, we assume away any bilateral inefficiency (e.g. asymmetric information) between the buyer and each of the two suppliers. In particular, the buyer and the incumbent would have no reason to distort the traded quantity in the absence of a rival. Similarly, we assume throughout the article that the negotiation between the buyer and the rival takes place under perfect information and is efficient. Formally, the game is thus equivalent to an asymmetric information set-up where the principal would be the buyer-incumbent pair and the agent the buyer-rival pair, and we can thus use insights from the nonlinear pricing literature, see Wilson (1993) and Laffont and Martimort (2002). The fact that the buyer is part of both coalitions raises interesting theoretical questions that are discussed at the end of the paper. In particular, the buyer's dual role might open a scope for more sophisticated screening instruments and create subtle patterns of information revelation.

In the spirit of Martimort and Stole (2009), we are interested in distortions of productive allocations at both the extensive and the intensive margins. In their terminology, our framework is a common-agency game: the buyer may supply exclusively from the incumbent firm, in which case the rival is driven out of the market. We carefully examine distortions at the "extensive" margin, and indeed find that complete exclusion of an efficient rival occurs with positive probability. A contribution of the present article is to consider distortions at the intensive margin as well. To this aim, we model the incumbent and the rival goods as imperfect substitutes for the buyer. The degree of substitution can vary from perfect substitutes to independent goods.³ We find intensive distortions of the quantity supplied by the rival, specifically that quantity is positive but distorted downwards, which is sometimes referred to as "partial foreclosure" in the antitrust literature.

We emphasize a second kind of intensive distortions, which pertains to the quantity of incumbent good *at given level of rival supply*. This distortion is linked to an opportunistic behavior of the buyer at the last stage of the game, hereafter referred to as "buyer opportunism". The intuition goes as follows. The general purpose of the quantity-price schedules agreed upon by the incumbent and the buyer is to place the latter in a favorable position when bargaining with the rival. In this bargain, the buyer can argue she will lose rebates if

²Judgment of the European Court of Justice of 13 February 1979. Hoffmann-La Roche & Co. AG v Commission of the European Communities. Case $85 \setminus 76$.

 $^{^{3}}$ Marx and Shaffer (2004) also study a model à la Aghion and Bolton with differentiated goods but they restrict themselves to a complete information setting.

she purchases less from the incumbent, which allows her to extract surplus from the rival. Ex ante, the incumbent and the buyer share expected profits and their interests are aligned. Ex post, however, the buyer does not take into account the production costs of the incumbent good. Due to the offered rebates, the buyer has an incentive to purchase inefficiently many units from the incumbent conditionally on the quantity supplied from the rival.

A key issue in the paper is to compare the exclusionary properties of the three considered price schedules – conditional, exclusivity-based, and non-conditional. In Aghion and Bolton (1987) the buyer's demand is inelastic and is supplied from only one producer, making it hard to distinguish between the three types of schedules. In contrast, here, the results differ strikingly across the three pricing regimes.

When the price of the incumbent good can freely depend on the supply from the rival (conditional regime), the optimal schedule is a two-part tariff. The incumbent good is priced at marginal cost, hence the absence of buyer ex post opportunism. The fixed part of the tariff is increasing and concave in the quantity purchased from the rival. That fixed part can be seen as a penalty imposed for buying from the rival, in line with Aghion and Bolton (1987), but here the rival's supply is distorted at both the extensive and the intensive margins. These distortions increase with the rival's bargaining power vis-à-vis the buyer. Market-share rebates are shown to be ill-adapted to control buyer opportunism.

When the price schedule only depends on the incumbent quantity (non-conditional regime), the buyer purchases the efficient quantity of rival good given the incumbent's quantity. This link between the two quantities creates a channel through which the buyer and the incumbent can indirectly control the rival's activity. In equilibrium, the marginal price of the incumbent is lower than the marginal cost of production up to a certain quantity threshold. These generous rebates allow the buyer to extract a good deal from the rival but at the same time induce her to behave opportunistically *ex post*. This distortion, in turn, translates into complete or partial foreclosure of efficient rival types. The presence of complete exclusion in equilibrium implies that the price schedule is not globally concave: the price is set at a high level beyond the quantity threshold mentioned above to deter the buyer from purchasing even more units of incumbent good, hence a convex kink in the schedule.

In the exclusivity-based regime, the price schedule is the same as in the non-conditional case for low quantities of incumbent good. The exclusivity offer allows to avoid buyer opportunism when the rival is inactive. On the other hand, this offer creates locally a strong distortion at the extensive margin, excluding a bunch of efficient rival types.

Finally, we are able to extend the analysis to the case where the buyer can dispose of or resell unconsumed units of incumbent good. In practice, the magnitude of the disposal costs depends on the seller's ability to impose or to prevent particular uses of the purchased units and on the buyer's ability to avoid such monitoring by the dominant firm. Depending on the industry, unused items can be difficult to store or dispose of making disposal costs large. On the contrary, the buyer may have access to a secondary market and resell the extra units making disposal costs negative.

Purchasing units from the incumbent with the sole purpose of pocketing rebates, and then throwing away the unneeded units, would constitute an extreme form of buyer opportunism. We show that this form is never part of an equilibrium. We find that low disposal costs prevent the incumbent from committing on too generous rebates because the buyer could purchase units and discard them. Lower disposal costs are associated to less exclusion and higher values of the expected total welfare. Antitrust authorities, therefore, should pay close attention to contracting provisions that help increase disposal costs.

It is worthwhile relating our work to recent studies on market-share discounts. In a setting with a dominant firm, a competitive fringe and two retailers, Inderst and Shaffer (2010) show that market-share discounts can be used by the dominant firm to dampen intra- and inter-brand competition. Their anticompetitive scenario, contrary to the one presented here, highlights retail competition and assume complete information. Turning to models with imperfect information, most of the literature has examined how specific forms of pricing perform in discriminating among privately informed buyers. For instance, in a discrete type model, Kolay, Shaffer, and Ordover (2004) show that all-units discounts are more effective than menus of two-part tariffs in screening out retailers with private information about the state of demand. Majumdar and Shaffer (2009) and Calzolari and Denicolo (2013) introduce market-share discounts. In the former article, a dominant firm resorts to nonlinear pricing to screen a buyer who is informed about the size of demand and who also sells a good provided by a competitive fringe. The latter article addresses the issue in a symmetric duopoly setting, considering both market-share discounts and exclusive contracts.

The article is organized as follows. Section 2 introduces the model, and Section 3 studies conditional price-quantity schedules. Assuming very large disposal costs, Sections 4 and 5 explore the non-conditional and exclusivity-based regimes. Section 6 describes the effect of moderate disposal costs. Section 7 discusses a couple of extensions regarding the timing of the game, the informational environment, and the available instruments.

2 The model and purchase decisions

A dominant firm, I, competes with a rival, E, to serve a buyer, B. Marginal production costs are assumed to be constant and are denoted by c_I and c_E . The timing of events reflects the incumbency advantage of the dominant firm and the uncertainty as to the characteristics of the rival good: 1) B and I design a price-quantity schedule to maximize (and split) their joint expected surplus. At this stage, they know c_I and the characteristics of good I, but they do not know c_E nor the willingness to pay v_E for the rival good. 2) B and E discover c_E and v_E and jointly decide on the variables under their control, namely a transfer p_E and quantities q_E and q_I , knowing both the terms of the agreement between B and I and all the relevant cost and preference parameters.

At the first stage, we consider three types of price-quantity schedules that differ in how the price of the incumbent good depends on the quantity supplied from the rival: (i) under a non-conditional schedules $T(q_I)$, the price depends only on the number of *I*-units purchased; (ii) under a conditional schedule $T(q_E, q_I)$, the price of q_I units of good *I* freely depends on the quantity purchased from the rival; (iii) an exclusivity scheme is a pair of schedules $(T(q_I), T^x(q_I))$ that specifies the price of q_I units of good *I* if the buyer supplies exclusively from the incumbent, $T^x(q_I)$, and if she purchases a positive number of units from the rival firm, $T(q_I)$.⁴

At the second stage, we assume that B and E negotiate under complete information (Nash bargaining where β denotes E's bargaining power) to maximize their joint surplus. The timing of negotiations assumes that B and I cannot renegotiate once uncertainty is resolved. This assumption and a couple of variants are discussed in Section 7.

Buyer's demand When the buyer consumes x_E units of good E and x_I units of good I, she earns a gross profit of $v_E x_E + v_I x_I - h(x_E, x_I)$, where h is a convex function of (x_E, x_I) with first derivatives at (0,0) equal to zero and with positive cross-derivative to reflect the imperfect substitutability of the two goods.

A key feature of the model is that the buyer can dispose of unneeded units of each good at a cost $\gamma_E \ge -c_E$ and $\gamma_I \ge -c_I$. That is, it is always inefficient (from a welfare perspective) to produce units in order to throw them away or to resell them. Consequently, the buyer's net utility if she purchases q_E units from the rival and q_I units from the incumbent is

$$V(q_E, q_I) = \max_{x_E \le q_E, x_I \le q_I} v_E x_E + v_I x_I - h(x_E, x_I) - \gamma_E(q_E - x_E) - \gamma_I(q_I - x_I).$$
(1)

The buyer disposes of units of good k, k = E, I, when the purchased quantity q_k is so large that the marginal utility $v_k - \partial h(q_k, q_l)/\partial q_k$ becomes smaller than the utility loss caused by disposal, $-\gamma_k$. In this region, the buyer net utility V decreases linearly with q_k , and the marginal net utility $\partial V/\partial q_k$ is equal to $-\gamma_k$. When the buyer consumes all the purchased

 $^{^{4}}$ We do not impose a priori restrictions on the shape of the price schedules. Some authors have studied specific types of schedules such as two-part tariffs (Marx and Shaffer (1999)) and all-units discounts (Feess and Wohlschlegel (2010)) under complete information.

units of the rival and incumbent goods ("no-disposal region"), the marginal net utility is greater than $-\gamma_k$ for each good.

Efficient quantities We denote by q_E^{**} and q_I^{**} the quantities that maximize the total surplus

$$W(q_E, q_I) = V(q_E, q_I; v_E) - c_E q_E - c_I q_I.$$

The efficient quantities involve no disposal and hence do not depend on the magnitude of disposal costs. These quantities also maximize $\omega_E q_E + \omega_I q_I - h(q_E, q_I)$, where $\omega_E = v_E - c_E$ and $\omega_I = v_I - c_I$. Hence q_E^{**} and q_I^{**} are respectively nondecreasing and non-increasing in ω_E . Hereafter, we denote by ω_E^{**} the maximum value of ω_E for which $q_E^{**}(\omega_E) = 0$. We now introduce the distribution of ω_E , that we denote by F, and a set of assumptions maintained throughout the paper.

Assumption 1. The distribution of ω_E has a positive density f on its support $[\underline{\omega}_E, \overline{\omega}_E]$, with $\underline{\omega}_E < \omega_E^{**} < \overline{\omega}_E$ and $q_I^{**}(\overline{\omega}_E) > 0$. The hazard rate f/(1-F) is nondecreasing in ω_E .

The assumption on ω_E^{**} allows us to concentrate on the most interesting case where full exclusion is socially optimal with positive probability. Moreover, to avoid uninteresting complications, we assume that both firms are active when the surplus created by the rival is maximal, formally $q_E^{**}(\overline{\omega}_E), q_I^{**}(\overline{\omega}_E) > 0$.

Definition 1. The quantity of good E that maximizes the social welfare W given q_I is said to be conditionally efficient and is denoted by $q_E^*(q_I; \omega_E)$. The conditionally efficient quantity of incumbent good, $q_I^*(q_E; \omega_I)$, is symmetrically defined.

If the buyer consumes all the units of good I she has purchased, then $q_E^*(q_I; \omega_E)$ is defined by the first order condition $\partial h/\partial q_E(q_E^*, q_I) = \omega_E$. In this region, the function $q_E^*(q_I; \omega_E)$ is decreasing by substitutability. In contrast, in the region where q_I is so high that the buyer disposes of some units of good I, q_E^* does not vary with q_I as only the *consumed* quantity of good I is relevant to determine the conditionally efficient quantity of good E. In this region, total surplus W decreases linearly with q_I , and the partial derivative $\partial W/\partial q_I$ is $-c_I - \gamma$.

Definition 2. The rival firm is said to be super-efficient when $q_E^*(q_I; \omega_E)$ is positive for any value of q_I .

Example: Quadratic utility The leading example in this paper has $h(x_E, x_I) = x_E^2/2 + x_I^2/2 + \sigma x_E x_I$, $0 \le \sigma < 1$. The efficient quantities involve no disposal cost and are given by

$$q_E^{**}(\omega_E) = \max\left(\frac{\omega_E - \sigma\omega_I}{1 - \sigma^2}, 0\right) \text{ and } q_I^{**}(\omega_E) = \frac{\omega_I - \sigma\omega_E}{1 - \sigma^2}.$$
(2)

To respect Assumption 1, we must have in the quadratic case: $\underline{\omega}_E < \omega_E^{**} = \sigma \omega_I < \overline{\omega}_E < \omega_I / \sigma$. The efficient allocation is represented by the point A on Figure 1. When the buyer's utility is quadratic, the welfare isolines are ellipses centered at A.

If the buyer has purchased q_I units of good I, with $q_I \ge v_I + \gamma - \sigma q_E$, she consumes $x_I = v_I + \gamma - \sigma q_E$ units of good I, thus an amount that is independent of q_I . The no-disposal region is located below the bold dashed line on the figure. Applying the envelope theorem, we find that the conditionally efficient quantity $q_E^*(q_I; \omega_E)$ is constant in this region and equal to the second argument of the following maximum:

$$q_E^*(q_I;\omega_E) = \max\left(\omega_E - \sigma q_I, \frac{\omega_E - \sigma(v_I + \gamma)}{1 - \sigma^2}, 0\right).$$

The rival firm is super-efficient if and only if $\omega_E > \sigma(v_I + \gamma)$. This is the case represented on Figure 1, where $q_E^*(q_I; \omega_E)$ is positive for any value of q_I .

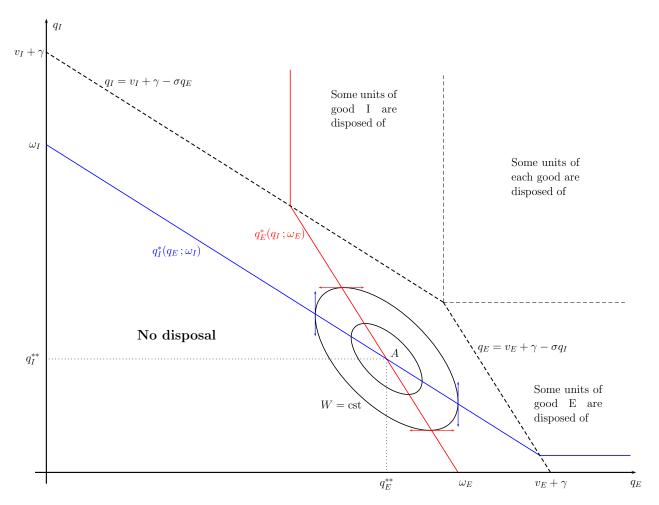


Figure 1: The total welfare is maximal at A (quadratic example)

Purchase decisions The last stage of the game takes place under perfect information, given the price schedule $T = T(q_E, q_I)$ or $T = T(q_I)$ and the known characteristics of the rival good. The buyer and the rival choose the quantities to maximize their joint surplus

$$S_{BE} = \max_{q_E, q_I} V(q_E, q_I) - T(q_E, q_I) - c_E q_E,$$
(3)

with no consideration for the incumbent's cost or profit. The above expression shows that under a non-conditional schedule $T(q_I)$, the quantity of rival good is efficient given that of the incumbent good, formally $q_E = q_E^*(q_I; \omega_E)$, implying that no unit of the rival good is produced and disposed of. To avoid uninteresting developments, we take the latter property as granted under conditional schedules as well.⁵

Without loss of generality, the competitor's outside option is normalized to zero. As to the buyer, she may source exclusively from the incumbent, so her outside option is

$$V_B^0 = \max_{q_I \ge 0} V(0, q_I) - T(0, q_I).$$
(4)

The reservation utility V_B^0 , which depends on the price schedule by (4), is endogenous but independent from ω_E . The surplus created by the buyer and the rival firm can thus be written as

$$\Delta S_{BE} = S_{BE} - V_B^0. \tag{5}$$

Denoting by $\beta \in (0, 1)$ the competitor's bargaining power vis-à-vis the buyer, we derive the competitor's and buyer's profits:

$$\Pi_E = \beta \quad \Delta S_{BE} \Pi_B = (1 - \beta) \quad \Delta S_{BE} + V_B^0.$$
(6)

If $\beta = 0$, the competitor has no bargaining power and may be seen as a competitive fringe from which the buyer can purchase any quantity at price c_E . On the contrary, the case $\beta = 1$ happens when the competitor has all the bargaining power vis-à-vis the buyer.

Perfect information Marx and Shaffer (2004) have shown that quantities are efficient under perfect information. When the incumbent can make an exclusivity offer to the buyer, all the surplus from the rival can be extracted by adjusting the level of that offer in such a way that the surplus created by the rival, ΔS_{BE} , is zero. The situation is subtler when the sole instrument available to the buyer and the incumbent is a non-conditional schedule $T(q_I)$. In our terminology, the result can be expressed as follows: full extraction occurs if and only if the rival is not super-efficient, see Section 7.

⁵It would be extremely counter-intuitive that the buyer and the incumbent use their pricing instrument, e.g. $T(q_E, q_I)$, to encourage production and disposal of the rival good. The following analysis finds no force pushing in that direction. A formal proof is available upon request.

Virtual surplus We henceforth focus on the situation where the buyer and the incumbent commit to a price-quantity schedule before the uncertainty on the rival good is realized. In this context, the schedule is designed ex ante to maximize the expected joint surplus, equal to the total surplus minus the profit left to the competitor:

$$\mathbb{E}_{c_E, v_E} \Pi_{BI} = \mathbb{E}_{c_E, v_E} \left\{ W(q_E, q_I; c_E, v_E) - \Pi_E \right\},\tag{7}$$

where q_E and q_I are solution to (3) and Π_E is given by (6). The sharing of the expected joint surplus between the buyer and the incumbent, and hence the respective bargaining power of each party, play no role in the following analysis.⁶

As all purchased units of rival good are consumed, the surplus (3) depends on the uncertain cost and preference parameters c_E and v_E only through the difference $\omega_E = v_E - c_E$. The surplus S_{BE} is a convex function of ω_E because it is the upper bound of a family of functions that are affine in ω_E ; hence S_{BE} is almost everywhere differentiable in ω_E . By the envelope theorem, the rent left to the rival satisfies:

$$\frac{\partial \Pi_E}{\partial \omega_E} = \beta \frac{\partial \Delta S_{BE}}{\partial \omega_E} = \beta q_E(\omega_E). \tag{8}$$

Integrating by parts, we get

$$\int_{\underline{\omega}_E}^{\overline{\omega}_E} \Pi_E(\omega_E) f(\omega_E) \, \mathrm{d}\omega_E = \Pi_E(\underline{\omega}_E) + \beta \int_{\underline{\omega}_E}^{\overline{\omega}_E} q_E(\omega_E) [1 - F(\omega_E)] \, \mathrm{d}\omega_E.$$

Substituting in (7), we rewrite the buyer-incumbent objective as

$$\mathbb{E}_{\omega_E} \Pi_{BI} = \mathbb{E}_{\omega_E} S^{\mathsf{v}}(q_E, q_I; \omega_E) - \Pi_E(\underline{\omega}_E), \tag{9}$$

where, following Jullien (2000), we have defined the "virtual surplus" S^{v} as

$$S^{\mathsf{v}}(q_E, q_I; \omega_E) = W(q_E, q_I; \omega_E) - \beta q_E \frac{1 - F(\omega_E)}{f(\omega_E)}.$$
(10)

The virtual surplus is the total surplus $W(q_E, q_I; \omega_E)$ adjusted for the informational rents $\beta q_E (1 - F(\omega_E)) / f(\omega_E)$ induced by the self-selection constraints.

Buyer opportunism Expression (7) reflects a standard rent-extraction tradeoff. From the ex ante perspective, the tariff has two purposes: on the one hand, maximizing the expected welfare W; on the other, making $\Pi_E = \beta \Delta S_{BE}$ as small as possible. Rent extraction is obtained

⁶Figueroa, Ide, and Montero (2014) restrict the ability of the buyer and the incumbent to share rents through transfers and explore the implications for inefficient exclusion in a model with inelastic demand and one-dimensional uncertainty.

by placing competitive pressure on the rival firm, i.e., granting the buyer low marginal price to force the rival to match these rebates, which may drive the rival out of the market or distort downwards the quantity it sells, $q_E < q_E^{**}$.

The novelty in our analysis lies in the possible distortion of q_I . We call buyer opportunism the fact that the buyer purchases too many units of incumbent good given her supply from the rival, formally $q_I > q_I^*(q_E; \omega_I)$. We show below that buyer opportunism is observed in equilibrium except when the buyer and the incumbent firm have the most powerful instrument $T(q_E, q_I)$ at their disposal. Granting rebates to the buyer induces her to distort the quantity purchased from the dominant firm upwards. The buyer indeed wants to pocket the rebates and does not internalize the production cost c_I when she purchases from the dominant firm.

Purchasing and throwing away units of incumbent good would constitute an extreme form of buyer opportunism. We show that this form is never part of an equilibrium. On the contrary, we find that the possibility of disposing of units of good I alters the terms of the rent-extraction tradeoff and limits the exclusionary effects of nonlinear pricing.

3 Conditional price-quantity schedules

For each type of pricing instrument, we proceed as follows. First, we derive necessary conditions for a quantity allocation $(q_E(\omega_E), q_I(\omega_E))$ to be achieved with the considered type of price-quantity schedule. Second, we maximize the virtual surplus under those necessary conditions. Third, we check that the found allocation can indeed be implemented.

We start with conditional schedules $T(q_E, q_I)$. As regards implementability, we simply observe that the quantity of rival good q_E is a nondecreasing function of ω_E . This follows from the convexity of the surplus function $S_{BE}(\omega_E)$, combined to the envelope condition (8).

Maximization of the virtual surplus The maximum of the virtual surplus (10) is achieved in the no-disposal region. At the optimum, the quantity of good I is conditionally efficient, $q_I = q_I^*(q_E; \omega_I)$. More precisely, for each ω_E , the virtual surplus S^v is maximal at (q_E^c, q_I^c) such that

$$\omega_E - \frac{\partial h}{\partial q_E}(q_E^c, q_I^c) \le \beta \frac{1 - F(\omega_E)}{f(\omega_E)} \quad \text{and} \quad \frac{\partial h}{\partial q_I}(q_E^c, q_I^c) = \omega_I.$$
(11)

with equality in the first inequality when $q_E^c > 0$. In this case, the two conditions can be collapsed into

$$\omega_E - \frac{\partial h}{\partial q_E} (q_E^c, q_I^*(q_E^c; \omega_I)) = \beta \frac{1 - F(\omega_E)}{f(\omega_E)}.$$
(12)

By convexity of h, the function $\partial h/\partial q_E(q_E, q_I^*(q_E))$ increases with q_E , and hence the left-hand side of (12) decreases with q_E^c . Under Assumption 1, the right-hand side is non-increasing

in ω_E . The function $q_E^c(\omega_E)$, therefore, is nondecreasing. Let ω_E^c be defined by

$$\omega_E^c - \beta \frac{1 - F(\omega_E^c)}{f(\omega_E^c)} - \frac{\partial h}{\partial q_E}(0, q_I^*(0; \omega_I)) = 0.$$

The left-hand side of the above equation increases with ω_E^c and is negative for $\omega_E = \omega_E^{**} = \partial h / \partial q_E(0, q_I^*(0; \omega_I))$, hence $\omega_E^c > \omega_E^{**}$.

For $\omega_E > \omega_E^c$, the rival supplies a positive quantity, $q_E^c > 0$, as represented by point Con Figure 2. For ω_E below ω_E^c , the virtual surplus is maximum at the point $(q_E^c, q_I^c) =$ $(0; q_I^*(0; \omega_I))$, i.e., the rival is driven out of the market – the distortion is at the extensive margin. (On Figure 2, the point C would lie on the q_I -axis.) The dashed ellipses centered at C represent the isolines of the virtual surplus.

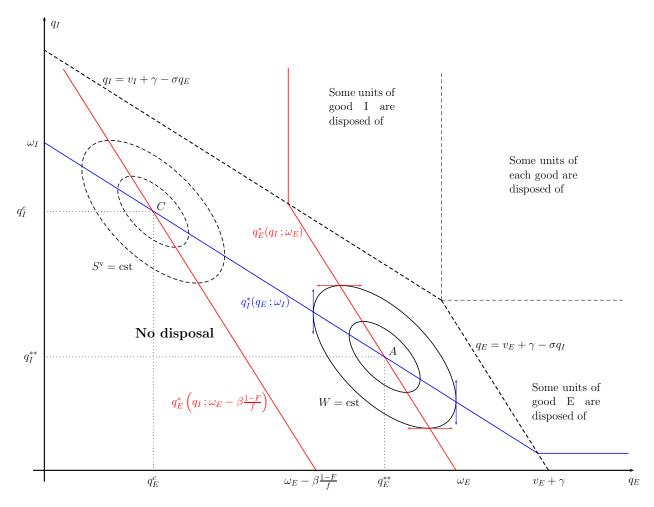


Figure 2: The virtual surplus is maximal at C (quadratic example)

Implementation The quantity allocation $(q_E^c(\omega_E), q_I^c(\omega_E))$ can be represented by a curve in the (q_E, q_I) -space, see Figure 4c for an example. Conditional schedules $T(q_E, q_I)$ are defined on the whole space $q_E \ge 0, q_I \ge 0$. Considering perturbations of T far away from the quantity allocation shows that many schedules $T(q_E, q_I)$ yield the same allocation. Yet there are necessary conditions for implementation. We have seen that the surplus

$$S_{BE}(\omega_E) = \omega_E q_E^c(\omega_E) + v_I q_I^c(\omega_E) - h(q_E^c(\omega_E), q_I^c(\omega_E)) - T(q_E^c(\omega_E), q_I^c(\omega_E))$$

is almost everywhere differentiable in ω_E , with its derivative being $q_E^c(\omega_E)$. It follows that Tis differentiable along the quantity allocation, but in general it need not be differentiable with respect to (q_E, q_I) . The simplest way to implement the allocation $(q_E^c(\omega_E), q_I^c(\omega_E))$ is a twopart tariff of the form $T(q_E, q_I) = c_I q_I + P(q_E)$. In this case, the right-hand side depends on ω_E through $q_E^c(\omega_E)$ but not through $q_I^c(\omega_E) = q_I^*(q_E^c(\omega_E))$ by definition of q_I^* . It follows that the function P is differentiable. Differentiating with respect to ω_E and simplifying by $dq_E^c/d\omega_E$ in the region where q_E^c is increasing, we get $\omega_E - \partial h/\partial q_E = P'(q_E^c(\omega_E))$, where the partial derivative is evaluated at $(q_E^c(\omega_E), q_I^c(\omega_E))$. Combining with (12), we find

$$P'(q_E^c(\omega_E)) = \beta \frac{1 - F(\omega_E)}{f(\omega_E)}.$$
(13)

We check in Appendix A that such a two-part tariff indeed implements the allocation (q_E^c, q_I^c) .

Proposition 1. The following properties hold at the second-best optimum with a conditional price-quantity schedule:

- 1. For any level of rival's surplus ω_E but $\overline{\omega}_E$, the quantity purchased from the rival, q_E^c , is distorted downwards relative to q_E^{**} . Exclusion is complete for $\omega_E \leq \omega_E^c$, where $\omega_E^c > \omega_E^{**}$.
- 2. The quantity purchased from the incumbent firm, $q_I^c = q_I^*(q_E^c; \omega_E)$, is efficient given q_E^c but distorted upwards relative to q_I^{**} .
- 3. The magnitude of the disposal costs, γ_I , does not affect the buyer's supply policy or the price quantity schedule $T(q_E, q_I)$.
- 4. The buyer and the incumbent firm may agree on a price schedule that is linear in q_I with slope c_I and nondecreasing and concave in q_E .

Letting the price of the incumbent good depend on the quantity purchased from the rival allows the buyer and the incumbent to neutralize buyer ex post opportunism, i.e., to make sure that the quantity of incumbent good is efficient given the quantity supplied from the rival. Conditional efficiency imposes that the partial derivative of T with respect to q_I is c_I at the second-best allocation. This condition is hard to meet when the price schedule T depends on the market share $q_I/(q_E + q_I)$ rather than directly on q_E , because the market share is nonlinear in q_I . Market-share discounts, for this reason, appear as a less convenient way to implement the second-best allocation than two-part tariffs of the form $c_I q_I + P(q_E)$. Proposition 1 builds a bridge between the literatures on market foreclosure and nonlinear pricing. As in Aghion and Bolton (1987), the buyer and the incumbent jointly act like a monopoly towards the rival, setting $P(q_E)$ to extract rent at the cost of reducing the extent of entry: $q_E < q_E^{**}$, which yields inefficient market foreclosure. The efficiency-rent tradeoff leads to more inefficient exclusion as the rival's bargaining power, β , rises. When β is high, the rival has a strong bargaining power vis-à-vis the buyer, which makes rent extraction a more serious issue and pushes towards reducing q_E .

Aghion and Bolton (1987) assume that the buyer's demand was supplied entirely by a single supplier. Hence they interpret the difference P(1) - P(0) as a penalty for breach of contract. In contrast, we allow the buyer to split her purchase requirements between the two suppliers and find that inefficient foreclosure may be complete or partial: $0 \le q_E < q_E^{**}$. We interpret the difference $P(q_E) - P(0)$ as rebates lost when supplying from the competitor. The presence of these rebates implies a form of below-cost pricing. Specifically, when $q_E > 0$, the average incremental price of the "last" units of good I (units between $q_I^*(q_E; \omega_I)$ and $q_I^*(0; \omega_I)$) is lower than the production cost:

$$\frac{T(0, q_I^*(0; \omega_I)) - T(q_E, q_I^*(q_E; \omega_I))}{q_I^*(0; \omega_I) - q_I^*(q_E; \omega_I)} = c_I - \frac{P(q_E) - P(0)}{q_I^*(0; \omega_I) - q_I^*(q_E; \omega_I)} < c_I$$

because the penalty function is increasing, $P(q_E) > P(0)$, and the function q_I^* is decreasing, $q_I^*(0; \omega_I) > q_I^*(q_E; \omega_I)$. The above price-cost comparison is reminiscent of the "as-efficient competitor test". The precise form of the test advocated by the European Commission, which involves the notion of contestable demand, is more accurately described in a model with inelastic demand (see our companion paper, Choné and Linnemer (2014)).

Quadratic example With $h(q_E, q_I; s_E) = q_E^2/2 + q_I^2/2 + \sigma q_E q_I$, the second-best quantities purchased from both suppliers under a conditional tariff are given by

$$q_E^c(\omega_E) = \max\left(\omega_E - \beta \frac{1 - F(\omega_E)}{f(\omega_E)} - \sigma q_I^c, 0\right) \text{ and } q_I^c(\omega_E) = q_I^*(q_E^c),$$

The quantity purchased from the incumbent is conditionally efficient while that purchased from the rival is distorted downwards. We get the allocation that would be efficient if the rival's efficiency index ω_E were artificially reduced by $\beta(1 - F(\omega_E))/f(\omega_E)$:

$$q_E^c(\omega_E) = q_E^{**}\left(\omega_E - \beta \frac{1 - F(\omega_E)}{f(\omega_E)}\right), q_I^c(\omega_E) = q_I^{**}\left(\omega_E - \beta \frac{1 - F(\omega_E)}{f(\omega_E)}\right)$$

where the efficient quantities q_E^{**} and q_I^{**} are given by (2). When ω_E is uniformly distributed over the interval $[\underline{\omega}_E, \overline{\omega}_E]$, the penalty function is quadratic, with its derivative being given by

$$P'(q_E) = \frac{\beta}{1+\beta} \left[q_E^{**}(\overline{\omega}_E) - q_E \right].$$

In the limit case where the demands for the two goods are independent ($\sigma = 0$), the penalty is given by the formula above with $q_E^{**}(\overline{\omega}_E) = \overline{\omega}_E$, and hence is increasing in q_E . Rent-shifting appears here as pure extortion, and we now turn to more realistic price instruments.

4 Non-conditional price-quantity schedules

The analysis is more involved when the price schedule cannot freely depend on the quantity purchased from the rival, because buyer opportunism will materialize at the second-best allocation and the degree of buyer opportunism will depend on the magnitude of the disposal costs. To simplify the presentation, in this and the next section, we assume that the buyer must consume the all the purchased units, $\gamma_E = \gamma_I = +\infty$, and hence $V(q_E, q_I) = v_E q_E + v_I q_I - h(q_E, q_I)$. The effect of disposal costs is examined Section 6.

Implementable quantity functions We now suppose that the buyer and the dominant firm are constrained to use a schedule of the form $T(q_I)$. As the schedule does not depend on q_E , the buyer and the rival trade the efficient quantity of good E given q_I , $q_E = q_E^*(q_I; \omega_E)$. Following Martimort and Stole (2009), we think of the buyer and rival joint utility as a function of the quantity purchased from the incumbent:

$$\tilde{S}_{BE}(q_I;\omega_E) = \max_{q_E \ge 0} v_I q_I + \omega_E q_E - h(q_E, q_I) = v_I q_I + \omega_E q_E^*(q_I;\omega_E) - h(q_E^*(q_I;\omega_E), q_I).$$

The function \tilde{S}_{BE} is concave in q_I as the marginal utility

$$\frac{\partial S_{BE}}{\partial q_I} = v_I - \frac{\partial h}{\partial q_I} (q_E^*(q_I; \omega_E), q_I)$$
(14)

decreases in q_I by convexity of h. It is nondecreasing in ω_E with derivative $q_E^*(q_I; \omega_E)$, and satisfies the single-crossing property:

$$\frac{\partial^2 \tilde{S}_{BE}}{\partial q_I \partial \omega_E} = \frac{\partial}{\partial q_I} \left(\frac{\partial \tilde{S}_{BE}}{\partial \omega_E} \right) = \frac{\partial q_E^*}{\partial q_I} \le 0$$
(15)

by substitutability of the two goods: the buyer and rival marginal utility for good I decreases with ω_E . For non super-efficient rival types, the isolines of \tilde{S}_{BE} coincide with those of $v_Iq_I - h(0, q_I)$ for large values of q_I , namely in the region where $q_E^*(q_I; \omega_E) = 0$; in this region, the marginal joint utility (14) does not depend on ω_E , and the Spence-Mirrlees inequality (15) is in fact an equality.

The chosen quantity of incumbent good, $q_I(\omega_E)$, is solution to

$$S_{BE}(\omega_E) = \max_{q_I \ge 0} \tilde{S}_{BE}(q_I; \omega_E) - T(q_I), \tag{16}$$

for some price schedule $T(q_I)$. Adapting usual arguments, we find that a quantity allocation $(q_E(\omega_E), q_I(\omega_E))$ is implementable under a non-conditional schedule if and only if the two conditions are satisfied: (i) $q_E = q_E^*(q_I; \omega_E)$; (ii) q_I is decreasing in ω_E where $q_E > 0$ and constant in ω_E where $q_E = 0$.

Constrained maximization of the virtual surplus We now maximize the virtual surplus under the two constraints listed above, namely $q_E = q_E^*(q_I; \omega_E)$ and q_I non-increasing in ω_E . To account for the former constraint, we define the constrained virtual surplus as

$$\hat{S}^{\mathsf{v}}(q_I;\omega_E) = S^{\mathsf{v}}(q_E^*(q_I;\omega_E), q_I;\omega_E).$$

Then we maximize the constrained surplus subject to the monotonicity requirement imposed on the function $q_I(\omega_E)$. Following Martimort and Stole (2009)'s approach in multi-principal games, we make the following regularity assumption:

Assumption 2. The constrained virtual surplus $\tilde{S}^{v}(q_{I}; \omega_{E})$ is strictly quasi-concave in q_{I} and has strict decreasing differences with respect to q_{I} and ω_{E} where $q_{E}^{*}(q_{I}; \omega_{E}) > 0$.

Before proceeding to the maximization, we comment on the two conditions stated in Assumption 2. The concavity condition is equivalent to the following function being decreasing in q_I :

$$\frac{\partial \tilde{S}^{v}(q_{I};\omega_{E})}{\partial q_{I}} = \omega_{I} - \frac{\partial h}{\partial q_{I}}(q_{E}^{*}(q_{I};\omega_{E}),q_{I}) - \beta \frac{1 - F(\omega_{E})}{f(\omega_{E})} \frac{\partial q_{E}^{*}(q_{I};\omega_{E})}{\partial q_{I}}.$$
(17)

The second term of the right-hand side is indeed decreasing in q_I by convexity of h, which tends to make the virtual surplus concave in q_I . The last term involves the slope of the conditionally efficient quantity, $\partial q_E^*/\partial q_I$. In the quadratic example, that slope is $-\sigma$, and hence the virtual surplus is concave. In general, however, the slope is equal to a ratio of second-order derivatives of h whose variations with q_I depend on properties of third-order derivatives of h.⁷

The second part of Assumption 2 is equivalent to the partial derivative $\partial \tilde{S}^{v}(q_{I};\omega_{E})/\partial q_{I}$ being decreasing in ω_{E} . By substitutability, the second term at the right-hand side of (17) is decreasing in ω_{E} when $q_{E}^{*} > 0$ and constant when $q_{E}^{*} = 0$. The last term has two factors: by Assumption 1 the hazard rate f/(1-F) also tends to make $\partial \tilde{S}^{v}/\partial q_{I}$ decrease with ω_{E} (recall that $\partial q_{E}^{*}/\partial q_{I}$ is negative). The contribution of the last factor, however, is ambiguous as we do not know how the slope of the conditionally efficient quantity, $\partial q_{E}^{*}/\partial q_{I}$, varies with ω_{E} . In the quadratic case, the slope is constant and the first two forces yield the desired property.

⁷The derivative of q_E^* with respect to q_I is $-\left(\partial^2 h/\partial q_E \partial q_I\right) / \left(\partial^2 h/\partial q_E^2\right)$ evaluated at $(q_E^*(q_I;\omega_E),q_I)$.

Lemma 1. Let $(\hat{q}_E^u, \hat{q}_I^u)$ denote the quantity allocation that maximizes the constrained virtual surplus for each value of ω_E . There exists $\hat{\omega}_E^u$ in $(\underline{\omega}_E, \overline{\omega}_E)$ such that $(\hat{q}_E^u, \hat{q}_I^u)$ satisfies

$$\omega_I - \frac{\partial h}{\partial q_I}(\hat{q}_E^u, \hat{q}_I^u) = \beta \frac{1 - F(\omega_E)}{f(\omega_E)} \frac{\partial q_E^*}{\partial q_I} \quad and \quad \omega_E - \frac{\partial h}{\partial q_E}(\hat{q}_E^u, \hat{q}_I^u) = 0, \tag{18}$$

for $\omega_E \geq \hat{\omega}_E^u$ and $\hat{q}_E^u = q_E^*(\hat{q}_I^u; \omega_E) = 0$ for $\omega_E \leq \hat{\omega}_E^u$. The quantity \hat{q}_I^u decreases (increases) with ω_E above (below) $\hat{\omega}_E^u$.

Proof. Under Assumption 2, the virtual surplus is concave and hence its maximum is determined by the first-order conditions. These conditions are given by (18) when $\hat{q}_E^u > 0$. The second part of Assumption 2 guarantees that \hat{q}_I^u decreases with ω_E as long as $\hat{q}_E^u > 0$. It follows that $\hat{q}_E^u = q_E^*(\hat{q}_I^u; \omega_E)$ increases with ω_E in this region.

The existence of the threshold $\hat{\omega}_E^u$ follows from the assumption that $q_E^{**}(\omega_E^{**}) = 0 < q_E^{**}(\overline{\omega}_E)$ and the observation that q_E^u is equal to (lower than or equal to) q_E^{**} at $\overline{\omega}_E$ (at ω_E^{**}). Below that threshold, the maximum of the constrained virtual surplus is achieved at a point where $q_E^u = 0$ and the value of \hat{q}_I^u is determined by conditional efficiency, i.e., by the condition $0 = q_E^*(\hat{q}_I^u; \omega_E)$, implying that \hat{q}_I^u is increasing in ω_E in this region.

Figure 3 shows a situation in the quadratic example where the maximum of the constrained virtual surplus is achieved at a point where $q_E > 0$, i.e., the represented case corresponds to a value of ω_E higher than $\hat{\omega}_E^u$. For ω_E lower than that threshold, the point U lies on the vertical q_I -axis. The non-monotonicity of \hat{q}_I^u is apparent on Figure 4b, see the thin dotted line.

Lemma 1 shows that the pointwise maximization of the constrained virtual surplus yields a quantity of incumbent good that is not monotonic and hence not implementable. There must therefore be bunching at the bottom of the distribution of ω_E . The next proposition characterizes the optimal quantity allocation (q_E^u, q_I^u) under a non-conditional schedule.

Proposition 2. Under Assumption 2, the optimal quantities implementable with a nonconditional schedule $T(q_I)$ satisfy the following properties:

- 1. There exists $\tilde{\omega}_E^u$ in $(\underline{\omega}_E, \overline{\omega}_E)$ such that $q_I^u(\omega_E)$ is constant up to $\tilde{\omega}_E^u$ and then equal to $\hat{q}_I^u(\omega_E)$.
- 2. The quantity purchased from the rival is efficient given q_I^u , $q_E^u = q_E^*(q_I^u; \omega_E)$, and distorted downwards relative to q_E^{**} for all $\omega_E < \overline{\omega}_E$. Exclusion is complete for $\omega_E \le \omega_E^u$, with $\omega_E^{**} < \omega_E^u < \widetilde{\omega}_E^u$.
- 3. The quantity purchased from the dominant firm is distorted upwards relative to the conditionally efficient quantity, $q_I^u > q_I^*(q_E; \omega_I)$ ("buyer opportunism") for all $\omega_E < \overline{\omega}_E$.

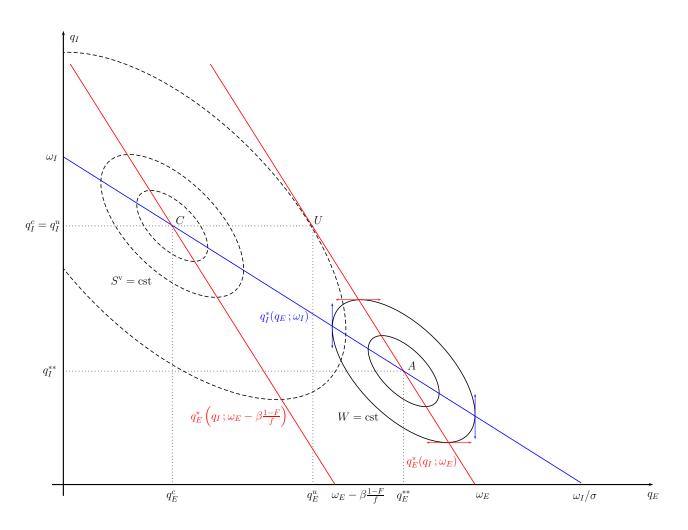


Figure 3: The constrained virtual surplus is maximal at U (quadratic example)

Proof. The condition that determines the bunching threshold $\tilde{\omega}_E^u$ is

$$\int_{\underline{\omega}_E}^{\tilde{\omega}_E^u} \frac{\partial}{\partial q_I} \tilde{S}^{\mathbf{v}}(\bar{q}_I; \omega_E) \,\mathrm{d}F(\omega_E) = 0, \tag{19}$$

where $\bar{q}_I = \hat{q}_I^u(\tilde{\omega}_E^u)$ is the constant value of q_I over the interval $[\underline{\omega}_E, \tilde{\omega}_E^u]$, see Figure 4b. The derivative of the constrained virtual surplus $\partial \tilde{S}^v / \partial q_I$ depends on whether q_E is positive or zero. Let ω_E^u be defined by $q_E^*(\bar{q}_I; \omega_E^u) = 0$. For $\omega_E < \omega_E^u$, $q_E^u = 0$, the derivative of the constrained virtual surplus is $w_I - \partial h / \partial q_I(0, \bar{q}_I)$, which is negative because \bar{q}_I is above $\hat{q}_I^u(\omega_E)$. For $\omega_E^u < \omega_E^u < \tilde{\omega}_E^u$, $q_E^u > 0$, the derivative features the additional (positive) term $-\beta(1-F)/f\partial q_E^*/\partial q_I$; in this region it is positive because \bar{q}_I is below $\hat{q}_I^u(\omega_E)$. The threshold $\tilde{\omega}_E^u$ is such that the positive and negative contributions offset each other.

The quantity purchased from the rival is undistorted for $\omega_E = \overline{\omega}_E$ and is zero below a threshold ω_E^u that is strictly larger than ω_E^{**} . The quantity purchased from the dominant firm, being distorted upwards relative to $q_I^*(q_E; \omega_I)$, is a fortiori distorted upwards relative to q_I^{**} . In particular, $q_I^u(\omega_E)$ is above $q_I^*(0; \omega_I)$ for low values of ω_E . This can be seen on Figure 4c where the "trajectories" of the quantity pairs (q_E, q_I) are represented in various regimes. We see that q_I is efficient conditionally on q_E at the first-best allocation as well as under a conditional price-quantity schedule. In contrast, inefficiently many units of incumbent good given rival supply are purchased under a non-conditional schedule.

Shape of the price-quantity schedule Under Assumption 2 and assuming furthermore that h is twice continuously differentiable, $q_I^u = \hat{q}_I^u$ is differentiable outside the bunching region, i.e., for $\omega_E > \tilde{\omega}_E^u$, and its derivative is positive in that region. Now we observe that the surplus function $S_{BE}(\omega_E) = v_I q_I + \omega_E q_E^* - h(q_E^*, q_I) - T(q_I)$ is convex and hence differentiable at almost every value of ω_E . It follows that the price schedule T is almost everywhere differentiable over the range of $q_I^u(\omega_E)$. Differentiating S_{BE} and simplifying by $dq_I^u/d\omega_E$, we get $v_I - \partial h/\partial q_I(q_E^*, q_I) = T'(q_I)$, which, combined with (18), yields

$$T'(q_I^u(\omega_E)) = c_I + \beta \frac{1 - F(\omega_E)}{f(\omega_E)} \frac{\partial q_E^*}{\partial q_I} < c_I,$$
(20)

where the slope $\partial q_E^*/\partial q_I$ is evaluated at $(q_I^u(\omega_E); \omega_E)$. The monotonicity of the hazard rate tends to make the schedule concave in q_I . Indeed, as ω_E rises, the quantity q_I^u falls and the hazard rate pushes the the right-hand side of (20) upwards because $\partial q_E^*/\partial q_I$ is negative. There is, however, the additional effect that the derivative $\partial q_E^*/\partial q_I$ can itself move with ω_E ; this effect is absent in the quadratic case where the derivative is constant. The following proposition presents sufficient conditions (derived from (20)) for the price schedule to be concave below the maximum quantity purchased from the incumbent, \bar{q}_I , given by (19).

Proposition 3. Suppose that the slope of the conditionally efficient quantity, $\partial q_E^*/\partial q_I$, is nonincreasing (nondecreasing) in q_I (resp. ω_E). Then the optimal non-conditional price-quantity schedule $T(q_I)$ is concave in q_I up to \bar{q}_I and has a convex kink at this point.

The shape of the optimal non-conditional schedule is shown on Figure 5. The convex kink at \bar{q}_I is due to complete exclusion and the associated bunching phenomenon at the bottom of the distribution. Indeed, the slope of the price schedule at the left of \bar{q}_I is equal to the marginal rate of substitution for $v_I - \partial h/\partial q_I$ evaluated at $(q_E^*(\bar{q}_I; \tilde{\omega}_E^u), \bar{q}_I)$. This rate is higher for the agents with lower type, and is the highest for $\omega_E = \underline{\omega}_E$, because these types value the rival good less, and hence the incumbent good more. To prevent these agents from purchasing more than \bar{q}_I , the price schedule must lie above the iso-utility curve of the lowest type, hence a the convex kink. To be specific, the right derivative of the schedule at \bar{q}_I must be greater than $v_I - \partial h/\partial q_I$ evaluated at $(0, \bar{q}_I)$.⁸

⁸The bunching at the bottom of the distribution of ω_E , and the corresponding non-concavity of $T(q_I)$ at \bar{q}_I ,

In the limit case of two independent markets, the conditionally efficient quantity of rival good, q_E^* , does not depend on q_I , and Lemma 2 and Proposition 2 show that both quantities are fully efficient at the second-best allocation. In particular, the quantity of incumbent good does not vary with the rival's efficiency index ω_E , so the range of $q_I^u(\omega_E)$ is the singleton $\{q_I^{**}\}$, which makes the above analysis inoperative. Here we see directly that $T' = c_I$ is necessary to induce efficiency.

Quadratic example When the buyer's utility is quadratic, the second-best quantities under a non-conditional schedule are given in the no-bunching region, i.e., for $\omega_E > \tilde{\omega}_E^u$, by

$$q_E^u(\omega_E) = q_E^*(q_I^u;\omega_E)$$
 and $q_I^u(\omega_E) = \omega_I + \sigma\beta \frac{1 - F(\omega_E)}{f(\omega_E)} - \sigma q_E^u(\omega_E)$

which yields

$$q_E^u(\omega_E) = q_E^{**}(\omega_E) - \beta \frac{\sigma^2}{1 - \sigma^2} \frac{1 - F(\omega_E)}{f(\omega_E)} \quad \text{and} \quad q_I^u(\omega_E) = q_I^{**}(\omega_E) + \beta \frac{\sigma}{1 - \sigma^2} \frac{1 - F(\omega_E)}{f(\omega_E)}$$

When the distribution is uniform, the bunching condition (19) can be rewritten as:

$$(\omega_I - \bar{q}_I)(\omega_E^u - \underline{\omega}_E) + \int_{\omega_E^u}^{\bar{\omega}_E^u} \left[\omega_I - (1 - \sigma^2)\bar{q}_I - \sigma\omega_E + \beta\sigma(\overline{\omega}_E - \omega_E) \right] \, \mathrm{d}\omega_E = 0, \tag{21}$$

with $\omega_E^u = \sigma \bar{q}_I$ and q_I^u continuous at $\tilde{\omega}_E^u$. The quantities are represented as a function of ω_E on Figures 4a and 4b.

As already observed, the sufficient conditions of Proposition 3, that guarantee the concavity of the price schedule, are satisfied when the buyer's utility is quadratic. To illustrate, we compute the curvature of the schedule when the distribution of ω_E is uniform. Observing that $(1-F)/f = \overline{\omega}_E - \omega_E$ and combining (20) with the expression of $q_I^u(\omega_E)$, we find that the first derivative of the schedule is linear in q_I :

$$T'(q_I) = c_I - \frac{\beta}{1+\beta} (1-\sigma^2) \left[q_I - q_I^{**}(\overline{\omega}_E) \right] < c_I$$

for all q_I between $q_I^u(\overline{\omega}_E)$ and \overline{q}_I ; the schedule is quadratic (and concave) in this region.

5 Exclusivity offer

In this section, we investigate the situation where the price of the incumbent good can be conditioned on the rival supply only through the events $q_E = 0$ and $q_E > 0$. This situation is somewhat intermediary between conditional and non-conditional schedules.

are present because $\hat{q}_E^u(\omega_E) = 0$ for low values of ω_E . This is due in particular to our assumption that q_E^{**} is zero at the bottom of the distribution ($\omega_E^{**} > \underline{\omega}_E$, see Assumption 1). We would have no bunching and a globally concave schedule if $q_E^*(q_I; \omega_E)$ were positive for all q_I and ω_E .

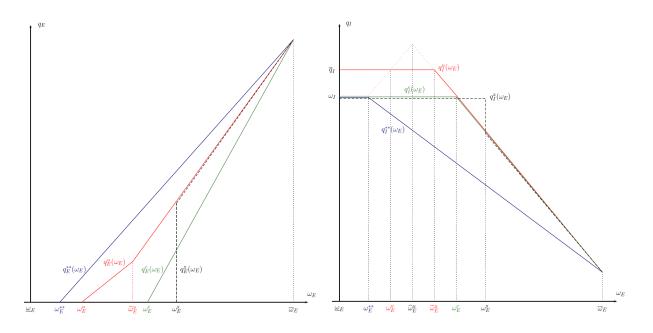


Figure 4a: Equilibrium quantities of good E under each type of price schedule

Figure 4b: Equilibrium quantities of good I under each type of price schedule

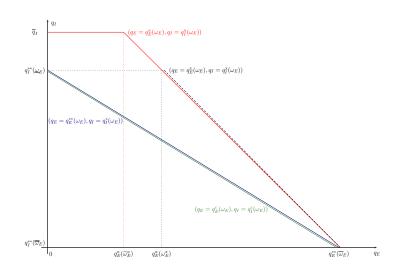


Figure 4c: Buyer opportunism in regimes u and x: q_I is above $q_I^*(q_E; \omega_I)$

Let $(T(q_I), T^*(q_I))$ be an exclusivity price scheme constituted of a pair of non-conditional schedules, where T^* is available to the buyer only if she supplies exclusively from the dominant firm. Under such a scheme, the buyer and the rival, should they settle on a positive quantity, choose $q_E = q_E^*(q_I; \omega_E)$ and q_I solution to (16). If they fail to find such an agreement, the buyer earns

$$S^{\mathbf{x}} = v_I q_I - h(0, q_I) - T^{\mathbf{x}}(q_I),$$

which does not depend on ω_E . It follows that the price schedule T^x consists in fact of a single price-quantity pair. The only difference with the non-conditional situation studied in Section 4 is the availability of an independent instrument to control the outside option.

Proposition 4. There exists a threshold ω_E^x such that the quantities purchased by the buyer under an exclusivity scheme satisfy $(q_E^x, q_I^x) = (0, q_I^*(0))$ for $\omega_E \leq \omega_E^x$ and $(q_E^x, q_I^x) = (q_E^u, q_I^u)$ for $\omega_E \geq \omega_E^x$.

Proof. Maximizing the virtual surplus under the constraint $q_E = 0$ yields the conditionally efficient quantity of incumbent good, $q_I^*(0; \omega_I)$. If $q_E > 0$, we maximize as above the constrained virtual surplus to account for the constraint $q_E = q_E^*(q_I; \omega_E)$. The virtual surplus is $S^{v}(0, q_I^*(0; \omega_I)) = W(0, q_I^*(0; \omega_I))$ in the former situation, $\max_{q_I} S^{v}(q_E^*(q_I; \omega_E), q_I; \omega_E)$ in the latter. Let ω_E^x be the type for which the buyer and the incumbent are ex ante indifferent between these alternatives:

$$\max_{q_I} S^{v}(q_E^*(q_I; \omega_E^{x}), q_I; \omega_E^{x}) = W(0, q_I^*(0; \omega_I)).$$
(22)

Since $\max_{q_I} S^{v}(q_E^*(q_I; \omega_E), q_I; \omega_E)$ increases with ω_E , the quantity allocation (q_E^x, q_I^x) defined in the statement of the proposition maximizes the virtual surplus.

We now explain how to implement this allocation with a pair $(T, T^{\mathbf{x}})$. Regarding T, we use the same schedule as in Section 4. We define $T^{\mathbf{x}}$ as a two-part tariff with slope c_I to ensure that $q_I = q_I^*(0; \omega_I)$. The intercept of this tariff, and hence the price $T^{\mathbf{x}}(q_I^*(0; \omega_I))$ associated to the exclusivity offer, is adjusted so that the buyer and the rival, for $\omega_E = \omega_E^{\mathbf{x}}$, are ex post indifferent between $(q_E^u(\omega_E^{\mathbf{x}}), q_I^u(\omega_E^{\mathbf{x}}))$ and $(0, q_I^*(0; \omega_I))$. Then the types above the threshold $\omega_E^{\mathbf{x}}$, who value the incumbent good less than $\omega_E^{\mathbf{x}}$, prefer a non-exclusive arrangement and pick a point in the nonlinear schedule T. In contrast, the types below $\omega_E^{\mathbf{x}}$, who value the incumbent good more than $\omega_E^{\mathbf{x}}$, are attracted by the exclusivity offer. That offer is represented by the point X on Figure 5.

Next, we compare the magnitude of exclusionary effects in the three considered pricing regimes.

Assumption 3. The nonlinear part of the buyer's utility, $h(q_E, q_I)$ satisfies

$$\int_{q_I^0}^{q_I^1} \left[\frac{\partial^2 h}{\partial q_E^2}(q_E, q_I^1) \frac{\partial^2 h}{\partial q_I^2}(q_E, q_I) - \frac{\partial^2 h}{\partial q_E \partial q_I}(q_E, q_I^1) \frac{\partial^2 h}{\partial q_E \partial q_I}(q_E, q_I) \right] \, \mathrm{d}q_I \ge 0$$

for all q_E and $q_I^1 \ge q_I^0$.

Assumption 3 holds for any convex quadratic function because the term under the integral is then constant and nonnegative. If h is a convex function with positive second-order cross

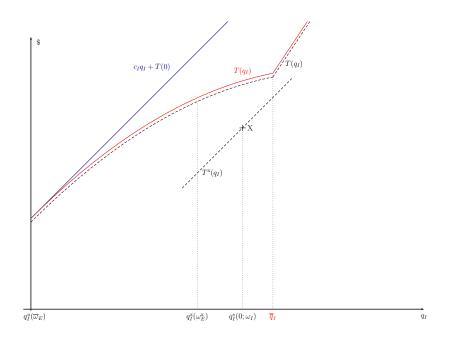


Figure 5: Price-quantity schedules in the three regimes

derivative as assumed in this paper, the assumption is true for instance when $\partial^2 h / \partial q_I^2$ and $\partial^2 h / \partial q_E \partial q_I$ are respectively non-increasing and nondecreasing in q_I .

Recall ω_E^{**} , ω_E^u , ω_E^c and ω_E^x denote the maximum values of ω_E for which the rival is inactive at the first-best optimum and at the second-best optima under respectively a non-conditional schedule $T(q_E, q_I)$, a conditional schedule $T(q_I)$, and an exclusivity price scheme. We refer to these values as the exclusion thresholds in each regime.

Proposition 5. Under Assumption 3, the quantities purchased from the rival firm in each regime are ordered as follows:

$$0 = q_E^{\mathbf{x}}(\omega_E) \le q_E^c(\omega_E) \le q_E^u(\omega_E) < q_E^{**}(\omega_E)$$
(23)

for $\omega_E^{\mathbf{x}} < \omega_E$ and

$$q_E^c(\omega_E) \le q_E^u(\omega_E) = q_E^x(\omega_E) < q_E^{**}(\omega_E)$$
(24)

for $\omega_E > \omega_E^{\mathbf{x}}$. The exclusion thresholds are ordered as follows:

$$\omega_E^{**} \le \omega_E^u \le \omega_E^c \le \omega_E^{\mathbf{x}}.$$
(25)

Proof. The first part of the proposition, relative to the ordering of q_E^c and q_E^u is proved in the appendix. The left two inequalities in (25) follow directly. We now prove the right inequality. From the analysis of Section 3, we have:

$$W(0, q_I^*(0; \omega_I)) = \max_{q_E, q_I} S^{\mathsf{v}}(q_E, q_I; \omega_E^c).$$

Imposing the constraint that q_E must be efficient conditional on q_I reduces the maximum value of the virtual surplus:

$$\max_{q_I} S^{v}(q_E^*(q_I;\omega_E^c), q_I;\omega_E^c) < W(0, q_I^*(0;\omega_I)) = \max_{q_E,q_I} S^{v}(q_E, q_I;\omega_E^c).$$
(26)

The right inequality in (25) follows from the comparison of (22) and (26), combined with the observation that $\max_{q_I} S^{v}(q_E^*(q_I; \omega_E), q_I; \omega_E)$ increases with ω_E .

The above analysis implies that $q_I^c(\omega_E^x) < q_I^c(\omega_E^c) = q_I^*(0;\omega_I)$ and hence the optimal quantity of incumbent good under an exclusivity scheme, q_I^x , admits a downward discontinuity at ω_E^x , see the dashed line on Figure 4b for an illustration.

Quadratic Example For $\omega_E = \omega_E^x$, the buyer and the incumbent are ex ante indifferent between the points $(0, q_I^*(0))$ and the point U on Figure 3. Geometrically, the same isoline of the virtual surplus contains the point $(0, q_I^*(0))$ and the non-conditional second-best allocation denoted by U (the dashed ellipsis passing through $(0, q_I^*(0))$ is tangent to the straight line $q_E = q_E^*(q_I; \omega_E^x)).$

The quantities sold by each suppliers in each of the three regimes are represented on Figures 4a and 4b. A specificity of the quadratic case is that when $q_E > 0$ the quantity of incumbent good is the same under the conditional and non-conditional regimes. (Geometrically the points C and U are on the same horizontal line on Figure 3.) The ordering of q_I across regimes is unclear in general.

Welfare analysis The welfare implications of the three pricing regimes involve two types of distortion. First, the quantity of rival good is distorted downwards, which deteriorates the social welfare. The best regime in this dimension is non-conditional pricing. Second, the quantity of incumbent good may be distorted upwards conditionally on the rival supply. The best regime in this dimension is conditional pricing because it completely eliminates buyer opportunism. In this respect, non-conditional schedules perform badly at the bottom of the distribution because q_I is larger than $q_I^*(0; \omega_I)$ in this region. Exclusivity schemes avoid the latter effect while behaving like unconditional schedules at the top of the distribution; they induce, however, the largest distortions for both goods in an intermediate range of values for the efficiency index ω_E . All these effects are summarized on Figure 6.

In the quadratic case with a uniform distribution, numerical simulations suggest that the non-conditional regime is socially preferred to the conditional and exclusivity regimes and that the exclusivity regime is preferred to the conditional regime for small values of β .

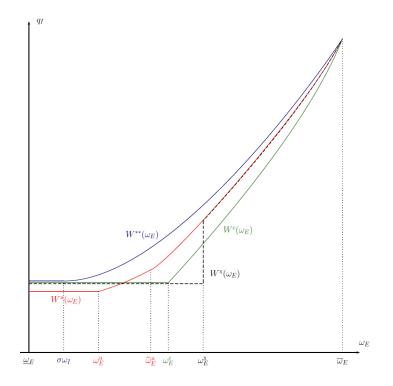


Figure 6: Welfare at the first-best and second-best allocations

6 Disposal costs

We now allow the buyer to dispose of unconsumed units at the unit cost $\gamma_I > -c_I$. We know that the total welfare and the virtual surplus linearly decrease in the region where the buyer indeed does not consume all of the purchased units of incumbent good. As noted in Section 3, the possibility of disposal is of no importance for the analysis of the conditional regime because the virtual surplus attains its maximum in the interior of the no-disposal region for all $\gamma_I > -c_I$.

In contrast, we have seen in Sections 4 and 5 that when the buyer must consume all purchased units ($\gamma_I = \infty$) the second-best allocations under a non-conditional schedule and under an exclusivity scheme are essentially determined by the maximum of the *constrained* virtual surplus, see the characterization of $(\hat{q}_E^u, \hat{q}_I^u)$ in Lemma 1. More precisely, (q_E^u, q_I^u) and (q_E^x, q_I^x) coincide with $(\hat{q}_E^u, \hat{q}_I^u)$ respectively for $\omega_E \ge \tilde{\omega}_E^u$ and for $\omega_E \ge \omega_E^x$, with $\omega_E^x \ge \tilde{\omega}_E^u$. Below these thresholds, the quantities purchased from the incumbent, q_I^u and q_I^x , are constant in ω_E , equal to respectively $\hat{q}_I^u(\tilde{\omega}_E^u)$ and $q_I^*(0;\omega_I)$.

The possibility of disposal does not change the second-best allocations if and only if the solutions found for $\gamma_I = \infty$ remain in the no-disposal region for finite γ_I . This is the case if and only if the buyer is strictly better off consuming all the units purchased than disposing of

some of them:

$$v_I - \frac{\partial h}{\partial q_I}(\hat{q}_E^u(\omega_E), \hat{q}_I^u(\omega_E)) = T'(\hat{q}_I^u(\omega_E)) > -\gamma_I,$$
(27)

for all ω_E greater than $\tilde{\omega}_E^u$ or ω_E^x depending on the considered regime. If this condition is violated, the maximum of the constrained virtual surplus lies on boundary of the no-disposal region. It is then determined as the intersection of that boundary, $v_I - \partial h/\partial q_I(q_E, q_I) = -\gamma_I$, and of the conditionally efficient curve, $q_E = q_E^*(q_I; \omega_E)$. The intersection point is denoted by B^{γ} on Figure 7 for the quadratic example.⁹

Proposition 6. Suppose the assumptions of Proposition 3 hold. Then the second-best allocations under a non-conditional schedule and under an exclusivity scheme do not vary with the magnitude of disposal costs as long as γ_I remains above $-T'(q_I^u(\tilde{\omega}_E^u))$ and $-T'(q_I^u(\omega_E^x))$ respectively. As γ_I falls below these thresholds and tends to $-c_I$, the quantity purchased from the rival and the incumbent respectively increases and decreases, tending to q_E^{**} and q_I^{**} ; the slope of the price schedule tends to c_I ; the welfare rises to its first-best optimum.

Proof. Under the assumptions of Proposition 3, the optimal non-conditional schedule is concave, i.e., $T'(\hat{q}_I^u(\omega_E))$ increases with ω_E . The condition imposed by (27), therefore, is stronger for lower values of ω_E or equivalently higher values of \hat{q}_I^u . If (27) holds for $\omega_E = \tilde{\omega}_E^u$ in the non-conditional regime and for $\omega_E = \omega_E^x$ in the exclusivity regime, it holds for all ω_E above the threshold.

Otherwise, if (27) is violated at the relevant lower bound $(\tilde{\omega}_E^u \text{ or } = \omega_E^x)$, it is violated for all values of ω_E below some threshold. As ω_E falls from this threshold to the lower bound, the maximum of the constrained virtual surplus is first located on the boundary of the no-disposal region (point B^{γ} on Figure 7); at some point, q_E reaches zero (point D^{γ} on Figure 7); for lower values of ω_E , the maximum of the constrained virtual surplus is determined by $q_E = 0$ and $q_E^*(q_I; \omega_E) = 0$. Under the non-conditional regime, the latter phenomenon gives rise to bunching as in Section 4; under an exclusivity scheme, the second-best solution switches to $(0, q_I^*(0; \omega_I))$ before the point D^{γ} is reached.

When γ_I falls to $-c_I$, the boundary of the no-disposal region, $v_I - \partial h/\partial q_I = -\gamma_I$, moves closer to the conditional efficiency line $q_I = q_I^*(q_E; \omega_I)$. On Figure 7, the point B^{γ} tends to the first-best optimum A. At the same time, the slope of the price schedule, $T'(q_I)$, which lies between $-\gamma_I$ and c_I , tends to c_I .

It is ex ante suboptimal for the buyer and the incumbent that some units of incumbent good are produced and disposed of. When the magnitude of the disposal cost is low, the

⁹In this case, the tangency point of the isoline of the virtual surplus (dashed ellipsis) to the straight line $q_E = \omega_E - \sigma q_I$, lies above the boundary of the no-disposal region, $q_I = v_I + \gamma_I - \sigma q_E$.

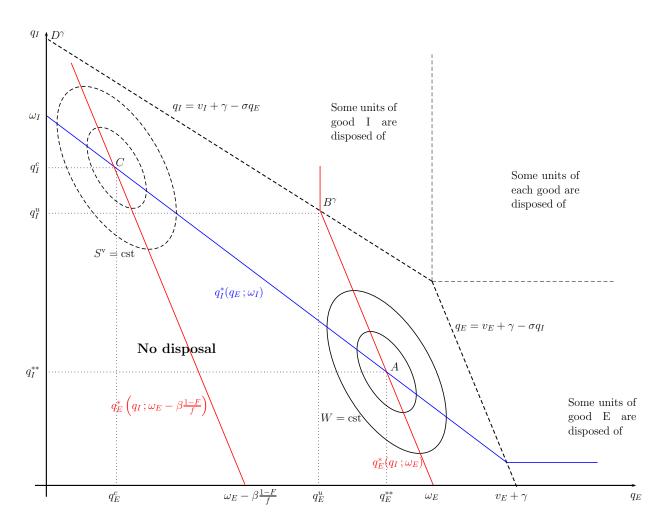


Figure 7: The constrained virtual surplus is maximal at B^{γ}

purchased quantity of incumbent good cannot be too far away from the conditionally efficient quantity, $q_I^*(q_E; \omega_I)$. In other words, the possibility of disposing of unconsumed units of good I reduces the degree of buyer opportunism present at the second-best allocation.

7 Discussion

We now consider a couple of variants in the timing of events and the instruments available to the parties.

First suppose the buyer and the incumbent can wait for the uncertainty to be resolved before deciding on the price-quantity schedule and still enjoy the same commitment power at this point. They can then implement the efficient allocation and extract all the surplus from non super-efficient rival types through a non-conditional price-quantity schedule. Indeed, if \bar{q}_I is such that $q_E^*(\bar{q}_I; \omega_E) = 0$, the following non-conditional schedule yields the first-best outcome: $T(q_I) = c_I q_I + T(0)$ for $q_I < \bar{q}_I$; $T(\bar{q}_I)$ is such that $V(q_E^{**}, q_I^{**}) - c_E q_E^{**} - T(q_I^{**}) =$ $W(q_E^{**}, q_I^{**}) - T(0)$ is slightly above $V(0, \bar{q}_I) - T(\bar{q}_I)$; and $T(q_I) = +\infty$ beyond \bar{q}_I . (The constant T(0) serves to share the surplus $W(q_E^{**}, q_I^{**})$.) It is easy to check that the quantities purchased in equilibrium are q_E^{**} and q_I^{**} . If the rival and the buyer failed to agree on a price and a quantity for good E, the buyer would purchase \bar{q}_I from the incumbent. It follows from the definition of $T(\bar{q}_I)$ that the surplus ΔS_{BE} created by from the trade with the rival is negligible, and the rival profit can be made arbitrarily close to zero.¹⁰ This timing, therefore, would be very favorable to the buyer and the incumbent. In contrast, this paper has assumed that the incumbent and the buyer cannot wait for the resolution of uncertainty and at the same time keep their commitment power.

Next we discuss the perhaps intriguing feature of the model that the buyer is part of two successive coalitions. One might consider an interim stage where the buyer has learnt the characteristics of the rival good but has not yet started negotiating a price and a quantity with the rival. It would then be natural to endow the buyer and the incumbent firm with a more powerful instrument consisting of a menu of price-quantity schedules, $(T(q_I; \hat{\omega}_E))_{\hat{\omega}_E}$, and to consider the following game: (i) the buyer and the incumbent agree on such a menu; (ii) the buyer learns ω_E and announces $\hat{\omega}_E$; (iii) the buyer and the rival negotiate under the price-quantity schedule $T(q_I; \hat{\omega}_E)$. At the interim stage, the buyer pursues her own interest and may therefore try to cheat on the incumbent by manipulating $\hat{\omega}_E$. The menu should be designed to maintain truthfulness.

A fundamental observation is that at the interim stage the buyer is weakly better off colluding with the rival firm on the announcement $\hat{\omega}_E$. In other words, it is in the buyer's interest to agree with the rival not only on the quantities of both goods and the price of the rival good *but also on the announcement*. Indeed, negotiating on all variables under control weakly increases the surplus to be shared with the rival, and hence the part that goes to the buyer. We believe that in practice collusion on the announcement is unavoidable, and for this reason we have not included such an interim stage in our modeling framework.

Suppose, for the sake of the discussion, that the buyer and the rival can be prevented from colluding on the announcement. We now show that if the rival is never super-efficient and has all the bargaining power vis-à-vis the buyer ($\beta = 1$), then there exists a menu of schedules $T(q_I; \hat{\omega}_E)$ that yields the first-best outcome. Let \bar{q}_I be such that $q_E^*(\bar{q}_I; \omega_E) = 0$ for all ω_E . We define $T(q_I; \hat{\omega}_E)$ for each $\hat{\omega}_E$ in the same way as in the complete information case presented above. The only difference with that case is that we choose $T(0; \hat{\omega}_E) =$ $W(q_E^{**}(\hat{\omega}_E), q_I^{**}(\hat{\omega}_E); \hat{\omega}_E) - \bar{V}$, where \bar{V} is a constant. The latter equality ensures that $T(\bar{q}_I; \hat{\omega}_E)$,

¹⁰When the rival is super-efficient, dealing with the rival creates a positive surplus however large q_I becomes. Formally the decreasing function $\beta[V(q_E^*(q_I;\omega_E);q_I) - c_E q_E^*(q_I;\omega_E) - V(0,q_I)]$ remains positive for all q_I . It can be shown that the rival's rent at the second-best optimum is equal to the lower bound of this function.

and hence the buyer's outside option, does not depend on ω_E or $\hat{\omega}_E$. Since $\beta = 1$, the buyer, at the interim stage, gets utility \bar{V} irrespective of her announcement. If we assume that she declares the true value of ω_E to the incumbent, then the first-best allocation obtains.¹¹ Yet, as explained above, the mechanism is not collusion-proof because the rival would like $\hat{\omega}_E$ to be as low as possible and is ready to bribe the buyer in return for such an announcement. Since an arbitrarily small bribe is sufficient to break the buyer's indifference, truthful revelation is unrealistic.

In our companion paper, Choné and Linnemer (2014), we assume that the rival firm cannot compete for the entire buyer's demand. Assuming that the size of the contestable demand is uncertain, we obtain concave price-quantity schedules together with full exclusion (which we do not have here), as well as many other shapes of nonlinear schedules, including retroactive rebates.

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¹¹The problem with $\beta < 1$, under the assumption that the buyer decides on $\hat{\omega}_E$ without colluding with the rival, is open. We only know that the first-best allocation cannot be achieved.

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Appendix

A Implementation with a two-part tariff

We start by introducing a function $P(q_E)$ whose derivative is given by (13) on the interval $[0, q_E^c(\overline{\omega}_E)]$ and is zero above $q_E^c(\overline{\omega}_E)$. The value of P(0) determines the sharing of the surplus between the buyer and the dominant firm. It is straightforward to verify that the function P is globally concave. Moreover, by definition of q_E^c , we have

$$\frac{\partial h}{\partial q_E}(q_E^c(\omega_E), q_I^*(q_E^c(\omega_E))) + P'(q_E^c(\omega_E)) = \omega_E,$$
(28)

for all ω_E between $\underline{\omega}_E$ and $\overline{\omega}_E$. We now check that the function $h(q_E, q_I^*(q_E)) + P(q_E) - \omega_I q_I^*(q_E)$ is convex in q_E . Indeed its derivative at some $q_E = q_E^c(\omega_E)$ in the interval $[0, q_E^c(\overline{\omega}_E)]$ is the left-hand side of (28) and, therefore is increasing with ω_E and q_E . Hence the convexity result.

Under the two-part tariff $T(q_E, q_I) = c_I q_I + P(q_E)$, the buyer and the rival choose the efficient quantity of good I given q_E , $q_I^*(q_E; \omega_I)$. Replacing q_I with $q_I^*(q_E; \omega_E)$ in their common objective (3), we find that the buyer and the rival choose the quantity q_E that maximizes the function $\omega_E q_E + \omega_I q_I^*(q_E) - h(q_I, q_I^*(q_E)) - P(q_E)$. This function is concave in q_E from the above analysis. The quantity of good E, therefore, is determined by the first-order conditions, and is thus $q_E^c(\omega_E)$ for any ω_E .

B Proof of Proposition 5

We first observe that the bunching procedure at the bottom of the distribution leads to increase the quantity of good E, i.e., $q_E^u \ge \hat{q}_E^u$, where \hat{q}_E^u maximizes the constrained virtual surplus, see Lemma 1. This follows from $\hat{q}_E^u = q_E^*(\hat{q}_I^u; \omega_E)$ and $q_E^u = q_E^*(\bar{q}_I; \omega_E)$, together with $\bar{q}_I \le \hat{q}_I^u$ when $\hat{q}_E^u > 0$. It is therefore sufficient to prove that $\hat{q}_E^u \ge q_E^c$.

Let \tilde{q}_I be defined by $q_E^*(\tilde{q}_I; \omega_E) = q_E^c$. By concavity of the modified virtual surplus, the ordering $q_E^c(\omega_E) \leq \hat{q}_E^u(\omega_E; \gamma)$ is equivalent to

$$\omega_I - \frac{\partial h}{\partial q_I}(q_E^c, \tilde{q}_I) - \beta \frac{1 - F(\omega_E)}{f(\omega_E)} \frac{\partial q_E^*}{\partial q_I}(q_E^c, \tilde{q}_I) \le 0.$$
⁽²⁹⁾

This inequality is indeed equivalent to the modified virtual surplus reaching its maximum for $q_I < \tilde{q}_I$, and hence $q_E > q_E^c$. We have, using $q_I^c = q_I^*(q_E^c)$

$$\omega_I - \frac{\partial h}{\partial q_I}(q_E^c, \tilde{q}_I) = -\int_{q_I^c}^{\tilde{q}_I} \frac{\partial^2 h}{\partial q_I^2}(q_E^c, q_I) \,\mathrm{d}q_I \tag{30}$$

and, using $q_E^c = q_E^*(\tilde{q}_I)$

$$\beta \frac{1 - F(\omega_E)}{f(\omega_E)} = \omega_E - \frac{\partial h}{\partial q_E} (q_E^c, q_I^c) = \int_{q_I^c}^{\tilde{q}_I} \frac{\partial^2 h}{\partial q_E \partial q_I} (q_E^c, q_I) \,\mathrm{d}q_I \tag{31}$$

Finally recall that

$$\frac{\partial q_E^*}{\partial q_I}(q_E^c, \tilde{q}_I) = -\left.\frac{\partial^2 h}{\partial q_E \partial q_I}(q_E^c, \tilde{q}_I)\right/ \frac{\partial^2 h}{\partial q_E^2}(q_E^c, \tilde{q}_I)$$
(32)

We get (29) by combining (30), (31), and (32) and applying the inequality of Assumption 3 with $q_E = q_E^c$, $q_I^0 = q_I^c$ and $q_I^1 = \tilde{q}_I$.