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Ranking of VaR and ES Models: Performance in Developed and Emerging Markets

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Ranking of VaR and ES Models: Performance in Developed and Emerging Markets

Abstract

An inherent problem with comparing and ranking competing Value at Risk (VaR) and Expected shortfall (ES) models is that they measure only a single realization of the underlying data generation process. The question is whether there is any significant statistical difference in the performance of different models. Is it only a matter of chance that in a particular market and in particular time period a certain model performs better than some other? It all comes down to a question whether something that we subjectively perceive as different is actually statistically different. We introduce a new methodology for ranking and comparing the performance of VaR and ES models based on a nonparametric ANOVA test. The relative performance of VaR and ES models is analysed using daily returns for sixteen stock market indices (eight each from developed and emerging markets) prior to and during the global financial crisis. Results show that for a large number of different models there is no statistically significant difference in their performance. The top performers are conditional extreme value GARCH model, models based on volatility updating and nonparametric mirrored historical simulation. ES backtesting results are similar to VaR results with the models being even more closely matched. The same models that were the top performers in VaR comparison also perform significantly better in ES estimation.

JEL-Code: G240, C140, C220, C520, C530.

Keywords: ranking, Value at Risk, Expected Shortfall, extreme value theory.

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1 Introduction

The years leading up to the recent financial market turbulence have been characterized by exceptionally high growth of the world economy accompanied by moderate inflation. This strong performance resulted in unusually high returns in financial markets, especially in emerging and Anglo-Saxon countries. Risk premia and volatilities were exceptionally low across a very wide spectrum of assets including bonds, stocks, foreign exchange, and derivatives in general. Perception of a low risk environment and strong growth prospects were further fuelled by historically low interest rates, booming real-estate prices and expanding monetary aggregates. The high level of asset prices kept leverage ratios low, while the combination of strong income flows and historically low interest rates did the same with debt service ratios. However in 2005 Alan Greenspan (2005) noted: "...history has not dealt kindly with the aftermath of protracted periods of low risk premiums." Indeed, historically risk premia and Value at Risk (VaR) measures tend to be at their lowest immediately prior to the outbreak of a crisis or a period of exceptionally high market volatility. In 2007 Knight (2007) warned: "We might be witnessing the proliferation of... 'option-like' payoff patterns in the financial system," whereby investors assumed positions that yielded modest but steady income streams in times of prosperity but which could result in large, discontinuous losses in times of crisis. This "pattern" can be attributed to the introduction of new instruments and patterns of behaviour that raised the risk of extreme events while giving a false impression of a low-risk environment. In hindsight, it is clear that these warnings should have been heeded. The non-linear payoffs during worsening market conditions, combined with the assumptions of normality and IID behaviour widely used in VaR models, wrecked havoc on financial institutions, led to a massive need for government intervention in financial markets and created wide-spread doubts about VaR models not only in the eyes of academic community

but also among regulators (see CEBS guidelines, 2009). Institutional users are the only ones still defending the use of VaR as the only acceptable risk measure, mostly due to their very relaxed treatment of the true level of risk in banking portfolios (for example see ESBG, 2010).

Since its introduction VaR as a risk measure has been criticized theoretically, especially for the fact that these models do not account for the extent of losses that could be suffered beyond the specified threshold. In the eyes of investors and regulators, these extreme losses are precisely what a risk measure should flag. VaR is, however, inherently incapable of distinguishing between situations where losses in the tail are only slightly worse than the threshold, and those where they are overwhelming. It provides only a lower bound for losses in the tail and thus has a bias toward optimism instead of the conservatism that is generally thought to be beneficial in risk management.

An alternative measure of risk that quantifies losses that might be encountered in the tail is the Expected Shortfall (ES). While VaR represents a minimum loss one expects at a determined confidence level, ES is the expected value of that loss, provided that the loss is equal to or greater than the VaR. Artzner, et al. (1997, 1999) have shown, using an axiomatic approach to define a satisfactory or "coherent" risk measure, that VaR fails a coherency test because it does not universally exhibit sub-additivity, whereby the risk of a combined portfolio cannot be greater than the sum of the risks associated with any possible division of that portfolio. VaR can only be made sub-additive if the implausible assumption that returns are elliptically distributed is imposed. In this case, however, VaR and ES are equivalent and give exactly the same information (see Embrechts, et al., 1999). Even though VaR measures have substantial theoretical flaws, they have been imposed on financial institutions as a regulatory obligation under Basel I, II and III rules. ES, on the other hand, although a coherent measure of risk, has not been approved by regulators to calculate capital

requirements. This failure is actually quite surprising given that VaR and ES are inherently connected in the sense that ES figures can be easily calculated from the VaR surface in the tail. Perhaps because of this lack of approval, ES has not been as extensively studied as VaR in empirical research. Estimation techniques that have been developed for VaR measures in the past decades, however, can easily be employed to yield superior ES forecasts. This means that advances in VaR estimation need not be lost with the adoption of coherent risk measures into regulatory framework. The inherent connection between VaR and ES is extremely helpful for financial institutions, since all the building blocks required for VaR estimation (databases, risk drivers, calculation routines, etc.) are also needed for estimation of ES. Thus, if an institution already has the capacity to calculate VaR, it needs only small adjustments to produce estimates of a coherent risk measure, such as ES. Such a measure should be valuable for internal purposes even before it is required by regulators.

As opposed to the purely VaR-oriented literature, the empirical literature that compares VaR and ES has been limited in both emerging and developed markets. Gencay, Selcuk, and Ulugulyagci (2003) and Gencay and Selcuk (2004) analyzed the performance of unconditional Extreme Value Theory (EVT) models against variance-covariance and historical simulation models in nine emerging countries. They found that an unconditional EVT model outperformed classical VaR models at extreme confidence levels. Maghyereh and Al-Zoubi (2006) investigated the relative performance of popular VaR models against an unconditional EVT methodology for seven Middle Eastern and North African countries. Again EVT models outperformed classical variance-covariance and historical simulation models in most cases. Similar results were reported by Mendes (2000) for Latin American countries. Cotter (2004 and 2007) tested a parametric EVT and Gaussian estimates of VaR and ES in six Asian markets during the Asian crisis and five equity indexes from European markets. He found that EVT estimates are superior under both VaR and ES risk measures

looking at both the Kupiec and Christoffersen criterions, although it was hard to reach any conclusion regarding the significance of these differences. Nyströmand and Skoglund (2002) tested the performance of VaR models on a wide range of assets in developed countries and found that for quantiles higher than the 98 percentile the use of unconditional EVT models made a substantial predictive contribution and that the generalized Pareto distribution more accurately modelled the empirically observed tails than the normal distribution. In contrast to these findings, however, Silva and Mendes (2003) found that the performance of an unconditional EVT model is not satisfactory in meeting Basel II criteria in Asian stock markets since it is overly conservative and thus very expensive for banks.

To remedy the problems of the unconditional estimation that is traditional in EVT, McNeil and Frey (2000) developed a conditional EVT approach to both VaR and ES estimation and showed empirically that the traditional parametric VaR models with normal density fail to accurately estimate losses during financial crises. They, along with many others (see Acerbi et al. 2001, Yamai and Yoshiba, 2002 and Inui and Kijima, 2005), advocated the use of ES as an alternative risk measure with good theoretical properties. Overall, the literature strongly suggests that although ES provides superior risk measures to VaR, these have not been as exhaustively studied as VaR measures.

Apart from these well known "technical" problems there is also a usually overlooked systemic problem with risk model comparison and ranking. When evaluating and backtesting VaR/ES figures we are looking at only a single realization of the underlying data generation process. Consequently our judgement on the performance of particular risk models is based only on the performance of the model with regards to a single realization. The VaR model comparison literature is vast but it rarely addresses the question of whether there is truly any significant statistical difference in the performance of different models. Is it only a game of chance that in a particular market and in particular time period a certain model performs

better than some other, or does a certain model consistently and statistically significantly outperform some another model?

In this paper we first develop a new methodology for VaR and ES model comparison which allows us to rank competing VaR/ES models. Next, we provide an empirical investigation and tail risk assessment of a wide array of VaR and ES models in both developed and emerging countries prior to and during the global financial crisis.

The following VaR models are analyzed in the paper:¹

- (a) Normal simple moving average (VCV) method,
- (b) RiskMetrics system,
- (c) Historical simulation,
- (d) Mirrored historical simulation,
- (e) Kernel historical approach,
- (f) BRW (time weighted) simulation with decay factors of 0.97 and 0.99,
- (g) GARCH model,
- (h) Filtered Historical simulation (FHS) method,
- (i) Unconditional EVT approach using Generalized Pareto distribution (GPD) and
- (j) Conditional EVT approach.

The ES models analyzed in the paper are:

- (a) VCV with GPD,
- (b) RiskMetrics with GPD,
- (c) GARCH with GPD,
- (d) Bootstrapped historical simulation,

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¹ For a good overview of a wide range of VaR and ES models see, for example, Dowd (2005).

- (e) Bootstrapped "mirrored" historical simulation,
- (f) Bootstrapped kernel historical approach,
- (g) Bootstrapped BRW simulation,
- (h) FHS-ES approach,
- (i) Conditional EVT approach and
- (i) Unconditional EVT approach.

2 Value at Risk and Expected Shortfall

VaR is usually defined as:

"the maximum potential loss that a portfolio can suffer within a fixed confidence level (cl) during a holding period."

Let $(X, t \in Z)$ be a strictly stationary time series representing daily observations of the negative log return for a financial asset. The dynamics of X are given by:

$$X_{t} = \mu_{t} + \sigma_{t} Z_{t} \tag{1}$$

where the innovations Z are IID with zero mean, unit variance and marginal distribution function $F_z(z)$. It is typical to assume that μ_t and σ_t are measurable with respect to ψ_{t-1} (the information set up to time t-1) and that $F_x(x)$ denotes the marginal distribution of (X_t) . For a horizon hp, $F_{X_{t+1}+...+X_{t+hp}|\psi_t}(x)$ denotes the predictive distribution of the return over the next hp days, given the information set up to and including day t. From a tail event perspective, for a given confidence level cl (0 < cl < 1), the unconditional $VaR_{cl}(X)$ is a quantile of the marginal distribution denoted by:

$$VaR_{cl}(X) = \inf\{x \in R : F_X(x) \ge cl\}$$
(2)

while the conditional $VaR_{cl}(X)$ is a quantile of the predictive distribution for the return over the next hp days denoted by:

$$VaR_{cl,hp}^{t}(X) = \inf \left\{ x \in R : F_{X_{t+1} + \dots + X_{t+hp} | \psi_{t}}(x) \ge cl \right\}.$$
 (3)

This definition can sometimes be misleading because VaR does not actually represent maximum losses since, as we have seen, a portfolio can lose much more than suggested by VaR depending on the shape of the tail of the distribution. A more insightful definition of VaR, based on equation (2), is:

"VaR is the minimum potential loss that a portfolio can suffer in the 100(1-cl)% worst cases during a holding period,"

or

"VaR is the maximum potential loss that a portfolio can suffer in the 100cl% best cases during a holding period."

VaR can be thought of as "the best possible outcome among a set of the worst case scenarios" and, therefore, systematically underestimates the potential losses associated with any specific confidence level. Both VaR and ES contain implicit assumptions regarding agents' risk aversion. If a user has a 'well-behaved' risk-aversion function, then the weights will rise smoothly, and the more risk-averse the user, the more rapidly the weights will rise. Given that VaR explicitly weights all losses greater than that at the confidence level as zero it actually assumes that agents are risk-loving (i.e., have negative risk-aversion) in the tail region. ES, in contrast, is characterized by all losses in the tail region (i.e., the 100(1-cl)% largest losses) having an identical weight. This implies that the investor is risk-neutral in the tail region. Both assumptions seem highly unlikely in real life.

Following equation (2), the unconditional ES is defined as:

$$ES_{cl}(X) = E[X \mid X > VaR_{cl}(X)] = -cl^{-1} \int_{-\infty}^{VaR} x f(x) dx$$
 (4)

while the conditional ES can be expressed as:

$$ES_{cl,hp}^{t}(X) = E\left[\sum_{j=1}^{hp} X_{t+j} \mid \sum_{j=1}^{hp} X_{t+j} > VaR_{cl,hp}^{t}(X), \psi_{t}\right]$$
(5)

ES is very appealing as a risk measure because it sums all values of *x*, weighted by f(x), from minus infinity to VaR threshold, thus taking into account the magnitude of potential losses beyond VaR threshold. ES has been referred to in the literature under many names including Expected tail loss (ETL), Conditional VaR (CVaR), tail VaR, tail conditional expectation, and mean excess loss. ES has been used by insurance practitioners, especially casualty insurers, for a long time as conditional average claim size. For continuous loss distributions, the ES at a given confidence level is the expected loss given that the loss is greater or equal to the VaR at that level. For distributions with possible discontinuities it has a more subtle definition and can differ depending on whether the loss is strictly greater to the VaR (CVaR⁺) or is greater than or equal to the VaR (CVaR⁻). CVaR⁺ is also known as "mean shortfall", although the seemingly identical term "expected shortfall" has been interpreted by Acerbi, et al. (2001) as a synonym for CVaR itself. CVaR⁻ in also known as "tail VaR" (Artzner, et al. 1999).

Although, as discussed above, ES (CVaR) is a coherent measure of risk, it has its own problems. Yamai and Yoshiba (2002) find that even ES, although better at forecasting the true level of risk, it is not reliable during periods of market turmoil and can also give overly optimistic results. Kondor and Varga-Haszonits (2008) find that whenever there is an asset in a portfolio that dominates, with regards to risk and reward, others in a given sample, the portfolio's return cannot be maximized under any coherent measure on that sample, including ES. In periods of high volatility and/or extreme price spikes, classical, widely used VaR models prove to be overly liberal and optimistic.

One possible avenue for improving risk models' estimates lies in extreme value theory (EVT), which specifically models the extreme price changes (i.e., the tails of the return distribution). Focusing on extreme returns rather than the entire distribution seems natural since, by definition, risk management is concerned with measuring the economic impact of rare events.

EVT provides a framework for analyzing extreme (rare) events using historical data. By definition, extreme events are rare, meaning that their estimates are often required for levels of a process that are greater that those in the available data. EVT is based on the Extreme Value Theorem, a relative of the widely used Central Limit Theorem. Suppose we have a set of observed returns drawn from an unknown distribution. The EVT says that as the sample size increases, in the limit, the distribution of extreme returns converges to:

$$G_{\xi,\sigma,\mu}(x) = \begin{cases} 1 - \left(1 + \xi \frac{x - \mu}{\sigma}\right)^{-\frac{1}{\xi}} & \text{if} \quad \xi \neq 0 \\ 1 - e^{-(x - \mu)/\sigma} & \text{if} \quad \xi = 0 \end{cases} \quad x \in \begin{cases} \left[\mu, \infty\right] & \text{if} \quad \xi \geq 0 \\ \left[\mu, \mu - \sigma/\xi\right] & \text{if} \quad \xi < 0 \end{cases}$$
(6)

where, μ is the distribution mean, σ is the dispersion of the distribution and ξ indicates the heaviness of the tails.

When $\mu=0$ and $\sigma=1$, the representation is known as the standard Generalized Pareto distribution (GPD). The GPD embeds a number of other distributions. For the analysis of financial time series the most relevant is the heavy-tailed Fréchet distribution in which case the tail index, $\xi>0$.

It is important to be aware of the limitations implied by the EVT paradigm. EVT models are developed using asymptotic arguments, which can create difficulties when applied to finite samples. In order to estimate the tails of the loss distribution we use the result from asymptotic theory that for a sufficiently high threshold u, $F_u(y) \approx G_{\xi,\beta(u)}(y)$. An approximation of F(x), for X>u, can be obtained as:

$$F(x) = [1 - F(u)]G_{\varepsilon,\sigma,u}(x - u) + F(u)$$

$$\tag{7}$$

An estimate of F(u) can also be obtained non-parametrically by means of the empirical cdf:

$$\hat{F}(u) = (n - k)/n \tag{8}$$

where k represents the number of observations exceeding the threshold u and n the total number of observations. By substituting equation (7) into equation (8), the following estimate for F(x) is obtained:

$$\hat{F}(x) = 1 - \frac{k}{n} \left(1 + \hat{\xi} \frac{x - u}{\hat{\sigma}} \right)^{-\frac{1}{\xi}} \quad \text{given that } G_{\xi, \sigma, u}(x) = 1 - \left(1 + \xi \frac{x - u}{\sigma} \right)^{-\frac{1}{\xi}} \tag{9}$$

where $\hat{\xi}$ and $\hat{\sigma}$ are the maximum likelihood estimates of ξ and σ . This equation can be inverted to obtain a quantile of the underlying distribution, which is actually the VaR. For $cl \geq F(u)$ VaR is calculated as:

$$VaR_{cl} = q_{cl}(F) = u + \frac{\sigma}{\xi} \left(\left(\frac{1 - cl}{\overline{F}(u)} \right)^{-\xi} - 1 \right) = u + \frac{\sigma}{\xi} \left(\left(\frac{1 - cl}{k/n} \right)^{-\xi} - 1 \right)$$
(10)

Assuming that $\xi < 1$, ES is calculated as:

$$ES_{cl} = \frac{1}{1 - cl} \int_{cl}^{1} q_x(F) dx = \frac{VaR_{cl}}{1 - \xi} + \frac{\sigma - \xi u}{1 - \xi}.$$
 (11)

The estimation of return distributions of financial time series using the EVT has been studied by McNeil (1997); Embrechts, et. al. (1999), Danielsson and de Vries (1997); and Danielsson, Hartmann and de Vries (1998), among others. In all these papers, however, the focus has been on estimating an unconditional (stationary) distribution of asset returns. None of the unconditional EVT-based methods for quantile estimation yields estimates that are easily updated to reflect the recent volatility. Given the conditional heteroskedasticity of most

financial data, McNeil and Frey (2000) developed a conditional EVT approach combining GARCH volatility forecasting with EVT tail estimation, which in empirical testing provides very good conditional and unconditional risk coverage.

EVT models are also plagued by problems in the estimation of tail index (see, for example, Diebold, Schuermann, and Stroughair (2000)). Although a number of methods have been proposed for estimation of tail indices, none provide robust results when analyzed over changing sample periods or with the inclusion or omission of extreme values (outliers). Parametric ES estimates, even those based on the GPD distribution, are highly sensitive to functional form misspecification. Simpler parametric models cannot adequately adapt to sudden changes in volatility levels. Nonparametric ES models such as calculating the ES from historical data regarding tail losses are, by definition, unresponsive to shifts in market regimes and the occurrence of extreme events.

3 Methodology for comparing and ranking VaR and ES models

In the risk literature there are a number of methods that test the hypothesis whether a certain model is better than some other model, such as Diebold and Mariano (1995) equal predictive ability (EPA), White (2000) reality check (RC) and Hansen (2005) superior predictive ability (SPA). The question of interest in all of these tests is whether an alternative forecast is better than the benchmark forecast, or equivalently, whether the best alternative forecasting model is better than the benchmark. This question can be addressed by testing the null hypothesis that the benchmark is not inferior to any alternative forecast. For a more complete discussion on this issue, see Sullivan, Timmermann, and White (2003) and references therein. Such tests are useful for a forecaster who wants to explore whether a

better forecasting model than the model currently being used is available. After a search over several alternative models, the relevant question is whether the observed excess performance by an alternative model is significant or not. Tests for equal predictive ability (EPA), in a general setting, were proposed by Diebold and Mariano (1995) and extended by West (1996), to accommodate the situation where forecasts involve estimated parameters. A test for comparing multiple nested models was given by Harvey and Newbold (2000) and Mc-Cracken (2000) derived results for the case with estimated parameters and non-differentiable loss functions, such as the mean absolute deviation loss function. West and McCracken (1998) developed regression-based tests and other extensions were made by Harvey, Leybourne, and Newbold (1998), West (2001), and Clark and McCracken (2001) who considered tests for forecast encompassing.

There is an inherent problem with comparing and ranking competing VaR and ES models since we are usually measuring only a single realization of the underlying data generation process. The question is whether there is any significant statistical difference in the performance of different models. Although at first it might seam that the difference between models is obvious, we are often faced with situations where one model is preferred for one market or security but inferior to another model for a different sample or time period. Is it only a matter of chance that in a particular market and in particular time period a certain model performs better than some other? It all comes down to a question whether something that we subjectively perceive as different is actually statistically different. We propose a simple nonparametric approach to making statistical comparisons between competing risk models that allows us to rank different VaR and ES models depending on their performance under the metric of our choice.

The proposed ranking procedure for competing VaR/ES models is performed according to Lopez score for VaR models and modified Blanco-Ihle error statistic for ES models. The reason for using different measurement metrics stems from the simple fact that metrics intended to measure VaR performance need to measure the frequency and distance of VaR exceedances while ES metrics measure the closeness of fit between realized and forecasted excess losses. The proposed ranking procedure consists of:

- 1) Fitting an ARMA-GARCH model to the time series in order to obtain IID observations.
- 2) Estimating the empirical CDF of each time series (applying it to the non-tail regions of distribution) with a Gaussian kernel. This smoothes the CDF estimates, eliminating the staircase pattern of unsmoothed sample CDFs.
- 3) Finding the upper and lower thresholds such that x% of the residuals are reserved for each tail and fitting the amount by which those extreme residuals in each tail fall beyond the associated threshold to a parametric GPD.
- 4) Generating N simulated paths for the residuals from the obtained semi-parametric distribution (each path is T observations long)
- 5) Adding the ARMA-GARCH model to the residuals to obtain N x T simulated time series returns
- 6) Calculating VaR/ES for each of the N x T simulated returns for each VaR/ES model
- Calculating N Lopez/modified Blanco-Ihle scores for each of the N VaR/ES simulated return pairs, for each VaR/ES model
- 8) Comparing if the mean values of the Lopez/modified Blanco-Ihle scores for different VaR/ES models are significantly different from each other. For this purpose one-way ANOVA approach is employed. The purpose of one-way ANOVA is to find out whether data from several groups have a common mean. The p-value returned by ANOVA depends on assumptions about the random disturbances in the model equation. For the p-

- value to be correct, these disturbances need to be independent, normally distributed, and have constant variance.
- 9) Checking for autoregression, heteroskedasticity and normality in the Lopez/modified Blanco-Ihle scores. If the data is not normally distributed it needs to be transformed to uniform variates by empirical CDF and then to normal via inverse CDF after which one-way ANOVA can be calculated. Critical values used for the multiple comparisons are based on Tukey-Kramer honestly significant difference criterion since it is optimal for balanced one-way ANOVA. An alternative that we use in this paper is the non-parametric Kruskal-Wallis test (a nonparametric version of one-way ANOVA) which makes only mild assumptions about the data and is appropriate when the distribution of the data is non-normal. The assumption behind this test is that the measurements come from a continuous, but not necessarily a normal, distribution. The test is based on an analysis of variance using the ranks of the data values, not the data values themselves.

An obvious limitation of this approach is the assumption that the description of the central mass and the tails of the process distribution are adequate i.e. that the underlying process is well described by the visible realization. This is not an unusual or strong assumption and is made in all the models that are used in practice. We do not accept, however, that the single visible realization of the underlying process is the "ultimate truth" but, by simulating the data, allow for stochastic randomness. Even so, when thinking about the nature of forecasting one is always faced with inherent problem of forecasting the future by using only visible past data.

4 Data and backtesting methodology

We analyze the performance of the various VaR and ES models summarized in Table 1 using the log of daily returns of eight equity indices from developed markets (US - Dow Jones Industrial (DJIN), Nasdaq, S&P 500, Russell 2000 (RTY); Japan – Nikkei; Germany – DAX; France – CAC; and UK - FTSE) and eight emerging markets (Brazil – Bovespa; Russia - CRTX; India - Sensex; South Africa - Jalsh; Malaysia - KLCI; Mexico - Mexbol; Hong Kong - Heng Seng; and Taiwan - Taipei). Returns were collected from the Bloomberg website for the period January 1, 2000 through July 1, 2010. In order to differentiate between "normal" and stressed market conditions we choose two backtesting periods consisting of 750 observations each. The period between June/July 2004 and June/July 2007 forms the precrisis backtesting period, and the period between June/July 2007 and July 2010 forms the crisis backtesting period. VaR and ES figures were calculated for a one-day ahead horizon and 99 percent confidence level. Based using the proposed ranking procedure the VaR models are tested using: Kupiec test, Christoffersen Unconditional Coverage (UC), Conditional Coverage (CC) and Independence (IND) test, and Lopez and Blanco-Ihle tests as well as root mean squared error (RMSE) and mean average percentage error (MAPE) statistics. The Christoffersen UC test is problematic because it gives a distorted image of VaR models' performance. Since it is chi-square distributed with one degree of freedom, deviations from the test's expected value that occur on the conservative side (i.e. with number of exceedances lower than their expected value) are penalized more severely. characteristic is not compatible with risk-averse or risk-neutral assumptions. Thus, from the regulatory standpoint, the Kupiec binomial test is preferable to the Christoffersen UC test because it is more desirable to have positive than negative deviations. The same logic extends to Christoffersen conditional coverage (CC) test, which should also be treated

sceptically since it automatically disadvantages VaR models that err on the conservative side.

Blanco and Ihle (1998) suggested evaluating forecasts according to a loss function equal to:

$$C_{t} = \begin{cases} \frac{L_{t} - VaR_{t}}{VaR_{t}} & \text{if} \quad L_{t} > VaR_{t} \\ 0 & \text{if} \quad L_{t} \leq VaR_{t} \end{cases}$$

$$(12)$$

This loss function allows for the sizes of tail losses to influence the rankings of VaR models. Models that generate higher tail losses would generate higher values under this size-adjusted loss function than models that generate lower tail losses, *ceteris paribus*. The problem with the Blanco-Ihle loss function is that it compares the calculated VaR with tail losses, which does not make sense since VaR forecasts only the least possible tail losses. Since VaR does not contain any information about the size of the expected tail loss, the Blanco-Ihle loss function only measures the discrepancy between the lowest possible tail loss and actual tail losses. The Blanco-Ihle loss function can easily be modified to compare ES with the actual value of the tail loss, a more meaningful comparison. The modified function equals:

$$C_{t} = \begin{cases} \frac{\left| L_{t} - ES_{t} \right|}{ES_{t}} & \text{if} \quad L_{t} > VaR_{t} \\ 0 & \text{if} \quad L_{t} \leq VaR_{t} \end{cases}$$

$$(13)$$

In order to select superior ES models, each model will be graded by four symmetrical error statistics: the mean absolute error (MAE), two versions of the root mean squared error (RMSE), and the proposed ES modification of the Blanco-Ihle loss function. Among these error statistics, ES modification of the Blanco-Ihle loss function is probably the most informative, since it compares the tail loss to ES while taking into account the relative size of the tail loss compared to the difference between the two. In our two-stage backtesting procedure, the best performing VaR/ES model must first satisfy both the Kupiec and

Christoffersen independence (IND) tests and then provide superior tail loss forecasts, in the sense of minimizing the error statistics.

5 Backtesting results and findings

To secure the same out-of-the-sample backtesting period for all of the examined stock indices, the out-of-the-sample data sets are formed by removing the 1.500 most recent observations from each stock index and forming two sub-periods of 750 days. The first sub-period from June/July 2004 to June/July 2007 represents the pre-crisis period. The second sub-period from June/July 2007 to July 2010 represents the crisis period. The remaining observations are used to calculate the VaR and ES starting values and calibrate volatility. The length of the tail-loss data set used for backtesting depends on the number of errors generated by each VaR model. The quality of ES forecasts depends on both the ES estimation model and the quality of the VaR forecast. This dependence can be easily seen from the simple fact that a loss that might fall in the extreme range under one VaR model and, as such, be included in the ES forecast might not exceed another, more conservative, VaR measure.

Data from all the analyzed stock indices shows leptokurtosis, asymmetry and significant heteroskedasticity, with autoregression being especially pronounced in the emerging markets. Based on the Akaike and Bayesian information criterion asymmetric EGARCH representation of volatility with GED and Student's *t* distribution was used to capture the dynamics of data-generating processes. The asymmetry parameter in the EGARCH model was significantly different from zero for most of the indexes.² The asymmetry parameter, which controls the asymmetric impact of positive and negative shocks

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² For the BOVESPA, CRTX, JALSH, KLCI and HENG SENG indices the asymmetric impact is not significantly different from zero. Results are available from the authors on request.

on conditional variance, indicates significantly higher conditional volatility after negative shocks.

Estimation of the tail index parameter is crucial in applying EVT models, which are directly linked to threshold value u which defines the level above which returns are considered extreme. The threshold value for each index was determined by comparing the Hill estimator with the mean excess plot and the quantile-quantile (QQ) plot (Danielsson and de Vries, 1997). The same procedure of estimating the threshold value was also performed on IID innovations required for the implementation of the McNeil and Frey (2000) EVT-GARCH model. Maximum likelihood estimates (MLE) of the shape (tail index) and scale (sigma) parameters for the GPD, during the pre-crisis and crisis period, for the analyzed stock indices' threshold losses (losses surpassing the threshold value set by Hill estimator), and threshold innovations are presented in Table 2. The mean excess and QQ plots, Hill estimator and MLE all show that tail indexes for both developed and emerging countries are greater than zero, implying empirically fat tails and that the GPD belongs to the Fréchet and Gumbel domains of attraction. This clearly shows that the normal distribution is inappropriate for modelling tail returns. In the pre-crisis period the tail indexes vary between -0.195 (FTSE) and 0.129 (NIKKEI) for the developed markets and between -0.074 (MEXBOL) and 0.173 (HENG SENG) for the emerging markets. During the crisis most of the tail indexes changed substantially and ranged between -0.042 (NASDAQ) and 0.18 (S&P500) for the developed markets and between -0.099 (MEXBOL) and 0.251 (JALSH) for the emerging markets. The greatest changes in the size of the tail index between the two periods were recorded for FTSE (0.253) and CRTX (0.214). The distribution of tail losses for the stock indices in South Africa, Hong Kong and Russia shows that they may not even have a finite fourth moment, since the estimated tail index is around 0.25³. The tails of the innovations from the analysed time series are similar to the values of returns. Since we are measuring the tail index of the extreme left (negative) tail of the distribution of returns, the impact of severe crashes in the stock markets is directly reflected in the increased size of the extreme left tail. The visible change in the fatness of the left tail (high tail index) in the majority of markets is a clear warning sign that the dynamics of the markets have shifted towards a more extreme end of the spectrum.

As is visible from table 3a, during the pre crisis period, in both developed and emerging markets, satisfactory performance with regards to Basel and independence criteria is recorded for nonparametric models (HS, MHS and KHS) as well as FHS and extreme value based approaches. Very weak performance is recorded for BRW, VCV, RiskMetrics and Hull-White models. As we shall see, the performance of the tested VaR models is significantly different during the crisis period. In developing markets good performance is recorded for the Hull-White, GPD and EVT-GARCH models.

For the crisis period, for which the VaR models performance with regards to Basel and independence criteria is presented in table 3b, we make a distinction between the standard EVT GARCH model and EVT GARCH (L) model, where L stands for a longer time series. We introduce two EVT GARCH models and this notation because we find an interesting pattern of behaviour – if we use the standard rolling window for GARCH parameters (calculated just in the crisis period) and from that calculate standardized innovations, EVT GARCH forecasts are very poor. This is due to the very thin tail indicated by fitting the GPD. If, instead, we use a longer period such as 6 years, results are much better since the GPD tail is closer to what we might expect. At first sight this finding indicates

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³ For $\xi > 0$, $E[X^k]$ is infinite for $k > 1/\xi$. The number of finite moments is ascertained by the value of ξ : if $0.25 \le \xi \le 0.5$ the second and higher moments are infinite; if $\xi \le 0.25$, the fourth and higher moments are infinite.

counter-intuitive behaviour (if we are using newer information we should have better volatility forecasts ergo better risk measures). In reality, if we are using a very accurate volatility forecast reflecting the current environment there is a lack of outliers and standardized innovations are bunched around zero with their tails exponentially decreasing. When calculating GPD parameters from such a innovation series it is logical to obtain low, or even negative, estimates of the tail parameter. The paradox lies in the fact that if the volatility estimate is fairly good but not perfect there will be outliers in the standardized innovations series which will lead to higher a GPD tail index and thus actually increase the accuracy of EVT GARCH VaR forecasts. In emerging markets only the EVT GARCH (L) and MHS 250 models performed satisfactorily, again with a clear distinction between standard and prolonged EVT GARCH models.

Overall we find good performance across both developed and emerging markets for extreme value based approaches. Mirrored historical simulation, a simple extension of historical simulation, yielded surprisingly good risk coverage and satisfied the backtesting criteria for a great majority of stock indices tested. Backtest results also show that the kernel historical approach VaR estimator, although inferior to mirrored historical simulation, delivers significant variance and mean square error reductions when compared to plain historical simulation. This difference is similar to that found by Song and Tang (2005).

It is also useful to analyze the averages of VaR forecasts for the models that satisfy the Basel II/III-required Kupiec test as well as the Christoffersen independence criterion. Rankings according to the minimum average VaR value (provided the Basel II/III criteria and Christoffersen independence test at a 5 percent significance level are satisfied) are presented in Table 4. For all of the indices in both developed and emerging markets, GPD and HW models provide the highest VaR estimates, with HW providing very high values during the crisis period. This characteristic makes them the most conservative but also the most

expensive in terms of capital requirements for financial institutions. During the precrisis period for the developed markets, the GARCH model yielded the lowest average VaR four out of eight times (Nikkei, DAX, CAC and FTSE index) followed by BRW simulation with a decay factor of 0.99, which was the best performer in two cases (DJIN and Nasdaq index). For emerging markets, the performance of GARCH model is even better, yielding the lowest average VaR for five out of eight indices (BOVE, Mexbol, KLCI, SENSEX and Heng Seng index). During the crisis period for the developed countries EVT GARCH (L) was the top performer (S&P 500, DJI, NASDAQ and FTSE index), followed by FHS model (RTY, Nikkei, DAX). For emerging markets, both GARCH and FHS models were the best performers for three indexes. In summary, among VaR models that satisfy the Basel criteria, the FHS and GARCH models provided the lowest average VaR in most cases, making them the models with the lowest opportunity cost of holding idle capital. Results of the Lopez size adjusted test, presented in tables 5a and 5b, are very similar to the minimal average VaR values, especially in the crisis period with the EVT-GARCH model having the best Lopez score in the developed markets and FHS model having the best score in the emerging markets.

According to the conventional investment logic one might expect that the performance of VaR models is better adapted to developed and liquid markets than emerging ones. Our backtesting results during the crisis period, however, show quite the opposite. Nonparametric models (especially mirrored HS models), as well as parametric GARCH and FHS models, perform far better in emerging markets than developed ones. These results confirm that regulators and investors should change their traditional perception that since emerging markets are more volatile and less developed they need more robust risk measures, while VaR models are adequate for "tranquil" and "well behaved" developed markets. One explanation for such nonconformist VaR performance is based on the simple fact that since

the emerging markets are usually more volatile and experience more frequent market crashes, parameters of VaR models are more attuned to such events. Thus, if the observation windows used for nonparametric VaR models are long enough, they will contain a significant number of past crashes and parameters of the classical parametric and EVT VaR models will be more in line with the volatile and crash prone environment. On the other hand, developed markets, having experienced positive and steady growth for almost a decade, mislead the VaR models by lacking high volatility and crashes in the information set. In such circumstances, regulators and investors should be even more worried about the reality and usefulness of traditional VaR risk measures when applied to portfolios containing mostly stocks from developed markets as opposed to emerging ones.

To backtest the various ES models, we ranked the models by their ability to yield minimal loss functions, i.e. the minimum departure from the reported tail loss values. Rankings of the ES models according to modified Blanco-Ihle error statistics at the 99 percent confidence level are presented in Table 6. According to the modified Blanco-Ihle statistic, in the pre-crisis period, both in the developed and emerging markets, the bootstrapped MHS model was the best performing ES model. In the developed markets the basic bootstrap historical simulation model followed closely. In emerging markets, bootstrapped FHS and GPD model were ranked as second and third performers. The worst performers across all the markets were the VCV, RiskMetrics and GARCH models with GPD distribution. During the crisis period, both in the developed and emerging markets bootstrapped FHS, MHS and EVT GARCH were the best performing ES models. The worst performing models were again the VCV, RiskMetrics and GARCH models with GPD distribution.

In summary, backtesting results show that bootstrapped mirrored historical simulation is the superior ES measure. We find no benefit to using a kernel approach instead of

bootstrapped historical simulation. This finding is similar to that reported in Song (2008) for plain historical simulation. The underlying reason that there is no benefit from kernel smoothing of ES estimates lies in the fact that the unconditional ES is a mean parameter, which can be estimated accurately by simple averaging and therefore does not call for additional data smoothing. It is also interesting to note that, although historical simulation models are clearly inferior to EVT models in VaR estimation, in ES estimation bootstrapping historical exceedances over VaR performs better than theoretically well-founded EVT models.

Going beyond standard VaR/ES performance reporting, we apply the methodology presented in section 3 to test whether there is any statistically significant difference in the performance of the various VaR and ES models. The data is simulated based on the distribution of returns in the crisis period. For each index, 2,000 simulations were performed with length of each simulated index being 1.000 data points. Since we are using Lopez size adjusted score (modified Blanco-Ihle) metrics for VaR (ES) model comparison, the closer the score of an individual model is to zero, the better the performance. After obtaining 2,000 Lopez size adjusted (modified Blanco-Ihle) scores for each VaR (ES) model and for each of sixteen index data generating processes we apply a non-parametric Kruskal-Wallis test to determine the existence of statistically significant differences between competing VaR (ES) models. Results are reported in Table 7. If the simulated mean value of the VaR(ES) model lies outside of the 95% confidence interval of all the other tested models that model is ranked according to its relative performance. If a model is not significantly different from all the other models it shares the same ranking as the models not significantly different from it. Analysing the VaR model performance on simulated data, presented in table 7a, for a large number of different models there is no statistical difference in their performance. When looking at overall performance in the developed markets the best performing VaR model that is statistically different from other tested models is the conditional EVT GARCH model, followed by the unconditional GPD model. Even in the summary results across eight developed markets there is no statistical difference between the FHS and BRW (λ =0.99) models. In the emerging markets overall the best model is MHS 250, followed by EVT GARCH model. Similarly to the developed markets there is again an overlapping between the FHS and MHS 500 models. The statistically worst performing VaR models across both markets are the simplest models, the Normal VCV, plain historical simulation and RiskMetrics models. Overall, the statistically significant top performers are conditional EVT GARCH, models based on volatility updating (HW and FHS) and nonparametric mirrored historical simulation. Since our metric of choice is the size adjusted Lopez score, these models provide the closest fit to the actual level of risk encountered in the analysed markets.

ES backtesting results are similar to VaR results with the models being even more closely matched. A noticeable difference from the VaR results is that the mirrored historical simulation model is similar in rank or even superior to the conditional EVT GARCH model. In the developed markets the best ES models were MHS 250 and FHS followed by conditional and unconditional extreme value based models. In the emerging markets EVT GARCH is the best performing model followed by both MHS models and FHS. Again the same models that were the top performers in the VaR comparison perform significantly better then other tested models. We find no benefit to using a kernel approach instead of bootstrapped historical simulation. It is interesting to note that, although historical simulation models are clearly inferior to EVT models in VaR estimation, in ES estimation bootstrapping historical exceedances over VaR often perform better than theoretically better-founded EVT models.

6 Conclusion

Our findings show that the mainstream opinion that VaR models are better adapted to developed and liquid markets as opposed to the emerging ones is ill founded, especially during a crisis period. Regulators, as well as investors, should change their misperception that since, emerging markets are more volatile and less developed, only they need more robust risk measures and using VaR models is adequate for "tranquil" and "well behaved" developed markets. A protracted period of prosperity and tranquillity is precisely why VaR models underperform especially severely during the crisis in the developed markets. Such circumstances mislead VaR models in the developed markets since, unlike the emerging markets, they lack sever volatility and crashes in the information set used in parameter estimation. In such circumstances regulators should be even more wary about the usefulness of traditional VaR risk measures when applied to portfolios containing mostly stocks from developed markets. As our results warn, greater attention must be given to realistically modelling the tails of the distribution and choosing the most realistic approach to VaR and ES modelling even if it means lower investment profits. Although the industry is opposing such moves, due to inevitable rise in required capital reserves and lower short-term profitability, in order to construct a sound risk management framework regulators must take into account the fragility VaR models which also extends to a degree to ES models. As we show there is far less difference between competing VaR/ES models than thought and only a few models are significantly superior. Our results cast doubt on VaR/ES model comparison studies since they mostly measure the performance of the analysed risk models on a single realization od the data generating process. As we have shown such evaluation of model performance can often be misleading.

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Appendix

Table 1 Overview of VaR and ES models

Model	VaR	ES	Description
Historical simulation	$VaR^{cl} = F^{-1}(cl) = X_{(i)}$	$ES^{cl} = \left(\sum_{i=[ncl]}^{n} X_{n(i)}\right) / (n - [ncl])$	$F_n(t) = \frac{1}{n} \sum_{i=1}^n I(X_i \le t)$
Mirrored HS	$Y_i = X_i $ $VaR^{cl} = F^{-1}(cl) = Y_{(i)}$	$ES^{cl} = \left(\sum_{i=[ncl]}^{n} Y_{n(i)}\right) / (n - [ncl])$	
Kernel HS	$G(x) = \sum_{k=0}^{N} \frac{N!}{k!(N-k)!} g(x)$ $VaR^{l} = (r \in \{r_{l-1},, r_{l-1-N}\} \mid G(r, t, N) \ge cl)$	$ES^{cl} = \left(\sum_{i=[ncl]}^{n} X_{n(i)}\right) / (n - [ncl])$	$\hat{f}(x) = (1/nh) \sum_{i=1}^{n} K((x - X_i)/h)$ $g(x) = F(x)^k (1 - F(x))^{N-k}$
BRW simulation	$G(x;t,N) = \sum_{i=1}^{N} 1_{\{r_{t-i} \le x\}} w_{t-i}$ $VaR_{i}^{cl} = (r \in \{r_{t-1}, \dots r_{t-1-N}\} \mid G(r;t,N) \ge cl)$	$ES_{t}^{cl} = \left(\sum_{i=[ncl]}^{n} X_{n(i)}\right) / (n - [ncl])$	$\{w\} = \frac{1-\lambda}{1-\lambda^N}, \dots, \left(\frac{1-\lambda}{1-\lambda^N}\right)\lambda^{N-1}$
VCV	$VaR_t^{cl} = (r \in \{r_{t-1}, \dots r_{t-1-N}\} \mid G(r, t, N) \ge cl)$ $VaR_t^{cl} = \mu_t + \sigma_t \alpha_{cl}$	$ES_t^{cl} = \mu_t + \sigma_t E[Z \mid Z < z_{cl}]$	$\sigma_t = \sqrt{\frac{1}{T} \sum_{t=1}^{T} (r_t - \overline{r})^2}$
RiskMetrics	$VaR_t^{cl} = \mu_t + \sigma_t \alpha_{cl}$	$ES_t^{cl} = \mu_t + \sigma_t E[Z \mid Z < z_{cl}]$	$\sigma_t = \sqrt{0.94\sigma_{t-1}^2 + 0.06\varepsilon_t^2}$
GARCH	$VaR_t^{cl} = \mu_t + \sigma_t \alpha_{cl}$	$ES_t^{cl} = \mu_t + \sigma_t E[Z \mid Z < z_{cl}]$	$\sigma_t^2 = \alpha_0 + \sum_{i=1}^q \alpha_i \varepsilon_{t-i}^2 + \sum_{i=1}^p \beta_i \sigma_{t-i}^2$
FHS	$VaR^{l} = (r \in \{r_{t-1},, r_{t-1-N}\} \mid G(r, t, N) \ge cl)$	$ES_t^{cl} = \left(\sum_{i=[ncl]}^n \hat{Z}_{n(i)}\right) / (n - [ncl])$	$\begin{aligned} z_t &= \varepsilon_t / \sigma_t \hat{z}_{t+1} = z_t \times \hat{\sigma}_{t+1} \\ \hat{r}_{t+1} &= \alpha_0 + \sum_{i=1}^p \alpha_i r_{t-i+1} + \sum_{i=1}^q \theta_i \hat{z}_{t-i+1} + \hat{z}_{t+1} \end{aligned}$
Unconditional GPD	$VaR^{sl} = q^{cl}(F) = u + \frac{\sigma}{\xi} \left(\left(\frac{1 - cl}{\overline{F}(u)} \right)^{-\xi} - 1 \right)$	$E\xi^{el} = \frac{1}{1 - cI} \int_{cI}^{1} q_x(F) dx = \frac{VaR_{el}}{1 - \xi} + \frac{\sigma - \xi u}{1 - \xi}$	
Conditional GPD (McNeil, Frey)	$VaR_t^{cl} = \mu_t + \sigma_t VaR(Z)_{cl}$	$ES_{t}^{cl} = \mu_{t} + \sigma_{t}ES(Z)^{cl}$ $ES(Z)^{cl} = \frac{VaR_{cl}}{1 - \xi} + \frac{\sigma - \xi u}{1 - \xi}$	$\sigma_{t}^{2} = \alpha_{0} + \sum_{i=1}^{q} \alpha_{i} \varepsilon_{t-i}^{2} + \sum_{i=1}^{p} \beta_{i} \sigma_{t-i}^{2}$ $Z = \left(\frac{x_{t-n+1} - \mu_{t-n+1}}{\sigma_{t-n+1}}, \dots, \frac{x_{t} - \mu_{t}}{\sigma_{t}}\right)$ $VaR(Z)^{cl} = u_{Z} + \frac{\sigma_{Z}}{\xi_{Z}} \left(\left(\frac{1 - cl}{\overline{F}(u_{Z})}\right)^{-\xi_{Z}} - 1\right)$

Table 2a Maximum likelihood estimates of shape and scale parameter of the GPD for negative returns and innovations, 750 observations, period June/July 2004 - June/July 2007

		Returns		l	nnovation	ıs		Returns		lı	novation	ıs
	estimate	s.e.	threshold	estimate	s.e.	threshold	estimate	s.e.	threshold	estimate	s.e.	threshold
		DAX (09	.08.2004 - 1	6.07.2007)				BOVE	SPA (03.06.	2004 - 14.0	6.2007)	
Tail index	-0,037	0,094	2,518	0,017	0,137	1,610	0,061	0,147	3,569	0,042	0,144	1,508
Sigma	1,189	0,161		0,531	0,102		1,010	0,204		0,535	0,107	
		CAC (20.	08.2004 - 2	4.07.2007)				SENS	EX (17.06.2	2004 - 14.06	.2007)	
Tail index	0,014	0,096	2,175	0,199	0,166	2,017	0,055	0,146	3,273	-0,092	0,126	1,476
Sigma	0,993	0,134		0,431	0,093		1,266	0,255		0,828	0,155	
		FTSE (23	.07.2004 - 1	2.07.2007)				CRT	X (01.06.20	04 - 18.06.2	007)	
Tail index	-0,195	0,112	2,246	-0,029	0,120	1,344	-0,012	0,137	4,934	-0,100	0,125	1,510
Sigma	1,231	0,217		0,645	0,111		1,987	0,387		0,775	0,144	
		NIKKEI (2	0.05.2004 -	06.06.2007)			JALS	SH (01.07.20	004 - 29.06.	2007)	
Tail index	0,129	0,157	2,757	0,016	0,141	1,593	0,146	0,159	2,209	0,014	0,141	1,509
Sigma	0,741	0,154		0,660	0,130		0,800	0,168		0,636	0,126	
		DJIN (16.	.07.2004 - 1	0.07.2007)				KLC	CI (08.06.20	04 - 19.06.2	007)	
Tail index	0,102	0,112	1,625	0,167	0,145	1,396	0,049	0,162	1,781	0,263	0,175	1,448
Sigma	0,682	0,101		0,475	0,090		0,911	0,250		0,438	0,097	
		SP500 (16	6.07.2004 - <i>′</i>	10.07.2007)				MEXE	OL (20.07.2	2004 - 05.07	.2007)	
Tail index	0,062	0,147	2,252	0,124	0,156	1,502	-0,074	0,128	2,659	0,078	0,150	1,632
Sigma	0,656	0,133		0,516	0,107		1,230	0,232		0,499	0,102	
	N	IASDAQ (*	16.07.2004 -	10.07.2007	7)			HENG S	SENG (02.06	5.2004 - 13.0	06.2007)	
Tail index	-0,013	0,116	3,335	0,045	0,130	1,425	0,173	0,119	2,050	-0,086	0,127	1,558
Sigma	1,031	0,224		0,522	0,093		0,762	0,118		0,627	0,118	
		RTY (16.	07.2004 - 10	0.07.2007)				TAIP	EI (15.06.20	004 - 27.06.	2007)	
Tail index	0,082	0,107	2,127	0,028	0,142	1,568	0,002	0,139	3,212	0,027	0,142	1,419
Sigma	0,630	0,092		0,475	0,094		0,944	0,196		0,772	0,153	

Table 2b Maximum likelihood estimates of shape and scale parameter of the GPD for negative returns and innovations, 750 observations, period June/July 2007 – July 2010

		Returns		lı	nnovation	ıs		Returns		lı	novation	ıs
	estimate	s.e.	threshold	estimate	s.e.	threshold	estimate	s.e.	threshold	estimate	s.e.	threshold
		DAX (17.	.07.2007 - 0	1.07.2010)				BOVES	SPA (15.06.	2007 - 01.0	7.2010)	
Tail index	0,111	0,078	2,697	0,007	0,116	1,250	0,132	0,157	4,263	-0,146	0,118	1,622
Sigma	1,472	0,172		0,622	0,102		1,393	0,291		0,566	0,103	
		CAC (25.	07.2007 - 0	1.07.2010)				SENS	EX (15.06.2	007 - 01.07	.2010)	
Tail index	0,031	0,143	3,851	0,250	0,173	2,172	0,067	0,148	4,094	0,015	0,141	1,448
Sigma	1,130	0,225		0,420	0,092		1,367	0,277		0,620	0,122	
		FTSE (13.	.07.2007 - 0	1.07.2010)				CRT	X (19.06.20	07 - 01.07.2	2010)	
Tail index	0,058	0,125	2,722	-0,118	0,162	1,524	0,202	0,167	6,226	-0,071	0,129	1,394
Sigma	1,185	0,203		0,647	0,145		2,407	0,518		0,674	0,127	
		NIKKEI (07	7.06.2007 -	01.07.2010)			JALS	SH (02.07.20	07 - 01.07.	2010)	
Tail index	0,076	0,149	3,421	0,048	0,206	1,879	0,251	0,173	3,077	-0,122	0,107	1,431
Sigma	1,633	0,332		0,425	0,109		0,781	0,171		0,510	0,083	
		DJIN (11.	07.2007 - 0	1.07.2010)				KLC	1 (20.06.200	7 - 01.07.2	010)	
Tail index	0,000	0,139	2,911	-0,234	0,069	1,019	0,093	0,152	1,983	0,077	0,149	1,381
Sigma	1,365	0,268		0,831	0,097		1,151	0,236		0,668	0,136	
		SP500 (11	.07.2007 - 0	01.07.2010)			MEXB	OL (06.07.2	2007 - 01.07	'.2010)	
Tail index	0,180	0,164	3,128	-0,011	0,170	2,020	-0,099	0,115	3,368	-0,089	0,098	1,204
Sigma	1,189	0,253		0,560	0,085		1,201	0,206		0,686	0,100	
	N	IASDAQ (1	11.07.2007 -	01.07.201	0)			HENG S	ENG (14.06	5.2007 - 01.	07.2010)	
Tail index	-0,042	0,133	4,264	-0,065	0,139	1,688	0,218	0,169	3,776	-0,073	0,109	1,376
Sigma	1,536	0,295		0,614	0,105		1,235	0,267		0,504	0,081	
		RTY (11.	07.2007 - 0 ⁻	1.07.2010)				TAIP	EI (28.06.20	07 - 01.07.	2010)	
Tail index	0,061	0,147	3,608	0,152	0,204	1,966	-0,047	0,094	3,129	-0,169	0,093	1,309
Sigma	1,562	0,316		0,350	0,094		0,989	0,135		0,732	0,106	

Table 3a Number of VaR model successes according to Kupiec and Christoffersen independence tests at 5 and 10% significance level, 99% confidence level, 750 observations (June/July 2004 - June/July 2007)

			Developed	l markets	(8)			
	HS 250	HS 500	MHS 250	MHS 500	KHS 250	KHS 500	BRW λ=0,97	BRW λ=0,99
Kupiec test*	5	8	8	8	8	8	2	7
Kupiec test**	2	8	8	8	8	8	1	7
Independence***	8	7	7	7	7	7	7	5
	VCV	Risk Metrics	GARCH	FHS	HW	EVT GARCH	GPD	
Kupiec test*	2	1	6	8	2	8	8	
Kupiec test**	2	1	6	8	1	8	8	
Independence***	7	3	8	8	6	8	8	
			Emerging	markets	(8)			
	HS 250	HS 500	MHS 250	MHS 500	KHS 250	KHS 500	BRW λ=0,97	BRW λ=0,99
Kupiec test*	7	6	8	8	8	8	3	8
Kupiec test**	5	6	8	8	8	7	2	6
Independence***	6	6	6	6	7	5	8	7
	VCV	Risk Metrics	GARCH	FHS	HW	EVT GARCH	GPD	
Kupiec test*	2	0	5	8	3	8	8	
Kupiec test**	0	0	2	8	2	8	8	
Independence***	5	5	8	8	7	8	8	

^{* 5%} significance level

HS n – historical simulation model with n day moving window; MHS n – "mirrored" historical simulation model with n day moving window; KHS n – kernel historical approach with n day moving window; BRW - Boudoukh, Richardson, Whitelaw (time weighted) simulation model, λ - decay factor; VCV – normally distributed variance-covariance model; GARCH – parametric EGARCH(p, q) model with GED or T distributed innovations; FHS – Filtered historical simulation Barone-Adesi et. al. (1999); HW – Hull-White (1998) model; EVT-GARCH – McNeil, Frey (2002) conditional EVT model, GPD – unconditional EVT model using Generalized Pareto distribution;

Table 3b Number of VaR model successes according to Kupiec and Christoffersen independence tests at 5 and 10% significance level, 99% confidence level, 750 observations (June/July 2007 – July 2010)

^{** 10%} significance level

^{***} Christoffersen (1998) independence tests at 5% significance level

			Develop	ed marke	ets (8)			
	HS 250	HS 500	MHS 250	MHS 500	KHS 250	KHS 500	BRW λ=0,97	BRW λ=0,99
Kupiec test*	0	0	1	1	1	1	0	3
Kupiec test**	0	0	1	0	1	0	0	2
Independence***	7	6	8	8	8	7	8	8
	VCV	Risk Metrics	GARCH	FHS	HW	EVT GARCH	EVT GARCH (L)	GPD
Kupiec test*	0	0	1	3	7	2	8	8
Kupiec test**	0	0	1	0	7	2	8	7
Independence***	6	8	8	8	5	8	7	8
			Emergir	ng marke	ts (8)			
	HS 250	HS 500	MHS 250	MHS 500	KHS 250	KHS 500	BRW λ=0,97	BRW λ=0,99
Kupiec test*	1	1	8	6	5	1	0	5
Kupiec test**	1	1	7	6	2	1	0	5
Independence***	6	5	7	6	7	6	7	6
	VCV	Risk Metrics	GARCH	FHS	HW	EVT GARCH	EVT GARCH (L)	GPD
Kupiec test*	0	0	4	6	5	3	8	6
Kupiec test**	0	0	4	5	4	3	6	6
Independence***	6	6	8	8	5	8	8	7

^{* 5%} significance level

Table 4a VaR ranking according to minimal average VaR values, 99% confidence level, 750 observations (June/July 2004 - June/July 2007)

^{** 10%} significance level

^{***} Christoffersen (1998) independence tests at 5% significance level

	S&P 500	DJIN	NASDAQ	RTY	NIKKEI	FTSE	DAX	CAC
HS 250	1,55	1,57	2,07	2,40	2,85	1,81	2,35	2,25
HS 500	1,70	1,73	2,35	2,50	3,12	1,98	2,85	2,51
MHS 250	1,72	1,76	2,26	2,66	3,05	1,94	2,48	2,35
MHS 500	2,00	2,04	2,64	2,69	3,22	2,30	3,08	2,81
KHS 250	1,63	1,66	2,23	2,59	3,06	1,92	2,53	2,37
KHS 500	1,78	1,78	2,44	2,59	3,26	2,08	2,93	2,60
BRW λ=0,97	1,50	1,48	2,01	2,30*	2,67	1,62	2,21	2,02
BRW λ=0,99	1,60**	1,62**	2,13	2,46	2,97	1,85	2,44	2,33
Normal VCV	1,51	1,49	2,11	2,47	2,56	1,51	2,04	1,86
Risk Metrics	1,46*	1,43*	1,95**	2,32	2,33*	1,47*	1,93*	1,79
GARCH	1,52	1,49	1,99	2,38	2,48**	1,51**	2,00**	1,86*
HW	1,76	1,70	2,10	2,59	3,38	2,24	2,60	2,54
FHS	1,81	1,75	2,30	2,67	2,68	1,83	3,07	2,06
EVT GARCH	2,07	2,06	2,24	2,37	3,34	1,78	2,16	2,73
GPD	3,44	3,29	3,90	3,45	4,22	2,84	3,44	3,28
	JALSH	BOVE	MEXBOL	KLCI	CRTX	SENSEX	H SENG	TAIPEI
HS 250	JALSH 2,65	BOVE 3,94	MEXBOL 2,92	KLCI 1,53	CRTX 6,04	SENSEX 3,68	H SENG 2,37	TAIPEI 3,39
HS 250 HS 500								
	2,65	3,94	2,92 2,74 3,40	1,53	6,04	3,68	2,37	3,39
HS 500	2,65 2,51	3,94 4,07	2,92 2,74	1,53 1,58	6,04 5,82	3,68 3,58	2,37 2,38	3,39 3,42
HS 500 MHS 250	2,65 2,51 3,26	3,94 4,07 4,35	2,92 2,74 3,40	1,53 1,58 1,82	6,04 5,82 6,92	3,68 3,58 4,37	2,37 2,38 2,54	3,39 3,42 3,63
HS 500 MHS 250 MHS 500	2,65 2,51 3,26 3,15	3,94 4,07 4,35 4,61	2,92 2,74 3,40 3,28	1,53 1,58 1,82 1,96	6,04 5,82 6,92 6,50	3,68 3,58 4,37 4,01	2,37 2,38 2,54 2,71	3,39 3,42 3,63 4,07
HS 500 MHS 250 MHS 500 KHS 250	2,65 2,51 3,26 3,15 2,85	3,94 4,07 4,35 4,61 4,23	2,92 2,74 3,40 3,28 3,12	1,53 1,58 1,82 1,96 1,64	6,04 5,82 6,92 6,50 6,56	3,68 3,58 4,37 4,01 4,03	2,37 2,38 2,54 2,71 2,51	3,39 3,42 3,63 4,07 3,58
HS 500 MHS 250 MHS 500 KHS 250 KHS 500	2,65 2,51 3,26 3,15 2,85 2,75	3,94 4,07 4,35 4,61 4,23 4,23	2,92 2,74 3,40 3,28 3,12 2,83	1,53 1,58 1,82 1,96 1,64 1,66	6,04 5,82 6,92 6,50 6,56 6,06	3,68 3,58 4,37 4,01 4,03 3,74	2,37 2,38 2,54 2,71 2,51 2,47	3,39 3,42 3,63 4,07 3,58 3,57
HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW λ=0,97	2,65 2,51 3,26 3,15 2,85 2,75 2,41	3,94 4,07 4,35 4,61 4,23 4,23 3,75	2,92 2,74 3,40 3,28 3,12 2,83 2,64	1,53 1,58 1,82 1,96 1,64 1,66 1,45	6,04 5,82 6,92 6,50 6,56 6,06 5,52	3,68 3,58 4,37 4,01 4,03 3,74 3,35	2,37 2,38 2,54 2,71 2,51 2,47 2,27	3,39 3,42 3,63 4,07 3,58 3,57 2,85
HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW \(\lambda = 0,97 \) BRW \(\lambda = 0,99 \)	2,65 2,51 3,26 3,15 2,85 2,75 2,41 2,69	3,94 4,07 4,35 4,61 4,23 4,23 3,75 4,08	2,92 2,74 3,40 3,28 3,12 2,83 2,64 2,94	1,53 1,58 1,82 1,96 1,64 1,66 1,45	6,04 5,82 6,92 6,50 6,56 6,06 5,52 6,28	3,68 3,58 4,37 4,01 4,03 3,74 3,35 3,83	2,37 2,38 2,54 2,71 2,51 2,47 2,27 2,47	3,39 3,42 3,63 4,07 3,58 3,57 2,85 3,41
HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW \(\lambda = 0,97 \) BRW \(\lambda = 0,99 \) Normal VCV	2,65 2,51 3,26 3,15 2,85 2,75 2,41 2,69 2,32*	3,94 4,07 4,35 4,61 4,23 4,23 3,75 4,08 3,64	2,92 2,74 3,40 3,28 3,12 2,83 2,64 2,94 2,53	1,53 1,58 1,82 1,96 1,64 1,66 1,45 1,59	6,04 5,82 6,92 6,50 6,56 6,06 5,52 6,28 4,85	3,68 3,58 4,37 4,01 4,03 3,74 3,35 3,83 3,18	2,37 2,38 2,54 2,71 2,51 2,47 2,27 2,47 2,05	3,39 3,42 3,63 4,07 3,58 3,57 2,85 3,41 2,54 **
HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW \(\lambda = 0,97 \) BRW \(\lambda = 0,99 \) Normal VCV Risk Metrics	2,65 2,51 3,26 3,15 2,85 2,75 2,41 2,69 2,32* 2,24	3,94 4,07 4,35 4,61 4,23 4,23 3,75 4,08 3,64 3,37*	2,92 2,74 3,40 3,28 3,12 2,83 2,64 2,94 2,53 2,47*	1,53 1,58 1,82 1,96 1,64 1,66 1,45 1,59 1,35	6,04 5,82 6,92 6,50 6,56 6,06 5,52 6,28 4,85 4,45*	3,68 3,58 4,37 4,01 4,03 3,74 3,35 3,83 3,18 2,79*	2,37 2,38 2,54 2,71 2,51 2,47 2,27 2,47 2,05 1,95*	3,39 3,42 3,63 4,07 3,58 3,57 2,85 3,41 2,54 ** 2,18*
HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV Risk Metrics GARCH	2,65 2,51 3,26 3,15 2,85 2,75 2,41 2,69 2,32* 2,24 2,33	3,94 4,07 4,35 4,61 4,23 4,23 3,75 4,08 3,64 3,37* 3,49**	2,92 2,74 3,40 3,28 3,12 2,83 2,64 2,94 2,53 2,47* 2,59 **	1,53 1,58 1,82 1,96 1,64 1,66 1,45 1,59 1,35 1,31*	6,04 5,82 6,92 6,50 6,56 6,06 5,52 6,28 4,85 4,45*	3,68 3,58 4,37 4,01 4,03 3,74 3,35 3,83 3,18 2,79* 2,84**	2,37 2,38 2,54 2,71 2,51 2,47 2,27 2,47 2,05 1,95* 2,08 **	3,39 3,42 3,63 4,07 3,58 3,57 2,85 3,41 2,54 ** 2,18*
HS 500 MHS 250 MHS 500 KHS 250 KHS 250 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV Risk Metrics GARCH HW	2,65 2,51 3,26 3,15 2,85 2,75 2,41 2,69 2,32* 2,24 2,33 3,80	3,94 4,07 4,35 4,61 4,23 4,23 3,75 4,08 3,64 3,37* 3,49** 4,20	2,92 2,74 3,40 3,28 3,12 2,83 2,64 2,94 2,53 2,47* 2,59** 4,33	1,53 1,58 1,82 1,96 1,64 1,66 1,45 1,59 1,35 1,31* 1,36** 2,29	6,04 5,82 6,92 6,50 6,56 6,06 5,52 6,28 4,85 4,45* 4,62 7,06	3,68 3,58 4,37 4,01 4,03 3,74 3,35 3,83 3,18 2,79* 2,84** 4,93	2,37 2,38 2,54 2,71 2,51 2,47 2,27 2,47 2,05 1,95* 2,08** 2,71	3,39 3,42 3,63 4,07 3,58 3,57 2,85 3,41 2,54** 2,18* 2,23 3,08

Grey areas mark VaR models which satisfied the Kupiec (1995) and the Christoffersen (1998) independence test at 5% significance level, * lowest average VaR value, ** lowest average VaR value for a model which satisfies the Kupiec and the Christoffersen independence test

Table 4b VaR ranking according to minimal average VaR values, 99% confidence level, 750 observations (June/July 2007 - July 2010)

	S&P 500	DJIN	NASDAQ	RTY	NIKKEI	FTSE	DAX	CAC
HS 250	4,98	4,40	4,61	5,40	5,87	4,43	4,67	4,74
HS 500	4,70	4,29	4,47	5,43	5,46	4,39	4,61	4,99
MHS 250	5,53	4,88	5,52	5,94	6,10	5,29	5,54	5,75
MHS 500	5,69	5,22	5,15	6,14	6,87	5,80	5,47	6,18
KHS 250	5,15	4,57	4,99	5,76	6,05	4,85	4,87	5,03
KHS 500	4,98	4,43	4,64	5,62	5,77	4,59	4,84	5,07
BRW λ=0,97	4,06	3,60	3,94	4,56	4,47	3,80	3,92	4,09
BRW λ=0,99	4,92	4,37	4,72	5,40	5,65	4,55	4,65	4,75
Normal VCV	4,07	3,70	4,19	4,97	4,55	3,84	4,00	4,20
Risk Metrics	3,90	3,54	4,05	4,86	4,32	3,72	3,86	4,15
GARCH	4,00	3,65	4,16	4,90	4,32	3,75	3,94	4,19
HW	13,70	12,38	11,18	14,08	12,75	10,76	10,20	10,69
FHS	3,85	3,68	3,88	4,73**	4,20**	3,67	3,84**	3,93
EVT GARCH	4,32	3,62	4,35	4,91	4,06	3,70	4,81	6,44
EVT GARCH (L)	4,89**	5,00**	4,91**	5,27	5,03	3,78**	4,85	5,08
000	0.40	6,23	6 27	000	5	0 40	E 00	E E2**
GPD	8,43	0,23	6,37	8,22	8,92	6,19	5,23	5,53**
GPD	JALSH	BOVE	MEXBOL	KLCI	CRTX	SENSEX		TAIPEI
HS 250				,	,	,		
	JALSH	BOVE	MEXBOL	KLCÍ	CRTX	SENSEX	H SENG	TAIPEI
HS 250	JALSH 4,25	BOVE 5,83	MEXBOL 4,28	KLCI 2,96 **	CRTX 9,37	SENSEX 5,27	H SENG 5,62 5,67	TAIPEI 4,41
HS 250 HS 500	JALSH 4,25 4,29	BOVE 5,83 6,10	MEXBOL 4,28 4,67	KLCI 2,96** 3,13	CRTX 9,37 9,52	SENSEX 5,27 5,44	H SENG 5,62 5,67	TAIPEI 4,41 4,37
HS 250 HS 500 MHS 250	JALSH 4,25 4,29 4,80	5,83 6,10 7,24	MEXBOL 4,28 4,67 5,18	KLCI 2,96** 3,13 3,23	9,37 9,52 10,53	SENSEX 5,27 5,44 5,96	H SENG 5,62 5,67 7,06	TAIPEI 4,41 4,37 4,84
HS 250 HS 500 MHS 250 MHS 500	JALSH 4,25 4,29 4,80 5,21	5,83 6,10 7,24 7,22	MEXBOL 4,28 4,67 5,18 5,44	XLCI 2,96** 3,13 3,23 3,35	9,37 9,52 10,53 12,16	5,27 5,44 5,96 6,22	H SENG 5,62 5,67 7,06 7,09	TAIPEI 4,41 4,37 4,84 4,91
HS 250 HS 500 MHS 250 MHS 500 KHS 250	JALSH 4,25 4,29 4,80 5,21 4,55	BOVE 5,83 6,10 7,24 7,22 6,34	MEXBOL 4,28 4,67 5,18 5,44 4,61	KLCI 2,96** 3,13 3,23 3,35 3,09	CRTX 9,37 9,52 10,53 12,16 9,90	SENSEX 5,27 5,44 5,96 6,22 5,62	H SENG 5,62 5,67 7,06 7,09 5,98	TAIPEI 4,41 4,37 4,84 4,91 4,64
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 500	JALSH 4,25 4,29 4,80 5,21 4,55 4,58	5,83 6,10 7,24 7,22 6,34 6,22	MEXBOL 4,28 4,67 5,18 5,44 4,61 4,78	KLCI 2,96** 3,13 3,23 3,35 3,09 3,22	9,37 9,52 10,53 12,16 9,90 10,31	SENSEX 5,27 5,44 5,96 6,22 5,62 5,71	H SENG 5,62 5,67 7,06 7,09 5,98 5,92	TAIPEI 4,41 4,37 4,84 4,91 4,64 4,54
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 250 KHS 500 BRW λ=0,97	JALSH 4,25 4,29 4,80 5,21 4,55 4,58 3,60	5,83 6,10 7,24 7,22 6,34 6,22 5,06	MEXBOL 4,28 4,67 5,18 5,44 4,61 4,78 3,93	KLCI 2,96** 3,13 3,23 3,35 3,09 3,22 2,41	CRTX 9,37 9,52 10,53 12,16 9,90 10,31 7,76	SENSEX 5,27 5,44 5,96 6,22 5,62 5,71 4,73	H SENG 5,62 5,67 7,06 7,09 5,98 5,92 4,71	TAIPEI 4,41 4,37 4,84 4,91 4,64 4,54 4,11
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW λ=0,97 BRW λ=0,99	JALSH 4,25 4,29 4,80 5,21 4,55 4,58 3,60 4,22	5,83 6,10 7,24 7,22 6,34 6,22 5,06 6,06	MEXBOL 4,28 4,67 5,18 5,44 4,61 4,78 3,93 4,57	KLCI 2,96** 3,13 3,23 3,35 3,09 3,22 2,41 2,97	CRTX 9,37 9,52 10,53 12,16 9,90 10,31 7,76 9,30	5,27 5,44 5,96 6,22 5,62 5,71 4,73 5,39	H SENG 5,62 5,67 7,06 7,09 5,98 5,92 4,71 5,55	TAIPEI 4,41 4,37 4,84 4,91 4,64 4,54 4,11 4,52
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 250 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV	JALSH 4,25 4,29 4,80 5,21 4,55 4,58 3,60 4,22 3,87	5,83 6,10 7,24 7,22 6,34 6,22 5,06 6,06 5,29	MEXBOL 4,28 4,67 5,18 5,44 4,61 4,78 3,93 4,57 4,06	KLCI 2,96** 3,13 3,23 3,35 3,09 3,22 2,41 2,97 2,46	9,37 9,52 10,53 12,16 9,90 10,31 7,76 9,30 7,56	5,27 5,44 5,96 6,22 5,62 5,71 4,73 5,39 4,98	H SENG 5,62 5,67 7,06 7,09 5,98 5,92 4,71 5,55 5,28	TAIPEI 4,41 4,37 4,84 4,91 4,64 4,54 4,11 4,52 3,86
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 500 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV Risk Metrics	JALSH 4,25 4,29 4,80 5,21 4,55 4,58 3,60 4,22 3,87 3,70	5,83 6,10 7,24 7,22 6,34 6,22 5,06 6,06 5,29 4,96	MEXBOL 4,28 4,67 5,18 5,44 4,61 4,78 3,93 4,57 4,06 3,75	KLCI 2,96** 3,13 3,23 3,35 3,09 3,22 2,41 2,97 2,46 2,20	9,37 9,52 10,53 12,16 9,90 10,31 7,76 9,30 7,56 7,27	5,27 5,44 5,96 6,22 5,62 5,71 4,73 5,39 4,98	H SENG 5,62 5,67 7,06 7,09 5,98 5,92 4,71 5,55 5,28 5,02	TAIPEI 4,41 4,37 4,84 4,91 4,64 4,54 4,11 4,52 3,86 3,81
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 500 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV Risk Metrics GARCH	JALSH 4,25 4,80 5,21 4,55 4,58 3,60 4,22 3,87 3,70 3,79	5,83 6,10 7,24 7,22 6,34 6,22 5,06 6,06 5,29 4,96 5,14 **	MEXBOL 4,28 4,67 5,18 5,44 4,61 4,78 3,93 4,57 4,06 3,75 3,96 8,40	KLCI 2,96** 3,13 3,23 3,35 3,09 3,22 2,41 2,97 2,46 2,20 2,26	CRTX 9,37 9,52 10,53 12,16 9,90 10,31 7,76 9,30 7,56 7,27 7,31	5,27 5,44 5,96 6,22 5,62 5,71 4,73 5,39 4,98 4,66 4,79 **	H SENG 5,62 5,67 7,06 7,09 5,98 5,92 4,71 5,55 5,28 5,02 5,11 **	TAIPEI 4,41 4,37 4,84 4,91 4,64 4,54 4,11 4,52 3,86 3,81 3,98
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV Risk Metrics GARCH HW	JALSH 4,25 4,80 5,21 4,55 4,58 3,60 4,22 3,87 3,70 3,79 7,81	5,83 6,10 7,24 7,22 6,34 6,22 5,06 6,06 5,29 4,96 5,14 **	MEXBOL 4,28 4,67 5,18 5,44 4,61 4,78 3,93 4,57 4,06 3,75 3,96 8,40	KLCI 2,96** 3,13 3,23 3,35 3,09 3,22 2,41 2,97 2,46 2,20 2,26 5,28	CRTX 9,37 9,52 10,53 12,16 9,90 10,31 7,76 9,30 7,56 7,27 7,31 21,66	\$\sumset \text{SENSEX}\$ \[\frac{5,27}{5,44} \] \[\frac{5,96}{6,22} \] \[\frac{5,62}{5,71} \] \[\frac{4,73}{4,73} \] \[\frac{5,39}{4,98} \] \[\frac{4,66}{4,79**} \] \[\frac{11,39}{11,39} \]	H SENG 5,62 5,67 7,06 7,09 5,98 5,92 4,71 5,55 5,28 5,02 5,11 **	TAIPEI 4,41 4,37 4,84 4,91 4,64 4,54 4,11 4,52 3,86 3,81 3,98 8,21
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV Risk Metrics GARCH HW FHS	JALSH 4,25 4,80 5,21 4,55 4,58 3,60 4,22 3,87 3,70 3,79 7,81 3,87**	5,83 6,10 7,24 7,22 6,34 6,22 5,06 6,06 5,29 4,96 5,14 ** 9,98	MEXBOL 4,28 4,67 5,18 5,44 4,61 4,78 3,93 4,57 4,06 3,75 3,96 8,40 4,25	KLCI 2,96** 3,13 3,23 3,35 3,09 3,22 2,41 2,97 2,46 2,20 2,26 5,28 2,59	CRTX 9,37 9,52 10,53 12,16 9,90 10,31 7,76 9,30 7,56 7,27 7,31 21,66 7,71**	\$\sumset \text{SENSEX}\$ \[\frac{5,27}{5,44} \] \[\frac{5,96}{6,22} \] \[\frac{5,62}{5,71} \] \[\frac{4,73}{4,73} \] \[\frac{4,98}{4,66} \] \[\frac{4,79**}{11,39} \] \[\frac{5,26}{5,26} \]	H SENG 5,62 5,67 7,06 7,09 5,98 5,92 4,71 5,55 5,28 5,02 5,11** 13,04 4,78 4,28	TAIPEI 4,41 4,37 4,84 4,91 4,64 4,54 4,11 4,52 3,86 3,81 3,98 8,21 4,34**

Grey areas mark VaR models which satisfied the Kupiec (1995) and the Christoffersen (1998) independence test at 5% significance level, * lowest average VaR value, ** lowest average VaR value for a model which satisfies the Kupiec and the Christoffersen independence test

Table 5a VaR ranking according to minimal Lopez size adjusted score, 99% confidence level, 750 observations (June/July 2004 - June/July 2007)

	S&P 500	DJIN	NASDAQ	RTY	NIKKEI	FTSE	DAX	CAC
HS 250	4,05	3,04	1,04	1,05	4,06	4,05	3,05	3,05
HS 500	1,04	0,03**	-1,97	0,04	1,04	0,06	0,04	0,05
MHS 250	-0,98	-0,98	-2,97	0,03**	-0,96	0,04**	-1,97	-1,97
MHS 500	-2,98	-1,98	-3,98	-0,97	-1,97	0,04	-1,97	0,03**
KHS 250	2,04	1,03	-1,97	-1,97	1,05	1,04	1,03	-0,96
KHS 500	-0,97**	-0,97	-2,98	0,04	-0,96	0,05	0,03**	0,04
BRW λ=0,97	7,06	5,06	4,06	2,06	6,08	6,05	3,06	8,06
BRW λ=0,99	2,03	-0,96	-0,97	-0,96	0,05	5,04	0,04	0,03
Normal VCV	4,05	5,05	0,04**	1,05	9,10	11,08	9,08	9,08
Risk Metrics	9,06	7,07	2,06	5,06	7,09	8,07	7,09	7,07
GARCH	4,04	4,05	1,04	0,04	2,06	2,04	2,04	2,05
HW	9,06	8,07	15,08	6,08	7,06	3,02	5,06	1,04
FHS	-4,98	-1,97	-3,97	-1,97	-0,96**	-2,98	-6,99	-1,97
EVT GARCH	-6,98	-5,98	-2,97	0,05	-5,98	-1,98	-1,97	-6,99
GPD	-7,00	-7,00	-7,00	-7,00	-7,00	-7,00	-7,00	-7,00
	JALSH	BOVE	MEXBOL	KLCI	CRTX	SENSEX	H SENG	TAIPEI
HS 250	JALSH 6,11	BOVE 2,07	MEXBOL 1,09	KLCI 3,10	CRTX 0,16	SENSEX 2,11	H SENG 3,05	TAIPEI -0,94**
HS 250 HS 500						2,11		
	6,11	2,07	1,09	3,10	0,16	2,11 2,12	3,05	-0,94**
HS 500	6,11 5,13	2,07 -2,94	1,09 2,11	3,10 4,11	0,16 -0,86	2,11 2,12	3,05 1,05	-0,94 ** -2,96
HS 500 MHS 250	6,11 5,13 2,07	2,07 -2,94 -2,95	1,09 2,11 -1,95	3,10 4,11 0,07	0,16 -0,86 -1,88	2,11 2,12 -1,92	3,05 1,05 1,04	-0,94 ** -2,96 -0,95
HS 500 MHS 250 MHS 500	6,11 5,13 2,07 0,07 **	2,07 -2,94 -2,95 -4,96	1,09 2,11 -1,95 -0,94	3,10 4,11 0,07 -1,93	0,16 -0,86 -1,88 -2,90	2,11 2,12 -1,92 0,09	3,05 1,05 1,04 -0,97	-0,94** -2,96 -0,95 -2,97
HS 500 MHS 250 MHS 500 KHS 250	6,11 5,13 2,07 0,07 ** 2,09	2,07 -2,94 -2,95 -4,96 -1,95	1,09 2,11 -1,95 -0,94 -0,93	3,10 4,11 0,07 -1,93 2,08 **	0,16 -0,86 -1,88 -2,90 -1,87	2,11 2,12 -1,92 0,09 -0,92 1,11	3,05 1,05 1,04 -0,97 2,04	-0,94** -2,96 -0,95 -2,97 -1,95
HS 500 MHS 250 MHS 500 KHS 250 KHS 500	6,11 5,13 2,07 0,07 ** 2,09 3,12	2,07 -2,94 -2,95 -4,96 -1,95 -2,95	1,09 2,11 -1,95 -0,94 -0,93 1,10	3,10 4,11 0,07 -1,93 2,08 ** 0,10	0,16 -0,86 -1,88 -2,90 -1,87 -0,87	2,11 2,12 -1,92 0,09 -0,92 1,11	3,05 1,05 1,04 -0,97 2,04 1,04 4,07	-0,94** -2,96 -0,95 -2,97 -1,95 -2,97
HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW \(\lambda=0,97\)	6,11 5,13 2,07 0,07 ** 2,09 3,12 9,11	2,07 -2,94 -2,95 -4,96 -1,95 -2,95 4,09	1,09 2,11 -1,95 -0,94 -0,93 1,10 6,09	3,10 4,11 0,07 -1,93 2,08** 0,10 5,08	0,16 -0,86 -1,88 -2,90 -1,87 -0,87 2,18	2,11 2,12 -1,92 0,09 -0,92 1,11 2,11	3,05 1,05 1,04 -0,97 2,04 1,04 4,07	-0,94** -2,96 -0,95 -2,97 -1,95 -2,97 3,11
HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW \(\lambda = 0,97 \) BRW \(\lambda = 0,99 \)	6,11 5,13 2,07 0,07** 2,09 3,12 9,11 3,09	2,07 -2,94 -2,95 -4,96 -1,95 -2,95 4,09 0,06 **	1,09 2,11 -1,95 -0,94 -0,93 1,10 6,09 3,07	3,10 4,11 0,07 -1,93 2,08 ** 0,10 5,08 1,07	0,16 -0,86 -1,88 -2,90 -1,87 -0,87 2,18 0,11	2,11 2,12 -1,92 0,09 -0,92 1,11 2,11 0,08	3,05 1,05 1,04 -0,97 2,04 1,04 4,07 0,04 **	-0,94** -2,96 -0,95 -2,97 -1,95 -2,97 3,11 -1,96
HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW \(\lambda = 0,97 \) BRW \(\lambda = 0,99 \) Normal VCV	6,11 5,13 2,07 0,07** 2,09 3,12 9,11 3,09 9,16	2,07 -2,94 -2,95 -4,96 -1,95 -2,95 4,09 0,06 **	1,09 2,11 -1,95 -0,94 -0,93 1,10 6,09 3,07 7,12	3,10 4,11 0,07 -1,93 2,08** 0,10 5,08 1,07 6,12	0,16 -0,86 -1,88 -2,90 -1,87 -0,87 2,18 0,11 9,29	2,11 2,12 -1,92 0,09 -0,92 1,11 2,11 0,08 11,18	3,05 1,05 1,04 -0,97 2,04 1,04 4,07 0,04 **	-0,94** -2,96 -0,95 -2,97 -1,95 -2,97 3,11 -1,96 3,11
HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV Risk Metrics	6,11 5,13 2,07 0,07 ** 2,09 3,12 9,11 3,09 9,16 7,10	2,07 -2,94 -2,95 -4,96 -1,95 -2,95 4,09 0,06 ** 3,08 7,11	1,09 2,11 -1,95 -0,94 -0,93 1,10 6,09 3,07 7,12 10,11	3,10 4,11 0,07 -1,93 2,08 ** 0,10 5,08 1,07 6,12 7,08	0,16 -0,86 -1,88 -2,90 -1,87 -0,87 2,18 0,11 9,29 9,24	2,11 2,12 -1,92 0,09 -0,92 1,11 2,11 0,08 11,18 10,16	3,05 1,05 1,04 -0,97 2,04 1,04 4,07 0,04 ** 10,09 6,07	-0,94** -2,96 -0,95 -2,97 -1,95 -2,97 3,11 -1,96 3,11 5,12
HS 500 MHS 250 MHS 500 KHS 250 KHS 250 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV Risk Metrics GARCH	6,11 5,13 2,07 0,07 ** 2,09 3,12 9,11 3,09 9,16 7,10 5,09	2,07 -2,94 -2,95 -4,96 -1,95 -2,95 4,09 0,06** 3,08 7,11 2,07	1,09 2,11 -1,95 -0,94 -0,93 1,10 6,09 3,07 7,12 10,11 -0,94	3,10 4,11 0,07 -1,93 2,08 ** 0,10 5,08 1,07 6,12 7,08 3,06	0,16 -0,86 -1,88 -2,90 -1,87 -0,87 2,18 0,11 9,29 9,24 6,16	2,11 2,12 -1,92 0,09 -0,92 1,11 2,11 0,08 11,18 10,16 3,11	3,05 1,05 1,04 -0,97 2,04 1,04 4,07 0,04** 10,09 6,07 3,05	-0,94** -2,96 -0,95 -2,97 -1,95 -2,97 3,11 -1,96 3,11 5,12 5,11
HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV Risk Metrics GARCH HW	6,11 5,13 2,07 0,07 ** 2,09 3,12 9,11 3,09 9,16 7,10 5,09 4,04	2,07 -2,94 -2,95 -4,96 -1,95 -2,95 4,09 0,06** 3,08 7,11 2,07 4,11	1,09 2,11 -1,95 -0,94 -0,93 1,10 6,09 3,07 7,12 10,11 -0,94 0,05 **	3,10 4,11 0,07 -1,93 2,08** 0,10 5,08 1,07 6,12 7,08 3,06 6,04	0,16 -0,86 -1,88 -2,90 -1,87 -0,87 2,18 0,11 9,29 9,24 6,16 1,10	2,11 2,12 -1,92 0,09 -0,92 1,11 2,11 0,08 11,18 10,16 3,11 3,05 0,05	3,05 1,05 1,04 -0,97 2,04 1,04 4,07 0,04** 10,09 6,07 3,05 5,04	-0,94** -2,96 -0,95 -2,97 -1,95 -2,97 3,11 -1,96 3,11 5,12 5,11 6,06

Reported figures represent Lopez (1998) test scores. Grey areas mark VaR models satisfying the Kupiec (1995) and the Christoffersen (1998) independence test at 5% significance level,, ** lowest Lopez score i.e. smallest deviation from expected values.

Table 5b VaR ranking according to minimal Lopez size adjusted score, 99% confidence level, 750 observations (June/July 2007 - July 2010)

	S&P 500	DJIN	NASDAQ	RTY	NIKKEI	FTSE	DAX	CAC
HS 250	15,25	14,23	16,26	14,30	8,29	10,22	6,17	10,23
HS 500	21,36	18,30	22,31	15,37	11,37	9,27	8,26	9,28
MHS 250	10,18	10,15	8,15	6,20	4,23	4,15	1,12	6,16
MHS 500	14,26	11,22	10,21	6,25	8,32	5,21	3,18	5,21
KHS 250	11,21	10,19	12,20	8,23	4,24	5,18	2,14	7,19
KHS 500	20,33	17,27	15,27	14,33	8,34	8,24	3,24	7,26
BRW λ=0,97	16,24	11,19	17,22	15,27	9,28	9,22	11,18	12,22
BRW λ=0,99	11,21	7,17	12,20	9,24	3,24	2,19	2,15	5,18
Normal VCV	29,41	27,34	22,31	22,39	20,41	20,32	13,29	18,35
Risk Metrics	16,14	11,12	14,13	10,09	7,18	11,14	9,12	5,13
GARCH	9,09	8,08		5,06	2,10	7,12	4,10	6,10
HW	-1,97	4,04	1,05**	-1,96	2,05	0,03**	1,05**	1,06
FHS	15,11	8,07	14,13	3,67	3,11	10,14	3,47	8,13
EVT GARCH	4,06	8,08	4,07	5,06	4,12	7,13	-5,95	-6,98
EVT GARCH (L)	-2,97**	-6,00	-3,96	0,03**	-1,94**	3,09	-5,95	-4,95
GPD	-4,97	-3,94**	-3,91	-4,93	-3,94	-4,94	1,11	1,12**
GPD	-7,57	-3,34	0,01	7,00	0,54	7,07	1,11	1,12
GPD	JALSH	BOVE	MEXBOL	KLCI	CRTX	SENSEX		TAIPEI
HS 250		BOVE		,				,
	JALSH	BOVE 7,24	MEXBOL	KLCI	CRTX	SENSEX	H SENG	TAIPEI
HS 250	JALSH 6,15	BOVE 7,24	MEXBOL 10,14	KLCI 1,09	CRTX 7,55	SENSEX 4,16	H SENG 13,25 18,37	TAIPEI 6,11
HS 250 HS 500	JALSH 6,15 5,16	7,24 6,29 0,15 **	MEXBOL 10,14 5,13	KLCI 1,09 1,12	7,55 7,74 3,41	SENSEX 4,16 7,20	H SENG 13,25 18,37 2,13	TAIPEI 6,11 6,13
HS 250 HS 500 MHS 250	JALSH 6,15 5,16 2,11	7,24 6,29 0,15 **	MEXBOL 10,14 5,13 2,07 -1,94	KLCI 1,09 1,12 0,08 **	7,55 7,74 3,41 2,57	\$ENSEX 4,16 7,20 1,12	H SENG 13,25 18,37 2,13	TAIPEI 6,11 6,13 2,08
HS 250 HS 500 MHS 250 MHS 500	JALSH 6,15 5,16 2,11 0,10	BOVE 7,24 6,29 0,15 ** 0,20 4,19	MEXBOL 10,14 5,13 2,07 -1,94	1,09 1,12 0,08 ** 1,10	7,55 7,74 3,41 2,57	SENSEX 4,16 7,20 1,12 2,13	H SENG 13,25 18,37 2,13 11,22 7,17	TAIPEI 6,11 6,13 2,08 4,09
HS 250 HS 500 MHS 250 MHS 500 KHS 250	JALSH 6,15 5,16 2,11 0,10 3,12	BOVE 7,24 6,29 0,15 ** 0,20 4,19	MEXBOL 10,14 5,13 2,07 -1,94 4,09	1,09 1,12 0,08 ** 1,10 0,09	7,55 7,74 3,41 2,57 3,46	SENSEX 4,16 7,20 1,12 2,13 3,12	H SENG 13,25 18,37 2,13 11,22 7,17	TAIPEI 6,11 6,13 2,08 4,09 1,09
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 500	JALSH 6,15 5,16 2,11 0,10 3,12 4,14 8,17 2,14	7,24 6,29 0,15** 0,20 4,19 5,27 11,25	MEXBOL 10,14 5,13 2,07 -1,94 4,09 5,11	1,09 1,12 0,08** 1,10 0,09 2,11	7,55 7,74 3,41 2,57 3,46 6,67	SENSEX 4,16 7,20 1,12 2,13 3,12 7,18	H SENG 13,25 18,37 2,13 11,22 7,17 17,33	TAIPEI 6,11 6,13 2,08 4,09 1,09 5,11
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW λ=0,97	JALSH 6,15 5,16 2,11 0,10 3,12 4,14 8,17	7,24 6,29 0,15** 0,20 4,19 5,27 11,25	MEXBOL 10,14 5,13 2,07 -1,94 4,09 5,11 8,13	KLCI 1,09 1,12 0,08** 1,10 0,09 2,11 7,14	7,55 7,74 3,41 2,57 3,46 6,67 12,48 5,41	\$ENSEX 4,16 7,20 1,12 2,13 3,12 7,18 8,19	H SENG 13,25 18,37 2,13 11,22 7,17 17,33 13,27	TAIPEI 6,11 6,13 2,08 4,09 1,09 5,11 10,14
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 250 KHS 500 BRW λ=0,97 BRW λ=0,99	JALSH 6,15 5,16 2,11 0,10 3,12 4,14 8,17 2,14	7,24 6,29 0,15** 0,20 4,19 5,27 11,25 4,19	MEXBOL 10,14 5,13 2,07 -1,94 4,09 5,11 8,13 1,08 16,21	KLCI 1,09 1,12 0,08** 1,10 0,09 2,11 7,14 1,09	7,55 7,74 3,41 2,57 3,46 6,67 12,48 5,41	\$ENSEX 4,16 7,20 1,12 2,13 3,12 7,18 8,19 2,13	H SENG 13,25 18,37 2,13 11,22 7,17 17,33 13,27 9,21	TAIPEI 6,11 6,13 2,08 4,09 1,09 5,11 10,14 0,09**
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 500 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV	JALSH 6,15 5,16 2,11 0,10 3,12 4,14 8,17 2,14 13,22	80VE 7,24 6,29 0,15** 0,20 4,19 5,27 11,25 4,19 13,32	MEXBOL 10,14 5,13 2,07 -1,94 4,09 5,11 8,13 1,08 16,21	1,09 1,12 0,08** 1,10 0,09 2,11 7,14 1,09 8,18	CRTX 7,55 7,74 3,41 2,57 3,46 6,67 12,48 5,41 16,76	SENSEX 4,16 7,20 1,12 2,13 3,12 7,18 8,19 2,13 15,26	H SENG 13,25 18,37 2,13 11,22 7,17 17,33 13,27 9,21 18,33 5,17 2,09	TAIPEI 6,11 6,13 2,08 4,09 1,09 5,11 10,14 0,09**
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV Risk Metrics	JALSH 6,15 5,16 2,11 0,10 3,12 4,14 8,17 2,14 13,22 12,11	80VE 7,24 6,29 0,15** 0,20 4,19 5,27 11,25 4,19 13,32 10,16	MEXBOL 10,14 5,13 2,07 -1,94 4,09 5,11 8,13 1,08 16,21 11,16	1,09 1,12 0,08** 1,10 0,09 2,11 7,14 1,09 8,18 11,17	CRTX 7,55 7,74 3,41 2,57 3,46 6,67 12,48 5,41 16,76 10,37 2,26	SENSEX 4,16 7,20 1,12 2,13 3,12 7,18 8,19 2,13 15,26 12,19 2,12 4,08	H SENG 13,25 18,37 2,13 11,22 7,17 17,33 13,27 9,21 18,33 5,17 2,09	TAIPEI 6,11 6,13 2,08 4,09 1,09 5,11 10,14 0,09** 17,25 14,18
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV Risk Metrics GARCH	JALSH 6,15 5,16 2,11 0,10 3,12 4,14 8,17 2,14 13,22 12,11 4,06	80VE 7,24 6,29 0,15** 0,20 4,19 5,27 11,25 4,19 13,32 10,16 2,09	MEXBOL 10,14 5,13 2,07 -1,94 4,09 5,11 8,13 1,08 16,21 11,16 8,13	KLCI 1,09 1,12 0,08** 1,10 0,09 2,11 7,14 1,09 8,18 11,17 4,11	CRTX 7,55 7,74 3,41 2,57 3,46 6,67 12,48 5,41 16,76 10,37 2,26	SENSEX 4,16 7,20 1,12 2,13 3,12 7,18 8,19 2,13 15,26 12,19 2,12	H SENG 13,25 18,37 2,13 11,22 7,17 17,33 13,27 9,21 18,33 5,17 2,09	TAIPEI 6,11 6,13 2,08 4,09 1,09 5,11 10,14 0,09** 17,25 14,18 9,11
HS 250 HS 500 MHS 250 MHS 500 KHS 500 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV Risk Metrics GARCH HW FHS EVT GARCH	JALSH 6,15 5,16 2,11 0,10 3,12 4,14 8,17 2,14 13,22 12,11 4,06 4,04	80VE 7,24 6,29 0,15** 0,20 4,19 5,27 11,25 4,19 13,32 10,16 2,09 6,12	MEXBOL 10,14 5,13 2,07 -1,94 4,09 5,11 8,13 1,08 16,21 11,16 8,13 0,06 **	KLCI 1,09 1,12 0,08** 1,10 0,09 2,11 7,14 1,09 8,18 11,17 4,11 3,03	CRTX 7,55 7,74 3,41 2,57 3,46 6,67 12,48 5,41 16,76 10,37 2,26 0,07	SENSEX 4,16 7,20 1,12 2,13 3,12 7,18 8,19 2,13 15,26 12,19 2,12 4,08	H SENG 13,25 18,37 2,13 11,22 7,17 17,33 13,27 9,21 18,33 5,17 2,09 1,05**	TAIPEI 6,11 6,13 2,08 4,09 1,09 5,11 10,14 0,09** 17,25 14,18 9,11 2,08 3,07 9,12
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV Risk Metrics GARCH HW FHS	JALSH 6,15 5,16 2,11 0,10 3,12 4,14 8,17 2,14 13,22 12,11 4,06 4,04 0,03**	80VE 7,24 6,29 0,15** 0,20 4,19 5,27 11,25 4,19 13,32 10,16 2,09 6,12 1,07 26,32	MEXBOL 10,14 5,13 2,07 -1,94 4,09 5,11 8,13 1,08 16,21 11,16 8,13 0,06** 7,09	KLCI 1,09 1,12 0,08** 1,10 0,09 2,11 7,14 1,09 8,18 11,17 4,11 3,03 -2,92	CRTX 7,55 7,74 3,41 2,57 3,46 6,67 12,48 5,41 16,76 10,37 2,26 0,07 1,22	SENSEX 4,16 7,20 1,12 2,13 3,12 7,18 8,19 2,13 15,26 12,19 2,12 4,08 -0,91**	H SENG 13,25 18,37 2,13 11,22 7,17 17,33 13,27 9,21 18,33 5,17 2,09 1,05** 7,13 11,21	TAIPEI 6,11 6,13 2,08 4,09 1,09 5,11 10,14 0,09** 17,25 14,18 9,11 2,08 3,07

Reported figures represent Lopez (1998) test scores. Grey areas mark VaR models satisfying the Kupiec (1995) and the Christoffersen (1998) independence test at 5% significance level,, ** lowest Lopez score i.e. smallest deviation from expected values.

Table 6a Ranking of ES model according to modified Blanco-Ihle error statistic, 99% confidence level, 750 observations (June/July 2004 - June/July 2007)

	S&P500	DJIN	NASDAQ	RTY	NIKKEI	FTSE	DAX	CAC	Total
VCV GPD	11	12	11	12	12	13	13	12	12
RM GPD	13	13	13	13	13	12	11	13	13
GARCH GPD	12	11	12	11	11	11	12	11	11
Bootstr FHS	4	4	5	1	1	5	1	4	2
Bootstr HS250	1	3	7	9	4	6	3	5	4
Bootstr HS500	8	7	2	7	5	8	5	7	6
Bootstr KHS250	5	6	9	5	9	10	8	9	9
Bootstr KHS500	6	5	4	8	8	9	10	8	8
Bootstr MHS250	2	1	1	2	6	4	9	2	3
Bootstr MHS500	3	2	3	3	3	3	2	3	1
Bootstr BRW	7	8	6	6	7	7	6	6	7
EVT GARCH	10	10	8	4	2	2	7	1	5
GPD	9	9	10	10	10	1	4	10	10
OI D	J	Ŭ	.0		.0	•			
Ol D	JALSH	BOVE	MEXBOL	KLCI	CRTX	SENSEX	H SENG	TAIPEI	Total
VCV GPD									
<u> </u>	JALSH	BOVE	MEXBOL	KLCI	CRTX	SENSEX	H SENG	TAIPEI	Total
VCV GPD	JALSH 11	BOVE 12	MEXBOL 11	KLCI 9	CRTX 12	SENSEX 13	H SENG 12	TAIPEI 8	Total
VCV GPD RM GPD	JALSH 11 13	BOVE 12 13	MEXBOL 11 13	KLCI 9 11	CRTX 12 13	SENSEX 13 12	H SENG 12 13	TAIPEI 8 5	Total 12 13
VCV GPD RM GPD GARCH GPD	JALSH 11 13 12	BOVE 12 13 11	MEXBOL 11 13 12	KLCI 9 11 6	CRTX 12 13 11	SENSEX 13 12 5	H SENG 12 13 11	TAIPEI 8 5 7	Total 12 13 11
VCV GPD RM GPD GARCH GPD Bootstr FHS	JALSH 11 13 12 1	BOVE 12 13 11	MEXBOL 11 13 12 2	KLCI 9 11 6	CRTX 12 13 11 3	SENSEX 13 12 5 6	H SENG 12 13 11 1	TAIPEI 8 5 7 3	Total 12 13 11 1
VCV GPD RM GPD GARCH GPD Bootstr FHS Bootstr HS250	JALSH 11 13 12 1 6	BOVE 12 13 11 1 2	MEXBOL 11 13 12 2 7	KLCI 9 11 6 1	CRTX 12 13 11 3 9	SENSEX 13 12 5 6 9	H SENG 12 13 11 1 7	TAIPEI 8 5 7 3 12	Total 12 13 11 1 7
VCV GPD RM GPD GARCH GPD Bootstr FHS Bootstr HS250 Bootstr HS500	JALSH 11 13 12 1 6 7	BOVE 12 13 11 1 2 7	MEXBOL 11 13 12 2 7 5	KLCI 9 11 6 1 5	CRTX 12 13 11 3 9 5	SENSEX 13 12 5 6 9 8	H SENG 12 13 11 1 7 5	TAIPEI 8 5 7 3 12 9	Total 12 13 11 1 7 6
VCV GPD RM GPD GARCH GPD Bootstr FHS Bootstr HS250 Bootstr HS500 Bootstr KHS250	JALSH 11 13 12 1 6 7 9	BOVE 12 13 11 1 2 7 8	MEXBOL 11 13 12 2 7 5 9	KLCI 9 11 6 1 5 10 7	CRTX 12 13 11 3 9 5 10	SENSEX 13 12 5 6 9 8 11	H SENG 12 13 11 1 7 5 8	TAIPEI 8 5 7 3 12 9 11	Total 12 13 11 1 7 6 10
VCV GPD RM GPD GARCH GPD Bootstr FHS Bootstr HS250 Bootstr HS500 Bootstr KHS250 Bootstr KHS250	JALSH 11 13 12 1 6 7 9 8	BOVE 12 13 11 1 2 7 8 10	MEXBOL 11 13 12 2 7 5 9	KLCI 9 11 6 1 5 10 7	CRTX 12 13 11 3 9 5 10 6	SENSEX 13 12 5 6 9 8 11 10	H SENG 12 13 11 1 7 5 8 6	TAIPEI 8 5 7 3 12 9 11 10	Total 12 13 11 1 7 6 10 9
VCV GPD RM GPD GARCH GPD Bootstr FHS Bootstr HS250 Bootstr HS500 Bootstr KHS250 Bootstr KHS250 Bootstr KHS250 Bootstr KHS250	JALSH 11 13 12 1 6 7 9 8 4	BOVE 12 13 11 1 2 7 8 10 5	MEXBOL 11 13 12 2 7 5 9 8 1	KLCI 9 11 6 1 5 10 7 12 2	CRTX 12 13 11 3 9 5 10 6 2	SENSEX 13 12 5 6 9 8 11 10 3	H SENG 12 13 11 1 7 5 8 6 4	TAIPEI 8 5 7 3 12 9 11 10 2	Total 12 13 11 1 7 6 10 9
VCV GPD RM GPD GARCH GPD Bootstr FHS Bootstr HS250 Bootstr HS500 Bootstr KHS250 Bootstr KHS250 Bootstr KHS500 Bootstr MHS250 Bootstr MHS250 Bootstr MHS250	JALSH 11 13 12 1 6 7 9 8 4 5	BOVE 12 13 11 1 2 7 8 10 5 6	MEXBOL 11 13 12 2 7 5 9 8 1 6	KLCI 9 11 6 1 5 10 7 12 2 3	CRTX 12 13 11 3 9 5 10 6 2 8	SENSEX 13 12 5 6 9 8 11 10 3 2	H SENG 12 13 11 1 7 5 8 6 4 2	TAIPEI 8 5 7 3 12 9 11 10 2 1	Total 12 13 11 1 7 6 10 9 2 3

Lowest value

marks the most successful ES model

Table 6b Ranking of ES model according to modified Blanco-Ihle error statistic, 99% confidence level, 750 observations (June/July 2007 - July 2010)

	S&P500	DJIN	NASDAQ	RTY	NIKKEI	FTSE	DAX	CAC	Total
VCV GPD	12	12	12	12	13	12	11	12	12
RM GPD	13	13	13	13	10	13	14	13	13
GARCH GPD	14	14	14	14	12	14	13	14	14
Bootstr FHS	2	4	1	1	4	1	2	2	1
Bootstr HS250	6	6	5	6	8	6	5	7	6
Bootstr HS500	5	7	6	5	7	8	8	8	7
Bootstr KHS250	9	8	8	9	11	9	9	10	9
Bootstr KHS500	8	9	9	11	9	10	10	11	10
Bootstr MHS250	1	3	3	2	2	7	3	6	2
Bootstr MHS500	4	5	4	4	6	5	4	4	5
Bootstr BRW	10	11	10	7	14	11	12	9	11
EVT GARCH	3	2	2	8	3	2	6	1	3
EVT GARCH (L)	7	10	11	10	5	3	7	5	8
GPD	11	1	7	3	1	4	1	3	4
	JALSH	BOVE	MEXBOL	KLCI	CRTX	SENSEX	H SENG	TAIPEI	Total
VCV GPD	JALSH 11	BOVE 13	MEXBOL 14	KLCI 10	CRTX 12	SENSEX 13	H SENG 13	TAIPEI 13	Total 12
VCV GPD RM GPD									
	11	13	14	10	12	13	13	13	12
RM GPD	11 14	13 14	14 13	10 9	12 11	13 14	13 12	13 12	12 13
RM GPD GARCH GPD	11 14 13	13 14 12	14 13 12	10 9 14	12 11 9	13 14 12	13 12 14	13 12 14	12 13 14
RM GPD GARCH GPD Bootstr FHS	11 14 13 1	13 14 12 5	14 13 12 3	10 9 14 2	12 11 9 3	13 14 12 4	13 12 14 5	13 12 14 2	12 13 14 2
RM GPD GARCH GPD Bootstr FHS Bootstr HS250	11 14 13 1 9	13 14 12 5 7	14 13 12 3 7	10 9 14 2 5	12 11 9 3 7	13 14 12 4 7	13 12 14 5 10	13 12 14 2 7	12 13 14 2 7
RM GPD GARCH GPD Bootstr FHS Bootstr HS250 Bootstr HS500	11 14 13 1 9 6	13 14 12 5 7 8	14 13 12 3 7 6	10 9 14 2 5 13	12 11 9 3 7 8	13 14 12 4 7 3	13 12 14 5 10 9	13 12 14 2 7 8	12 13 14 2 7 8
RM GPD GARCH GPD Bootstr FHS Bootstr HS250 Bootstr HS500 Bootstr KHS250	11 14 13 1 9 6 10	13 14 12 5 7 8 10	14 13 12 3 7 6 8	10 9 14 2 5 13 6	12 11 9 3 7 8 10	13 14 12 4 7 3 9	13 12 14 5 10 9	13 12 14 2 7 8 9	12 13 14 2 7 8 9
RM GPD GARCH GPD Bootstr FHS Bootstr HS250 Bootstr HS500 Bootstr KHS250 Bootstr KHS250	11 14 13 1 9 6 10	13 14 12 5 7 8 10	14 13 12 3 7 6 8	10 9 14 2 5 13 6	12 11 9 3 7 8 10	13 14 12 4 7 3 9	13 12 14 5 10 9 11	13 12 14 2 7 8 9	12 13 14 2 7 8 9
RM GPD GARCH GPD Bootstr FHS Bootstr HS250 Bootstr KHS250 Bootstr KHS250 Bootstr KHS250 Bootstr KHS250	11 14 13 1 9 6 10 8	13 14 12 5 7 8 10 11	14 13 12 3 7 6 8 10	10 9 14 2 5 13 6 12 4	12 11 9 3 7 8 10 13 5	13 14 12 4 7 3 9 6	13 12 14 5 10 9 11 8	13 12 14 2 7 8 9 10 5	12 13 14 2 7 8 9 11
RM GPD GARCH GPD Bootstr FHS Bootstr HS250 Bootstr KHS250 Bootstr KHS250 Bootstr KHS250 Bootstr KHS500 Bootstr MHS250 Bootstr MHS250	11 14 13 1 9 6 10 8 2	13 14 12 5 7 8 10 11 3 6	14 13 12 3 7 6 8 10 5	10 9 14 2 5 13 6 12 4	12 11 9 3 7 8 10 13 5	13 14 12 4 7 3 9 6 10	13 12 14 5 10 9 11 8 2	13 12 14 2 7 8 9 10 5	12 13 14 2 7 8 9 11 4
RM GPD GARCH GPD Bootstr FHS Bootstr HS250 Bootstr HS500 Bootstr KHS250 Bootstr KHS250 Bootstr KHS500 Bootstr MHS250 Bootstr MHS250 Bootstr MHS250	11 14 13 1 9 6 10 8 2 4	13 14 12 5 7 8 10 11 3 6	14 13 12 3 7 6 8 10 5 2	10 9 14 2 5 13 6 12 4 3	12 11 9 3 7 8 10 13 5 4	13 14 12 4 7 3 9 6 10 5	13 12 14 5 10 9 11 8 2 6	13 12 14 2 7 8 9 10 5 6	12 13 14 2 7 8 9 11 4 5

Lowest value marks the most successful ES model

Table 7a Rankings of simulated VaR models performance (N = 2.000) according to Lopez size adjusted score

	S&P 500	DJIN	NASDAQ	RTY	NIKKEI	FTSE	DAX	CAC	Average
HS 250	5	5	6	6	5	6	4	6	12
HS 500	6	6	8	6	7	6	4	5	13
MHS 250	4	3	4	4	4	3	1	4	6
MHS 500	4	3	4	4	5	4	2	4	8
KHS 250	4	3	5	4	4	4	1	4	7
KHS 500	7	6	6	6	5	6	2	4	10
BRW λ=0,97	6	4	7	6	6	6	5	6	11
BRW λ=0,99	3	2	6	5	2	2	1	3	4
Normal VCV	7	6	8	7	7	8	5	7	14
Risk Metrics	5	4	6	5	5	7	5	3	9
GARCH	2	3	5	3	1	5	3	3	5
HW	2	2	3	2	3	5	2	1	3
FHS	4	2	1	2	2	6	2	5	4
EVT GARCH	1	1	2	1	1	1	3	2	1
GPD	3	1	3	2	2	1	1	1	2
	JALSH	BOVE	MEXBOL	KLCI	CRTX	SENSEX	H SENG	TAIPEI	Average
HS 250	5	5	6	KLCI 1	6	SENSEX 4	H SENG 5	4	Average 11
	5 5	-	6 3					4 5	
HS 250	5	5	6 3 2	1	6	4	5	4 5 2	11
HS 250 HS 500	5 5	5 4	6 3 2 2	1	6	4 5	5 6	4 5 2 3	11 10
HS 250 HS 500 MHS 250	5 5 2	5 4 1	6 3 2	1 1 1	6 6 4	4 5 1	5 6 1	4 5 2	11 10 1
HS 250 HS 500 MHS 250 MHS 500	5 5 2 1	5 4 1 1	6 3 2 2	1 1 1 2 1 2	6 6 4 4	4 5 1 1	5 6 1 3	4 5 2 3	11 10 1 3
HS 250 HS 500 MHS 250 MHS 500 KHS 250	5 5 2 1 3 4 6	5 4 1 1 3	6 3 2 2 3	1 1 1 2 1 2 5	6 6 4 4	4 5 1 1 2	5 6 1 3	4 5 2 3 2	11 10 1 3 5
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 500	5 5 2 1 3 4	5 4 1 1 3 4	6 3 2 2 3 3	1 1 1 2 1 2	6 6 4 4 4 5	4 5 1 1 2 5	5 6 1 3 3 5	4 5 2 3 2 4	11 10 1 3 5
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW λ=0,97	5 5 2 1 3 4 6	5 4 1 1 3 4 6	6 3 2 2 3 3 4	1 1 1 2 1 2 5	6 6 4 4 4 5 7	4 5 1 1 2 5 5	5 6 1 3 5 5	4 5 2 3 2 4 6	11 10 1 3 5 9
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW λ=0,97 BRW λ=0,99	5 5 2 1 3 4 6 2	5 4 1 1 3 4 6 3	6 3 2 2 3 3 4 1	1 1 1 2 1 2 5 2	6 6 4 4 4 5 7 5	4 5 1 1 2 5 5	5 6 1 3 5 5 4	4 5 2 3 2 4 6 1	11 10 1 3 5 9 12 4
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV	5 5 2 1 3 4 6 2	5 4 1 3 4 6 3 6	6 3 2 2 3 3 4 1 6	1 1 1 2 1 2 5 2 5	6 6 4 4 5 7 5 7	4 5 1 1 2 5 5 2 6	5 6 1 3 3 5 5 4 6	4 5 2 3 2 4 6 1 7	11 10 1 3 5 9 12 4
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV Risk Metrics	5 5 2 1 3 4 6 2 7	5 4 1 3 4 6 3 6	6 3 2 2 3 3 4 1 6	1 1 1 2 1 2 5 2 5 5	6 6 4 4 5 7 5 7	4 5 1 1 2 5 5 2 6	5 6 1 3 3 5 5 4 6 3	4 5 2 3 2 4 6 1 7 6	11 10 1 3 5 9 12 4 14
HS 250 HS 500 MHS 250 MHS 500 KHS 500 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV Risk Metrics GARCH	5 5 2 1 3 4 6 2 7 7	5 4 1 3 4 6 3 6 6	6 3 2 2 3 3 4 1 6 6 5	1 1 1 2 1 2 5 2 5 5 4	6 6 4 4 5 7 5 7 6 3	4 5 1 1 2 5 5 2 6 6 2	5 6 1 3 3 5 5 4 6 3 1	4 5 2 3 2 4 6 1 7 6 5	11 10 1 3 5 9 12 4 14 13 7
HS 250 HS 500 MHS 250 MHS 500 KHS 250 KHS 500 BRW λ=0,97 BRW λ=0,99 Normal VCV Risk Metrics GARCH HW	5 5 2 1 3 4 6 2 7 7 4 4	5 4 1 3 4 6 3 6 6 2 5	6 3 2 2 3 3 4 1 6 5 1	1 1 1 2 1 2 5 2 5 2 5 4 4	6 6 4 4 5 7 5 7 6 3	4 5 1 1 2 5 5 2 6 6 2 3	5 6 1 3 3 5 5 4 6 3 1 3	4 5 2 3 2 4 6 1 7 6 5 3	11 10 1 3 5 9 12 4 14 13 7

Lowest value marks the most successful VaR model

Table 7b Rankings of simulated ES models performance (N = 2.000) according to modified Blanco Ihle score

	S&P500	DJIN	NASDAQ	RTY	NIKKEI	FTSE	DAX	CAC	Average
VCV GPD	8	7	7	8	7	7	5	6	10
RM GPD	8	7	8	8	7	7	6	6	11
GARCH GPD	8	7	8	8	7	7	6	6	11
Bootstr FHS	1	3	1	1	2	4	2	2	1
Bootstr HS250	4	5	3	4	4	3	3	4	5
Bootstr HS500	3	5	3	4	4	5	4	4	6
Bootstr KHS250	5	6	5	7	6	5	4	5	7
Bootstr KHS500	5	6	5	7	5	6	4	5	8
Bootstr MHS250	1	2	2	2	1	2	2	4	1
Bootstr MHS500	3	4	2	3	3	2	2	3	4
Bootstr BRW	6	7	6	5	8	6	6	5	9
EVT GARCH	2	2	1	6	2	1	3	1	2
GPD	7	1	4	2	1	1	1	2	3
	JALSH	BOVE	MEXBOL	KLCI	CRTX	SENSEX	H SENG	TAIPEI	Average
VCV GPD	JALSH 6	BOVE 6	MEXBOL 6	KLCI 4	CRTX 6	SENSEX 6	H SENG 5	TAIPEI 7	Average 9
VCV GPD RM GPD					-				
RM GPD GARCH GPD	6	6	6	4	6	6	5	7	9
RM GPD	6 7	6	6	4	6	6 7	5 5	7 7	9 10
RM GPD GARCH GPD	6 7	6 6 6	6 6 6	4 4 6	6 6 5	6 7 6	5 5 5	7 7 7	9 10 10
RM GPD GARCH GPD Bootstr FHS	6 7 7 1	6 6 6 3	6 6 6 2	4 4 6 1	6 6 5	6 7 6 5	5 5 5 2	7 7 7 4	9 10 10 3
RM GPD GARCH GPD Bootstr FHS Bootstr HS250	6 7 7 1 4	6 6 6 3 4	6 6 6 2 3	4 4 6 1 2	6 6 5 1 4	6 7 6 5 4	5 5 5 2 4	7 7 7 4 3	9 10 10 3 5
RM GPD GARCH GPD Bootstr FHS Bootstr HS250 Bootstr HS500	6 7 7 1 4 3	6 6 6 3 4	6 6 6 2 3	4 4 6 1 2 5	6 6 5 1 4	6 7 6 5 4 2	5 5 5 2 4 4	7 7 7 4 3 3	9 10 10 3 5
RM GPD GARCH GPD Bootstr FHS Bootstr HS250 Bootstr HS500 Bootstr KHS250	6 7 7 1 4 3 5	6 6 6 3 4 4 5	6 6 6 2 3 3	4 4 6 1 2 5	6 6 5 1 4 4 6	6 7 6 5 4 2 4	5 5 5 2 4 4 4	7 7 7 4 3 3 5	9 10 10 3 5 5
RM GPD GARCH GPD Bootstr FHS Bootstr HS250 Bootstr HS500 Bootstr KHS250 Bootstr KHS250	6 7 7 1 4 3 5	6 6 6 3 4 4 5 5	6 6 6 2 3 3 4 4	4 4 6 1 2 5 2 5	6 6 5 1 4 4 6 7	6 7 6 5 4 2 4 3	5 5 5 2 4 4 4 3	7 7 7 4 3 3 5 5	9 10 10 3 5 5 6
RM GPD GARCH GPD Bootstr FHS Bootstr HS250 Bootstr HS500 Bootstr KHS250 Bootstr KHS500 Bootstr MHS250	6 7 7 1 4 3 5 4	6 6 6 3 4 4 5 5	6 6 6 2 3 3 4 4	4 4 6 1 2 5 2 5 2	6 6 5 1 4 4 6 7 2	6 7 6 5 4 2 4 3 3	5 5 5 2 4 4 4 3 2	7 7 7 4 3 3 5 5 3	9 10 10 3 5 5 6 7
RM GPD GARCH GPD Bootstr FHS Bootstr HS250 Bootstr HS500 Bootstr KHS250 Bootstr KHS500 Bootstr MHS250 Bootstr MHS250	6 7 7 1 4 3 5 4 1 2	6 6 6 3 4 4 5 5 5 2 4	6 6 6 2 3 3 4 4 2 1	4 4 6 1 2 5 2 5 2	6 6 5 1 4 4 6 7 2	6 7 6 5 4 2 4 3 3	5 5 5 2 4 4 4 3 2 3	7 7 7 4 3 3 5 5 5 3	9 10 10 3 5 6 7 2

Lowest value marks the most successful ES model