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Fertility, Human Capital Accumulation, and the Pension System

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Abstract

This paper provides a unified treatment of externalities associated with fertility and human capital accumulation as they relate to pension systems. It considers an overlapping generations model in which every generation consists of high earners and low earners with the proportion of types being determined endogenously. The number of children is deterministically chosen but the children's future ability is in part stochastic, in part determined by the family background, and in part through education. In addition to the customary externality source associated with a change in average fertility rate, this setup highlights another externality source. This is due to the effect of a parent's choice of number and educational attainment of his children on the proportion of high-ability individuals in the steady state. Our results include: (i) Investments in education of high- and low-ability parents must be subsidized, (ii) direct child subsidies to one or both parent types can be negative; i.e., they can be taxes, (iii) net subsidies to children (direct child subsidies plus education subsidies) to high-ability parents are always positive, and to low-ability parents can be positive or negative, (iv) either education subsidies or child subsidies, when used alone, can dominate the other instrument, (v) using child subsidy instruments alone entails a higher fertility rate and a lower ratio of high- to low-ability children, as compared to using education subsidies alone.

JEL Code: H55, J13.

Keywords: pay-as-you-go social security, endogenous fertility, education, endogenous ratio of high to low ability types, three externality sources, education subsidies, child subsidies.

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1 Introduction

One of the most pressing problems facing the economies of the industrialized world is the fiscal solvency of their pay-as-you-go (PAYGO) social security systems.¹ An important contributing factor to this problem has been the recent drastic fertility declines in Western Europe and Japan. What truly determines fertility, and what accounts for the observed evolution in fertility behavior, are still open questions. What is clear, however, is that, faced with a PAYGO social security system, parents do not have the right incentives to choose a fertility rate that is optimal. In such systems, each person's fertility decision affects the economy's population growth rate and with it everybody's pension benefits. Specifically, an increase in the rate of population growth increases the number of future workers who will have to support a retired person. No individual, however, takes this impact into account and that leads to a decentralized equilibrium outcome with too few children.²

The above problem is exacerbated by another externality associated with the "quality" of children, and their human capital accumulation, through the education decisions of parents. The rate of return of a pay-as-you-go system depends not just on the fertility rate, but also on productivity growth. The more productive the children, the higher will be their ability to produce and to pay taxes. This reinforces the public good nature of a family's child-rearing activities.³

Most of the literature has thus far treated the quality and quantity issues separately; or else have lumped the investments in quantity and quality together as if one decision

¹This has led to reforms in a number of countries. See Penner (2007) who surveys the recent reforms in Canada, Germany, Italy, Japan, Sweden, and the UK.

²In addition to this "intergenerational transfer" effect, the literature has also noted an offsetting force called "capital dilution" effect: A higher fertility rate, given the aggregate capital saved by the previous generation, implies a lower capital to labor ratio reducing per capita output; see Michel and Pestieau (1993) and Cigno (1993).

³To internalize the quantity and quality effects, some economists have advocated a policy of linking pension benefits (or contributions) to individuals' fertility choices. See, among others, Abio *et al.* (2004), Bental (1989), Cigno *et al.* (2003), Fenge and Meier (2004), Kolmar (1997), van Groezen *et al.* (2000, 2003).

determines both.⁴ A basic shortcoming of this approach is that it cannot distinguish between child subsidies, which correct externalities emanating from fertility decisions, and education subsidies which correct for externalities due to investing in education. This lack of distinction becomes more of a serious problem when the two types of externalities interact as they often do.

To be sure, there are a number of studies in the literature that distinguish between quantity and quality decisions and study them both in one unified framework. Peters (1995) is an early example of this. In his model, both fertility and education choices are made deterministically. The main shortcomings of his approach are the deterministic nature of both quantity and quality decisions, and the lack of any heterogeneity among parents. Cigno *et al.* (2003) also allow for both fertility and quality. Fertility is fully deterministic, but children's quality, which Cigno *et al.* define in terms of "lifetime tax contributions", is in part random and in part determined through actions of parents. The limitations of their study come from the static nature of their model, in looking at the decisions of the initial parent only, and their not allowing for heterogeneity among parents.

Cigno and Luporini (2003), while building on Cigno *et al.* (2003), allow for parents' heterogeneity in terms of their ability to influence their children's probability of success in life.⁵ However, their model remains static in nature as they too do not go beyond the decisions of the initial parents. In Meier and Wrede (2008) both fertility and types are partly stochastic and partly determined by investments. The limitation of their model comes from their ignoring the impact of fertility and education investments on the distribution of types in the economy. But this induced change in the distribution of types constitutes an important component of fertility and education externalities.⁶

⁴Cremer *et al.* (2003, 2008) are examples of this latter approach, while Cremer *et al.* (2006) is concerned only with quantity decisions.

⁵They also drop Cigno *et al.*'s (2003) assumption that fertility is fully deterministic.

⁶Sinn (2004) also considers a model that allows for both fertility and quality. In his setup fertility is fully random and quality fully deterministic. However, Sinn is interested more in examining the

The current paper addresses the quantity and quality questions in an overlapping generations model with high- and low-ability individuals. The unique feature of our study is its endogenous determination of the distribution of types. Specifically, we allow for this distribution to be affected by both education and fertility decisions. This framework gives rise to three sources of externality. First, there is the customary externality associated with the change in average fertility—the intergenerational transfer effect. It arises from the fertility decisions of parents. This source of externality disappears if the pension system is a pre-funded one. The second source of externality emanates from decisions that change the distribution of types even if average fertility is kept constant. It arises from both education decisions and fertility decisions. Its unique feature is that it does not depend on the institution of social security and exists for pre-funded systems as well. The third source of externality is due to interaction between average fertility and the distribution of types. It too arises from both education decisions and fertility decisions. It is different from the second externality source in that it exists because of the PAYGO institution and disappears if one moves to a pre-funded system. It is also different from the first externality source because it will not exist if the distribution of types were immutable.

One distinguishing element between quantity and quality decisions is that of timing. One decides on the number of children quite early; the quality of children, i.e. their future earning capacity, is determined much later. We incorporate this timing sequence in our two-period overlapping generations model by assuming a sequential decision making process: At the end of the first-period, the young decide on starting a family and having children first and then on the extent of their children’s education.

We assume that parents choose the number of their children deterministically. It is true that the actual number of children in a family does not necessarily coincide with the number that parents initially intended to have.⁷ However, this choice is intrinsically

properties of a traditional PAYGO system rather than the design of an optimal pension plan.

⁷Infertility, premature death, misplanning and multiple births are some of the reasons explaining

more deterministic and less susceptible to random and other shocks than determining the quality of one's children. As to the quality, it is unrealistic to expect that one can determine the future earning abilities of one's children in a deterministic fashion simply by investing in their education and training. We assume that quality is determined by three factors. One is random; the second is due to education; and the third is pre-determined by one's "genes" and family background. Nevertheless all children of a particular parent turn out to be either of high- or of low-ability.

Finally, we study the design of pension systems within the Samuelson's (1958) overlapping generations framework as opposed to Diamond's (1965). We thus assume that transfer of resources to the future can occur only through a storage technology with a fixed rate of return. This approach makes the choice of PAYGO or storage to be optimally mutually exclusive: One uses one mechanism or the other depending on whether the average fertility rate⁸ or the interest rate is higher. This dichotomy yields a stark picture of the externality sources that remain even in the absence of PAYGO pension plans.

2 The model

2.1 Preliminaries

Consider, within an overlapping generations framework, the sequence of decisions a child has to face after he is born. First, upon reaching adulthood, he has to decide on starting a family and having children. Subsequently, as a parent, he has to decide on the extent of his children's education. Finally, the retirement period arrives. Such a rich model allows for children, adults, parents, and the retired (grand parents) to overlap, requiring a four-period overlapping generations model. Figure 1 depicts this sequence. However, analyzing a full-fledged four period model quickly becomes cumbersome and too detailed

this gap.

⁸What Samuelson (1958) called the "biological" rate of interest.



Figure 1:

for developing insights. We thus take a short cut and transform the four-period setup we have in mind into a simple two-period overlapping generations model. To do this we assume the decisions of having children and educating them occur sequentially just prior to the beginning of one’s retirement; see Figure 2. This saves us from having to distinguish between working as an adult and working as a parent.

Assume each generation consists of two types of people; they possess either a high or a low earning ability. Denote high- and low-ability types by subscripts h and l and let $j = h, l$. All children of a particular parent will turn out to be either of high- or of low-ability; no mix of high- and low-ability children is possible. There are three factors that determine if a child turns into a high- or a low-ability individual. One is due education; the second is a random element; and the third is pre-determined by one’s “genes” and family background. The effect of education on ability is, *ceteris paribus*, most certainly positive. To introduce randomness into this process, we assume that investing in education does not necessarily transform a child into a high-ability type; instead, it only increases the *probability* of its occurrence. Thus, when a j -type parent invests e “units” in educating his child, the child will have a $\pi_j = \pi_j(e)$ *probability* of turning out to be of *high-ability*. Naturally, the probability that the child will be of

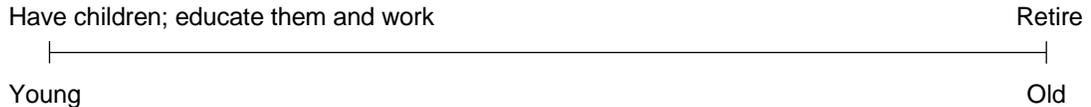


Figure 2:

low-ability is $1 - \pi_j$. We assume that $\pi_j(\cdot)$ is an increasing and strictly concave function with $\pi_j(0) > 0$.

The third factor, the child's family background, manifests itself through the functional form of $\pi_j(e)$ and that is why the function is indexed by j . Specifically, one would expect that $\pi_h(e) > \pi_l(e)$. That is, for the same level of (formal) education, children of high-ability parents have a higher chance of becoming more able. This reflects the fact that high-ability parents tend to spend more time reading to their children and engage them in activities that builds up their human capital. To say more about the structure of $\pi_j(e)$, one needs to know the precise nature of the interaction between (formal) education and family background on a child's ability. Decompose $\pi_j(e)$ into two distinct elements: an educational component $\pi(e)$ and a family background component represented by a parameter θ_j , with $\theta_l < \theta_h$. One can make either of the following assumptions about the interaction between $\pi(e)$ and θ_j . In one, the relationship is *additive* so that $\pi_j = \pi(e) + \theta_j$.⁹ According to this formulation, the marginal productivity of spending e dollars on educating one's children is the same regardless of the parent's type.

⁹Observe that in this case $\theta_l < \theta_h \leq 1 - \pi(e)$.

In the other, the relationship between $\pi(e)$ and θ_j is *multiplicative* with $\pi_j = \theta_j \pi(e)$.¹⁰ This alternative assumption states that the marginal productivity of spending e dollars is higher for the more able parents. We will point out below when the implications of the two assumptions differ for the results.

Assume generation T consists of N_T people. Denote the proportion of high-ability persons in generation T by δ_T ($0 < \delta_T < 1$) so that the number of high-ability persons in generation T is $\delta_T N_T$. Parents choose the number of the children they want to have and do so deterministically. Denote the number of children each j -type parent will have by n_j . Thus $\delta_T N_T$ high-ability parents of generation T end up with $(\delta_T N_T) n_h \pi_h$ high-ability children and $(\delta_T N_T) n_h (1 - \pi_h)$ low-ability children. Similarly, $(1 - \delta_T) N_T$ low-ability persons of generation T end up with $(1 - \delta_T) N_T n_l \pi_l$ high-ability children and $(1 - \delta_T) N_T n_l (1 - \pi_l)$ low-ability children. Consequently, the proportion of high-ability children in the next generation will be

$$\delta_{T+1} = \frac{\delta_T N_T n_h \pi_h + (1 - \delta_T) N_T n_l \pi_l}{\delta_T N_T n_h + (1 - \delta_T) N_T n_l} = \frac{\delta_T n_h \pi_h + (1 - \delta_T) n_l \pi_l}{\delta_T n_h + (1 - \delta_T) n_l}. \quad (1)$$

2.2 Steady state

In the steady state, $\delta_{T+1} = \delta_T \equiv \delta$. It then follows from equation (1) relating δ_{T+1} to δ_T that

$$\frac{\delta n_h \pi_h + (1 - \delta) n_l \pi_l}{\delta n_h + (1 - \delta) n_l} = \delta. \quad (2)$$

Observe that δ is a weighted average of π_h and π_l and thus bracketed by them. Moreover, equation (2) indicates that δ is homogeneous of degree zero in (n_l, n_h) . It follows from Euler's Theorem that

$$n_h \frac{\partial \delta}{\partial n_h} + n_l \frac{\partial \delta}{\partial n_l} = 0. \quad (3)$$

Let e_j denote the j -type's investment in the education of his children. Solve equation

¹⁰In this case, $\theta_l < \theta_h \leq 1/\pi(e)$.

(2) for δ and write the solution as $\delta = \delta(e_h, e_l, n_h, n_l)$. Introduce

$$Z \equiv 2\delta(n_h - n_l) + n_l(1 + \pi_l) - n_h\pi_h. \quad (4)$$

Differentiating (2) yields the following partial derivatives:

$$\frac{\partial\delta}{\partial e_h} = \frac{\delta n_h \pi'_h(e_h)}{Z}, \quad (5)$$

$$\frac{\partial\delta}{\partial e_l} = \frac{(1 - \delta)n_l \pi'_l(e_l)}{Z}, \quad (6)$$

$$\frac{\partial\delta}{\partial n_h} = \frac{\delta(\pi_h - \delta)}{Z}, \quad (7)$$

$$\frac{\partial\delta}{\partial n_l} = \frac{(1 - \delta)(\pi_l - \delta)}{Z}. \quad (8)$$

We prove in Appendix A that a necessary condition for the stability of steady-state solution for δ , namely $|\partial\delta_{T+1}/\partial\delta_T| < 1$, is that $Z > 0$. Thus, assuming a stable steady state implies that $Z > 0$ so that

$$\frac{\partial\delta}{\partial e_h} > 0, \quad \frac{\partial\delta}{\partial e_l} > 0, \quad \frac{\partial\delta}{\partial n_h} \times \frac{\partial\delta}{\partial n_l} < 0.$$

2.3 Laissez faire

Individuals have preferences over consumption when young, c , consumption when retired, d , and the number of children, n . Preferences are represented by

$$U = u(c) + v(d) + \varphi(n). \quad (9)$$

Assume each j -type person earns an income equal to $\beta_j I$ when young, where $\beta_h > \beta_l$. Without any loss of generality, set $\beta_l = 1$ and $\beta_h = \beta > 1$. Denote the non-education cost of raising a child by a and the “quantity” of education provided to a child by e . Choose the units of measurement for c , d , and e such that their producer prices are one. The young individual spends a portion of his income on his immediate consumption, c , a portion on raising his children, an , and another portion on educating his children,

en. He saves the rest of his income in a storage technology with a rate of return equal to r . Upon retirement, the individual receives and spends all his savings plus interest, leaving no bequests.

The budget constraint for the j -type is given by

$$\beta_j I = c_j + \frac{d_j}{1+r} + e_j n_j + a n_j. \quad (10)$$

The j -type young individual chooses c_j, d_j, n_j , and e_j to maximize his utility (9) subject to his budget constraint (10). One can easily see that the solution for education expenditures requires $e = 0$. This is not surprising given that education is costly to the parent but bestows no utility upon him.¹¹ Setting $e = 0$ and manipulating the first-order conditions with respect to c_j, d_j , and n_j , the laissez faire solutions for these variables are found from

$$\frac{v'(d_j)}{u'(c_j)} = \frac{1}{1+r}, \quad (11)$$

$$\frac{\varphi'(n_j)}{u'(c_j)} = a, \quad (12)$$

$$\beta_j I = c_j + \frac{d_j}{1+r} + n_j a. \quad (13)$$

Given strong separability and concavity of all subutility functions, c, d , and n are all normal goods so that $c_h > c_l, d_h > d_l$, and $n_h > n_l$. This result is summarized as

Proposition 1 *Consider an overlapping generations model in the steady state with two types of people in each generation: high- and low-ability. Each type receives an income commensurate with his ability when young and has preferences over consumption during working years and retirement, as well as the number of children he will have. Each type can have children of either ability. The probability of having a high-ability child*

¹¹This result is due to the assumption that parents love children of the same ability equally. If parents prefer a high-ability child to a low-ability child, their utility will be affected through educational attainment of their children. Under this circumstance, $e \neq 0$. See Section 5.2 below.

depends positively on investment in education and is higher, *ceteris paribus*, for high-ability parents. Then:

(i) Investment in education by either type of parents increases the proportion of high-ability persons in the steady state, δ .

(ii) The increase in the number of children of either type of parents can increase as well as decrease δ . If δ increases with the number of children of one type parents, it will decrease with the number of children of the other type.

(iii) In *laissez-faire*, high-ability parents consume more during working years and retirement, and have a higher number of children (as compared to low-ability parents). Neither types invests in education.

3 Utilitarian First Best

3.1 The problem and its solution

Denote the savings of an individual of type j by $S_j \geq 0$ and the population growth rate by

$$\bar{n} \equiv \delta n_h + (1 - \delta)n_l. \quad (14)$$

The economy's resource constraint is then written as

$$\begin{aligned} [\delta\beta + (1 - \delta)]I + \frac{[\delta S_h + (1 - \delta)S_l](1 + r)}{\bar{n}} \geq \delta \left[c_h + \frac{d_h}{\bar{n}} + \right. \\ \left. n_h(a + e_h) + S_h \right] + (1 - \delta) \left[c_l + \frac{d_l}{\bar{n}} + n_l(a + e_l) + S_l \right]. \end{aligned} \quad (15)$$

Given a fixed rate of return on savings, the consumption of the retired should be financed either through private savings or from taxes imposed on the young as in a pay-as-you-go retirement system. The mechanism with a higher rate of return, r or \bar{n} , Samuelson's (1958) biological rate of return, should be used exclusively. This property makes it simpler to solve the social planner's problem in a sequential manner. First, one finds the optimum conditional on the use of storage and PAYGO; then one compares the

associated welfare levels of the two conditional optima. We study the more interesting case of PAYGO in the text and discuss the storage technology in Appendix B.

In the absence of private savings, the economy's resource constraint (15) simplifies to

$$[1 + (\beta - 1)\delta]I \geq \delta \left[c_h + n_h (a + e_h) + \frac{d_h}{n} \right] + (1 - \delta) \left[c_l + n_l (a + e_l) + \frac{d_l}{n} \right]. \quad (16)$$

The government's optimization problem is then summarized by the Lagrangian

$$\begin{aligned} \mathcal{L} = & \delta [u(c_h) + v(d_h) + \varphi(n_h)] + (1 - \delta) [u(c_l) + v(d_l) + \varphi(n_l)] \\ & + \mu \left\{ [1 + (\beta - 1)\delta]I - \delta \left[c_h + n_h (a + e_h) + \frac{d_h}{n} \right] \right. \\ & \left. - (1 - \delta) \left[c_l + n_l (a + e_l) + \frac{d_l}{n} \right] \right\}, \end{aligned}$$

leading to the following first-order conditions with respect c_h, c_l, d_h and d_l :

$$\frac{\partial \mathcal{L}}{\partial c_h} = \delta [u'(c_h) - \mu] = 0, \quad (17)$$

$$\frac{\partial \mathcal{L}}{\partial c_l} = (1 - \delta) [u'(c_l) - \mu] = 0, \quad (18)$$

$$\frac{\partial \mathcal{L}}{\partial d_h} = \delta [v'(d_h) - \frac{\mu}{n}] = 0, \quad (19)$$

$$\frac{\partial \mathcal{L}}{\partial d_l} = (1 - \delta) [v'(d_l) - \frac{\mu}{n}] = 0. \quad (20)$$

Manipulating these conditions yields

$$c_h = c_l = c, \text{ and } d_h = d_l = d.$$

3.2 Externalities due to e and n

Introduce

$$\begin{aligned} D \equiv & \frac{\partial \mathcal{L}}{\partial \delta} = [\varphi(n_h) - \varphi(n_l)] \\ & + u'(c) \left\{ (\beta - 1)I - [n_h (a + e_h) - n_l (a + e_l)] + \frac{(n_h - n_l) d}{n^2} \right\}, \quad (21) \end{aligned}$$

so that D shows the change in social welfare due to an increase in the proportion of high-ability persons in the population.¹² With $c_h = c_l$ and $d_h = d_l$, the first bracketed term on the right-hand side of (21) shows the net change in utilities. The second bracketed expression shows the *net* change in resources; i.e. the increase in the available resources minus the extra resources required in consumption. Using the definition of D and the previous findings that $c_h = c_l = c$, $d_h = d_l = d$, and $\mu = u'(c)$, one can write the first-order conditions for the maximization of social welfare with respect to n_h, n_l, e_h , and e_l as

$$\frac{\partial \mathcal{L}}{\partial e_h} = -\delta n_h u'(c) + D \frac{\partial \delta}{\partial e_h} = 0, \quad (22)$$

$$\frac{\partial \mathcal{L}}{\partial e_l} = -(1 - \delta) n_l u'(c) + D \frac{\partial \delta}{\partial e_l} = 0, \quad (23)$$

$$\frac{\partial \mathcal{L}}{\partial n_h} = \delta \left[\varphi'(n_h) - \left(a + e_h - \frac{d}{\bar{n}^2} \right) u'(c) \right] + D \frac{\partial \delta}{\partial n_h} = 0, \quad (24)$$

$$\frac{\partial \mathcal{L}}{\partial n_l} = (1 - \delta) \left[\varphi'(n_l) - \left(a + e_l - \frac{d}{\bar{n}^2} \right) u'(c) \right] + D \frac{\partial \delta}{\partial n_l} = 0. \quad (25)$$

Note that, with $\partial \delta / \partial e_h > 0$ and $\partial \delta / \partial e_l > 0$, either one of conditions (22) or (23) implies $D > 0$.

Recall that investing in education imposes only a cost on the individual but no benefit. Indeed, considering that the individual treats δ as given, this cost will be the only effect on him as e_j increases. This increase entails a cost measured by $-n_j$. Equations (22) and (23) thus reveal the existence of an externality represented by

$$\frac{D}{u'(c)} \frac{1}{\delta} \frac{\partial \delta}{\partial e_h} \quad \text{for increasing } e_h, \quad (26)$$

$$\frac{D}{u'(c)} \frac{1}{1 - \delta} \frac{\partial \delta}{\partial e_l} \quad \text{for increasing } e_l. \quad (27)$$

This externality arises through the effect of e_j on δ . Moreover, given that $\partial \delta / \partial e_j > 0$ and $D > 0$, this is a positive externality.

¹²Being a proportion, this is matched by a reduction in the proportion of low-ability persons.

The externality terms (26)–(27) coming through δ may be divided into two parts. One is due to the direct change in δ as e_j changes. When there is an increase in the proportion of high-ability persons in the population, matched of course by a reduction in the proportion of low-ability persons, social welfare changes by the difference in the utilities of high- and low-ability types *and* the change in the *net* resources (income minus consumption). This effect does not work through fertility; it is present also in the absence of PAYGO pension plans when all second-period consumptions are financed by private savings. The second part, on the other hand, works through changing average fertility. Its existence depends on having a PAYGO pension plan in place.¹³ It arises indirectly as the change in δ changes \bar{n} as well. Remember that \bar{n} depends on δ and δ depends on e_j (as well as n_j). This change in \bar{n} is also neglected in private calculations. With $\bar{n} = n_l + \delta(n_h - n_l)$, this effect depends on the difference between n_h and n_l . The various terms in $D/u'(c)$ represent these two direct and indirect externalities. The latter is captured by the $(n_h - n_l) d/\bar{n}^2$ term that appears in the definition of $D/u'(c)$, and the former by the remaining expressions therein.

Similarly, increasing n_j has externalities of its own. When a j -type individual increases his fertility rate, he does not take the effect of his decision on \bar{n} into consideration. He thus perceives the effect of increasing n_j in his *net* welfare to consist of an increase in his utility, $\varphi'(n_j)/u'(c)$ when expressed in monetary units, minus an increase in his expenditures on n_j , measured by a . Comparing this with the expressions in equations (24) and (25) reveals the existence of externalities represented by

$$\frac{d}{\bar{n}^2} + \frac{D}{u'(c)} \frac{1}{\delta} \frac{\partial \delta}{\partial n_h} \quad \text{for increasing } n_h, \quad (28)$$

$$\frac{d}{\bar{n}^2} + \frac{D}{u'(c)} \frac{1}{1 - \delta} \frac{\partial \delta}{\partial n_l} \quad \text{for increasing } n_l. \quad (29)$$

The externalities associated with n_j , as depicted by expressions (28)–(29), consist of two distinct elements. While the first element has no counterpart in the externalities

¹³That only one of the two components of the externality through δ is active for pre-funded systems is demonstrated in Appendix B.

associated with e_j , the second element is identical in nature to the externality coming from e_j . The term d/\bar{n}^2 represents the first element and captures the effect of increasing n_h or n_l on \bar{n} , and through it on the aggregate resources available for distribution between the young and the old under PAYGO. Specifically, this externality tells us that increasing fertility increases the number of future working people who support a retired person. This is the familiar positive “intergenerational transfer” effect that appears in the literature on growth with endogenous fertility; see Cigno (1993) and Michel and Pestieau (1993). The second externality source, represented by the second expressions in (28)–(29), is due to the change in δ . It is the same type of externality discussed previously in relation to the effect of e_j on δ . The crucial point is that these externalities emanate from a change in δ which can come about from a change in either n_j or e_j . This is why each of the second expressions in (28)–(29) is identical to its counterpart in (26)–(27) except that $\partial\delta/\partial n_h$ and $\partial\delta/\partial n_l$ have replaced $\partial\delta/\partial e_h$ and $\partial\delta/\partial e_l$. Finally, observe that with $D > 0$, this externality source is positive if $\partial\delta/n_j > 0$ and is negative if $\partial\delta/n_j < 0$. Recall also that $\partial\delta/n_h$ and $\partial\delta/n_l$ are of opposite signs; hence one ability type exerts a positive externality, and the other a negative externality, on the society through their fertility decisions when mediated through δ .

The results thus far are summarized as

Proposition 2 *(i) Under the utilitarian first-best solution with PAYGO, consumption when working and consumption when retired are equalized across types.*

(ii) Investing in education of children by either type of parents increases the proportion of high-ability children in the economy and bestows a positive externality on everybody else. This externality has two components, one of which exists only in the presence of PAYGO pension plans.

(iii) A parent’s fertility choice imposes two kinds of externalities on everyone else. One is the familiar positive externality known as “intergenerational transfer” effect. The other emanates from a change in the proportion of high-ability children. This externality

too has two components, one of which exists only in the presence of PAYGO pension plans.

3.3 Optimal characterizations of e_j and n_j

To characterize of the first-best solutions for e_j and n_j , substitute the expressions for $\partial\delta/\partial e_h$ and $\partial\delta/\partial e_l$ from (5)–(6) into equations (22)–(23), simplify, and subtract one equation from another to get

$$\frac{D}{u'(c)} \frac{\pi'_h(e_h) - \pi'_l(e_l)}{Z} = 0. \quad (30)$$

With $D > 0$, it follows from (30) that

$$\pi'_h(e_h) = \pi'_l(e_l). \quad (31)$$

This makes perfect sense. At the optimum, the last dollar spent on education by either type must have the same impact on each type's probability of having a high-ability child.

Turning to the relationship between n_h and n_l , substitute the expressions for $\partial\delta/\partial n_h$ and $\partial\delta/\partial n_l$ from (7)–(8) into equations (24)–(25) and simplify. Then subtract one equation from another to get

$$\varphi'(n_h) - \varphi'(n_l) - (e_h - e_l) u'(c) + \frac{D}{Z} (\pi_h - \pi_l) = 0. \quad (32)$$

To see the intuition for this result, consider a concomitant increase in n_h and a reduction in n_l . On the one hand, this changes the utilities of the two types of parents by $\varphi'(n_h) - \varphi'(n_l)$. On the other hand, there will be an increase in resource cost to the economy because educational expenditures increase by $e_h - e_l$ which is worth $(e_h - e_l) u'(c)$ in terms of utilities. This should be subtracted from $\varphi'(n_h) - \varphi'(n_l)$. Additionally, there is a gain to the economy through the externalities that emanate from a change in δ . This added to the expression. The above relationship tells us that at the optimum the sum of all the marginal effects must be zero.

To go beyond these observations, and determine the precise relationships between e_h and e_l and between n_h and n_l , we have to know more about the structure of $\pi_j(\cdot)$. It is clear from (31) that the relative size of e_h and e_l is otherwise indeterminate. Moreover, with an indeterminate relationship between e_h and e_l , equation (32) shows that the relationship between n_h and n_l is also indeterminate. We examine these issues next.

3.3.1 Additive relationship between education and family background

Assume $\pi_j = \pi(e) + \theta_j$. It then follows from equation (31) that

$$e_h = e_l \equiv e. \quad (33)$$

The intuition behind this result is that e_h and e_l have identical effects on the *net* resources of the economy as well as on utilities; hence their values should be the same. Given that parents do not care about the type of their children, e_h and e_l have no effect on utilities. As far as costs are concerned, one unit of education has the same resource cost regardless of who spends it. Finally, when the marginal productivity of education is independent of the parent's type, e_h and e_l imply identical externalities as well.

Next, observe that $e_h = e_l$ implies that $\pi_h > \pi_l$ (because $\theta_h > \theta_l$). It then follows from equations (7)–(8) that $\partial\delta/\partial n_h > 0$ and $\partial\delta/\partial n_l < 0$. That is, an increase in the fertility rate of high-ability parents increases δ and an increase in the fertility rate of low-ability parents decreases δ . Recall also that the externality due to δ is positive if $\partial\delta/\partial n_j > 0$ and negative if $\partial\delta/\partial n_j < 0$. Consequently, increasing the fertility rate of high-ability parents entails a positive externality while increasing the fertility rate of low-ability parents entails a negative externality.

Finally, substitute $e_h = e_l \equiv e$ in equation (32) and simplify to get

$$\varphi'(n_h) - \varphi'(n_l) = \frac{D}{Z}(\theta_l - \theta_h) < 0.$$

It follows from the strict concavity of $\varphi(\cdot)$ that

$$n_h > n_l.$$

To see the intuition for this result, observe that with $e_h = e_l$ the only effect of a concomitant increase in n_h and a reduction in n_l on resources comes from the externalities that emanate from a change in δ . This is equal to $(\theta_h - \theta_l) D/Z$. At the optimum, this effect must just offset the change in the utilities, $\varphi'(n_h) - \varphi'(n_l)$. That is, the two effects must sum to zero. Given that the externality effect is positive, $\varphi'(n_h) - \varphi'(n_l)$ must be negative.

We have:

Proposition 3 *Assume the relationship between education and family background is additive. Then under the utilitarian first-best solution with PAYGO,*

(i) *Both types of parents invest equally in education.*

(ii) *High-ability parents have more children.*

(iii) *Increasing the fertility rate of high-ability parents increases the proportion of high-ability children in the economy and thus bestows a positive externality on everybody else.*

(iv) *Increasing the fertility rate of low-ability parents, reduces the proportion of high-ability children and imposes a negative externality on everybody else.*

3.3.2 Multiplicative relationship between education and family background

Assume next that $\pi_j = \theta_j \pi(e)$. It then follows from equation (31) that

$$\frac{\pi'(e_h)}{\pi'(e_l)} = \frac{\theta_l}{\theta_h} < 1.$$

This equation implies $\pi'(e_h) < \pi'(e_l)$. Hence, given the concavity of $\pi(\cdot)$,

$$e_h > e_l.$$

The difference between this case and the previous case is the positive effect of a parent type on the marginal productivity of education. It is precisely because of this reason that one now requires e_h to exceed e_l .

Now with $e_h > e_l$ and $\theta_h > \theta_l$, we will again have $\pi_h > \pi_l$. Consequently, as in the previous additive case, equations (7)–(8) imply that $\partial\delta/\partial n_h > 0$ and $\partial\delta/\partial n_l < 0$. That is, an increase in the fertility rate of high-ability parents increases δ and entails a positive externality. On the other hand, an increase in the fertility rate of low-ability parents decreases δ and entails a negative externality.

Turning to the comparison between n_h and n_l , we now have from equation (32) that

$$\varphi'(n_h) - \varphi'(n_l) = (e_h - e_l)u'(c) + \frac{D}{Z} [\theta_l\pi(e_l) - \theta_h\pi(e_h)].$$

Now $e_h - e_l > 0$ implies that $\pi(e_h) > \pi(e_l)$. With $\theta_h > \theta_l$, then $\theta_l\pi(e_l) - \theta_h\pi(e_h) < 0$. Thus the first expression on the right-hand side of the above equation is positive and the second expression is negative. This implies that one no longer knows if n_h is larger or n_l . This result may at first appear counter-intuitive given the positive externality associated with the fertility of high-ability parents and the negative externality associated with the fertility of low-ability parents. The intuition comes from the observation that $e_h - e_l > 0$. This term did not exist in the previous case with $e_h = e_l$. Its presence means that increasing the fertility rate of high-ability parents entails extra resource costs to the society as compared to increasing the fertility rate of low-ability parents.

We have:

Proposition 4 *Assume the relationship between education and family background is multiplicative. Then under the utilitarian first-best solution with PAYGO,*

- (i) *High-ability parents invest more in their children.*
- (ii) *Either type can have more children.*
- (iii) *Increasing the fertility rate of high-ability parents increases the proportion of high-ability children in the economy and thus bestow a positive externality on everybody else.*
- (iv) *Increasing the fertility rate of low-ability parents, reduces the proportion of high-ability children and imposes a negative externality on everybody else.*

3.4 Decentralization

As observed earlier, the choice of storage technology or PAYGO is mutually exclusive in our setup. Thus, assuming that PAYGO is preferable, one wants to ensure that all second-period consumptions are financed through pensions. This requires the government to impose a one-hundred percent tax on savings and their returns. Recall also that the optimum required equal consumption levels both during working years and retirement. Consequently, the government must provide everyone with the same pension $P = d_h = d_l = d$ where d is evaluated at its first-best value. Next, to induce the correct choice of fertility and education, two types of subsidies are required. One is a subsidy on education at the rate τ_j for the j -type, the other is a direct child subsidy to the j -type equal to t_j dollars per child. Finally, first-period lump-sum taxes, T_j , are required to ensure that consumption levels during working years are the same for both types. Below, we show how these instruments decentralize the first-best allocations.

Give these instruments, parents decide only on their first-period consumption and fertility rate. Let α_j denote the Lagrangian multiplier associated with the budget constraint of a j -type parent. The optimization problem of this parent is summarized by the Lagrangian expression,

$$\mathcal{L}_j = u(c_j) + \varphi(n_j) + \alpha_j [\beta_j I - c_j - n_j(a - t_j) - (1 - \tau_j)e_j n_j - T_j].$$

The first-order conditions are

$$\frac{\partial \mathcal{L}_j}{\partial c_j} = u'(c_j) - \alpha_j = 0, \quad (34)$$

$$\frac{\partial \mathcal{L}_j}{\partial e_j} = -\alpha_j(1 - \tau_j)n_j = 0, \quad (35)$$

$$\frac{\partial \mathcal{L}_j}{\partial n_j} = \varphi'(n_j) - \alpha_j [a - t_j + (1 - \tau_j)e_j] = 0. \quad (36)$$

The question one needs to examine is how to set the tax rates such that the solution to the individual's first-order conditions (34)–(36) above coincide with the first-best solution (c, e_j, n_h, n_l) from equations (17)–(25).

First, compare equation (35), using (34), with (22) and (23). This tells us that education costs must be subsidized at a rate equal to

$$\tau_h = \frac{D}{u'(c)} \frac{1}{\delta n_h} \frac{\partial \delta}{\partial e_h} = 1, \quad (37)$$

$$\tau_l = \frac{D}{u'(c)} \frac{1}{(1-\delta)n_l} \frac{\partial \delta}{\partial e_l} = 1, \quad (38)$$

where c is set at its first-best value. To understand the intuition behind equations (37)–(38), note that the algebraic expressions in these equations are precisely the externality terms that come into play through δ as e_h and e_l change. The equations then tell us that at the optimum the subsidy rates on education must equate their marginal externality benefits. Moreover, they also tell us that at the optimum the values of these externalities must be unity. This should not be surprising. With education investment generating no private benefits, its price must be subsidized at one-hundred percent; otherwise, one never invests in education.

Second, substitute $\tau_h = \tau_l = 1$ in equation (36) to rewrite it as

$$\varphi'(n_j) - \mu(a - t_j) = 0.$$

Comparing this equation with (24) and (25) results in per child subsidies equal to

$$t_h = \frac{d}{\bar{n}^2} + \frac{D}{u'(c)} \frac{1}{\delta} \frac{\partial \delta}{\partial n_h} - e_h, \quad (39)$$

$$t_l = \frac{d}{\bar{n}^2} + \frac{D}{u'(c)} \frac{1}{1-\delta} \frac{\partial \delta}{\partial n_l} - e_l, \quad (40)$$

where c and e are set at their first-best values.

To understand the intuition behind equations (39)–(40), it will be useful to rewrite them as

$$t_h + \tau_h e_h = \frac{d}{\bar{n}^2} + \frac{D}{u'(c)} \frac{1}{\delta} \frac{\partial \delta}{\partial n_h}, \quad (41)$$

$$t_l + \tau_l e_l = \frac{d}{\bar{n}^2} + \frac{D}{u'(c)} \frac{1}{1-\delta} \frac{\partial \delta}{\partial n_l}, \quad (42)$$

by moving e_j to the left-hand side and recalling that $\tau e_j = e_j$ because $\tau = 1$. The left-hand sides of (41) and (42), $t_h + \tau_h e_h$ and $t_l + \tau_l e_l$, show the *net* subsidy given to an h -type and to an l -type parent for each of his children. The right-hand sides of (41) and (42) consist of the two externality sources described previously; they both are present when n_h and n_l change. These equations thus tell us that, at the optimum, we should subsidize the cost of having a child by an amount equal to its net externality benefit.

Recall that the cost of raising and educating a child is $a + e_j$. A child subsidy of t dollars per child reduces this cost. Similarly, a subsidy to education reduces this cost but through lowering the price of one particular element of it, namely, education cost. Thus a subsidy to education is also a subsidy to children. The difference is that the education subsidy lowers the share of education cost in total cost. On the other hand, a subsidy to children is “neutral” between the two sources of costs.

With $\partial\delta/\partial n_h > 0$, equation (41) tells us that $t_h + \tau_h e_h > 0$, so that the *net* subsidy given to an h -type parent for each of his children must be positive. On the other hand, with $\partial\delta/\partial n_l < 0$, one cannot a priori determine the sign of the expression on the right-hand side of (42). Consequently, the sign of $t_l + \tau_l e_l$ remains indeterminate.

Equations (39)–(40) do not allow us to determine the signs of t_h and t_l . However, if we subtract equation (40) from equation (39), while substituting the expressions for $\partial\delta/\partial n_h$ and $\partial\delta/\partial n_l$ from (7)–(8) in them, we get

$$t_h - t_l = \frac{D}{u'(c)} \frac{\pi_h - \pi_l}{Z} > 0,$$

so that $t_h > t_l$. This makes sense. Recall that we have at the optimum $\partial\delta/\partial n_h > 0$, $\partial\delta/\partial n_l < 0$. Increasing n_h has positive externalities and increasing n_l has negative externalities emanating from δ . The net marginal benefits associated with increasing n_h thus exceeds the net marginal benefits associated with increasing n_l . Because of this, the net subsidy on n_h must exceed the net subsidy on n_l .

Finally, to ensure that the two types will have identical consumption levels during working years, one has to set first-period lump-sum taxes such that both individual

types spend the same amount of money on c . Comparing equation (34) with (17), while setting $\tau_h = \tau_l = 1$, then tells that T_h and T_l must satisfy the following condition

$$T_h - T_l = (\beta - 1)I + n_l(a - t_l) - n_h(a - t_h), \quad (43)$$

where t_h and t_l are set according to equations (39)–(40).

To sum, we have shown that first-best education subsidies must be levied at one hundred percent and that higher ability parents should receive higher child subsidies. However, we have not been able to determine the signs of t_h and t_l . That is, we have not been able to rule out child taxes (as opposed to child subsidies). Nor have we been able to determine the sign of the net subsidy for the children of the low-ability parents, $t_l + \tau_l e_l$. Although, we have established that $t_h + \tau_h e_h > 0$. To throw some light on this issue, we resort to a numerical example. With $t_h > t_l$ and $t_l + \tau_l e_l > t_l$, the strongest candidate is of course t_l .

3.5 A numerical example

Assume (i) the preferences are logarithmic and represented by

$$u = \ln c + b \ln d + \ln n,$$

where b is a positive constant, (ii) the probability of having a high-ability child is related to investment in education according to

$$\pi(e) = 0.75 - \frac{1}{e + 2},$$

and (iii) the relationship between $\pi(e)$ and θ_j is additive with $\theta_l = 0$ and $\theta_h = 0.05$. Set $\beta = 8.5$, and $I = 10$. Then solve this problem for the utilitarian first best following the steps taken in the paper. The following solutions emerge when parameter b takes the indicated values below.

(i) $b = 1.1$:

$$\begin{aligned}n_h &= 8.04; n_l = 5.65; \bar{n} = 6.81; \delta = 0.48; c = 11.04; d = 82.69; \\e &= 1.40; t_h + \tau_h e_h = 2.03; t_l + \tau_l e_l = 1.45; t_h = 0.63; t_l = 0.05.\end{aligned}$$

(ii) $b = 1$:

$$\begin{aligned}n_h &= 7.98; n_l = 5.70; \bar{n} = 6.81; \delta = 0.48; c = 11.59; d = 78.88; \\e &= 1.40; t_h + \tau_h e_h = 1.95; t_l + \tau_l e_l = 1.37; t_h = 0.55; t_l = -0.03.\end{aligned}$$

(iii) $b = 0.10$:

$$\begin{aligned}n_h &= 7.44; n_l = 6.16; \bar{n} = 6.78; \delta = 0.48; c = 20.95; d = 14.77; \\e &= 1.41; t_h + \tau_h e_h = 0.59; t_l + \tau_l e_l = 0.01; t_h = -0.82; t_l = -1.40.\end{aligned}$$

(iv) $b = 0.09$:

$$\begin{aligned}n_h &= 7.43; n_l = 6.17; \bar{n} = 6.78; \delta = 0.48; c = 21.14; d = 13.47; \\e &= 1.41; t_h + \tau_h e_h = 0.57; t_l + \tau_l e_l = -0.02; t_h = -0.85; t_l = -1.43.\end{aligned}$$

Thus as b , the weight of retirement consumption in the utility function, decreases, d decreases and with it the intergenerational transfer effect. This reduces the size of the positive externality of the first type. As a result, we see that first t_l , then t_h , and finally $t_l + \tau_l e_l$, net subsidy for children of the low-ability type, turn into a tax.

The following proposition summarizes our results on decentralization.

Proposition 5 (i) *Investments in education of high- and low-ability parents must be subsidized at one hundred percent and set equal to the externalities they bestow to everyone as given by expressions (37)–(38).*

(ii) *Let t_j denote the direct child subsidy to a j -type parent in dollars. Its value must be set according to (39)–(40). We have $t_h > t_l$ and both t_h and t_l can take positive as well as negative values.*

(iii) *Direct child subsidies and education subsidies both reduce the cost of raising children. Thus a subsidy to education is also a subsidy to fertility. The difference is that the education subsidy lowers the share of education cost in the fertility subsidy. On the other hand, a subsidy to children is “neutral” between the two sources of costs.*

(iv) *Denote the subsidy rate on education investment for the j -type by τ_j . Net subsidies to children are then equal to $t_j + \tau_j e_j$. They must be set equal to the net externalities associated with increasing n_j as shown by expressions (41) and (42). While $t_h + \tau_h e_h$ is always positive, $t_l + \tau_l e_l$ can take positive as well as negative values.*

4 Limited instruments

This section studies the properties of optimal child subsidies versus optimal education subsidies. The underlying assumption is that either one or the other instrument is used so that we have a second-best solution.

4.1 Education subsidy

Without child subsidies, one cannot directly control the number of children. However, one can affect parents’ fertility through education subsidies. Equations (22) or (23) continue to apply

$$\begin{aligned} -\delta n_h u'(c) + D \frac{\partial \delta}{\partial e_h} &= 0, \\ -(1 - \delta) n_l u'(c) + D \frac{\partial \delta}{\partial e_l} &= 0. \end{aligned}$$

With $\partial \delta / \partial e_h > 0$ and $\partial \delta / \partial e_l > 0$, we continue to have $D > 0$. Again, substituting the expressions for $\partial \delta / \partial e_h$ and $\partial \delta / \partial e_l$ into the above equations and subtracting one equation from another yields

$$\frac{D}{u'(c)} \frac{\pi'_h(e_h) - \pi'_l(e_l)}{Z} = 0.$$

Consequently, as with the case with both instruments,

$$\begin{aligned} e_h &= e_l \quad \text{if } \pi_j = \pi(e) + \theta_j, \\ e_h &> e_l \quad \text{if } \pi_j = \theta_j \pi(e). \end{aligned}$$

To decentralize this, one must again subsidize the price of education at one hundred percent. That is

$$\begin{aligned} \tau_h &= \frac{D}{u'(c)} \frac{1}{\delta n_h} \frac{\partial \delta}{\partial e_h} = 1, \\ \tau_l &= \frac{D}{u'(c)} \frac{1}{(1-\delta) n_l} \frac{\partial \delta}{\partial e_l} = 1. \end{aligned}$$

Finally, turning to the choice of n_j , with no child subsidies, individuals set the marginal rate of substitution between n_j and c_j equal to the cost of raising a child: $\varphi'(n_j)/u'(c_j) = a$ as in equation (12). Now since the solution requires $c_h = c_l$, it follows that $n_h = n_l$.

4.2 Child subsidy

Without education subsidies, and with parents not benefiting directly from educating their children, nobody invests in education so that $e_h = e_l = 0$. In this case, equations (24) and (25) continue to apply albeit for the suboptimal value of $e_h = e_l = 0$. We have

$$\begin{aligned} \varphi'(n_h) - \left(a - \frac{d}{\bar{n}^2}\right) u'(c) + \frac{D}{\delta} \frac{\partial \delta}{\partial n_h} &= 0, \\ \varphi'(n_l) - \left(a - \frac{d}{\bar{n}^2}\right) u'(c) + \frac{D}{(1-\delta)} \frac{\partial \delta}{\partial n_l} &= 0. \end{aligned}$$

Subtracting one of the above equations from the other one yields

$$\varphi'(n_l) - \varphi'(n_h) = \frac{D(\pi_h(0) - \pi_l(0))}{Z}.$$

With $\pi(0) > 0$, $\pi_h(0) - \pi_l(0)$ will be positive whether the relationship between $\pi(e)$ and θ_j is additive or multiplicative. Moreover, for education to be of value to the society, the values of $\partial \mathcal{L} / \partial e_h$ and $\partial \mathcal{L} / \partial e_l$ must be positive at $e_h = e_l = 0$. It follows

from the expressions for $\partial\mathcal{L}/\partial e_h$ and $\partial\mathcal{L}/\partial e_l$, shown in equations (22)–(23) that $D > 0$. Consequently, $\varphi'(n_l) - \varphi'(n_h) > 0$ and

$$n_h > n_l.$$

Turning to decentralization, equation (36) continues to apply. Given $e_h = e_l = 0$, this equation implies

$$t_j = a - \frac{\varphi'(n_j)}{u'(c)},$$

which is the equation we had for decentralization of the first-best.¹⁴ Equations (39)–(40) also apply and we have,

$$\begin{aligned} t_h &= \frac{d}{\bar{n}^2} + \frac{D}{u'(c)} \frac{(\pi_h(0) - \delta)}{Z}, \\ t_l &= \frac{d}{\bar{n}^2} + \frac{D}{u'(c)} \frac{(\pi_l(0) - \delta)}{Z}, \end{aligned}$$

with

$$t_h - t_l = \frac{D}{u'(c)} \frac{\pi_h(0) - \pi_l(0)}{Z} > 0.$$

Observe that in this case, child subsidies and net subsidies to children are one and the same.

4.3 Education or child subsidy

The question we would like to address is which instrument should be used if one can use only one of the two. To answer this question, one has to compare the optimal solution when using the education subsidy with the optimal solution when using the child subsidy. There does not seem to be a general answer to this question. One expects that education subsidies will be the better policy whenever productivity differential between high- and low-ability individuals is high, and whenever one's family background plays a minor role

¹⁴Here $e_j = 0$ implies that $(1 - \tau_j)e_j = 0$; at the first best, it was $\tau_j = 1$ which implied $(1 - \tau_j)e_j = 0$.

in determining the ability of a child. To shed some light on this issue, we again resort to a numerical question.

We use the same logarithmic specification for preferences as before with the coefficient of $\ln d$ being set equal to one, the same additive specification for $\pi_j(e)$, and the same functional form for $\pi(e)$. We also set $\theta_l = 0$ and $I = 10$. The parameter values that we allow to change are those for θ_h and β . Below are three sets of solutions.

(i) $\theta_h = 0.05, \beta = 5$:

Education subsidy: $\bar{n} = 2.57; \delta = 0.53; e = 2.05; \delta u_h + (1 - \delta) u_h = 6.57$.

Child subsidy: $\bar{n} = 5.18; \delta = 0.27; e = 0.00; \delta u_h + (1 - \delta) u_h = 6.56$.

(ii) $\theta_h = 0.05, \beta = 4$:

Education subsidy : $\bar{n} = 2.25; \delta = 0.51; e = 1.75; \delta u_h + (1 - \delta) u_h = 5.88$.

Child subsidy : $\bar{n} = 4.51; \delta = 0.27; e = 0.00; \delta u_h + (1 - \delta) u_h = 6.01$.

(iii) $\theta_h = 0.10, \beta = 5$:

Education subsidy : $\bar{n} = 2.64; \delta = 0.56; e = 2.10; \delta u_h + (1 - \delta) u_h = 6.71$.

Child subsidy : $\bar{n} = 5.50; \delta = 0.30; e = 0.00; \delta u_h + (1 - \delta) u_h = 6.74$.

Case (i) illustrates a solution where an education subsidy dominates a child subsidy. In case (ii) we lower the value of β , leaving all other parameter values intact, and the child subsidy dominates. A lower β represents a smaller productivity differential between high- and low-ability individuals. Similarly, in case (iii) we increase the value of θ_h , leaving all other parameter values intact, and the child subsidy dominates. A higher θ_h represents a more significant role for family background in determining the ability of a child. Rather unsurprisingly, the numbers also indicate that child subsidies generally entail higher fertility and a lower ratio of high- to low-ability children. The following proposition summarizes our results on decentralization.

Proposition 6 *(i) Assume education subsidies are feasible but not child subsidies. The optimal solution requires equalization of all objects of choice across the two types. education subsidies continue to be levied at one hundred percent and equal to the positive externalities bestowed on everyone through education.*

(ii) Assume child subsidies are feasible but not education subsidies. The optimal solution requires $c_h = c_l$, $d_h = d_l$, $e_h = e_l = 0$, and $n_h > n_l$. Child subsidies are set equal to fertility externalities and equal to net subsidies on children.

(iii) Either education subsidies or child subsidies can dominate the other instrument. In general, child subsidies become the more dominant policy if productivity differential between high- and low-ability individuals become smaller or family background assumes a more significant role in determining the ability of a child.

(iv) In general, child subsidies entail a higher fertility rate and a lower ratio of high- to low-ability children, as compared to education subsidies.

5 Concluding remarks

In discussing PAYGO pension plans, models with endogenous fertility have emphasized the positive externality that each person's fertility decision bestows on everybody by increasing everybody's pension benefits through a higher population growth rate. This type of externality, has been argued, may be internalized through child subsidies. Similarly, models with endogenous human capital formation have emphasized the positive externality of investing in education of one's children (because parents cannot expropriate the children's extra earnings due to parents' education expenditures). The same argument has been put forward in cases when parents build their own human capital which they subsequently pass on to their children. These types of externalities may be internalized through education subsidies.

In this paper, we have combined the different externality sources to learn what their interactions teach us about the combination of child and education subsidies one

must use to internalize them both. We have also been concerned with the question of heterogeneity of parents and how this may come into play in connection with externality-correcting policies. This is particularly relevant when child and education subsidies change the distribution of parent types. To this end, the paper has modeled endogenous fertility and human capital formation in an overlapping-generations framework wherein every generation consists of high earners and low earners with the proportion of types being determined endogenously. We have found, among other results, that:

(1) Investing in education of children by either type of parents increases the proportion of high-ability children in the economy and bestows a positive externality on everybody else. This externality has two components, one of which exists only in the presence of PAYGO pension plans.

(2) When high-ability parents increase their fertility rate, they increase the proportion of high-ability children in the economy and thus bestow a positive externality on everybody else. On the other hand, an increase in the fertility rate of low-ability parents, reduces the proportion of high-ability children and imposes a negative externality on everybody else.

(3) Direct child subsidies and education subsidies both reduce the cost of raising children. Thus a subsidy to education is also a subsidy to fertility. The difference is that the education subsidy lowers the share of education cost in the fertility subsidy. On the other hand, a subsidy to children is “neutral” between the two sources of costs.

(4) Investments in education of high- and low-ability parents must always be subsidized because they entail positive externalities.

(5) Direct child subsidies to one or both parent types can be negative; i.e., they can be taxes. However the high-ability type should always get a higher subsidy per child (or pay a lower tax).

(6) Net subsidies to children of a particular parent type (direct child subsidies plus education subsidies) must be set equal to the net externalities associated with increasing

the fertility rate of that type. While net child subsidies to high-ability parents are always positive, net child subsidies to low-ability parents can be positive or negative.

(7) Either education subsidies or child subsidies, when used alone, can dominate the other instrument. In general, child subsidies become the more dominant policy if productivity differential between high- and low-ability individuals become smaller or family background assumes a more significant role in determining the ability of a child.

(8) In general, using child subsidy instruments alone entails a higher fertility rate and a lower ratio of high- to low-ability children, as compared to using education subsidies alone.

As a final observation, we remind our readers that our study has been conducted primarily in a first-best environment. Many other interesting issues surface in a second-best environment when investments and/or type are not publicly observable. We have left the examination of these other issues to a subsequent paper.

Appendix A

Proof of $2\delta(n_h - n_l) + n_l(1 + \pi_l) - n_h\pi_h > 0$: Rewrite equation(1) as

$$\delta_{T+1} = \frac{\delta_T n_h \pi_h + (1 - \delta_T) n_l \pi_l}{\delta_T n_h + (1 - \delta_T) n_l} \equiv f(\delta_T, n_h, \pi_h, n_l, \pi_l). \quad (\text{A1})$$

The steady-state value of δ is found from

$$\begin{cases} \delta_{T+1} = f(\delta_T, n_h, \pi_h, n_l, \pi_l), \\ \delta_{T+1} = \delta_T = \delta. \end{cases} \quad (\text{A2})$$

Differentiating δ totally with respect to π_h yields

$$\frac{d\delta}{d\pi_h} = \frac{\partial f}{\partial \delta_T} \frac{d\delta}{d\pi_h} + \frac{\partial f}{\partial \pi_h}. \quad (\text{A3})$$

Then one finds $d\delta/d\pi_h$ from equation (A3) as

$$\frac{d\delta}{d\pi_h} = \frac{\partial f / \partial \pi_h}{1 - \partial f / \partial \delta_T}. \quad (\text{A4})$$

Next, partially differentiate equation (A1) with respect to π_h to arrive at

$$\frac{\partial \delta_{T+1}}{\partial \pi_h} = \frac{\partial f}{\partial \pi_h} = \frac{\delta_T n_h}{\bar{n}}. \quad (\text{A5})$$

Substituting from (A4) into (A5) yields

$$\frac{d\delta}{d\pi_h} = \frac{\delta_T n_h / \bar{n}}{1 - \partial f / \partial \delta_T},$$

or, alternatively,

$$\frac{d\delta}{de_h} = \frac{d\delta}{d\pi_h} \theta \pi'(e_h) = \frac{\delta_T n_h \theta \pi'(e_h)}{\bar{n} [1 - \partial f / \partial \delta_T]}. \quad (\text{A6})$$

Comparing the expressions for $d\delta/de_h$ as given by equation (A6) above and equation (7) derived in the text tells us that the denominator in equations (7)–(8) is equal to the denominator of (A6). That is,

$$Z \equiv 2\delta(n_h - n_l) + n_l(1 + \pi_l) - n_h\pi_h = \bar{n} [1 - \partial f / \partial \delta_T].$$

Now if $\partial f / \partial \delta_T < 0$, then $1 - \partial f / \partial \delta_T > 0 \Rightarrow Z > 0$. On the other hand, if $\partial f / \partial \delta_T > 0$, the stability condition $|\partial \delta_{T+1} / \partial \delta_T| = |\partial f / \partial \delta_T| < 1$ implies that $1 - \partial f / \partial \delta_T > 0$ and we again have $Z > 0$.

Appendix B: Storage

When the use of storage technology is the better option, all second-period consumption is financed by private savings. We thus have

$$[\delta S_h + (1 - \delta)S_l](1 + r) = \delta d_h + (1 - \delta)d_l.$$

This simplifies the resource constraint (15) to

$$[1 + (\beta - 1)\delta]I \geq \delta \left[c_h + n_h(a + e_h) + \frac{d_h}{1 + r} \right] + (1 - \delta) \left[c_l + n_l(a + e_l) + \frac{d_l}{1 + r} \right]. \quad (\text{B1})$$

The social planner's problem is thus summarized by the Lagrangian

$$\begin{aligned} \mathcal{L} = & \delta [u(c_h) + v(d_h) + \varphi(n_h)] + (1 - \delta) [u(c_l) + v(d_l) + \varphi(n_l)] + \mu \left\{ [1 + (\beta - 1)\delta]I \right. \\ & \left. - \delta \left[c_h + n_h(a + e_h) + \frac{d_h}{1 + r} \right] - (1 - \delta) \left[c_l + n_l(a + e_l) + \frac{d_l}{1 + r} \right] \right\}. \quad (\text{B2}) \end{aligned}$$

Observe that the difference of this expression with \mathcal{L} under PAYGO is that $d_j/(1 + r)$ has replaced d_j/\bar{n} .

Start with the first-order conditions for this problem with respect c_h, c_l, d_h and d_l . They are identical to their counterparts under PAYGO except for $(1 + r)$ replacing \bar{n} . Hence we again have $c_h = c_l = c$, and $d_h = d_l = d$.

Next introduce

$$D \equiv \frac{\partial \mathcal{L}}{\partial \delta} = \varphi(n_h) - \varphi(n_l) + u'(c) [(\beta - 1)I - n_h(a + e_h) + n_l(a + e_l)], \quad (\text{B3})$$

and note that, unlike D under PAYGO given by equation (21), this expression does not contain the term $u'(c)(n_h - n_l)d/\bar{n}^2$; the other terms are identical. The first-order

conditions with respect to n_h, n_l, e_h and e_l as

$$\frac{\partial \mathcal{L}}{\partial e_h} = -\delta n_h u'(c) + D \frac{\partial \delta}{\partial e_h} = 0, \quad (\text{B4})$$

$$\frac{\partial \mathcal{L}}{\partial e_l} = -(1 - \delta) n_l u'(c) + D \frac{\partial \delta}{\partial e_l} = 0, \quad (\text{B5})$$

$$\frac{\partial \mathcal{L}}{\partial n_h} = \delta [\varphi'(n_h) - (a + e_h) u'(c)] + D \frac{\partial \delta}{\partial n_h} = 0, \quad (\text{B6})$$

$$\frac{\partial \mathcal{L}}{\partial n_l} = (1 - \delta) [\varphi'(n_l) - (a + e_l) u'(c)] + D \frac{\partial \delta}{\partial n_l} = 0. \quad (\text{B7})$$

Note that the expressions in (B4)–(B5) are the same as their counterparts under PAYGO, equations (22)–(23), except for the difference in D . Equations (B6)–(B7) differ with their PAYGO counterparts (24)–(25) not only in terms of D , but they do not contain d/\bar{n}^2 in their middle expression either. Manipulating these conditions in the same way as we did with PAYGO yield: $e_h = e_l = e$ and $n_h > n_l$ if $\pi_j(e) = \pi(e) + \theta_j$; and $e_h > e_l$ with an indeterminate relationship between n_h and n_l if $\pi_j(e) = \theta_j \pi(e)$.

Turning to the externality terms, they are now given by

$$\frac{D}{u'(c)} \frac{1}{\delta} \frac{\partial \delta}{\partial e_h} \quad \text{for increasing } e_h, \quad (\text{B8})$$

$$\frac{D}{u'(c)} \frac{1}{1 - \delta} \frac{\partial \delta}{\partial e_l} \quad \text{for increasing } e_l, \quad (\text{B9})$$

$$\frac{D}{u'(c)} \frac{1}{\delta} \frac{\partial \delta}{\partial n_h} \quad \text{for increasing } n_h, \quad (\text{B10})$$

$$\frac{D}{u'(c)} \frac{1}{1 - \delta} \frac{\partial \delta}{\partial n_l} \quad \text{for increasing } n_l. \quad (\text{B11})$$

They all arise from a change in δ ; there are no externalities associated with a change in \bar{n} whether directly as in intergenerational transfer effect or indirectly through δ . That there is no indirect externality through interaction of \bar{n} and δ also means that the extent of this externality depends on the type of pension plan in use. Observe that if δ remains unchanged, we have only the usual private calculations of utility and cost changes; there will be no externality. It is thus the externality associated with the change in δ that

distinguishes the storage story here as compared to Cremer *et al.* (2006, 2008) where the laissez faire solution under the storage technology was optimal.

Regarding decentralization, we will again have 100% education subsidies with τ_h and τ_l also being equal to their corresponding externality terms (B8)–(B9). Net subsidies to children, $t_h + \tau_h e$ and $t_l + \tau_l e$ are set equal to the externality terms associated with n_h and n_l as given by (B10)–(B11). With $D > 0$, from (B4) or (B5), and $\partial\delta/\partial n_h > 0$ and $\partial\delta/\partial n_l < 0$, we now have

$$t_h + \tau_h e > 0 \text{ and } t_l + \tau_l e < 0.$$

Given $\tau_h = \tau_l$, this also means that the sign of t_h is indeterminate but that $t_l < 0$. Finally, we continue to have $t_h > t_l$.

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