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The Present-Value Model of the Current Account Has Been Rejected: Round Up the Usual Suspects

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The Present-Value Model of the Current Account Has Been Rejected: Round Up the Usual Suspects

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Abstract: Tests of the present-value model of the current account are frequently rejected by the data. Standard explanations rely on the "usual suspects" of nonseparable preferences, shocks to fiscal policy and the world real interest rate, and imperfect international capital mobility. The authors confirm these rejections on postwar Canadian data, then investigate their source by calibrating and simulating alternative versions of a small open economy, real business cycle model. Monte Carlo experiments reveal that, although each of the suspects matters in some way, a "canonical" RBC model moves closest to the data when it features exogenous world real interest rate shocks.

JEL classification: F41, E32

Key words: current account, present value model, world real interest rate, international capital mobility, Bayesian Monte Carlo

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The Present-Value Model of the Current Account Has Been Rejected: Round Up the Usual Suspects

1. Introduction

Current account fluctuations resist easy explanations. Large current account deficits have persisted in the U.S. through periods of large government budget deficits and surpluses, large and persistent real appreciations and depreciations of the dollar, and all phases of the business cycle. In Canada, the expansion of the 1980s coincided with large current account deficits, but an expansion in the 1990s witnessed current account surpluses.

Economists have increasingly used the intertemporal approach to study the current account. The intertemporal approach views the current account as a tool domestic residents use to smooth consumption by borrowing from or lending to the rest of the world. For example, if future income is expected to rise, say due to a technology shock, domestic agents attempt to smooth consumption by borrowing internationally prior to the high-income years, thereby running a current account deficit. As such, the intertemporal approach emphasizes permanent income fluctuations (driven by technology shocks) to explain current account movements. Compared to traditional Keynesian views, the intertemporal approach reduces emphasis on the economy's intratemporal competitiveness measured by the real exchange rate.

The intertemporal approach to the current account encompasses several classes of small open economy models. The most basic is the present-value model (PVM) of the current account. Sheffrin and Woo (1990), Otto (1992), Ghosh (1995), and Bergin and Sheffrin (2000) find that the testable implications of the PVM are routinely rejected by the data.

Despite rejections of the PVM's cross-equation restrictions, it is argued that abandonment of the underlying scheme is not warranted. Adherents point out the (in-sample) current account forecast from the most unadorned PVM often tracks the actual current account fairly closely (e.g., Obstfeld and Rogoff (1996), pp. 92-94).¹ Thus, the PVM, although strictly rejected, is viewed in the literature as "useful" overall. This conclusion, while appropriate, is less than satisfactory because it fails to say which elements of the intertemporal model are most responsible for the poor empirical performance of the PVM.

In this paper, we consider a set of "usual suspects" – i.e., factors that theory teaches us can matter for the current 1 Other authors, such as Ahmed (1986) and more recently Glick and Rogoff (1995), İşcan (2000), and Nason and Rogers (2002), test a variety of implications of the intertemporal approach and present evidence that favors some aspects of it.

account, yet are unaffected by technology shocks – as potential sources of the empirical rejections of the PVM of the current account. These factors are non-separable preferences, country-specific fiscal shocks, a common world real interest rate shock, and imperfect international capital mobility. We place the suspects in a "canonical" small open economy-real business cycle (RBC) model which nests the PVM and serves as our benchmark intertemporal model of the current account.

Our "testing" strategy compares moments of synthetic data produced by the RBC model to those of actual data. Rather than focus on the usual variances and covariances, the "moments" we study are the cross-equation restrictions of the PVM. The actual data we use to document rejections of the restrictions (and to calibrate our RBC model) is from post-war Canada, a proto-type small open economy for which rejections of the PVM are found uniformly in the literature.² We evaluate the empirical and theoretical distributions implied by the cross-equation restrictions using Bayesian Monte Carlo methods, which measure the fit of the RBC model to the actual data.

The canonical RBC model includes none of our suspects. This economy features a permanent, country-specific technology shock, but has no transitory shocks to fiscal policy or the world real interest rate. Capital is perfectly mobile internationally. Thus, the canonical model nests the PVM. Next, we add suspects to the canonical model one-at-a-time to create alternative specifications. With each alternative, we generate artificial time series, repeat tests of the cross-equation restrictions, and again compare the outcomes to the actual data. These exercises give us evidence about the culpability of each of the suspects.

Our choice of suspects is guided by related work on the intertemporal approach. Non-separable preferences can matter for the current account in several ways. Ghosh and Ostroy (1997) find that incorporating precautionary saving into the PVM helps to explain current account volatility.³ Bergin and Sheffrin (2000) improve the fit of the basic PVM by allowing for non-separable utility (between tradable and non-tradable goods) and a stochastic (consumption-based) real world interest rate. The impact of fiscal and interest rate shocks on small open economies is well studied. Striking evidence of the importance of fiscal shocks, especially large ones, for intertemporal external borrowing decisions has been presented by Ahmed (1986) and Ahmed and Rogers (1995). Hercowitz (1986) and Blankenau, Kose, and Yi (2001) report that world real interest rate shocks help to explain aggregate fluctuations in small open economies. Cole and Obstfeld (1991) argue that

²An example is Ghosh (1995), who obtains rejections for Canada, but ironically, finds the PVM holds better in U.S. data. He and Obstfeld and Rogoff (1996) report "excess smoothness" of the predicted Canadian current account, as we report below.

³Interestingly, Canadian data rejects the precautionary saving hypothesis according to Ghosh and Ostroy.

small barriers to international capital mobility lead to a smaller current account on average because the benefits of consumption smoothing are negated. Barriers to international capital mobility have been modeled formally by Mendoza (1991b), Valderrama (2002), and Schmitt-Grohé and Uribe (2003), in different fashions. Mendoza adds capital controls to a small open economy-RBC model, Valderrama places an arbitrary bound on debt accumulation, while Schmitt-Grohé and Uribe introduce an endogenous risk premium into a similar model.

In the next section, we describe the testable predictions of the PVM of the current account and confirm rejections of those predictions on Canadian data. Section 3 presents our small open economy-RBC model, derives its optimality conditions, and explains the numerical methods we employ to solve our model. We report the results of the Monte Carlo experiments in section 4 and discuss our conclusions in section 5.

2. The Present-Value Model of the Current Account

Empirical studies of the PVM of the current account have adapted the permanent-income model of consumption to the small open economy to derive the tests of Campbell (1987) and Campbell and Shiller (1987). As Sheffrin and Woo (1990), Otto (1992), Ghosh (1995), and Bergin and Sheffrin (2000) demonstrate, the cross-equation restrictions implied by the PVM are almost always rejected by the data. In this section, we review these restrictions and confirm their rejections on a sample of post-war Canadian data. We then pursue the paper's main objective of uncovering the sources of these rejections.

2.1 Tests of the Present-Value Model of the Current Account

The PVM of the current account is derived from the permanent-income decision rule of a small open economy, $\bar{C}_t = rB_t + r(1+r)^{-1} \sum_{j=0}^{\infty} (1+r)^{-j} E_t \{Y_{t+j} - I_{t+j} - G_{t+j}\}, 0 < r$, where \bar{C}_t is the permanent income-level of consumption, and r, Y_t , I_t , G_t , and B_t denote the non-stochastic world real interest rate, output, investment, government spending, and net domestic ownership of foreign assets, respectively. It is assumed that there is only one disturbance, a unit root country-specific technology shock that generates a permanent response in Y_t . Replacing C_t with \bar{C}_t in the expenditure identity, $Y_t \equiv C_t + I_t + G_t + NX_t$, where net exports, NX_t , equals the current account minus income from net domestic ownership of foreign assets, $CA_t - rB_t$, it follows that

$$CA_t = -\sum_{j=1}^{\infty} \left(\frac{1}{1+r}\right)^j \mathcal{E}_t \Delta N Y_{t+j}, \quad NY_t \equiv Y_t - I_t - G_t, \tag{1}$$

where Δ represents the difference operator. The current account-PVM relation (1) implies that when future net income is expected to be above trend, the current account is in deficit. This occurs because agents smooth consumption by borrowing in response to the (positive) shock to permanent income.

The cross-equation restrictions of the PVM rely on the assumption that the joint data generating process (DGP) of ΔNY and CA is an unrestricted *p*th-order bivariate autoregression, AR(*p*). Create a 2*p*-dimensional vector AR(1), $W_t = \mathcal{D} W_{t-1} + \mathcal{V}_t$, from this AR(*p*), where \mathcal{D} is the companion matrix, $W_t \equiv [\Delta NY_t \dots \Delta NY_{t-p+1} \ CA_t \dots CA_{t-p+1}]'$, and $\mathcal{V}_t \equiv [v_{\Delta NY,t} \ 0 \dots 0 \ v_{CA,t} \ 0 \dots]'$ is a vector of mean zero, homoskedastic unrestricted errors. The vector AR(1) yields an unrestricted forecast of W_{t+j} , $E_t W_{t+j} = \mathcal{D}^j W_t$. This and the row vector $\mathcal{F} \equiv [1 \ 0_{p-1}]$ yield $E_t \Delta NY_{t+j} = \mathcal{F} \mathcal{D}^j W_t$. Substitute this into the present-value relation (1) to find $\mathcal{H} = -\mathcal{F} \mathcal{D}[I - \mathcal{D}/(1+r)]^{-1}/(1+r)$, where \mathcal{H} is a 2*p* row vector.

The cross-equation restrictions of the PVM are embodied in \mathcal{H} . Note that these restrictions imply the linear rational expectations forecast of the current account, $CA_{f,t} = \mathcal{H}W_t$. The PVM predicts that $CA_{f,t}$ is identical to the actual current account because the contemporaneous current account is contained in the date *t* information set of the vector AR(1). Recalling that the *p* + 1st element of W_t is CA_t , the null hypothesis $CA_{f,t} = CA_t$ holds when all elements of \mathcal{H} are zero except its *p* + 1st element, which equals one.

Another implication of the model is that the difference between the forecast and actual current account is unpredictable, given the history of W_t . Campbell (1987) provides a way to test this prediction. When the PVM is assumed to be exact, only the country-specific technology shock drives the small open economy. In this case, \mathcal{D} is singular because the difference between its p + 1st row and first row equals its p + 2nd row multiplied by (1 + r). We define the implied variable as $C\mathcal{A}_t$ (notice the script notation).⁴ Given that \mathcal{D} is singular, $C\mathcal{A}_t$ is orthogonal to lags of W_t . However, these predictions fail to hold in the presence of a transitory demand shock.⁵ In this case, since $C\mathcal{A}_t$ and W_{t-1} are correlated, the PVM predicts that W_{t-1} has no power to forecast $C\mathcal{A}_{t+1}$ rather than $C\mathcal{A}_t$. This is a test of the extent to which current account fluctuations can be explained by shocks other than those that affect permanent income.

In sum, there are two tests of the cross-equation restrictions of the PVM of the current account: (*i*) all elements of \mathcal{H} are zero except the p + 1st element which equals one; and (*ii*) the forecast innovation is orthogonal to \mathcal{W}_{t-1} , so the

⁴The p + 1st row of \mathcal{D} contains the response of CA_t to \mathcal{W}_{t-1} , while the first and p + 2nd rows of \mathcal{D} are the responses of ΔNY_t and CA_{t-1} , respectively. Hence, $CA_t \equiv CA_t - \Delta NY_t - (1+r)CA_{t-1}$.

⁵This shock is serially uncorrelated and uncorrelated with lags of \mathcal{W}_t ; see Campbell (1987).

coefficients of the regression of CA_t or CA_{t+1} on W_{t-1} are all zero.

2.2 The Data and Empirical Results

We employ data on the Canadian current account and GDP net of investment and government spending. Our data sources are Statistics Canada and Basic Economics. The entire sample covers 1961Q1 through 1998Q1. Our estimation sample period begins in 1963Q1 and ends with 1997Q4, for a total of T = 140 observations. The data is measured on a per capita basis in 1992 Canadian dollars and is seasonally adjusted at annual rates. We demean ΔNY_t and CA_t , and estimate a vector AR (VAR) conditional on p = 4. The calibration sets r = 0.0091 (or 3.70 percent on an annual basis) to compute $\mathcal{H}^{.6}$

The data reject the cross-equation restrictions of the PVM. The Wald statistic of the cross-equation restrictions (computed as in Sheffrin and Woo (1990)) embodied in \mathcal{H} is 16.12 with an asymptotic p-value of 0.04 given eight degrees-of-freedom. This yields a rejection of the PVM. The LM test statistic, $T \times R^2$, of the orthogonality conditions discussed above supports this rejection. When $C\mathcal{A}_{t+1}$ ($C\mathcal{A}_t$) is the dependent variable, the test statistic of 14.78 (19.55) has an asymptotic p-value of 0.06 (0.01) on eight degrees-of-freedom. This indicates the regression coefficients are not all zero.

Rejections of the cross-equation restrictions of the PVM are confirmed by estimates of \mathcal{H} . These estimates, [0.11 - 0.03 - 0.06 0.06 0.08 0.06 - 0.04 - 0.10]', are all smaller than 0.12 in absolute value and none is significantly different from zero.⁷ The key theoretical prediction that $\mathcal{H}_5 = 1.0$, implying that the PVM forecast moves one-for-one with the actual current account, is strongly rejected in the data. This suggests that permanent income shocks do not dominate current account fluctuations because the PVM forecast is too smooth.

Finally, as derived in the previous section, $\hat{\mathcal{H}}$ yields a forecast of the current account, $CA_{f,t}$. The left-side window of figure 1 plots this forecast (the dot-dash line) and compares it to the actual current account (the solid line). Clearly, $CA_{f,t}$ is less persistent and less volatile than the actual current account. This "excess smoothness", which is found uniformly for Canada in the literature, still exists when we account for estimation uncertainty in the parameters of the unrestricted VAR. This can be seen from the right-side window of figure 1, which contains the actual Canadian current account, the solid line,

⁶Sheffrin and Woo (1990), Otto (1992), and Ghosh (1995) also demean ΔNY_t and CA_t prior to estimating the VAR. To select p, we compute the Akaike information criterion (AIC) and general-to-specific likelihood ratio (LR) tests for VARs of ΔNY_t and CA_t . The AIC and the LR tests select p = 4. The Canadian sample average of r is calculated using Fisher's equation, the three-month Euro-dollar deposit rate, the Canadian dollar-U.S. dollar exchange rate, and the implicit GDP deflator of Canada.

⁷The associated asymptotic standard errors are [0.20 0.20 0.14 0.09 0.41 0.12 0.12 0.11]/.

and the fifth and 95th percentiles of the piecewise probability bands of $CA_{f,t}$ (the dotted lines) which are generated using Bayesian Monte Carlo integration methods of Geweke (1999a).⁸ For most of the sample, the actual current account falls outside of the 90 percent probability bands. This is particularly striking for the second half of the 1980s and the early 1990s, when the actual current account is below the lower probability band of the PVM current account forecast.

Thus we have confirmed the rejections of the PVM of the current account that have been reported elsewhere. In the next section, we present a small open economy-RBC model that allows us to examine several possible sources of these empirical rejections.

3. A Small Open Economy-RBC Model

In this section, we construct a one-sector small open economy-RBC model. The model acts as a restricted DGP to explore the role of the usual suspects in explaining the empirical failures of the PVM of the current account. We solve our small open economy-RBC model numerically around its deterministic steady state and choose prior distributions of the model's parameters. We do this for our benchmark model containing only country-specific permanent technology shocks, which we label the "canonical RBC model", and for alternative specifications that feature our suspects.

3.1 Tastes, Technology, and the Impulse Structure

The small open economy-RBC model consists of a representative household, a constant returns to scale (CRS) technology, and an external sector. The household chooses uncertain streams of the single consumption good, C_t , and leisure, L_t , to maximize discounted expected lifetime utility

$$E_t \left\{ \sum_{i=0}^{\infty} \beta^i U(C_{t+i}, L_{t+i}) \right\}, \quad 0 < \beta < 1.$$
(2)

Leisure plus time supplied to the labor market, N_t , sums to the unit of time endowment the household receives each date t, $L_t = 1 - N_t$. Consumption and leisure enter the period utility function either separably

$$U(C_t, L_t) = \phi \ln[C_t] + (1 - \phi) \ln[1 - N_t], \qquad (3)$$

or in non-separable form

⁸We generate 5000 replications of $CA_{f,t}$ with software Geweke provides at *http://www.econ.umn.edu/~bacc*. Serial correlation in the 90 percent confidence bands is handled by computing the two largest principal components of the covariance matrix of the ensemble of synthetic $CA_{f,t}$.

$$U(C_t, L_t) = \frac{\left[C_t^{\phi} (1 - N_t)^{(1-\phi)}\right]^{(1-\psi)}}{1 - \psi}, \quad 0 < \phi < 1, \quad \psi \neq 1.$$
(4)

The restriction is $\psi = 1$ for the separable and log period utility function (3).

When period utility is non-separable in consumption and leisure, there is a link between demand for foreign assets (the current account) and current and expected future domestic labor market activity. Changes in time-worked alter the discount the small open economy applies to future expected returns, and hence the degree of consumption smoothing undertaken. Thus, under non-separable utility, there is an additional channel for shocks to produce current account fluctuations: through transitory movements in time-worked. A second way in which the assumption of non-separable utility can influence the current account is because the (non-log utility) risk aversion it implies yields "consumption-tilting" behavior. The greater the risk aversion, the more responsive is the current account to transitory shocks to consumption.

The household consumes, C_t , accumulates capital, K_{t+1} , through investment, I_t , or alters its stock of the internationally traded bond, B_{t+1} , through net exports, NX_t . The law of motion of capital is

$$K_{t+1} = (1-\delta)K_t + \left(\frac{K_t}{I_t}\right)^{\alpha} I_t, \quad 0 < \alpha, \delta < 1.$$
 (5)

This features installation costs in the flow of new capital as in Baxter and Crucini (1993).

An international bond is the only financial asset available to the household, which may purchase (sell) a unit of B_{t+1} from (to) the rest of the world at the end of date t. During date t + 1, the small open economy receives (sends) one unit of the consumption good plus a stochastic return, r_t , from (to) the rest of the world. The stochastic return is the world real interest rate. Thus, the law of motion of B_{t+1} is

$$B_{t+1} = (1 + r_t)B_t + NX_t, (6)$$

where NX_t reflects the net flow of the good between the small open economy and the rest of the world.

There are two components to r_t , an exogenous and stochastic return q_t , which is common across the world, and a risk premium that is specific to the small open economy, which is assumed to be a linear function of the economy's bond-output ratio.⁹ Thus,

⁹Placing this risk premium in the law of motion (6) negates a unit root in the *linearized* solution of our small open economy-RBC model. Schmitt-Grohé and Uribe (2003) study several devices that achieve a well-posed linearized solution for this class of RBC models, including an endogenous risk premium that is strictly increasing in the unit discount bond, and show that they all produce the same responses to one-time technology shocks. One contribution of our

$$r_t = q_t - \varphi \frac{B_t}{Y_t}, \quad 0 < \varphi.$$
⁽⁷⁾

In our model, movements in the world real interest rate are an additional source of consumption smoothing. Interest rate fluctuations can arise from exogenous shocks, q_t , or from endogenous fluctuations in the risk premium, $\varphi(B_t/Y_t)$, in response to other shocks. Exogenous shocks generate income and substitution effects in the small open economy and produce current account fluctuations by driving a wedge between expected returns to the international bond and domestic physical capital (which equals the marginal product of K_{t+1}). Movements in the risk premium have the same effect and imply, for example, that an economy that is a net debtor, $B_{t+1} < 0$, must pay a premium above q_t .¹⁰

We assume that the small open economy internalizes its risk premium, i.e., that its decision rules take account of fluctuations in the risk premium, $\varphi(B_t/Y_t)$.¹¹ From the perspective of the small open economy, imperfect capital mobility is equivalent to the (internalized) risk premium because either produces a wedge between q_t and r_t . We examine the extent to which the decisions of the small open economy affect current account fluctuations through the risk premium.

Our model is tied together by the resource constraint

$$Y_t = C_t + I_t + G_t + NX_t. (8)$$

Output is produced with the CRS technology

$$Y_t = K_t^{\theta} [A_t N_t]^{(1-\theta)}, \quad 0 < \theta < 1,$$
(9)

where A_t denotes a country-specific technology shock. It evolves as a random walk with drift

$$A_{t+1} = A_t \exp\{\gamma + \varepsilon_{t+1}\}, \quad 0 < \gamma, \quad \varepsilon_{t+1} \sim \mathcal{N}(0, \sigma_{\varepsilon}^2).$$
(10)

Since A_t drives permanent movements in the model's quantity variables (except for N_t), it plays the role of the domestic

disturbance to permanent income.

paper is to show the extent to which the Schmitt-Grohé and Uribe result holds in a model with multiple shocks. This is discussed in detail in the appendix; see below.

¹⁰The risk premium a debtor pays is higher the more negative is its bond-output ratio. However, a debtor whose output grows faster than its foreign

liabilities sees its risk premium fall. This allows our small open economy in principle to remain in debt permanently.

¹¹Alternatively, one could assume that foreigners set the risk premium, in which case it is treated as given by the small open economy. This is discussed more fully in the appendix.

Shocks to the transitory component of government spending, $g_t = G_t/Y_t$, and the exogenous component of the world real interest rate, q_t are assumed to follow AR(1) processes

$$g_{t+1} = g^{*(1-\rho_g)} g_t^{\rho_g} \exp\{\eta_{t+1}\}, \quad |\rho_g| < 1, \quad \eta_{t+1} \sim \mathcal{N}(0, \sigma_\eta^2),$$
(11)

and

$$1 + q_{t+1} = (1 + q^*)^{(1-\rho_q)} (1 + q_t)^{\rho_q} \exp\left\{\xi_{t+1}\right\}, \quad |\rho_q| < 1, \quad \xi_{t+1} \sim \mathcal{N}\left(0, \sigma_{\xi}^2\right), \tag{12}$$

where g^* is the steady state or unconditional mean of g_t and q^* is the exogenous component of the world real interest rate. We assume that the innovations ε_t , η_t , and ξ_t are uncorrelated at all leads and lags.

3.2 Optimality and Equilibrium

Maximizing (2) subject to (5) – (12) and K_{t+1} , C_t , I_t , and N_t non-negative, we derive the following optimality conditions

$$\left(\frac{1-\phi}{\phi}\right)\frac{C_t}{1-N_t} = (1-\theta)\frac{Y_t}{N_t}\left[1+\varphi\left(\frac{B_t}{Y_t}\right)^2\right],\tag{13}$$

$$\left(\frac{I_t}{K_t}\right)^{\alpha} = \mathbf{E}_t \left\{ \Gamma_{t+1} \left[\theta(1-\alpha) \frac{Y_{t+1}}{K_{t+1}} \left[1 + \varphi \left(\frac{B_{t+1}}{Y_{t+1}} \right)^2 \right] + \left[1 - \delta + \alpha \left(\frac{I_{t+1}}{K_{t+1}} \right)^{1-\alpha} \right] \left(\frac{I_{t+1}}{K_{t+1}} \right)^{\alpha} \right] \right\}, \quad (14)$$

and

$$1 = E_t \left\{ \Gamma_{t+1} \left(1 + r_{t+1} - \varphi \frac{B_{t+1}}{Y_{t+1}} \right) \right\}.$$
 (15)

The stochastic discount factor, Γ_{t+1} , equals $\beta (C_{t+1}/C_t)^{\phi(1-\psi)-1} ([1 - N_{t+1}]/[1 - N_t])^{(1-\phi)(1-\psi)}$ if period utility is given by (4) or $\beta (C_{t+1}/C_t)^{-1}$ when period utility is (3).¹²

Equation (13) equates the marginal rate of substitution between leisure and consumption to the marginal product of labor gross of the response of the risk premium to a change in employment. Along an equilibrium path, employment is higher than under perfect international capital mobility because the risk premium produces a negative income effect. Hence, the international bond's risk premium ties demand for foreign assets to the marginal rate of substitution between leisure and consumption. This is independent of period utility being separable or non-separable in consumption and leisure.

 $^{^{12}}$ Notice that the optimality conditions (13) – (15) reflect the social planner's problem. We compare and contrast the social planner's and the decentralized market economy's solutions of our small open economy model in the appendix. The appendix shows that for the cases that are most relevant the numerical solutions are very similar.

Equation (14) sets the marginal cost of increasing date t investment equal to the expected discounted benefit of the extra unit of capital available at date t + 1. The extra unit of capital contributes to greater production gross of the risk premium, higher depreciation, and smaller adjustment costs. This is the expected return to an additional unit of capital and is the right hand side of the Euler equation (14).

The Euler equation (15) describes optimality in the international bond market. It states that the unit of consumption foregone by holding one more bond is equal to the expected discounted benefit of holding that bond. The benefit includes the world real interest rate, r_{t+1} , net of the risk premium, $-\varphi(B_{t+1}/Y_{t+1})$, which moves endogenously with the bond-output ratio.

It is possible to price the risk premium. Excess returns on B_{t+1} are generated by

$$E_t \{r_{t+1} - r_{F,t+1}\} = \varphi \left[E_t \left\{ \frac{B_{t+1}}{Y_{t+1}} \right\} + E_t \{1 + r_{F,t+1}\} Cov_t \left(\Gamma_{t+1}, \frac{B_{t+1}}{Y_{t+1}}\right) \right].$$
(16)

According to (16), large excess returns on the internationally traded bond occur for two reasons. First, at the margin a creditor small open economy demands a larger excess return to lend more to the rest of the world. Second, excess returns are large when the stochastic discount factor is high at the same time the economy's international borrowing is high. This occurs in states of the world in which the small open economy is a debtor and wants to bring utility forward in time through additional borrowing.¹³

The degree of international capital mobility is parameterized with φ . As seen in (16), a small open economy that is a debtor (creditor) faces a higher (lower) world real interest rate, r_t , because its risk premium rises (falls) with φ . This drives the steady state bond-output ratio to zero as φ increases. The sense in which the risk premium is endogenous can be seen in that, for any φ greater than zero, it becomes increasingly expensive for a debtor economy to accumulate debt. Hence, greater imperfections in international capital mobility raise the cost of accumulating debt, and so limit the net benefits a small open economy derives from consumption smoothing.

Any candidate equilibrium path must satisfy the optimality conditions (13) – (15), the laws of motion of (5) – (7), and aggregate resource constraint (8) by necessity, given the production function (9) and exogenous shock processes (10) – (12). The transversality conditions $\lim_{j\to\infty} \beta^j E_t \{\lambda_{K,t+j}K_{t+1+j}\} = 0$ and $\lim_{j\to\infty} \beta^j E_t \{\lambda_{B,t+j}B_{t+1+j}\} = 0$, provide sufficient conditions for any candidate equilibrium, where $\lambda_{K,t+j}$ and $\lambda_{B,t+j}$ are shadow prices attached to the laws

¹³This idea is responsible for much of the literature that tests equilibrium international asset pricing models. Mark (2001) is a good review of this literature.

of motion of (5) and (6), respectively. Brock (1982) shows that the optimality, equilibrium, and transversality conditions are used to establish uniqueness of the equilibrium for a class of economies that covers our small open economy-RBC model.

3.3 The Numerical Solution and Priors

Our numerical solution proceeds by first, stochastically detrending the aggregate quantity variables (with the exception of N_t) using A_t . Second, we take a first-order Taylor expansion around the deterministic steady state of the stochastically detrended optimality and equilibrium conditions. Next, we arrange the results of the linearization into a two-sided linear vector stochastic difference equation for $\mathcal{M}_{t+1} = [\widetilde{K}_{t+1} \ \widetilde{B}_{t+1}]'$, where, for example, $\widetilde{K}_{t+1} = K_{t+1} A_t^{-1}/K^* - 1$ and K^* denotes the steady state value of capital. We conjecture the solution

$$\mathcal{M}_{t+1} = \mu_{\mathcal{M}} \mathcal{M}_t + \mu_{\mathcal{Z}} \mathcal{Z}_t \tag{17}$$

of the linearized system and follow Zadrozny (1998) to compute a solution.¹⁴ The matrices $\mu_{\mathcal{M}}$ and $\mu_{\mathcal{Z}}$ of (17) are two-by-two and two-by-three matrices of coefficients to be determined by our numerical solution and $\mathcal{Z}_t = [\varepsilon_t \ \tilde{g}_t \ \tilde{q}_t]'$. The vector of state variables $\mathcal{S}_t = [\mathcal{M}'_t \ \mathcal{Z}'_t]'$ drives the "flow" vector

$$\mathcal{C}_t = \pi_S \mathcal{S}_t, \tag{18}$$

where $C_t = [\widetilde{C}_t \ \widetilde{I}_t \ \widetilde{N}_t \ \widetilde{Y}_t]'$ and π_S is a four-by-five matrix.

Our simulation exercises adapt the Bayesian methods of DeJong, Ingram, and Whiteman (1996). This requires us to calibrate prior distributions for the parameters of our small open economy-RBC model. Since the prior distributions induce probability distributions for the moments of interest (the tests of the PVM) implied by the theoretical model, we can measure the fit of the theoretical model to the actual data.

Priors for γ , σ_{ε} , g^* , ρ_g , σ_{η} , q^* , ρ_q , and σ_{ξ} are based on sample observations. We impose a degenerate prior on the deterministic growth rate of technology, γ , calibrating it to 0.0024, the sample mean of $\Delta ln[A_t]$. The prior of its standard deviation, σ_{ε} , is assumed to be normal, centered on its sample mean of 0.0120 with a 95 percent coverage interval of [0.0115, 0.0125]. The sample mean of the government spending-output ratio, 0.2326, serves as the mean of the prior of g^* , while the means of the priors of the slope coefficient and standard deviation of the fiscal shock are calibrated from the relevant AR(1) estimates, [$\rho_g \sigma_\eta$]' = [0.9923 0.0127]'. This gives 95 percent coverage intervals for g^* , ρ_g , and σ_η of

¹⁴Zadrozny employs an eigenvalue method of undetermined coefficients – the elements of $\mu_{\mathcal{M}}$ – to solve the AR part of the linear vector stochastic difference equation of \mathcal{M}_{t+1} . Given this solution, the forward-looking moving average component of the difference equation imposes linear restrictions on the elements of the matrix $\mu_{\mathcal{Z}}$.

[0.2062, 0.2593], [0.9609, 0.9983], and [0.0121, 0.0133], respectively. These intervals are drawn from normal distributions, except for ρ_g whose prior is based on a log-normal distribution.

The priors of the parameters of the exogenous world real interest rate process are set in the same way. The mid-point of the prior of q^* is set at 0.0071 (or 2.87 percent on an annual basis), $[\rho_q \ \sigma_{\xi}]' = [0.9076 \ 0.0040]'$ is calibrated from AR(1) estimates of q_t , and normal distributions produce the 95 percent coverage intervals for q^* , ρ_q , and σ_{ξ} of [0.0058, 0.0084], [0.8580, 0.9567], and [0.0035, 0.0045], respectively.

Priors for the technology and utility function parameters follow standard RBC calibration practice. We center the prior of capital's share of income, θ , on 0.35 and draw its 95 percent coverage interval, [0.3201, 0.3802], from a normal distribution. Likewise, the prior of the depreciation rate, δ , is given by a normal distribution with a median of 0.02, which yields a 95 percent coverage interval of [0.0149, 0.0250]. The prior of the utility function parameter ϕ is chosen to be consistent with the steady state of optimality condition (13). This centers the prior of ϕ at 0.3716. Along with a normal distribution, this gives a 95 percent coverage interval of [0.3498, 0.3941]. We choose a mid-point for the risk aversion parameter ψ of two to be consistent with Mendoza (1991a). The 95 percent coverage interval of ψ drawn from a normal distribution is [1.5025, 2.5100].

We choose the prior of the installation cost (on the flow) of new capital parameter, α , to be consistent with the international RBC literature (e.g., Mendoza (1991a), Baxter and Crucini (1993), Correia, Neves, and Rebelo (1995), and Mendoza and Tesar (1998)). The first moment of α , 0.0503, and the 95 percent coverage interval, [0.0301, 0.0703], are drawn from a normal distribution.

The literature provides little guidance for choosing a prior for the risk premium parameter φ . In our canonical RBC model, capital is perfectly mobile internationally, suggesting that $\varphi = 0.0$. However, in order to avoid the well-known problems associated with a unit root in the bond accumulation process (e.g., Mendoza (1991a), Rebelo, Correia, and Neves (1995), Senhadji (1997), and Schmitt-Grohé and Uribe (2003)) we cannot set $\varphi = 0.^{15}$ Thus, we assume that the risk premium is "small", just one basis point at an annual rate (which implies $\varphi = 0.000071$) at the steady state, in this case.

Under imperfect international capital mobility, we calibrate the prior for φ to the Canadian data. Estimates reported by Clinton (1998) and Fung, Mitnick, and Remolona (1999) are consistent with risk premia anywhere between 10 to 90

¹⁵This problem does not necessarily arise for non-linear solution methods when $r^* < (1 - \beta)/\beta$, but does arise for linear approximate solution methods irrespective of the relationship of r^* and β .

basis points at an annual rate on medium to long-term Canadian bonds in international financial markets. We fix φ in the middle of this range, implying a risk premium of 50 basis points. This yields $\varphi = 0.0035$ at the mean of the Canadian bond-output ratio (about -0.35). We also assume that the risk premium is about 75 basis points at the top end of the 95 percent coverage interval of φ and 25 basis points at the low end. Given a normal distribution, these imply a 95 percent coverage interval for φ of [0.0019, 0.0052].¹⁶

Under this calibration, the effects of the risk premium are similar to those of Backus, Kehoe, and Kydland (1992), as well as Bergin's (2001) estimate of the cost arising from current account flows. Our risk premia imply a loss of less than 0.03 percent of the net exports-output ratio at the sample mean of our Canadian data. Cole and Obstfeld (1991) argue that even small barriers to perfect capital mobility such as these may be sufficient to outweigh the benefits associated with consumption smoothing.

4. Understanding Rejections of the Present-Value Model of the Current Account

Given the approximate linear equilibrium law of motion of the state vector (17), the associated flow relationship (18), and priors of our model, we construct distributions of the test statistics of the PVM from artificial time series. These series are generated by Bayesian Monte Carlo experiments.

4.1 Monte Carlo Strategy

We measure the fit of our small open economy-RBC model using PVM test statistics (described in section 2) as our "moments" of interest. Monte Carlo experiments generate $\mathcal{J} = 5000$ replications of the multivariate artificial time series $\{\mathcal{W}_{\mathcal{T},\mathcal{K}}\}_{\mathcal{K}=1}^{140}$, where \mathcal{T} denotes an object conditional on the RBC model.¹⁷ An unrestricted VAR(4) is estimated on the synthetic data to compute $\mathcal{H}_{\mathcal{T}}$, its Wald statistic, and $CA_{f,\mathcal{T},t}$.¹⁸ In addition, a regression of $\mathcal{CA}_{\mathcal{T},t+1}$ on $\mathcal{W}_{\mathcal{T},t-1}$ is used to

¹⁶The calibration of φ ignores higher order moments of the data, which suggest a larger risk premium. Using the unconditional version of the excess return generating equation (16), implies a φ equal to 0.0104 and 0.0162 for the separable and log period utility function (3) and the non-separable power utility function (4), respectively. At the steady state, these values of φ imply risk premiums of 150 and 230 basis points, respectively, which is one half or more of the world real interest rate we calculate from the data. These seem much too large for Canada, so we opt for the range of values noted above.

¹⁷We generate 315 synthetic observations, but drop the first 175 observations to remove dependency to initial conditions.

¹⁸The simulations use the mean of synthetic realizations of $\{r_{\mathcal{K}}\}_{\mathcal{K}=1}^{140}$ to calibrate the non-stochastic world real interest rate.

test the orthogonality condition. The empirical distributions, denoted \mathcal{E} , are posterior distributions of the actual data's PVM moments. We produce these \mathcal{E} distributions using Bayesian simulation techniques described by Geweke (1999a). Geweke (1999b) argues that to measure the fit of a dynamic stochastic general equilibrium model to the data requires an explicit statistical model.¹⁹ In our case, the statistical model is the unrestricted VAR or the orthogonality regression. The statistical models link population PVM moments implied by \mathcal{T} distributions to the actual data's \mathcal{E} distributions of the same moments.

An obvious requirement for our analysis is a metric of "closeness". Consider our comparison involving the individual elements of \mathcal{H} . The distance between $\mathcal{T}(\mathcal{H}_i)$ and $\mathcal{E}(\mathcal{H}_i)$ is measured by the difference in their ensemble averages, $\mathcal{H}_{\mathcal{T},i}$ and $\mathcal{H}_{\mathcal{E},i}$, normalized by the latter ensemble's standard deviation. DeJong, Ingram, and Whiteman (1996) refer to this as the standardized difference of means (*SDM*) statistic. Since the *SDM* statistic gauges how close the probability distribution of $\mathcal{T}(\mathcal{H}_i)$ is to $\mathcal{E}(\mathcal{H}_i)$ for each element of \mathcal{H} , a large value for this *t*-ratio-like statistic indicates our small open economy-RBC model fits the actual data poorly.

A second comparison of the T and \mathcal{E} distributions examines the validity of the cross-equation restrictions. This is measured with non-parametric estimates of the probability densities of (*i*) the Wald statistic of \mathcal{H}_T and (*ii*) the LM statistic, $T \times R^2$, of the orthogonality condition.²⁰

We assess the goodness of fit in two ways. First, we display plots of estimated \mathcal{T} and \mathcal{E} densities, which should be close and overlap if the RBC model is a good fit to the data. Second, we use the confidence interval criterion (*CIC*) statistic developed by DeJong, Ingram, and Whiteman (1996). The *CIC* measures the intersection of \mathcal{T} and \mathcal{E} distributions of either the LM or Wald statistics. Given a $1 - \omega$ percent confidence level, the *CIC* measures the fraction of \mathcal{T} and \mathcal{E} distributions that reside in an interval from the (lower) 0.5ω quantile \mathcal{L} to the (upper) $1 - 0.5\omega$ quantile \mathcal{U} .²¹ The larger the *CIC* the better the theoretical RBC model fits the actual data. In their study of a proto-type RBC model, DeJong, Ingram, and Whiteman regard *CIC* statistics of 0.3 or greater as indicating support for the theoretical model.

We focus on the orthogonality condition of the PVM that accounts for a transitory demand shock, rather than the

¹⁹Canova (1995) develops Bayesian model evaluation methods that treat the theoretical model in a similar fashion.

²⁰Non-parametric density estimation uses the normal kernel $\mathcal{N}(x) = \exp\{-0.5x^2\}/\sqrt{2\pi}$ where x is the distance between two points in the density. The density, $d(x) = (1/\mathcal{J}) \sum_{i=1}^{\mathcal{J}} \mathcal{N}([\mathcal{X} - \mathcal{X}_i]/h)$, simply plugs in the kernel, where h is the bandwidth or smoothing parameter of the density and \mathcal{X}_i is the *i*th Monte Carlo replication of either the Wald statistic of $\mathcal{H}_{\mathcal{T}}$ or the LM statistic, $T \times \mathbb{R}^2$. We follow Silverman (1986) to compute d(x).

²¹This is $CIC_x = (1 - \omega)^{-1} \int_{\mathcal{L}}^{\mathcal{U}} \mathcal{T}(x_j) dx_j$, where x is either the LM or Wald statistic. DeJong, Ingram, and Whiteman normalize the CIC by $1 - \omega$ so that it equals $\int_{\mathcal{L}}^{\mathcal{U}} \mathcal{E}(x) dx_j$. We always set $\omega = 0.10$.

orthogonality condition of the exact PVM, because the latter will always be strongly rejected by the small open economy-RBC model no matter its configuration. This is not surprising in light of the RBC model's structure and linearized solution. We discuss this point in the appendix.

4.2 The Canonical RBC Model

We begin with a "canonical" version of our small open economy-RBC model outlined in section 3 that embodies the restrictions of the PVM of section 2. The restrictions produce a prototype small open economy-RBC model with perfect international capital mobility, a constant world real interest rate, and a country-specific technology shock that is the dominant source of business cycle fluctuations. We show that the canonical model generates predictions that *are* consistent with the implications of the PVM of the current account, and hence could *not* be consistent with the actual data.

As noted above, by design, the canonical model rules out several of our "usual suspects", such as fiscal policy shocks. Seven parameter restrictions on the full model imply the canonical model. The household discount factor β is set equal to $1/(1 + q^*)$ which approximates the permanent income hypothesis (PIH) restriction. Unless otherwise noted, this restriction is always in effect. The restrictions $g^* = 0.0$, $\rho_g = 0.0$, and $\sigma_\eta = 0.0$ remove the fiscal shock from the model. Notice also that because the PVM assumes the data generating process is a VAR in ΔNY_t and CA_t , our synthetic DGP must possess two fundamental disturbances. The first is naturally the country-specific unit root technology shock. We assume that the second shock in the canonical RBC model is ξ_t , the innovation to the exogenous component of the world real interest rate, q_t . However, to maintain the spirit of the basic intertemporal model, we make the innovation to q_t "small", setting the point mass prior of σ_{ξ} to 2.110×10^{-5} (its calibrated value is 0.004) and eliminate any persistence in q_t with $\rho_q = 0.0$. Also, as noted above, we cannot have international capital mobility being literally perfect. Therefore, we employ the degenerate prior, $\varphi = 0.000071$, which is consistent with a steady state risk premium of one basis point (at an annual rate).

The upper panels of figure 2 plot the distribution of the LM statistics from the \mathcal{T} and \mathcal{E} densities. There are two important elements to evaluating these densities, the comparison between: (1) the synthetic data and the theoretical orthogonality prediction (how far to the left of the sample test statistic is the \mathcal{T} density?), and (2) the synthetic data and the actual data (how much do the \mathcal{T} and \mathcal{E} densities overlap?).

First, we see that the canonical RBC model has little problem satisfying the theoretical orthogonality prediction. Under either separable or non-separable utility, the model produces \mathcal{T} densities of the LM statistic that are mostly to the left of the sample LM statistic. Thus, the canonical RBC model is consistent with the theoretical prediction that lags of ΔNY_t and CA_t have no power to forecast CA_{t+1} . The match to this theoretical prediction is stronger for separable utility than for non-separable utility, as manifested in the *CIC* statistics of 0.33 for the model with separable utility and 0.84 for the non-separable utility model. This suggests that the assumption of separable utility is in part responsible for rejections of the PVM that we observe in the actual data.

The probability densities of the Wald statistic appear in the bottom panels of figure 2. The version with separable utility generates a distribution for \mathcal{H} that resembles the PVM's theoretical cross-equations restrictions, as indicated by the fact that the density lies to the left of the sample Wald statistic. In this particular case, the overlap with the \mathcal{E} distribution is substantial, as seen from the *CIC* statistic of 0.68. With non-separable utility, the \mathcal{T} density of the Wald statistic is close to uniform, and hence matches neither the basic PVM theory nor the actual data well at all. Its *CIC* statistic is 0.03.

Table 1 displays the ensemble means of the elements of $\mathcal{H}_{\mathcal{T}}$ and their *SDM* statistics. As shown in column 1, the canonical RBC model with the separable and log period utility function (3) yields estimates of $\mathcal{H}_{\mathcal{T},i}$ that are all close to zero, except the fifth element which, at 0.97, is close to the theoretical value of unity. The *SDM* statistics indicate that the canonical RBC model does not appear to match the actual data very well. For example, $\mathcal{H}_{\mathcal{T},5}$ is nearly two standard deviations above its empirical counterpart.

The canonical RBC model with the non-separable period utility function (4) fails to replicate the theoretical predictions of the PVM and to resemble the actual data. In this case, there is excess sensitivity of the current account to contemporaneous and lagged changes in net output, as $\mathcal{H}_{T,1} = -1.66$ and $\mathcal{H}_{T,2} = -1.34$ are more than six standard deviations below $\mathcal{H}_{\mathcal{E},1}$ and $\mathcal{H}_{\mathcal{E},2}$. Also, the estimate of $\mathcal{H}_{T,5}$ (= 1.02) indicates that allowing for non-separable utility does little to move the canonical RBC model closer to the data. Hence, in what follows we focus on versions of the RBC model with the separable and log period utility function (3).

The final piece of evidence about the fit of the canonical RBC model appears in the top row of figure 3. This displays the actual Canadian current account (the solid plot) and the fifth and 95th percentiles of the Bayesian Monte Carlo pointwise probability bands (the dot-dash plots) of the PVM forecast of the current account from the canonical RBC model with separable utility, the left-side window, and with non-separable utility, the right-side window.²² The model with

²²The 90 percent probability bands use the two largest principal components of the covariance matrix of the $CA_{f,T}$ ensemble.

separable preferences matches the actual PVM forecasts because the 90 percent probability bands of $CA_{f,T}$ contain zero except for a brief episode in the early 1980s and then during the late 1980s and early 1990s. With non-separable utility, the actual Canadian current account lies above the 90 percent probability bands of $CA_{f,T}$ except, once again, during the late 1980s and early 1990s. Thus, the fit of the canonical model to the actual Canadian current account is poor irrespective of the restrictions on utility. The canonical RBC model fits the PVM predictions much better with separable utility.

In sum, we have shown that in artificial data generated by the canonical RBC model, the familiar present-value restrictions on the current account and net output are typically not rejected. This finding ought not to come as a surprise in retrospect given the restrictions on the canonical model. We also show that the canonical model does a relatively poor job explaining the actual current account data, as our results in section 2 would suggest. This indicates that the true DGP for the current account is more complex than the canonical RBC model. In the next section, we see if incorporating our "usual suspects" into the canonical RBC model improves its fit to the actual data.

4.3 The Usual Suspects

We investigate the impact of each of the usual suspects by introducing them one-by-one into the canonical RBC model with the separable utility function (3). The suspects are transitory shocks to fiscal policy and the world real interest rate, and imperfect international capital mobility. When we introduce a suspect the rest of the priors are the same as for the canonical model with separable, log period preferences.

The transitory shock to fiscal policy is specified by the univariate AR(1) process (11). These highlight the role of a country-specific demand shock for current account fluctuations. We set up the fiscal policy experiment with priors on the parameters of the AR(1) government spending-output ratio process, its steady state, g^* , the slope coefficient ρ_g , and the standard deviation σ_η . These priors reflect observation from Canadian data and are described in section 3.3. Movements in the identified transitory component of government spending exhibit a substantial amount of persistence and volatility. The prior on ρ_g is a near unit root and its 95 percent coverage interval implies that the half-life of an innovation to g_t ranges from 3.5 to more than 100 years. Transitory shocks to fiscal policy possess more volatility than either technology shocks or shocks to the exogenous component of the world real interest rate. Innovations to g_t , η_t , are more than three times as volatile as innovations to q_t .

In the interest rate experiment, shocks to q_t focus attention on the response of the current account to changes in the

rate at which the rest of the world is willing to move consumption intertemporally. Although the exogenous component of the world real interest rate is persistent, it is not as persistent as fiscal shocks. The 95 percent coverage interval of the prior of ρ_q implies that the half-life of a shock to q_t is between one year and four years. The prior on the standard deviation of the innovation of the exogenous component of the world real interest rate, σ_{ξ} , makes this shock the least volatile of the model.

Figure 4 contains densities of the LM and Wald statistics of the fiscal policy and exogenous world real interest shock experiments. The fiscal policy experiment yields a T density of the LM statistic that has the most overlap and is closest to the \mathcal{E} density of the LM statistic (top left window), with a *CIC* statistic of 0.51. This statistic is 0.35 in the exogenous world real interest rate experiment (top right window).

The bottom panels of figure 4 depict the T and \mathcal{E} densities of the Wald statistic for the interest rate and fiscal policy experiments. These generate *CIC* statistics of 0.93 and 0.47, respectively, which suggest an exogenous shock to the world real interest rate is crucial to explain rejections of the PVM. This is consistent with the estimation work of Bergin and Sheffrin (2000), who report that adding a consumption-based real interest rate to the standard VAR used in present-value tests produces fewer rejections of the PVM's predictions. Since our experiments distinguish between different potential sources of interest rate movements, our results help to understand the underlying reasons for Bergin and Sheffrin's findings.²³

The distributions of $\mathcal{H}_{\mathcal{T}}$ in the interest rate and fiscal policy experiments are qualitatively similar to one another, and similar to those of the canonical RBC model. This can be seen from columns 3 and 4 of table 1. The only substantive difference appears in the all-important fifth element of this vector. The fiscal policy experiment generates an $\mathcal{H}_{\mathcal{T},5}$ of 0.68 and SDM = 1.33. In the interest rate experiment, $\mathcal{H}_{\mathcal{T},5} = 1.24$, which is more than two standard deviations greater than its $\mathcal{H}_{\mathcal{E},5}$ counterpart. Thus, the fiscal policy experiment is closer to the actual data according to this test of the PVM.

The 90 percent probability bands that are associated with the \mathcal{T} and \mathcal{E} distributions of CA_f , appear in the bottom row of figure 3 along with the actual Canadian current account. When we consider these current account forecast plots, we see that the world real interest rate experiment generates \mathcal{T} 90 percent probability bands (the dot-dash plot) that almost always contain the actual current account (the solid plot) and often do not cover zero or the \mathcal{E} piecewise 90 percent probability bands (the dots plot). The \mathcal{T} bands associated with the fiscal policy experiment, on the other hand, fail to contain the actual current account, except during the late 1980s and early 1990s (lower left window of figure 3).

²³Schmitt-Grohé (1998) finds that terms-of-trade and U.S. business cycle shocks help to explain aggregate fluctuations in Canada. The outcomes of our experiments are consistent with her results to the extent that our calibration of q_t captures the shocks she identifies.

As noted in section 3.3, imperfect international capital mobility is identified with the risk premium, $-\varphi B_t/Y_t$.

Introducing this risk premium affects the current account of a debtor small open economy such as Canada for two reasons. First, the interest rate it faces, r_t , is higher than the common world real interest rate, q_t . This creates a flow of asset income out of the small open economy, generating current account fluctuations as households smooth consumption. Second, a larger risk premium is synonymous with a larger debt-output ratio (more negative B_t/Y_t) for the economy, which implies a smaller current account on average. Thus, the current account exhibits more sensitivity to any shock that affects the debt-output ratio.

As seen in the right-side windows of figure 5, the imperfect international capital mobility experiment produces T densities of the LM and Wald statistics with *CICs* of 0.32 and 0.66, respectively. These lie in the range of those of the world interest rate and fiscal policy experiments.

The ensemble averages of $\mathcal{H}_{\mathcal{T}}$ and the *SDM* statistics of the imperfect international capital mobility experiment appear in the final column of table 1. These statistics indicate that the elements of $\mathcal{H}_{\mathcal{T}}$ are much further away from their empirical counterparts than in the canonical RBC model, the fiscal policy, or world real interest rate shock experiments. There is evidence of excess sensitivity of the current account to changes in net output, as seen from the fact that $\mathcal{H}_{\mathcal{T},1}, \mathcal{H}_{\mathcal{T},2}$, and $\mathcal{H}_{\mathcal{T},3}$ are negative (and more than 25 standard deviations below the same parameters of the \mathcal{E} distribution). Also, this experiment generates a negative response of the PVM current account forecast to contemporaneous current account movements, as indicated by $\mathcal{H}_{\mathcal{T},5} = -7.70$. All the lagged revisions to this forecast are large, $[\mathcal{H}_{\mathcal{T},6}, \mathcal{H}_{\mathcal{T},7}, \mathcal{H}_{\mathcal{T},8}]'$ = [15.97 -4.24 -5.63]', and therefore suggest substantial volatility in the 90 percent probability bands.

As noted in section 3, incorporating imperfect capital mobility into our canonical RBC model induces additional variability in the current account. The left-side window of figure 5 reflects this quite clearly. Thus, there is mixed evidence on the importance of departures from perfect capital mobility in explaining rejections of the PVM. According to the LM and Wald tests, imperfect capital mobility is nearly as important a suspect as transitory shocks to fiscal policy and shocks to world interest rates. However, the forecasted current account from the model with imperfect capital mobility exhibits considerably more variability than is consistent with the data.

4.4 Changing Preferences: What if $r^* < (1 - \beta)/\beta$?

Up to this point, we have imposed the PIH restriction, $q^* = (1 - \beta)/\beta$. This restriction, or more generally $r^* \ge (1 - \beta)/\beta$, is problematic when studying the limiting distributions of small open economies, if φ is identically zero.

Under these conditions, domestic households are sufficiently patient that the small open economy eventually accumulates the entire universe of wealth. In this case, the joint limiting distribution of the endogenous variables is not defined.²⁴ This problem can be rendered moot if it is assumed that $r^* < (1 - \beta)/\beta$, even when $\varphi = 0$. In this case, the future discounted marginal utility of consumption converges in the limit, which produces a finite level of consumption and bond value. Therefore, it is potentially useful to study cases in which $r^* < (1 - \beta)/\beta$.

Table 2 contains the ensemble averages of the elements of \mathcal{H}_T and their *SDM* statistics for (i) our canonical RBC model, (ii) the fiscal shock and the world real interest rate shock experiments, and (iii) the alternative that allows for imperfect international capital mobility, given $r^* < (1 - \beta)/\beta$.²⁵ Densities of the LM and Wald statistics and plots of the 90 percent confidence bands for these experiments appear in figures 6 - 9.

The results in table 2 for the canonical RBC model given $r^* < (1 - \beta)/\beta$ show the model fails to match the actual data and the theoretical predictions of the PVM. For example, $\mathcal{H}_{T,1} = 0.48$ indicates excess sensitivity of the current account to movements in changes in net output, while $\mathcal{H}_{T,5} = 0.36$ is well below the theoretical restriction that this element of \mathcal{H} equals one. This is reflected in the 90 percent confidence bands of the left-side window of figure 6. The bands are always below the actual current account. The restriction that the steady state world real interest rate is below the subjective rate of time preference gives the small open economy incentive to bring consumption forward, thereby leading to a lower current account balance. The left-side window of figure 6 suggests that such modifications to the canonical RBC model do not bring the current account forecast closer to the actual Canadian data.

The densities of the LM and Wald statistics provide further evidence on the usefulness of relaxing the PIH restriction. For the LM test, both specifications of the model yield *CICs* of about one-third. For the Wald test, relaxing the PIH restriction worsens the fit, as the *CIC* falls to only 0.03. Thus, the change in preferences afforded by $r^* < (1 - \beta)/\beta$ moves the model further away from the PVM predictions, but not in such a way as to move it closer to the actual data.

The impact of the fiscal and the world real interest rate shocks on the theoretical predictions of the small open economy-RBC model are qualitatively the same. The ensemble averages of the elements of $\mathcal{H}_{\mathcal{T}}$ from the 5000 replications

²⁴Chamberlain and Wilson (1984) discuss this problem in the context of a household saving problem. Aiyagari (1994) provides intuition and suggests a

resolution, while chapter 14 of Ljungqvist and Sargent (2000) is a good introduction.

²⁵We impose $\beta_j = 1/(1 + q_j^*) - (0.01 \times \check{\beta}_j)$ where the prior of q^* is described in section 3.3 and $\check{\beta}$ is normally distributed with mean 0.9940 and 95 percent coverage interval [0.9920, 0.9961].

neither match the sample estimates nor the theoretical PVM restrictions as found in the middle columns table 2. This is apparent from the 90 percent confidence bands of the left-side window of figures 7 and 8, which are wide, and the theoretical distributions of the Wald test of the PVM cross-equation restrictions, which are flat. Unlike the small open economy-RBC model with the PIH restriction $r^* = (1 - \beta)/\beta$, the fit of the model is not improved by the fiscal and the world real interest rate shocks when it is assumed that households are "impatient".

Finally, we conduct an experiment that assumes $r^* < (1 - \beta)/\beta$ and allows for imperfect international capital mobility. Qualitatively, the results are little changed from those we presented in the previous section. The fit of the model in terms of the densities of the LM and Wald statistics is reasonable as shown in the right-side windows of figure 9. The problem is that model with a prior centered on a 50 basis point per annum risk premium predicts that the PVM current account forecast exhibits excess sensitivity to lags of net output changes and a negative response to contemporaneous and lagged current account movements. This evidence is found in the right-most column of table 2 and the left-side window of figure 9. Thus, our results show that even fairly small and conservatively calibrated imperfections in capital mobility induce too much volatility in the current account no matter the restrictions on r^* and β .

4.5 Caveats

As with any applied study of this topic, our results could be affected by plausible extensions of our framework. It may help to find such extensions, because our simulations fail to achieve *complete* success in matching the data. Our RBC model has no monetary sector. This allows us to avoid the well-known difficulties associated with modeling money demand, the behavior of price setters, and the instruments, targets, and objectives of monetary policy in the open economy. The omission of a monetary sector from our model is not likely to affect our results much, and is surely a reasonable starting point, given that we expect monetary shocks to have only a minor effect on real variables beyond the short-run, while PVM tests place weight on the medium and long-run as well as the short-run. It might also be argued that non-monetary foreign demand shocks ought to play more of a role in our small open economy model. In earlier versions of this paper, we appended to the law of motion of the international bond, equation (6), an additive term that we interpreted as a shock to foreign demand. We found that the effect of this shock was negligible, and hence dropped it from our list of suspects.²⁶ We

²⁶Bergin's (2003) variance decomposition for Canada shows that at the 10 quarter horizon the sum of money demand and supply shocks account for under 20 percent of current account variability while foreign demand shocks account for seven percent.

also considered a terms-of-trade shock – a multiplicative shock to net exports in the aggregate resource constraint (8) – that acts as a taste shock and causes domestic households to act as if they are extremely patient. Thus, the current account of the small open economy is larger, on average, which fails to fit the Canadian data. Adding a non-tradables sector to the small open economy model could also improve the fit to the data. However, there is some reason to suspect that this channel might have only minor effects too. When the Glick and Rogoff (1995) model is extended to include non-traded goods, the responses of both thecurrent account and investment to relative price shocks (the terms of trade and nominal exchange rates) are insignificant (e.g., İşcan (2000)). Finally, one might consider incorporating physical trading costs of the type identified by Obstfeld and Rogoff (2000) as going a long way to resolve several major puzzles in international macroeconomics. However, the results of the two-country complete markets model of Backus, Kehoe, and Kydland (1992) suggest trading frictions may not be able to improve the fit of the intertemporal model to observed current account fluctuations. Continued progress on these fronts will undoubtedly shed more light on the questions that have been raised in this literature.

5. Conclusion

We study the importance of various explanations for the poor empirical performance of a basic intertemporal model of the current account, the present value model. First, we confirm the results of existing papers that reject the cross-equation restrictions and orthogonality conditions of the present-value model, in our case using a sample of post-war Canadian data. To understand these empirical results, we construct a small open economy-real business cycle model. We show that a "canonical" version of the model *is* consistent with the theoretical predictions of the present-value model, and hence is *not* consistent with the actual data.

The usual suspects we study, non-separable preferences, shocks to fiscal policy and the real interest rate, and imperfect international capital mobility, are portrayed in the literature as potential explanations of rejections of the present-value model. We conduct Bayesian Monte Carlo experiments to generate evidence about the culpability of our suspects. Although each matters in some way, world real interest rate shocks appear to do the most to move the model closer to the data. Thus, the attention paid to transitory movements in domestic fiscal policy to explain the current account while appropriate, may have missed other important factors. Given, our finding that transitory shocks to the exogenous component of the world real interest matter more at business cycle horizons, future research should perhaps look for additional

underlying macroeconomic factors that drive the current account. Finally, our results suggest the sources of current account movements have a larger common, cross-country component than is perhaps usually suspected, at least in the case of Canada.

The intuition for our results rest with households hedging against country-specific permanent income shocks through the current account. Any transitory shock to consumption generates current account fluctuations independent of movements in permanent income and hence could produce rejections of the present-value model. Shocks to the world real interest rate, for example, produce these sorts of current account fluctuations, whether they come from an endogenous country-specific component, an exogenous world shock, or an endogenous common world component. This is especially important because ever since Cole and Obstfeld (1991) pointed out even small imperfections in international capital markets can wipe out the (consumption smoothing) benefits of international portfolio diversification, the sources and causes of such imperfections have eluded researchers. We hope this paper invigorates this research agenda.

References

- Ahmed, S., 1986. Temporary and permanent government spending in an open economy: Some evidence for the United Kingdom, Journal of Monetary Economics 17, 197 224.
- Ahmed, S., Rogers J.H., 1995. Government budget deficits and trade deficits: Are present value constraints satisfied in long-term data?, Journal of Monetary Economics 36, 351 374.
- Aiyagari, S.R., 1994. Uninsured idiosyncratic risk and aggregate saving, Quarterly Journal of Economics 103, 659 684.
- Backus, D.K., Kehoe, P.J., Kydland, F.E., 1992. International real business cycles, Journal of Political Economy 100, 745 775.
- Baxter, M., Crucini, M.J., 1993. Explaining saving-investment correlations, American Economic Review 83, 416 436.
- Bergin, P.R., 2003. Putting the 'new open economy macroeconomics' to a test, Journal of International Economics, forthcoming.
- Bergin, P.R., 2001. How well can we explain the current account in terms of optimizing behavior, manuscript, Department of Economics, University of California, Davis.
- Bergin, P.R., Sheffrin, S.M., 2000. Interest rates, exchange rates, present value models of the current account, Economic Journal 110, 535 558.
- Blankenau, W., Kose, M.A., Yi, K.M., 2001. Can world real interest rates explain business cycles in a small open economy?, Journal of Economic Dynamics and Control 25, 867 889.
- Brock, W.A., 1982. Asset prices in a production economy, in: McCall, J.J. (Ed.). The Economics of Information and Uncertainty, University of Chicago Press, Chicago, pp. 1 43.
- Campbell, J.Y., 1987. Does saving anticipate declining labor income: an alternative test of the permanent income hypothesis, Econometrica, 55, 1249 1273.
- Campbell, J.Y., R. Shiller, 1987. Cointegration and tests of present value models, Journal of Political Economy 93, 1062 1088.

- Canova, F., 1995. Sensitivity analysis and model evaluation in simulated dynamic general equilibrium economies, International Economic Review 36, 477 501.
- Chamberlain, G., C. Wilson, 1984. Optimal intertemporal consumption under uncertainty, SSRI Working Paper 8422, Department of Economics, University of Wisconsin, Madison.
- Clinton, K., 1998. Canada-U.S. long-term interest differentials in the 1990s, Bank of Canada Review (Spring), 17 38.
- Cole, H., Obstfeld M., 1991. Commodity trade and international risk sharing: How much do financial markets matter?, Journal of Monetary Economics 28, 3 24.
- Correia, I., Neves, J.C., Rebelo, S., 1995. Business cycles in a small open economy, European Economic Review 39, 1089 1113.
- DeJong, D.N., Ingram, B.F., Whiteman, C.H., 1996. A Bayesian approach to calibration, Journal of Business and Economic Statistics 14, 1 9.
- Fung, B., Mitnick, S., Remolona, E., 1999. Uncovering inflation expectations and risk premiums from internationally integrated financial markets, Working Paper 99 – 6, Bank of Canada, Ottawa, Canada.
- Geweke, J., 1999*a*. Using simulation methods for Bayesian econometric models: Inference, development, communication, Econometric Reviews 18, 1 73.
- Geweke, J., 1999b. Computational experiments and reality, manuscript, Department of Economics, University of Minnesota.
- Ghosh, A.R., 1995. International capital mobility amongst the major industrialized countries: Too little or too much?, Economic Journal 105, 107 128.
- Ghosh, A.R, Ostry, J.D., 1997. "Macroeconomic uncertainty, precautionary saving, the current account, Journal of Monetary Economics 40, 121-139.
- Glick, R., Rogoff, K., 1995. Global versus country-specific productivity shocks and the current account, Journal of Monetary Economics 35, 159 192.
- Hercowitz, Z., 1986. The real interest rate and aggregate supply, Journal of Monetary Economics 18, 121 145.
- İşcan, T.B., 2000. The terms of trade, productivity growth, the current account, Journal of Monetary Economics 45, 587–611.
- Ljungqvist, L., Sargent, T.J., 2000. Recursive Macroeconomic Theory, MIT Press, Cambridge, MA.
- Mark, N.C., 2001. International Macroeconomics and Finance: Theory and Econometric Methods. Blackwell Publishers, New York, NY.
- Mendoza, E.G., 1991a. Real business cycles in a small open economy, American Economic Review 81, 797 818.
- Mendoza, E.G., 1991b. Capital controls and the gains from trade in a business cycle model of a small open economy, IMF Staff Papers 38, 480 504.
- Mendoza, E.G., Tesar, L.L., 1998. The international ramification of tax reforms: Supply-side economics in the global economy, American Economic Review 88, 226 245.
- Nason, J.M., J.H. Rogers, 2002. Investment and the current account in the short-run and long-run, Journal of Money, Credit, and Banking 34, 967 986.
- Obstfeld, M., Rogoff, K. 1996. Foundations of International Macroeconomics, The MIT Press, Cambridge, MA.
- Obstfeld, M., Rogoff, K., 2000. The six major puzzles in international macroeconomics: Is there a common cause?, in: Blanchard, O.J., Bernanke, B.S., (Eds.)., NBER Macroeconomics Annual, MIT Press, Cambridge, MA, pp. 339 389.

- Otto, G., 1992. Testing a present value model of the current account: Evidence from the U.S. and Canadian time series, Journal of International Money and Finance 11, 414 430.
- Schmitt-Grohé, S., 1998. The international transmission of economic fluctuations: Effects of U.S. business cycles on the Canadian economy, Journal of International Economics 44, 257 287.
- Schmitt-Grohé, S., Uribe, M., 2003. Closing small open economy models, Journal of International Economics 61, 163 185.
- Senhadji, A., 1997. Sources of debt accumulation in a small open economy, Working Paper no. 97/146, International Monetary Fund, Washington, D.C.
- Sheffrin, S.M., Woo, W.T., 1990. Present value tests of an intertemporal model of the current account, Journal of International Economics 29, 237 253.
- Silverman, B.W., 1986. Density Estimation for Statistics and Data Analysis, Chapman and Hall, Ltd., London, England.
- Valderrama, D., 2002. The impact of financial frictions on small open economies: when current account borrowing hits a limit, Working Paper 2002 15, Federal Reserve Bank of San Francisco.
- Zadrozny, P.A., 1998. An eigenvalue method of undetermined coefficients for solving linear rational expectations models, Journal of Economic Dynamics and Control 22, 1353 1373.

Table 1:	Tests of the Canonical				
and Alternative SOE-RBC Models					

			r		
	Separable Utility	Non-Separable Utility	Transitory Fiscal Shock	World Interest Rate Shock	Imperfect Capital Mobility
$\mathcal{H}_{\mathcal{T},1}$	-0.20	-1.66	-0.09	0.11	-4.98
	(-1.44)	(-8.64)	(-0.87)	(0.09)	(-25.02)
$\mathcal{H}_{\mathcal{T},2}$	-0.20	-1.34	-0.10	0.11	-15.11
	(-0.88)	(-6.84)	(-0.32)	(0.79)	(-79.16)
$\mathcal{H}_{\mathcal{T},3}$	-0.04	-0.24	-0.04	0.05	-5.73
	(0.21)	(-1.30)	(0.20)	(0.90)	(-42.52)
$\mathcal{H}_{\mathcal{T},4}$	0.03	-0.00	0.02	0.02	-0.04
- 2 ,1	(-0.57)	(-0.86)	(-0.69)	(-0.57)	(-1.39)
$\mathcal{H}_{\mathcal{T},5}$	0.97	1.02	0.68	1.24	-7.70
	(1.87)	(1.97)	(1.33)	(2.39)	(-14.69)
$\mathcal{H}_{\mathcal{T},6}$	0.14	0.12	0.02	-0.16	15.97
	(0.72)	(0.56)	(-0.18)	(-1.66)	(127.29)
$\mathcal{H}_{\mathcal{T},7}$	-0.13	-0.41	-0.06	0.15	-4.24
	(-0.81)	(-3.13)	(-0.25)	(1.59)	(35.57)
$\mathcal{H}_{\mathcal{T},8}$	-0.03	-0.16	-0.05	0.04	-5.63
	(0.77)	(-0.51)	(0.54)	(1.37)	(-52.26)

Experiment

The canonical RBC specification employs log separable utility, $\beta_j = 1/(1 + q_j^*)$, point mass priors of $g^* = \rho_g = \rho_q = \sigma_\eta = 0$, $\varphi = 0.000071$, $\sigma_{\xi} = 2.110 \times 10^{-5}$. The non-separable utility specification employs a prior on the risk aversion parameter of $\psi \in [1.50, 2.51]$ centered on two. Imperfect international capital mobility is achieved with the prior $\varphi \in [0.0019, 0.0052]$ centered on $\varphi = 0.0035$. The prior on the transitory shock to the government spending-output ratio are $\rho_g \in [0.9609, 0.9983]$ and $\sigma_\eta \in [0.0121, 0.0133]$. The Monte Carlo experiment with a transitory exogenous world real interest rate is based on the priors $\rho_q \in [0.8580, 0.9567]$ and $\sigma_{\xi} \in [0.0035, 0.0045]$. Details about the priors of the model parameters are discussed in section 3.3 of the text. The simulation experiments rely on 5000 replications of 140 artificial observations of ΔNY_t and the CA_t generated by the linearized solution of our small open economy-RBC model over the priors of the model's parameters. The $SDM(\mathcal{H})$ statistics appear in parentheses and are computed as $[\mathcal{H}_{T,i} - \mathcal{H}_{\mathcal{E},i}]/\text{STD}(\mathcal{H}_{\mathcal{E},i})$, $i = 1, \ldots, 8$, where $\text{STD}(\mathcal{H}_{\mathcal{E},i})$ is the standard deviation of $\mathcal{H}_{\mathcal{E},i}$.

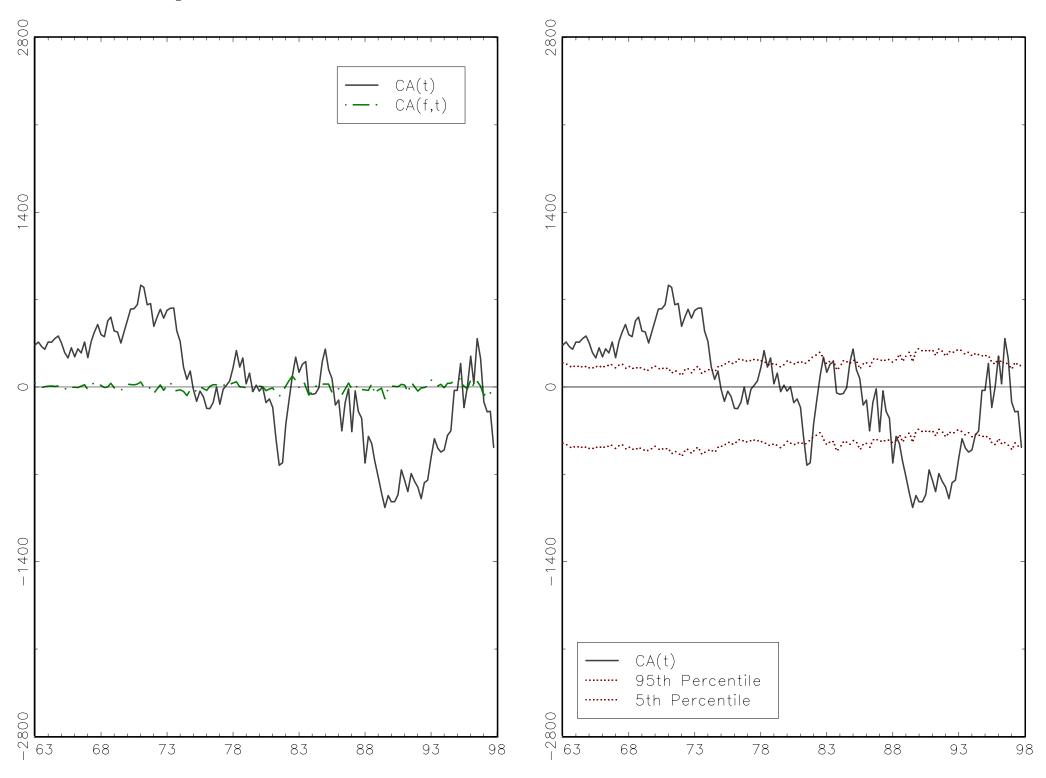
Table 2: Tests of the Canonical RBC Specification with Smaller β to Force $r^* < (1 - \beta)/\beta$

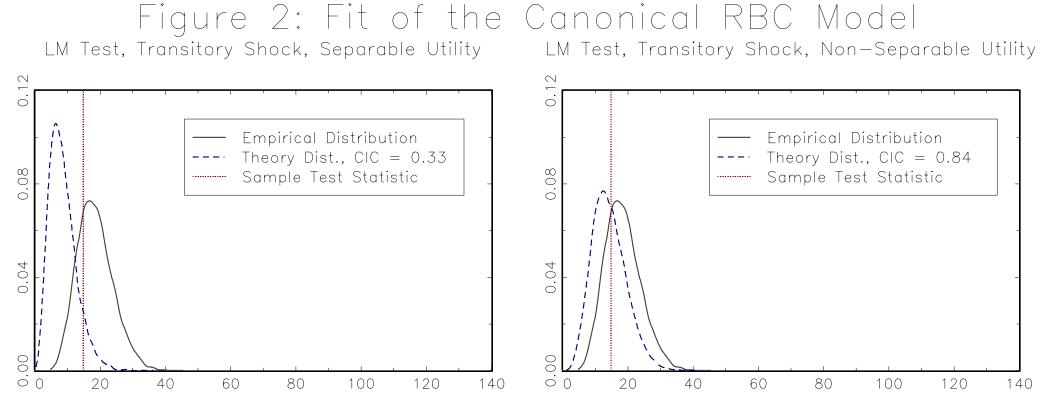
	Canonical Model	Transitory Fiscal Shock	World Interest Rate Shock	Imperfect Capital Mobility
$\mathcal{H}_{\mathcal{T},1}$	0.48	0.30	-16.48	-0.04
	(1.93)	(1.03)	(-81.78)	(-0.66)
$\mathcal{H}_{\mathcal{T},2}$	0.19	0.14	-14.40	-1.89
	(1.20)	(0.94)	(-75.40)	(-9.74)
$\mathcal{H}_{\mathcal{T},3}$	0.05	0.06	-10.02	-1.00
,	(0.86)	(0.93)	(-74.74)	(-7.04)
$\mathcal{H}_{\mathcal{T},4}$	-0.00	0.01	0.02	-0.01
_ , .	(-0.90)	(-0.72)	(-0.64)	(-0.94)
$\mathcal{H}_{\mathcal{T},5}$	0.36	-0.23	15.50	-1.00
- ,-	(0.71)	(-0.42)	(29.61)	(-1.88)
$\mathcal{H}_{\mathcal{T},6}$	0.19	-0.19	-1.76	2.41
2,0	(1.18)	(-1.86)	(-14.44)	(18.87)
$\mathcal{H}_{\mathcal{T},7}$	0.09	-0.10	-4.03	-0.06
- , ,	(1.10)	(-0.56)	(-33.73)	(-0.18)
$\mathcal{H}_{\mathcal{T},8}$	0.03	-0.05	-9.62	-0.98
, , , , , , , , , , , , , , , , , , , ,	(1.33)	(0.56)	(-90.10)	(-8.29)

Experiment

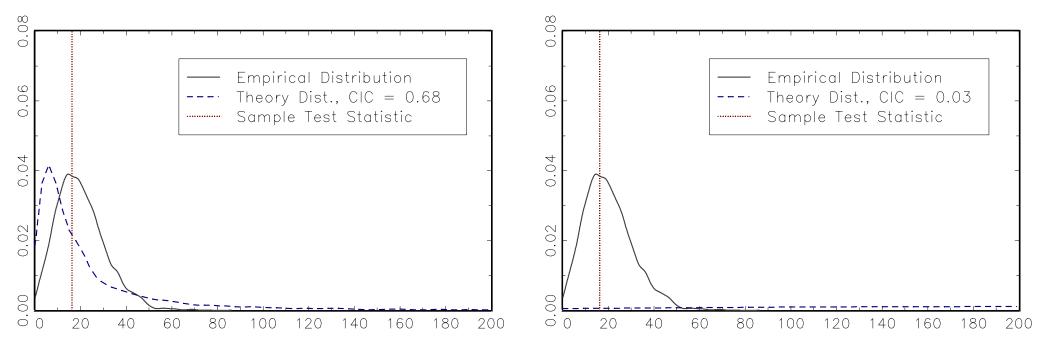
Details about the canonical and imperfect capital mobility RBC specifications are in the notes at the bottom of table 1. The restriction $r^* < (1 - \beta)/\beta$ is satisfied at the *j*th replication by drawing from the prior of q^* to create $\beta_j = 1/(1 + q_j^*) - (0.01 \times \check{\beta}_j)$ where the prior of $\check{\beta}$ is normally distributed with mean 0.9940 and 95 percent coverage interval [0.9920, 0.9961]. Otherwise, the priors of the model parameters are discussed in section 3.3 of the text.

Figure 1: Canadian CA and PVM Forecast

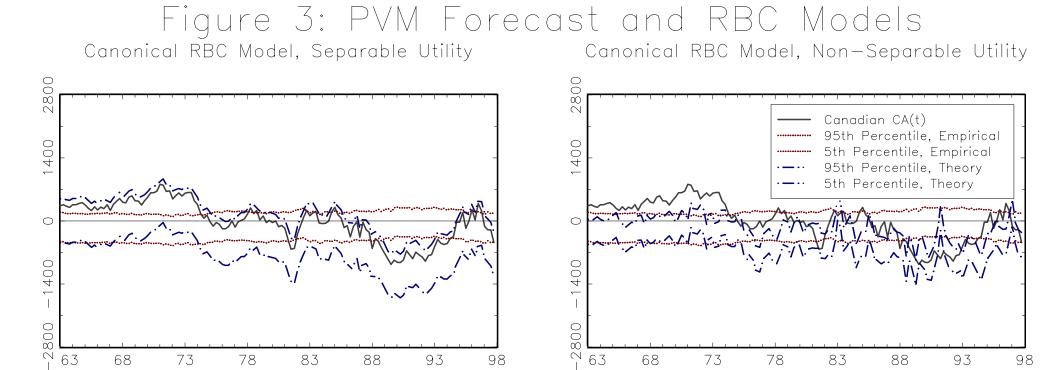




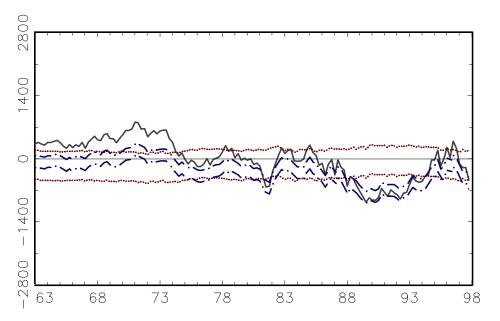
Wald Test, Separable Utility



Wald Test, Non-Separable Utility



Fiscal Shock, Separable Utility



World Real Interest Rate Shock, Separable Utility

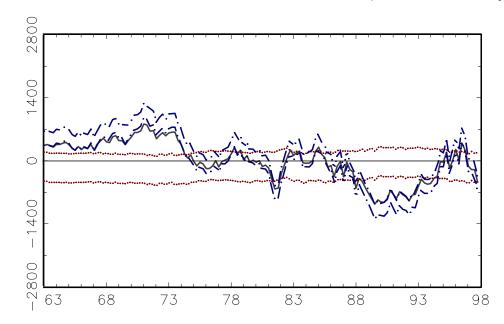
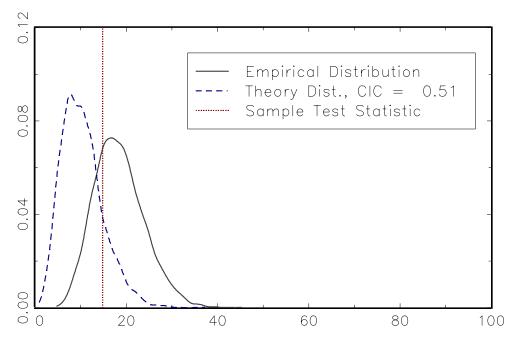
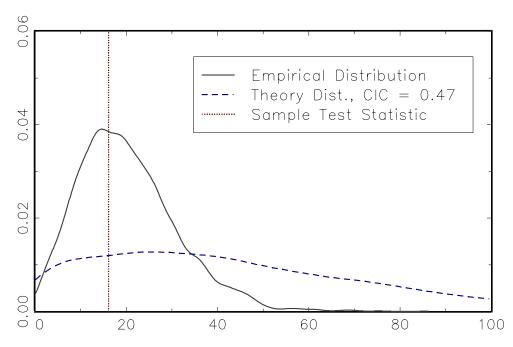
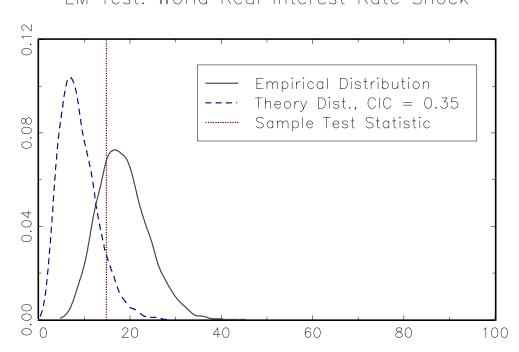


Figure 4: PVM Tests and the RBC Models LM Test: Fiscal Shock LM Test: World Real Interest Rate Shock



Wald Test: Fiscal Shock





Wald Test: World Real Interest Rate Shock

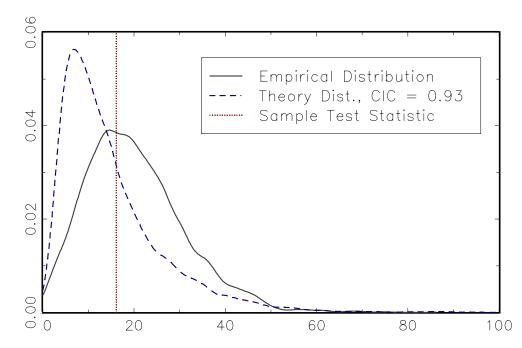


Figure 5: Imperfect Capital Mobility and RBC Model

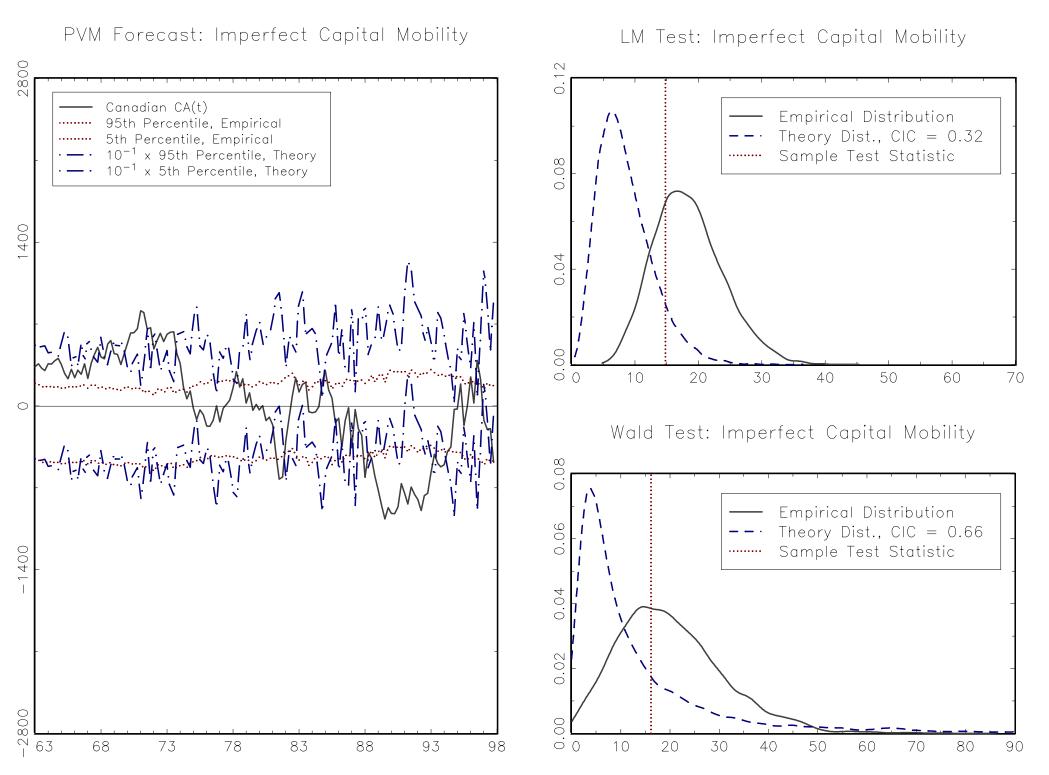


Figure 6: Lower β to Force $r^* < (1-\beta)/\beta$

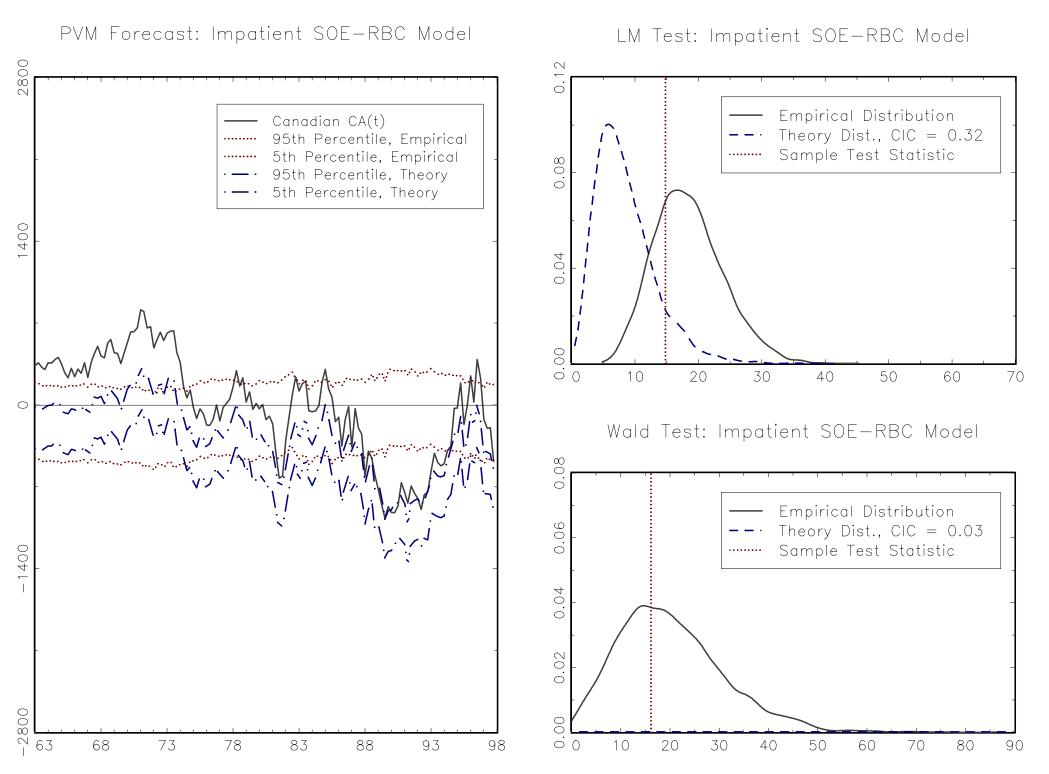


Figure 7: Lower β to Force $r^* < (1-\beta)/\beta$

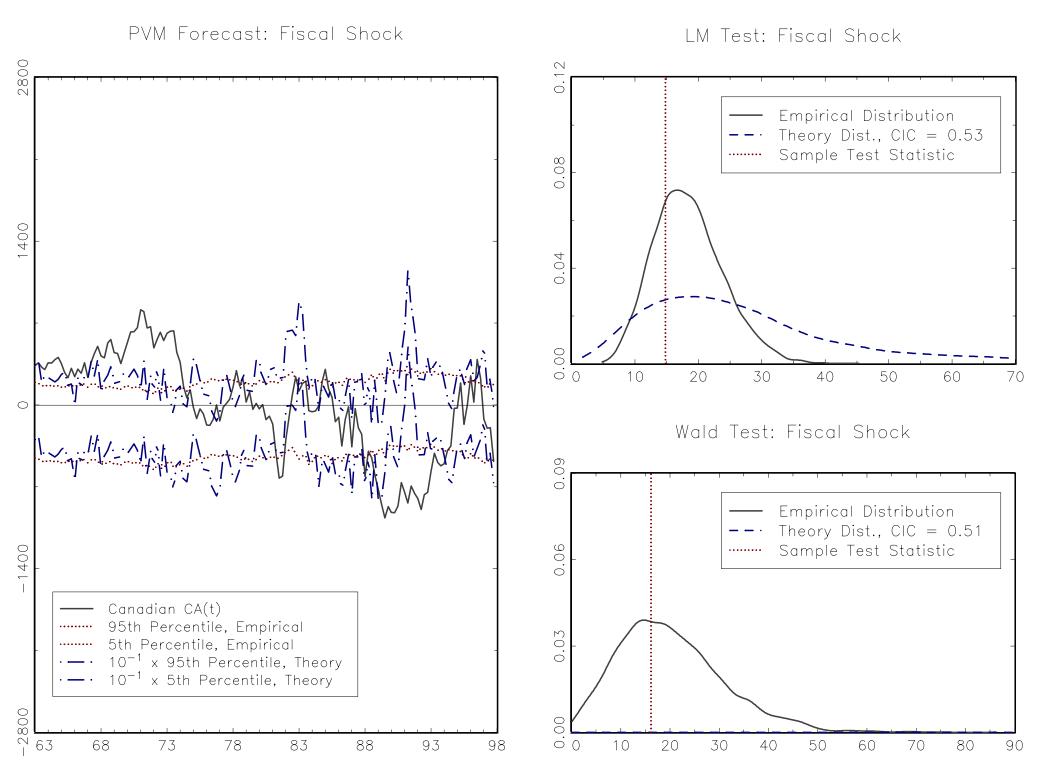


Figure 8: Lower β to Force $r^* < (1-\beta)/\beta$

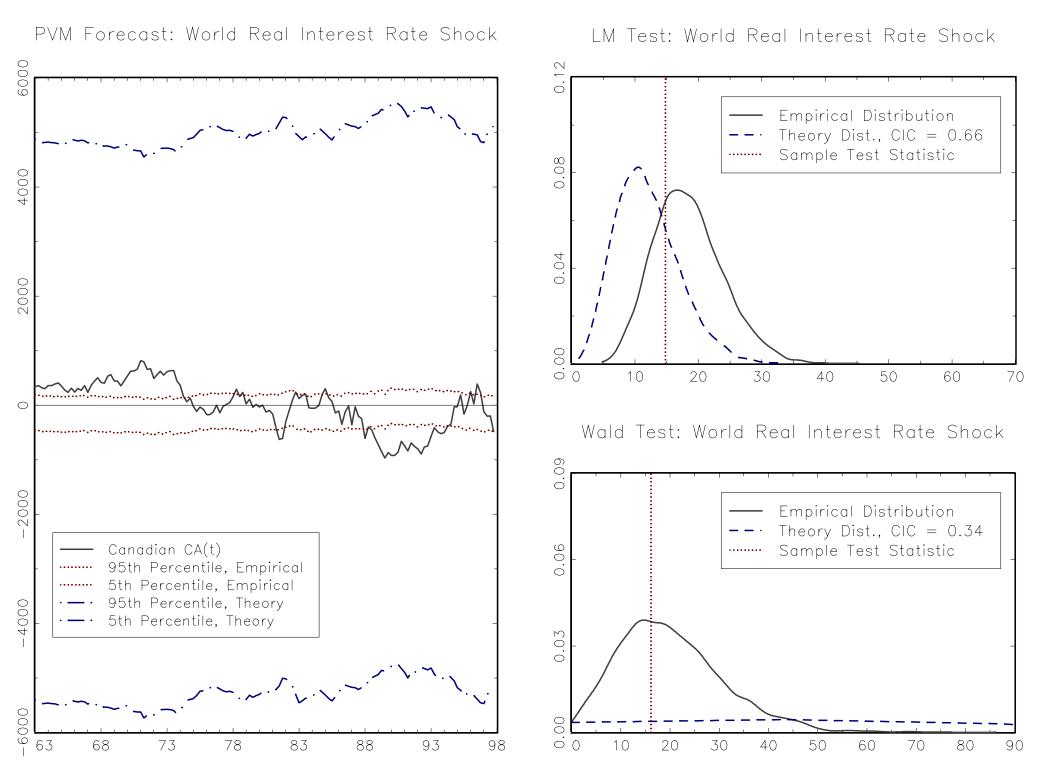
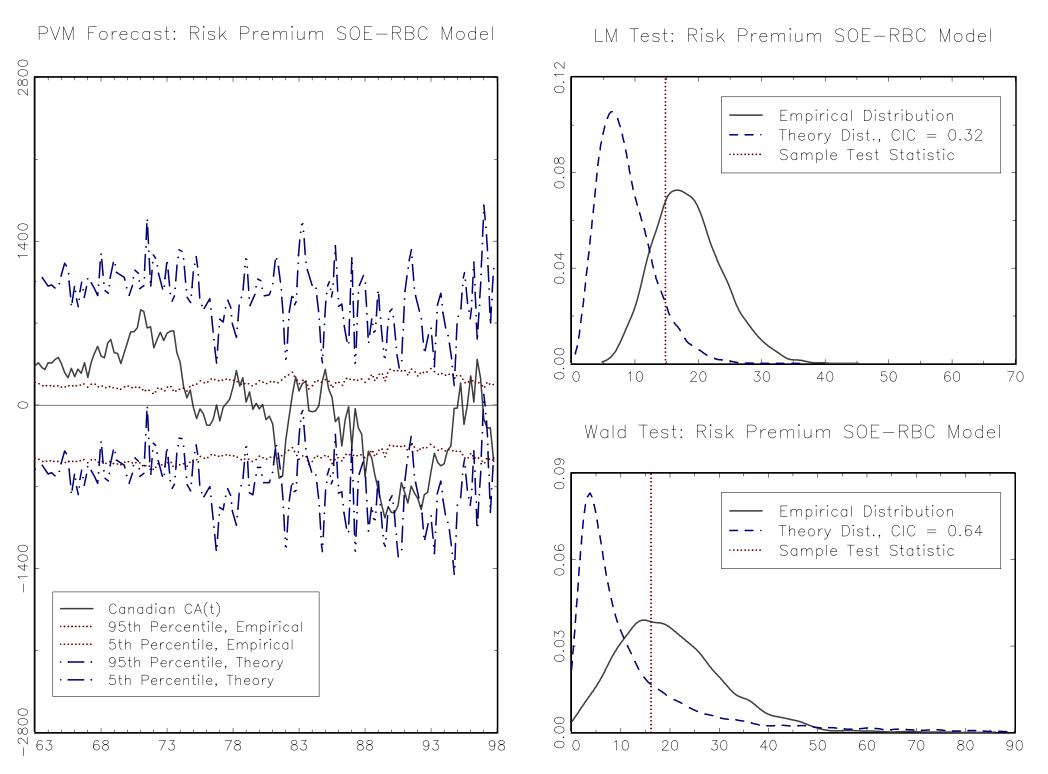


Figure 9: Lower β to Force $r^* < (1-\beta)/\beta$



Appendix

This appendix compares and contrasts the social planner's and decentralized market economy's solutions of our small open economy-RBC model, describes the analytics of the rejection of the exact orthogonality conditions of the PVM by the RBC model, outlines the impact of the terms-of-trade shock on the equilibrium and optimality conditions of our RBC model, and reports the Bayesian calibration and results of the associated simulation experiments. These items appear in sections *A*.1, *A*.2, *A*.3, and *A*.4 respectively.

A.1 The Impact of the Endogenous Risk Premium across the Social Planner and the Decentralized Market Economies

The social planner recognizes the impact her decisions about capital, the unit discount bond, and employment have on the world real interest rate, r_t . The decisions made by the representative household and firm about these variables in the decentralized market economy (DME) solution ignore this. The DME solution implies the risk premium is observed directly by the rest of the world when it sets its demand for (supply of) bonds of the creditor (debtor) small open economy. Across these two economies, it is easy to construct equivalent steady state bond-output ratios and Euler equations for the unit discount bond. This leaves the optimality condition for employment and the Euler equation for capital as the sources of different steady state allocations and (linear approximate) equilibrium dynamic paths for the social planner's economy (SPE) and the DME.

The results of this section of the appendix rely on restricting the parameter of international capital mobility, φ , across the SPE and DME. Also, the permanent income hypothesis restriction is imposed on β . The Euler equation of B_{t+1} of the DME is standard, $1 = E_t \{\Gamma_{t+1} (1 + r_{t+1})\}$. The restrictions this Euler equation places on any candidate equilibrium path is the same as the social planner's Euler equation (15) if $\varphi_{SPE} = 0.5\varphi_{DME}$, conditional on all other model parameters being held fixed. The parameter restriction on φ implies the B^*/Y^* ratio are equal across the two economies. In this case, employment and the capital-output ratio are smaller and the consumption-output ratio is larger in the DME than the SPE. The failure to internalize the endogenous risk premium leads to a lower level of economic activity in the steady state of the DME.

To study the impact of $\varphi_{SPE} = 0.5\varphi_{DME}$ on the dynamics of the SPE and the DME, require their (linear approximate) numerical solutions. We use the solution methods described in section 3.3 about the equilibrium law of motion (17) and the flow relationship (18) for both models. Instead of presenting simulation results for both economies, we focus on $\mu_{\mathcal{M}}$ and the underlying stable roots. At $\varphi_{SPE} = 0.71 \times 10^{-4}$,

$$\mu_{\mathcal{M},SPE} = \begin{bmatrix} 0.911220 & 0.035384 \\ -0.033886 & 1.009646 \end{bmatrix}, \quad \mu_{\mathcal{M},DME} = \begin{bmatrix} 0.918353 & 0.017379 \\ -0.032788 & 1.002611 \end{bmatrix},$$

and the stable roots of the unit discount bond (capital) are 0.995404 (0.925463) and 0.995196 (0.925768) for the SPE and the DME, respectively. Thus, the differences between the SPE and the DME begin at the third significant digit given the steady state risk premium is small (one basis point per annum). When φ_{SPE} is set to generate a steady state risk premium of 50 basis points per annum, the stable roots of the capital (bond) accumulation process are 0.967803 (0.818671) and 0.968318 (0.811462) for the SPE and the DME. The AR1 matrices of the equilibrium of laws of motion of capital and the unit discount bond are

$$\mu_{\mathcal{M},SPE} = \begin{bmatrix} 0.940179 & -0.005314 \\ -0.631614 & 0.846295 \end{bmatrix} \text{ and } \mu_{\mathcal{M},DME} = \begin{bmatrix} 0.941553 & -0.005377 \\ -0.647500 & 0.838227 \end{bmatrix}$$

for this parameterization of international capital mobility. The larger steady state risk premium generates differences in the response of \widetilde{B}_{t+1} to \widetilde{K}_t and \widetilde{B}_{t+1} to \widetilde{B}_t at the second significant digit across the SPE and the DME. Since the SPE internalizes the endogenous risk premium, this economy adjusts its bond position a bit more slowly to any given shock as well as accounting for the impact of capital on the accumulation of bonds and the endogenous risk premium. This lessens the response of the bond to movements in lagged capital.

The upshot is the equilibrium dynamics of the SPE and the DME are not all that dissimilar. Around a small steady state risk premium, these dynamics are nearly identical. At a larger steady state risk premium, the differences in the dynamics are more apparent, particularly for bond accumulation. Since we find that these larger steady state risk premium and the associated imperfections in capital mobility are not consistent with Canadian current account fluctuations and thus focus on economies that possess a small steady state risk premium, we conclude it is another reason to work with the SPE.

A.2 Orthogonality Conditions and the RBC Model

This section of the appendix explains why the small open economy-RBC model will always reject the exact version of the orthogonality condition. Note that an implication of the unit root technology shock (10) is that NY_t can be decomposed

as $NY_t = NY_{P,t} + NY_{\tau,t}$, where $NY_{P,t}$ and $NY_{\tau,t}$ are the permanent and transitory components of net output. It follows that the permanent component is a random walk with drift, $NY_{P,t} = \gamma + NY_{P,t-1} + \varepsilon_t$. Subsequent to applying this decomposition of NY_t to the PVM equation

$$CA_t = NY_t + \frac{r}{1+r} \sum_{j=0}^{\infty} \left(\frac{1}{1+r}\right)^j E_t \{NY_{t+j}\},$$

we find $CA_t = constant + \zeta(L)NY_{\tau,t}$, where $\zeta(L)$ is a lag polynomial of order *m* (possibly infinite) implied by the ARMA process of $NY_{\tau,t}$. The linearized solution (18) and (19) of the RBC model yields the equilibrium process $\widetilde{NY}_t = \pi_{S,NY}S_t$, where $\pi_{S,NY}$ is a row vector conformable with the state vector S_t . Identify the detrended and demeaned component of NY_t with its transitory component and it is easy to see that

$$\mathcal{CA}_t = \Delta \widetilde{NY}_t + [1 - (1 + r)L]\zeta(L)\widetilde{NY}_t,$$

where any constants have been ignored. Hence, CA_t is serially correlated and correlated with information of date t - 1 and earlier. It is important to note that this holds even when the innovation to the technology shock, ε_t , is the only exogenous state variable of the RBC model. Hence, the test of the orthogonality condition of the exact PVM possess no power against alternatives like our small open economy-RBC model.

A.3 The Small Open Economy-RBC Model with a Terms-of-Trade Shock

The transitory terms-of-trade shock, s_t , enters the small open economy-RBC model through its resource constraint

$$Y_t = C_t + I_t + G_t + s_t N X_t.$$
 (A.1)

We assume the terms-of-trade shock follows a AR(1) processes

$$s_{t+1} = s^{*(1-\rho_s)} s_t^{\rho_s} \exp\{\tau_{t+1}\}, \quad |\rho_s| < 1, \quad \tau_{t+1} \sim N(0, \sigma_\tau^2),$$
(A.2)

where s^* is the steady state or unconditional mean of s_t and the innovation τ_t is uncorrelated at all leads and lags with all other shock innovations.

The optimality conditions (13) - (15) become

$$\left(\frac{1-\phi}{\phi}\right)\frac{C_t}{1-N_t} = (1-\theta)\frac{Y_t}{N_t}\left[1+s_t\varphi\left(\frac{B_t}{Y_t}\right)^2\right],\tag{A.3}$$

$$\left(\frac{I_t}{K_t}\right)^{\alpha} = \mathbf{E}_t \left\{ \Gamma_{t+1} \left[\theta(1-\alpha) \frac{Y_{t+1}}{K_{t+1}} \left[1 + s_{t+1}\varphi \left(\frac{B_{t+1}}{Y_{t+1}}\right)^2 \right] + \left[1 - \delta + \alpha \left(\frac{I_{t+1}}{K_{t+1}}\right)^{1-\alpha} \right] \left(\frac{I_{t+1}}{K_{t+1}}\right)^{\alpha} \right] \right\}, \quad (A.4)$$

and

$$1 = E_t \left\{ \Gamma_{t+1} \frac{s_{t+1}}{s_t} \left(1 + r_{t+1} - \varphi \frac{B_{t+1}}{Y_{t+1}} \right) \right\}.$$
 (A.5)

given the terms-of-trade shock (A.2).

The terms-of-trade shock induces more persistence and volatility in the labor market optimality condition (A.3) and the Euler equation of capital (A.4). The real wage the firm offers is more persistent and volatile because the left-side of (A.3) is driven, in part, by s_t . The same is true for the discounted expected benefits the small open economy demands for it to increase its stock of capital by one unit. A persistent terms-of-trade shock generates negative income effects in the labor market and higher returns to domestic capital that introduce another way for the risk premium to affect the small open economy intertemporally.

The impact on the Euler equation of the unit discount bond (A.5) of the terms-of-trade shock is stinkingly different. It creates a "taste" shock, s_{t+1}/s_t , that alters the stochastic discount factor, Γ_{t+1} , of the small open economy. Note that the "taste" shock only appears in the optimality condition the small open economy uses to derive its net demand for foreign assets. Thus, the terms-of-trade shock provides another wedge between domestic returns to capital and way in which the small open economy discounts the returns it receives from the rest of the world.

A.4 Bayesian Calibration and Monte Carlo Experiment of the Small Open Economy-RBC Model with a Terms-of-Trade Shock

The Bayesian calibration of the terms-of-trade shock employs Canadian import and export price deflators and a least squares regression. The slope coefficient of the estimated AR(1) is 0.9621. Thus, the half-life of a Canadian terms-of-trade shock is nearly 4.5 years. This is more persistent than the exogenous shock to the world real interest rate, but much less

persistent than the fiscal policy shock. The prior on ρ_s is lognormal (the same distribution used for ρ_g and ρ_q), with a 95 percent coverage interval of [0.9000 0.9857]. We find the sample standard error of the terms-of-trade regression to be 0.0121, which makes s_t a bit less volatile than the degenerate prior on the fiscal policy shock. A normal distribution is employed for the prior of the standard deviation of τ_t . The priors' 95 percent coverage interval is [0.0112 0.0130].

We operate the Bayesian Monte Carlo experiment of the small open economy RBC model as described in sections 3.3 and 4.1 of the paper. The results are found in figure A.1 and the ensemble averages of the elements of \mathcal{H}_T are [0.1519 0.1408 0.0452 0.0079 0.8789 - 0.0375 0.0455 0.0379] and the associated standardized difference of means are [0.3071 0.9260 0.8386 0.7816 1.7019 0.6760 0.6796 1.3767]. These theoretical present-value model predictions suggests the addition of the terms-of-trade shock pushes the canonical RBC model closer to the data, as does the world real interest rate shock. Figure A.1 should disabuse one of this notion. The upper and lower 95 percent confidence bands of the theoretical current account forecast are above the actual Canadian current account for the entire sample (see the left-side window). This reflects the "taste" shock imposed on the Euler equation of the unit discount bond, which causes the small open economy to become more patient, as if $r^* > (1 - \beta)/\beta$. Hence, the small open economy runs a larger current account, on average. Otherwise, the simulation results show the densities of the LM and Wald tests produced by the terms-of-trade shock experiment to not fit the sample as well as the experiment with the exogenous world real interest rate shock. We conclude the exogenous world real interest rate shock dominates the terms-of-trade shock we study as an explanation of tests of the present-value model on and fluctuations of the Canadian current account.

Figure A.1: Canonical Model with T-of-T Shock

