# ECONSTOR 

A Service of zBய

Leibniz-Informationszentrum Wirtschaft Leibniz Information Centre

# Working Paper <br> Why votes have a value 

SFB 649 Discussion Paper, No. 2007,068

## Provided in Cooperation with:

Collaborative Research Center 649: Economic Risk, Humboldt University Berlin

Suggested Citation: Dittmann, Ingolf; Kübler, Dorothea; Maug, Ernst; Mechtenberg, Lydia (2007) : Why votes have a value, SFB 649 Discussion Paper, No. 2007,068, Humboldt University of Berlin, Collaborative Research Center 649 - Economic Risk, Berlin

This Version is available at: https://hdl.handle.net/10419/25240

## Standard-Nutzungsbedingungen:

Die Dokumente auf EconStor dürfen zu eigenen wissenschaftlichen Zwecken und zum Privatgebrauch gespeichert und kopiert werden.

Sie dürfen die Dokumente nicht für öffentliche oder kommerzielle Zwecke vervielfältigen, öffentlich ausstellen, öffentlich zugänglich machen, vertreiben oder anderweitig nutzen.

Sofern die Verfasser die Dokumente unter Open-Content-Lizenzen (insbesondere CC-Lizenzen) zur Verfügung gestellt haben sollten, gelten abweichend von diesen Nutzungsbedingungen die in der dort genannten Lizenz gewährten Nutzungsrechte.

## Terms of use:

Documents in EconStor may be saved and copied for your personal and scholarly purposes.

You are not to copy documents for public or commercial purposes, to exhibit the documents publicly, to make them publicly available on the internet, or to distribute or otherwise use the documents in public.

If the documents have been made available under an Open Content Licence (especially Creative Commons Licences), you may exercise further usage rights as specified in the indicated licence.


## SFB 649 Discussion Paper 2007-068

# Why Votes Have a Value 

## Ingolf Dittmann* <br> Dorothea Kübler** Ernst Maug*** Lydia Mechtenberg**



* Erasmus University Rotterdam, Netherlands
** Technische Universität Berlin, Germany *** Universität Mannheim, Germany

This research was supported by the Deutsche
Forschungsgemeinschaft through the SFB 649 "Economic Risk".
http://sfb649.wiwi.hu-berlin.de ISSN 1860-5664

SFB 649, Humboldt-Universität zu Berlin
Spandauer Straße 1, D-10178 Berlin

# Why Votes Have a Value* 

Ingolf Dittmann ${ }^{\text {a }}$

Dorothea Kübler ${ }^{\text {b }}$
Lydia Mechtenberg ${ }^{\text {d }}$

December 17, 2007


#### Abstract

We perform an experiment where subjects pay for the right to participate in a shareholder vote. We find that experimental subjects are willing to pay a significant premium for the voting right even though there should be no such premium in our setup under full rationality. Private benefits from controlling the firm are absent from our setup and overconfidence cannot explain the size of the observed voting premium. The premium disappears in treatments where voting has no material consequences for the subjects. We conclude that individuals enjoy being part of a group that exercises power and are therefore willing to pay for the right to vote even when the impact of their own vote on their payoffs is negligible.


JEL Classification: C92, D72, G32
Keywords: Voting, dual-class shares, paradox of voting, experimental economics

[^0]
## 1 Introduction

In this paper we investigate experimentally why individuals value the right to vote. The observation that people generally value the right to vote is common to the literature in political science as well as in financial economics. However, no generally accepted explanation of this phenomenon has emerged, and the two disciplines just mentioned differ substantially in their approach to this problem. We contrast two explanations. The instrumental voting hypothesis holds that voters value the right to vote only as a mean to an end, as voting allows each voter to affect decisions he cares about, whereas voters do not attach a value to the opportunity to vote itself. The non-instrumental voting hypothesis holds that voters value the right to vote beyond purely instrumental reasons. Our experimental evidence is inconsistent with all versions of the instrumental voting hypothesis we consider and we interpret our results as supportive of non-instrumental voting. In particular, we conclude that experimental subjects value the opportunity to join a group that exercises power over decisions that have an effect on their own wealth, even if their own influence on the group's decision is negligible.

In political science the instrumental view of voting is a key element of the rational choice literature (Downs, 1957; Riker and Ordeshook, 1968) but has usually been criticized because with a larger number of voters the opportunity of any individual voter to affect the outcome and to be pivotal for the final result is miniscule. ${ }^{1}$ Hence, if voting is associated with costs, however small, then it is not rational for voters to participate in elections. Several authors have therefore argued that there may be alternative benefits from voting. These theories have in common that voters do not just benefit from the votes indirectly through their ability to affect decisions in their favor, but they receive also a direct benefit from voting. ${ }^{2}$ We use the term non-instrumental voting in order to describe motivations to vote other than the utility derived from the outcome of the vote weighted with the probability of being pivotal for the outcome.

[^1]In financial economics the right to vote has a monetary value that can be observed for those companies that issue two classes of stock with the same dividend rights, where one class (henceforth referred to as A-shares) has the right to vote, whereas the other class of otherwise identical B-shares do not carry any voting rights. The difference between the prices of two classes of otherwise identical shares represents the monetary value of a vote and is referred to as the "voting premium." Empirically this voting premium varies between 5\% and $80 \%$ across countries (see Appendix A for a discussion of this literature).

Financial economists have addressed the problem of pivotality with a different (but solely instrumental) argument. If bidders in a takeover want to take control of the company, then they are willing to pay a premium for voting shares but not for non-voting shares. At any point in time there is a certain probability that a company is taken over and that such a premium would be paid, so we should always expect non-voting shares to trade at a discount to voting shares, which is exactly what we observe. In Appendix A we review the empirical literature that analyzes whether observed takeover premiums can be explained by future expected takeover premiums, and we conclude that the takeover theory and its variants alone cannot explain the voting premiums actually paid in financial markets. The reason is that we also observe large voting premiums in countries with no or hardly any takeovers, that only a part of the ex ante voting premiums can be justified by the average voting premiums that are paid ex post when takeovers actually occur, and that we also observe large voting premiums for companies where the bylaws force bidders to pay the same price for the B-shares as they pay for the A -shares.

Combining the literatures from political economy and financial economics yields a number of unique insights for both fields. In our experiment we model a firm where shareholders vote on replacing the manager. This set-up allows us to quantify the value of voting, and to distinguish between instrumental and non-instrumental explanations. ${ }^{3}$ Also the setup is largely immune to moral considerations such as a duty to vote in order to support democracy. Our analysis shows that behavioral biases affect the premium shareholders are willing to pay

[^2]for being allowed to vote. To the best of our knowledge, we are the first to show that the voting premium can be explained by behavioral biases. ${ }^{4}$

In our experiment, there are two classes of shares, which are auctioned off at the beginning. One class of shares has the right to vote and the other class has not. In the first period the company pays a dividend that depends on the quality of a randomly assigned manager. The second period's dividend is influenced by an intermediate vote where those experimental subjects who bought the voting shares decide on the replacement of the manager by a majority vote. Since non-voting shares receive exactly the same dividends as voting shares, there are no conflicts of interest between the holders of the two classes of shares. In our experiment we find that individuals nevertheless attach a significant value to the right to vote, which equals about $13 \%$ of the value of the shares. Note that we observe this voting premium in a context without the possibility of takeovers. Thus, our design leads to voting premiums beyond those explained by takeovers, just as observed in the empirical literature on dual class shares.

Within our setup we can separate the instrumental and the non-instrumental aspects of voting. We develop two different versions of the instrumental voting hypothesis:
A. Individuals are either fully rational (Nash equilibrium) or they make errors, but the errors are symmetric and common knowledge (for example, in a Quantal Response Equilibrium).
B. Individuals make random errors and they are overconfident, i.e. they believe that they can avoid errors better than other voters.

We show that both cases considered in version A of the instrumental voting hypothesis predict that there should be no voting premium. The more restrictive setup assumes that all subjects are rational and that rationality is common knowledge. A somewhat milder implementation of the rational choice paradigm is an error model such as the Quantal Response Equilibrium (QRE) as proposed by McKelvey and Palfrey (1995, 1998), where voters are assumed to make random mistakes and then formulate strategies that are best responses in such a context. We show that QRE is a good model of the voting behavior in our experiment. As errors are assumed to be symmetric and common knowledge, however, the QRE does not predict a voting premium.

[^3]In version $B$ of the instrumental voting hypothesis we drop the assumption that rationality is common knowledge and assume instead that voters are overconfident and believe that they make fewer mistakes when voting than other participants in the same game. We show how this leads to a voting premium, but it is orders of magnitude smaller than the voting premium actually observed. We therefore reject all versions of the instrumental voting hypothesis as it contributes little to understanding our experimental results.

With the help of our experimental design we can differentiate between three different versions of the non-instrumental voting hypothesis:
A. Individuals value the right to vote because they enjoy the status of being a voter and expressing themselves, even if the outcome of the vote has no material consequences for them. We call this the "expressive voting hypothesis."
B. Individuals enjoy voting for the winner and joining a "bandwagon," and they are willing to pay for this opportunity.
C. Individuals enjoy being part of an influential group, but only in so far as the group's decisions have material consequences.

We find that our results are consistent only with version $C$ of the non-instrumental voting hypothesis. If the decision voters take has no material consequences, then experimental subjects are not willing to pay more for the voting shares compared to the non-voting shares, which is inconsistent with version A of the instrumental voting hypothesis. We also do not observe a preference for joining a majority in the voting game, and our experimental subjects are not willing to pay a premium for the opportunity to join the bandwagon, which rejects also version $B$ of the non-instrumental voting hypothesis.

Our paper contributes to the literature in political science by considering a setting that allows us to quantify the subjective value of voting. In addition, the experiment is phrased in a way that makes it unlikely that moral or status considerations have an effect on the outcome. If we had modeled the experiment as a political election, subjects might have paid for a voting right, because they regard voting as a civic duty to support democracy or as a sign of being a full member of society. ${ }^{5}$ Our experimental design also rules out the "voter's illusion" (see

[^4]Quattrone and Tversky, 1984) where the voter believes that if he incurs the costs of voting, others from the same interest group will do so as well. In our setting, the number of voters (or the "turnout") is always constant and the question is not how many individuals vote, but who votes. Also, there are no interest groups because the incentives of all subjects are fully aligned.

We contribute to the literature on financial economics by offering an additional hypothesis for the existence of the voting premium. We suggest that the price of the corporate voting right may be influenced by non-instrumental considerations. While behavioral biases like this have been used in many applications in financial economics, they have never been applied to shareholder voting to the best of our knowledge. ${ }^{6}$

The remaining part of the paper is structured as follows. Section 2 develops the model and the main hypotheses. Section 3 describes the experimental setup. Section 4 discusses our experimental evidence on the instrumental voting hypothesis, and Section 5 analyzes the noninstrumental voting hypothesis. Section 6 concludes. The appendix summarizes our reading of the literature on dual class shares and contains a proof and more details on the experiments.

## 2 The model

### 2.1 Model setup

General setup. The game has $N$ potential risk-neutral investors with an initial endowment of cash who can bid for shares in a company. There are two classes of shares: A-shares, which give shareholders voting rights in the company, and B-shares, which have no voting rights. Ashares and B-shares are both entitled to the same dividends per share and the number of Ashares and the number of B -shares is $M<N$ for each class. At the beginning investors bid for shares in the company, and each investor can buy at most one share of each class. Then there are two periods, $t=1,2$, and the firm pays a dividend $D_{\mathrm{t}}$ in each period. Dividends depend on the quality of the manager employed and on a state of nature. The basic setup is the same for both periods. After observing the dividend paid in the first period shareholders vote on the replacement of the manager and decide who runs the firm in the second period.

Technology and dividends. Managers are drawn from a pool and the number of good managers and bad managers in the pool is the same. If the manager is good, then the dividend

[^5]in period $t$ is high $\left(D_{t}=H\right)$ with probability $p \geq 0.5$. In the complementary state the dividend is low $\left(D_{t}=L<H\right)$ with probability $1-p$. If the manager is bad, then $D_{t}=L$ with probability $p$ and $D=H$ with probability $1-p$. Investors know the probability $p$, but not the quality of the manager. Since firms draw a good manager or a bad manager from the pool with equal likelihood, the posterior probability of having a good manager is therefore $p$ if $D_{t}=H$ and $1-$ $p$ if $D_{t}=L$.

Voting. Shareholders observe the dividend in the first period and then vote on the replacement of the manager by majority vote. Only owners of A-shares are allowed to vote and they have one vote per share. We assume $M$ is odd for simplicity, so the manager will be replaced whenever at least $(M+1) / 2$ votes are cast for the replacement of the manager. Then a new manager is drawn from the same pool for the second period, so the new manager is good or bad with the same probability $p$. If fewer than $(M+1) / 2$ votes are cast for the replacement of the manager, then the old manager stays in charge.

Initial allocation of shares. At the beginning, each investor can submit a bid for one A-share and another bid for one B-share. No investor is allowed to bid for multiple shares of the same class, but each investor bids simultaneously for one A-share and one B-share. ${ }^{7}$ It is not possible not to bid, but it is possible to bid zero. The auctioneer collects the $N$ bids for each class of shares. The shares for each class are then allocated to the investors who submitted the $M$ highest bids. Investors pay a price equal to the $M+1^{\text {st }}$ bid submitted for this class of shares. If several investors submit identical bids so that the $M^{\text {th }}$ bid is not unique, then the auctioneer allocates the shares by lot among these investors.

Sequence of events. We therefore obtain the following extensive form of the game:

1. Nature draws the quality of the manager who runs the firm. Investors bid for shares in the firm.
2. The auctioneer allocates the shares of the firm to investors and sets prices. Investors pay the price for the shares they are allocated.

[^6]3. The dividend for the first period is realized, becomes observable to all investors, and is paid to all shareholders.
4. A-shareholders vote on the replacement of the manager.
5. The dividend for the second period is realized, becomes observable to all investors, and is paid to all shareholders.

The setup is the simplest setup that allows us to separate the different versions of the instrumental voting hypothesis and the non-instrumental voting hypothesis, respectively. We need a minimum of two periods, so that individuals can learn and make inferences from the first dividend, and then make appropriate decisions contingent on the first dividend.

We use two classes of otherwise identical shares in order to control for unobservable factors that might affect individuals' valuations. In particular, our setup is robust to risk-aversion, because risk-aversion affects the prices of the two types of shares, but not the price difference, which is the quantity we are most interested in.

### 2.2 Instrumental voting

In this section we make theoretical predictions for the voting premium that are implied by different versions of the instrumental voting hypothesis. We first calculate the symmetric Nash equilibrium under the assumption that investors are fully rational. Then we allow for symmetric errors that are common knowledge (Quantal Response Equilibrium), and finally introduce overconfidence as a behavioral bias.

### 2.2.1 Nash equilibrium

Voting. Shareholders observe the dividend of the first period and infer that the manager is good with probability $p$ and bad with probability $1-p$. Denote by $\delta \in\{R, K\}$ the decision to replace $(R)$ or to keep $(K)$ the manager. In the first period and, if the manager is replaced, also in the second period, we have:

$$
\begin{equation*}
E\left(D_{1}\right)=E\left(D_{2} \mid D_{1}=H, \delta=R\right)=E\left(D_{2} \mid D_{1}=L, \delta=R\right)=\frac{H+L}{2} . \tag{1}
\end{equation*}
$$

After observing a high dividend, the posterior probability of the manager to be good is $p$. Hence, if the manager is kept, we obtain:

$$
\begin{align*}
E\left(D_{2} \mid D_{1}=H, \delta=K\right) & =p(p H+(1-p) L)+(1-p)(p L+(1-p) H) \\
& =\frac{H+L}{2}+2\left(\frac{1}{4}-p(1-p)\right)(H-L) . \tag{2}
\end{align*}
$$

Similarly, after observing a low dividend:

$$
\begin{align*}
E\left(D_{2} \mid D_{1}=L, \delta=K\right) & =p(p L+(1-p) H)+(1-p)(p H+(1-p) L) \\
& =\frac{H+L}{2}-2\left(\frac{1}{4}-p(1-p)\right)(H-L) . \tag{3}
\end{align*}
$$

Note that $p(1-p) \leq 1 / 4$, with equality only if $p=1 / 2$. It follows from (1), (2) and (3) that if $p>1 / 2$ then A-shareholders wish to replace the manager if $D_{1}=L$ and they wish to keep the manager if $D_{1}=H$. If $p=1 / 2$ they are indifferent between replacing and keeping the manager. In principle there are many asymmetric equilibria of this game where a majority of shareholders either votes to replace or to keep and no shareholder is pivotal for the decision. For example, in one equilibrium $(M+1) / 2+1 \mathrm{~A}$-shareholders always vote to replace the manager and $(M-1) / 2-1$ shareholders always vote to keep her. However, there is no central coordinating mechanism in this game to allocate different roles to shareholders. In the unique symmetric trembling hand-perfect equilibrium all A-shareholders vote to replace if $D_{1}=L$ and to keep if $D_{1}=H$ as long as $p>1 / 2 .{ }^{8}$ We focus on this equilibrium here and ignore the asymmetric equilibria of the voting game. We also ignore non-responsive symmetric equilibria where all shareholders vote for the same alternative all of the time. Note that these would not be trembling-hand perfect.

Bidding and valuation. Using equation (1), we obtain from the equilibrium replacement decision:

$$
\begin{align*}
V_{\text {Nash }} & =E\left(D_{1}\right)+\frac{1}{2} E\left(D_{2} \mid D_{1}=H, \delta=K\right)+\frac{1}{2} E\left(D_{2} \mid D_{1}=L, \delta=R\right) \\
& =H+L+\left(\frac{1}{4}-p(1-p)\right)(H-L) . \tag{4}
\end{align*}
$$

Whenever $p>1 / 2$ we have $V_{\text {Nash }}>H+L$. Without voting $V_{\text {Nash }}=H+L$. The second term in equation (4) therefore reflects the benefits from voting to shareholders, which are zero when

[^7]$p=1 / 2$. The intrinsic value $V_{\text {Nash }}$ is the same for A-shares and for B-shares. The auction is a standard multi-unit Vickrey auction, so it is a weakly dominant strategy for each investor to bid the intrinsic value $V_{\text {Nash }}$ for one A-share and also for one B-share. If all investors do this, then the unique price for the A-shares is $P_{A}=V_{\text {Nash }}$, and, similarly for the B -shares $P_{B}=V_{\text {Nash }}$, so there is no price difference between the two classes of shares. Since all investors bid the same the auctioneer then allocates the shares by lot.

### 2.2.2 Errors and overconfidence

It is well-known that participants in experiments deviate from pure Nash strategies and that they also take into account the possibility that other players make mistakes in the formulation of their own optimal strategy. For this reason McKelvey and Palfrey $(1995,1998)$ develop the concept of a Quantal Response Equilibrium (QRE), which has been successfully applied to the analysis of experimental results. ${ }^{9}$ The notion of a QRE is based on the assumption that players make mistakes and that their strategies are best responses given the mistakes they anticipate other players to make. We first develop the symmetric, standard notion of QRE and show that as long as it is common knowledge that errors are symmetric across players, the valuation of the two classes of shares is the same (although lower than in Nash equilibrium). We then go one step further and analyze the case where investors are overconfident and believe that they make fewer errors than other bidders.

Rationality with errors. We denote the probability that an A-shareholder makes an error when voting on the dismissal of the manager by $\tau_{D_{1}}$. So $\tau_{L}$ is the probability that an Ashareholder votes against a dismissal after observing a low dividend, and $\tau_{H}$ is the probability that a shareholder votes for dismissal after observing a high dividend. As individual errors are independent from one another, the voting equilibrium now involves a certain probability of a mistake, namely:

$$
\begin{align*}
& e_{L}=\operatorname{Pr}\left(\delta=K \mid D_{1}=L\right)=\sum_{i=(M+1) / 2}^{M}\binom{M}{i} \tau_{L}^{i}\left(1-\tau_{L}\right)^{(M-i)},  \tag{5}\\
& e_{H}=\operatorname{Pr}\left(\delta=R \mid D_{1}=H\right)=\sum_{i=(M+1) / 2}^{M}\binom{M}{i} \tau_{H}^{i}\left(1-\tau_{H}\right)^{(M-i)} . \tag{6}
\end{align*}
$$

[^8]The manager is therefore kept after a high dividend with probability $\left(1-e_{H}\right) / 2$. Then the expected dividend in the second period is $E\left(D_{2} \mid D_{1}=H, \delta=K\right)$ as given in equation (2). With probability $\left(1-e_{L}\right) / 2$ the manager is replaced after a low dividend, and with probability $e_{H} / 2$ the manager is replaced after a high dividend. In both cases the expected dividend then equals $(H+L) / 2$ from (1). With probability $e_{L} / 2$ the manager is kept after a low dividend and then $E\left(D_{2} \mid D_{1}=L, \delta=K\right)$ as given in equation (3). Then the value of one share is:

$$
\begin{equation*}
V_{Q R E}=H+L+\left(\frac{1}{4}-p(1-p)\right)(H-L)\left(1-e_{L}-e_{H}\right) \tag{7}
\end{equation*}
$$

For the case without errors we have $e_{L}=e_{H}=0$ and then the value of the shares in the QRE becomes equal to $V_{\text {Nash }}$ as in (4). Under our assumptions that the probability of making a mistake is symmetric across players and common knowledge, $P_{A}=P_{B}=V_{Q R E}$, so there is no price difference between voting A-shares and non-voting B-shares. Notice that this argument holds for any model with symmetric errors that are common knowledge.

Responsiveness. We follow the literature on QRE and assume that the error probabilities $\tau_{H}$ and $\tau_{L}$ are smaller if the utility that is at stake in the vote is higher and parameterize this relationship using a logistic function. We define the benefits from making the correct decision relative to making an incorrect decision by $\Delta U$ from the payoffs in (2) and (3) above as:

$$
\begin{equation*}
\Delta U=2\left(\frac{1}{4}-p(1-p)\right)(H-L) \geq 0 \tag{8}
\end{equation*}
$$

The probability of any A-shareholder to be pivotal is:

$$
\begin{equation*}
\pi_{D_{1}}=\binom{M-1}{(M-1) / 2} \tau_{D_{D_{1}}}{ }^{(M-1) / 2}\left(1-\tau_{D_{1}}\right)^{(M-1) / 2} \tag{9}
\end{equation*}
$$

Then the expected payoff from making the correct decision is $\pi \Delta U$ and with this the probability of making an error can be written as:

$$
\begin{equation*}
\tau(\lambda)=\frac{1}{1+\exp (\lambda \pi \Delta U)} \tag{10}
\end{equation*}
$$

We can write equation (10) without reference to the dividend paid at $\mathrm{t}=1$ because $\Delta U$ is identical for both levels of the dividend. Here, $\lambda$ is the responsiveness coefficient. If $\lambda=0$, then shareholders randomize between keeping and replacing the manager with equal
probability and $\tau_{H}=\tau_{L}=0.5$, independently of the utility difference from replacing or keeping the manager $\Delta U$. If $\lambda=\infty$, then $\tau_{H}=\tau_{L}=0$, so we obtain the symmetric responsive Nash equilibrium described in equation (4). Note that the definition of QRE requires that each Ashareholder chooses the error probability $\tau$ as a best response to that of all other shareholders, so that the error probabilities used in (9) are consistent with the probability of being pivotal used in (10).

Overconfidence. We now go one step further and assume that investors are overconfident in the following sense. At the voting stage they make errors as described above and the probabilities of making mistakes are the same for all investors. However, the symmetry of errors is no longer common knowledge and each investor believes that only other shareholders will make mistakes, whereas each investor himself can make the correct judgment without fail at the voting stage. With this belief, investors value the right to be pivotal at the voting stage because according to their beliefs it helps them to avoid the errors other investors would make. With this assumption the voting stage remains unchanged and the actual error probabilities are still given by (5) and (6).

With overconfident investors the valuation formulae for the expected dividends and therefore the intrinsic valuation in (7) have not changed. However, overconfident investors anticipate that they can improve on this valuation if they own a voting share and become pivotal in the voting game. The investor believes that whenever he is pivotal he can change the probability of replacing the manager if $D_{1}=L$ from $1-\tau_{L}$ to 1 and, if $D_{1}=H$ he can change it from $\tau_{H}$ to 0 . Hence, an overconfident investor overvalues the shares conditional on himself being able to vote by a premium $\omega$ :

$$
\begin{equation*}
\omega=\left(\pi_{H} \tau_{H}+\pi_{L} \tau_{L}\right)\left(\frac{1}{4}-p(1-p)\right)(H-L) \tag{11}
\end{equation*}
$$

The premium $\omega$ is the increase in intrinsic value of a share from the point of view of an overconfident investor who removes the errors he attributes to all other shareholders. This will generally not be the voting premium in equilibrium because of the interdependence between his valuation of the B -shares and his ability to obtain an A -share in the auction. An overconfident investor also values the non-voting shares above their intrinsic value (7) conditional on obtaining an A-share, because whenever he owns a voting share this also increases his valuation of the non-voting share. This interdependence makes the analysis of the equilibria of the auction game somewhat tedious and a complete characterization of these
equilibria is beyond the scope of this paper. ${ }^{10}$ We summarize the facts that are most important for our empirical analysis in the following proposition, which is proved in Appendix C.

Proposition 1: Assume that each investor believes that he himself will make the optimal decision at the voting stage of the game for certain, whereas all other investors make an error with positive probability. Each investor believes that each share of the company increases in value by $\omega$ if he owns one $A$-share. Then: (i) There exists no symmetric equilibrium in pure strategies; (ii) There exists a continuum of asymmetric equilibria in weakly undominated pure strategies where the voting premium satisfies $0 \leq P_{A}-P_{B} \leq 2 \omega$.

Intuitively, Proposition 1 can be understood as follows. Investors are willing to pay $2\left(V_{Q R E}+\omega\right)$ for both shares together. Prices below $V_{Q R E}$ cannot be sustained in equilibrium for any B-share, and, similarly, prices below $V_{\text {QRE }}+\omega$ cannot be sustained for any A-share. The reason is that those investors who bid low and receive no shares in equilibrium would otherwise be better off by bidding high for one type of share. However, the premium $\omega$ for the B-share can be allocated in any possible way between the A-share and the B-share. The highest premium results when the price of the A-share reflects the whole increase in value of both shares while the price of the B-share is just equal to $\mathrm{V}_{\text {QRE }}$. Conversely, both shares may be priced at $V_{Q R E}+\omega$ in equilibrium, so that the voting premium is zero. Any intermediate case is also possible.

### 2.3 Non-instrumental theories of voting

The discussion in the previous section relies on the notion of instrumental voting, where an individual's right to vote has a positive effect on the individual's payoffs. However, whenever the probabilities $\pi_{L}$ and $\pi_{H}$ of being pivotal are small, then the voting premium from (11) is also small. This is the paradox of voting discussed in political science, which has led to the investigation of alternative benefits of voting. We distinguish between three different notions of non-instrumental voting and discuss the related literature:

A: Expressive voting. At the most basic level, voters enjoy voting because it gives them the opportunity to "make their voice heard." The outcome and the ultimate effect of one's own vote on the outcome are secondary in this case. As Brennan and Hamlin (1998) describe the

[^9]expressive motivation to vote, "voter participation just is the act of consumption that brings the voter to the poll" (p.156). ${ }^{11}$ In the context of our model, we should then observe that investors value the voting right independently of how much influence it has on their payoffs.

B: Joining the bandwagon. Voters may derive satisfaction from voting for the winner. This desire can have several reasons, for example conformity (Bartels 1988) or the hope to benefit from patronage after the election (Fiorina 1974). Callander (2006) models such preferences and examines the formation of bandwagons in sequential and simultaneous elections. Schuessler (2000) argues that citizens like to attach to collectives, and he relates this to their preference to join the majority when voting. If this is the primary motivation of the participants in our experiments, then we should see that (1) they try to vote with the majority, i.e., there is some kind of "bandwagon," and (2) that they value votes more if they have more opportunities to join a collective. In particular, a stronger bandwagon effect should be associated with a higher voting premium.

C: Being part of an influential group. In this interpretation voters enjoy voting because it is associated with the status of being part of a group that is in control of a decision that affects the payoffs of group members. The key difference to version A of the non-instrumental voting hypothesis is that the group is influential, i.e. the group's decisions affect the utility of all citizens or - in case of a firm - of all shareholders. In our model, the A-shareholders collectively exercise power over the manager and therefore over the future dividends of the firm. This version of the non-instrumental voting hypothesis differs from instrumental voting in that it does not rely on the ability of any individual to change the outcome, which is only possible if the individual is pivotal. The key aspect of this notion of non-instrumental voting is that the individual benefits from being associated with a group that exercises influence collectively.

At first glance, hypothesis C seems to be identical to rule utilitarianism, which holds that individuals receive utility from following a rule that maximizes social surplus. ${ }^{12}$ While the welfare maximizing decision is obvious in the voting stage of the game, it is unclear,

[^10]however, what "welfare" is in the first stage of the game when the shares are auctioned off. If welfare is set equal to the payoff of the whole group, a bid of zero for A-shares and for Bshares is the welfare maximizing rule, so that the voting premium predicted by rule utilitarianism is zero. On the other hand, if welfare includes the payoff of the experimenter, any rule becomes welfare maximizing and rule utilitarianism does not yield any predictions on the voting premium. We therefore cannot test for rule utilitarianism in our framework.

## 3 Experimental setup

We implement the model described in Section 2.1 in an experiment and test if participants in our experiments value the right to vote, and if voting premiums are better explained by instrumental or by non-instrumental motivations.

All treatments have $N=8$ investors. There are $M=5 \mathrm{~A}$-shares and 5 B -shares, and the dividends are $H=20$ and $L=0$. The participants played the same game (treatment) for 30 rounds, and no participant played more than one of the treatments. There are four treatments: ${ }^{13}$

BASE: The base treatment has $p=80 \%$. With this the difference between the good manager with $\mathrm{E}(D)=16$ and the bad manager with $\mathrm{E}(D)=4$ is substantial and it should pay to solve the inference problem correctly. The inference problem is non-trivial, so it is plausible that some players do not trust other players to vote correctly and overconfident players should therefore tend to overvalue the voting rights associated with the A-shares.

NU: In the no-uncertainty treatment $p=100 \%$. Then $\mathrm{E}(D)=20$ with a high quality manager and $\mathrm{E}(D)=0$ with a low quality manager, so that the stakes have increased relative to the base treatment. In addition, the inference problem is now trivial, which should reduce the number of shareholders who vote against their interest and therefore also the inclination of our experimental subjects to distrust other participants. This treatment therefore serves as a robustness check on the base treatment, in particular to detect behavior in the base treatment

[^11]that should be properly attributed to errors in the statistical inference individuals need to perform.

NI: In the non-influential manager treatment $p=50 \%$. Then $\mathrm{E}(D)=10$ independently of the quality of the manager and the vote has no consequences for the value of the firm. The inference problem is trivial. While A-shareholders have an impact on decisions of the firm, they cannot influence the distribution of future dividends with their vote. If experimental subjects are motivated by expressive reasons as postulated by version A of the noninstrumental voting hypothesis, then they should value the right to vote in this treatment.

BH: In the block holder treatment all parameters are as in the base treatment, so $p=80 \%$. However, in addition to the 5 A -shares auctioned off in the beginning there is a block holder who owns 6 A-shares and who always votes in favor of the incumbent manager. As a result, it will never be possible to replace the manager no matter how the 5 new A-shareholders vote. This treatment is similar to the non-influential manager (NI) treatment with respect to the instrumental value of the vote, which is zero. However, from a behavioral point of view there is a difference between joining a pre-specified majority (the "bandwagon") and pure expressive voting. If individuals want to join the bandwagon (version $B$ of the noninstrumental voting hypothesis), then they should be willing to pay a premium on voting shares in treatment BH but not in treatment NI. On the other hand, if they vote for expressive reasons (version A of the non-instrumental voting hypothesis), then we should observe a voting premium in both treatments, BH and NI.

## Insert Table 1 here.

Table 1 shows an overview over the four different treatments. It contains the probability $p$ of a good manager to generate a high dividend and the number of additional shares held by a block holder who does not participate in the initial auction. In addition, the table shows the Nash value of the shares from equation (4). Shares are most valuable in treatment NU with $V_{\text {Nash }}=$ 25 and least valuable in treatments NI or BH with $V_{\text {Nash }}=20$.

Each treatment comprised 10 sessions that lasted for about 90 minutes each. In each session, eight subjects participated; and no subject participated in more than one session. Subjects' average earnings were 28 Euros, including a show-up fee of 3 Euros. The currency in the experiment was "points," which were exchanged into real money at the end of the experiment at the exchange rate of 1 point $=3$ cent. The exchange rate was commonly known to all participants. At the beginning of the experiment, each participant was given a budget of 150
points. In order to prevent investors from running out of money after a series of low (i.e. zero) dividends, each individual also received an additional 16 points at the end of each round. Appendix B contains a translation of the instructions for the base treatment.

All experiments were carried out in the computer lab at Technical University Berlin between January 2006 and September 2007. We used the software tool kit z-Tree, which was developed by Urs Fischbacher in 2007. Participants were students at universities in Berlin.

## 4 The instrumental voting hypothesis

We first investigate the different versions of the instrumental voting hypothesis by focusing on the base treatment and on the no uncertainty-treatment. We defer the discussion of noninstrumental approaches to Section 5.

### 4.1 Learning in the base treatment

We first analyze to what extent our experimental subjects learn during the experiment and motivate our decision to focus on the averages of all variables during the last 15 rounds of each session.

## Insert Figure 1 here.

The left panel of Figure 1 shows the frequency $\tau$ of incorrect votes, i.e. the frequency that Ashareholders vote for either replacing the manager after observing a high dividend or for keeping the manager after a low dividend. Similarly, the right part of Figure 1 shows the prices of voting and non-voting shares over time. The frequencies for the 30 rounds of each session are aggregated into six blocks of five rounds each. The figure indicates that subjects do learn during the experiment: Voting errors decrease over time and prices increase over time. The difference for individual errors $\tau$ between blocks 1 to 3 and blocks 4 to 6 is statistically highly significant for votes after a high dividend ( $\chi^{2}$-test with p -value $0.8 \%$ ). All other changes from blocks 1 to 3 to blocks 4 to 6 are not statistically significant. Thus, there is some learning in the data concerning the voting behavior after a high dividend, but it is not an important feature of our results. Thus, unless otherwise noted, we use averages across the last 15 periods (i.e. over the last 3 blocks in Figure 1) where learning processes have converged in all following analyses.

### 4.2 Prices in the base treatment

We analyze pricing behavior first. Table 2 shows statistics for the prices of voting and nonvoting shares $\left(P_{A}\right.$ and $\left.P_{B}\right)$ as well as for the voting premium $P_{A}-P_{B}$ and the scaled voting premium $\left(P_{A}-P_{B}\right) / 21.8$. We need to scale prices because the intrinsic values of the shares change across treatments. As the prices $P_{A}$ and $P_{B}$ are very volatile and therefore unsuitable for scaling, we scale by the risk-neutral value of the shares in Nash equilibrium from (4). Prices might be correlated within each session, so we average prices across the last 15 rounds for each session and present the results on these 10 observations in Panel A. For completeness we also report the same results for all 300 observations ( 10 sessions with 30 rounds each) in Panel B, where we treat every round as if it were an independent observation.

Insert Table 2 here.
From Table 2 we can clearly reject the hypothesis that the voting premium is zero, so individuals do value the right to vote. The voting premium is 2.91 on average (median 2.63). If we look at the entire sample of all 300 rounds then the voting premium is only slightly different with a mean of 2.82 and a median of 2.00 . These numbers are different from zero at all conventional significance levels, and at about $13 \%$ of the intrinsic value of the shares they are also economically significant.

The individual prices are also interesting. The average (median) price for an A-share is 18.52 (18.27), the average (median) price of a B-share is 15.61 (17.37). Hence, average prices are substantially below the risk-neutral Nash-equilibrium value of 21.80 in the base treatment ( $15 \%$ for A-shares, $28 \%$ for B-shares), and this difference is statistically highly significant. One interpretation is that individuals are risk-averse and therefore value the shares at less than their risk-neutral values.

### 4.3 Offers in the base treatment

Our analysis of offers arrives at the same qualitative conclusions as the analysis of prices. Table 3 shows descriptive statistics for the 80 average offers across the last 15 rounds for each subject in Panel A. Panel B displays the results for 2,400 individual offers ( 10 sessions with 8 subjects and 30 rounds). Offers are much more volatile than prices: Their standard deviation is six to eight times higher than the standard deviation of prices. Offers vary between 0 and 300 and there are no systematic changes over the rounds (not shown in the tables) as we observe them for prices and for voting behavior (see Figure 1). Given that the maximum
payout per share is 40 (if both dividends turn out to be high), any offer above 40 appears irrational at first glance. However, the five winners in the auction do not pay their own offers but the offer of the sixth highest bid, so bidding more than the intrinsic value of the share (or more than 40) is merely a weakly dominated strategy. Given that the equilibrium price is consistently lower than the expected value of the shares, subjects who make extremely high offers typically receive high payouts. So there is little incentive to refrain from offers that seem irrationally high as long as there are at least three subjects who offer less than the expected value of the shares. For this reason, we only interpret the median of the offers since it is less sensitive to these outliers.

Insert Table 3 here.
Median offers are by construction higher than (average or median) prices, because prices equal the sixth highest bid, i.e. the $25^{\text {th }}$ percentile of all offers. Table 3, Panel B reveals that $53.8 \%$ of all 2,400 pairs of bids feature a positive voting premium and only $10.8 \%$ bid less for the A-share than for the B-share. The remaining bids (35.4\%) have the same price for both shares. Again, voting premiums are positive and statistically significant at all conventional significance levels and we conclude that our experimental subjects value the right to vote. Overall, this shows that the Nash equilibrium described in Section 2.2.1 is a poor prediction for the outcomes of this experiment.

### 4.4 Voting behavior in the base treatment

The results may deviate from the standard Nash equilibrium simply because subjects make errors at the voting stage of the game. If sufficiently many subjects are overconfident and believe that they are better at voting than their fellow group members, then they might be willing to pay more for a voting share than for a non-voting share and drive up the voting premium. We explore this explanation by analyzing voting behavior.

$$
\text { Insert Table } 4 \text { here. }
$$

Table 4 displays the results of the voting stage. The table contains the results for all treatments, but we only interpret the results of the base treatment in this section. Panel A of Table 4 gives the individual and the collective errors from voting on the replacement of the manager. It shows that the frequency of A-shareholders voting for keeping the manager after observing a low dividend, $\tau_{L}$, is $18.33 \%$ averaged over the last 15 rounds. The frequency $e_{L}$ that after a low dividend more than two A-shareholders vote against replacing the manager is
$7.14 \%$. After a high dividend $11.82 \%$ of A-shareholders vote incorrectly (i.e. for replacing the manager), which results in an actual dismissal in $3.03 \%$ of all cases. Shareholders make significantly more mistakes after a low dividend than after a high dividend (the p-value for the $\chi^{2}$-test is $1.4 \%$, for the Wilcoxon test it is $14.8 \%$ ). This can be due to the fact that they are relatively more reluctant to fire a manager than to keep a manager. In Panel C, we display the responsiveness parameters $\lambda_{L}$ and $\lambda_{H}$ for the voting decisions after a high dividend and after a low dividend. The parameter $\lambda_{L}$ is smaller than $\lambda_{H}$, which mirrors the fact that the observed error rate is higher after a low dividend, but the difference between the two parameters is not statistically significant.

Panel B of Table 4 draws the relevant conclusions for the valuation of the shares. If the errors from decision-making at the voting stage are taken into account, then the value of shares in the Quantal Response Equilibrium, $V_{Q R E}$ is 21.69 from equations (5) to (7), so it is 0.11 lower than the Nash value of 21.8 . If the subjects in our experiment are overly optimistic in the sense that they believe that only the other subjects but not they themselves make errors, then we can estimate the premium $\omega$ they are willing to pay for a voting share as described in Proposition 1. This maximum premium turns out to be 0.116 , which is just $4.0 \%$ of the average observed premium of 2.911 , and this difference is also statistically significant at the $2 \%$ level. We conclude that errors and overconfidence cannot explain a meaningful portion of the observed voting premium.

### 4.5 The no-uncertainty treatment

We repeated the experiment with $p=1$, i.e. a good manager generates a high dividend with certainty and a bad manager generates a low dividend with certainty. Therefore, the inference problem at the voting stage is greatly reduced, and we expect fewer errors at the voting stage. Table 4, Panel B, shows that there are indeed fewer errors under NU than under BASE. After a low dividend, $18.33 \%$ of the subjects vote for keeping the manager in the base treatment while only $11.03 \%$ do so in the no-uncertainty treatment. However, the difference is only marginally significant in a one-sided Wilcoxon test (p-value: 7.8\%). ${ }^{14}$ Moreover, under BASE we observe inefficient voting outcomes after a low dividend in $7.14 \%$ of all cases while we do not observe any inefficient voting outcomes under NU. This difference is significant with a pvalue of $2.5 \%$. After a high dividend, error rates are also lower under NU than under BASE,
but here the differences are not statistically significant. Interestingly, the reluctance of some shareholders to fire the manager after a low dividend, observed in BASE, is clearly lower in treatment NU : the difference between $\tau_{L}$ and $\tau_{H}$ is not significant in NU . Note that in NU , it is certain that the manager is bad when a low dividend was paid whereas in BASE, there is a small probability after a low dividend that the manager is good. This might explain the reluctance to fire the manager after a low dividend in BASE but not in NU.

The potential loss $\Delta U$ that is incurred after a wrong decision is markedly higher in the NU treatment than in the BASE treatment (see Table 1). If this higher loss is the reason for the decrease in the error rates in NU relative to BASE, then the responsiveness parameters from (10) should not differ between the two treatments. Panel C of Table 4 shows that the responsiveness parameters $\lambda_{L}$ and $\lambda_{H}$ indeed do not differ significantly between BASE and NU.

We also investigate whether overconfidence can explain the voting premium in the NUtreatment. Interestingly, the maximum voting premium that could be explained by overconfidence from Proposition 1 is 0.120 and therefore almost identical to that observed in the base treatment. There are two opposing effects here. The first is that error probabilities go down relative to BASE, which reduces the maximum voting premium with overconfidence. However, the loss $\Delta U$ caused by a wrong decision increases from 3.6 in BASE to 10 in NU (see Table 1). This second effect increases the upper bound $2 \omega$ from Proposition 1 (see equations (8) and (11)) on the voting premium. Both effects cancel each other and the maximum premium with overconfidence stays constant at 0.12 .

## Insert Table 5 here.

Table 5 shows descriptive statistics for prices (Panel A) and offers (Panel B) averaged across the last 15 rounds for the no-uncertainty treatment. Given that the Nash-value of the shares is higher under the no-uncertainty treatment than in the base treatment, it is not surprising that prices and offers are also generally higher. However, the differences between prices in BASE and NU are never significant. The mean (median) relative price premium of voting shares is $16.0 \%(12.5 \%)$ in Table 5, Panel A which is higher than in the base treatment, where it is $13.4 \%$ ( $12.1 \%$, see Table 2, Panel A), although the difference is also not significant. Mean and median offers are slightly lower under NU than under BASE (compare Table 5, Panel B

[^12]with Table 3, Panel A), but the difference is again not significant. We conclude that the results for the no-uncertainty treatment are similar to those in the base treatment overall.

Summary on the instrumental voting hypothesis. Our evidence from the base treatment and the no uncertainty treatment is inconsistent with the hypothesis that voters are willing to pay a premium on voting shares because they are overconfident. Altogether, this rejects all variants of the instrumental voting hypothesis exposed in Section 2. Whereas voting behavior can be explained reasonably well by applying the QRE-concept, actual bidding behavior violates not only the predictions of Nash equilibrium, but also the boundedly rational QRE and the interpretation of voting premiums as prices that overconfident voters are willing to pay. We therefore conclude that the voting premium must have a significant non-instrumental component.

## 5 Non-instrumental theories of voting

The remaining task is to distinguish the three different versions of the non-instrumental voting hypothesis from each other. We use two further treatments, the non-influential manager (NI) treatment and the block holder (BH) treatment for this purpose (see Section 3 and Table 1 for the details of these treatments).

The block holder and non-influential manager treatments are similar in that the vote of the Ashareholders does not affect the expected second period dividend. In the NI-treatment this is the case because the quality of the manager does not affect dividend payments, and in the BHtreatment the vote has no influence because the manager can never be replaced. However, the BH-treatment differs in two important respects from the NI-treatment. Firstly, in the block holder treatment it is clear what the dividend-maximizing decision is, even though this decision cannot be taken here because of the veto power of the block holder. By contrast, in the non-influential manager treatment there is no dividend-maximizing decision. Secondly, in the block holder treatment the outcome of the vote is given ex ante and known to the experimental subjects, because they know the voting behavior of the block holder, so it is clear what the majority is. In the non-influential manager treatment the outcome of the vote is uncertain and there is no clear majority ex ante.

If there is a voting premium in the non-influential manager treatment (NI), then subjects must value the act of voting itself, even if it has no payoff consequences for them.

Insert Table 6 here.

Table 6 reports the results for the non-influential manager treatment. It is structured like Table 5, with average prices in Panel A and average offers in Panel B. From Panel A we can see that the voting premium becomes very small and statistically indistinguishable from zero. Moreover, the voting premium is significantly smaller under the NI treatment than under either the BASE or the NU treatments. All tests for the premium are significant with p-values below $5 \%$ for comparisons with the base treatment and below $1 \%$ for comparisons with the no uncertainty treatment. If subjects valued the act of voting in itself as hypothesized by the expressive voting hypothesis, then we should not observe any significant difference between the NI-treatment on the one hand and the BASE or the NU-treatment on other hand. The results from treatment NI in Table 6 therefore reject version A of the non-instrumental voting hypothesis.

Insert Table 7 here.
Table 7 reports the results for the block holder treatment. It is structured like Tables 5 and 6. From the discussion above a voting premium in the block holder treatment ( BH ) can be explained with a propensity to vote for the winner, i.e. the bandwagon effect. This would be consistent with version B of the non-instrumental voting hypothesis. Utility from voting for the winner (version B) would require (1) that subjects value the voting right and pay a premium for it and (2) that they vote with the block holder. Table 7 shows that there is no voting premium in treatment BH . The premium is 0.29 on average, but no test can reject the null hypothesis that it is zero even at the $10 \%$-level. By contrast, all tests reject the hypothesis that the premium under the BH-treatment is the same as under the BASE treatment or the NU treatment. Table 4, Panel A shows that voting behavior in the BH treatment is also inconsistent with the bandwagon hypothesis as the number of votes for keeping the manager is always lower in the BH treatment than in the NU treatment which generates exactly the same payoffs. After a low dividend, only $31.2 \%$ of the voters "join the bandwagon" and vote for the incumbent manager in the BH treatment, i.e. only 13 percentage points more than in the BASE treatment. We therefore find no evidence that would be consistent with version B ("bandwagon-effect") of the non-instrumental voting hypothesis.

Summary on the non-instrumental voting hypothesis. The block holder and non-influential manager treatments clearly reject the hypothesis that voters are willing to pay a premium for the right to vote if they have collectively no influence on the final outcome. It does not matter whether this is so because the outcome of the vote itself does not matter, as in the non-
influential manager treatment, or whether somebody else effectively makes the decision, as in the block holder treatment. However, all of our observations are consistent with version C of the non-instrumental voting hypothesis, which stipulates that voters value the right to be part of a group that makes relevant decisions, even though their own contribution to the decisionmaking process (i.e., their probability to be pivotal) is small.

The results on the non-influential manager treatment and the block holder treatment allow us to address a potential criticism of our experiment, which holds that subjects pay for the right to vote for the mere entertainment value of voting: They might value the right to vote simply to avoid looking at a blank screen while the other participants in the experiment vote. This argument implies that a positive voting premium should be found in all our treatments. Our results show, however, that individuals are not willing to pay for the right to vote when the voting decision does not have material consequences.

## 6 Conclusion

We perform an experiment where experimental subjects pay for the right to vote. The main conclusion from our analysis is that experimental subjects are willing to pay a significant premium for the right to vote. This voting premium cannot be explained by any version of the instrumental voting hypothesis. Even overconfident subjects who believe that they can avoid mistakes other subjects would make would not be willing to pay more than $4 \%$ of the voting premium we actually observe in our experiment. Our results therefore strongly suggest that people value the right to vote, and that they do so for reasons not addressed by the instrumental voting hypothesis.

We distinguish between three non-instrumental theories of voting. (A) Purely expressive voting implies that individuals value the right to vote independently of their impact on the outcome, but we find no evidence for this implication. The voting premium vanishes in both treatments where individuals cannot influence the dividend paid to the shareholders. (B) We also investigate whether individuals join the bandwagon and value the opportunity to be part of a majority, but in our block holder treatment voting behavior as well as bidding behavior is inconsistent with this notion. (C) We argue that experimental subjects might value the right to vote in order to be part of a influential group. Our evidence is consistent only with the third hypothesis, which can explain why the voting premium is high if individuals collectively
influence the outcome, even though their individual probability of affecting decisions may be small.

Some conclusions may be specific to our setup. For example, the bandwagon effect has been documented in the literature in a number of contexts (see Bartels (1988)). Individuals might value being part of a majority under certain circumstances, for example, when they know each other or when they have to identify themselves with a particular group or opinion in public. Investigating these nuances of non-instrumental voting is left for future research.

## References

Baker, Malcolm, Richard S. Ruback, and Jeffrey Wurgler, 2006, Behavioral Corporate Finance, in: Eckbo, Espen B. (editor): Handbook of Corporate Finance, Volume A Empirical Corporate Finance, (Elsevier/North-Holland), chapter 4.
Barclay, Michael J. and Clifford G. Holderness, (1989): Private Benefits from Control of Public Corporations, Journal of Financial Economics, 25, 371-395.
Bartels, L.M. (1988): Presidential Primaries and the Dynamics of Public Choice. Princeton (Princeton University Press).
Battaglini, Marco; Rebecca Morton, and Thomas R. Palfrey, (2006): The Swing Voter's Curse in the Laboratory, CEPR Working Paper
Bergström, Clas, and Kristian Rydqvist, (1992): Differentiated Bids for Voting and Restricted Voting Shares in Public Tender Offers, Journal of Banking and Finance, 16, 97114.

Bigelli, Marco (2004): Dual class stock unifications and shareholders' expropriation, Discussion paper, University of Bologna.
Blais, André, Robert Young and Miriam Lapp (2000): The calculus of voting: an empirical test, European Journal of Political Research, 37, 181-201.
Brennan, Geoffrey, and Alan Hamlin (1998): Expressive voting and electoral equilibrium, Public Choice, 95, 149-175.
Brennan, Geoffrey, and L. Lomasky (1993): Democracy and Decision, Cambridge (Cambridge University Press)
Butler, David, and Donald Stokes, 1969, Political Change in Britain, New York (St. Martins)
Callander, Steven (2006): Bandwagons and momentum in sequential voting. Working Paper, Northwestern University
Coate, Stephen, and Michael Conlin, (2004): A Group Rule-Utilitarian Approach to Voter Turnout: Theory and Evidence, American Economic Review, 94, 1476-1504.
Daske, Stefan, and Olaf Ehrhardt, (2002): Kursunterschiede und Renditen Deutscher Stamm- und Vorzugsaktien, Financial Markets and Portfolio Management, 16, 179-207.
DeAngelo, Harry, and Linda DeAngelo, (1985): Managerial Ownership of Voting Rights A Study of Public Corporations With Dual Classes of Common Stock, Journal of Financial Economics, 14, 33-69.
Dittmann, Ingolf and Niels Ulbricht (2008): Timing and wealth effects of German dualclass stock unifications, European Financial Management forthcoming.

Downs, Anthony, 1957, An Economic Theory of Democracy, New York (Harper)
Duffy, John, and Margit Tavits, (2007): Beliefs and Voting Decisions: A Test of the Pivotal Voter Model, Working Paper, University of Pittsburgh
Dyck, Alexander and Luigi Zingales (2004): Private Benefits of Control: An International Comparison, Journal of Finance, 59, 537-600.
Feddersen, Timothy J., and Alvaro Sandroni, (2006): A Theory of Participation in Elections, American Economic Review, 96, 1271-1282.

Fiorina, Morris P., (1974): Representatives, Roll Calls, and Constituencies, Lexington (Lexington Books)
Fiorina, Morris P., (1976): The Voting Decision: Instrumental and Expressive Aspects, Journal of Politics, 38, 390-413.
Grossman, Sanford J. and Oliver D. Hart (1988): One share - one vote and the market for corporate control, Journal of Financial Economics 20, 175-202.
Guarnaschelli, S.; R. D. McKelvey, and T. R. Palfrey, (2000): An Experimental Study of Jury Decision Rules, American Political Science Review, 94
Güth, Werner, and Hannelore Weck-Hannemann, (1997): Do People Care About Democracy? An Experiment Exploring the Value of Voting Rights, Public Choice, 91, 2747.

Hauser, Shmuel and Beni Lauterbach (2004): The value of voting rights to majority shareholders: Evidence from dual class stock unifications, forthcoming in: Review of Financial Studies.
Horner, Melchior R., (1988): The Value of the Corporate Voting Right: Evidence From Switzerland, Journal of Banking and Finance, 12, 69-83.

Kunz, Roger M. (2002): Simplification of equity capital structure and market value, Financial Markets and Portfolio Management 16, 30-52.
Kunz, Roger M., and James J. Angel, (1996): Factors Affecting the Value of the Stock Voting Right: Evidence From the Swiss Equity Market, Financial Management, 25, 7-20.
Lease, R. C.; J. J. McConnell, and W. H. Mickelson, (1983): The Market Value of Control in Publicly-Traded Corporations, Journal of Financial Economics, 11, 439-471.
Levine, David K., and Thomas R. Palfrey, (2007): The Paradox of Voter Participation? A Laboratory Study, American Political Science Review, 101, 143-158.
Levy, Haim, (1982): Economic Evaluation of Voting Power of Common Stock, Journal of Finance, 38, 79-93.
Maynes, Elizabeth (1996): Takeover rights and the value of restricted shares, Journal of Financial Research 19, 157-173.
McKelvey, Richard D., and Thomas R. Palfrey, (1998): Quantal Response Equilibria for Extensive Form Games, Experimental Economics, 1, 9-41.
——, (1995): Quantal Response Equilibria for Normal Form Games, Games and Economic Behavior, 10, 6-38.
Megginson, William L., (1990): Restricted Voting Stock, Acquisition Premiums, and the Market Value for Corporate Control, Financial Review, 25, 175-198.

Myerson, Roger B., 1998, Extended Poisson Games and The Condorcet Jury Theorem, Games and Economic Behavior 25, pp. 111-131.
Nenova, Tatiana, (2002): The Value of Corporate Votes and Control Benefits: A CrossCountry Analysis, Journal of Financial Economics, 68, 325-351.
Palfrey, Thomas R., and Howard Rosenthal, (1983): A Strategic Calculus of Voting, Public Choice, 41, 7-53.
——, (1985): Voter Participation and Strategic Uncertainty, American Political Science Review, 79, 62-78.

Quattrone, George A., and Amos Tversky, (1984): Causal versus diagnostic contingencies: On self-deception and on the voter's illusion, Journal of Personality and Social Psychology, 46, 237-248.
Riker, William H., and Peter C. Ordeshook, (1968): A Theory of the Calculus of Voting, American Political Science Review, 62, 25-42.
Rydqvist, Kristian (1996): Takeover bids and the relative prices of shares that differ in their voting rights, Journal of Banking and Finance 20, 1407-1425.
Schram, Arthur, (1997): Do People Care About Democracy?: Comment, Public Choice, 91, 49-51.

Schram, Arthur, and Joep Sonnemans, (1996): Voter Turnout as a Participation Game: An Experimental Investigation, International Journal of Game Theory, 25, 385-406.
——, (1996): Why People Vote: Experimental Evidence, Journal of Economic Psychology, 17, 417-442
Schuessler, Alexander A., (2000): Expressive Voting, Rationality and Society, 12, 87-119.
Smith, Brian F., and Ben Amaoko-Adu, (1995): Relative Prices of Dual Class Shares, Journal of Financial and Quantitative Analysis, 30, 223-238.
Tyran, Jean-Robert (2004): Voting when money and morals conflict: an experimental test of expressive voting, Journal of Public Economics, 88, 1645-1664.
Zingales, Luigi, (1994): The Value of the Voting Right: A Study of the Milan Stock Exchange Experience, The Review of Financial Studies, 7, 125-148.

Zingales, Luigi, (1995): What Determines the Value of Corporate Votes?, Quarterly Journal of Economics, 110, 1047-1073.

## Appendix A: Empirical evidence on voting premiums from dual class shares

Many countries allow dual class shares where the inferior class of shares has no or less voting power than the superior class. The price difference between the two classes of shares (the "voting premium") varies widely across countries from $5 \%$ for the U.S. (Lease, McConnell and Mikkelson, 1983) to $82 \%$ for Italy (Zingales, 1994). The theoretical literature (Grossman and Hart, 1988; Bergström and Rydqvist, 1992; Zingales, 1995; Rydqvist, 1996) explains the voting premium with corporate takeovers. They argue that a bidder in a takeover contest will bid more for voting shares (which confer control) than for non-voting shares (which are useless for gaining control). The voting premium is then equal to the future expected difference in the takeover prices of the two types of shares. In many empirical studies, this theory turned out to be successful in explaining the relative size of the voting premium. However, for most countries for which evidence is available, the takeover theory cannot explain the absolute size of the voting premium, because takeovers are too infrequent and takeover premiums are too small.

To substantiate this claim, Table 8 displays some key results of eleven empirical studies on the value of the voting right. The table focuses on those studies that report information on the voting premium and differential tender offers for the same sample. The first three columns describe the analyzed sample. The fourth column displays the ex ante voting premium, i.e. the average relative price difference between voting and non-voting shares. This price difference varies between $5.4 \%$ for the US and $81.5 \%$ for Italy. In addition, the table shows the number of tender offers with differential bids that are reported in these studies, the average premium paid for voting shares relative to non-voting shares in these tender offers, and the ex post voting premium, which is the average tender offer premium multiplied by the number of differential tender offers and divided by the number of firms in the sample. If a shareholder buys one voting share in a randomly selected firm at the beginning of the sample period and holds it over the entire sample period, he on average receives the ex post voting premium compared to an investment into a single non-voting share of the same company. In order to obtain this ex post premium, the shareholder has to pay the ex ante premium when he buys the voting share (instead of the non-voting share) at the beginning of the sample period. Note that the takeover theory does not predict that the
two premiums must be identical, because shareholders might speculate on a differential bid after the end of the sample period. Nevertheless as the length of the sample period increases, the ex post premium should approach the ex ante premium. The table shows that even for the US and the UK, the ex post voting premium is much lower than the ex ante voting premium. In addition, the studies for Sweden, Germany, and Italy, report a large discrepancy between ex ante and ex post voting premium. ${ }^{19}$ Only for Canada, ex ante and ex post voting premiums are of comparable size. Hence, Table 8 suggests that the takeover theory cannot explain the observed ex ante voting premium (except for Canada).

One might try to reconcile the evidence presented in Table 8 with the takeover theory by recognizing that there are events other than tender offers that can terminate the dual class structure. Frequently, dual class firms choose to convert non-voting shares into voting shares in order to simplify their share structure. If non-voting shares are treated unfavorably in such dual class stock unifications, these stock unifications might explain the discrepancy between ex ante and ex post voting premium in Table 8. The empirical evidence shows, however, that this is not the case, at least for the U.S., Israel, Germany, Switzerland, and Italy. On the contrary, non-voting shares are typically converted one-to-one into voting shares without any compensation to voting shareholders. In those cases, in which voting shareholders receive a compensation, the compensation is considerably lower than the previous voting premium. Hence, compared to the ex ante voting premium, non-voting shares clearly benefit from dual class stock unifications. ${ }^{20}$ Only for the U.K., there is evidence that voting shareholders receive a compensation in dual class stock unifications that justifies the observed ex ante voting premium (see Ang and Megginson, 1989). Other differences between the two types of shares, like liquidity or different dividend rights, do not help either, because they often work in the opposite direction: Nonvoting shares often pay more dividends and are more liquid than voting shares. To sum up, the theory can explain the size of the ex ante voting premium for Canada and the U.K. For the U.S., Israel,

[^13]Germany, Switzerland, and Italy, however, a large part of the voting premium cannot be attributed to takeovers or stock unifications.

There is also more direct evidence that the takeover hypothesis cannot be the whole story. Maynes (1996) analyzes 46 Canadian dual class firms, 19 of which have a so-called "participation coattail", i.e. a company by-law which states that, in case of a takeover bid, the holders of restricted voting shares have the right to convert their shares one-to-one into superior voting shares and tender them to the bidder. This by-law effectively prevents tender offers with differential bids. Consequently, the takeover theory predicts that the voting premium should be zero for firms with such a participation coattail. Maynes (1996) finds however that the voting premium is still 5.5 percent for firms with participation coattail compared to 8.2 percent for firms without coattail provision. Altogether, the empirical literature shows clearly that the existing theory cannot fully explain the observed size of the voting premium for many countries.

## Appendix B: Instructions for the base treatment

Welcome! This is an experiment in behavioral economics. You and the other participants in the experiment will take part in a situation where you have to make a decision. In this situation, you can earn money that will be paid to you in cash at the end of the experiment. How much you will earn depends on the decisions that you and the other participants in the experiment make.

These instructions describe the situation where you have to make a decision and they are identical for all participants in the experiment. It is important that you read the instructions carefully so that you understand the decision-making problem well. If something seems unclear to you while reading, or if you have other questions, please let us know by raising your hand. We will then answer your questions individually.

Please do not, under any circumstances, ask your question(s) aloud. You are not permitted to give information of any kind to other participants.

You are also not permitted to speak to other participants at any time throughout the experiment. Whenever you have a question, please raise your hand and we will come to you and answer it. If you break these rules, we may be compelled to terminate the experiment.

Once everyone has read the instructions and there are no further questions, we will conduct a short quiz where each of you will complete two short tasks on your own. We will walk around, look over your answers, and solve comprehension problems. The quiz serves solely to ensure that you thoroughly understand the crucial details of the decision-making problem.

Of course, your anonymity and the anonymity of the other participants will be guaranteed throughout the entire experiment. You will not find out the true identity of the other participants, nor will they find out your identity.

## 1. General

The experiment consists of several rounds in which decisions must be made and information must be processed. Through your decisions, you can earn points. These points represent your income and will be converted into euros at the end of the experiment and paid out in cash.
The exact sequence of the experiment, the different decisions, and the payment modalities will be explained in detail in the following.
2. The distribution of roles

You will find yourself in a situation where you have to make decisions. This situation will be repeated for 30 rounds. This situation can be compared to a simple stock market. On this stock market, there is one single company issuing shares. You can buy shares of this company and thus take on the role of shareholder. The amount of dividends paid out on the shares depends on how good or bad the manager of the company is.

Chance plays an important role here: it decides whether the manager of the company is good or bad. The computer takes on the roles of company, manager, and chance.
3. Two possible stock market conditions

At the beginning of each round, the computer generates the quality of the manager randomly. You can imagine it as if the computer were to pick a ball blind out of a hat that contains five balls inscribed with the
words "good manager" and another five inscribed with the words "bad manager." Neither you nor any of the other participants know the quality of the manager. You only know the following: there is a $50 \%$ probability of a good manager, and a $50 \%$ probability of a bad manager.

The quality of the manager influences the probability that the company will make a profit. First, we will look at the situation that arises in the case of a good manager.

## 4. The stock market condition in the (unobservable) case of a good manager

If the manager is good (which neither you nor any of the others can know), there is an $80 \%$ probability that the company will make a profit. Thus, you can imagine the situation with a good manager as if the computer were to pick a ball blind out of a hat containing eight balls inscribed with the words "profit", and two balls inscribed with the words "no profit." For you, the question of whether the company makes a profit is only important in relation to the dividends on shares.

If the company makes a profit, the dividends on shares amount to 20 points per share. If, however, the company does not make a profit, the dividends amount to 0 points per share.

Now we will look at the situation in the (also unobservable) case of a bad manager.
5. The stock market condition in the (also unobservable) case of a bad manager

If the manager is bad, there is a $20 \%$ probability that the company will make a profit. The case of a bad manager can thus be conceived as if the computer were to pick a ball blind out of a hat, in which there are two balls inscribed with the word "profit" and eight inscribed with "no profit." For you, the question of whether the company makes a profit or not is only important in relation to the dividends on shares.

If the company makes a profit, the dividends paid out amount to 20 points per share, as above. If the company does not make a profit, however, the dividends amount to 0 points per share, as above.

Obviously, a dividend of 20 points per share is more likely if the manager is good. Conversely, a dividend of 0 points per share is more likely if the manager is bad.

Please keep in mind that the quality of the manager is unknown to all participants and that there is an equal probability of both possible qualities at the beginning of each round.

## 6. The auctioning of shares

There are two kinds of shares: type A shares and type B shares. The next section will explain the difference between them. The dividends are the same for both types.

Per round there are five type A shares and five type B shares.
Apart from you, there are seven other people who can buy shares of the company: namely, the other participants in the experiment. Thus, there are a total of eight people on the market who can bid for shares. All of these people are subject to the same rules. These rules will be explained to you in the following.

You can buy a maximum of one share of each type per round. In total, therefore, you can buy a maximum of two shares per round: one type A share and one type B share.

You can attempt to buy the shares of your choice by taking part in two simultaneous auctions. In the one auction, type A shares are sold, and in the other, type B shares are sold.

You will be asked to make a bid for each share type. In each of the two auctions, the following rule applies: the five participants in the experiment who submit the five highest bids for the type of shares offered in that
auction will each receive one share of that type. The price they will each pay for their share will be the amount of the sixth-highest bid in that auction. (If two or more bids in one auction are identical, the computer will randomly determine their order.) Those participants who made the sixth-to-eighth-highest bids will not receive any share of the type offered and also will not pay anything in this auction.

The most sensible thing you can do in both of these auctions is to submit a bid that corresponds to your true appraisal of the share in question, in other words, the maximum amount you would be willing to pay for it.

After everyone has placed their bids in the two simultaneous auctions, each of you will be informed of the price of the type A and type B shares, and of the dividends per share (which is the same for both share types). You will always be given this information, no matter whether you have purchased shares or not.

Furthermore, each of you will be told which share, if any, you have acquired. You will not receive any information on which shares, if any, others have acquired.

The auction winners will then receive the five type A shares and the five type B shares. If you have purchased at least one share, your interim earnings will amount to, in points:

The dividends on the shares you purchased, multiplied by the number of shares you purchased, minus the price(s) you had to pay.
You can also have negative earnings.
If you did not acquire a share, your interim earnings amount to zero.
You (and only you) will be told your interim earnings.
In the next section, the difference between $A$ shares and $B$ shares will be described.

## 7. The share types

When you purchase a type A share, you attain the right to participate in a vote. You do not attain such a right with type B shares, however.

All five participants who have purchased a type A share take part in a vote whose outcome decides whether the company manager will be retained or not. This vote takes place after all share purchases have been made and after you have been told your interim earnings from that round. At this point in time, therefore, you know whether the shares had dividends of 0 or 20 points.

If the majority of the participants who have a type A share are in favor of keeping the same manager, she will be retained. Retaining the same manager means that the computer does not again randomly generate the quality of the manager. If retained, the manager has the same quality as before the vote.

If the majority of participants who have a type A share vote to fire the manager, she will be fired and a new manager will be hired. Firing means that the computer will again randomly generate the quality of the new manager. This will again entail a $50 \%$ probability that the new manager will be good and a $50 \%$ probability that the new manager will be bad.

## 8. The second dividend payout on shares

After the vote on the manager, the company will again become active on the market, either with the old or a new manager depending on the outcome of the vote.

Depending on the quality of the manager and the corresponding probability of the company's success, the computer again determines the dividends on the shares. The dividends again amount to 20 points in the case
that the company is successful and 0 points in the case that the company is unsuccessful. As before, the probability of earning 20 points is higher when the manager is good (namely, $80 \%$ for a good manager in comparison to $20 \%$ for a bad manager).

You will then be told your final dividends from that round. In the next round, the situation will be repeated with a new manager. All rounds have the same structure.

## 9. Your finances

At the beginning of the experiment, you receive an initial budget of 150 points. You will also be paid a fixed amount of 16 points each round, in addition to your profits (or losses) in that round. Your final payout consists of the sum of the payouts from all rounds. Furthermore, you receive three euros if you arrive 10 minutes before the beginning of the experiment. The exchange rate used to convert points into cents is the following:

1 point $=3$ cents

## 10. The entire procedure of one round in overview

1. The manager's ability is determined randomly but not disclosed. The auctions for type A shares and type B shares take place.
2. All participants are informed of the prices and dividends of the shares. Furthermore, each of you is informed individually which share(s) you have acquired.
3. The dividends of 0 or 20 points per share are announced. You are told your interim earnings from that round.
4. The vote on retaining or firing the manager takes place among all holders of type A shares. Depending on the results of the vote, either the same manager is retained or a new manager is hired.
5. The result of the vote is announced to all participants.
6. The second dividend payout of 0 or 20 points per share is announced. You receive the total payout in this round, which comprises the following items: if you did not purchase any shares, you are only paid the fixed amount of 16 points in this round. If you purchased one or two shares, your profits from this round comprise the dividends on the shares that you own, minus the price(s) you had to pay for these share(s), plus the fixed payment of 16 points.

This procedure is repeated 30 times.
After the end of the thirtieth round, you fill out another questionnaire containing questions on your behavior during the experiment. After everyone has completed the questionnaire, you will be told your total profits. You will not be told anything about the total profits of the other participants.

Please remain seated and wait quietly until we come to you and pay out your total earnings in cash. Please do not talk to the other participants. After your total earnings have been paid out, please leave the room quietly.

If there was anything you did not understand, please let us know by raising your hand. We will answer your questions on an individual basis.

Thank you for participating!

## Appendix C: Proof of Proposition 1

Denote by $\Pi^{i}$ the profits of investor $i$ and by $\alpha^{i}, \beta^{i}$ the probability that the $i^{\text {th }}$ investor obtains an A-share, respectively, a B-share in the auction. We denote bids by $B_{A}^{i}$ and $B_{B}^{i}$ and equilibrium prices by $P_{A}$ and $P_{B}$. Then equilibrium profits for each investor can be written as:

$$
\begin{equation*}
\Pi^{i}=\alpha^{i}\left(V+\omega-P_{A}\right)+\beta^{i}\left(V+\alpha^{i} \omega-P_{B}\right) . \tag{12}
\end{equation*}
$$

## Part 1: Non-existence of symmetric pure strategy equilibria.

We prove this part by contradiction. Hence, assume that a symmetric pure strategy equilibrium exists where each investor bids the equilibrium prices $P_{A}$ and $P_{B}$. Then each investor is rationed in equilibrium, and $\alpha=\beta=M / N$. Also, it must be the case that $\partial \Pi / \partial \alpha=\partial \Pi / \partial \beta=0$. If $\partial \Pi / \partial \alpha<0(\partial \Pi / \partial \alpha>0)$, then the investor has an incentive to reduce (increase) his bid for the A-share, and analogously for the B-share. We therefore obtain the following prices for the conjectured equilibrium from (12):

$$
\begin{align*}
& \frac{\partial \Pi}{\partial \alpha}=0 \Rightarrow P_{A}=V+\left(1+\frac{M}{N}\right) \omega  \tag{13}\\
& \frac{\partial \Pi}{\partial \beta}=0 \Rightarrow P_{B}=V+\frac{M}{N} \omega
\end{align*}
$$

For any other set of prices each investor would have an incentive to deviate from the conjectured equilibrium strategy. However, with these prices we obtain $\Pi=-(M / N)^{2} \omega<0$. Hence, all investors would make negative profits. However, this cannot be the case because each investor has the option not to bid in the auction and receive zero profits.
Part 2: Existence of asymmetric pure strategy equilibria.
Denote by $\varepsilon>0$ the smallest increment by which investors can increase their bids. We now construct an asymmetric pure strategy equilibrium as follows.

$$
\begin{align*}
B_{A}^{i} & =V+(1+\gamma) \omega, \quad i=M+1 \ldots N, \\
B_{A}^{i} & =V+(1+\gamma) \omega+\varepsilon, \quad i=1 \ldots M, \\
B_{B}^{i} & =V+(1-\gamma) \omega, \quad i=M+1 \ldots N,  \tag{14}\\
B_{B}^{i} & =V+(1-\gamma) \omega+\varepsilon, \quad i=1 \ldots M,
\end{align*}
$$

where: $0 \leq \gamma \leq 1$.
The parameter $\gamma$ describes how the valuation premium for the B -share is allocated between the price for B -shares and the price for A -shares. Then $\alpha^{i}=\beta^{i}=1$ for the $M$ highest bidders, $i=1 \ldots M$, who win all the shares in equilibrium. $\alpha^{i}=\beta^{i}=0$ for the $M-N$ other bidders,
$i=M+1 \ldots N$, who never win a share in any auction. The profits of the winners in the auction are then:

$$
\begin{equation*}
\Pi=V+\omega-(V+(1+\gamma) \omega)+V+\omega-(V+(1-\gamma) \omega)=0 \tag{15}
\end{equation*}
$$

The losers in the auctions also make zero profits. The profits of a winner who would deviate by reducing his bid below the stipulated equilibrium price in one of the auctions (and without changing the strategy in the other auction) would be:

$$
\begin{align*}
& \Pi^{\text {Winner }}\left(\operatorname{bid}<B_{B}^{M+1}\right)=V+\omega-(V+(1+\gamma) \omega)=-\gamma \omega \leq 0 \\
& \Pi^{\text {Winner }}\left(\operatorname{bid}<B_{A}^{M+1}\right)=V-(V+(1-\gamma) \omega)=-(1-\gamma) \omega \leq 0 \tag{16}
\end{align*}
$$

Bidding lower in both auctions results in profits of zero. If winners increase their bids above those in (14) has no consequence unless one of the losing bidders also increases their price, in which case they would then overpay. Hence, bidding higher is a weakly dominated strategy. The auction losers could bid higher in one or both auctions. In order to win they would have to increase their bids at least to $B_{A}^{M}$ and $B_{B}^{M}$ (then they would be rationed) or by an increment $\varepsilon$ higher to win with probability one. The payoffs from bidding $B_{A}^{M}$ and $B_{B}^{M}$ are (note that $\varepsilon, \alpha$, and $\beta$ are all strictly positive):

$$
\begin{align*}
\Pi\left(\operatorname{bid} B_{A}^{M} \text { for } \mathrm{A}\right) & =\alpha^{i}(V+\omega-(V+(1+\gamma) \omega+\varepsilon)) \\
& =-\alpha^{i}(\gamma \omega+\varepsilon)<0 \\
\Pi\left(\operatorname{bid} B_{B}^{M} \text { for } \mathrm{B}\right)= & \beta^{i}(V-(V+(1-\gamma) \omega+\varepsilon))=-\beta^{i}((1-\gamma) \omega+\varepsilon)<0 \\
\Pi\left(\operatorname{bid} B_{A}^{M} \text { and } B_{B}^{M}\right)= & \alpha^{i}(V+\omega-(V+(1+\gamma) \omega+\varepsilon))  \tag{17}\\
& +\beta^{i}\left(V+\alpha^{i} \omega-(V+(1-\gamma) \omega+\varepsilon)\right) \\
& =-\alpha^{i}(\gamma \omega+\varepsilon)-\beta^{i}\left(\left(1-\gamma-\alpha^{i}\right) \omega+\varepsilon\right)<0
\end{align*}
$$

Bidding above $B_{A}^{M}$ and $B_{B}^{M}$ increases the probabilities of winning to one and generates even lower payoffs. Hence, the auction losers have no incentive to deviate by bidding higher for either the A-share, or the B-share, or both. Then the voting premium is

$$
\begin{equation*}
P_{A}-P_{B}=B_{A}^{M+1}-B_{B}^{M+1}=2 \gamma \omega \tag{18}
\end{equation*}
$$

Since $\gamma$ can be any number in the unit interval, $0 \leq P_{A}-P_{B} \leq 2 \omega$.

## Figures

Figure 1: Incorrect votes and prices over time
The left figure shows the frequency $\tau$ of wrong votes conditional on the observed first dividend $D_{1}$. The right figure shows the average price of voting and non-voting shares. The 30 rounds of the sessions are aggregated into blocks of 5 , so block 5 contains rounds 1 to 5 , block 2 contains rounds 6 to 10 , and analogously for blocks 3 to 6 .



## Tables

## Table 1: Overview over the different treatments

This table shows the two defining parameters for each treatment, i.e. the probability $p$ that the dividend is high (low) when the manager is good (bad) and the number of shares held by a block holder that are always voted in favor of the manager. In addition, the table shows the utility $\Delta U$ from equation (8) that is at stake in the vote, the Nash value of the shares, $V_{\text {Nash }}$, from equation (4), the number of sessions, the number of rounds per session, and the number of subjects per session.

| Treatment | Link $\boldsymbol{p}$ <br> between skill <br> and dividend | Shares <br> held by <br> block <br> holder | $\Delta \boldsymbol{U}$ | $\boldsymbol{V}_{\text {Nash }}$ | Sessions | Rounds <br> per <br> session | Subjects <br> per <br> session |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Base treatment (BASE) | $80 \%$ | 0 | 3.6 | 21.8 | 10 | 30 | 8 |
| No uncertainty (NU) | $100 \%$ | 0 | 10.0 | 25.0 | 10 | 30 | 8 |
| Non-influential manager (NI) | $50 \%$ | 0 | 0.0 | 20.0 | 10 | 30 | 8 |
| Block holder (BH) | $80 \%$ | 6 | 0.0 | 20.0 | 10 | 30 | 8 |

## Table 2: Prices in the Base Treatment (BASE)

This table contains statistics on four variables for the base treatment: the price of voting A-shares, the price of non-voting B-shares, the difference between these two prices (the premium), and the premium scaled by the Nash value (from Table 1) of the shares (the relative premium). The table shows mean, median, standard deviation, and the p-values of two tests, the t -test for zero mean and the Wilcoxon signed rank test for zero median. For the prices of voting and non-voting shares, the table also shows the mean difference between the price and the Nash value, and the p-value of the $t$-test for this difference being zero. In Panel A, we first calculate one value of the respective variable for each session by averaging the variable across the last 15 rounds of the session. In the second step, we calculate the statistics across the 10 sessions. Panel B shows the results for the pooled sample of all sessions and rounds.

Panel A: Average of last $\mathbf{1 5}$ rounds

| Variable | Obs. | Mean | Median | Standard <br> deviation | T-test <br> p-value | Wilcoxon <br> p-value | Difference to Nash |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Mean | T-test <br> p-value |  |  |  |  |  |  |  |
| Voting A-share | 10 | 18.52 | 18.27 | 4.65 | 0.000 | 0.002 | 3.28 | 0.053 |
| Non-voting B-share | 10 | 15.61 | 17.37 | 5.41 | 0.000 | 0.002 | 6.19 | 0.006 |
| Premium | 10 | 2.91 | 2.63 | 2.50 | 0.005 | 0.004 |  |  |
| Relative premium | 10 | $13.35 \%$ | $12.08 \%$ | $11.49 \%$ | 0.005 | 0.004 |  |  |

Panel B: All rounds

| Variable | Obs. | Mean | Median | Standard <br> deviation | T-test <br> p-value | Wilcoxon <br> p-value | Difference to Nash |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  |  |  |  |  |  | Mean | T-test <br> p-value |  |
| Voting A-share | 300 | 17.41 | 18.00 | 4.63 | 0.000 | 0.000 | 4.39 | 0.000 |
| Non-voting B-share | 300 | 14.60 | 15.76 | 5.30 | 0.000 | 0.000 | 7.20 | 0.000 |
| Premium | 300 | 2.82 | 2.00 | 3.31 | 0.000 | 0.000 |  |  |
| Relative premium | 300 | $12.92 \%$ | $9.17 \%$ | $15.20 \%$ | 0.000 | 0.000 |  |  |

## Table 3: Offers in the Base Treatment (BASE)

This table contains statistics on four variables for the base treatment: the offer for voting A-shares, the offer for non-voting B-shares, the difference between these two offers (the premium), and the premium scaled by the Nash value (from Table 1) of the shares (the relative premium). The table shows mean, median, standard deviation, and the p-values of two tests, the t-test for zero mean and the Wilcoxon signed rank test for zero median. For the the premium, the table also shows the frequencies that the premium is negative or, respectively, positive. In Panel A, we first calculate one value of the respective variable for each subject by averaging the variable across the last 15 rounds. In the second step, we calculate the statistics across the 80 subjects. Panel B shows the results for the pooled sample of all subjects and rounds.

Panel A: Average of last $\mathbf{1 5}$ rounds

| Variable | Obs. | Mean | Median | Standard <br> deviation | T-test <br> p-value | Wilcoxon <br> p-value | Frequency |  |
| :--- | :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  |  |  |  | negative | positive |  |  |  |
| Voting A-share | 80 | 29.41 | 20.17 | 37.81 | 0.000 | 0.000 |  |  |
| Non-voting B-share | 80 | 23.95 | 18.40 | 33.58 | 0.000 | 0.000 |  |  |
| Premium | 80 | 5.46 | 1.67 | 13.91 | 0.001 | 0.000 | $16.3 \%$ | $70.0 \%$ |
| Relative premium | 80 | $25.05 \%$ | $7.65 \%$ | $63.81 \%$ | 0.001 | 0.000 |  |  |

Panel B: All rounds

| Variable | Obs. | Mean | Median | Standard <br> deviation | T-test <br> p-value | Wilcoxon <br> p-value | Frequency |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  |  |  |  | negative | positive |  |  |  |
| Voting A-share | 2,400 | 27.76 | 20.00 | 36.43 | 0.000 | 0.000 |  |  |
| Non-voting B-share | 2,400 | 22.65 | 18.00 | 32.18 | 0.000 | 0.000 |  |  |
| Premium | 2,400 | 5.11 | 1.00 | 17.39 | 0.000 | 0.000 | $10.8 \%$ | $53.8 \%$ |
| Relative premium | 2,400 | $23.42 \%$ | $4.59 \%$ | $79.77 \%$ | 0.000 | 0.000 |  |  |

## Table 4: Voting behavior

This table describes the voting outcomes for all four treatments. Panel A shows for each treatment (1) the frequency $\tau_{L}$ that A-shareholders vote for keeping the manager after a low dividend, (2) the frequency $e_{L}$ that a manager is actually kept after a low dividend (from equation (5)), (3) the frequency $\tau_{H}$ that A-shareholders vote for replacing the manager after a high dividend, and (4) the frequency $e_{H}$ that a manager is actually replaced after a high dividend (from equation (6)). In addition, the table shows the p -value of the $\chi^{2}$-test and the Wilcoxon signed rank test that $\tau_{L}$ equals $\tau_{H}$. The $\chi^{2}$-test assumes that every vote cast is an independent observation. The Wilcoxon test allows for dependence within a group. Here we calculate for each group the difference between the percentage of wrong votes after a high dividend and the percentage of wrong votes after a low dividend and apply the Wilcoxon test to these 10 differences per treatment. Panel B displays the Nash value of the shares, $V_{\text {Nash }}$, from equation (4), the Quantal Response Equilibrium value, $V_{Q R E}$, when the empirical error probabilities are taken into account (from equations (5) to (7)), the maximum voting premium $2 \omega$ from Proposition 1 and equation (11), the observed voting premium and the p-values of the Wilcoxon signed rank test that the observed voting premium differs from, respectively, zero and the maximum voting premium $2 \omega$. Panel C shows for the treatments BASE and NU the responsiveness coefficients $\lambda_{L}$ and $\lambda_{H}$ calculated from $\tau_{L}$ and, respectively, $\tau_{H}$ as shown in equation (10). This panel also displays the p -values of three tests that, respectively, $\lambda_{L}=\lambda_{H}$, that the $\lambda_{L}$ are identical in the two treatments, and that the $\lambda_{H}$ are identical in the two treatments. For these tests, we first calculate the $\lambda$ 's for each session and then test for equal location of the $\lambda$ 's between the two groups with a two-sample Wilcoxon signed rank test.

## Panel A: Individual and collective errors

| Treatment | $\boldsymbol{\tau}_{\boldsymbol{L}}$ | $\boldsymbol{e}_{\boldsymbol{L}}$ | $\boldsymbol{\tau}_{\boldsymbol{H}}$ | $\mathbf{e}_{\boldsymbol{H}}$ | P-value for $\boldsymbol{\tau}_{\boldsymbol{L}}=\boldsymbol{\tau}_{\boldsymbol{H}}$ |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | $3.03 \%$ | $\chi^{2}$ |
| Base treatment (BASE) | $11.03 \%$ | $0.00 \%$ | $10.56 \%$ | $1.39 \%$ | 0.836 | 0.148 |
| No uncertainty (NU) | $56.32 \%$ | $64.47 \%$ | $21.89 \%$ | $8.11 \%$ | 0.000 | 0.625 |
| Non-influential manager (NI) | 51.010 |  |  |  |  |  |
| Block holder (BH) | $31.16 \%$ | $15.12 \%$ | $23.75 \%$ | $7.81 \%$ | 0.025 | 0.742 |

Panel B: Valuation

| Treatment | $\boldsymbol{V}_{\text {Nash }}$ | $\boldsymbol{V}_{\boldsymbol{Q R E}}$ | Voting Premium |  | Wilcoxon p-value: Voting <br> premium different from |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Max $=\mathbf{2 \omega}$ |  | Observed | Zero |
| Base treatment (BASE) | 21.80 | 21.69 | 0.116 | 2.911 | 0.004 | 0.014 |
| No uncertainty (NU) | 25.00 | 24.89 | 0.120 | 3.993 | 0.002 | 0.006 |
| Non-influential manager (NI) | 20.00 | 20.00 | 0.000 | 0.403 | 0.158 | 0.004 |
| Block holder (BH) | 20.00 | 20.00 | 0.000 | 0.293 | 0.219 | 0.002 |

Panel C: Responsiveness

| Treatment | $\lambda_{L}$ | $\lambda_{H}$ | Wilcoxon p-value for |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\lambda_{L}=\lambda_{H}$ | $\lambda_{L}^{N U}=\lambda_{L}^{\text {BASE }}$ | $\lambda_{H}^{\text {NU }}=\lambda_{H}^{\text {BASE }}$ |
| Base treatment (BASE) | 3.09 | 8.57 | 0.255 | 0.710 | 0.940 |
| No uncertainty (NU) | 3.62 | 4.00 | 0.547 |  |  |

## Table 5: Prices and Offers in the No Uncertainty treatment (NU)

This table describes prices (Panel A) and offers (Panel B) for the No Uncertainty (NU) treatment. Panel A shows statistics on the price of voting A-shares, the price of non-voting B-shares, the difference between these two prices (the premium), and the premium scaled by the Nash value (from Table 1) of the shares (the relative premium). The table shows mean, median, standard deviation, and the p-values of two tests, the t test for zero mean and the Wilcoxon signed rank test for zero median. In addition it shows the p-values of the two-sample t-test and the two-sample Wilcoxon signed rank test that the location of the distribution is identical under the NU and the BASE treatment. We first calculate one value of the respective variable for each session by averaging the variable across the last 15 rounds of the session. In the second step, we calculate the statistics across the 10 sessions. Panel B displays the same statistics for individual offers.

## Panel A: Average prices of the last 15 rounds

| Variable | Obs. | Mean | Median | Standard <br> deviation | T-test <br> p-value | Wilcoxon <br> p-value |  | P-value two-sample <br> comparison with BASE |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| Voting A-share | 10 | 20.90 | 20.77 |  | 4.37 | 0.000 | 0.002 | 0.254 |  |
| Non-voting B-share | 10 | 16.91 | 17.37 | 2.96 | 0.000 | 0.002 | 0.518 | 0.303 |  |
| Premium | 10 | 3.99 | 3.13 | 3.27 | 0.004 | 0.002 | 0.417 | 0.396 |  |
| Relative premium | 10 | $15.97 \%$ | $12.53 \%$ | $13.07 \%$ | 0.004 | 0.002 | 0.640 | 0.682 |  |

Panel B: Average offers of last 15 rounds

| Variable | Obs. | Mean | Median | Standard <br> deviation | T-test <br> p-value | Wilcoxon <br> p-value |  | P-value two-sample <br> comparison with BASE |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Voting A-share | 80 | 25.89 | 22.70 |  | 17.21 | 0.000 | 0.000 | 0.450 | 0.203 |
| Non-voting B-share | 80 | 22.16 | 19.77 | 13.23 | 0.000 | 0.000 | 0.659 | 0.127 |  |
| Premium | 80 | 3.72 | 1.53 | 17.42 | 0.060 | 0.000 | 0.487 | 0.766 |  |
| Relative premium | 80 | $14.90 \%$ | $6.13 \%$ | $69.69 \%$ | 0.060 | 0.000 | 0.338 | 0.567 |  |

Table 6: Prices and Offers in the Non-influential manager treatment (NI)
This table describes prices (Panel A) and offers (Panel B) for the Non-influential Manager (NI) treatment. Panel A shows statistics on the price of voting A-shares, the price of non-voting B-shares, the difference between these two prices (the premium), and the premium scaled by the Nash value (from Table 1) of the shares (the relative premium). The table shows mean, median, standard deviation, and the p -values of two tests, the t -test for zero mean and the Wilcoxon signed rank test for zero median. In addition it shows the p-values of the two-sample t-test and the two-sample Wilcoxon signed rank test for two hypotheses: (1) that the location of the distribution is identical under the NI and the BASE treatment and (2) that the location of the distribution is identical under the NI and the NU treatment. We first calculate one value of the respective variable for each session by averaging the variable across the last 15 rounds of the session. In the second step, we calculate the statistics across the 10 sessions. Panel B displays the same statistics for individual offers.

Panel A: Average prices of the last $\mathbf{1 5}$ rounds

| Variable | Obs. | Mean | Median | Standard deviation | T-test p-value | Wilcoxon p-value | P-value two-sample comparison with BASE |  | P-value two-sample comparison with NU |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | T-test | Wilcoxon | T-test | Wilcoxon |
| Voting A-share | 10 | 16.38 | 17.03 | 2.63 | 0.000 | 0.002 | 0.225 | 0.178 | 0.014 | 0.028 |
| Non-voting B-share | 10 | 15.98 | 16.47 | 2.72 | 0.000 | 0.002 | 0.851 | 0.577 | 0.475 | 0.437 |
| Premium | 10 | 0.40 | 0.28 | 0.67 | 0.089 | 0.158 | 0.012 | 0.028 | 0.007 | 0.005 |
| Relative premium | 10 | 2.01\% | 1.40\% | 3.34\% | 0.089 | 0.158 | 0.013 | 0.032 | 0.008 | 0.006 |

Panel B: Average offers of the last 15 rounds

| Variable | Obs. | Mean | Median | Standard <br> deviation | T-test <br> p-value | Wilcoxon <br> p-value |  | P-value two-sample <br> comparison with BASE |  | P-value two-sample <br> comparison with NU |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Voting A-share | 80 | 19.45 | 18.10 |  | 9.09 | 0.000 | 0.000 | 0.024 | 0.010 | 0.004 |
| Non-voting B-share | 80 | 18.55 | 18.07 | 7.51 | 0.000 | 0.000 | 0.164 | 0.529 | 0.035 | 0.000 |
| Premium | 80 | 0.91 | 0.07 | 4.26 | 0.060 | 0.000 | 0.006 | 0.001 | 0.164 | 0.005 |
| Relative premium | 80 | $4.54 \%$ | $0.33 \%$ | $21.30 \%$ | 0.060 | 0.000 | 0.008 | 0.001 | 0.207 | 0.009 |

## Table 7: Prices and Offers in the Block holder treatment (BH)

This table describes prices (Panel A) and offers (Panel B) for the Block holder (BH) treatment. Panel A shows statistics on the price of voting A-shares, the price of nonvoting B-shares, the difference between these two prices (the premium), and the premium scaled by the Nash value (from Table 1) of the shares (the relative premium). The table shows mean, median, standard deviation, and the p-values of two tests, the $t$-test for zero mean and the Wilcoxon signed rank test for zero median. In addition it shows the p-values of the two-sample t-test and the two-sample Wilcoxon signed rank test for two hypotheses: (1) that the location of the distribution is identical under the BH and the BASE treatment and (2) that the location of the distribution is identical under the BH and the NU treatment. We first calculate one value of the respective variable for each session by averaging the variable across the last 15 rounds of the session. In the second step, we calculate the statistics across the 10 sessions. Panel B displays the same statistics for individual offers.

Panel A: Average prices of the last 15 rounds

| Variable | Obs. | Mean | Median | Standard deviation | $\begin{gathered} \text { T-test } \\ \text { p-value } \end{gathered}$ | Wilcoxon p-value | P-value two-sample comparison with BASE |  | P-value two-sample comparison with NU |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | T-test | Wilcoxon | T-test | Wilcoxon |
| Voting A-share | 10 | 13.14 | 12.97 | 4.08 | 0.000 | 0.002 | 0.013 | 0.041 | 0.001 | 0.005 |
| Non-voting B-share | 10 | 12.85 | 12.73 | 4.02 | 0.000 | 0.002 | 0.212 | 0.138 | 0.020 | 0.048 |
| Premium | 10 | 0.29 | 0.33 | 0.93 | 0.346 | 0.219 | 0.010 | 0.051 | 0.006 | 0.005 |
| Relative premium | 10 | 1.47\% | 1.67\% | 4.67\% | 0.346 | 0.219 | 0.011 | 0.060 | 0.007 | 0.006 |

Panel B: Average offers of the last 15 rounds

| Variable | Obs. | Mean | Median | Standard <br> deviation | T-test <br> p-value | Wilcoxon <br> p-value |  | P-value two-sample <br> comparison with BASE |  | P-value two-sample <br> comparison with NU |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Voting A-share | 80 | 24.96 | 15.20 |  | 0.000 | 0.000 | 0.454 | 0.000 | 0.840 | 0.000 |
| Non-voting B-share | 80 | 22.56 | 15.00 | 29.45 | 0.000 | 0.000 | 0.781 | 0.014 | 0.913 | 0.000 |
| Premium | 80 | 2.40 | 0.00 | 16.70 | 0.203 | 0.185 | 0.209 | 0.001 | 0.624 | 0.003 |
| Relative premium | 80 | $11.99 \%$ | $0.00 \%$ | $83.48 \%$ | 0.203 | 0.185 | 0.268 | 0.001 | 0.811 | 0.006 |

Table 8: Empirical literature on differential tender offers and the voting premium
This table summarizes 11 empirical papers that include information on the voting premium and on the frequency of tender offers with differential bids. For each line, all numbers refer to a single dataset, so that ex ante and ex post voting premiums can be directly compared. The ex ante voting premium is the average relative price difference between voting and non-voting shares (or superior and inferior-voting shares), i.e. ( $\left.P^{v}-P^{n v}\right) / P^{n v}$. The average tender offer premium is $\left(T O^{v}-T O^{n \nu}\right) / T O^{n v}$, where $T O^{v}$ is the tender offer (in money or stock) on voting shares and $T O^{n v}$ on non-voting shares. The ex post voting premium is the average tender offer premium multiplied by the number of differential tender offers and divided by the number of firms in the sample.

| Country | Sample period | Number of firms in the sample | Ex ante voting premium | Number of differential tender offers | Average tender offer premium | Ex post voting premium | Source |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| USA | 1940-1978 | 26 | 5.4\% | 0 | N/A | 0\% | Lease, McConnell and Mikkelson (1983) |
| USA | 1984-1990 | 94 | 10.5\% | 2 | 81.5\% | 1.7\% | Zingales (1995) |
| USA | 1960-1980 | 144 | N/A | 4 | 130.9\% | 3.6\% | DeAngelo and DeAngelo (1985) |
| UK | 1955-1982 | 152 | 13.3\% | 37 | 32.1\% | 7.8\% | Megginson (1990) |
| Canada | 1981-1992 | 98 | 10.4\% | 20 | 57.2\% | 11.7\% | Smith and Amoako-Adu (1995) |
| Israel | 1981 | 25 | 45.5\% | N/A | N/A | N/A | Levy (1982) |
| Sweden | 1980-1990 | 65 | 15.2\% | 9 | 27\% | 3.7\% | Bergström and Rydqvist (1992) |
| Germany | 1956-1998 | 101 | 17.2\% | 3 | 20.6\% | 0.6\% | Daske and Ehrhardt (2002) and own research |
| Switzerland | 1973-1983 | 45 | 22.4\% | N/A | N/A | N/A | Horner (1988) |
| Switzerland | 1990-1991 | 29 | 18\% | N/A | N/A | N/A | Kunz and Angel (1996) |
| Italy | 1987-1990 | 96 | 81.5\% | 0 | N/A | 0\% | Zingales (1994) |

## SFB 649 Discussion Paper Series 2007

For a complete list of Discussion Papers published by the SFB 649, please visit http://sfb649.wiwi.hu-berlin.de.

001 "Trade Liberalisation, Process and Product Innovation, and Relative Skill Demand" by Sebastian Braun, January 2007.
002 "Robust Risk Management. Accounting for Nonstationarity and Heavy Tails" by Ying Chen and Vladimir Spokoiny, January 2007.
003 "Explaining Asset Prices with External Habits and Wage Rigidities in a DSGE Model." by Harald Uhlig, January 2007.
004 "Volatility and Causality in Asia Pacific Financial Markets" by Enzo Weber, January 2007.
005 "Quantile Sieve Estimates For Time Series" by Jürgen Franke, JeanPierre Stockis and Joseph Tadjuidje, February 2007.
006 "Real Origins of the Great Depression: Monopolistic Competition, Union Power, and the American Business Cycle in the 1920s" by Monique Ebell and Albrecht Ritschl, February 2007.
007 "Rules, Discretion or Reputation? Monetary Policies and the Efficiency of Financial Markets in Germany, 14th to 16th Centuries" by Oliver Volckart, February 2007.
008 "Sectoral Transformation, Turbulence, and Labour Market Dynamics in Germany" by Ronald Bachmann and Michael C. Burda, February 2007.
009 "Union Wage Compression in a Right-to-Manage Model" by Thorsten Vogel, February 2007.
010 "On $\sigma$-additive robust representation of convex risk measures for unbounded financial positions in the presence of uncertainty about the market model" by Volker Krätschmer, March 2007.
011 "Media Coverage and Macroeconomic Information Processing" by Alexandra Niessen, March 2007.
012 "Are Correlations Constant Over Time? Application of the CC-TRIG-test to Return Series from Different Asset Classes." by Matthias Fischer, March 2007.
013 "Uncertain Paternity, Mating Market Failure, and the Institution of Marriage" by Dirk Bethmann and Michael Kvasnicka, March 2007.
014 "What Happened to the Transatlantic Capital Market Relations?" by Enzo Weber, March 2007.
015 "Who Leads Financial Markets?" by Enzo Weber, April 2007.
016 "Fiscal Policy Rules in Practice" by Andreas Thams, April 2007.
017 "Empirical Pricing Kernels and Investor Preferences" by Kai Detlefsen, Wolfgang Härdle and Rouslan Moro, April 2007.
018 "Simultaneous Causality in International Trade" by Enzo Weber, April 2007.

019 "Regional and Outward Economic Integration in South-East Asia" by Enzo Weber, April 2007.
020 "Computational Statistics and Data Visualization" by Antony Unwin, Chun-houh Chen and Wolfgang Härdle, April 2007.
021 "Ideology Without Ideologists" by Lydia Mechtenberg, April 2007.
022 "A Generalized ARFIMA Process with Markov-Switching Fractional Differencing Parameter" by Wen-Jen Tsay and Wolfgang Härdle, April 2007.

## SFB 649, Spandauer Straße 1, D-10178 Berlin http:/ / sfb649.wiwi.hu-berlin.de

023 "Time Series Modelling with Semiparametric Factor Dynamics" by Szymon Borak, Wolfgang Härdle, Enno Mammen and Byeong U. Park, April 2007.
024 "From Animal Baits to Investors' Preference: Estimating and Demixing of the Weight Function in Semiparametric Models for Biased Samples" by Ya'acov Ritov and Wolfgang Härdle, May 2007.
025 "Statistics of Risk Aversion" by Enzo Giacomini and Wolfgang Härdle, May 2007
026 "Robust Optimal Control for a Consumption-Investment Problem" by Alexander Schied, May 2007.
027 "Long Memory Persistence in the Factor of Implied Volatility Dynamics" by Wolfgang Härdle and Julius Mungo, May 2007.
028 "Macroeconomic Policy in a Heterogeneous Monetary Union" by Oliver Grimm and Stefan Ried, May 2007.
029 "Comparison of Panel Cointegration Tests" by Deniz Dilan Karaman Örsal, May 2007.
030 "Robust Maximization of Consumption with Logarithmic Utility" by Daniel Hernández-Hernández and Alexander Schied, May 2007.
031 "Using Wiki to Build an E-learning System in Statistics in Arabic Language" by Taleb Ahmad, Wolfgang Härdle and Sigbert Klinke, May 2007.

032 "Visualization of Competitive Market Structure by Means of Choice Data" by Werner Kunz, May 2007.
033 "Does International Outsourcing Depress Union Wages? by Sebastian Braun and Juliane Scheffel, May 2007.
034 "A Note on the Effect of Outsourcing on Union Wages" by Sebastian Braun and Juliane Scheffel, May 2007.
035 "Estimating Probabilities of Default With Support Vector Machines" by Wolfgang Härdle, Rouslan Moro and Dorothea Schäfer, June 2007.
036 "Yxilon - A Client/Server Based Statistical Environment" by Wolfgang Härdle, Sigbert Klinke and Uwe Ziegenhagen, June 2007.
037 "Calibrating CAT Bonds for Mexican Earthquakes" by Wolfgang Härdle and Brenda López Cabrera, June 2007.
038 "Economic Integration and the Foreign Exchange" by Enzo Weber, June 2007.

039 "Tracking Down the Business Cycle: A Dynamic Factor Model For Germany 1820-1913" by Samad Sarferaz and Martin Uebele, June 2007.
040 "Optimal Policy Under Model Uncertainty: A Structural-Bayesian Estimation Approach" by Alexander Kriwoluzky and Christian Stoltenberg, July 2007.
041 "QuantNet - A Database-Driven Online Repository of Scientific Information" by Anton Andriyashin and Wolfgang Härdle, July 2007.
042 "Exchange Rate Uncertainty and Trade Growth - A Comparison of Linear and Nonlinear (Forecasting) Models" by Helmut Herwartz and Henning Weber, July 2007.
043 "How do Rating Agencies Score in Predicting Firm Performance" by Gunter Löffler and Peter N. Posch, August 2007.

## SFB 649, Spandauer Straße 1, D-10178 Berlin http:/ / sfb649.wiwi.hu-berlin.de

044 "Ein Vergleich des binären Logit-Modells mit künstlichen neuronalen Netzen zur Insolvenzprognose anhand relativer Bilanzkennzahlen" by Ronald Franken, August 2007.
045 "Promotion Tournaments and Individual Performance Pay" by Anja Schöttner and Veikko Thiele, August 2007.
046 "Estimation with the Nested Logit Model: Specifications and Software Particularities" by Nadja Silberhorn, Yasemin Boztuğ and Lutz Hildebrandt, August 2007.
047 "Risiken infolge von Technologie-Outsourcing?" by Michael Stephan, August 2007.
048 "Sensitivities for Bermudan Options by Regression Methods" by Denis Belomestny, Grigori Milstein and John Schoenmakers, August 2007.
049 "Occupational Choice and the Spirit of Capitalism" by Matthias Doepke and Fabrizio Zilibotti, August 2007.
050 "On the Utility of E-Learning in Statistics" by Wolfgang Härdle, Sigbert Klinke and Uwe Ziegenhagen, August 2007.
051 "Mergers \& Acquisitions and Innovation Performance in the Telecommunications Equipment Industry" by Tseveen Gantumur and Andreas Stephan, August 2007.
052 "Capturing Common Components in High-Frequency Financial Time Series: A Multivariate Stochastic Multiplicative Error Model" by Nikolaus Hautsch, September 2007.
053 "World War II, Missing Men, and Out-of-wedlock Childbearing" by Michael Kvasnicka and Dirk Bethmann, September 2007.
054 "The Drivers and Implications of Business Divestiture - An Application and Extension of Prior Findings" by Carolin Decker, September 2007.
055 "Why Managers Hold Shares of Their Firms: An Empirical Analysis" by Ulf von Lilienfeld-Toal and Stefan Ruenzi, September 2007.
056 "Auswirkungen der IFRS-Umstellung auf die Risikoprämie von Unternehmensanleihen - Eine empirische Studie für Deutschland, Österreich und die Schweiz" by Kerstin Kiefer and Philipp Schorn, September 2007.
057 "Conditional Complexity of Compression for Authorship Attribution" by Mikhail B. Malyutov, Chammi I. Wickramasinghe and Sufeng Li, September 2007.
058 "Total Work, Gender and Social Norms" by Michael Burda, Daniel S. Hamermesh and Philippe Weil, September 2007.
059 "Long-Term Orientation in Family and Non-Family Firms: a Bayesian Analysis" by Jörn Hendrich Block and Andreas Thams, October 2007.
060 "Kombinierte Liquiditäts- und Solvenzkennzahlen und ein darauf basierendes Insolvenzprognosemodell für deutsche GmbHs " by Volodymyr Perederiy, October 2007.
061 "Embedding R in the Mediawiki" by Sigbert Klinke and Olga ZlatkinTroitschanskaia, October 2007.
062 "Das Hybride Wahlmodell und seine Anwendung im Marketing" by Till Dannewald, Henning Kreis and Nadja Silberhorn, November 2007.
063 "Determinants of the Acquisition of Smaller Firms by Larger Incumbents in High-Tech Industries: Are they related to Innovation and Technology Sourcing? " by Marcus Wagner, November 2007.

## SFB 649, Spandauer Straße 1, D-10178 Berlin http:/ / sfb649.wiwi.hu-berlin.de

064 "Correlation vs. Causality in Stock Market Comovement" by Enzo Weber, October 2007.
065 "Integrating latent variables in discrete choice models - How higherorder values and attitudes determine consumer choice" by Dirk Temme, Marcel Paulssen and Till Dannewald, December 2007.
066 "Modelling Financial High Frequency Data Using Point Processes" by Luc Bauwens and Nikolaus Hautsch, November 2007.
067 "A stochastic volatility Libor model and its robust calibration" by Denis Belomestny, Stanley Matthew and John Schoenmakers, December 2007
068 "Why Votes Have a Value" by Ingolf Dittmann, Dorothea Kübler, Ernst Maug and Lydia Mechtenberg, December 2007.


[^0]:    * We are grateful to Dana Novotny and Jana Stöver for research assistance. The paper has benefited from discussions with seminar audiences in Berlin, Helsinki, Frankfurt/Main, and Munich. This project was funded by the Rudolf von Bennigsen-Foerder foundation and by the Deutsche Forschungsgemeinschaft through the collaborative research center 649 "Economic Risk" at Humboldt University, Berlin, and through the collaborative research center 504 "Rationality concepts, decision behavior, and economic modeling" at the University of Mannheim.
    ${ }^{\text {a }}$ Erasmus University Rotterdam, P.O. Box 1738, 3000 DR, Rotterdam, The Netherlands. E-mail: dittmann@few.eur.nl. Tel.: +31 104081283.
    b Technical University of Berlin, Faculty of Economics and Management, Straße des 17. Juni 135, 10623 Berlin. E-mail: d.kuebler@ww.tu-berlin.de, Tel.: +49 3031425263.
    c University of Mannheim, Department of Business Administration, 68131 Mannheim, Germany. E-mail: maug@bwl.uni-mannheim.de. Tel: +49621 1811952.
    d Technical University of Berlin, Faculty of Economics and Management, Straße des 17. Juni 135, 10623 Berlin. E-mail: l.mechtenberg@ww.tu-berlin.de, Tel.: +49 3031429760.

[^1]:    1 See Palfrey and Rosenthal $(1983,1985)$ for a non-cooperative analysis of voting and Myerson (1998) for a critique of this approach.
    2 To the best of our knowledge the earliest reference to this argument is Fiorina (1976). However, Fiorina credits Butler and Stokes (1969) with this distinction and refers to the "older tradition" in political science (i.e., the tradition preceding Downs, 1957) as supporting a non-instrumental view of voting. Clearly, even the canonical model of Riker and Ordeshook (1968) bases the choice among candidates on rational choice, whereas the motivation to participate in the election is also motivated by appealing to a "civic duty," which already introduces a non-instrumental aspect into rational choice theory.

[^2]:    3 Only one study attempts to evaluate the right to vote in an experiment. Güth and Weck-Hannemann (1997) try to elicit the value of the voting right in a field experiment in the context of a political election. See Schram (1997) for a comment that highlights the severe difficulties of this methodology.

[^3]:    4 A number of experimental studies have investigated behavioral aspects of voting in the political sphere. Schram and Sonnemans (1996a, 1996b), Battaglini, Morton and Palfrey (2006), Levine and Palfrey (2007),

[^4]:    Duffy and Tavits (2007) test various predictions of the pivotal voter model. Empirical evidence on this model based on surveys can be found in Blais et al. (2000).
    5 Note that depriving somebody of his political voting right is seen as a serious punishment that is only handed out to the worst criminals. On the other hand, not having the right to vote at an annual general meeting is unlikely to be seen as "shameful."

[^5]:    ${ }^{6}$ See Baker, Ruback, and Wurgler (2006) for a survey of behavioral corporate finance.

[^6]:    7 We impose this restriction for several reasons. At the bidding stage, this assumption greatly simplifies the potential bids of the investors, and (together with a sufficiently high budget) makes sure that investors always have enough resources to bid for all shares they want. At the voting stage, this restriction makes sure that there are always $M$ voters, so that it is not possible to buy a majority of votes. Barclay and Holderness (1989) and Dyck and Zingales (2004) show that blocks of voting shares that confer effective control of a firm trade at substantially higher prices than individual shares in the market. This effect is precluded by our assumptions.

[^7]:    8 In order to see this note that in any completely mixed strategy profile there is a positive probability for each A-shareholder to be pivotal. But then the expected second period dividend is strictly higher when the

[^8]:    manager is replaced compared to when she is kept (given that $D_{1}=L$ and $p>1 / 2$ ) and voting to replace her is then a strictly dominant strategy for each shareholder.
    9 See Guarnaschelli, McKelvey, and Palfrey (2000) for an application of the QRE to a voting game.

[^9]:    10 A complete analysis of all the pure-strategy equilibria of the auction game is available from the authors upon request.

[^10]:    ${ }^{11}$ Here, we refer only to the general definition of expressive voting by Brennan and Hamlin (1998) and Brennan and Lomasky (1993). Their so-called low-cost theory of expressive voting where voters tend to vote more expressively, the more they identify with the issue that is voted on and the less they think their vote matters, is not applicable to our setup. For an experimental test of the low-cost theory of expressive voting see Tyran (2004).
    ${ }^{12}$ See Harsanyi (1980) and Feddersen and Sandroni (2006), as well as Coate and Conlin (2004) for an empirical test.

[^11]:    13 For each treatment, we had two sub-treatments that only differ in the way the results of the vote were announced. In the limited information sub-treatment, only the decision whether or not the manager had been dismissed was announced. In the full information sub-treatment the computer program also announced the number of votes for and against dismissing the manager. For each of the four treatments, we ran five experiments with limited information and five experiments with full information. The premium in offers and prices was higher for the full information sub-treatment, but the difference between the sub-treatments was never statistically significant.

[^12]:    14 We calculate for each session the error probability $\tau_{0}$ and then apply a two-sample Wilcoxon signed rank test to these error probabilities. The results of this test are not shown in the tables.

[^13]:    19 The data for the German ex post voting premium are based on our own research. We are also indebted to Philipp Pohlmann for valuable information on some differential takeover bids in Germany. It turns out that there have been only seven differential takeover bids in post-war Germany, four of which took place after 1998. In all except one case, the differential bid has been justified by the price difference at which the two types of shares traded in the market. Hence, the price difference seemed to determine the differential bid rather than the other way round.
    ${ }^{20}$ See Lease, McConnell and Mikkelson (1983), Hauser and Lauterbach (2004), Kunz (2002), Bigelli (2004), and Dittmann and Ulbricht (2008) for an empirical analysis of the terms of conversion in, respectively, U.S., Israeli, Swiss, Italian, and German dual class stock unifications.

