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# Corporate Income Taxation of Multinationals in a General Equilibrium Model

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# Corporate Income Taxation of Multinationals in a General Equilibrium Model

## Abstract

This paper contributes to the discussion on Separate Accounting versus Formula Apportionment in the corporate income taxation of multinational enterprises (MNEs). The innovation of the analysis is that we consider a general equilibrium tax competition model with an endogenously determined world interest rate. Under the principle of Separate Accounting, it turns out that corporate tax rates may be inefficiently low or high, while under Formula Apportionment corporate tax rates are always inefficiently low. These results are true independent of whether the number of countries is small or large. They reverse the insights obtained by previous studies under the assumption of an exogenously given world interest rate.

JEL Code: H7, H73.

Keywords: corporate income tax, Separate Accounting, Formula Apportionment.

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# 1 Introduction

There are basically two alternative principles in the taxation of multinational enterprises (MNEs). The first principle is Separate Accounting. Under such a taxation system, corporate income of a MNE is taxed by the tax code of the country in which the MNE the income declares. The second principle is Formula Apportionment. This taxation system is mainly characterized by two properties. The tax bases of all subsidiaries of the MNE are first consolidated and then apportioned to the taxing countries according to a predetermined formula that usually reflects the MNE's property, sales and payroll shares in the respective countries. While Separate Accounting is in operation at the international level, some countries like the U.S., Canada, Germany and Switzerland apply Formula Apportionment at the national level.

The European Commission (2001) presented plans to reform the corporate income taxation of MNEs within the borders of the European Union. The idea is to replace the current system of Separate Accounting by Formula Apportionment. In 2004 the European Commission set up the so-called Common Consolidated Corporate Tax Base Working Group in order to develop concepts for introducing a common European tax base. Such a common tax base definition is seen as a prerequisite for introducing Formula Apportionment. The European Council plans to decide on the introduction of Formula Apportionment during 2008. These activities in the European Union brought in its wake a heated discussion about the pros and cons of the two corporate taxation principles both among politicians and among economists.

Our paper contributes to this discussion. Using a tax competition model with a representative MNE and Leviathan governments, we investigate the efficiency properties of the two tax principles by identifying fiscal externalities caused by the countries' tax policy. The innovation of the paper is that it uses a *general* equilibrium model. Such an approach explicitly takes into account the world capital market where the interest rate is endogenously determined. The advantage of the general equilibrium framework is that it allows to consider *large* countries whose governments are aware of their effects on the world price of capital. And even for *small* countries, each of which takes the interest rate as given, aggregate policy changes of all countries have an impact on the interest rate when it is endogenously determined. Hence, a general equilibrium model like ours is more appropriate to investigate the principles of Separate Accounting and Formula Apportionment: Regardless of whether countries are large or small in the above sense, taxation under both systems will have effects on the interest rate which

should be taken into account when evaluating the two principles in terms of efficiency.

This is particularly true as our analysis yields results that are detrimentally different from those obtained in previous studies under the assumption of a fixed world interest rate. Under Separate Accounting, it turns out that the cross country effect of one country's tax rate consists of a profit shifting externality and a tax base externality. The former states that a corporate tax rate increase in one country induces the MNE to shift more profit to other countries, thereby improving the tax base and tax revenue in other countries. This externality is positive. The tax base externality reflects the impact of one country's tax rate on the other countries' tax base and tax revenue via changes in the quantities and prices of production inputs. A tax rate increase in one country reduces capital demand in this country and raises investment in other countries through a fall in the world interest rate. As consequence, there is a positive effect on the tax base and tax revenue in other countries. But the increase in investment is accompanied by an increase in labor demand and wages which, in turn, reduces the tax base and tax revenue in the other countries. Overall the tax base externality may be positive or negative. Hence, the sign of the total cross country effect of corporate tax rates under Separate Accounting is ambiguous, leaving it open whether countries end up with inefficient over- or undertaxation.

Under Formula Apportionment, in contrast, corporate tax rates are unambiguously too low. With consolidation and apportionment the cross country effect of tax rates can be decomposed into a formula externality and a tax base externality. As the profit shifting externality under Separate Accounting, the formula externality is positive: If one country raises its tax rate the MNE reallocates capital and labor from this country to other countries. In doing so, it reduces its tax burden by lowering the share of the consolidated tax base assigned to the tax-increasing country and by increasing the share of the consolidated tax base assigned to the other countries. As consequence, the tax revenue in the other countries goes up. The tax base externality again reflects the impact of one country's tax rate on the other countries' tax base and tax revenue through changes in quantities and prices of production inputs. In contrast to Separate Accounting, however, it is now the consolidated tax base that determines tax revenue of the countries. Hence, the effects via investment and wages cancel out and do not influence the tax base. Only the reduction in the interest rate matters. It reduces capital cost and increases the consolidated tax base and tax revenue in the other countries. Hence, the tax base externality under Formula Apportionment is unambiguously positive and corporate tax rates will always fall short of their efficient levels.

These results reverse the insights obtained by previous studies. There is by now a large number of studies investigating Separate Accounting versus Formula Apportionment. Examples are McLure (1980), Mintz and Smart (2004) and Nielsen et al. (2003). Our paper is closely related to Gordon and Wilson (1986), Eggert and Schjelderup (2003), Wellisch (2004), Sørensen (2004), Nielsen et al. (2006), Riedel and Runkel (2007), Pinto (2007), Pethig and Wagener (2008) and Eichner and Runkel (2008). But in contrast to our approach, all these papers use partial equilibrium models with a given world interest rate. Hence, the tax base externality under Separate Accounting is missing since the increase in one country's tax rate reduces only the MNE's capital and labor demand in this country, but neither the world interest rate nor the production inputs in other countries. For the same reason, the effects on the consolidated tax base via changes in the production inputs do not cancel out, so the sign of the tax base externality under Formula Apportionment becomes indeterminate. The basic insight of previous studies is therefore that the corporate tax rates under Separate Accounting are inefficiently low (due to the positive profit shifting externality), whereas they may be inefficiently low or high under Formula Apportionment (due to the indeterminate sign of the tax base externality). These insights are detrimentally different to those derived in our framework under the assumption of an endogenous world interest rate. We show that this difference in results prevails if we let the number of countries go to infinity and each country becomes small.

If we abstract from profit shifting, our analysis of the Separate Accounting principle is also related to the traditional literature on (capital) tax competition. For example, Wilson (1985, 1986) and Zodrow and Mieszkowski (1986) establish inefficiently low capital tax rates in a tax competition model with a large number of countries. This result has been extended to settings with a small number of countries by Crombrughe and Tulkens (1990). Hoyt (1991) unifies both approaches and shows that the race to the bottom sharpens when the number of countries increases. The basic reason for undertaxation in these studies is a positive capital flight externality. If one country increases its tax rate, capital flows out of this country and thereby increases investment in other countries. This externality is similar to our tax base externality under Separate Accounting. In our framework, however, the tax base externality may be positive or negative. The reason for this difference is that the above authors model capital taxes as a (unit) wealth tax on capital, whereas we explicitly consider a tax on corporate income. Hence, in our model there may be a negative effect of one country's tax rate on the other countries' tax base working through changes in labor demand and wages.

The paper is organized as follows. In Section 2, we introduce the basic assumptions of our model. Section 3 and 4 investigate the efficiency properties of corporate tax rates under Separate Accounting and Formula Apportionment, and Section 5 concludes.

## 2 Basic Assumptions

Consider an economy with  $n \geq 2$  identical countries. We use  $i, j, h = 1, \dots, n$  as country indices. There is a large number of MNEs operating a plant in each country. The MNEs are structurally the same, so we restrict attention to a representative MNE. In country  $i$ , the MNE produces a consumption good according to the production function  $F(k_i, \ell_i)$  where  $k_i$  is capital and  $\ell_i$  is labor employed in the production of country  $i$ . The production function  $F$  has the usual properties. It exhibits positive and decreasing marginal returns to capital and labor, i.e.  $F_k, F_\ell > 0$  and  $F_{kk}, F_{\ell\ell} < 0$ . In addition, capital and labor are supposed to be complements in the sense that  $F_{\ell k} > 0$ . As the previous literature on Separate Accounting versus Formula Apportionment, we consider the case of decreasing returns to scale with respect to capital and labor. This assumption implies that there is at least one fixed factor in production (say, entrepreneurial services) that generates economic rents. In the analysis of corporate income taxation, the existence of economics rents is a useful property since these rents represent the corporate income the governments try to tax.

The MNE may shift profit between its subsidiaries. This can be done, for example, by manipulating the subsidiaries' debt equity structure, distorting transfer prices of goods and services traded between the subsidiaries or distributing overhead cost between the subsidiaries. The specific shifting channel is immaterial for our purpose. We simply model the effect that profit shifting changes the tax bases of the subsidiaries. Formally, the variable  $s_i$  denotes the change in the tax base of the subsidiary located in country  $i$ . If  $s_i > 0$  ( $s_i < 0$ ), then the tax base in country  $i$  goes up (down) since the MNE shifts profit to (from) country  $i$ . The shifting variables satisfy

$$\sum_j s_j = 0. \tag{1}$$

This condition ensures that  $s_i$  represents shifting from or to country  $i$  and not a change in the overall profit of the MNE. Profit shifting comes at a concealment cost that reflects, for example, the expense for tax consultants and the MNE's risk of being detected by the tax authority illegally shifting income (e.g. Kant, 1998, Haufler and

Schjelderup, 2000). The concealment cost is represented by the U-shaped function  $C(s_i)$  with  $C(0) = 0$ ,  $\text{sign}\{C''(s_i)\} = \text{sign}\{s_i\}$  and  $C'''(s_i) > 0$ . Note that this modeling implicitly assumes that one euro shifting between two subsidiaries causes cost in both subsidiaries. This is a realistic assumption. For example, in their transfer pricing regulation many countries force MNEs to document their transactions. This documentation is required for each subsidiary, i.e. the subsidiary in country  $i$  has to document the transaction even if the subsidiary in country  $j$  has already documented it. All documentations are costly since they are usually done by different tax consultants.<sup>1</sup>

For each unit of capital the MNE has to pay the world interest rate  $r$ . The user cost of capital in country  $i$  therefore amounts to  $rk_i$ . Payroll in country  $i$  is  $w_i\ell_i$ , where  $w_i$  stands for the local wage rate in country  $i$ . In order to define the tax base of the MNE, we have to specify which factor cost is tax-deductible. In accordance with most real world tax systems, we assume that payroll is fully deductible. In contrast, capital cost may be partially deductible since the governments may grant partial depreciation allowances only and/or allows the MNE to deduct the cost of debt finance but not the cost of equity finance. We denote the fraction of capital cost that is deductible by the parameter  $\rho \in [0, 1]$ . The tax base of the MNE in country  $i$  is then given by

$$\Phi^i = F(k_i, \ell_i) - \rho rk_i - w_i\ell_i + s_i. \quad (2)$$

The tax base of the MNE in country  $i$  equals sales (output) adjusted by the deductible capital and labor cost and by profit shifting from or to country  $i$ .

The decisive difference of our model to previous studies on the comparison between Separate Accounting and Formula Apportionment is that we consider a general equilibrium model. In our framework, not only the local wage rates are endogenously determined, but also is the world interest rate. Formally, the wage rate in country  $i$  follows from the local labor market equilibrium condition

$$\ell_i = \bar{\ell}, \quad (3)$$

which equates labor demand  $\ell_i$  and labor endowment  $\bar{\ell}$  that is inelastically supplied. Labor demand depends on the wage rates according to the MNE's profit maximization which is considered below. The world interest rate is determined on the world capital market which clears according to the condition

$$\sum_j k_j = n\bar{k}. \quad (4)$$

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<sup>1</sup>Most of our results are not affected if a transaction is associated with cost in one subsidiary only.



Equation (4) requires that world capital demand has to equal world capital supply, where each country is assumed to have capital endowment  $\bar{k}$  which it inelastically supplies at the world capital market. Capital demand depends on the interest rate due to the MNE's profit maximization considered in the next sections. Previous studies partially consider the labor market (3), but our approach is the first that takes into account an endogenous world interest rate determined on the world capital market (4).

### 3 Separate Accounting

**Profit Maximization and Markets.** Under Separate Accounting corporate income is taxed in the country where the MNE it declares. Denoting by  $t_j$  country  $j$ 's statutory tax rate, the MNE's total after-tax profit can be written as

$$\Pi = \sum_j (1 - t_j) \Phi^j - r(1 - \rho) \sum_j k_j - \sum_j C(s_j). \quad (5)$$

The MNE chooses investment, labor input and profit shifting in order to maximize after-tax profit (5) subject to the constraint (1) and the tax base definition (2). In doing so, it takes as given the tax rates and the factor prices. Denoting by  $\lambda$  the Lagrange multiplier associated with (1), the first-order conditions of profit maximization read

$$(1 - t_i) [F_k(k_i, \ell_i) - \rho r] - r(1 - \rho) = 0, \quad (6)$$

$$F_\ell(k_i, \ell_i) - w_i = 0, \quad (7)$$

$$(1 - t_i) - C'(s_i) + \lambda = 0. \quad (8)$$

These conditions have the usual interpretation. Equation (6) and (7) equate the (net-of-tax) marginal return to capital and labor to the respective (deductible) factor cost. Equation (8) states that the MNE shifts profit up to the point where the marginal concealment cost equals the marginal shifting benefit. This condition implies that shifting to country  $i$  will be larger than shifting to country  $j$  if country  $i$  has the lower tax rate, i.e.  $t_i < t_j$  implies  $C'(s_i) > C'(s_j)$  and  $s_i > s_j$  due to  $C''(\cdot) > 0$ . Together with (1) it follows that there is profit shifting from high-tax to low-tax countries as long as non-zero tax rate differentials between countries exist.

Below we will analyze the tax competition game between the  $n$  countries. To that end we need the comparative static effects of tax rate changes on the MNE's investment, labor demand and profit shifting decision. We follow previous studies and restrict attention to symmetric equilibria with  $t_i = t$ . Equations (1) – (4) and (6) – (8)

then imply  $k_i = \bar{k}$ ,  $\ell_i = \bar{\ell}$ ,  $w_i = w$ ,  $\Phi^i = \Phi$  and  $s_i = 0$ . Totally differentiating (1) – (4) and (6) – (8) and then applying the symmetry assumption, Appendix A shows

$$\frac{\partial r}{\partial t_i} = -\frac{F_k - \rho r}{n(1 - \rho t)} < 0, \quad (9)$$

$$\frac{\partial k_i}{\partial t_i} = \frac{(n-1)(F_k - \rho r)}{n(1-t)F_{kk}} < 0, \quad \frac{\partial k_i}{\partial t_j} = -\frac{F_k - \rho r}{n(1-t)F_{kk}} > 0, \quad (10)$$

$$\frac{\partial w_i}{\partial t_i} = \frac{(n-1)(F_k - \rho r)F_{\ell k}}{n(1-t)F_{kk}} < 0, \quad \frac{\partial w_i}{\partial t_j} = -\frac{(F_k - \rho r)F_{\ell k}}{n(1-t)F_{kk}} > 0, \quad (11)$$

$$\frac{\partial s_i}{\partial t_i} = -\frac{n-1}{nC'''} < 0, \quad \frac{\partial s_i}{\partial t_j} = \frac{1}{nC'''} > 0, \quad (12)$$

where  $i \neq j$ . These expressions have a straightforward interpretation. A unilateral increase in one country's tax rate causes a rise in the tax burden in this country and, thus, induces the MNE to reduce capital demand and the tax base in this country. As consequence, the equilibrium world interest rate falls and investment in all other countries goes up. Hence, the MNE reallocates capital from the tax-increasing country to all other countries as formally shown by (9) and (10). Since labor is complementary to capital ( $F_{\ell k} > 0$ ), decreases in capital call for a reduction in labor demand so that the input factor labor becomes more abundant and the wage rate decreases. Thus, the wage rate shrinks in the tax-increasing country but rises elsewhere as follows from (11). Finally, (12) shows that if a country raises its tax rate, profit shifting to this country declines whereas profit shifting to other countries increases.

**Tax competition.** We now turn to the tax competition game under Separate Accounting. It is assumed that the governments of the countries behave non-cooperatively, using tax rates as their strategic variables. We consider the case where each country's government chooses its corporate tax rate in order to maximize tax revenue. This assumption reflects the idea of Leviathan governments which is often seen quite relevant, in particular in the context of corporate taxation (e.g. Wilson 1999), and therefore has frequently been used by previous studies on Separate Accounting versus Formula Apportionment (e.g. Nielsen et al., 2006, and Pethig and Wagener, 2008).

Under the tax principle of Separate Accounting, a country's tax revenue equals its tax rate times the tax base. For country  $i$  we obtain

$$g_i = t_i \Phi^i. \quad (13)$$

Country  $i$  maximizes (13) with respect to its tax rate  $t_i$  taken as given the tax rates of the other countries. In doing so, it takes into account equations (9) – (12), i.e. the

impact of its tax policy on the MNE's behavior and on the local labor market as well as on the world capital market. The latter effect is the main difference of our analysis to previous studies: In our model, each country is aware of its impact on the capital market and the equilibrium interest rate. Only if the number of countries becomes large and, thus, each country becomes small, the effect of the *individual* country on the world interest rate vanishes. Formally, this follows from (9) and  $n \rightarrow \infty$ . As we will see below, however, even such an extreme case is different from assuming a fixed  $r$ , as done in previous studies, since the interest rate in our model is then still endogenous and varies with *aggregate* policy changes.

The first-order condition of country  $i$ 's tax revenue maximization is  $\partial g_i / \partial t_i = 0$ . It determines country  $i$ 's reaction function, i.e. its best response to the other countries' tax rates. Solving the first-order conditions of all  $n$  countries gives the equilibrium tax rates of the tax competition game. As already mentioned above, we follow previous studies and focus on a symmetric equilibrium with tax rates  $t_i = \tilde{t}$ . Our main interest is to assess the efficiency properties of  $\tilde{t}$ . This can be done by investigating the fiscal externality which is represented by the effect of country  $i$ 's tax rate on all other countries' tax revenues, i.e.  $\sum_{j \neq i} \partial g_j / \partial t_i$ . Starting from a symmetric equilibrium, the fiscal externality reflects the tax revenue effect of a coordinated tax rate increase. A positive (negative) sign of the fiscal externality shows that tax coordination leads to an increase (decrease) of tax revenue in each country and, thus, to a Pareto improvement (deterioration) so that the equilibrium tax rate  $\tilde{t}$  is inefficiently low (high). In order to determine the sign of the fiscal externality, we differentiate (13) and take into account (2), (9) – (12) and the symmetry property. This yields

$$\sum_{j \neq i} \frac{\partial g_j}{\partial t_i} = (n-1) \frac{\partial g_j}{\partial t_i} = \tilde{t}(n-1) \frac{\partial \Phi^j}{\partial t_i} = (n-1) \text{PE} + (n-1) \text{TE}|_{\text{SA}}, \quad (14)$$

where

$$\text{PE} = \tilde{t} \frac{\partial s_j}{\partial t_i} = \frac{\tilde{t}}{nC''} > 0, \quad (15)$$

$$\begin{aligned} \text{TE}|_{\text{SA}} &= \tilde{t} \left[ (F_k - \rho r) \frac{\partial k_j}{\partial t_i} - \rho \bar{k} \frac{\partial r}{\partial t_i} - \bar{\ell} \frac{\partial w_j}{\partial t_i} \right] \\ &= -\frac{\tilde{t}(F_k - \rho r)}{n(1 - \tilde{t})(1 - \rho \tilde{t}) F_{kk}} \left[ (1 - \rho \tilde{t})(F_k - \rho r - \bar{\ell} F_{\ell k}) - (1 - \tilde{t}) \rho \bar{k} F_{kk} \right]. \end{aligned} \quad (16)$$

According to (14) – (16), the total cross country effect of country  $i$ 's tax rate on tax revenue in country  $j \neq i$  can be decomposed into two sub-externalities. The first is the profit shifting externality PE in (15). If country  $i$  increases its tax rate  $t_i$ , the MNE

shifts more profit to country  $j$  which enhances country  $j$ 's tax base and tax revenue. The profit shifting externality is positive and tends to inefficient undertaxation. The second externality is the tax base externality  $\text{TE}|_{\text{SA}}$  in (16). This externality is constituted by three effects that build on each other. First, increasing  $t_i$  lowers the MNE's capital demand  $k_i$  in country  $i$ . As consequence, world capital demand and, thus, the price of capital represented by the interest rate  $r$  decrease. This has a positive effect on the tax base in country  $j$  as the MNE's capital cost in country  $j$  becomes lower. Second, the reduction in the interest rate  $r$  induces the MNE to increase investment  $k_j$  in country  $j$ .<sup>2</sup> Hence, also this second effect raises the tax base in country  $j$ . Third, the increase in investment  $k_j$  induces the MNE to demand more labor in country  $j$  since capital and labor are complements. The wage rate  $w_j$  in country  $j$  therefore goes up with a raise in payroll and a drop in the tax base in country  $j$  as an end result.

Since the third effect goes into the opposite direction of the first and second effect, the sign of the tax base externality is ambiguous. To illustrate this point, consider the special case of no deductibility of capital cost ( $\rho = 0$ ) and a CES production function  $F(k, \ell) = [\delta k^\nu + (1 - \delta)\ell^\nu]^{\frac{\mu}{\nu}}$  with  $\delta \in ]0, 1[$ ,  $\mu \in ]0, 1[$  and  $\nu \leq 1$ . Note that for the CES function the substitution elasticity  $\eta := 1/(1 - \nu)$  is positive correlated with the parameter  $\nu$ . For notational convenience, we define  $K := \delta \bar{k}^\nu$ ,  $L = (1 - \delta)\bar{\ell}^\nu$  and  $Z := K + L$ . We can then write  $F = Z^{\frac{\mu}{\nu}}$ ,  $F_k = \mu K Z^{\frac{\mu}{\nu}-1}/\bar{k}$ ,  $F_\ell = \mu L Z^{\frac{\mu}{\nu}-1}/\bar{\ell}$ ,  $F_{kk} = -\mu[(1 - \mu)K + (1 - \nu)L]K Z^{\frac{\mu}{\nu}-2}/\bar{k}^2$  and  $F_{\ell k} = \mu(\mu - \nu)KL Z^{\frac{\mu}{\nu}-2}/\bar{k}\bar{\ell}$ . Inserting this and  $\rho = 0$  into (16) and defining  $\Psi := \tilde{t}\mu K Z^{\frac{\mu}{\nu}-1}/[n(1 - \tilde{t})] > 0$  yields

$$\text{TE}|_{\text{SA}} = \Psi \frac{K + (1 - \mu + \nu)L}{(1 - \mu)K + (1 - \nu)L}. \quad (17)$$

From (17) we infer that the tax base externality is positive as long as  $\nu \geq 0$  or, equivalently,  $\eta \geq 1$ . For  $\nu = 0$  this parameter range covers as a special case the Cobb-Douglas production function. However, if the parameter  $\nu$  is sufficiently negative, then the tax base externality may become negative as well. This is intuitively plausible since for a very small  $\nu$  and, thus, a very small substitution elasticity  $\eta$ , capital and labor are strong complements. In such a case, the above mentioned third effect of country  $i$ 's tax rate on country  $j$ 's tax base via the rise in the wage rate is quite large because the increase in investment in country  $j$  induces the MNE to increase labor demand in country  $j$  a lot. Hence, the third effect may overcompensate the other two effects and, thus, may render the tax base externality negative pointing to overtaxation.

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<sup>2</sup>The fall in  $r$  exerts also a positive effect on investment  $k_i$  in the tax-increasing country  $i$ . But this effect is more than compensated by the initial drop in  $k_i$ .

The possibly different signs of the profit shifting and tax base externalities prove

**Proposition 1.** *Suppose the tax competition game under Separate Accounting attains a symmetric Nash equilibrium with  $t_i = \tilde{t}$ . Then the equilibrium corporate tax rate  $\tilde{t}$  may be inefficiently low or high.*

It is important to compare this insight with the result obtained by previous studies referred to in the Introduction. Previous authors came to the conclusion that under Separate Accounting tax revenue maximizing governments set their corporate tax rates inefficiently low. The reason for the difference to our result in Proposition 1 is that previous studies proceed on the assumption of a fixed interest rate. If  $r$  is exogenously given, none of the above mentioned three effects of country  $i$ 's tax rate on country  $j$ 's tax base is present since the decline of the MNE's investment in country  $i$  is then followed neither by a fall in the interest rate nor by an increase in investment and the wage rate in country  $j$ . Hence, with a fixed interest rate there is no tax base externality, and the remaining profit shifting externality results in inefficient undertaxation. As our proposition shows, however, this may no longer be true, if we explicitly consider the world capital market that endogenously determines the interest rate.

One may conjecture that this difference to previous studies is due to an implicit assumption that each country is sufficiently large in order to take into account its effect on the world interest rate. But the following proposition (proven in Appendix B) shows that our result prevails if  $n$  grows without bounds so that each country becomes infinitesimally small and no longer has an effect on the interest rate.

**Proposition 2.** *Suppose the tax competition game under Separate Accounting attains a symmetric Nash equilibrium with  $t_i = \tilde{t}$ . Then Proposition 1 is true also for small countries ( $n \rightarrow \infty$ ). Moreover, we obtain*

$$\text{sign} \left\{ \frac{d\tilde{t}}{dn} \right\} = -\text{sign} \{ \text{PE} + \text{TE}|_{\text{SA}} \}.$$

It is true that for an infinite number of countries the impact of country  $i$ 's tax rate on the interest rate and, thus, on investment and wages in an *individual* country  $j \neq i$  converges to zero. Formally,  $\text{TE}|_{\text{SA}}$  in (16) vanishes if  $n \rightarrow \infty$ . However, if the number of countries grows without bounds, the effect of country  $i$ 's tax rate on the *aggregate* number of countries is still non-zero. This follows from (14) where  $\text{TE}|_{\text{SA}}$  is multiplied by  $n - 1$  which represents the number of competitors of country  $i$ . Put differently, the tax base externality inflicted by country  $i$ 's tax rate on a single competitor becomes

infinitesimally small when the number of countries becomes larger and larger, but the tax base externality inflicted on the aggregate number of competitors is still there and ambiguous in sign. This is the reason why Proposition 1 is also true for small countries. Consistently with this argument, the second part of Proposition 2 shows that the deviation of the equilibrium tax rate from its efficient level becomes larger if the number of countries increases. This is true independent of whether we have inefficient undertaxation ( $\text{PE} + \text{TE}|_{\text{SA}} > 0$ ) or overtaxation ( $\text{PE} + \text{TE}|_{\text{SA}} < 0$ ).

It may finally be worthwhile to compare our results under Separate Accounting to the insights of the (capital) tax competition literature already referred to in the Introduction. This literature identifies the so-called capital flight externality that reflects the increase in country  $j$ 's investment upon an increase in country  $i$ 's tax rate. It is positive and unambiguously points to inefficiently low tax rates. This effect is similar to the comparative static effect in (10). As shown by Proposition 1 and 2, however, in our framework countries may end up with inefficient overtaxation. The reason for this difference is that we model corporate taxation as a tax on taxable income whereas the (capital) tax competition literature uses the short cut of a (unit) wealth tax on capital, i.e. tax payments there amounts to  $t_i k_i$ . Hence, in the previous literature there is no cross country effect on tax bases working through an increase in wages. This effect is the driving force behind possible overtaxation in our framework.

## 4 Formula Apportionment

**Profit Maximization and Markets.** We now turn to the principle of Formula Apportionment. Under this taxation principle, the tax bases of the MNE's subsidiaries are first consolidated and then apportionment to the taxing countries according to a certain formula. We consider a formula that contains all three apportionment factors usually employed in practice. More specifically, the part of the MNE's consolidated tax base assigned to country  $i$  is proportional to the MNE's capital share  $k_i / \sum_j k_j$ , sales share  $F(k_i) / \sum_j F(k_j)$  and payroll share  $w_i \ell_i / \sum_j w_j \ell_j$ . Denoting by  $\gamma$ ,  $\sigma$  and  $\varphi$  the formula weights of these apportionment factors, the share of the consolidated tax base assigned to country  $i$  reads

$$A^i(k_i, k_{-i}, \ell_i, \ell_{-i}, w_i, w_{-i}) = \gamma \frac{k_i}{\sum_j k_j} + \sigma \frac{F(k_i, \ell_i)}{\sum_j F(k_j, \ell_j)} + \varphi \frac{w_i \ell_i}{\sum_j w_j \ell_j}, \quad (18)$$

where  $x_{-i} := (x_1, \dots, x_{i-1}, x_{i+1}, \dots, x_n)$  for  $x = k, \ell, w$ , and where  $(\gamma, \sigma, \varphi) \in \{(\gamma, \sigma, \varphi) \mid (\gamma, \sigma, \varphi) \in [0, 1]^3 \text{ and } \gamma + \sigma + \varphi = 1\}$ .

The MNE's tax burden in country  $i$  is given by  $t_i A^i(\cdot) \sum_j \Phi^j$ . The MNE's total after-tax profit under Formula Apportionment can be written as

$$\Pi = (1 - \tau) \sum_j \Phi^j - r(1 - \rho) \sum_j k_j - \sum_j C(s_j), \quad (19)$$

where

$$\tau = t_i A^i + \sum_{j \neq i} t_j A^j = t_i + \sum_{j \neq i} (t_j - t_i) A^j \quad (20)$$

is the effective tax rate of the MNE. Note that in equation (20) we used the property  $\sum_j A^j = 1$ . The objective of the MNE is to maximize the after-tax profit (19) with respect to capital, labor and profit shifting taking into account (2), (20) and  $\sum_j s_j = 0$ . Because tax bases are consolidated, the MNE is not able to reduce its tax liability by profit shifting. It therefore chooses profit shifting such that the concealment cost is minimized, i.e.  $s_i = 0$  for all  $i$ . The MNE's optimal capital and labor demand, respectively, is characterized by the first-order conditions

$$\sum_j \Phi^j \cdot \sum_{j \neq i} (t_i - t_j) A_{k_i}^j + (1 - \tau) [F_k(k_i, \ell_i) - \rho r] - r(1 - \rho) = 0, \quad (21)$$

$$\sum_j \Phi^j \cdot \sum_{j \neq i} (t_i - t_j) A_{\ell_i}^j + (1 - \tau) [F_\ell(k_i, \ell_i) - w_i] = 0. \quad (22)$$

There are two differences of these first-order conditions to the respective first-order conditions (6) and (7) under Separate Accounting. First, under Formula Apportionment the net-of-tax marginal returns to the input factors are computed with the effective tax rate  $\tau$  instead of the national tax rates  $t_i$ . The reason is consolidation of tax bases. Second, due to the apportionment mechanism the MNE has *ceteris paribus* an incentive to invest more and demand more labor in countries with below-average tax burden than in countries with above-average tax burden. The reason is that, by doing so, the MNE increases the share of the consolidated tax base assigned to low-tax countries and reduces the share of the consolidated tax base assigned to high-tax countries so that its total tax burden falls. This formula manipulation incentive of the MNE is reflected by the first term on the LHS of (21) and (22), respectively.

Equations (21) and (22) together with the market clearing conditions (3) and (4) determine the MNE's decision and the factor prices as functions of the corporate tax rates. We again need the comparative static effects of tax rate changes on the economy's equilibrium and restrict our attention to symmetric Nash equilibria with equal tax

rates  $t_i = \tau = t$ . It then follows  $k_i = \bar{k}$ ,  $\ell_i = \bar{\ell}$ ,  $w_i = w$  and  $\Phi^i = \Phi$ . Moreover, the apportionment formula satisfies  $A^j = 1/n$ ,  $A_{k_i}^j = -A_{k_i}^i/(n-1) = -(\gamma/k + \sigma F_k/F)/n^2$ ,  $A_{\ell_i}^j = -A_{\ell_i}^i/(n-1) = -(\sigma F_\ell/F + \varphi/\ell)/n^2$  and  $A_{w_i}^j = -A_{w_i}^i/(n-1) = -\varphi/(n^2 w)$ . The comparative static analysis, which is delegated to Appendix C, yields

$$\frac{\partial r}{\partial t_i} = -\frac{F_k - \rho r}{n(1-t\rho)} < 0, \quad (23)$$

$$\frac{\partial k_i}{\partial t_i} = \frac{(n-1)\Phi}{n(1-t)F_{kk}} \left( \frac{\gamma}{k} + \frac{\sigma F_k}{F} \right) < 0, \quad \frac{\partial k_i}{\partial t_j} = -\frac{\Phi}{n(1-t)F_{kk}} \left( \frac{\gamma}{k} + \frac{\sigma F_k}{F} \right) > 0, \quad (24)$$

$$\frac{\partial w_i}{\partial t_i} = \frac{(n-1)\Phi}{n(1-t)F_{kk}} \left[ \frac{\gamma F_{\ell k}}{k} + \frac{\sigma(F_{\ell k}F_k - F_\ell F_{kk})}{F} - \frac{\varphi F_{kk}}{\ell} \right] < 0, \quad (25)$$

$$\frac{\partial w_i}{\partial t_j} = -\frac{\Phi}{n(1-t)F_{kk}} \left[ \frac{\gamma F_{\ell k}}{k} + \frac{\sigma(F_{\ell k}F_k - F_\ell F_{kk})}{F} - \frac{\varphi F_{kk}}{\ell} \right] > 0, \quad (26)$$

for  $i \neq j$ . The comparative static effects (23) – (26) have the same signs as the corresponding effects (9) – (11) under Separate Accounting. However, the intuition is different. Under Separate Accounting, the MNE reduces investment in a tax-increasing country since this lowers the tax base in this country. Such an effect is not present under Formula Apportionment since taxes fall on the consolidated tax base, so the MNE is not able to reduce the tax base by reallocating capital between countries. But under Formula Apportionment the MNE reduces capital demand in a tax-increasing country since it faces the above mentioned formula manipulation incentive. It reallocates capital from a tax-increasing country to the other countries since this raises the share of the consolidated tax base assigned to the other countries. The increase in investment in the other countries is brought about by a reduction in the world interest rate. Formally, these effects are captured by (23) and (24). Moreover, the complementarity between labor and capital implies that labor demand and wages move into the same direction as investment. This effect is amplified by the formula manipulation incentive that holds also with respect to labor and wages.<sup>3</sup> Overall, (25) and (26) show that wages in the tax-increasing country go down while they increase in all other countries.

**Tax competition.** Under Formula Apportionment tax revenue of a country equals the share of the MNE's consolidated tax base assigned to this country multiplied by

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<sup>3</sup>Strictly speaking, the formula manipulation incentive holds with respect to labor and wages only if the formula contains the sales and/or payroll factors. It holds with respect to investment only if the formula contains the property and/or sales factors. But in any case, the formula manipulation incentive will be present at least with respect to one of the input factors.



the national corporate tax rate. For country  $i$  we obtain

$$g_i = t_i A^i(k_i, k_{-i}, \ell_i, \ell_{-i}, w_i, w_{-i}) \sum_j \Phi^j. \quad (27)$$

Country  $i$  maximizes (27) with respect to  $t_i$  taking as given  $t_j$  for all  $j \neq i$ . It takes into account the impact of its policy choice on the MNE's behavior and the factor markets. This impact is represented by (23) – (26). The Nash equilibrium of the tax competition game is constituted by  $\partial g_i / \partial t_i = 0$  for all  $i$ . The focus is again on a symmetric equilibrium with  $t_i = \hat{t}$ . In order to evaluate the efficiency properties of the equilibrium tax rate, we compute in Appendix D the cross derivative of (27) as

$$\sum_{j \neq i} \frac{\partial g_j}{\partial t_i} = (n-1) \frac{\partial g_j}{\partial t_i} = (n-1) (\text{TE}|_{\text{FA}} + \text{FE}|_{(\gamma, \sigma, \varphi)}), \quad (28)$$

where

$$\text{TE}|_{\text{FA}} = \hat{t} A \frac{\partial \sum_j \Phi^j}{\partial t_i} = -\hat{t} \rho \bar{k} \frac{\partial r}{\partial t_i} = \hat{t} \rho \bar{k} \frac{F_k - \rho r}{n(1 - \hat{t} \rho)} > 0 \quad (29)$$

$$\begin{aligned} \text{FE}|_{(\gamma, \sigma, \varphi)} &= \hat{t} n \Phi \frac{\partial A^j}{\partial t_i} = \hat{t} \Phi \left[ \left( \frac{\gamma}{\bar{k}} + \frac{\sigma F_k}{F} \right) \frac{\partial k_j}{\partial t_i} + \frac{\varphi}{w} \frac{\partial w_j}{\partial t_i} \right] \\ &= -\frac{\hat{t} \Phi^2}{n(1 - \hat{t}) F_{kk}} \left[ \left( \frac{\gamma}{\bar{k}} + \frac{\sigma F_k}{F} \right)^2 \right. \\ &\quad \left. + \frac{\varphi}{F_\ell} \left( \frac{\gamma F_{\ell k}}{\bar{k}} + \frac{\sigma (F_{\ell k} F_k - F_\ell F_{kk})}{F} - \frac{\varphi F_{kk}}{\bar{\ell}} \right) \right] > 0. \end{aligned} \quad (30)$$

According to (28) – (30), the cross country effect of tax rates under Formula Apportionment can be decomposed into two sub-externalities. The first is the tax base externality  $\text{TE}|_{\text{FA}}$  given by (29). The reason for this externality is that an increase in one country's tax rate reduces capital demand in this country and, thus, the world interest rate. As consequence, the MNE's capital cost falls so that the consolidated tax base and tax revenue in all countries go up. The tax base externality is always positive. Remember that under Formula Apportionment reallocating input factors has no effect on the consolidated tax base and, hence, does not influence the tax base externality. However, reallocation has an effect on the apportionment of the consolidated tax base. If one country increases its tax rate, the MNE shifts capital and labor from this country to all other countries since it faces the formula manipulation incentive. This raises the share of the consolidated tax base assigned to the other countries and causes the formula externality  $\text{FE}|_{(\gamma, \sigma, \varphi)}$  defined in (30). The formula externality is positive, too.

Since both externalities under Formula Apportionment are positive, we obtain

**Proposition 3.** *Suppose the tax competition game under Formula Apportionment attains a symmetric Nash equilibrium with  $t_i = \hat{t}$ . Then the equilibrium corporate tax rate  $\hat{t}$  is inefficiently low.*

It is again interesting to compare this insight with the result of previous studies referred to in the Introduction. Previous authors also derive the formula externality which is exactly the same as the externality in (30). In contrast, previous studies identify a tax base externality that is different from that in (29). When the interest rate is fixed, an increase in one country's tax rate reduces capital and labor demand in this country, but leaves unaltered the interest rate and factor demand in all other countries.<sup>4</sup> Hence, there is no direct effect on the consolidated tax base and the other countries' tax revenue via a decline in the interest rate. In addition, the effects on the consolidated tax base caused by changes in investment and wages do not cancel out. Only investment and wages in the tax-increasing country are varied, so the consolidated tax base and tax revenue of the other countries are now affected by these changes. As consequence, the tax base externality may be positive or negative, depending on whether the negative effect of the decline in investment or the positive effect of the fall in wages dominates. With a fixed interest rate, it is therefore not clear whether tax competition leads to inefficiently low or high corporate tax rates. In contrast, our Proposition 3 shows that with an endogenous interest rate corporate taxes under Formula Apportionment are inefficiently low since the tax base externality is unambiguously positive.

As for the case of Separate Accounting, we can again show that this conclusion prevails if the countries become infinitesimally small. By virtually the same proof as that of Proposition 2, we obtain

**Proposition 4.** *Suppose the tax competition game under Formula Apportionment attains a symmetric Nash equilibrium with  $t_i = \hat{t}$ . Then Proposition 3 is true also for small countries ( $n \rightarrow \infty$ ). Moreover, we obtain*

$$\text{sign} \left\{ \frac{d\hat{t}}{dn} \right\} = -\text{sign} \left\{ \text{TE}|_{\text{FA}} + \text{FE}|_{(\gamma, \sigma, \varphi)} \right\} < 0.$$

When the number of countries becomes very large, the cross country effect of tax rates between two countries converges to zero. However, the aggregate effect of one

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<sup>4</sup>This argument abstracts from the changes in factor inputs caused by the formula manipulation incentive since these changes are already reflected in the formula externality

country's tax rate on all other countries is still positive. This is the reason why we obtain inefficient undertaxation under Formula Apportionment even if countries are small. Moreover, if the number of countries grows, more and more countries compete for mobile capital. As shown by the second part of Proposition 4, it follows that the equilibrium corporate tax rate under Formula Apportionment is decreasing in the number of countries. Inefficient undertaxation is therefore more pronounced when there are many countries than when only a few countries compete for mobile input factors.

The extent of the inefficiency under Formula Apportionment depends not only on the number of countries, but also on the shape of the formula. We therefore now turn to the comparison of different formulas. Remember that  $TE|_{FA}$  is independent of the formula weights  $(\gamma, \sigma, \varphi)$ , so we need to focus on the formula externality (30) only. Defining  $\Upsilon := -\hat{t}\Phi^2/[n(1-\hat{t})F_{kk}] > 0$  and considering the extreme cases of the formula weights, the formula externality can be written as

$$FE|_{(1,0,0)} = \Upsilon \frac{1}{k^2}, \quad FE|_{(0,1,0)} = \Upsilon \frac{F_k^2}{F^2}, \quad FE|_{(0,0,1)} = -\Upsilon \frac{F_{kk}}{\ell F_\ell}. \quad (31)$$

Concavity of the production function implies  $F > \bar{k}F_k$  so that  $FE|_{(1,0,0)} > FE|_{(0,1,0)}$ . The other comparisons are not unique, in general. However, for the CES production function introduced above we obtain  $F_k^2/F^2 = \mu^2 K^2/[\bar{k}^2(K+L)^2]$  and  $-F_{kk}/(\bar{\ell}F_\ell) = [(1-\mu)K + (1-\nu)L]K/[\bar{k}^2 L(K+L)]$ . These expressions allow the following statement.

**Proposition 5.** *Suppose the tax competition game under Formula Apportionment attains a symmetric Nash equilibrium with  $t_i = \hat{t}$ . Then*

(i) *the tax rate under the pure sales formula  $(\gamma, \sigma, \varphi) = (0, 1, 0)$  is greater than the tax rate under the pure capital formula  $(\gamma, \sigma, \varphi) = (1, 0, 0)$ .*

*If additionally the production function is of the CES type  $F(k, \ell) = [\delta k^\nu + (1-\delta)\ell^\nu]^\frac{\mu}{\nu}$  with  $\delta \in ]0, 1[$ ,  $\mu \in ]0, 1[$  and  $\nu \leq 1$ , then*

(ii) *the tax rate under the pure sales formula  $(\gamma, \sigma, \varphi) = (0, 1, 0)$  is greater than the tax rate under the pure payroll formula  $(\gamma, \sigma, \varphi) = (0, 0, 1)$  if  $\nu \leq 2 - \mu - \mu^2$ .*

The first part of Proposition 5 implies that inefficient undertaxation is less severe if the formula uses the sales factor instead of the property factor. The reason for this result is that we assume decreasing returns to scale caused by a third fixed production factor. Hence, the MNE's formula manipulation incentive and the associated formula externality are larger under the property formula than under the sales formula. Under the property formula, apportionment is targeted directly at the production factors

whereas under the sales formula the MNE's manipulation effort is hampered by the third production factor which cannot be altered by the MNE. Whether the sales formula is also superior to the payroll formula, however, depends not only on the importance of the fixed production factor but also on the elasticity of substitution between capital and labor. Intuitively, apportionment is directed at the production factor also under the payroll formula. But this factor cannot as easily be manipulated as the capital factor because labor is immobile. Hence, the conditions rendering the sales formula superior to the payroll formula are stronger than those rendering the sales formula superior to the property formula. More specific, capital and labor have to be sufficiently strong complements in the sense that  $\nu \leq 2 - \mu - \mu^2$ .

## 5 Concluding Remarks

In this paper, we have investigated the efficiency properties of corporate income taxation under Separate Accounting and Formula Apportionment. In contrast to the previous literature, our analysis takes explicitly into account the world capital market and the world interest rate determined on this market. Such a change in assumptions turned out to reverse the results obtained in the previous literature. With a fixed interest rate, Separate Accounting leads to corporate tax rates that are always inefficiently low, while under Formula Apportionment countries may end up with inefficient overtaxation. In the presence of an endogenous world interest rate, in contrast, it is the other way round. Under Separate Accounting we obtain an ambiguous result whereas Formula Apportionment leads to inefficiently low tax rates. This conclusion is true independent of whether countries are large or small.

Our results may have important policy implications. For the Formula Apportionment systems in countries like Germany and Switzerland, one may argue that the fixed interest rate assumption is suitable since these countries usually take as given the world interest rate and it also cannot be expected that corporate income taxation in these countries has a significant impact on the world capital market. This is different, however, for the U.S. which is usually seen the largest player in global trade of capital. Hence, even if the U.S. states do not take into account the effects of their Formula Apportionment taxation on the world interest rate, such an effect will be present and important for evaluating the efficiency of corporate taxation. Perhaps even more important, the endogenous interest rate assumption is relevant for the current reform discussion in the European Union. The European Union, too, is large enough to in-

fluence the world capital market, even if the individual member countries ignore this effect. Therefore, the switch from Separate Accounting to Formula Apportionment may miss the indented aim of mitigating detrimental tax competition. Such a situation would occur if the present tax rates are close to their efficient levels because the profit shifting and tax base externalities neutralize each other.<sup>5</sup> Then a switch to Formula Apportionment would be welfare-reducing since it unambiguously reduces the corporate tax rates below their efficient levels.

## Appendix

**A. Derivation of (9) – (12).** Equations (1) – (4) and (6) – (8) determine  $r$ ,  $k_i$ ,  $\ell_i$  and  $w_i$  for all  $i$ . Inserting (3) into the other equations and differentiating (6) yields

$$(1 - t)F_{kk}dk_i = (1 - \rho t)dr + (F_k - \rho r)dt_i. \quad (\text{A1})$$

Inserting (A1) in  $\sum_i dk_i = 0$  from (4) and solving for  $dr$  gives

$$dr = -\frac{F_k - \rho r}{n(1 - \rho t)} \sum_i dt_i. \quad (\text{A2})$$

Setting all but one  $dt_i$  equal to zero then proves  $\partial r / \partial t_i$  in (9). Using this result in (A1) shows (10). From (7) we get  $dw_i = F_{\ell k}dk_i$ . Using (10) proves (11). In order to show (12), totally differentiate (8). This yields

$$C''ds_i = d\lambda - dt_i. \quad (\text{A3})$$

Inserting (A3) in  $\sum_i ds_i = 0$  from (1) and rearranging terms gives  $nd\lambda = \sum_i dt_i$ . If we set all but one  $dt_i$  equal to zero, it follows  $\partial \lambda / \partial t_i = 1/n$ . From (A3), we obtain (12).

**B. Proof of Proposition 2.** In a symmetric equilibrium, equation (6) reads

$$(1 - \tilde{t})[F_k(\bar{k}, \bar{\ell}) - \rho r] - r(1 - \rho) = 0. \quad (\text{A4})$$

It determines the equilibrium interest rate  $r$  as a function of  $\tilde{t}$ . Note that (A4) does not contain  $n$ , so  $r$  does not depend directly on the number of countries  $n$ . For a given

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<sup>5</sup>There are a lot of empirical studies showing that corporate tax rates in Europe have declined over the last decades and that there are strategic interactions between the policies of European countries, e.g. Devereux et al. (2002, 2008). But note that these studies do not explicitly quantify fiscal externalities and therefore do not allow for judging whether tax rates are inefficiently low or high.

$\tilde{t}$ , equations (15) and (16) then imply

$$\lim_{n \rightarrow \infty} (n-1)\text{PE} = \frac{\tilde{t}}{C'''} > 0,$$

$$\lim_{n \rightarrow \infty} (n-1)\text{TE}|_{\text{SA}} = -\frac{\tilde{t}(F_k - \rho r)[(1 - \rho\tilde{t})(F_k - \rho r - \bar{\ell}F_{\ell k}) - (1 - \tilde{t})\rho\bar{k}F_{kk}]}{(1 - \tilde{t})(1 - \rho\tilde{t})F_{kk}} \geq 0.$$

This proves the first part of Proposition 2.

In order to show the second part, note that in a symmetric equilibrium the first-order condition of country  $i$ 's revenue maximization can be written as  $G^i(t_1, \dots, t_n, n) := \partial g_i / \partial t_i = 0$  with  $t_1 = \dots = t_n = \tilde{t}$ . Total differentiation yields

$$\frac{d\tilde{t}}{dn} = -\frac{G_n^i}{\sum_j G_{t_j}^i}. \quad (\text{A5})$$

Due to symmetry, we can write  $\sum_j G_{t_j}^i = G_{t_i}^i + (n-1)G_{t_j}^i$  where in the latter term we have  $j \neq i$ . The sign of this expression can be determined by the stability of the tax competition game: Stability requires that the Jacobian matrix of the system  $G^i(t_1, \dots, t_n, n) = 0$  for  $i = 1, \dots, n$  is negative semi-definite. Computing the Jacobian matrix and its determinant and then applying the symmetry property yields  $(G_{t_i}^i - G_{t_j}^i)^{n-1}[G_{t_i}^i + (n-1)G_{t_j}^i]$ . This expression has to be positive if  $n$  is even and negative if  $n$  is odd. It follows  $G_{t_i}^i + (n-1)G_{t_j}^i < 0$  where we have used  $G_{t_i}^i < 0$  due to the second-order condition of country  $i$ 's tax revenue maximization. Hence, the denominator of (A5) is negative and the overall sign of  $d\tilde{t}/dn$  depends on the sign of  $G_n^i$ . To determine this sign, we explicitly compute  $G^i(t_1, \dots, t_n, n) = \partial g_i / \partial t_i = 0$  and apply the symmetry property. Using (6) – (8) and (9) – (12) yields after some tedious calculations

$$G^i(\tilde{t}, \dots, \tilde{t}, n) = F(\bar{k}, \bar{\ell}) - \bar{\ell}F_{\ell}(\bar{k}, \bar{\ell}) - \rho r \bar{k} + \tilde{t} \rho \bar{k} \frac{F_k - \rho r}{1 - \rho \tilde{t}} - (n-1)(\text{PE} + \text{TE}|_{\text{SA}}) = 0.$$

The first four terms of this expression do not depend on  $n$  as we argued above that  $r$  does not directly depend on  $n$ . Note also that we can keep  $\tilde{t}$  constant since we are looking for the partial derivative of  $G^i(\cdot)$  with respect to  $n$ . Using (15) and (16) it follows  $G_n^i = -(\text{PE} + \text{TE}|_{\text{SA}})/n$  which inserted into (A5) completes the proof.

**C. Derivation of (23) – (26).** Totally differentiating (3) yields  $d\ell_i = 0$ . Inserting this observation together with (22) in the total differential of (4), (21) and (22) and then applying the symmetry property yields

$$n\Phi \sum_{j \neq i} (dt_i - dt_j) A_{k_i}^j + (1-t)F_{kk}dk_i - (F_k - \rho r)d\tau - (1-t\rho)dr = 0, \quad (\text{A6})$$

$$n\Phi \sum_{j \neq i} (dt_i - dt_j) A_{\ell_i}^j + (1-t)F_{\ell k} dk_i - (1-t)dw_i = 0, \quad (\text{A7})$$

$$\sum_j dk_j = 0. \quad (\text{A8})$$

From equation (20) and the symmetry assumption we obtain

$$d\tau = dt_i + \sum_{j \neq i} (dt_j - dt_i) A^j = \sum_j \frac{dt_j}{n}. \quad (\text{A9})$$

Next, rearrange (A6) to

$$dk_i = \frac{1}{(1-t)F_{kk}} \left\{ \frac{F_k - \rho r}{n} \sum_j dt_j - n\Phi A_{k_i}^j \left[ (n-1)dt_i - \sum_{j \neq i} dt_j \right] + (1-t\rho)dr \right\} \quad (\text{A10})$$

Note that

$$\sum_i \left[ (n-1)dt_i - \sum_{j \neq i} dt_j \right] = 0. \quad (\text{A11})$$

Inserting (A10) into (A8), taking into account (A11) and solving for  $dr$  yields

$$dr = -\frac{F_k - \rho r}{n(1-t\rho)} \sum_j dt_j. \quad (\text{A12})$$

If we set one  $dt_j \neq 0$  and all others equal to zero, we obtain equation (23). Next, equations (23) and (A10) immediately imply

$$\frac{\partial k_i}{\partial t_i} = -\frac{n(n-1)\Phi A_{k_i}^j}{(1-t)F_{kk}}, \quad \frac{\partial k_i}{\partial t_j} = \frac{n\Phi A_{k_i}^j}{(1-t)F_{kk}}. \quad (\text{A13})$$

Using the expression for  $A_{k_i}^j$  in (A13) proves (24). Finally, we rearrange (A7) to

$$dw_i = F_{\ell k} dk_i + \frac{n\Phi}{1-t} \sum_{j \neq i} (dt_i - dt_j) A_{\ell_i}^j, \quad (\text{A14})$$

which establishes

$$\frac{\partial w_i}{\partial t_i} = F_{\ell k} \frac{\partial k_i}{\partial t_i} + \frac{n(n-1)\Phi}{1-t} A_{\ell_i}^j, \quad \frac{\partial w_i}{\partial t_j} = F_{\ell k} \frac{\partial k_i}{\partial t_j} - \frac{n\Phi}{1-t} A_{\ell_i}^j. \quad (\text{A15})$$

If we use equation (24) and the expression for  $A_{\ell_i}^j$  in (A15), we obtain after some rearrangements equations (25) and (26).

**D. Derivation of (28) – (30).** From the definition of  $\Phi^j$  in (2) we obtain

$$\text{TE}|_{\text{FA}} = \hat{t}A \frac{\partial \sum_j \Phi^j}{\partial t_i} = \frac{\hat{t}}{n} \left\{ (F_k - \rho r) \sum_j \frac{\partial k_j}{\partial t_i} - \bar{\ell} \sum_j \frac{\partial w_j}{\partial t_i} - n\rho \bar{k} \frac{\partial r}{\partial t_i} \right\}. \quad (\text{A16})$$

Equations (24) – (26) imply  $\sum_j (\partial k_j / \partial t_i) = \sum_j (\partial w_j / \partial t_i) = 0$ . Inserting these expressions into (A16) and taking into account (23) proves (29). In order to prove (30), we differentiate  $A^j$  from (18) to obtain

$$\begin{aligned} \text{FE}|_{(\gamma, \sigma, \varphi)} = \hat{t}n\Phi \frac{\partial A^j}{\partial t_i} = \hat{t}n\Phi \left[ A_{k_j}^j \frac{\partial k_j}{\partial t_i} + A_{k_i}^j \frac{\partial k_i}{\partial t_i} + (n-2)A_{k_h}^j \frac{\partial k_h}{\partial t_i} \right. \\ \left. A_{w_j}^j \frac{\partial w_j}{\partial t_i} + A_{w_i}^j \frac{\partial w_i}{\partial t_i} + (n-2)A_{w_h}^j \frac{\partial w_h}{\partial t_i} \right] \end{aligned} \quad (\text{A17})$$

where  $i \neq j \neq h \neq i$ . In a symmetric equilibrium, we have  $\partial k_h / \partial t_i = \partial k_j / \partial t_i$ ,  $\partial w_h / \partial t_i = \partial w_j / \partial t_i$ ,  $\partial k_i / \partial t_i = -(n-1)\partial k_j / \partial t_i$  and  $\partial w_i / \partial t_i = -(n-1)\partial w_j / \partial t_i$ . Inserting this into (A17) and taking into account  $A_{k_h}^j = A_{k_i}^j$  and  $A_{w_h}^j = A_{w_i}^j$  gives

$$\text{FE}|_{(\gamma, \sigma, \varphi)} = \hat{t}n\phi \left[ \frac{\partial k_j}{\partial t_i} (A_{k_j}^j - A_{k_i}^j) + \frac{\partial w_j}{\partial t_i} (A_{w_j}^j - A_{w_i}^j) \right]. \quad (\text{A18})$$

In the symmetric equilibrium, we get  $A_{k_j}^j - A_{k_i}^j = -(n-1)A_{k_i}^j - A_{k_i}^j = -nA_{k_i}^j = (\gamma\bar{k} + \sigma F_k / F) / n$  and  $A_{w_j}^j - A_{w_i}^j = -(n-1)A_{w_i}^j - A_{w_i}^j = -nA_{w_i}^j = \varphi / (nw)$ . Making use of these derivatives, (24) and (26) in (A18) proves (30).

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